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Rapid Solution of Large-scale Systems Of Equations

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The analysis and design of complex aerospace structures requires the rapid solution of large systems of linear and nonlinear equations, eigenvalue extraction for buckling, vibration and flutter modes, structural optimization and design sensitivity calculation. Computers with multiple processors and vector capabilities can offer substantial computational advantages over traditional scalar computers for these analyses. These computers fall into two categories: shared-memory computers (e.g., Cray C-90) and distributed-memory computers (e.g., Intel Paragon, IBM SP-2).

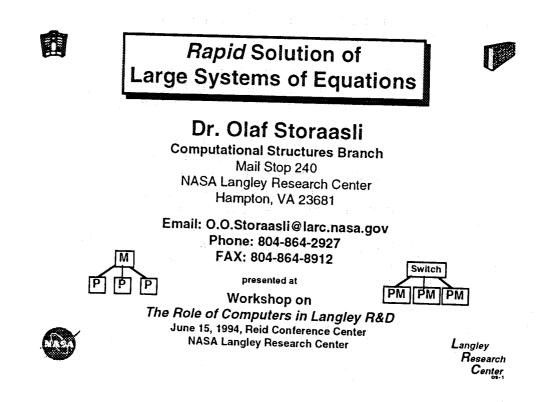
Shared-memory computers have only a few processors (16 on a Cray C-90), which rapidly process vector instructions (simultaneous adds and multiplies) and address a large memory. Information is shared among processors by referencing a common variable in shared-memory.

Distributed-memory computers may have thousands of processors, each with limited memory. Explicit message passing commands (i.e. send, receive), are used to communicate information between processors. Such communication is time consuming, so algorithms need to be designed to run efficiently on distributed-memory computers.

This presentation will cover general-purpose, highly-efficient algorithms for: generation/assembly of element matrices, solution of systems of linear and nonlinear equations, eigenvalue and design sensitivity analysis and optimization. All algorithms are coded in FORTRAN for shared-memory computers, and many adapted to distributed-memory computers. The capability and numerical performance of these algorithms will be addressed.

O. Storaasli, D. Nguyen, M. Baddourah and J. Qin (1993), "Computational Mechanics Analysis Tools for Parallel-Vector Supercomputers", AIAA/ASME/ ASCE/AHS/ASC 34th Structures, Structural Dynamics and Materials Conference Proceedings, Part 2, pp. 772-778 (Int. J. of Computing Systems in Engineering, Vol 4, No. 2-4, 1993) Dr. Olaf Oliver Storaasli is a senior research scientist in computational mechanics at the NASA Langley Research Center, Hampton, Virginia. He began his career at Langley after receiving a Ph.D. degree in Engineering Mechanics from North Carolina State University in 1970.

