

N95-32420

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Application of Impact Dampers in Vibration Control of Flexible Structures

Final Report
NASA/ASEE Summer Faculty Fellowship Program--1994
Johnson Space Center

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Date Submitted: August 5, 1994

Contract Number: NGT-44-005-803

- [28] R. L. Webber, J. B. Hazelrig, R. J. Patel, H. R Van Den Berg, and J. E. Lemmons. Evaluation of site-specific differences in trabecular bone using fractal geometry. *J. Dent. Res.*, page 70, 1991. Abstract no. 2095.
- [29] R. Heaney, "Osteoporotic Fracture Space: An Hypothesis," *Bone and Mineral*, 6(1989), 1-13.
- [30] J. Podenphant et al, "Bone mass, bone structure and vertebral fractures in osteoporotic patients," *Bone*, 1987, 8:127-130.
- [31] M. Kleerekoper et al, "Cancellous bone architecture and bone strength," *Osteoporosis 1987*, 294-300.
- [32] J.E. Aaron et al, "The microanatomy of of trabecular bone loss in normal aging men and women," *Clin Orthop Res*, 1987, 215:260-271.
- [33] J. Samarabandu, R. Acharya, E. Hausman, C. Allen, "Analysis of Bone Images using Morphological Fractals", *IEEE Trans on Medical Imaging*, 12, Sep 1993, pp466-470.

ACKNOWLEDGMENT

The writers wish to thank the staff at the of the Vibration and Acoustic Test Facility (VATF) for their valuable assistance in all phases of this investigation. Our deep appreciation is extended to the NASA and Lockheed Engineering Services Corporation employees. The amount of work completed in this ten weeks period would not have been possible without their assistance.

REFERENCES

1. Chalmers, R. and S. Semercigil, "Impact Damping the Second Mode of a Cantilever Beam," *Journal of Sound and Vibration*, Vol. 146, pp. 157-161. 1991.
2. Masri, S. F., "Forced Vibration of Class of Nonlinear Dissipative Beams," *Journal of the Engineering Mechanics Division, ASCE* Vol. 99, No. EM4, Proc. Paper 9959, pp. 669-683. August 1993.
4. D.B. Halpin, D.B., "Modal Special Studies Packet - Preliminary Tests of the Impact Damper Test Article," *Vibration and Acoustics Test Facility, NASA JSC*. June 1994.
5. *Modal Testing - Theory and Applications*. D.J. Ewins, Ed. 1983. Brüel & Kjaer Instrumentation, Inc.
6. Roy, R. K., R.D. Rocke, and J.E. Foster, "The application of Impact Dampers to Continuous Systems", *Trans. of the ASME, Journal of Engineering for Industry*, November, pp. 1317-1324. 1975.
7. Yousef, S. and F. Akl, "Forced Vibration Analysis of a Slender Stack Equipped with Sliding and Pendulum Impact Dampers," *Developments in Theoretical and Applied Mechanics*, Vol. 14, SECTAM XIV, University of Mississippi, pp. 433, April 1988.

TABLE 4.- MULTIPLE REGRESSION ANALYSIS OF THE RESULTS FOR THE FIRST MODE

Multiple Regression Y₁:DAMPING (%) 3 X variables

| | | | | |
|-----|------|------------|-----------------|-------------|
| DF: | R: | R-squared: | Adj. R-squared: | Std. Error: |
| 19 | .938 | .881 | .858 | .07 |

Analysis of Variance Table

| Source | DF: | Sum Squares: | Mean Square: | F-test: |
|------------|-----|--------------|--------------|-----------|
| REGRESSION | 3 | .581 | .194 | 39.399 |
| RESIDUAL | 16 | .079 | .005 | p = .0001 |
| TOTAL | 19 | .66 | | |

Residual Information Table

| | | | | |
|-------------------------|----|--------|--|----------|
| SS[e(i)-e(i-1)]: e ≥ 0: | | e < 0: | | DW test: |
| .147 | 11 | 9 | | 1.863 |

1

Multiple Regression Y₁:DAMPING (%) 3 X variables

Beta Coefficient Table

| Parameter: | Value: | Std. Err.: | Std. Value: | t-Value: | Probability: |
|------------|--------|------------|-------------|----------|--------------|
| INTERCEPT | .315 | | | | |
| Im(H)/FRQ | -.017 | .007 | -.337 | 2.5 | .0237 |
| MASS*MS^2 | 7.362 | .974 | .813 | 7.555 | .0001 |
| GAP (mm) | .02 | .005 | .495 | 4.277 | .0006 |

