

NASA Technical Memorandum 107285  
AIAA-96-2582

# A Performance Comparison of Two Small Rocket Nozzles

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Prepared for the  
32nd Joint Propulsion Conference  
cosponsored by AIAA, ASME, SAE, and ASEE  
Lake Buena Vista, Florida, July 1-3, 1996



National Aeronautics and  
Space Administration



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## Abstract

An experimental study was conducted on two small rockets (110N thrust class) to directly compare a standard conical nozzle with a bell nozzle optimized for maximum thrust using the Rao method. In large rockets, with throat Reynolds numbers of greater than  $1 \times 10^5$ , bell nozzles outperform conical nozzles. In rockets with throat Reynolds numbers below  $1 \times 10^5$ , however, test results have been ambiguous. An experimental program was conducted to test two small nozzles at two different fuel film cooling percentages and three different chamber pressures. Test results showed that for the throat Reynolds number range from  $2 \times 10^4$  to  $4 \times 10^4$ , the bell nozzle outperformed the conical nozzle. Thrust coefficients for the bell nozzle were approximately 4 to 12 percent higher than those obtained with the conical nozzle. As expected, testing showed that lowering the fuel film cooling increased performance for both nozzle types.

## Introduction

Future space exploration will require increasing payload fraction and decreasing system masses. Therefore, maximizing rocket engine performance is an important design goal. Maximizing the thrust for a rocket engine can be achieved by optimizing the nozzle contour. Optimizing the performance of finite length nozzles is typically accomplished using an inviscid core flow and a boundary layer displacement. G.V.R. Rao developed a method which optimizes a rocket nozzle contour for a given length or expansion ratio such that maximum thrust is achieved.<sup>1</sup> Rao's method was based on the assumption of inviscid isentropic flow.

This method has been used in many studies of different classes of rocket engines with a variety of results. Rocket engines are generally classified by their throat Reynolds number based on uniform flow and properties at the throat. For engines with Reynolds numbers larger than  $1 \times 10^5$ , the Rao optimization is quite effective, because the ratio of boundary layer flow to the total flow is small. In a study by Farley,<sup>2</sup> three large Rao optimized bell nozzles were compared to a 15 degree conical nozzle. The thrust produced by the optimized nozzles was greater than that obtained with the conical nozzle. In fact, bell contour

nozzles have been used routinely for many years in large liquid rocket engines.<sup>3,4,5</sup> Conical nozzles are typically used only when fabrication and design costs outweighed performance.

In very small thrusters with Reynolds numbers less than  $1 \times 10^4$ , viscous boundary layer effects are large in comparison to the total flow and a bell contour is not nearly as effective, as discussed in a pair of experimental studies.<sup>6,7</sup> In these studies, a variety of small nozzles were tested to determine the effect of contour, propellant, expansion ratio, and Reynolds number on performance. Normally, factors in performance loss are divergence, boundary layer effects, and heat transfer effects to the walls. By using ambient temperature gas, the heat transfer effect was eliminated in both studies. The nozzles were conical, trumpet, and Rao optimized bell contours. One paper concluded that the difference in contours had no effect on either divergence or viscous losses.<sup>6</sup> The other concluded the bell contour had the lowest performance of the nozzles tested.<sup>7</sup> The reasons given in both were that the viscous effects of boundary layer were so large that an inviscid isentropic assumptions were not valid.

For rockets that are sized between the very small and large ones the usefulness of the Rao optimization code is less clear. Investigations on a gaseous hydrogen/oxygen engine were

performed by M.A. Appel with different nozzle contours in the 134 to 445 N thrust class.<sup>8</sup> A rhenium 80 percent bell nozzle, a regeneratively cooled nozzle, and a stainless steel 18 degree half angle conical nozzle were each tested using the same injector in this effort. The stainless steel nozzle was built to verify injector and thrust stand operation prior to testing the other two nozzles. The regeneratively cooled nozzle had different dimensions for a different aspect of the study, but the conical and bell nozzles had the same length, exit area and expansion ratio. Unexpectedly, the test results showed that the conical nozzle provided a higher specific impulse than the bell nozzle. The author postulated that the conical nozzle operated with a higher kinetic efficiency and suggested this as an area for further investigation. Kushida<sup>9</sup> examined a 22 N monopropellant hydrazine thruster with a 100:1 area ratio conical nozzle, a 300:1 Rao optimized bell, and the same bell nozzle cut off at expansion ratios of 200:1 and 100:1. Results showed that the 300:1 bell nozzle outperformed the conical chamber but the conical was the better performer than the lower area ratio bell nozzles. A direct comparison was difficult, however, because several dimensions were changed in addition to the nozzle contours. Both the length and expansion ratio were greater for the optimized nozzle, which generally improves performance in a rocket engine. Based on the ambiguous results reported to date, the validity of the Rao nozzle optimization method is uncertain for thrusters with Reynolds numbers between  $1 \times 10^4$  and  $1 \times 10^5$ .

In the study reported herein, testing was performed to directly evaluate the applicability of Rao optimization methods to rockets with Reynolds numbers below  $1 \times 10^5$ . The performance of two 110 N chamber/nozzles with throat Reynolds numbers between  $2 \times 10^4$  and  $4 \times 10^4$  was measured to examine the effect of nozzle contour on performance in this intermediate Reynolds number range. Both nozzles were designed with the same chamber profile, throat diameter, and expansion ratio. Because the chamber and nozzle are one continuous structure, each piece of hardware is simply identified by the nozzle shape, ie. bell or conical, from here on. The conical nozzle had a 19 degree expansion half angle. This rocket was originally tested in 1993.<sup>10</sup> The bell nozzle was designed via the Rao code. As part of the effort, a one dimensional equilibrium code, ODE, was used to generate theoretical performance predictions to calculate the characteristic velocity efficiencies presented later in this study.<sup>11</sup>

## Test Hardware

Both nozzles tested were fabricated via the same techniques using oxygen free high conductivity (OFHC) copper with water cooling passages in the walls. The inner housings were milled first to cut water cooling passages into the outer surface. The chamber profiles were identical from the injector face to the throat. The contours of the nozzles are shown in figures 1(a) and (b), and further details of the bell nozzle contour are given in

table I. The divergence angle of the conical nozzle was about 19 degrees and the divergence angle of the bell nozzle was about 9 degrees at the exit plane. The design specified throat area was  $1.267 \text{ cm}^2$ . Post fabrication measurements of the chamber, throat, and exit gave dimensions that were very similar as shown in table II. The resulting dimensional differences based on area were 0.10 percent at the chamber, 2.2 percent at the throat, and 0.14 percent at the nozzle exit.