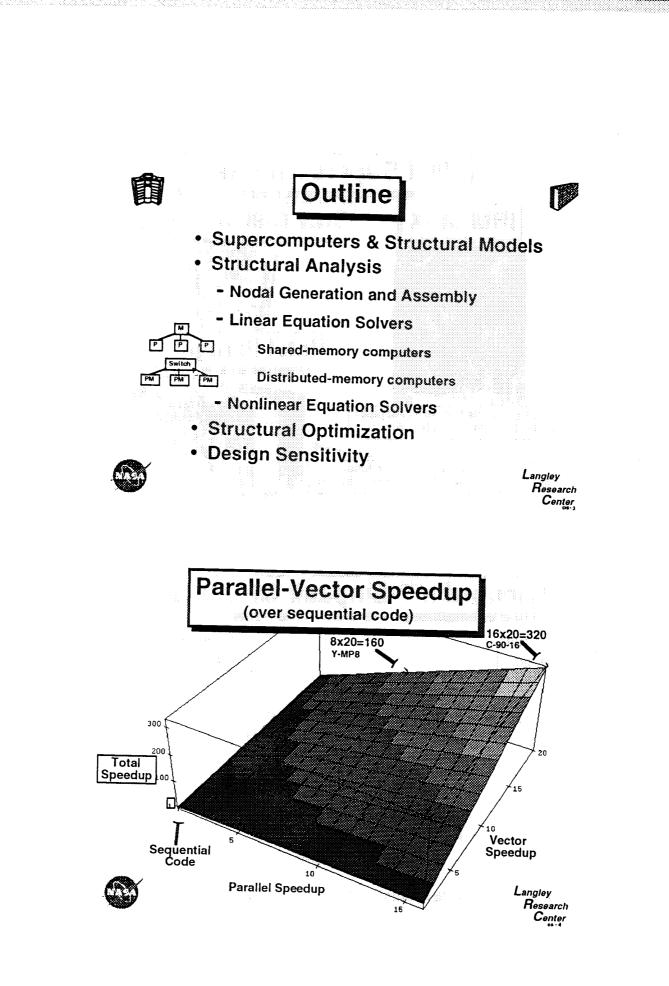
Long before parallel computers were commercially available, Dr. Storaasli led a hardware, software and applications team at NASA Langley Research Center to develop one of the first parallel computers, the Finite Element Machine. He has authored over 80 works in computational structural mechanics including static and dynamic structural analysis, eigenvalue and optimization methods, interdisciplinary analysis, data management, and parallel-vector structural analysis methods on supercomputers. He received the Floyd L. Thompson Fellowship of NASA Langley Research Center for post-doctoral research at Norges Tekniske Hogskole in Trondheim, Norway, and Det Norske Veritas, Oslo, Norway, during 1984-85 and has been invited back twice since He received 5 NASA-wide and 8 Langley Achievement awards for outstanding work in Computational Structural Mechanics. These awards included significant contributions to the NASA Viking and Integrated Programs for Aerospace-Vehicle Design (IPAD) Projects as well as to the development of Relational Information Management (RIM), since developed into the commercial relational data-base software: R:BASE. In August, 1989, Cray Research selected the general-purpose matrix equation solution software, pvsolve, developed by Dr. Storaasli and his colleagues, to receive the GigaFLOP Performance Award. pvsolve was used to solve the 54,870 equations (9.2 billion floating point operations) in the Space Shuttle Solid Rocket Booster structural analysis in six seconds elapsed time. His recent research has resulted in methods to analyze a 172,400 equation (5,737 bandwidth) refined model of a high speed civil transport and a 265,000 equation automobile (3,374 bandwidth) application in less than two minutes on the Cray C-90 and a method to generate and assemble stuctural stiffness matrices on the Intel Delta at speeds 25 times that of one Cray C-90 processor.

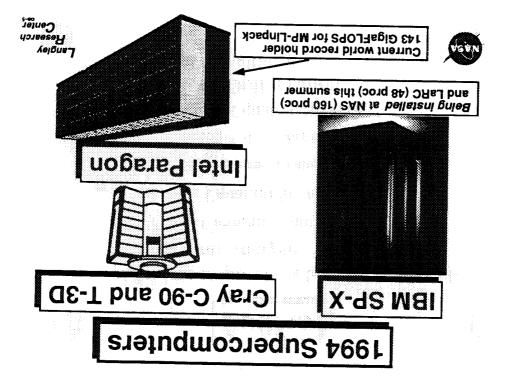


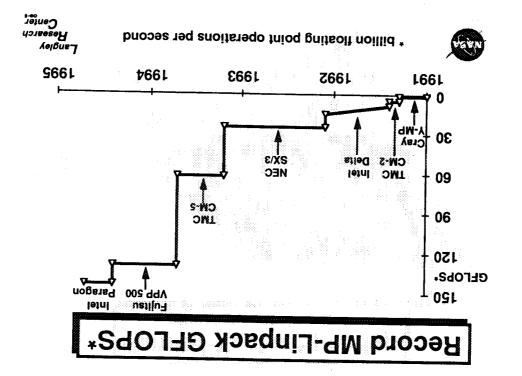


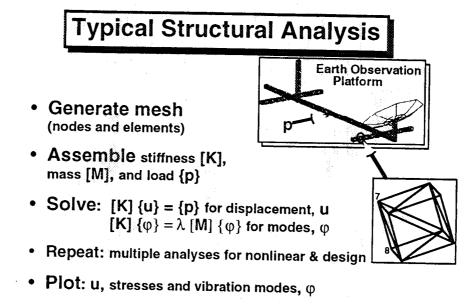
- Faster, cheaper, better analysis/design of large-scale structures
 - Develop algorithms to exploit highperformance computers
 - Evaluate computational performance