2

Multiple Regression Y₁:DAMPING (%) 3 X variables

Confidence Intervals and Partial F Table

| Parameter: | 95% Lower: | 95% Upper: | 90% Lower: | 90% Upper: | Partial F: |
|------------|------------|------------|------------|------------|------------|
| INTERCEPT | | | | | |
| Im(H)/FRQ | -.032 | -.003 | -.029 | -.005 | 6.248 |
| MASS*MS^2 | 5.296 | 9.428 | 5.66 | 9.063 | 57.072 |
| GAP (mm) | .01 | .03 | .012 | .028 | 18.289 |

3

TABLE 3.- DAMPING ESTIMATES FOR THE THIRST MODE

| Test File | Damping % | Mass (kg) | Gap (m) | Im(FRF) (m/s ₂ /N) | Freq. (Hz) | Φ_d |
|------------|-----------|-----------|---------|-------------------------------|------------|----------|
| TA_11110F3 | 0.356 | 0.017 | 0 | 188.9 | 22.12 | 1.436 |
| TB_11111F3 | 0.692 | 0.017 | 0.013 | 100.4 | 22.2 | 1.436 |
| TB_11112F3 | 0.384 | 0.017 | 0.008 | 134.66 | 22.2 | 1.436 |
| TA_11113F3 | 1.27 | 0.017 | 0.003 | 35.82 | 22.2 | 1.436 |
| TB_11121F3 | 0.693 | 0.013 | 0.013 | 99.22 | 22.16 | 1.436 |
| TB_11122F3 | 0.473 | 0.013 | 0.008 | 164.28 | 22.16 | 1.436 |
| TA_11123F3 | 1.535 | 0.013 | 0.003 | 41.54 | 22.16 | 1.436 |
| TA_11131F3 | 0.461 | 0.008 | 0.013 | 145.48 | 22.38 | 1.436 |
| TB_11132F3 | 0.638 | 0.008 | 0.008 | 86.48 | 22.38 | 1.436 |
| TA_11133F3 | 0.82 | 0.008 | 0.003 | 83.17 | 22.38 | 1.436 |
| TD_11210F3 | 0.318 | 0.017 | 0 | 101.61 | 24.32 | 0.837 |
| TD_11211F3 | 0.408 | 0.017 | 0.013 | 84.71 | 24.38 | 0.837 |
| TD_11212F3 | 0.446 | 0.017 | 0.008 | 70.64 | 24.38 | 0.837 |
| TD_11213F3 | 0.504 | 0.017 | 0.003 | 73.66 | 24.38 | 0.837 |
| TC_11221F3 | 0.357 | 0.013 | 0.013 | 95.23 | 24.38 | 0.837 |
| TD_11222F3 | 0.392 | 0.013 | 0.008 | 81.41 | 24.38 | 0.837 |
| TD_11223F3 | 1.086 | 0.013 | 0.003 | 35.35 | 24.38 | 0.837 |
| TD_11231F3 | 0.371 | 0.008 | 0.013 | 91.95 | 24.38 | 0.837 |
| TD_11232F3 | 0.341 | 0.008 | 0.008 | 98.01 | 24.38 | 0.837 |
| TD_11233F3 | 0.559 | 0.008 | 0.003 | 62.49 | 24.38 | 0.837 |

