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CALIBRATION IMPROVEMENTS TO ELECTRONICALLY-SCANNED PRESSURE SYSTEMS AND PRELIMINARY STATISTICAL ASSESSMENT

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Abstract

Orifice-to-orifice inconsistencies in data acquired with an electronically-scanned pressure system at the beginning of a wind tunnel experiment forced modifications to the standard, instrument calibration procedures. These modifications included a large increase in the number of calibration points which would allow a critical examination of the calibration curve-fit process, and a subsequent post-test reduction of the pressure data. Evaluation of these data has resulted in an improved functional representation of the pressure-voltage signature for electronically-scanned pressures sensors, which can reduce the errors due to calibration curve fit to under 0.10 percent of compared to the manufacturer specified 0.10 percent of full scale. Application of the improved calibration function allows a more rational selection of the calibration set-point pressures. These pressures should be adjusted to achieve a voltage output which matches the physical shape of the pressure-voltage signature of the sensor. This process is conducted in lieu of the more where a traditional approach calibration pressure is specified and the resulting sensor voltage is recorded. The fifteen calibrations acquired over the two-week duration of the wind tunnel test were further used to perform a assessment of the statistical preliminary. variation in the calibration process. The results allowed the estimation of the bias uncertainty for a single instrument calibration; and, they form the precursor for more extensive and more controlled studies in the laboratory.

Introduction

Electronically-scanned pressure systems have become a mainstay of experimental

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testing because they provide a low-cost-perchannel instrumentation solution where large numbers of pressure measurements are required. These systems are computer controlled; they are relatively easy to use; they provide ondemand, "rapid" calibration techniques; and, they are capable of high accuracy when used controlled. laboratory environments. However, as with any instrument, their use is pushed into originally unintended where unevaluated areas measurement uncertainties may become large. Such an area was explored when pressures were acquired on the external nozzle expansion ramp of a powered, generic, hypersonic configuration which was tested (Everhart, Ashby, and Monta 1992, 1993) in the 20-Inch Mach 6 Tunnel at the NASA Langley Research Center (Miller and Smith 1986, Miller 1990). During this experiment an electronically-scanned pressure system was used to acquire pressures at 257 orifice locations on the model. The pressures measured on the nozzle expansion ramp, specifically, varied from near atmospheric values at the engine exhaust plane to about 0.01 atmospheres near the model trailing edge; in other words, accurate measurements were required over two orders of magnitude in pressure, and the instrumentation had to be selected to accommodate this variation. Several typical nozzle centerline distributions of local static pressure, p, normalized by the engine exit-plane pressure, p4, are shown in Figure 1. Additionally, because the maximum freestream static pressure is on the order of 0.3 psi, the closest, logical reference pressure for the instrumentation is vacuum, which means that differential pressure gages must be used in the absolute sense by evacuating the reference side of the gage. Because the engine exhaustplane pressure and tunnel test conditions were varied widely, pressures on the nozzle at a fixed model station also varied widely; in many cases these pressures were outside the central portion of the sensor range, nominally 15- to 85-percent of full scale, where the most accurate measurements are typically achieved. In some cases the test conditions were such that the pressure at given orifice might drop below the 15-percent "limit" and exceed the 85-percent

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"limit" during the same wind tunnel run. The new pressure system was also required to measure nozzle pressures on the unpowered model where values near freestream were realized on all orifices simultaneously; thus, large range sensors were required to resolve small pressures. It is important to note that it was not feasible to modify the pressure orifice hookup between wind tunnel runs to more appropriately match measurement requirements sensor capabilities because of the complexity of the model buildup and time restrictions imposed by the facility schedule.

As a routine part of the initial setup and system checkout, the wind tunnel evacuated to low pressure and data were recorded in a "wind-off" mode on all model pressure orifices. Significant, inconsistent. orifice-to-orifice pressure variations which could not be resolved by "tuning" the measurement system were revealed in these data. This tuning included among other things changing the calibration reference-pressure set points which modified the calibration coefficients, and changing the reference pressure dwell time to ensure pressure settling. Because the observed inconsistencies could not be removed, the calibration procedures were modified to allow greater flexibility in the post-test evaluation of the data and the pressure system calibration process. Even though these data were acquired during a hypersonic experiment, they are applicable to all situations where low pressure measurements with electronically-scanned pressure systems are used because of a similar response of the sensor near zero differential pressure.

This paper, then, has the following three objectives:

- (1) It highlights some problems which exist in the currently used, standard calibration techniques.
- (2) It presents a new functional representation of the characteristic pressure-voltage signature which markedly improves the measurement accuracy across the pressure range for electronically-scanned pressure gages. Additionally, this new functional representation leads to a more rational criteria for selecting the calibration pressures.
- (3) This paper presents a preliminary statistical assessment of these calibration results. The assessment allows an estimate of the

uncertainty in this calibration process, and it serves as a precursor to more controlled and detailed experiments with these instruments.

Nomenclature

- a_i, b, c_i General calibration function fitting coefficients, see eqn 1.
- A₁, A₂, A₃, A₄ Calibration function fitting coefficients, see eqn 3.
- B_X Bias error.
- f Linear sum of g functions, see eqn. 7.
- g Arbitrary function, see eqn 7.
- G Matrix of g functions, see eqn 11.
- m, n Number of summation coefficients, see eqn 1.
- Px Precision error.
- p Pressure, psi
- p₄ Nozzle exit pressure, psi
- Q Weighting function, see eqn 10.
- t Student's t distribution
- U Uncertainty
- V Sensor output voltage, volt
- V₀ Zero-pressure offset voltage, volt
- X Arbitrary independent variable.
- \overline{X} Average of X over n repeats.
- Y Measured value at X.
- \hat{Y} Mathematical approximation to Y, see
- Z Offset-referenced voltage, volt, see egn 2

Subscripts

ref Reference

Abbreviations

- Cl Confidence interval
- ESP Electronically scanned pressure
- F.S. Full scale
- MLS Method of least squares
- PI Prediction interval
- Pnt Point
- PRE Percent residual error, |Δp|/p x 100%
- Rdg Reading
- RE Residual error, Δp, psi
- SD Standard deviation, psi
- SE Standard error, psi

Experimental Procedure

Specific information concerning the wind tunnel, model and experiment are discussed by Everhart, Ashby, and Monta (1992, 1993). This section presents a discussion of the instrumentation used to acquire the pressure data with particular emphasis on procedures used during the calibration process.

Instrumentation

The System 8400 data acquisition instrumentation manufactured by Pressure Systems, Incorporated (PSI) was used to acquire the pressure data. The system may be controlled either from the front panel or by an external computer. Seven different electronically-scanned pressure (ESP) modules in Table 1 were used as enumerated simultaneously to measure the pressures. Also listed are the number of ports (sensors) per module and the manufacturer-specified uncertainty as a percent of full-scale pressure range.

If the ESP modules are maintained in a temperature-controlled laboratory environment, these systems are capable of high-accuracy measurements. This high accuracy occurs because temperature sensitivity effects on the zero-pressure offset voltage for each sensor are minimized due to the on-demand calibration capability of the system. It is the error introduced by temperature variation of the ESP module which may yield first-order variation in the calibration voltages, and, as a result, the When performing a calibration coefficients. standard calibration, a mechanical, internal, sliding block in each ESP module is used to isolate all sensors from their individual pressure orifice tubes; external calibration pressures are then applied to all ESP sensors simultaneously by the Pressure Standard Unit which contains a high accuracy (0.02% FS) reference pressure standard; and, the output is digitized by the Scanner Digitizer Unit using a 16-bit analog-todigital converter. Calibrations in the present experiments were conducted immediately prior to each wind tunnel run, and the additional precaution of insulating the ESP modules was taken to further reduce the impact of temperature variations during the acquisition of test data. Stable ESP module temperatures were monitored throughout the calibration and test process.

The standard ESP calibration typically consists of either 3 or 5 data points which are used, respectively, to determine either a parabolic or a quartic polynomial representation of the pressure-voltage signature. As a result, the calibration curve, first, passes through the calibration data, encapsulating any random measurement error in the calibration coefficients, which, then propagates any error into the test data. Additionally, this polynomial

calibration curve may or may not model the actual pressure-voltage signature of each ESP module sensor, particularly for small pressures or for pressures exceeding the range of the calibration data where the fitting polynomial may exhibit a non-physical behavior; thus, extrapolation of calibration results is very tenuous and uncertain.

For the present study, the differential ESP modules were used as absolute gages by evacuating the reference side of the modules using a common vacuum source. Because of curve-fit inadequacies when using the standard calibration techniques and because calibration uncertainties experienced at the beginning of the study, the standard calibration method was unacceptable, and a different calibration procedure was used. In this procedure the sensor isolation block was slid into the calibrate position and a needle valve combined with a vacuum source was used to manually and successively apply 15 to 22 scheduled, calibration pressures to each of the ESP modules simultaneously. (Note that positive pressures were applied by venting to Each calibration reference atmosphere.) pressure was dialed into a digital channel on the data acquisition computer where it was recorded along with the digitized ESP voltage outputs of the System 8400 for post-test reduction.