The outer housing of each nozzle was machined in two pieces separated along the thruster axis. The sections fit around the inner housing as a shell to insure the interior contour was one continuous profile from chamber inlet to nozzle exit. The outer housing halves were attached to each other with bolts around the inner housing. All seams were filled with high temperature solder. Both chambers were instrumented with thermocouples and pressure taps in several quadrants along the contour.

The same injector,<sup>12</sup> shown schematically in figure 2, was used in all testing. The injector was designed to produce a core flow of combustion products with an annulus of fuel film cooling (FFC). In the core, oxygen was injected through a platelet stack into the combustion chamber just upstream of a spark plug used for ignition. The hydrogen flow was divided by means of a fuel splitting washer, with part injected downstream of the spark plug into the core and the rest used to fuel film cool the chamber wall. The washer was specifically designed to give a predetermined fuel film cooling split from the total fuel flow. The film cooling was directed along the chamber walls by an annular sleeve. By changing the washer, the amount of film cooling could be varied between 55 to 85 percent. A 61 percent FFC percentage was selected as the baseline for this study since that was nominal design operating point for this injector. Tests at 75 percent FFC were also run to investigate the sensitivity to FFC changes.

## Test Facility

All tests were conducted in a small rocket test facility,<sup>13</sup> in which an equivalent vacuum of 36.6 km altitude is achieved using air ejectors. Gaseous hydrogen and gaseous oxygen were used for propellants. A schematic is shown in figure 3. The tank is 1.8 m long between the flanges and 0.9 m in diameter. Inside the tank, the rockets are oriented horizontally to fire through a diffuser into an exhaust quenching chamber. The rocket exhaust is pulled through the pair of ejectors and vented to atmosphere by mufflers. The ejectors are supplied with 900 kPa air at 4.5 kg/sec to provide the pumping for the altitude tank.

Thrust is measured by mounting the rocket on a thrust stand. The stand and rocket are supported with flexure plates. Both float free on the flexures and apply a load to a strain gage load cell through a ball joint. To ensure accurate thrust calibration, the ball joint must make contact with the load cell at all times. The thruster is positioned to apply a small load on the load cell

even when the thruster is not firing, to ensure contact with the load cell is maintained. The small load is accounted for in thrust calibration and is subtracted from the rocket thrust. The propellant and pressure transducers lines are mounted perpendicular to the rocket axis with stainless steel tubing to provide repeatable thrust measurements. The thrust stand is calibrated by applying loads through a piston assembly to compare the thrust measurement load cell against another previously calibrated reference load cell. Pretest, posttest, and applied load tests are taken at altitude conditions with pressurized propellant lines. All thrust measurements are corrected for background pressure to determine vacuum thrust.

## Rao Optimization Code

Rao discussed the need for nozzle contour optimization.<sup>14</sup> In order to maximize thrust, a thruster is designed to produce uniform parallel exit flow, with the exit plane pressure equal to the ambient pressure. In a conical nozzle, flow divergence losses are significant, particularly as cone angles increase. Rao suggested that contouring the nozzle wall would turn the flow closer to the thruster axis and thus reduce flow divergence. He developed an optimization method for designing nozzles which assumes inviscid isentropic flow.<sup>15</sup> The method uses the calculus of variations for an ideal gas with constant gamma expansion to calculate the optimum nozzle contour. Supersonic flow properties across the nozzle throat are input to start the solution. Transonic flow in the throat region is calculated as a function of the upstream radius of curvature at the throat and the specific heat ratio for axisymmetric flow. The method iterates to an optimum nozzle contour defined to meet for one of three initial conditions: a given length, a given expansion ratio, or a fixed envelope (exit radius and length). The Rao code was used in this study to obtain an optimized bell nozzle contour with the dimensions shown in table I using the fixed envelope condition.

## Test Procedures

The same tests were conducted on each nozzle using gaseous hydrogen and oxygen propellants. Tests were conducted at three different chamber pressures, 500, 370, 255 kPa, and two FFC percentages, 61 and 75 percent, over a mixture ratio range of 4 to 8. The design condition for the rocket hardware was 500 kPa with 61 percent FFC. The higher FFC percentage and the lower chamber pressures were chosen to allow testing through a throat Reynolds number range of  $2 \times 10^4$  to  $4 \times 10^4$ . The throat Reynolds number ( $Re$ ) range was calculated using the equation

$$Re = \frac{4\dot{m}}{\pi\mu D_t}$$

where  $\dot{m}$  is the mass flow rate of the propellants,  $\mu$  is the absolute viscosity of the combustion products, and  $D_t$  is the diameter of the nozzle throat. The viscosity is determined from theoretical predictions generated by the Gordon-McBride program.<sup>11</sup> The two percent difference in throat areas sometimes resulted in slightly lower chamber pressure in the conical nozzle. A typical test began by pumping the test tank to altitude and pressurizing the propellant lines with fuel. A thrust stand calibration was then performed. After the calibration, a constant load was applied to the thrust stand, which provided data for determining the uncertainties. Once the applied load was removed and inlet pressure conditions at the injector were adjusted, the rocket engine was fired. By modifying the propellant inlet pressures, mixture ratios from 4 to 8 were tested. Once tests were completed for the day, another constant load test and another load cell calibration were conducted.

## Measurement Uncertainties

Measurement uncertainties were calculated using the JANNAF recommended procedure.<sup>16</sup> The uncertainties were calculated from the precision (random) and bias (constant) errors associated with the measurement instruments and data acquisition system. Precision errors propagated through the performance parameters of specific impulse, characteristic velocity, and thrust coefficient are shown in table III. Initial testing with the bell nozzle for the 500 and 370 kPa chamber pressure cases at 61 percent FFC had a very small pretest load (less than 0.5 N) on the thrust stand prior to ignition. Since the thrust stand could float free of the load cell at this load, a larger load was applied prior to ignition to ensure pretest contact between the thruster and the load cell. The low pretest load affected the repeatability of the thrust stand zero. In an effort to ensure that the thrust measurement was not affected by the small pretest load, the pretest load was increased and a few selected points in that test series were repeated. A field check at that time showed performance results consistent with the original tests at the smaller pretest load. However, in subsequent data reductions, the tests with the small pretest load had significantly larger uncertainties. The range of uncertainties for both cases are shown in table III, the cases with the smaller pretest load being indicated by parenthesis. The remainder of the test data uncertainties were also presented in the same table. In general, the greatest uncertainties were at the lower chamber pressures.