TABLE 2.- DAMPING ESTIMATES FOR THE SECOND MODE

| Test File | Damping % | Mass (kg) | Gap (m) | Im(FRF) (m/s ₂ /N) | Freq. (Hz) | Φ_d |
|------------|-----------|-----------|---------|-------------------------------|------------|----------|
| TA_11110F2 | 0.37 | 0.017 | 0 | 170.86 | 13.05 | 1.393 |
| TA_11111F2 | 0.566 | 0.017 | 0.013 | 113.2 | 13.07 | 1.393 |
| TA_11112F2 | 0.728 | 0.017 | 0.008 | 92.94 | 13.07 | 1.393 |
| TA_11113F2 | 0.62 | 0.017 | 0.003 | 99.33 | 13.07 | 1.393 |
| TA_11121F2 | 1.97 | 0.013 | 0.013 | 32.77 | 13.07 | 1.393 |
| TA_11122F2 | 1.19 | 0.013 | 0.008 | 53.49 | 13.07 | 1.393 |
| TA_11123F2 | 0.765 | 0.013 | 0.003 | 87.67 | 13.07 | 1.393 |
| TA_11131F2 | 0.593 | 0.008 | 0.013 | 112.06 | 13.19 | 1.393 |
| TA_11132F2 | 1.08 | 0.008 | 0.008 | 60.38 | 13.19 | 1.393 |
| TA_11133F2 | 0.621 | 0.008 | 0.003 | 104.19 | 13.19 | 1.393 |
| TA_11510F2 | 0.447 | 0.017 | 0 | 127.11 | 13.61 | 0.988 |
| TA_11511F2 | 0.684 | 0.017 | 0.013 | 82.82 | 13.62 | 0.988 |
| TA_11512F2 | 0.652 | 0.017 | 0.008 | 85.96 | 13.62 | 0.988 |
| TA_11513F2 | 0.828 | 0.017 | 0.003 | 70.39 | 13.62 | 0.988 |
| TA_11521F2 | 0.602 | 0.013 | 0.013 | 93.04 | 13.7 | 0.988 |
| TA_11522F2 | 0.63 | 0.013 | 0.008 | 90.05 | 13.7 | 0.988 |
| TA_11523F2 | 0.608 | 0.013 | 0.003 | 92.73 | 13.7 | 0.988 |
| TA_11531F2 | 0.592 | 0.008 | 0.013 | 94.83 | 13.67 | 0.988 |
| TA_11532F2 | 0.601 | 0.008 | 0.008 | 92.8 | 13.67 | 0.988 |
| TA_11533F2 | 0.683 | 0.008 | 0.003 | 83.09 | 13.67 | 0.988 |

TABLE 1.- DAMPING ESTIMATES FOR THE FIRST MODE

| Test File | Damping % | Mass (kg) | Gap (m) | Im(FRF) (m/s ₂ /N) | Freq. | Φ_d |
|------------|-----------|-----------|---------|-------------------------------|-------|----------|
| TN_21000 | 0.336 | 0.017 | 0 | 72.34 | 4.44 | 1.857 |
| TM_21111 | 0.976 | 0.017 | 0.013 | 25.66 | 4.44 | 1.857 |
| TM_21112 | 0.797 | 0.017 | 0.008 | 33.11 | 4.44 | 1.857 |
| TM_21113 | 0.503 | 0.017 | 0.003 | 54.83 | 4.44 | 1.857 |
| TM_21121 | 0.855 | 0.013 | 0.013 | 29.56 | 4.467 | 1.857 |
| TM_21122 | 0.59 | 0.013 | 0.008 | 49.86 | 4.467 | 1.857 |
| TN_21123 | 0.461 | 0.013 | 0.003 | 63.16 | 4.467 | 1.857 |
| TN_21131 | 0.617 | 0.008 | 0.013 | 34.68 | 4.5 | 1.857 |
| TN_21132 | 0.532 | 0.008 | 0.008 | 54.8 | 4.5 | 1.857 |
| TN_21133 | 0.391 | 0.008 | 0.003 | 70.81 | 4.5 | 1.857 |
| TA_21510F1 | 0.31 | 0.017 | 0 | 41.06 | 5.535 | 0.869 |
| TA_21511F1 | 0.482 | 0.017 | 0.013 | 30.06 | 5.54 | 0.869 |
| TA_21512F1 | 0.359 | 0.017 | 0.008 | 37.41 | 5.54 | 0.869 |
| TA_21513F1 | 0.344 | 0.017 | 0.003 | 38.29 | 5.54 | 0.869 |
| TA_21521F1 | 0.53 | 0.013 | 0.013 | 24.84 | 5.55 | 0.869 |
| TA_21522F1 | 0.456 | 0.013 | 0.008 | 30.89 | 5.55 | 0.869 |
| TA_21523F1 | 0.356 | 0.013 | 0.003 | 39.7 | 5.55 | 0.869 |
| TA_21531F1 | 0.452 | 0.008 | 0.013 | 30.23 | 5.565 | 0.869 |
| TA_21532F1 | 0.383 | 0.008 | 0.008 | 34.61 | 5.565 | 0.869 |
| TA_21533F1 | 0.311 | 0.008 | 0.003 | 43.48 | 5.565 | 0.869 |