When not in use, the ESP calibration block was slid into the calibrate position. Vacuum pressure was then applied to both the calibration and reference side of sensor to unload it to prevent the formation of a hysteresis bias. An important note is that the ESP sensors are structurally capable of sustaining the atmospheric differential pressure which was realized at the highest calibration pressures; however, a saturation voltage level of approximately 5 volts is achieved whenever the pressure exceeds the rated range of the ESP module, and these data were discarded when encountered.

Fifteen calibrations were made over the two-week duration of the study immediately prior to each wind tunnel run, each requiring 15-20 minutes to execute because of the modified calibration procedures.

Calibration-Pressure Working Standard

The value of the calibration reference pressure was set using a Mensor DPG II (Digital

Pressure Gauge, Model 14000) reference standard with a full scale range of 50 psi. The instrument has a compensated temperature range of 15° to 35° Centigrade. According to the UNCERTAINTY section in the Mensor operating guide (Mensor 1992)

"Measurement error due to the combined effects of hysteresis, repeatability, linearity and temperature is 0.01% of full scale or less over the compensated temperature range."

This yields an uncertainty of 0.005 psi which for the present test conditions represents 1.72% of freestream static pressure, 0.067% of freestream dynamic pressure, and 1.39% of the full-scale value of the 0.36-psi ESP module (i.e. the smallest module). While the Mensor range was larger than desired, it was the only pressure standard available on short notice and these uncertainties were deemed acceptable for the present application.

When selected the 50-psi Mensor was an acceptable choice. However, upon additional, post-test reading, the operating manual further states in the WARMUP section that after 30minute warm-up the zero drift of the instrument Span drift is is 0.01% full scale per hour. quoted as 0.005% full scale per week. Typical operating procedures are to leave instrumentation in a power-on state and to zero the instrumentation at the start of a shift; thus, significant zero-drift error may occur prior to acquiring calibration data, particularly if problems which delay testing occur. This subject will be further addressed in the "Preliminary Statistical Assessment" section in this paper.

Standard ESP Calibration Methods

The most crucial portion of any measurement process is the calibration of the instrumentation. Generally, the quality of the calibration is only as good as the functional representation of the physical process being modeled; in the case of the ESP, this physical process is represented by the pressure-voltage signature of the sensor. Typical calibration data are shown in Figure 2a for three ports, each from different ESP modules. The pressure data, p, are plotted on a linear scale for variations in output voltage, V. The port identification nomenclature is a single digit for the module combined with two digits for the

port; for example, port 624 represents module 6, port 24. Also shown in the inset is an expansion of the pressure region from 0 psi to 2 psi. Several observations can be made directly for all modules: first, away from zero pressure, the pressure-voltage signature is extremely linear; second, there appears to be significant nonlinearity near zero pressure; and, finally, there is a large variation in the zero-pressure offset value of the sensor.

The low-pressure variations are more readily apparent in Figure 2b which replots the pressure logarithmically. Additional data have been added to those of Figure 2a to highlight the variations in zero-pressure offset within a single module; filled symbols represent the minimum value, while open symbols represent the maximum value. Offset results from the other ports on a given module are randomly dispersed between the limits presented.

The remainder of this section evaluates the standard, polynomial calibration methods used in ESP system hardware. Then, it then extends this by applying the method of least squares (MLS) to all of the calibration data to evaluate possible improvements in the calibration fitting. Finally, it presents an improved functional representation of the pressure-voltage signature whose coefficients are determined by least squares fitting; recommendations for implementation are given for the improved curve-fit formulation.

Polynomial-Fitting Method

The standard, supplied method of representing an ESP pressure-voltage signature is to fit an n-1 order curve through n data points. Typically, the pressure data points are selected to cover the minimum and maximum expected values, and, then, equally spaced intervals are created within this range. Figure 3 considers calibration data from port 16 from each module, and examines how well successively higher order polynomials fit the unused, intermediate calibration data. Each of the figures are standardized to plot the calibration pressures (p) and curve fit, the residual error (Δp) , and the magnitude of the percent of reading error ($|\Delta p|/p$) versus output voltage. Figure 3a presents the linear fit using just the two end points. In this case, using the data extremes will bias the calibration curve such that it consistently underestimates intermediate Residual errors (RE) in the lowpressures. pressure region peak at values near 0.15 psi

while peak percent-reading errors (PRE) lie in the 30-50 percent range for all modules. Additionally. extrapolation of any calibration results toward zero pressure would be erroneous because the linear curve doesn't properly capture the roll off. A higher-order, parabolic representation is obtained by using a 3-point approximation and the results are shown in Figure 3b. Even though the data and the curve fit are in better agreement, the 2.5-psi (for example) has a significant module of 0.05 psi at 1.5 discrepancy (corresponding to 0.7 psi). This discrepancy exceeds the 0.0025 psi full-scale accuracy of the 2.5-psi module at 30 percent of the module range. Figure 3c presents a cubic fit of the data (4 points) which, again, offers little improvement to the calibration, and, in fact, shows a definite non-physical curvature within the range of the 0.36-psi data. Peak PRE values remain in the 8-45 percent range, and PRE is decreased for the 0.36-psi modules only because the calibration curve is fitting error due to smaller numbers of available calibration pressures. The "best-fit" capability of the System 8400 is with five points which yields a quartic polynomial as shown in Figure 3d. Errors in the high pressure regions have been significantly reduced due to fitting more data points; however, unacceptably large errors (40-percent PRE) still exist in the low-pressure regions.

Figure 4 presents calibration-curve differences resulting from pressure set-point The curves are standard 5-point (quartic) fits for port 16 on a 2.5-psi and port 16 on a 0.36-psi module. The open symbols represent all calibration data while the filled symbols are the data used to fit the curve. In the top case, large differences are visible the calibration curve and points at the "error calibration immediately to the left of the position labeled "Cal Set Point". In the bottom case, the "Cal Set Point" station has been interchanged with the "error station" and error is re-distributed to the right of the of "Cal Set Point". Additionally, the curves beyond the calibration range show very different, non-physical behavior. In other words, for the standard method, a judicious placement of the calibration data points is required to minimize the curve fitting error, as is an appropriate selection of the order of the fitting polynomial. It is important to note that the pressure-voltage signature for each sensor is unique and the best selection of calibration pressures will, therefore, also be unique and possibly vary from port to port.

Polynomial Fit Using Method of Least Squares

The method of least squares (MLS) was applied to the entire calibration data set (1) to minimize the "engineering-judgment" effects of calibration data point selection and (2) to obtain a rational definition of the fitting coefficients which allows for random error in the measurement process. The results using the calibration data of Figure 3 are shown in Figure 5 for linear (Fig. 5a), parabolic (Fig.5b), cubic (Fig.5c), and quartic (Fig.5d) MLS curve fits. Each of the figures are semi-logarithmic plots of the calibration pressures (p) and curve fit, the residual error (Δp), and the magnitude of the percent of reading error $(|\Delta p|/p)$ versus output voltage. Using this method, low-pressure PRE is reduced to about 10-percent compared to 30-50 percent with the Standard Method, while PRE of 0.1-1.0 percent are obtained in the high-pressure range. Because the pressurevoltage signature is represented by polynomials, the calibration curve will begin fitting error in the data, driving it to zero with successively higher-order terms, instead of fitting the actual functional representation of the Additionally, higher order polynomials may exhibit large oscillations within the range of the data even using MLS; this is known as the Runge Phenomena (ref. Young and Gregory, 1972).

Improved ESP Functional Representation

It was necessary to develop an alternate functional representation of the ESP pressure-voltage signature because of the previously cited data fitting inadequacies. A more general calibration function (compared to a standard polynomial) with the desired mathematical and physical properties is given by

$$p = \sum_{i=2}^{m} a_i Z^{\frac{1}{i}} + bZ + \sum_{j=2}^{n} c_j Z^j$$
 (1)

where

$$Z = V - V_0 \tag{2}$$

The V_0 is the sensor voltage at zero pressure and a_i , b, and c_j are fitting coefficients. General properties of this function include:

(1) As Z becomes large, the coefficients b and c_i dominate and a near-linear

- relationship may be retained for small n; and.
- (2) As Z approaches zero, the coefficient a dominates and the low-voltage nonlinearity in the pressure signature (see Fig. 2a) can be modeled.