## Results and Discussion

### Injector/Chamber Performance

To show that the injector and chamber behaved identically for the two nozzles, the characteristic velocity efficiencies are

plotted in figures 4 and 5 as a function of mixture ratio for tests run at 61 and 75 percent FFC, respectively. The efficiencies were determined by dividing the experimental characteristic velocity by the theoretical equilibrium characteristic velocity predictions.<sup>11</sup> As expected, the plots show no measurable differences in this parameter between the bell and conical nozzles as the injector and chamber profiles are the same. The slight difference in throat area resulted in slightly higher chamber pressures (approximately 1 percent), in the bell nozzle for the same inlet conditions. Clearly the difference did not have a measurable impact on the performance of the injector and chamber, since the characteristic velocities measured with both nozzles fell within the same uncertainty band. The overall efficiency is slightly higher for the 61 percent FFC cases. This was an expected result because more hydrogen is reacted in the core combustion flow at this condition. Similar trends are shown in the plots of characteristic velocity versus mixture ratio (figs. 6 and 7).

## Nozzle Performance

Vacuum specific impulse versus mixture ratio and thrust coefficient versus mixture ratio are typically used to illustrate nozzle performance. The vacuum specific impulse versus mixture ratio for the 61 and 75 percent FFC cases are plotted in figures 8 and 9, respectively, for each of the three chamber pressures tested. The data were fit to a second order polynomial curve and the measurement uncertainties added. At 61 percent FFC (fig. 8), the plots of nozzle data show that the bell nozzle specific impulse are at least 5 percent higher at 500 kPa, 6 percent higher at 370 kPa, and 12 percent higher at 255 kPa than that of the conical for the 61 percent FFC cases. In 75 percent FFC cases (fig. 9) the bell nozzle specific impulse is at least 5 percent higher at 500 kPa, 10 percent higher at 370 kPa, and 14 percent higher at 255 kPa. These results are statistically significant and show clearly that the bell nozzle outperformed the conical nozzle. The higher performance obtained with lower FFC percentage was expected as discussed above.

Thrust coefficients are plotted for the 61 and 75 percent FFC cases in figures 10 and 11, respectively, again for each chamber pressure case. As seen in the specific impulse plots, the bell nozzle had the higher performance for both FFC percentages. The thrust coefficients at 61 percent FFC are generally 6 percent higher at 500 kPa, 7 percent higher at 370 kPa, and 11 percent higher at 255 kPa for the bell nozzle than for the conical. The thrust coefficients at 75 percent FFC are generally 4 percent higher at 500 kPa, 8 percent higher at 370 kPa, and 11 percent higher at 255 kPa for the bell nozzle than for the conical. Again clearly, the bell nozzle outperforms the conical nozzle for this Reynolds number range of between 20,000 to 40,000.

## Conclusions

Testing was conducted to directly compare the performance of a bell nozzle designed by the Rao optimization method and a conical nozzle of the same size in the  $2 \times 10^4$  to  $4 \times 10^4$  throat Reynolds number range. Previous studies had indicated that an optimized bell nozzle may not outperform a conical nozzle at these Reynolds numbers. To eliminate the effects of injector performance, the same injector and chamber profile were used. Tests were conducted over a mixture ratio range of 4 to 8 for three different chamber pressures and two fuel film cooling levels. Characteristic velocity measurements indicated that the injector and chamber gave the same performance with both nozzles. Plots of vacuum specific impulse and thrust coefficients indicated a higher performance by the bell nozzle. Also, higher performance at the lower FFC percentages for both nozzles. For the throat Reynolds number range of this design, the test results confirm that the Rao optimized bell nozzle yields higher performance than a simple conical nozzle design.

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TABLE I.—WALL CONTOUR POINTS FOR RAO NOZZLE BEGINNING AT THROAT TO NOZZLE EXIT

Axial distance, cm	Radial distance, cm	Axial distance, cm	Radial distance, cm
0.000	0.638	1.267	1.349
0.157	0.681	1.359	1.400
0.175	0.691	1.450	1.450
0.203	0.709	1.544	1.501
0.231	0.726	1.623	1.542
0.262	0.744	1.727	1.595
0.295	0.765	1.910	1.687
0.330	0.785	2.217	1.836
0.366	0.808	2.621	2.017
0.404	0.833	2.891	2.129
0.444	0.856	3.152	2.233
0.488	0.884	3.495	2.362
0.533	0.912	3.843	2.487
0.579	0.942	4.280	2.631
0.632	0.973	4.740	2.774
0.686	1.006	5.314	2.936
0.744	1.041	5.928	3.096
0.805	1.080	6.302	3.185
0.871	1.120	6.891	3.315
0.940	1.161	7.534	3.444
1.016	1.204	8.037	3.538
1.095	1.252	8.434	3.607
1.179	1.298	8.989	3.693

TABLE II.—CROSS SECTIONAL AREAS OF THE BELL AND CONICAL NOZZLES

Location	Cross sectional area, cm <sup>2</sup> , cm	
	Bell nozzle, radius	Conical nozzle, radius
Chamber	5.045 (1.268)	5.050 (1.267)
Throat	1.248 (0.637)	1.275 (0.630)
Nozzle exit	42.65 (3.687)	42.70 (3.685)

TABLE III.—PERFORMANCE PARAMETER UNCERTAINTY PERCENTAGES FOR THE BELL AND CONICAL NOZZLES AS A FUNCTION OF CHAMBER PRESSURE

Uncertainty, ± percent		Bell nozzle		Conical nozzle	
		61% FFC	75% FFC	61% FFC	75% FFC
Specific impulse	500 kPa	2.6 (4.0)	2.6	1.1	1.1
	370 kPa	3.3 (6.8)	2.9	1.4	1.5
	255 kPa	5.7	4.6	2.0	1.9
Characteristic velocity	500 kPa	1.2	1.1	1.2	1.1
	370 kPa	1.6	1.4	1.5	1.5
	255 kPa	2.4	2.1	2.0	2.0
Thrust coefficient	500 kPa	2.6 (4.1)	2.6	0.4	0.5
	370 kPa	3.3 (7.0)	2.9	0.7	0.7
	255 kPa	6.0	4.5	1.1	0.9