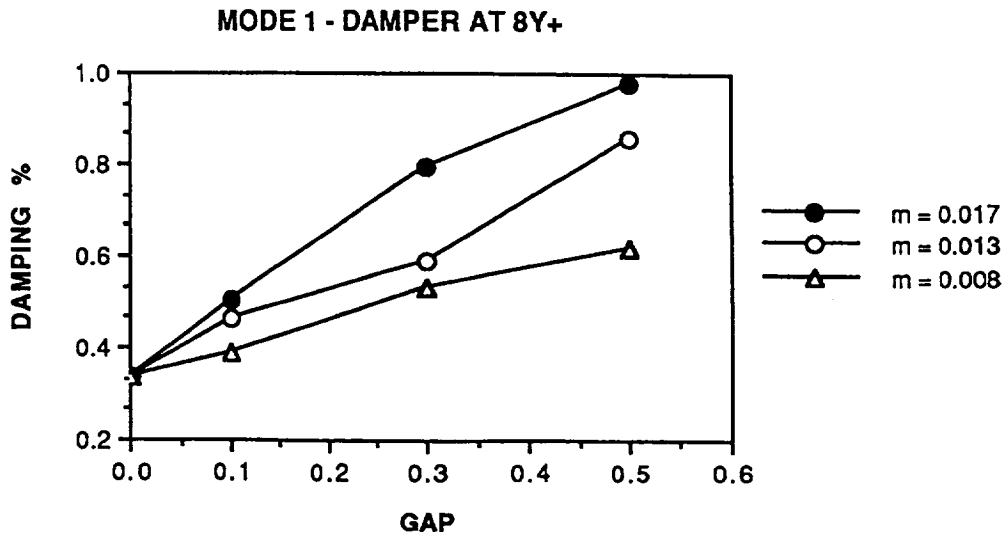
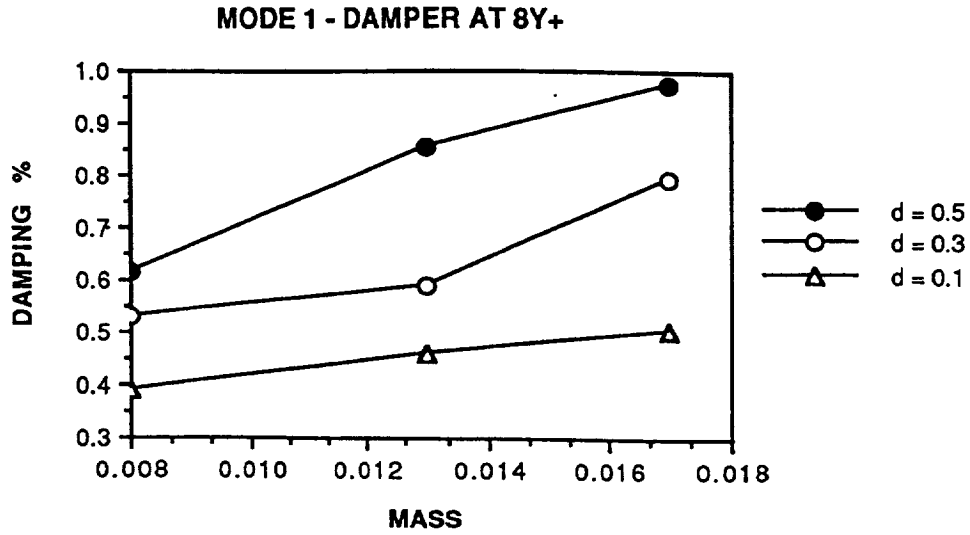


