

EXPERIENCES WITH TWO-EQUATION TURBULENCE MODELS

Ashok K. Singhal, Yong G. Lai, and Ram K. Avva
CFD Research Corporation
Huntsville, Alabama

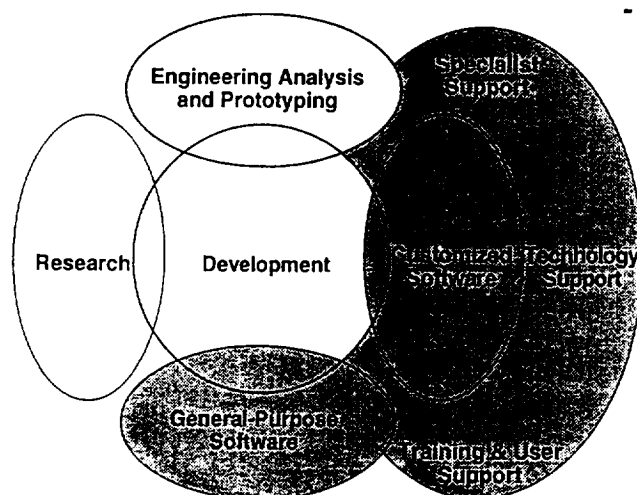
N95-27894

OUTLINE

- Introduction to CFDRC
- Experiences with 2-Equation Models
 - Models Used
 - Numerical Difficulties
 - Validation and Applications
 - Strengths & Weaknesses
- Answers to Three Questions (Posed by Workshop Organizing Committee)
 1. What Are Your Customers Telling You?
 2. What Are You Doing In-House?
 3. How Can NASA-CMOTT Help?

INTRODUCTION TO CFDRC

- Young and Energetic (Turbulent) Organization, Dedicated to the Continuous Process of Advancement and Effective Transfer of CFD Technology
- TWO TYPES OF COMPLEMENTARY ACTIVITIES:
 - PROJECTS
 - SOFTWARE



INTRODUCTION TO CFDRC (Continued)

- **Objective User of Turbulence Models (0, 1, and 2 Equation Models, RSM and LES)**
- **Humble Developer, e.g. Monte Carlo Joint Scalar PDF**
- **Active Participant in Recent Small Eddies of Turbulence, e.g.**
 - **Stanford Endeavor: "Collaborative Testing of Turbulence Models" 1989-1993**
 - **National Workshops at: NASA MSFC, LeRC/CMOTT, etc. 1987-1994**
 - **ASME/Fluids Engineering Division, Biathlon, Lake Tahoe, June 1994**

TWO-EQUATION MODELS USED

- **Standard k- ϵ Model (Launder & Spalding, 1974)**
- **Low-Re k- ϵ Model (Chien, 1982)**
- **Extended k- ϵ Model (Chen & Kim, 1987)**
- **Multiscale k- ϵ Model (Kim & Chen, 1988)**
- **RNG-Based k- ϵ Model (Yakhot et. al. 1993)**
- **2-Layer k- ϵ Model (Rodi, 1991)**
- **k- $\tilde{\epsilon}^{++}$ Models**
- **k- ω Model (Wilcox, 1991)**

++ Models with Corrections for: Curvature, Rotation, Buoyancy, Compressibility, etc.

NUMERICAL DIFFICULTIES

- **Positivity of k & ε (or ω) Is Not Guaranteed in Iterative Algorithms**
- **Strong Nonlinearity of Source Terms and Coupling Causes Numerical Difficulties**
- **Inappropriate Specifications of ε (or ω) at Boundaries or in Initial Conditions May Also Cause Divergence**
- **Non-orthogonality of Grids Adds to Difficulties**
- **Non-smooth Change Over for Two-Layer Model Hinders Convergence**

VALIDATIONS PERFORMED

- **Channel and Pipe Flows**
- **Backward-Facing Step**
- **Turnaround Duct**
- **Swirl-Flow Combustor**
- **Rotating Disk Cavities**
- **Boundary Layers**
- **Jets, Wakes, and Mixing Layers**
- **Periodic Wakes Behind Bluff Bodies**