Specific criteria for selecting the values of m and n are that the resulting equation should be physically representative of the pressure-voltage signature, and the number of coefficients should be minimized to decrease data acquisition requirements. Because of previous experience and because the pressure data presented in figure 2a show a distinctly linear trend as voltage becomes large, the value of n was specified as 2 to capture any existing nonlinearity. Trial and error solutions showed it sufficient to specify m as 3. The resulting specific calibration function is written as

$$p = A_1 Z^{\frac{1}{3}} + A_2 Z^{\frac{1}{2}} + A_3 Z^1 + A_4 Z^2$$
 (3)

Because absolute zero pressure can never be obtained when the ESP modules are used as absolute gages, the true value of V_0 will never be realized in practice. Therefore, V_0 must be determined as part of the solution process, resulting in an "apparent" zero-pressure value.

The fitting function coefficients A₁, A₂, A₃, and A₄, and the zero-pressure voltage V₀ are iteratively determined in the following manner. First, the minimum voltage measured during the calibration is selected as the initial value of Vo and used to compute a first estimate for Z for each calibration pressure. The coefficients are determined using MLS (Press, et al. 1990) and used to evaluate the standard error of the calibration data about this candidate fitting At this point, a new value of Vo is selected and the process is repeated until minimum standard error convergence (Note that Z can never assume a obtained. negative value.) For ESP modules used as differential gages, the value of Vo can be measured directly by unloading the sensor (i.e. venting both sides of the sensor to atmosphere). allowing Z to be computed directly. Separate calibrations for positive and negative values of Z may then be conducted, and positive-side and negative-side calibration coefficients may be iteratively obtained by using the absolute values of the calibration pressures and of Z.

Results of the fitting process applied to the improved calibration function are shown in

Figure 6 for port 16 (same data as that of Figures 2-5) on ESP modules with ranges of 0.36-, 2.5-, 5-, and 15-psi. As in Figure 5, the pressure data and RE are plotted semilogarithmically versus Z to highlight the differences at low pressure. The symbols represent the calibration data and the line represents the improved ESP fitting function. It is important to note that the RE and PRE scales have been reduced by an order of magnitude compared to previous results. Comparing the present results with Figure 5 (polynomial fitting with MLS) shows that maximum residual errors have been reduced from 0.04 to 0.006 psi. The maximum PRE values away from the immediate vicinity of the origin (Z=0 volt) occur in the region corresponding to the knee (Z=0.5 volt) of the pressure curve. Percent reading errors in this region have been reduced almost two orders of magnitude from about 10 percent for polynomial fitting with MLS to under 0.3 percent for the present method. Typical PRE values for the present method are 0.1 percent or less across the Z range. Calibration curves from three different 0.36-psi and two different 15-psi ESP modules show that not only do similar calibrations exist within a module range but that consistent results are obtained across the range.

Typical coefficients for several curves shown in Figure 6 are given in Table 2 where a regular order in their values can be observed for increasing module range. Coefficients A, and A₂ monotonically increase and decrease. respectively, with module range, though the significance of these trends are at present unknown. The magnitudes of the slope coefficient, A₃, are typical and linearly increase with module range as with standard ESP calibration techniques. The linearity of the ESP sensors is further demonstrated observing the small size of the nonlinear coefficient, A₄, as compared to the value of A₃. The size of A₄ is traditionally examined in the standard method to test for "calibration goodness". An additional indication of the goodness of the improved curve fit can be observed by examing the small size of the percent-full-scale error, defined as curve-fit standard error (SE) normalized by the full-scale module range, which is under 0.1%. previously demonstrated, this percent-full-scale error can be stated equally well as a percent-ofreading error.

Several properties of the present function can be observed by examining the equation, the results of Figure 6, and the values

in Table 2. First, in direct contrast to results presented for the other methods, this function properly captures the physical shape over all module ranges tested, especially in the lowpressure knee region about Z=0.5 volt. result, residual errors in pressure in both the absolute sense and as a percent of reading are very small compared to other methods across the entire pressure range of all modules tested. For large Z, the equation is a low-order, nearlylinear polynomial which allows a rational extrapolation toward the upper voltage limit of the sensor. For small Z, the equation reduces to a low-order root expansion which, again, allows a rational and consistent extrapolation toward the "apparent" zero-pressure value.

Residual Error Assessment

Residual errors (RE) are used to assess the calibration-method consistency for other sensor ports within a pressure range and when compared to other ranges. Residual errors for all ports obtained for a single calibration are presented in Figure 7. The RE distributions are similarly biased in both magnitude direction for each range which implies similarity of all calibrations (note that RE values are plotted for three 0.36-psi modules and two 15psi modules). Though not randomly distributed as ideally required by MLS theory, inclusion of higher-order calibration terms in the functional representation is unwarranted for the present case because immediately away from the origin RE are within the measurement accuracy of the calibration-pressure working standard.

Effect of Calibration Data Distribution

The sensitivity effects of the number of calibration pressures and their distribution on the calibration curve fit are plotted in Figure 8 for a 15-psi-range ESP module. The 22 calibration pressures are given by the open symbols and filled symbols are used to denote the evaluation subsets which include cases with 8, 7, 6, and 5 pressures. Three 5-point cases various selected with set-point arrangements because five points represent the minimum number for MLS fitting with four coefficients. Five points also helps minimize the time required to calibrate, which enhances wind tunnel productivity. Solid lines are used for the complete 22-point calibration, while are used for the lines calibrations. The pressure-selection criteria for the subset evaluations was to anchor the ends of the range (i.e. the maximum and minimum values), select a pressure in the midrange, and to distribute the remaining pressures in the knee region. In each case, the dashed subset lines are indistinguishable from the solid completecalibration lines. Values of the standard error, the curve-fit coefficients, and apparent Vo are presented in Table 3 for the cases plotted in Figure 8. Reducing the number of calibration pressures has little effect on the standard error until five points is reached. At this point, few degrees freedom exist so little variability is allowed; therefore, standard error is driven close to zero. The apparent zero-pressure voltage is virtually unaffected and varies only 0.00006 volts from minimum to maximum. Coefficients A₁, A₂, A₃, and A₄ have only a small variation with the largest variations appearing in A₁ and A₂ as expected. This insensitivity to number of points and location is a further indication that the physics (though empirically derived) are properly modeled with this mathematical representation.

Recommended Calibration Technique

The typical calibration philosophy is to prescribe a schedule of calibration pressures, record the resulting sensor voltage output, and curve fit these data with a standard polynomial. As has been demonstrated, this procedure can lead to substantial curve fit errors. It has also been demonstrated that the pressure-voltage relationship of the ESP module has a definite signature, that equation (3) is a significantly improved mathematical model of this signature, and that the curve fit is relatively insensitive to both number of points and their location. Therefore, based on current understanding, a new paradigm for calibrating ESP modules has emerged wherein the calibration should be applied to generate a voltage output These positions near specific values of Z. include a minimum of 5 pressure settings which significant features of the capture curve, including the minimum calibration (Z=0.0 volts), below the knee (Z=0.25 volts), above the knee (Z=1.0 volt), in the midrange (Z=2.5 volts), and near the maximum (Z=4.5 volts). Because of the insensitivity of the curve, Z may be approximated by initially using as V_0 that value corresponding to near vacuum pressure (a final Z will result from the curve-fit process). Obviously, additional pressures are desirable to reduce the curve fit uncertainty; however, they may not be required with standards data improved pressure and procedures, and with further acquisition experience.

Preliminary Statistical Assessment

A preliminary statistical evaluation of the ESP calibration is presented in this section. The present data were acquired over a two-week period and include changes in the System 8400 instrumentation and model hookup, as well as temperature cycling due to the operation of the wind tunnel. The present data, while sufficient for a wind tunnel experiment, are insufficient to perform a detailed, statistical characterization of the ESP calibration process, because data would be obtained which under more controlled, laboratory conditions were not acquired. Additional data required to satisfy were not these more stringent conditions would include, for instance,

- extensive back-to-back calibrations to assess error from random effects,
- (2) precise control of the sensor temperature to evaluate zero-pressure voltage variations.
- (3) more precise control and recording of calibration set-point pressure,
- (4) smaller range pressure standards,
- (5) variations in ambient pressure, and
- (6) vibration effects.

What the present data do allow is a statistical evaluation of the functional representation of the pressure-voltage signature, a near-term (over a 2-week period) statistical look at calibration coefficient variability in a real-world environment, and an estimate of systematic errors in the calibration. The first subsection presents some fundamental statistical concepts. In depth discussions of the required statistics can be obtained in standard texts such as Coleman and Steele (1989).