Figure 4.- Variation of Damping with Mass and Gap

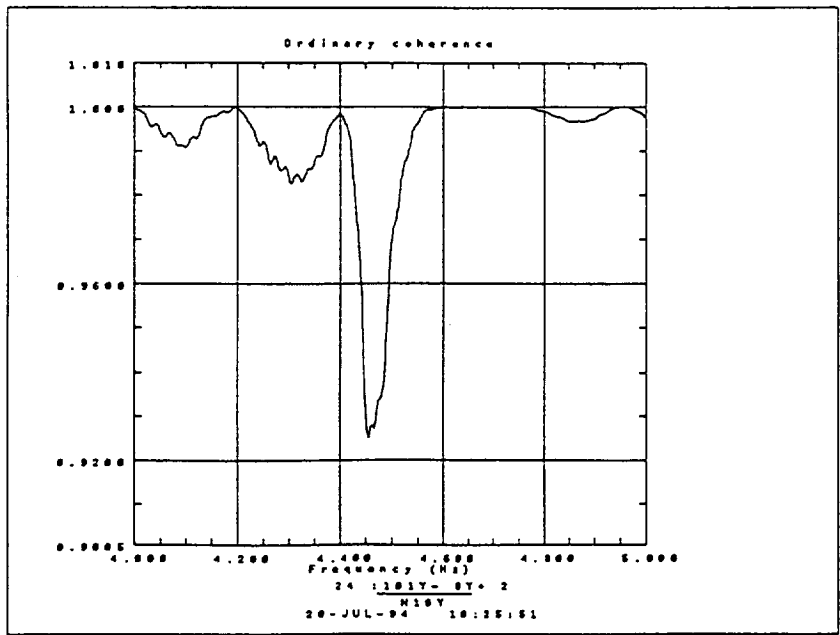
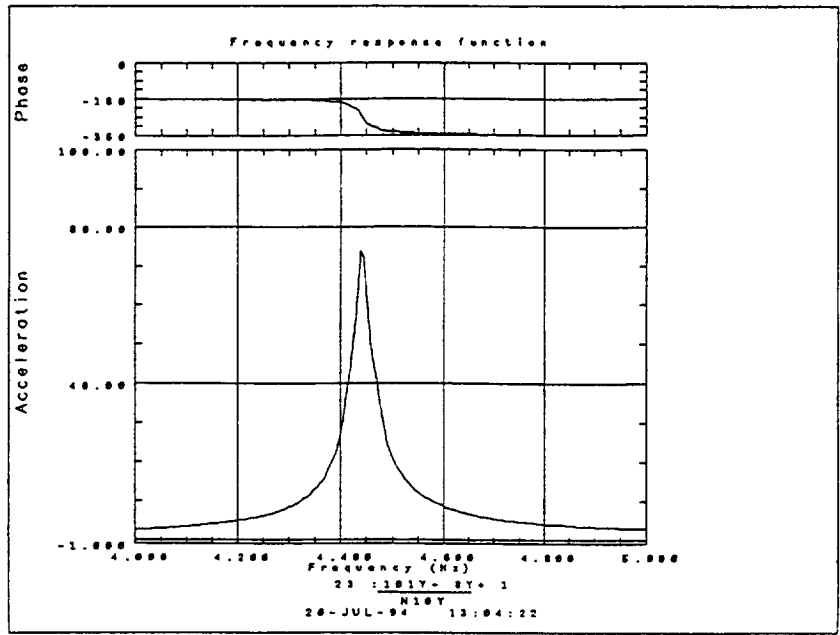
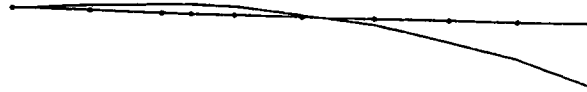
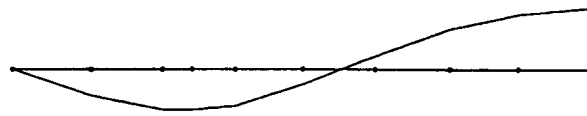


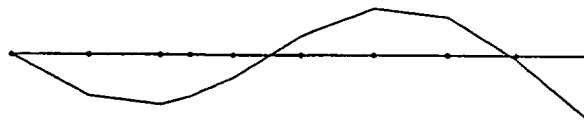
Figure 3.- Frequency Response Function and Coherence Plots for the First Mode



Mode 1 ($f_1 = 5.53$ Hz) - Spring at 81.5 in



Mode 2 ($f_2 = 13.04$ Hz) - Spring at 121.25 in



Mode 3 ($f_3 = 22.12$ Hz) - Spring at 121.25 in

Figure 2.- Modes Shapes of the Test Structure

to broaden the scope and the range of the parameters governing the behavior of flexible structures. Numerical simulation of the behavior of the problem would be needed to predict the behavior of the flexible structure under operating conditions in space.