Examples of Successes and Failures

1) Flow Around a Square Cylinder; 2) 180° Square Duct; 3) S-Shaped Annular Diffuser; 4) Dump Combustor; 5) Backward Facing Step

FLOW AROUND A SQUARE CYLINDER

Strouhal Number

$$\text{Strouhal Number} = \frac{fH}{U_o}$$

f = Frequency of Vortex Shedding

H = Obstacle Height

U_o = Freestream Velocity

Model/Expt.	Time Period	Strouhal Number
Expt.	7.25	0.138
Standard k-ε	7.1	0.141
2-Layer k-ε	7.1	0.141
RNG k-ε	7.6	0.132

Notes:

1. Experiments By Durao, Heitor, and Pereira (1988)

2. Computations with CFD-ACE

Inlet: 78H Upstream; Outlet: 22H Downstream

Grid: 120 x 80

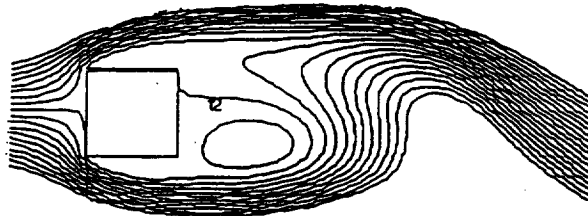
Time Steps: Over 70 Per Time Period

Ref.: Avva, R.K., Singhal, A.K., Lai, Y.G., "Numerical Simulation Of Periodic and 3-Dimensional, Turbulent Flows With CFD-ACE," ASME Fluid Dynamics Conference, Lake Tahoe, NV, June 19-23, 1994.