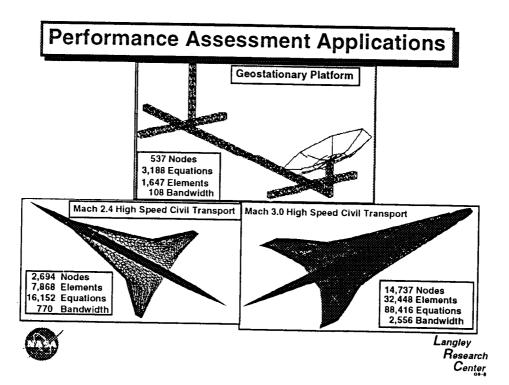


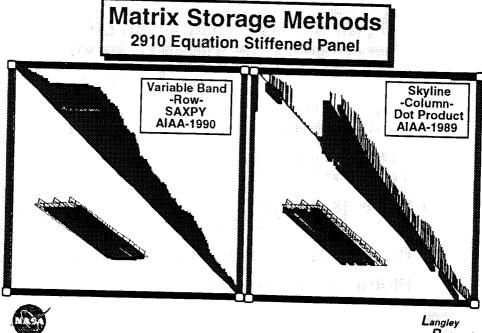










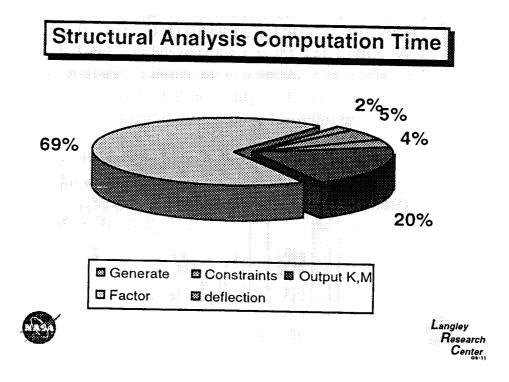


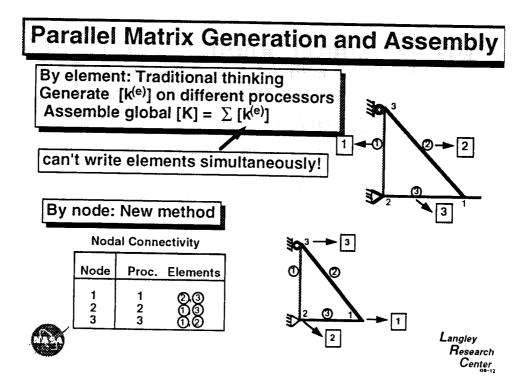
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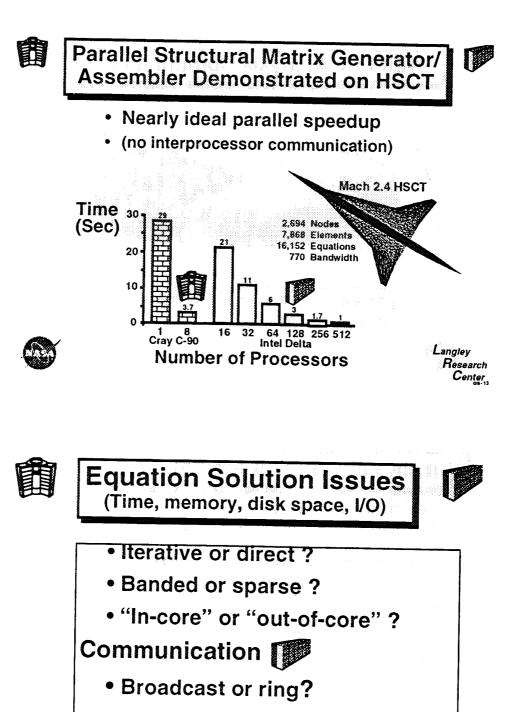
Parallel-Vector Structures Algorithms

Static	Eigenvalue	Dynamics-Control	Flutter	Optimization			
Ku = f Substructuring NL Algorithms	κφ = λΜφ Subspace Lanczos	Mü + Cu + Ku = f(t) Time Integration Reduced-Order Simulate Multibody	KΦ= λΜΦ Unsymmetric Choleski and Lanczos	b _{k+1} = b _k + s _k d _k Search methods Sensitivity			
Matrix Assemblers - Finite Element based - Degree-of-Freedom based							
Equation Solvers - Direct - Sparse - Iterative - SVD							









• OSF or SUNMOS?