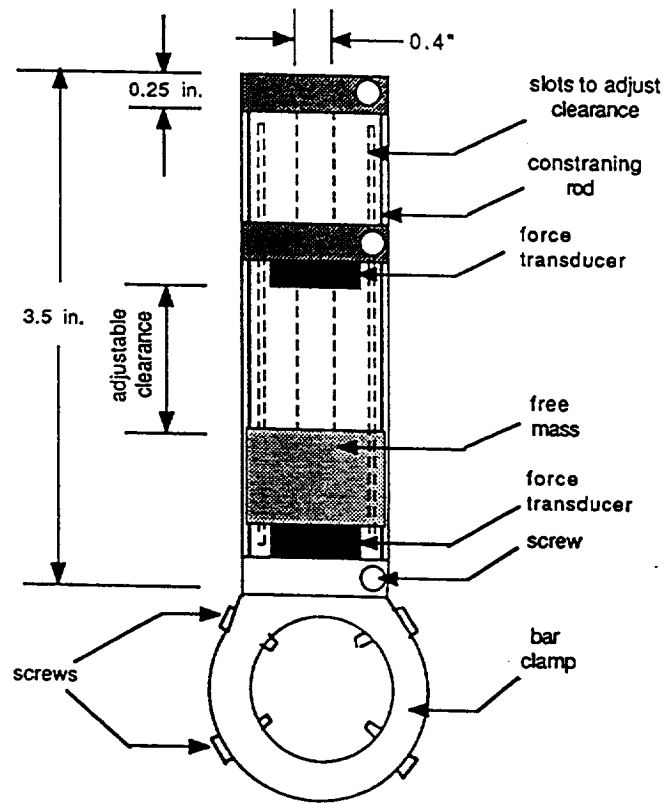


Figure 1.- Details of the Impact Damper

as follows.

$$\int_l v_i(x) dm + \int F_s dt + F_d (\Delta T) = \int_l v_f(x) dm$$

Where:

| | |
|------------------|---|
| $v_i(x), v_f(x)$ | the initial and final velocities, respectively. |
| l | the length of the test structure. |
| dm | an infinitesimal mass of the test structure. |
| F_s | the force supplied by the shaker. |
| $F_d(\Delta T)$ | the impulse exerted by the damper. |

The increase in the damping ratio of the test structure may be attributed to the presence of the third term in the L.H.S in the impulse and momentum equation above. The momentum of the beam is expected to be in the same direction before and after the impact. Therefore if the impulse is in the opposite direction to the momentum of the test article, it is then expected that the resulting momentum at the end of the half-cycle duration will be less due to the contribution of the impulse from the impact damper.

Figure 4 shows a plot of the variation of the damping ratio as a function of the moving mass of the damper and the gap. It is somewhat difficult to draw general conclusions about the behavior of the test structure from these figures.

A multiple linear regression analysis was performed using the *StatView* software. We observed, from the numerous tests we conducted, that in order for the damper to be active, it is necessary to drive the test structure at a certain level of excitation necessary to overcome friction between the damper and the guide rods on which it travels. We further hypothesize that the effectiveness of the damper depends on:

1. The velocity of the impact mass {X1 = Gap}
2. The mass multiplied by the square of the amplitude of the mode shape at the location of the damper, assuming a unit modal mass for the test structure {X2 = $m \cdot \Phi_d^2$ }, where Φ_d is the ordinate of the mode shape at the location of the damper.
3. The velocity of the test structure at the location of the damper {X3 = $\text{Im}(\text{FRF})/\text{Freq}$ }, where $\text{Im}(\text{FRF})$ is the imaginary part of the inertance frequency response function.

A multiple regression analysis based on the above hypothesis is presented in Table 4. From the statistical point view, the results indicate that the hypothesis is valid. For the first mode, the statistical analysis indicates that 88% of the variation in the damping ratio can be attributed to the independent variables {X1, X2, X3}.

CONCLUSIONS

Impact dampers can be effective in increasing the damping ratio of lightly damped flexible structures. The increase in damping is attributed to contribution of the impulse of the damper to the impulse and momentum equation of the test structure. Statistical analysis of the data obtained offers a degree of confidence in the multiple regression analysis performed in this study. It is believed that additional analysis of the data obtained can offer some insight in the behavior of the test structure. Additional experimental work on earth and in space is necessary

2. Using the multiple regression method to correlate the data.

INSTRUMENTATION

A 50-lb electromagnetic shaker was placed at a distance of 40.5 in from the center of the metal bracket. Eight accelerometers were placed approximately equally spaced along the length of the test structure (Halpin 1994). In addition a ninth accelerometer was used as a reference accelerometer at the point of excitation. A force transducer was attached to the test article at the location of the drive point to measure the input force. In addition, two force transducers were used to measure the impulsive force of the impact damper. Each steel billet was also instrumented with four accelerometers. Data acquisition was accomplished with the ZONIC 7000 48-channel data acquisition system.