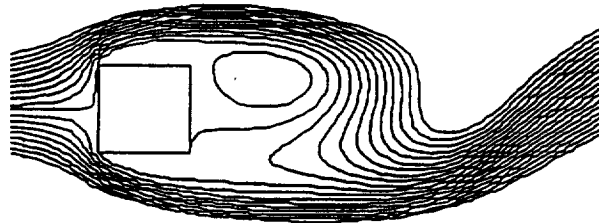
FLOW AROUND A SQUARE CYLINDER

Instantaneous Streamlines

Mid-Cycle

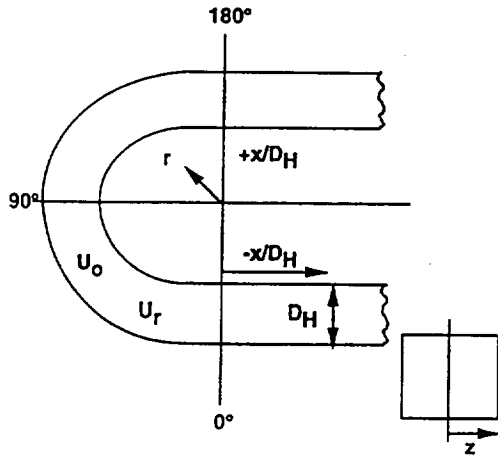


End of Cycle

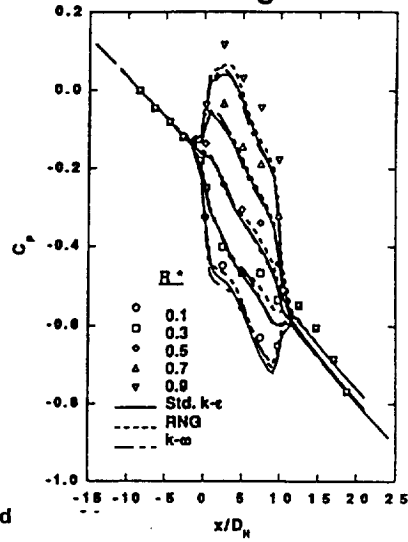


FLOW IN A 180° SQUARE DUCT

Computational Domain



Static Pressure Along Duct Walls

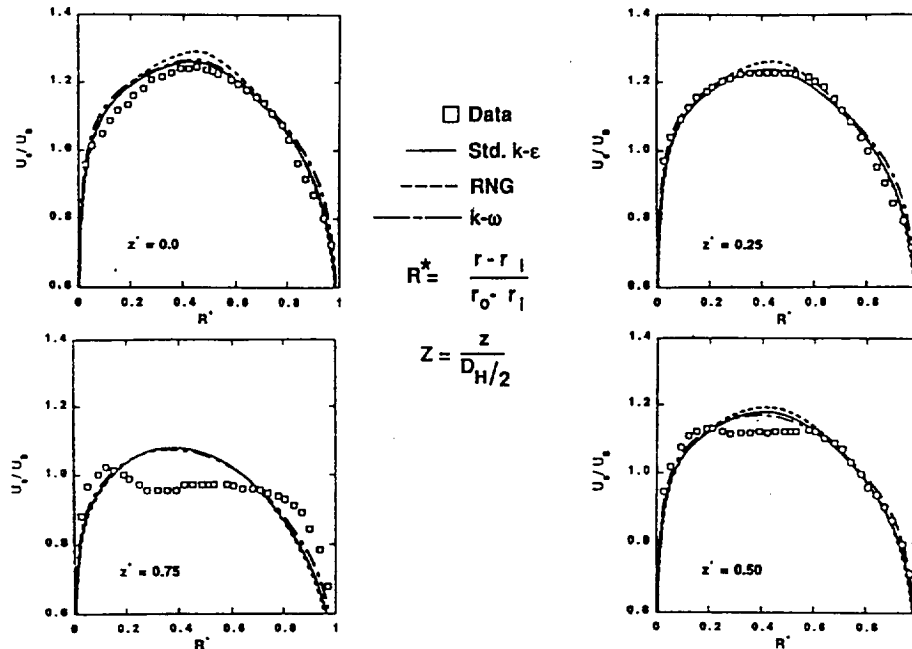


- Experiment by Chang, Humphrey and Modavi (1983)
- Computations Done with CFD-ACE on a 40x40x20 Grid

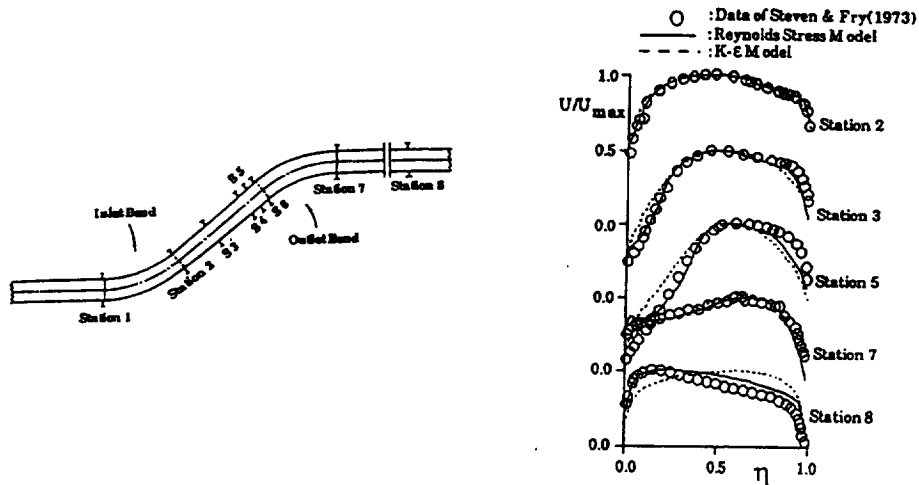
Ref.: Avva, R.K., Singhal, A.K., Lai, Y.G., "Numerical Simulation Of Periodic and 3-Dimensional, Turbulent Flows With CFD-ACE," ASME Fluid Dynamics Conference, Lake Tahoe, NV, June 19-23, 1994.