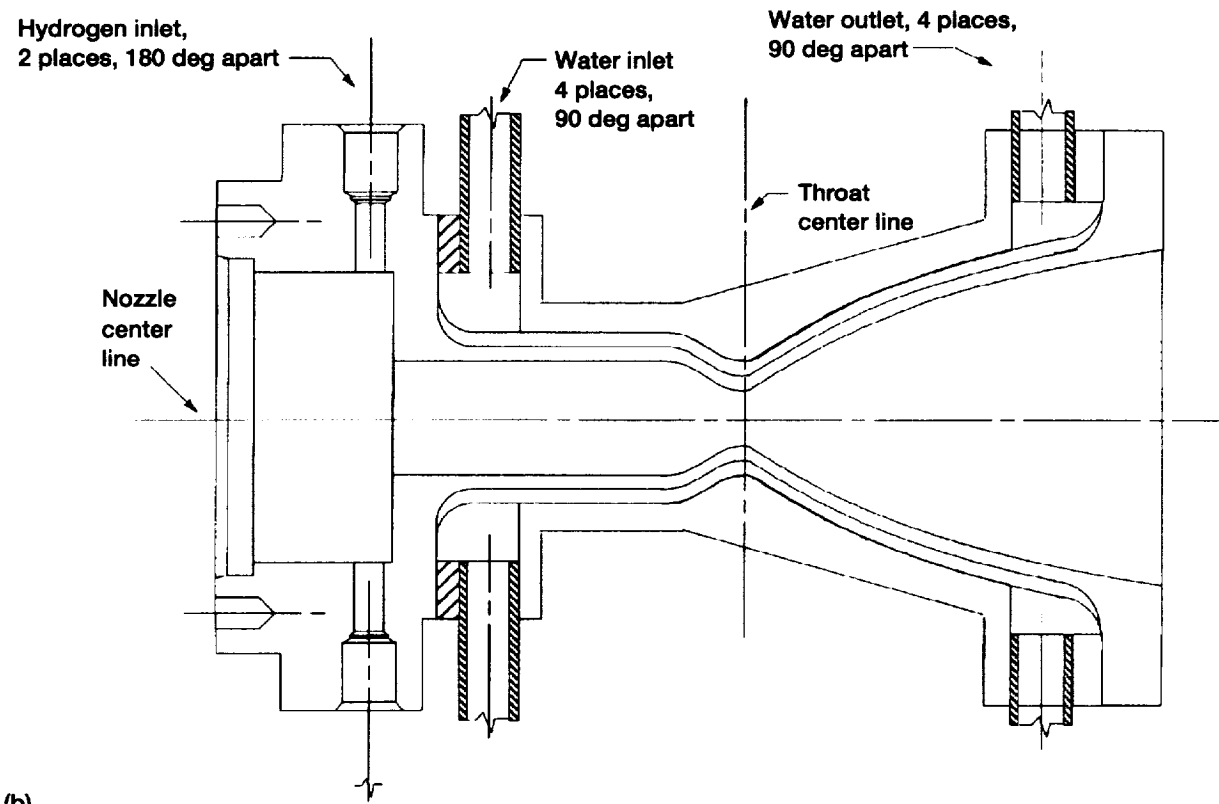
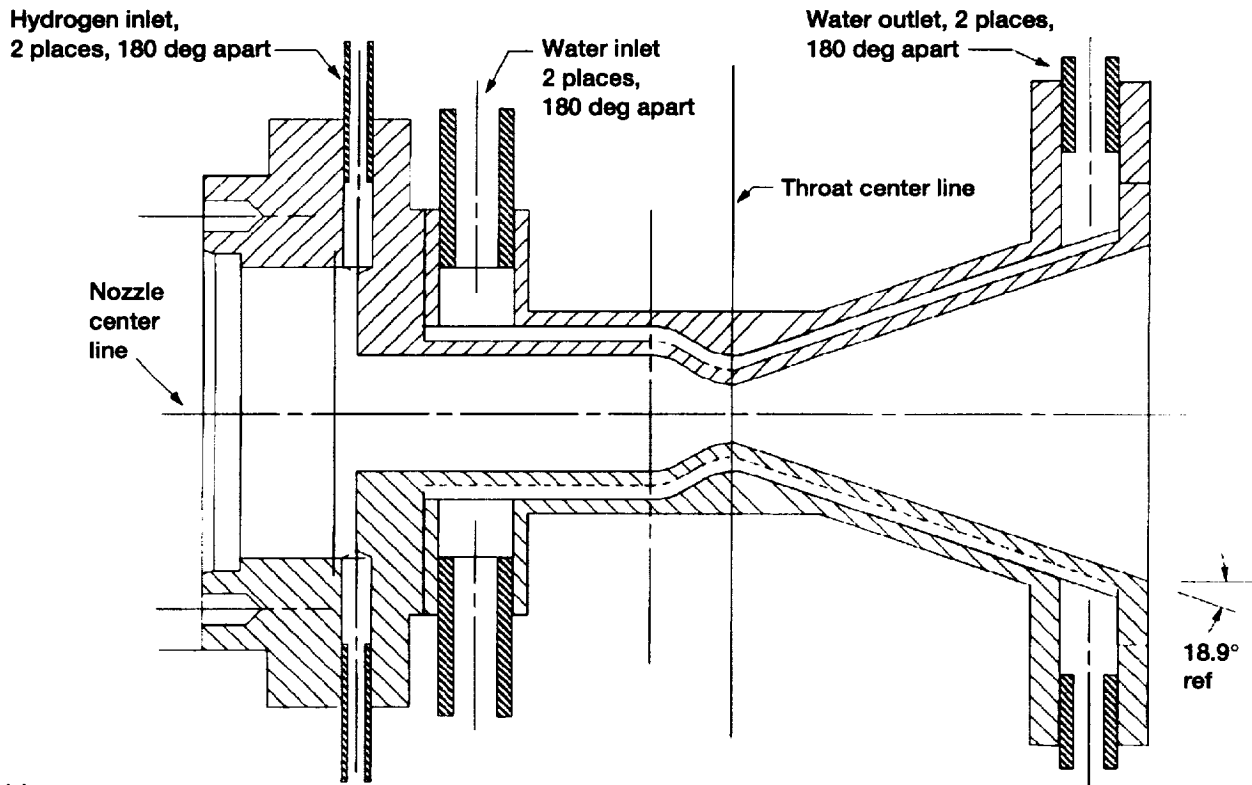


Figure 1.—(a) Schematic of conical nozzle. (b) Schematic of bell contoured nozzle.