TEST RESULTS AND ANALYSIS

Initial tests conducted on the test structure with impact occurring between the bare metal of the test article and the mass was recorded on magnetic tape and later digitized at rate of 10^6 samples per cycle. The results indicated that impact occurs at two impact per cycle at frequencies of 5, 10 and 20 Hz. It also showed that the impact force has the general form of an impulse with a duration of about 0.15 ms. A cushioning tape layer of about 0.1 in was used at both ends of the moving mass to widen the duration of the impact. This was necessary, first to eliminate the ringing effect of the noisy impact, and second to allow the capture of the impulse within the sampling limitations of the ZONIC 7000 system of 12,800 samples per second. The introduction of the cushioning tapes at both ends of the travelling mass resulted in impulse duration of about 1.5 ms, well within the limits of the ZONIC system.

To determine the damping ratios, twenty sine-sweep tests were performed for each of the first three natural frequencies for a total of sixty tests. Tables 1,2 and 3 show the results obtained. Six tests were conducted with the impact damper inactive, ie. the mass is restrained from moving. These tests form the baseline for comparison. It is noted that the intrinsic damping ratios ζ for the test structure are (0.336% and 0.31% for the first mode, 0.37% and 0.447% for the mode second, and 0.356% and 0.318% for third mode of vibration. Figure 2 shows the mode shapes for the test structure used in this investigation.

In performing the data acquisition, the maximum allowed block size of 4096 samples under triggered-continuous condition with 50% overlap was used. The Nyquist frequencies used were equal to 8, 16, 32 Hz for the first, second and third mode, respectively. The linear sweep rate recommended by Ewins (1983) was used to achieve accuracy.

The circle fit method was used to obtain an estimate of the damping ratio for each mode. Figure 2 shows a sample FRF and Coherence Functions. The results indicates that the parameters which was utilized in the acquisition and analysis of the data produced a good quality fit and hence an accurate estimate of the damping ratios. It is observed that the impact damper increases the damping ratio by as much as five folds.

Consider a mechanical system consisting of the test structure acted upon by the force supplied by the shaker and two impulses per cycle from the impact damper. The equation of impulse and momentum in the y-direction can be written covering a duration of one half cycle

TEST SETUP AND CONFIGURATION

The test structure consists of a 122 inch long brass tube, weighing 3.043 lb. It is simply supported at one end using a metal bracket and a universal joint. A linear helical spring is used to support the test structure at a variable distance from the simple support end. The stiffness of the spring was determined in the laboratory to be equal to 15 lb/in. The impact damper consists of a PVC cylindrical tube housing two aluminum discs at the top and bottom (Figure 1). The bottom disc is secured to a ring which fits around the brass tube with 4 screws. A sliding aluminum disc is used to adjust the distance in which the impacting mass is allowed to travel. The reader is advised to refer to Halpin (1994) for additional information related to the test setup and configuration.

The test structure was installed on two 2,000 pound steel billets. The billets were placed on steel supports to raise their levels high enough for shaker installation. The test structure was installed to the long sides of the billets for testing in the horizontal direction (Y+). One billet was used to attach the metal bracket providing the simple support for the test structure. It remained stationary throughout the test. The spring support was attached to the other billet which was moved as needed to vary the span between the two supports.

The test configurations can be summarized by the following conditions:

- a. Two spring support locations.
- b. Three impact damper locations.
- c. Three gaps.

TEST AND ANALYSIS PROCEDURES

To achieve the desired objectives of this investigation, the following test procedures were observed:

1. Check the quality of input forcing functions and driving point responses.
2. Confirm requested frequency range of 3 to 30 Hz is sufficient to obtain the desired flexural modes of test article.
3. Perform three tests at frequencies of 5, 10 and 20 Hz. Record the data on magnetic tape.
4. Digitize the data at a rate of one million per second and investigate the characteristics of the impact force at the top and bottom of the damper.
5. Determine optimum block size for data acquisition to have proper resolution for lowest test article flexural mode.
6. Find optimal input force level.
7. Document linearity and reciprocity of test structure (Halpin 1994).
8. Document repeatability of test structure from test to test.
9. Document modal characteristics of test structure.
10. Perform data quality review.
11. Perform sine sweeps of the test structure and record data.
12. Record time histories of all channels for selected tests and at selected frequencies.

