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Prepared for the 39th Structures, Structural Dynamics and Materials Conference sponsored by AIAA, ASME, ASCE, AES, and ASC Long Beach, California, April 20-23, 1998

National Aeronautics and Space Administration

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### **A MAGNETIC SUSPENSION AND EXCITATION SYSTEM FOR SPIN VIBRATION TESTING OF TURBOMACHINERY BLADES**

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#### **Abstract**

The Dynamic Spin Rig (DSR) is used to perform vibration tests of turbomachinery blades and components under spinning conditions in a vacuum. A heteropolar radial active magnetic bearing was integrated into the DSR to provide noncontact magnetic suspension and mechanical excitation of the rotor to induce turbomachinery blade vibrations. The magnetic bearing replaces one of the two existing conventional radial ball bearings. Prior operation of the DSR used two voice-coil type linear electromagnetic shakers which provided axial excitation of the rotor. The new magnetic suspension and excitation system has provided enhanced testing capabilities. Tests were performed at high rotational speeds for longer duration and with higher vibration amplitudes. Some characteristics of the system include magnetic bearing stiffness values up to 60 000 lb/in., closed loop control bandwidth around 500 Hz, and multidirectional radial excitation of the rotor. This paper reports on the implementation and operation of this system and presents some test results using this system.

#### Introduction

Today' s **turbomachinery** components have extensive testing requirements and therefore there **is a need** to provide enhanced testing capabilities (Refs. 2 and 3). Rotating components are expected to be used at very high rotational speeds, have extended life, and have better static and dynamic properties. The Dynamic Spin Rig (DSR) (see Fig. 1) is used to perform research on turbomachinery blades and components under spinning conditions by rotating them in a vacuum chamber (Ref. 1). During rotation the rotor can be vibrated by using two voice-coil type linear electromagnetic shakers that apply axial forces to the rotor. Dynamic measurements are obtained yielding the blade's natural frequencies. The current rotational speed in the DSR is limited due to heating problems with the mechanical bearings. Additionally, the life of the **mechanical** bearing is limited. The existing excitation system is limited in the excitation energy it can provide and it can only excite in one plane.

As an alternative to the existing excitation system, **a** radial active **magnetic** bearing has been **incorporated** into the rig to provide magnetic excitation. It also replaces the lower mechanical bearing thereby providing magnetic suspension. Magnetic suspension (Refs. 4 and 5) provides no physical contact at the support position which eliminates heating due to mechanical contact. Mechanical life is substantially extended. Increased flexibility in excitation orientation (direction and phasing) is achieved. Additionally, the magnetic bearing provides active control of stiffness and damping at the point of action. All of these features enable more useful testing to be performed.

#### The Dynamic Spin Rie

The DSR provides experimental data for evaluation of **vibration** analysis methods for rotating systems. **Bladed** rotors up to 81 cm (32 in.) in diameter can be spun to 20 000 rpm by a speed regulated air motor. Before installation of the magnetic bearing, electromagnetic shakers were primarily used to apply oscillatory axial forces to the rotor shaft through a thrust bearing. Strain gages, accelerometers, and optical blade-tip vibration sensors provide blade vibration signals.

Figure 2 is a cutaway drawing of the rig with two mechanical bearings supporting the rotor. Shown are the vacuum tank, the air motor drive, two electromagnetic shakers, a multiblade rotor (with a vertical axis of rotation), a 100-channel slipring assembly (which is located at the bottom of the rotor and is used to take signals from the rotor), and an indication of the optical probe system for blade-tip observation. The vacuum (down to 0.02 psia) reduces the torque required to drive the disk and renders aerodynamic effects negligible.

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The **two** 220-N **(50-1bf)** shakers move the shaft by acting on the **outer** race of a **thrust** bearing. The shakers are operated in phase to provide axial excitation and out of phase to produce a moment on the shaft. Shaft motion is permitted because the rotor bearings are mounted on rubber supports. These supports introduce damping into all modes that couple to axial or transverse motion of the shaft.

The original design of the DSR has the shaft supported by two bearings. There **is a** beating at the top and **bottom** end of the shaft and the blade disk is between the bearings. The bearings are deep groove ball type with grease packing and phenolic cages. A current study has concluded that the rig should be able to run at 10 000 rpm without exceeding the recommended DN limit of the bearings. However, running at 15 000 rpm is not recommended. The rig has been operated up to 20 000 rpm but only for short times. The bearings heat up during operation and a temperature of 220 °F is used to limit duration at high speeds. When this temperature is reached, the speed of the rig is reduced and the bearings allowed to cool down.