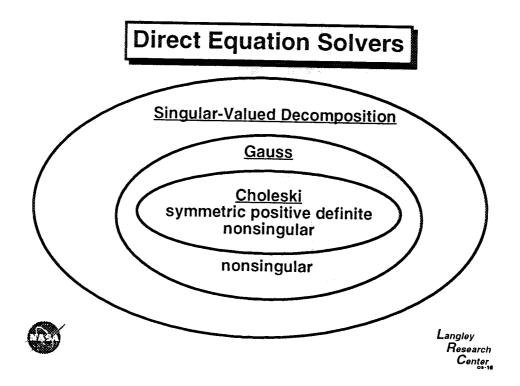
Equation Solvers

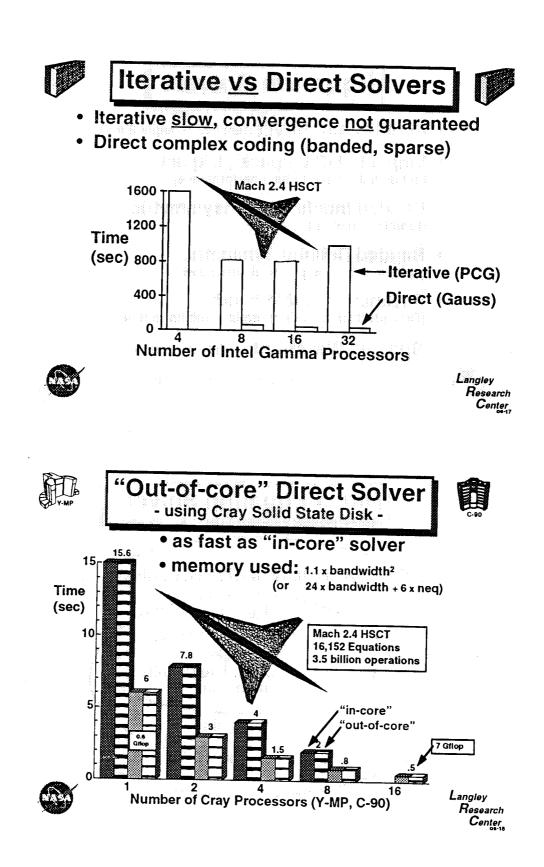
- Iterative and *Direct* (function of application)
- Linpack (MP Linpack), LApack (needs full matrix for best performance)
- Banded Indefinite, nonsymmetric (requires pivoting)
- Banded Definite Symmetric (seldom occurs in practical structures)
- Skyline*, Variable-band* (DOT-product, SAXPY operations minimize time)
- Sparse*, Wavefront* (<5% nonzeros)