Fundamental Statistical Concepts

Generally, a single data value, X, is the best estimate, $X_{measured}$, of the true value to within an uncertainty, U_X , at a specified level of confidence. That is,

$$X = X_{measured} \pm U_X \tag{4}$$

where the uncertainty may be further separated into precision error, P_X , and bias error, B_X . The uncertainty is given by

$$U_x^2 = B_x^2 + P_x^2 (5)$$

Bias errors are the systematic offset of a measurement from its true value. Bias errors are often erroneously excluded when quoting measurement accuracies; many times they are excluded because they must be referenced to some recognized absolute which is difficult to Precision errors are measurement errors. Typically, precision errors have a Gaussian or normal distribution about the mean value. A measure of the spread of this distribution about the mean is given by the standard deviation. Standard deviation is defined as

$$\sigma_X = \sqrt{\sum_{i=1}^n \frac{(X_i - \overline{X})^2}{(n-1)}}$$
 (6)

where \overline{X} is the mean value of the X_i taken over n repeats.

For a series of measured data values, Y, at independent variable X, the approximating functional variation, \hat{Y} , through these values is given by

$$\hat{Y}(X) = a_1 g_1(X) + a_2 g_2(X) + \dots + a_k g_k(X)$$

$$= f(X; a_j), \quad \text{with} \quad j = 1, 2, \dots, k$$
(7)

where f is the linear combination of the functions g_j . The coefficients a_j are, typically, determined in a "best-fit" sense using techniques such as the Method of Least Squares (Brownlee 1965) which minimize the data scatter about the approximating function $\hat{Y}(X)$, usually by assuming a normal or Gaussian distribution. A polynomial is an example of a function f where the g_1, g_2, g_3, \ldots functions would be given by 1, x, \hat{x}, \ldots , respectively.

Many measures of "curve-fit goodness" are available. One is given by the standard error defined as

$$SE = \sqrt{\sum_{i=1}^{n} \frac{[Y_i - \hat{Y}(X_i)]^2}{(n-k)}}$$
 (8)

where Y_i is the measured data value and \hat{Y} is the approximated value at X_i . The number of degrees of freedom is given by the difference between the number of data values, n, and the number of coefficients, k. The number of degrees of freedom is important for flexibility in mathematically "fairing" the curve through the

data trend, in contrast to "fitting" the curve through the data value. Another measure of goodness is given by the confidence interval, CI, which defines an uncertainty band at a specified level of confidence about the curve \hat{Y} and within which the true value is predicted to lie. Following the nomenclature of Wahls, et al. (1995), confidence interval at the point X_0 is defined as

$$CI(X_0) = \pm t_{\alpha/2,\nu} \times SE \times Q(X_0)$$
 (9)

where $t_{\alpha/2,\nu}$ is the value of the student's t distribution at the α confidence level for ν =n-k degrees of freedom. The term $Q(X_0)$ is a weighting function based on data density and is defined as

$$Q(X_0) = \sqrt{G_0^T (G^T G)^{-1} G_0}$$
 (10)

where

$$G = [g_1, g_2, g_3 ... g_k]_{kr}$$
 (11)

is a matrix of the g_i functions of equation (7), and the transpose of G evaluated at X_0 is given by

$$G_0^T = [g_1(X_0), g_2, (X_0), g_3(X_0), ..., g_k(X_0)]_{1 \times k}$$
 (12)

A final, necessary, statistical concept is that of the prediction interval, PI. A prediction interval is the uncertainty band about the curve \hat{Y} within which a future value or measurement is projected to lie based on available (historical) results and assuming the measurement process is unchanged. Prediction interval is defined as

$$PI = \pm t_{\alpha/2, \nu} \times SE \times \sqrt{1 + Q(X_0)^2}$$
 (13)

It is important to note that through Q the CI and PI are functions of the data density; therefore, they will generally have a narrower band in those regions where data density is the greatest since curve fits are generally more accurate there. The band will expand near the extremes where fewer data points usually exist. For the present paper, all uncertainties are taken at the 95% confidence level.

Coefficient Averages and Standard Deviations

The coefficient averages and standard deviations for each module for a single

calibration are presented in Table 4. coefficients A₁, A₂, and A₃ the averages are well behaved in that they exhibit a linear variation with module range and the standard deviations are, typically, an order of magnitude smaller than the coefficient averages, except for the smallest range where less data are available at the lowest pressures for fitting. The standard deviation of the A₄ coefficients is of comparable size with the average coefficient; this is an additional indication of the linearity of the pressure-voltage signature for large Z. A visual examination of the curve-fit plots and coefficient tabulations, the consistency of the coefficient averages and standard deviations, and the small size of the residual errors the empirical. mathematical validates modeling of the physical process.

Calibration Curve and Coefficient Variability

An example of the calibration-tocalibration variability is given in Figure 9 for the 15 separate ESP calibrations for port 16 from the 2.5-psi module. Fourteen calibrations for this port are contained within a tight band. These fourteen calibrations were obtained for a stable hardware configuration. The outlying, initial curve was obtained prior to a System 8400 hardware modification and demonstrates an effect of changing the measurement process. This outlying curve also demonstrates the need for end-to-end system characterization, calibration, and configuration Generally, the fourteen calibration are similar; however, the expanded control. scale shows visible variation occurring among the curves in the knee region below Z=1.0 volt. Control charts representing the historical variation of the curve coefficients are given in Figure 10. Generally, the coefficients contain only small variation between successive cases with the most significant difference occurring for the initial case. The relative invariance of V₀ for the larger range modules (Fig. 10a) is indicative of the general stability of the environmental temperature. Increased Vo variability is expected and is visible for the 0.36psi modules because the calibration pressure points are fewer and more evenly distributed over the module range compared to the dense data distribution at low pressures for the higher range modules (see Figure 2).

Calibration curve variational trends for the different pressure modules were further examined by subtracting a reference calibration for each module from the other calibrations of the same module. The resulting incrementalpressure expression

$$p - p_{ref} = (A_1 - A_{1,ref})Z^{\frac{1}{3}} + (A_2 - A_{2,ref})Z^{\frac{1}{2}} + (A_3 - A_{3,ref})Z^{1} + (A_4 - A_{4,ref})Z^{2}$$
(14)

was evaluated at Z=2 volts using calibration 7 as the reference, and the results are plotted in Figure 11. This incremental representation collapses the calibrations and it displays an obvious wavy trend in the calibration history. Because all modules are affected similarly, the cause of the trend is independent of the module and must be the result some external influence. The exact reason for this variation is unknown: however, part of the shift is believed to be the result of a drifting zero setting on the calibration-pressure working standard. If this is indeed the case, the reference standard would have a potential full-scale root-mean-square error (including transducer uncertainty plus zero-drift uncertainty) $\pm [(0.01)^2 + (0.01)^2]^{1/2} = \pm 0.014\%$ or ± 0.0071 psi. This would be particularly significant at the smallest pressures where it would translate into uncertainties in the A_1 and A_2 coefficients, which would most affect the calibration-curve knee region.

Estimate of Calibration Curve Uncertainty

Any constant, unknown shift in the data for a single calibration caused by an external error source (ex. erroneous zero setting on the pressure standard) is a bias error which, if uncorrected, becomes encapsulated in the final data. If these bias errors randomly vary between calibrations, then they become part of the measurement imprecision for the entire test. This calibration imprecision can be analyzed by examining the variability of the aggregate calibration data set, which will yield a estimate of the bias uncertainty for a single calibration. Random variation has been demonstrated for the present calibration curves (see Figure 11), and sufficient data are available (fourteen process-stable calibrations) for statistical assessment of the bias as follows. First, the individual, previously-determined. apparent zero-pressure voltages are subtracted from each data set and the data are, then, grouped into a single aggregate. Finally, the improved calibration curve (equation 3) is generated for this aggregate data set, and, CI and PI statistics (eqns. 9 and 13, respectively) are determined. The results for modules in each pressure range

are shown in Figure 12 where the symbols are the aggregate data for port 16 and the solid lines represent the aggregate curve fit. (Note, again, that the pressure scale is logarithmic.) The nominal magnitudes of the CI and PI at the 95% level of uncertainty are 0.003 and 0.020 psi. Normally, these values would be presented as positive and negative increments about the curve; however, because of their small size they are presented separately for clarity. Confidence interval increases somewhat at the higher calibration pressures because there are fewer data available to fit in this region. individual curves are not distinguished according to module range because the differences are negligible for the present purpose. Recall that the CI represents the uncertainty band about the estimated calibration curve within which the true curve will lie 95-percent of the time. The small CI value statistically implies that the estimated calibration curve is very representative of the of the true curve for these aggregate data. Recall also that the PI is based on historical data and that it represents the uncertainty band about the estimated curve within which calibration curve would lie assuming that no changes in the calibration process occur. bias uncertainty is 0.04-percent of the full-scale range of the calibration standard which exceeds the 0.01-percent accuracy specification of the instrument. By taking the root-mean-square difference between the potential error sources (0.01-percent accuracy specification and a 0.01-percent zero shift) and the actual 0.04percent measurement, an additional bias uncertainty of 0.014 percent is obtained for all other, unknown, sources.