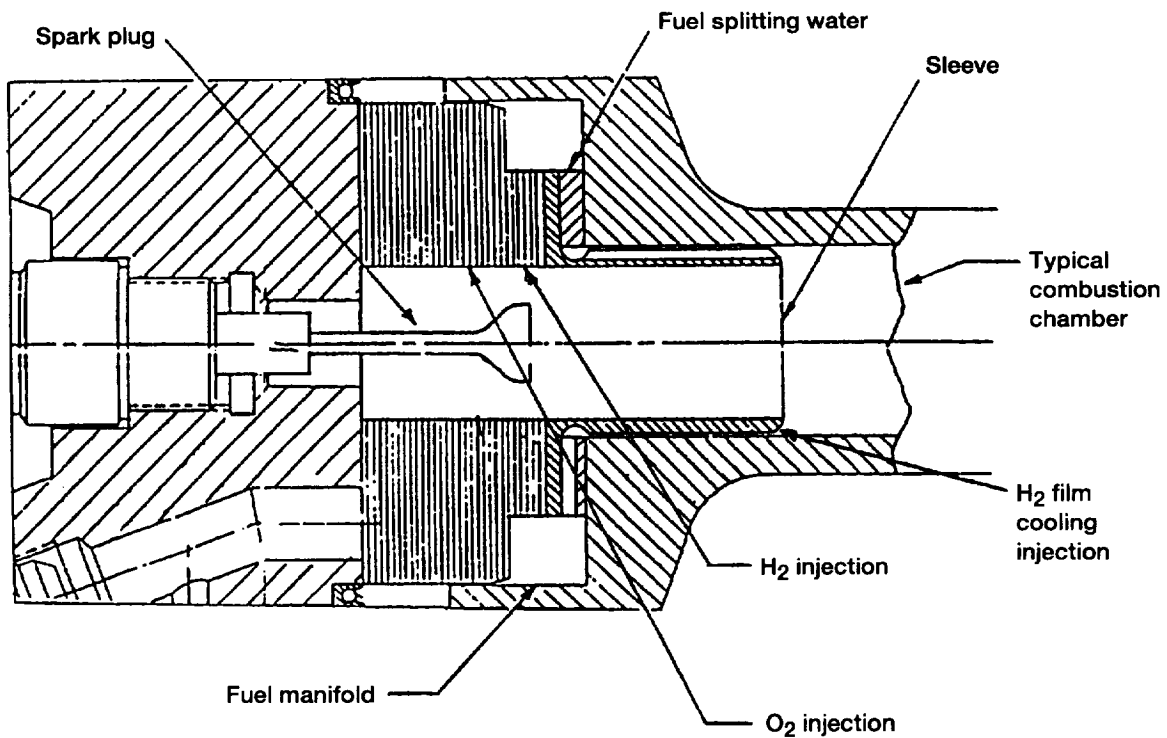


Figure 2.—Details for Aerojet SN 03 injector.

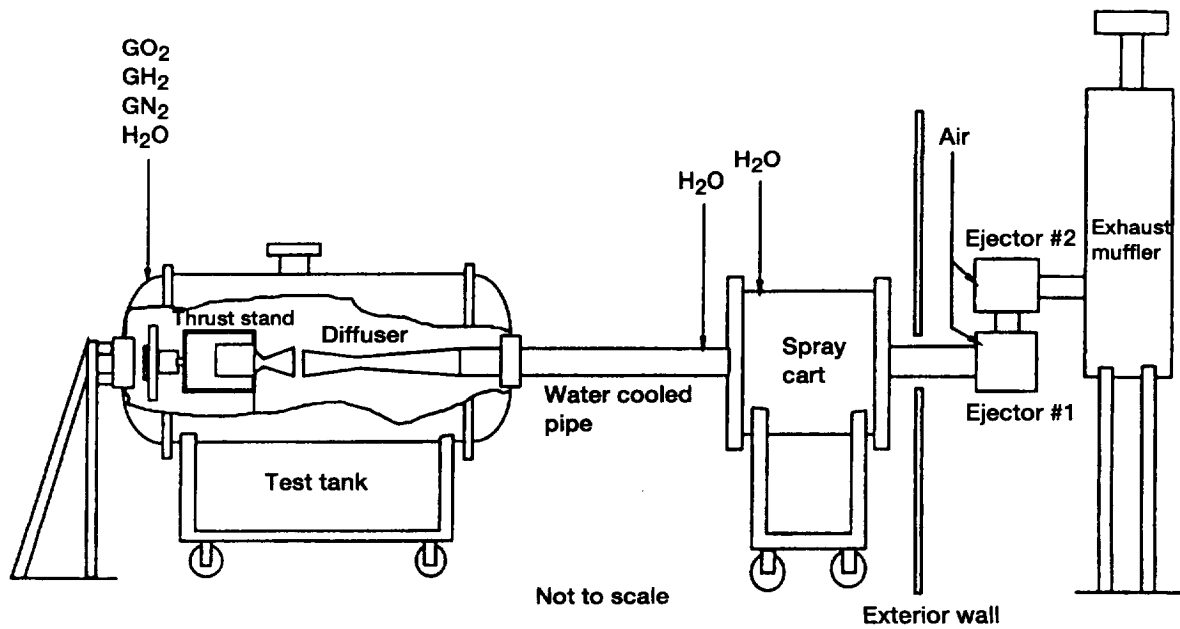


Figure 3.—Schematic of test rig.