The new magnetic suspension and excitation system involves using a single radial heteropolar active magnetic bearing to replace the lower mechanical bearing. In Fig. 3, the magnetic bearing is shown installed in the rig. This new system adds additional spin vibration testing capabilities to the rig. Details of the new system will be presented in a later section.

#### Magnetic Suspension and Excitation

#### **Magnetic Bearing**

The active magnetic bearing is a 4-pole (with 3 legs/ pole existing as an artifact of a previously fabricated stator stamping for a motor) heteropolor type (see Fig. 4). Each pole has 160 coil turns. Its outer diameter is 4.7 in. It is operated using a maximum of 4 A/coil. Measurements have produced stiffness values up to 60 000 lb/in. The nominal radial gap distance is 0.020 in. with a typical operating radial shaft excursion of about 0.005 in. The magnetic bearing system bandwidth, including computer controller, power amplifiers, etc., is about 500 Hz.

#### Control System

The control system uses proportional-derivative (PD) control implemented using Turbo Pascal programming language on a 486-PC. This control system allows modification of magnetic bearing parameters such as stiffness and damping. Figure 5 shows the control system block diagram. It includes all of the excitation and suspension elements which represent the system. The controller has two primary components. One component provides the magnetic bearing suspension and the other

provides the excitation. Gains can be programmed for various operating conditions.

#### System Dynamics

The force, *F,* generated by **one** pole of an electromagnet can be shown to be given by the following equation:

$$
F = -\frac{\mu_0 N^2 A}{4} \frac{i^2}{x \frac{2}{g}}
$$
 (1)

where  $i$  is the current in the coil,  $N$  is the number of coil turns, A is the pole face area,  $x_g$  is the gap distance, and  $\mu_0$ is the permeability of free space.

The force in Eq. (1) is attractive and increases as the gap decreases. This attractive force produces an unstable system for an open loop magnetic bearing configuration. The net force produced by an opposing pair of identical electromagnets on a single **axis** is the sum of the forces produced by each electromagnet, taking into account the sign convention. The net force,  $F_n$ , is obtained using the following equation:

$$
F_n = Z \left[ \frac{i_1^2}{x_{g1}^2} - \frac{i_2^2}{x_{g2}^2} \right]
$$
 (2)

where the **subscripts indicate** an association with aparticular **magnet,** and

$$
Z = \frac{\mu_0 N^2 A}{4} \tag{3}
$$

Conventional **magnetic** bearing practice linearizes the force-current relationship by using abias current along with a superimposed control current. In order to obtain a linear relation between force and control current we express the currents  $i_1$  and  $i_2$  in the opposing coils as:

$$
i_1 = i_b + i_c \tag{4}
$$

and

$$
i_2 = i_b - i_c \tag{5}
$$

where  $i<sub>b</sub>$  is the bias current and  $i<sub>c</sub>$  is the perturbation or control current. Generally, the bias current is chosen to be equal to one-half the maximum allowable current. Next we express each gap in terms of the nominal gap  $x_0$  and the deviation *x* from this nominal value caused by the rotor displacement:

$$
x_{g1} = x_0 - x \tag{6}
$$

and

$$
x_{g2} = x_0 + x \tag{7}
$$

Combining Eqs. (4) to (7) and (2) yields:

$$
F_n = Z \left[ \frac{\left(i_b + i_c\right)^2}{\left(x_0 - x\right)^2} - \frac{\left(i_b - i_c\right)^2}{\left(x_0 + x\right)^2} \right] \tag{8}
$$

For  $x = 0$ , we can simplify the force equation to involve only  $i_c$  as a variable:

$$
F_n = \frac{Z}{x_0^2} \left[ \left( i_b + i_c \right)^2 - \left( i_b - i_c \right)^2 \right] \tag{9}
$$

*This* further simplifies to a linear relationship between force and control current that can be used to implement control commands based **on** *classical* linear *control theory:*

$$
F_n = \frac{4Zi_b}{x_0^2} i_c
$$
 (10)

In order to find the change in force due to a change in position (position stiffness) and the change in force due to a change in current (current stiffness) it is necessary to take the derivative of the force with respect to the variable of interest. Using Eq. (8), the position stiffness evaluated about  $x = 0$  and  $i_c = 0$  is:

$$
K_{x} = \frac{\partial F_{n}}{\partial x}\Big|_{x=0, i_{c}=0} = \frac{4Zi_{b}^{2}}{x_{0}^{3}}
$$
(11)

and the current stiffness evaluated at  $x = 0$  and  $i_c = 0$  (from Eq. (10)) is:

$$
K_i = \frac{\partial F_n}{\partial i} \bigg|_{x=0, i_c=0} = \frac{4Zi_b}{x_0^2} \tag{12}
$$

Now we have a linear relationship between force and control current:

$$
F_n = K_x x + K_i i_c \tag{13}
$$

This linearized force equation is generally used for linear control development even though the assumptions that were made are occasionally violated in practice.