Estimate of Pressure Uncertainty

Uncertainties due to temperature variations are considered negligible because:

- the ESP modules were calibrated prior to each run which removes the first order effect of module temperature variation,
- (2) the ESP modules are mounted in the injection chamber beneath the wind tunnel, which is isolated from the high-temperature stream by a solid floor plate,
- (3) the ESP modules were insulated and stable temperatures were recorded on the external surface of the module case during each run, and
- (4) the relative invariance of the V₀ presented in Figure 10a, particularly for the larger

range modules, does not imply any significant temperatures excursions.

Back-to-back repeat calibrations required to assess uncertainties due to short-term randomness in the pressure were not acquired. However, as per Table 1, the manufacturer specifications for these instruments are 0.1% FS for modules in the range of 0.36 psi to 2.5 psi and 0.05% FS for modules in the range of 5 psi to 15 psi.

Uncertainties due to calibration curve fit have been identified herein to be 0.1% of reading or less.

An estimate of the bias error from all external sources has been shown to be four times the manufacturer specified level of 0.01% FS for the calibration standard. This error is a constant ± 0.02 psi for all ESP modules. The most likely error source is an erroneous zero setting on the reference standard.

For pressure data acquired using the present ESP calibration data, these estimates yield bias and precision uncertainties of

$$B_p^2 = (0.02)^2 + (0.001 x p)^2$$
 (15)

and,

$$P_P^2 = (0.0005 x p_{FS})^2, p_{FS} \ge 5 \text{psi}$$

= $(0.0010 x p_{FS})^2, p_{FS} < 5 \text{psi}$ (16)

where p_{FS} is the full-scale range of the ESP module under consideration.

Concluding Remarks

Pressure measurement inconsistencies which occurred during the conduct of a wind experiment prompted а examination of the calibration process and the mathematical relationship used to model the pressure-voltage signature of an electronicallyscanned pressure system. This examination revealed deficiencies and inadequacies with calibration techniques. the current Specifically, the standard 3-point parabolic-fit and 5-point quartic-fit calibration methods are insufficient in that (1) they do not capture the low-pressure variation of the sensor, and (2) that any extrapolation beyond the calibration data range to either low or high pressures is tenuous due to the Runge Phenomena, which is a

mathematical oscillation inherent in higherorder polynomials. Furthermore, extension of the standard polynomial fitting method by the method of least squares offers improvement to the calibration because of (1) inappropriate modeling of the pressure-voltage signature, (2) the uncertainty associated with the selection of the calibration set points, and (3) the possible deviations due to fitting-curve oscillations within the range of the data, again, due to the Runge Phenomena. functional representation of the pressure-voltage signature has been developed demonstrated to offer significant calibration improvements for low to high pressures, and it is applicable over all tested ESP module sizes. Calibration coefficients resulting from this procedure are well-behaved in that they have a regular variation and, where applicable, are comparable in magnitude to those obtained using standard techniques. In addition, the calibration curve varies properly within the data range and it can be safely extrapolated to the voltage limit of the sensor. The improved representation allows these instruments to achieve 0.1-percent of reading accuracy (or better) across the module pressure range.

With the improved calibration function, an alternate calibration procedure has emerged calibration wherein pressures should adjusted to achieve a specific schedule of This procedure calibration voltages. proposed in lieu of the more traditional approach where a calibration pressure is specified and the resulting voltage is recorded. In this revised approach, the calibration voltages are selected to match the physical characteristics of the well-defined pressuresignature, resulting significantly reduced inaccuracy and consistent calibration coefficients.

for the With curve-fit inaccuracies individual calibrations reduced to a second order effect, valid comparisons among the calibrations could be made. These comparisons revealed random pressure variations occurring simultaneously on all ESP modules, indicating a common, external bias. The magnitude of the bias uncertainty was evaluated using data from fourteen calibration repeats acquired over a 2-week period. bias uncertainty was found to be 0.020 psi, which is four times the quoted uncertainty of the calibration-pressure working standard (0.005 psi).

The process just described is the first of several such cycles required to achieve statistical process control of electronicallyscanned pressure measurements instrumentation. This preliminary calibration data base revealed several problems, corrective action was taken, and an assessment of the results was made. The next cycle is to reexamine this measurement process in the laboratory under more controlled conditions and to implement improved procedures and methods in the wind tunnel environment. The resulting product will be quality wind tunnel pressure data.

Acknowledgments

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TABLES

Module Number	Range (psi)	Number of Ports	Full-Scale Uncertainty
1	2.5	48	+/- 0.1%
2	5.0	48	+/- 0.05%
3	15.0	48	+/- 0.05%
4	15.0	48	+/- 0.05%
5	0.36	32	+/- 0.1%
6	0.36	32	+/- 0.1%
7	0.36	32	+/- 0.1%
Total		288	

Table 1.- Electronically-scanned pressure modules used with manufacture-specified, full-scale uncertainty specifications.

Module	Range (psi)	A ₁	A ₂	A ₃	A ₄	SE	SE/Range (%)
5	0.36	0.0437	0.1032	0.0445	0.0022	0.0003	0.095
1	2.5	0.2241	0.0141	0.5334	0.0083	0.0017	0.069
2	5	0.4092	-0.1422	1.1388	0.0072	0.0035	0.070
3	15	0.6676	-0.5038	3.5211	0.0026	0.0035	0.024

Table 2.- Typical fitting function coefficients for curves in Figure 6.

No. Pts	Pts Used	Std Error	V _o	A ₁	A ₂	A ₃	A4
22	all	0.00178	.03596	.12130	11864	3.51447	00114
8	1, 3, 7, 11, 12, 15, 19, 22	0.00174	.03600	.13960	14791	3.52571	00195
7	1, 3, 11, 12, 15, 19, 22	0.00193	.03601	.14657	15765	3.52859	00214
6	1, 3, 11, 15, 19, 22	0.00232	.03601	.14500	15397	3.52654	00193
5	1, 11, 13, 19, 22	4x10 ⁻⁷	.03595	.08036	05771	3.49379	.00059
5	1, 11, 14, 19, 22	3x10 ⁻⁷	.03596	.08138	05933	3.49439	.00055
5	1, 11, 15, 19, 22	1x10 ⁻⁷	.03599	.11311	11003	3.51313	00092

Table 3.- Effect of number of fitting points on calibration coefficients.

ESP No.	FS (psi)	Avg A ₁	Avg A₂	Avg A₃	Avg A ₄	SD A1	SD A₂	SD A ₃	SD A ₄
5	0.36	0.0482	0.0972	0.0464	0.0020	0.0236	0.0284	0.0082	0.0006
6	0.36	0.0380	0.1106	0.0445	0.0024	0.0123	0.0159	0.0041	0.0004
7	0.36	0.0586	0.0893	0.0513	0.0023	0.0285	0.0370	0.0102	0.0010
1	2.5	0.2518	-0.0277	0.5561	0.0060	0.0230	0.0333	0.0176	0.0016
2	5	0.4115	-0.1416	1.1378	0.0077	0.0178	0.0264	0.0213	0.0014
3	15	0.6889	-0.5285	3.4951	0.0034	0.0141	0.0172	0.0555	0.0011
4	15	0.6545	-0.5133	3.5129	0.0041	0.0125	0.0152	0.0686	0.0020

Table 4.- Variation of calibration coefficients within a module.

Figures

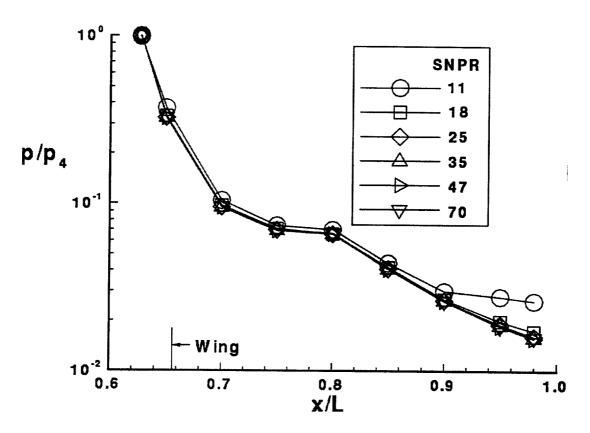
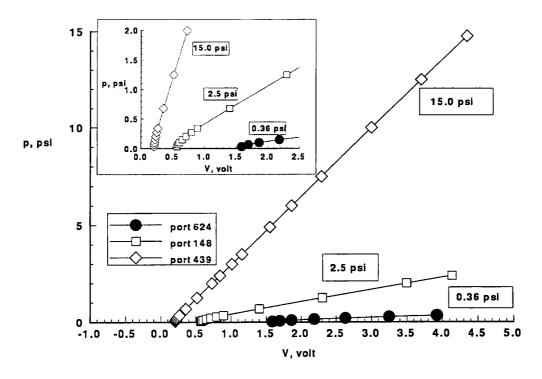
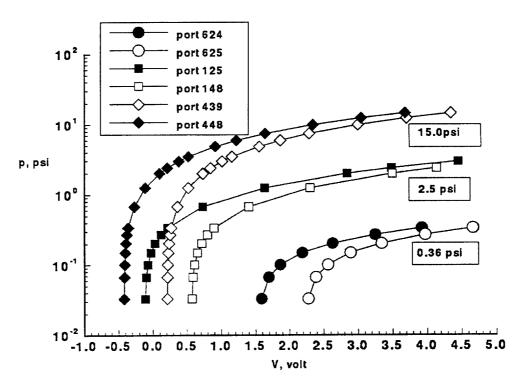


Figure 1.- Effect of static nozzle pressure ratio (SNPR) on external, centerline, nozzle pressure ratio on a generic hypersonic propulsion simulation model.



a. Linear scale.



b. Logarithmic scale.