Analysis of collected data was completed in two phases:

1. Using the SDRC-IDEAS software to obtain an estimate of the damping ratio using the circle fit method. The same software was used to obtain the mode shapes and natural frequencies.

INTRODUCTION

Attenuation of excessive vibration is an important design consideration in structural systems exposed to dynamic loads during their service. This can be achieved by actively or passively controlling the dynamic behavior of the structure. Methods of passive vibration control are quite often successful in achieving their objective at a relatively lower cost. They are often preferred over comparable active methods of vibration control if the structure will be used in a hostile operating environment, such as in outer space, where maintenance or monitoring is expensive.

An impact damper belongs to the category of passive vibration control devices. It consists of a free mass constrained to travel between two container walls. It produces substantial amount of damping in the structure it is attached to through momentum transfer.

Since the 1930's, numerous analytical and experimental studies have been conducted on SDOF and MDOF impact damped systems. However the experimental investigation of impact damped continuous systems was not undertaken until the early seventies.

In 1973 Masri (1973) performed experiments on a class of nonlinear dissipative cantilever and simply supported beams subjected to external sinusoidal excitation. He concluded that a heavier mass at an optimal clearance added to the systems damping. In addition the damper was more effective when located away from the node of the mode shape. In 1975 Roy and others (1975) produced similar results for fixed-fixed and simply supported beams subjected to base excitation.

Yousef and Akl (1987) performed a study of the free and forced vibration response of a vertical cantilever steel stack. Sliding and pendulum impact dampers were used in that investigation. A condition of two impacts per cycle was observed at frequencies higher than the fundamental frequency of the system. In addition it was concluded that an optimal clearance was associated with each impactor's mass.

Recently the second mode of a cantilever beam was studied by Chalmers and Semercigil (1992). They performed experiments with and without a rubber lining inside the boundaries of the damper's container. It was concluded that the rubber produced a characteristic behavior which was quite insensitive to the changes in particle clearance. Maximum damping was obtained by locating two dampers each at the locations of the largest amplitude.

OBJECTIVES

The objectives of this study are:

1. to investigate the effect of an impact damper on the dynamic behavior of a flexible structure where the effect of gravity is minimized.
2. to perform a number of tests on the flexible structure to study the effect of the mass, gap and location of the impact damper on the damping in the first three modes of vibration.
3. to analyze the data obtained in order to gain a better understanding of the behavior of the impact damper.

ABSTRACT

Impact dampers belong to the category of passive vibration devices used to attenuate the vibration of discrete and continuous systems. An Impact damper generally consists of a mass which is allowed to travel freely between two defined stops. Under the right conditions, the vibration of the structure to which the impact damper is attached will cause the mass of the impact damper to strike the structure. Previous analytical and experimental research work on the effect of impact dampers in attenuating the vibration of discrete and continuous systems have demonstrated their effectiveness. It has been shown in this study that impact dampers can increase the intrinsic damping of a lightly-damped flexible structure. The test structure consists of a slender flexible beam supported by a pin-type support at one end and supported by a linear helical flexible spring at another location. Sinusoidal excitation spanning the first three natural frequencies was applied in the horizontal plane. The orientation of the excitation and the test structure in the horizontal plane minimizes the effect of gravity on the behavior of the test structure. The excitation was applied using a linear sine sweep technique. The span of the test structure, the mass of the impact damper, the distance of travel, and the location of the impact damper along the span of the test structure were varied. The damping ratio are estimated for sixty test configurations. The results show that the impact damper significantly increases the damping ratio of the test structure. Statistical analysis of the results using the method of multiple linear regression indicates that a reasonable fit has been accomplished. It is concluded that additional experimental analysis of flexible structures in microgravity environment is needed in order to achieve a better understanding of the behavior of impact damper under conditions of microgravity. Numerical solution of the behavior of flexible structures equipped with impact dampers is also needed to predict stresses and deformations under operating conditions of microgravity in space applications.