For proportional-derivative (PD) feedback control the following relation is used:

$$
i_c = -\left(K_p x + K_d \dot{x}\right) \tag{14}
$$

where  $K_p$  is the proportional control gain and  $K_d$  is the derivative control gain.

Consequently, for a rigid rotor, an equivalent lumped mass model,  $m_{eq}$ , of the rotor can be used and the dynamics of the system would become:

$$
m_{eq}\ddot{x} = F_n \tag{15}
$$

Substituting Eq. (14) into Eq. (13) and Eq. (14) into Eq.  $(15)$  and simplifying, the following is obtained:

$$
m_{eq}\ddot{x} + K_i K_d \dot{x} + (K_i K_p - K_x) x = 0 \tag{16}
$$

Equation (16) represents the suspension system. To include the excitation portion we can add an excitation variable,  $i_{ex}$ , to Eq. (14) to get:

$$
i_c = -\left(K_p x + K_d \dot{x}\right) + i_{ex} \tag{17}
$$

The resulting system dynamics becomes:

$$
m_{eq}\ddot{x} + K_i K_d \dot{x} + \left(K_i K_p - K_x\right) x = F_{ex} \tag{18}
$$

where the excitation force,  $F_{ex}$ , is given by:

$$
F_{ex} = K_i i_{ex} \tag{19}
$$

Finally, if we define

$$
c_{eq} = K_i K_d \tag{20}
$$

and

$$
k_{eq} = K_i K_p - K_x \tag{21}
$$

**then the** final dynamic **equation** becomes:

$$
m_{eq}\ddot{x} + c_{eq}\dot{x} + k_{eq}x = F_{ex} \tag{22}
$$

Magnetic Suspension

The magnetic bearing operates not only as an exciter but as a fully functioning magnetic bearing. Magnetic suspension provides no physical contact at the support position which eliminates heating due to mechanical contact. Mechanical life is substantially extended. Increased flexibility in how the excitation is applied (direction and phasing) is achieved. The magnetic bearing supports the shaft at the lower end which was previously supported by

a mechanical bearing. The magnetic bearing provides active control of stiffness and damping at the point of action. In order to determine what combination of gains are useful and produce stable operation, a stability map was obtained experimentally by observing and recording what gain combinations produced instability. These gains are plotted to show a stability surface under which stable operation of the system is achieved (see Fig. 6). A frequency domain representation of the system's dynamic characteristic gives another perspective of the system. A transfer function between the excitation signal and the shaft position signal gives a spectral profile that indicates how well we can transmit energy to the system (see Fig. 7; K is the keyboard value of control stiffness and D is the keyboard value of control damping).

Testing yielded successful magnetic bearing **operation** for rotational speeds up to 9000 rpm, in **a vacuum,** with control gains producing stiffness up to 60 000 lbs/in. The success of the initial work has led to the design and intended implementation of a full magnetic suspension system. The full magnetic support will enable longer run time at higher speeds and larger vibration amplitudes for rotating blades.

#### **Excitation Operation**

In Fig. (8), a schematic of the reference coordinates is shown. The x-y axes are fixed and are representative of the stator frame of reference. The radius vector, *r,* is a representative vector of a fixed location on the moving shaft. This can be associated with the planar location of a set of blades on the shaft. The excitation force vector,  $F_{\rho r}$  is the excitation force produced by the magnetic bearing which can be oriented in any radial direction.  $\theta$  and  $\phi$  are the vector angles for the radius vector and the excitation force vector, respectively.

The excitation signal can have a variety of forms. It can be a sinusoidal signal of single frequency, random, broadband noise, or any general signal generated by a signal generator or a feedback control law in the control system. For most conditions the excitation has the following form:

$$
F_{ex} = F_0 \sin(\psi t) \tag{23}
$$

where  $F_0$  is the excitation signal amplitude and  $\psi$  is the excitation frequency. The force resolved onto the x-y axes yields:

$$
F_{ex_x} = F_{ex} \cos(\phi) = F_0 \sin(\psi t) \cos(\phi)
$$
  
=  $F_0 \sin(\psi t) \cos(\eta t)$  (24)

$$
F_{ex_y} = F_{ex} \sin(\phi) = F_0 \sin(\psi t) \sin(\phi)
$$
  
=  $F_0 \sin(\psi t) \sin(\eta t)$  (25)