Figure 2.- Typical electronically-scanned pressure system calibration data.

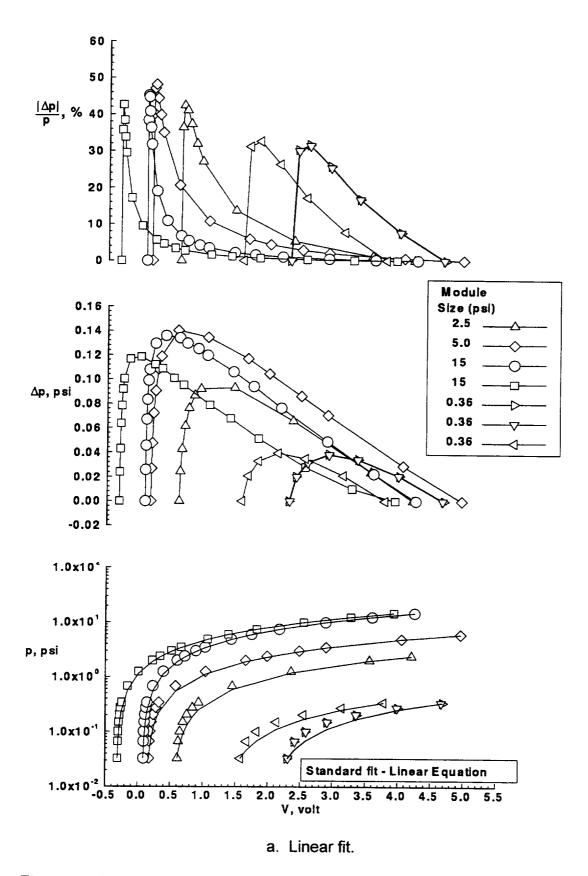
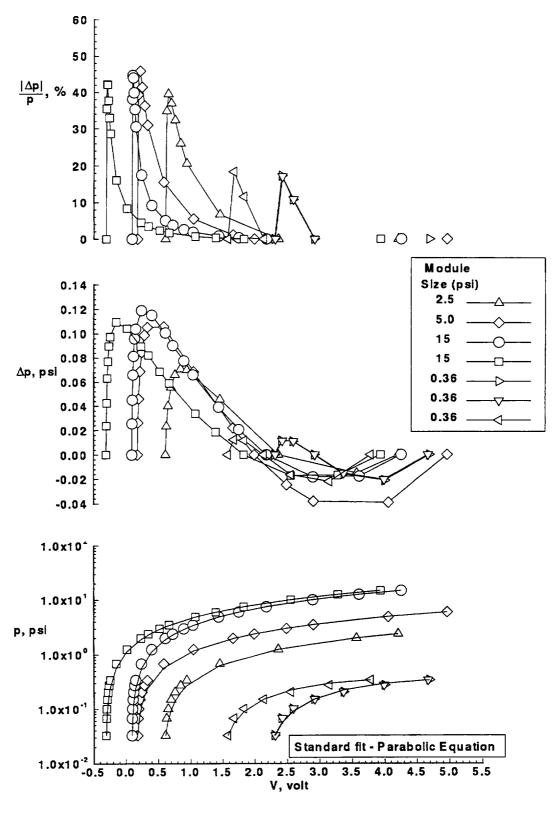


Figure 3.- Standard ESP calibration method using polynomial curve fitting.



b. Parabolic fit.

Figure 3.- Continued.

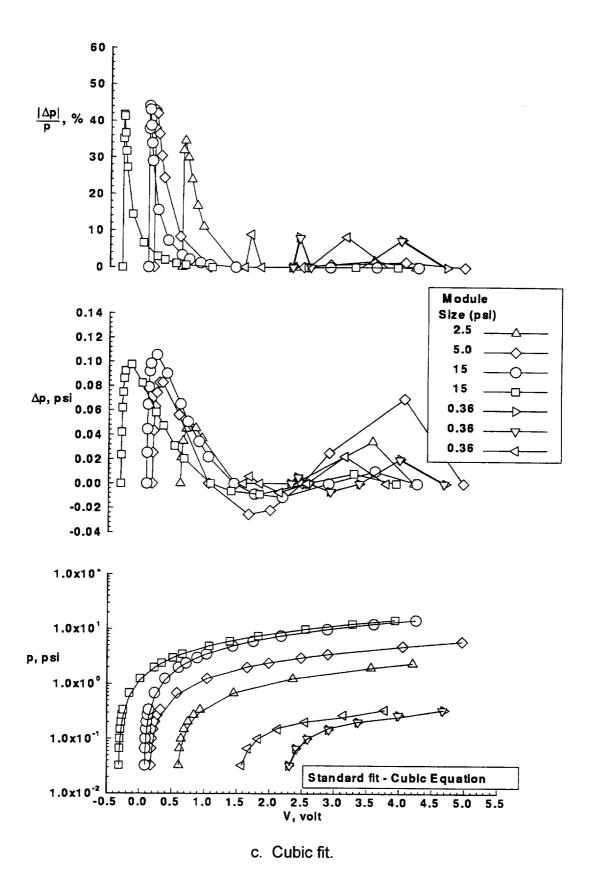


Figure 3.- Continued.

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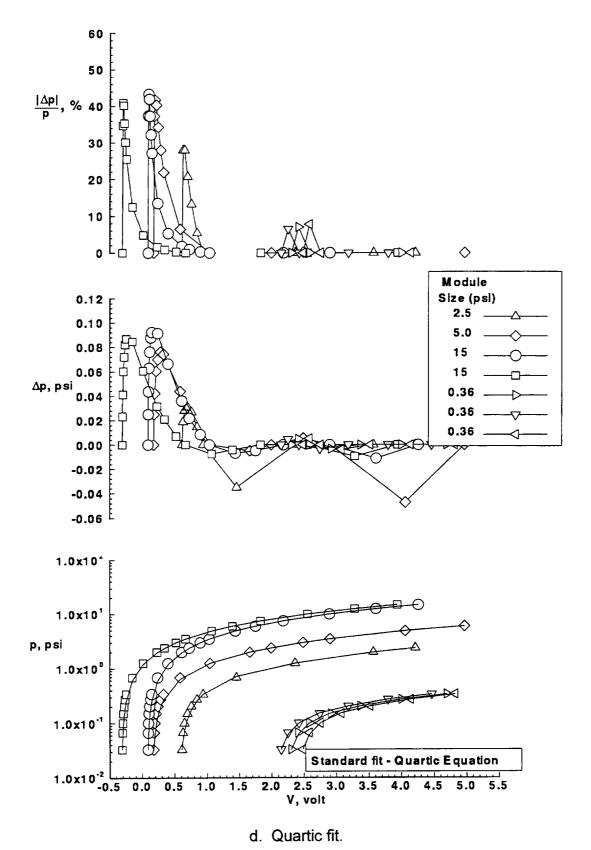
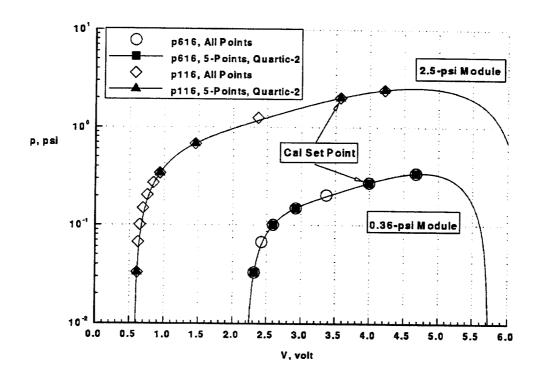


Figure 3.- Concluded.