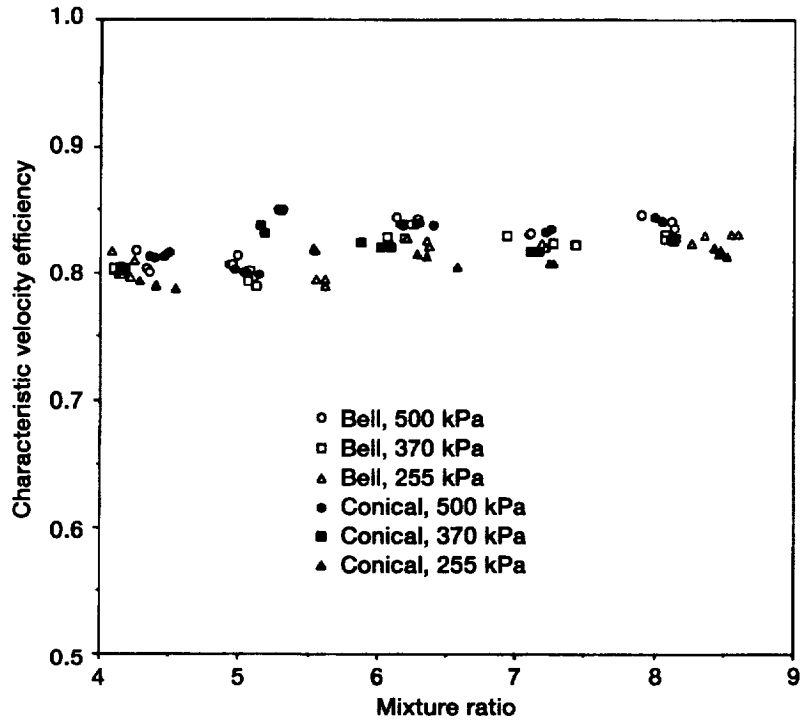


Figure 4.—Characteristic velocity efficiency versus mixture ratio for 61 percent FFC for both bell and conical nozzles.

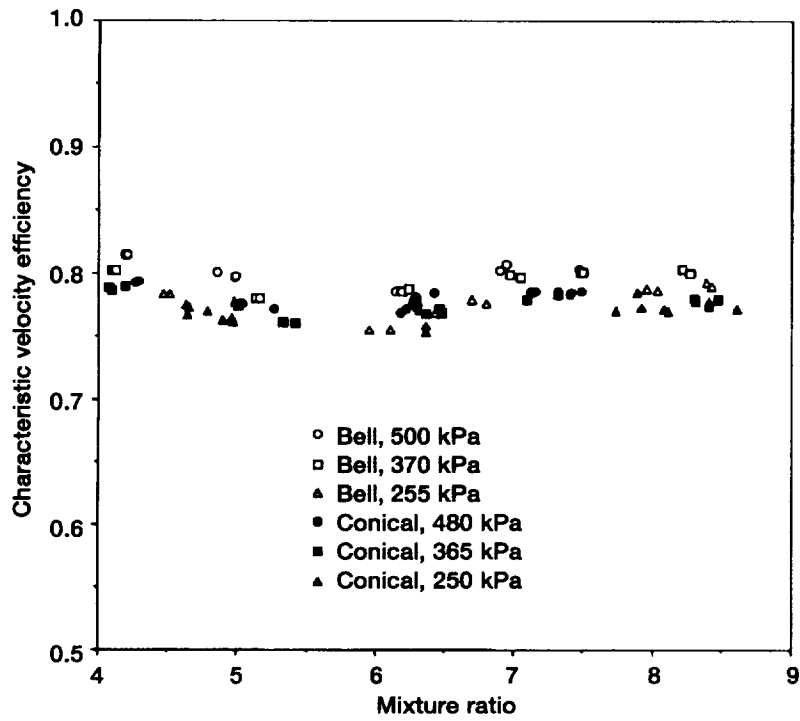


Figure 5.—Characteristic velocity efficiency versus mixture ratio for 75 percent FFC for both bell and conical nozzles.

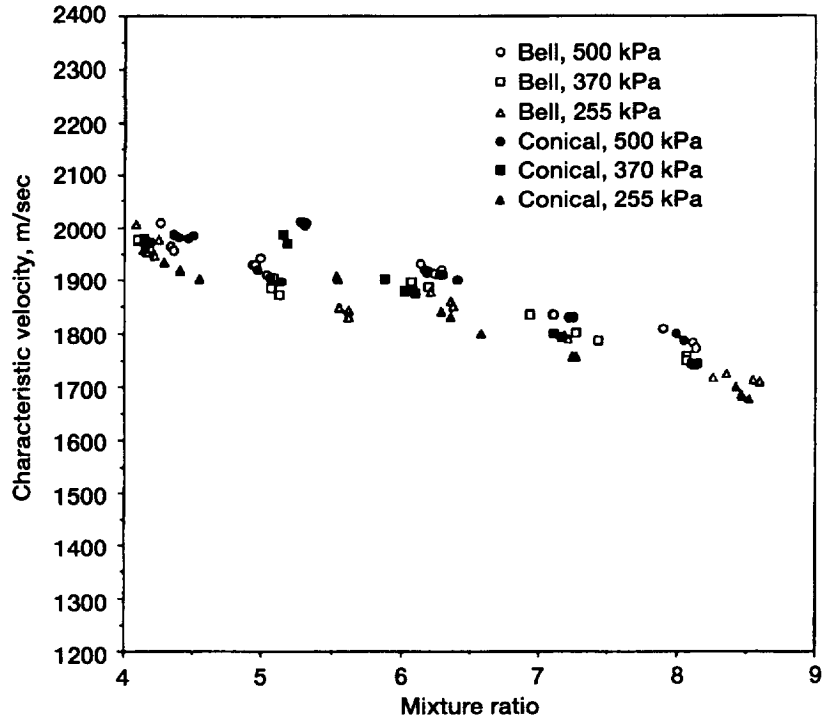


Figure 6.—Characteristic velocity versus mixture ratio for 61 percent FFC for both bell and conical nozzles.