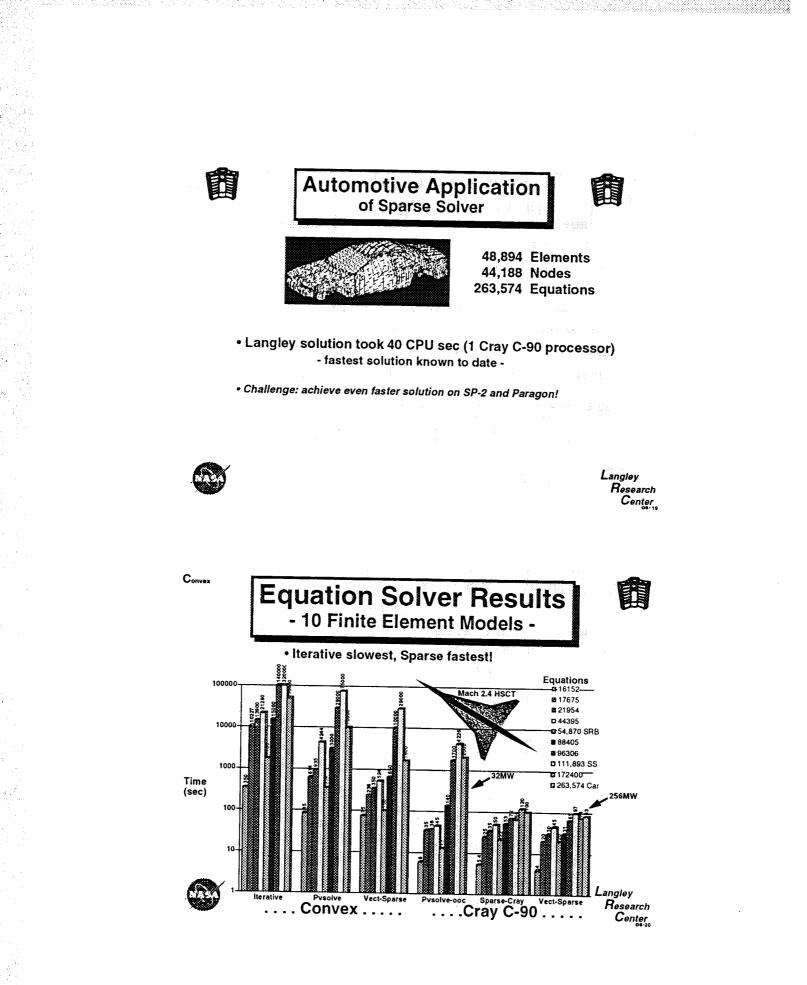


* node or equation reordering minimizes solution time











Industrial-Strength Equation Solvers for [A]{x}={b} and [A]{x}= λ [M]{x}



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<u>Solver</u>	Appl	ication	Memory	Parallel(shared)	Parallel(Distributed)
PVSOLVE	Symme	tric + Def*	equations X Bandwidth	Yes (Cray C-90, etc)	Yes (Intel Paragon, IBM SP-1)
PVSOLVE-000		••.	1.1 x Bandwidth ²	Yes (Cray C-90, etc)	Not yet
PVSOLVE-000	C+	"	24 x Bandwidth	No (Cray C-90, etc)	Not yet
VSS (Vector Sp	oarse)		function of sparsity	No (Cray C-90, etc)	Not yet
PCG(Iterative)		*	~ matrix nonzeros	Yes (Cray C-90, etc)	Yes (Intel Paragon, IBM SP-1)
LANZ(Eigensol	ver)	4	equations X bandwidth	Yes (Cray C-90, etc)	Yes (Intel Paragon)

NOTE: These solvers have been evaluated on real applications with up to <u>263.574 equations</u> and larger matrices with <u>several million equations</u>. PCG is slowest, VSS is fastest (for large, sparse problems) and PVSOLVE-OOC is the best all-around parallelvector solver. PVSOLVE-OOC exploits Cray solid-state disk.



special versions of PVSOLVE for unsymmetric and negative coefficient matrices solve panel flutter, CFD, nonlinear and optimization problems

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Parallel-Vector Equation Solver (PVSOLVE)



Shared Memory Cray GigaFLOP award

- "in-core skyline and variable-band versions
- "Out-of-core" versions: memory ~ 1.2 bandwidth² and 24 x bandwidth
- tuned for Crays (or shared memory computer/workstation)

Distributed Memory

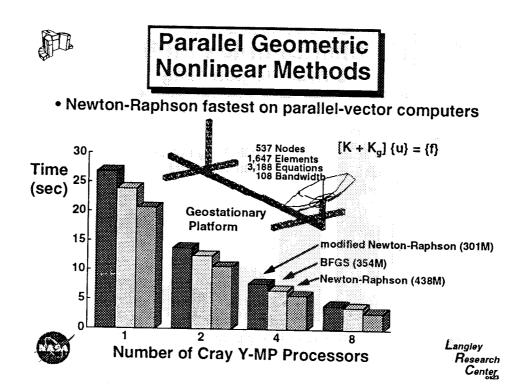
- "in-core" skyline Intel i/860 or Paragon
- "in-core" row version Intel 860 or Paragon, IBM SP-1

Conversion underway to TMC CM-5, Convex SSP-1 and Cray T-3D



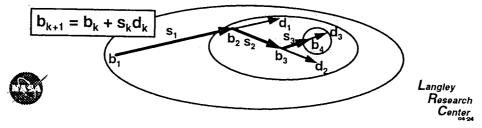
COMET, Ford, U. Virginia, IBM, Princeton, LLNL, NSF sites Langley Convex, COMCO, NASA Lewis + several dozen sites Research