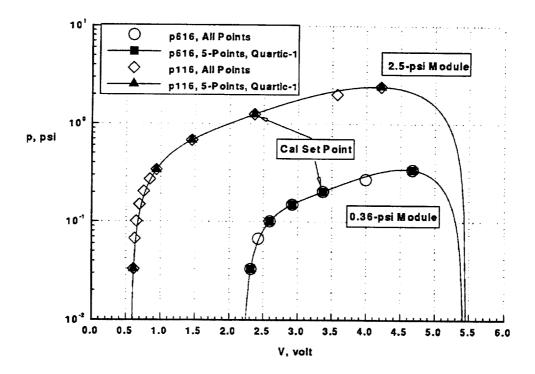


Figure 4.- Effect of calibration pressure location on standard-method ESP calibration curve.

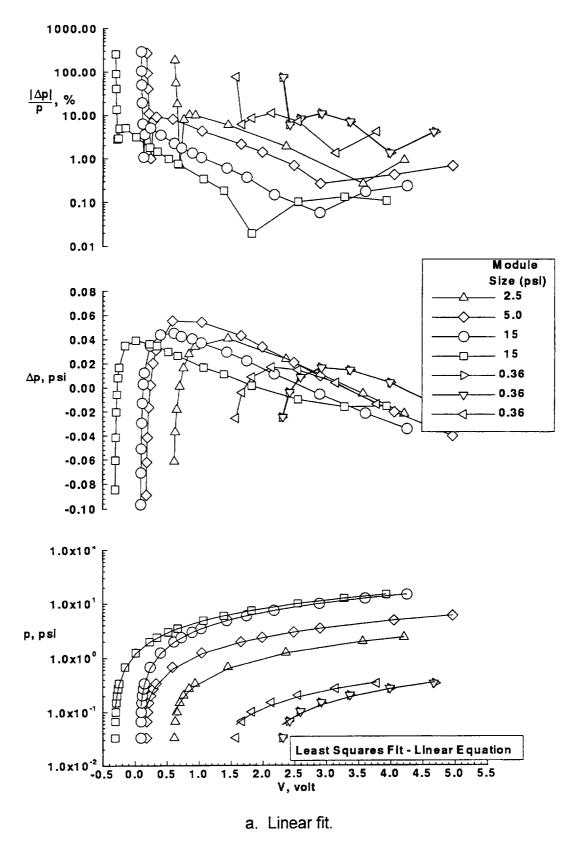
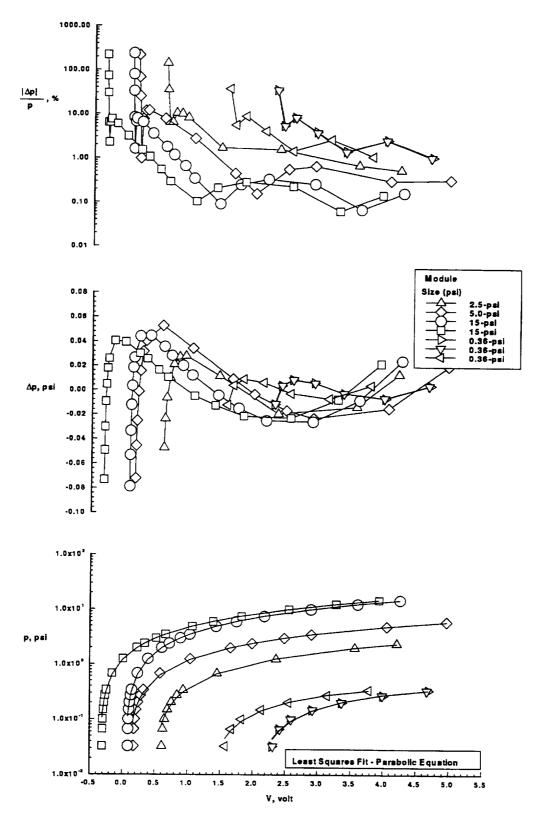


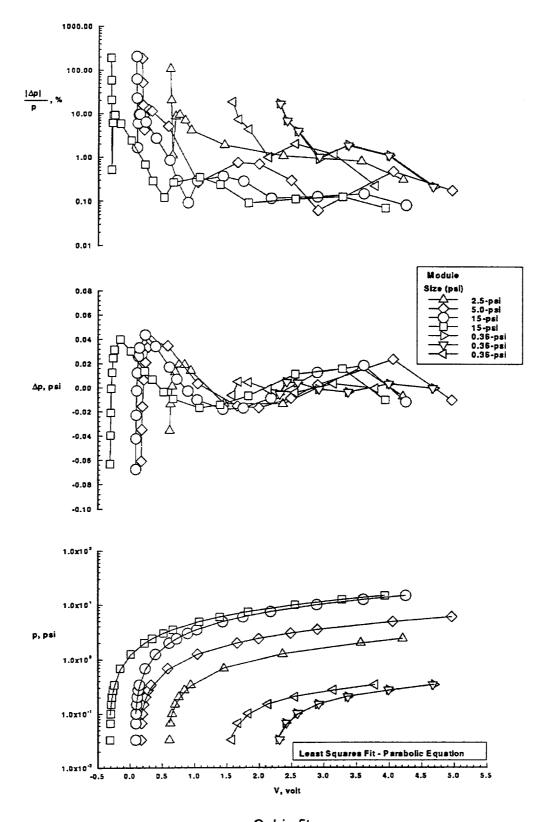
Figure 5.- ESP calibration method using method of least squares fitting.



b. Parabolic fit.

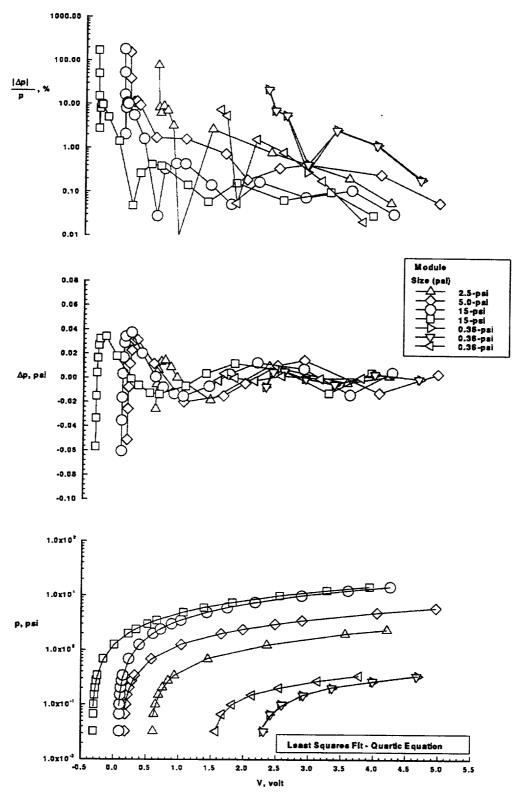
Figure 5.- Continued.

22



c. Cubic fit.

Figure 5.- Continued.



d. Quartic fit.

Figure 5.- Concluded.

24

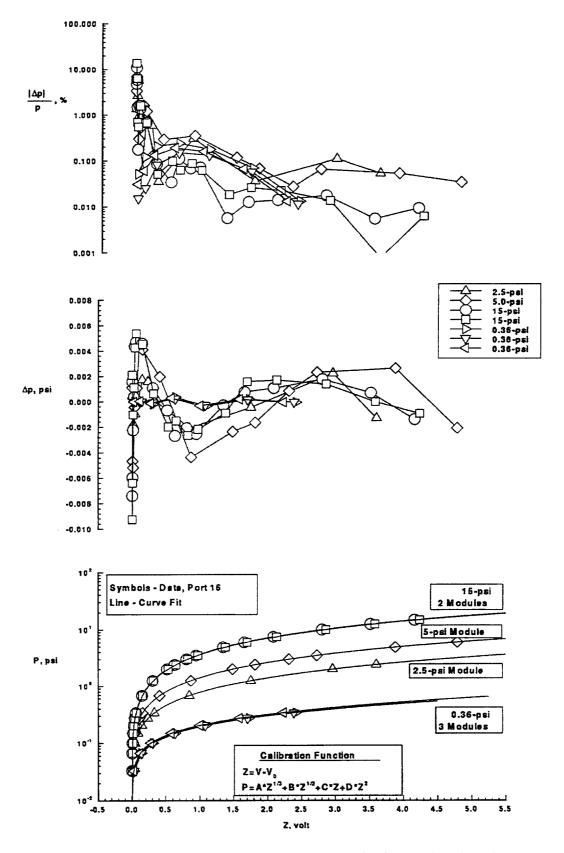


Figure 6.- Improved functional representation of ESP calibration data.