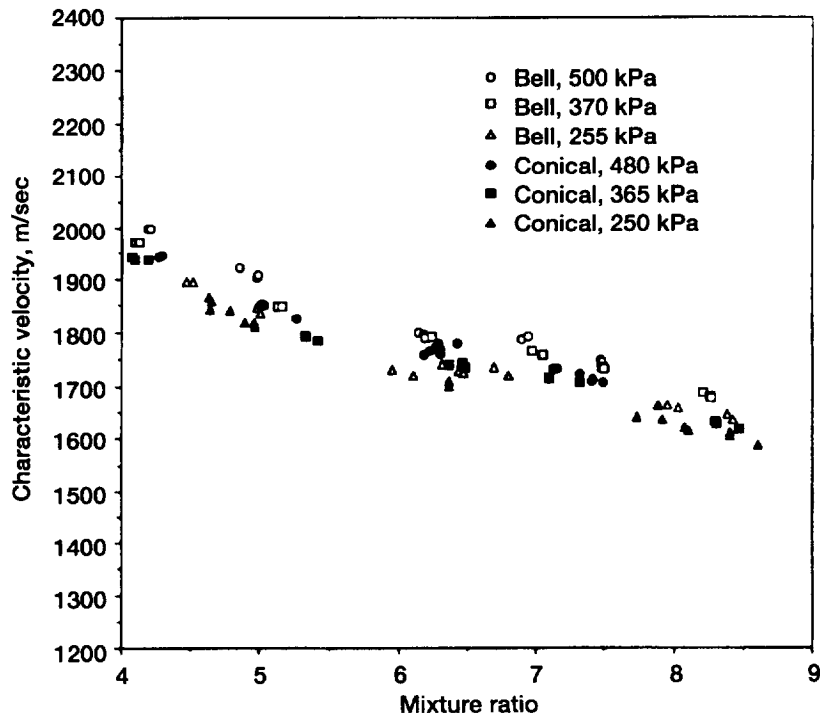


Figure 7.—Characteristic velocity versus mixture ratio for 75 percent FFC for both bell and conical nozzles.

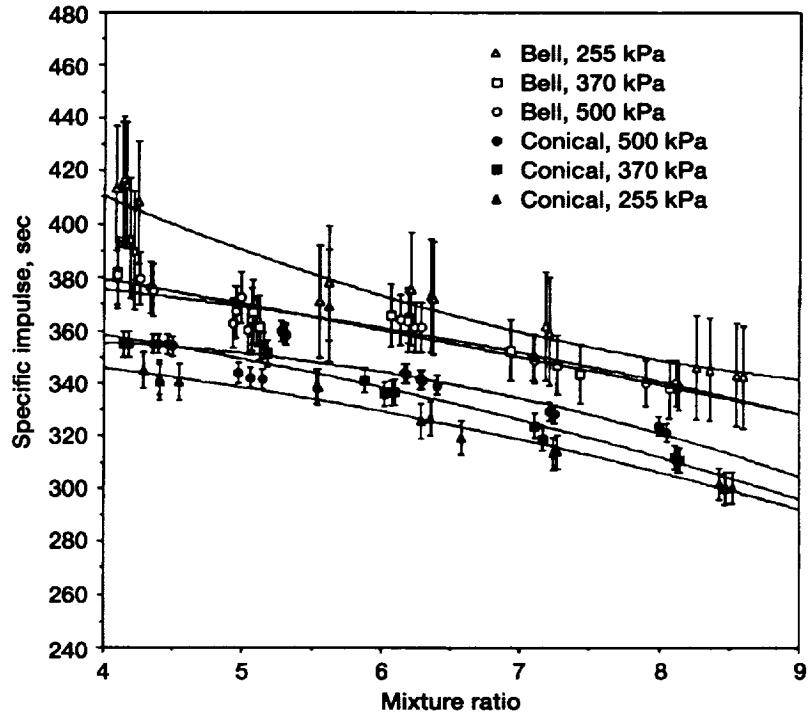


Figure 8.—Specific impulse versus mixture ratio for 61 percent FFC for both bell and conical nozzles, with uncertainty bars.

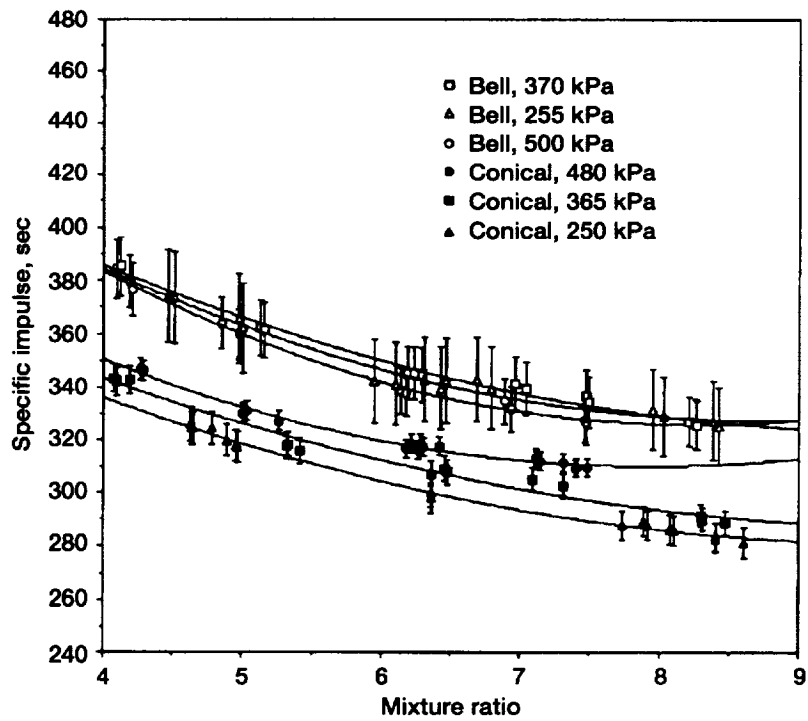


Figure 9.—Specific impulse versus mixture ratio for 75 percent FFC for both bell and conical nozzles, with uncertainty bars.