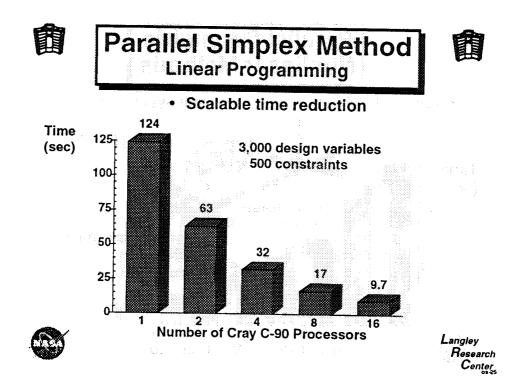
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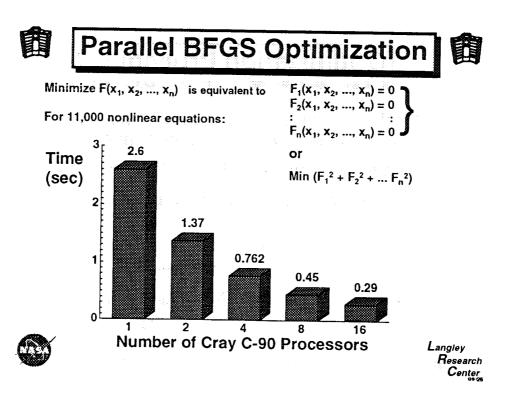


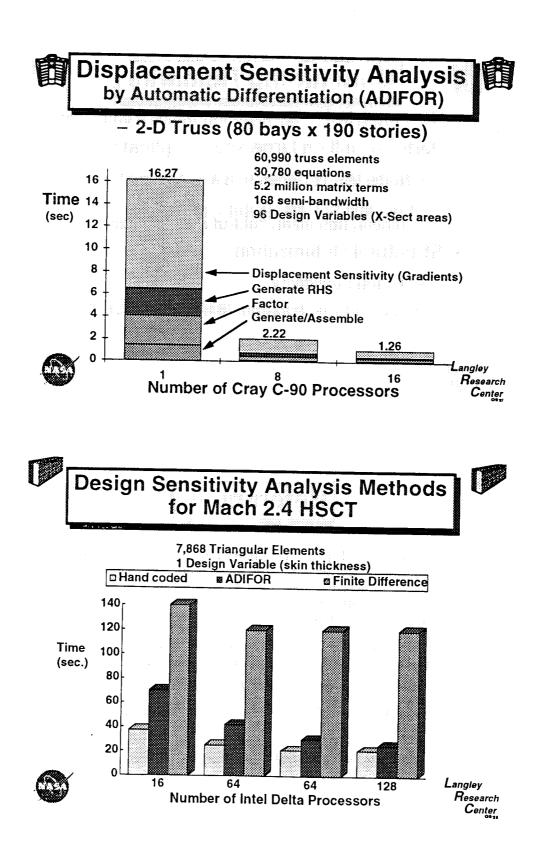
Optimization Procedure

- Find aircraft minimum weight subject to displacement and stress constraints
- Nonlinear constrained optimization finds:
 - Direction: BFGS, Simplex-Linear Programming
 - Step size: Golden Block









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Concluding Remarks



- New algorithms for high-performance computers
- Perform well on large-scale applications:
 - Nodal Matrix Generation and Assembly
 - Equation Solvers: [K]{u} = {p} (linear, nonlinear, "out-of core",sparse)
- Structural Optimization
 - Design Sensitivity
- Operate on Cray, Paragon, IBM SP-1 and SP-2!



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References

- Storaasli, O., Nguyen, D., Baddourah, M. and Qin, J.; Computational Mechanics Analysis Tools for Parallel-Vector Supercomputers", *AIAA/ASME/ASCE/AHS/ASC* 34th Structures, Structural Dynamics and Materials Conference Proceedings, Part 2, pp. 772-778, April 1993.
- also International Journal of Computing Systems in Engineering, Vol. 4, No. 2-4, 1993 pp. 349-354
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