FLOW IN A 180° SQUARE DUCT

Mean Axial Velocity at $\theta = 3^\circ$

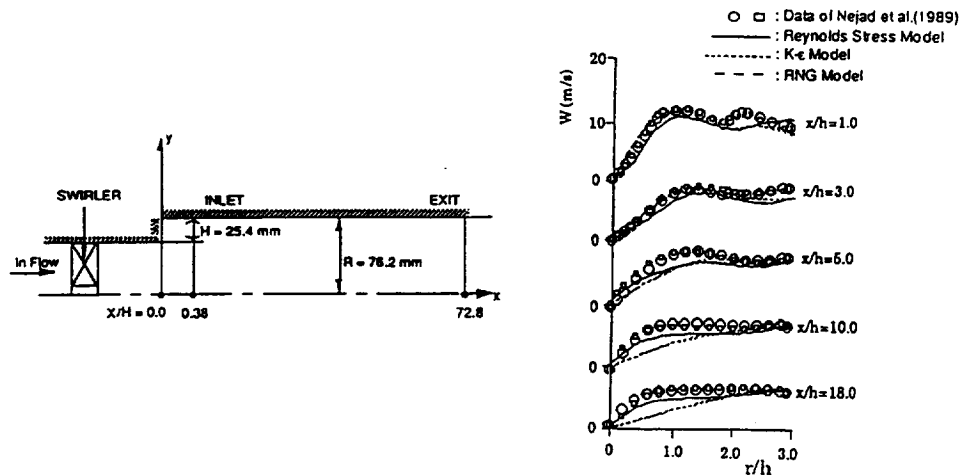


S-SHAPED ANNULAR DIFFUSER



- * k-ε Model and RNG Model Failed to Predict the Correct Location of the Maximum Velocity Downstream
- * Computations with CFD-ACE; Publication Under Preparation

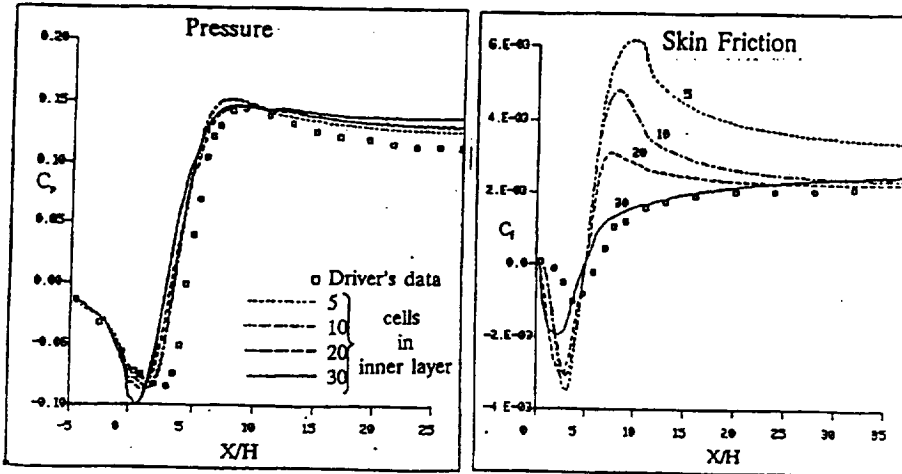
Confined Swirling Flow for a Dump Combustor



- * K-ε model failed to preserve the vortex core strength near center (see $x/h=10$ & 18)
- * Computational results to be presented at 1994 ASME Winter Annual Meeting (Chicago)

BACKWARD-FACING STEP

Sensitivity to Grid Refinement



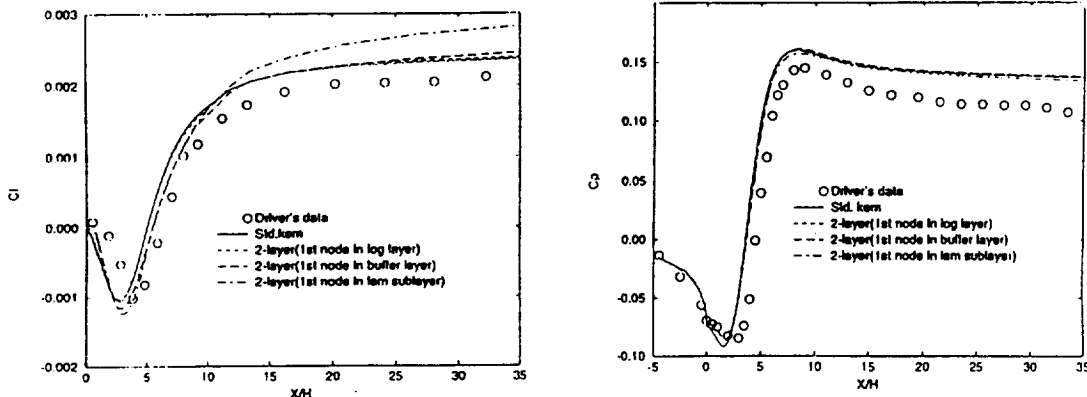
- Low-Re Model Requires >30 Nodes in the Inter Layer

Ref.: "Comparative Study of High and Low Reynolds Number Versions of k- ϵ Models," R.K. Avva, C.E. Smith, A.K. Singhal, AIAA-90-0246.