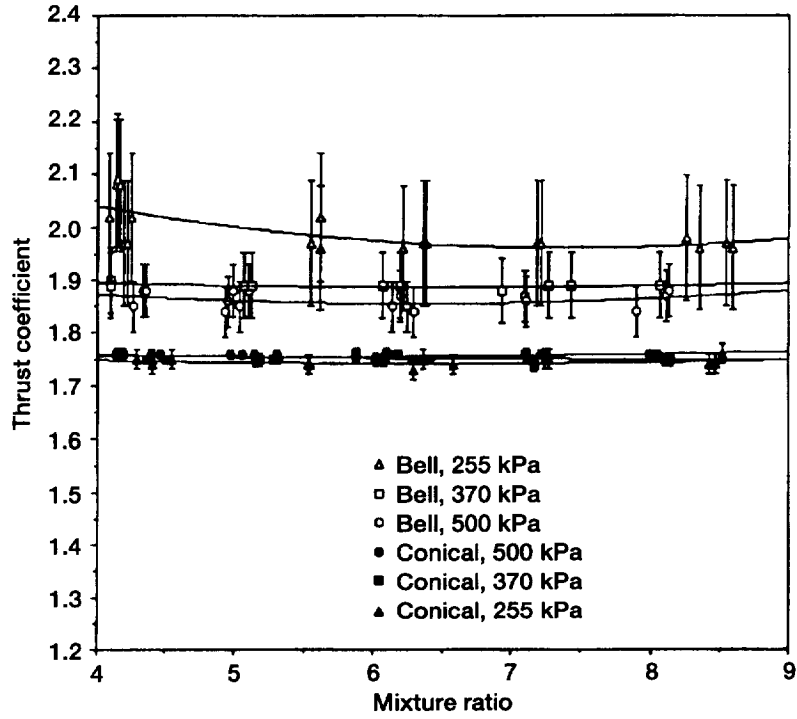


Figure 10.—Thrust coefficient versus mixture ratio for 61 percent FFC for both bell and conical nozzles, with uncertainty bars.

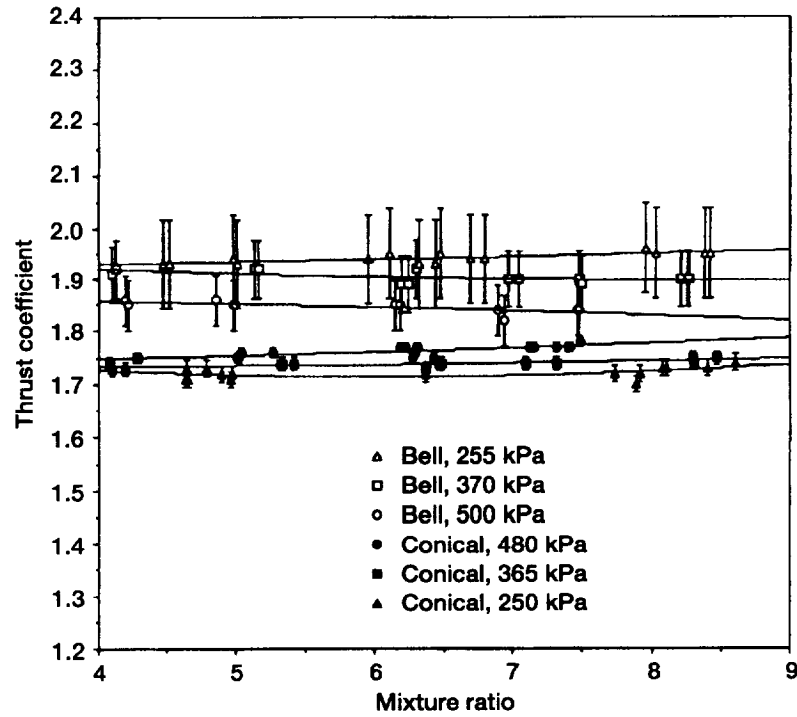


Figure 11.—Thrust coefficient versus mixture ratio for 75 percent FFC for both bell and conical nozzles, with uncertainty bars.

# REPORT DOCUMENTATION PAGE

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<b>1. AGENCY USE ONLY (Leave blank)</b>		<b>2. REPORT DATE</b> August 1996	<b>3. REPORT TYPE AND DATES COVERED</b> Technical Memorandum	
<b>4. TITLE AND SUBTITLE</b>  A Performance Comparison of Two Small Rocket Nozzles			<b>5. FUNDING NUMBERS</b>  WU-242-70-02	
<b>6. AUTHOR(S)</b>  Lynn A. Arrington, Brian D. Reed, and Angel Rivera, Jr.				
<b>7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)</b>  National Aeronautics and Space Administration Lewis Research Center Cleveland, Ohio 44135-3191			<b>8. PERFORMING ORGANIZATION REPORT NUMBER</b>  E-10360	
<b>9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)</b>  National Aeronautics and Space Administration Washington, D.C. 20546-0001			<b>10. SPONSORING/MONITORING AGENCY REPORT NUMBER</b>  NASA TM-107285 AIAA-96-2582	
<b>11. SUPPLEMENTARY NOTES</b>  Prepared for the 32nd Joint Propulsion Conference cosponsored by AIAA, ASME, SAE, and ASEE, Lake Buena Vista, Florida, July 1-3, 1996. Lynn A. Arrington, NYMA, Inc., 2001 Aerospace Parkway, Brook Park, Ohio 44142 (work performed under NAS3-27186); Brian D. Reed, NASA Lewis Research Center; Angel Rivera, Jr., Undergraduate Senior, University of Texas, San Antonio, Texas. Responsible person, Brian D. Reed, organization code 5330, (216) 977-7489.				
<b>12a. DISTRIBUTION/AVAILABILITY STATEMENT</b>  Unclassified - Unlimited Subject Category 18  This publication is available from the NASA Center for AeroSpace Information, (301) 621-0390.			<b>12b. DISTRIBUTION CODE</b>	
<b>13. ABSTRACT (Maximum 200 words)</b>  An experimental study was conducted on two small rockets (110N thrust class) to directly compare a standard conical nozzle with a bell nozzle optimized for maximum thrust using the Rao method. In large rockets, with throat Reynolds numbers of greater than $1 \times 10^5$ , bell nozzles outperform conical nozzles. In rockets with throat Reynolds numbers below $1 \times 10^5$ , however, test results have been ambiguous. An experimental program was conducted to test two small nozzles at two different fuel film cooling percentages and three different chamber pressures. Test results showed that for the throat Reynolds number range from $2 \times 10^4$ to $4 \times 10^4$ , the bell nozzle outperformed the conical nozzle. Thrust coefficients for the bell nozzle were approximately 4-12% higher than those obtained with the conical nozzle. As expected, testing showed that lowering the fuel film cooling increased performance for both nozzle types.				
<b>14. SUBJECT TERMS</b>  Nozzle; Rao; Conical; Low thrust; Reynolds number			<b>15. NUMBER OF PAGES</b> 13	
			<b>16. PRICE CODE</b> A03	
<b>17. SECURITY CLASSIFICATION OF REPORT</b> Unclassified	<b>18. SECURITY CLASSIFICATION OF THIS PAGE</b> Unclassified	<b>19. SECURITY CLASSIFICATION OF ABSTRACT</b> Unclassified	<b>20. LIMITATION OF ABSTRACT</b>	



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