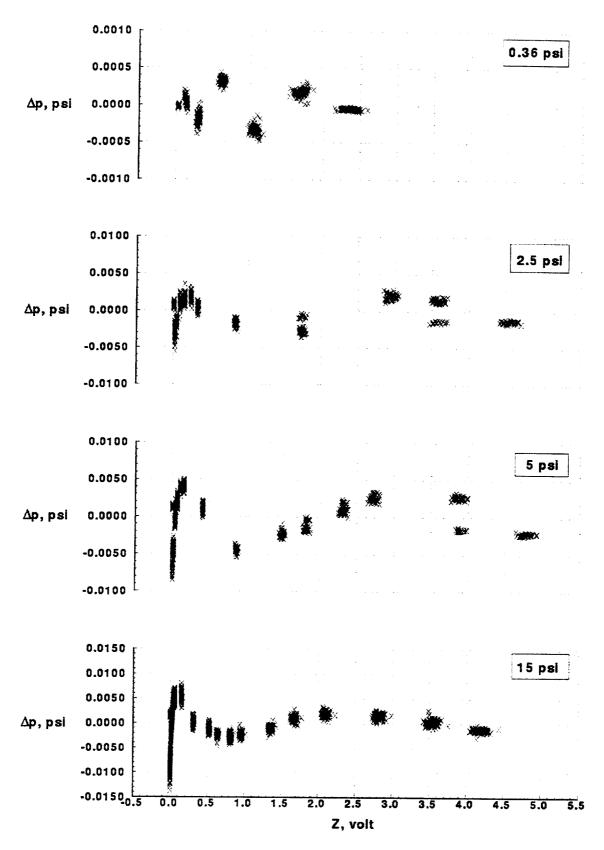


Figure 7.- Improved-method residual error distribution for all module ports.

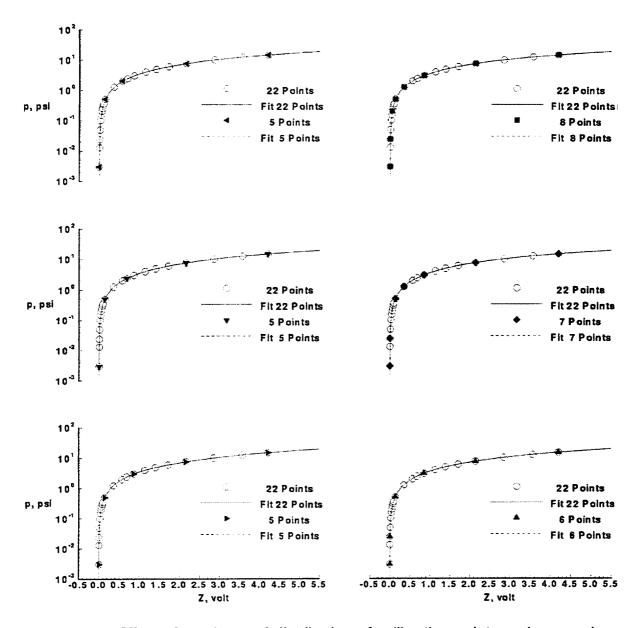


Figure 8.- Effect of number and distribution of calibration points on improvedmethod calibration curves.

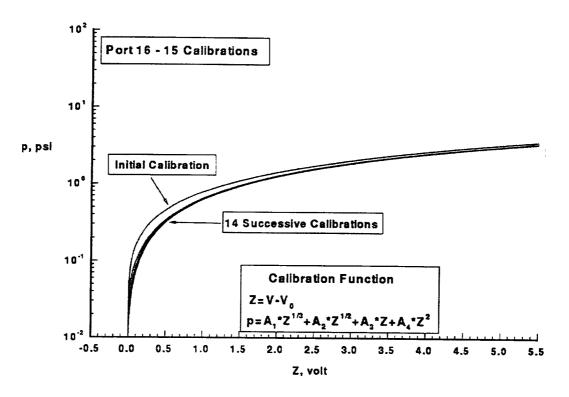
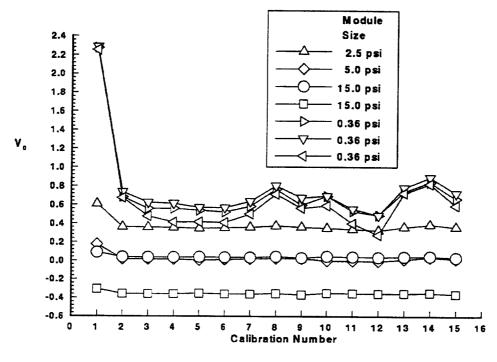
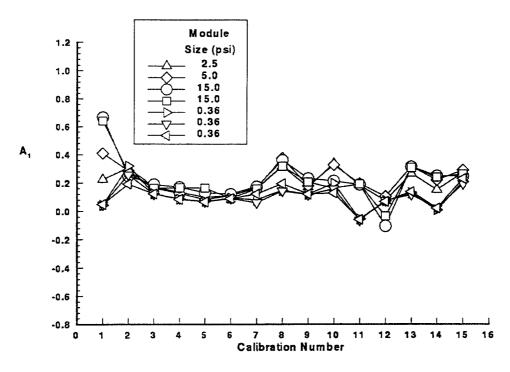


Figure 9.- Comparison of improved-method calibration curves, 2.5-psi module.



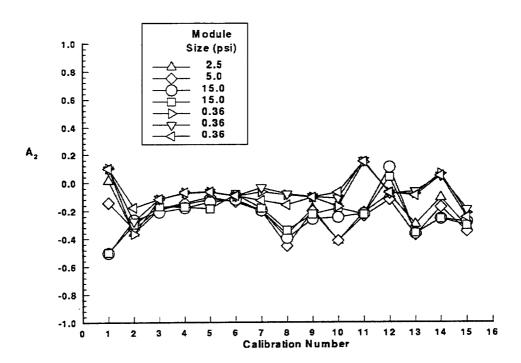
a. Zero-pressure offset voltage, V₀.

Figure 10.- Historical variation of zero-pressure offset voltage and calibration coefficients.



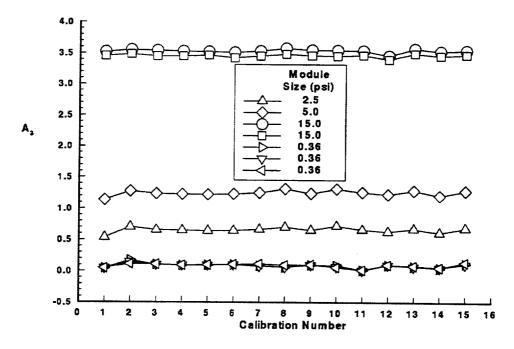
b. Coefficient A₁.

Figure 10.- Continued.



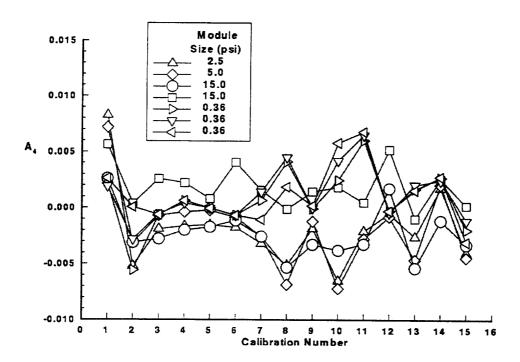
c. Coefficient A₂.

Figure 10.- Continued.



d. Coefficient A₃.

Figure 10.- Continued.



e. Coefficient A₄.

Figure 10.- Concluded.

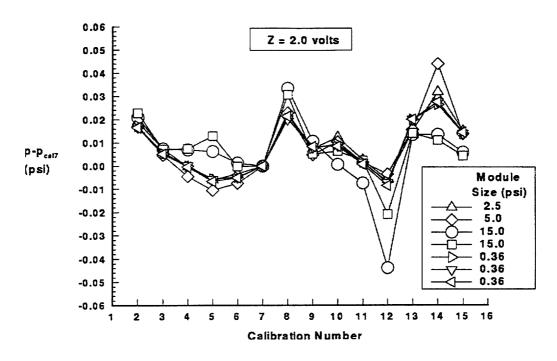


Figure 11.- Historical variation of incremental ESP calibration curves at Z=2.0 volts.

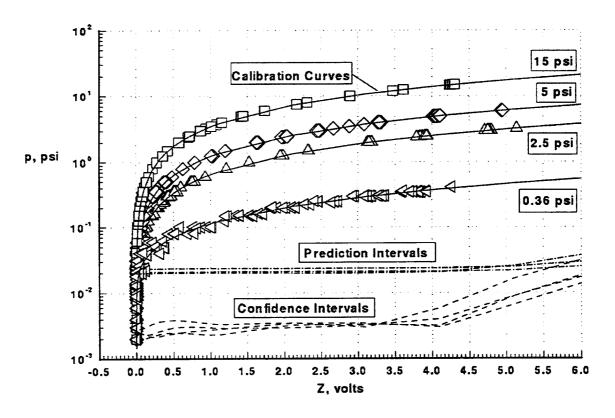


Figure 12.- Confidence and prediction intervals for all pressure ranges.

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