BACKWARD FACING STEP

2-Layer Model;

80 x 60 Grid; Central Differencing



Computations with CFD-ACE; To Be Published

EXAMPLE APPLICATIONS

- Gas Turbine Combustors
- Liquid Rocket Engines
- Seals and Bearing Cavities
- Impellers, Inducers, and Fans
- IC Engines
- CFD Reactors
- External Aerodynamic Flows
- Plus Many More

STRENGTHS & WEAKNESSES

Strengths of 2-Equation Models

- Numerically Economical
- Easy to Modify
- Reasonable Applicability Within Engineering Accuracy

Weaknesses

- Use of Wall Functions Requires First Grid Outside the Viscous Sublayer. This is Difficult to achieve, *a Priori*
- Low-Re Approach Does Not Offer Overall Advantage.
- Two-Layer Approach Needs More Work (e.g. Smoothing)
- Reynolds Analogy Inadequate for Heat-Transfer Applications.
- Effect of Surface Roughness on Turbulence.

CMOTT/CP QUESTIONS

- 1. What Are Your Customers Telling You?**
- 2. What Are You Doing In-House?**
- 3. How Can NASA-CMOTT Help?**

WHAT ARE CUSTOMERS TELLING?

- PLEASE Don't Confuse Us,
with Additional Models and False Hopes**
- Conclusions (Confusion) Over Last 15-Years**
 - Use $k\text{-}\epsilon$ Model, with Wall Functions**
 - Wall Functions, Oh No!, Never!!
Use Low-Re $k\text{-}\epsilon$,.: Which One?, How?? (Good Questions)**
 - $k\text{-}\epsilon$ Is No Good; Neglects Non-Isotropy, etc., etc.**
 - Jump on RSM Wagon, Now!
It Can Take You Anywhere, Eventually!!**
 - Look How Great is this $k\text{-}\epsilon^{++}$
When and How to Use it? (Good Questions)**
 - Look How Accurate is this Scheme, No Numerical Diffusion.
Don't Contaminate the Solutions with Turbulence**

WHAT IS CFDRC DOING?

- **Using What is Available, in Best Possible Ways**
- **Listening to Both Sides (Model Developers and Users)**
- **Trying to Resist Peer Pressures**
- **Struggling to Find Resources for Mundane Goals Such as Developing Guidelines for Correct Use of Turbulence Models**

HOW CAN CMOTT HELP?

- **CMOTT Has Been Providing Commendable Service in the Very Difficult Subject: Turbulence**
- **"Turbulence Subprogram" Should Help Further**
- **Additional Effort is Needed in Many Areas, Such As:**
 - **Near Wall Treatment**
 - **Effect of Surface Roughness**
 - **Economical Heat Transfer Model**
 - **Documentation of Experiences in:**
 - a) **Model Robustness(In Addition to Accuracy)**
 - b) **Model Sensitivity to Grid Distribution and Boundary Conditions**
 - **Transition Model (if Possible Suitable for $k\text{-}\epsilon$ Framework)**

HOW CAN CMOTT HELP? (Continued)

- **NASA-CMOTT Is One of the Few Groups Sustaining Momentum for Turbulence Modeling.**
- **It Is In Unique (Privileged) Position for Embracing the Challenge of Developing Specific Recommendations (Guidelines) For:**
 - a) **Selection of Adequate Models for Different Class of Problems**
 - b) **Correct Use of Each Model**
- **The Task Is Difficult But Practical**
- **Select Fewer Roads, Post Milestones, and Go Further**
- **Move An Inch Closer to Users**