where the sub-subscripts indicates the associated reference axis and the excitation angular frequency,  $\eta$ , is given by:

$$
\eta = \phi \tag{26}
$$

The **rotational** speed of the shaft, *to,* is given as follows:

$$
\omega = \theta \tag{27}
$$

The magnetic bearing exciter has **several** modes of shaking **the** rotor to produce blade vibrations. The differences between **the** modes are due **to the** radial orientation, phasing, and frequency of **the** applied force. There are two primary modes of operation. One mode produces an **excitation** force with a fixed orientation with respect to **the** stator, i.e.  $\phi$  is constant, which is called the stator-fixed mode. The other mode produces an **excitation** force with a fixed orientation with respect to the rotor, i.e.  $\phi$  is not constant, which is called **the rotor-fixed** mode. **For each** mode of operation, the shaft may or may not be rotating. For nonrotating tests, where  $\theta$  is constant, the stator fixed mode allows **the** force **to** be set at a desired orientation that may be optimal for large deflections. An example of **this** would be for a **two-bladed test** article in which the blades were positioned **to** lie coplanar **to** the plane made by **the** radial position vector, *r,* and **the shaft** vertical axis (see **Figs. 8** and 9). **For this** blade position, **the** force would best be oriented perpendicular **to the** blade plane, where  $\theta - \phi = (2n - 1)\pi/2$ ,  $n = 1, 2, 3, ...$ , and  $\theta = \text{const}$ , to produce large amplitude "flapping" vibrations. **For** rotating **tests** with the stator-fixed force,  $\phi$  can be arbitrary since any setting produces the same vibratory response. The **rotor**fixed mode produces an **excitation** force with a fixed orientation with respect **to the** rotor based upon a onceper-revolution signal. Operating **this** way for nonrotating tests, using an artificial once-per-revolution signal, allows whirling of the shaft to produce blade vibrations ( $\phi \neq const$ and  $\theta$  = const). For rotating tests, the orientation of the excitation force follows the test article as it rotates ( $\theta - \phi$ )  $=$  const,  $n = 1,2,3...$ , and  $\theta \neq$  const). This is an excellent spin **test** feature. Other modes of operation can be achieved. **For** any of these modes, **sinusoidal** or random signals can be used for *Fex.* Typically, one can use **random** noise **to** find the blade frequencies and **then** use a **sinusoidal signal to** drive at a particular frequency of interest.

Operation of the magnetic bearing as an **exciter** was successful and compared favorably **to the** electromagnetic shakers. The magnetic bearing can transmit more vibrational energy into the shaft, excite some blade modes to larger amplitudes, and improve flexibility in applying the excitation force in orientation and phasing. A summary of the excitation operation is given in Table I.

#### **Vibration Testing**

Dynamic tests have been performed using this new capability (Ref. 8). Blade like structures (see Fig. 9), provided by the University of California at San Diego, were tested and essential dynamic data was obtained (Ref. 7). Results from the tests indicated that using the new magnetic excitation system was extremely beneficial.

A preliminary investigation was performed using the magnetic bearing system to provide shaft actuation to suppress blade vibrations using blade strain gage feedback. Initial results were favorable and were presented at the High Cycle Fatigue Initiative Workshop - Active Vibration Control/Engine Health Monitoring Session December 10, 1996. The presentation was titled "Active Control of Blade Vibration Using Magnetic Forcing of Shafts." Two sample frequency response figures are shown in Figs. 10 and 11. In Fig. 10, the mechanical shakers are used for excitation with the magnetic bearing used for blade vibration control. In Fig. 11, the magnetic bearing is used for excitation and control. Comparing Figs. 10 and 11 indicate that for these tests the magnetic excitation transmitted more energy to the blades for the uncontrolled conditions.

#### Summary\_

In summary, a single radial active magnetic bearing was integrated into the Dynamic Spin Rig (DSR) to provide vibration excitation. The rig was modified to have the magnetic bearing replace a conventional ball bearing support thereby providing blade vibration excitation, and shaft suspension and control. The implementation of the new system has been outlined and the preliminary operational performance of the magnetic bearing has been assessed, producing favorable results. This work demonstrated the feasibility of using magnetic actuation to enhance structural dynamic testing. Consequently, the system will be converted to an all magnetically supported one, further enhancing its testing capabilities. The magnetic bearings will provide magnetic actuation for excitation and support, increase excitation energy and forceorientation **flexibility,** allow longer duration at high rotational speeds, and increase test duration (life cycles).

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Operational mode			
Stator-fixed reference nonrotating shaft rotating shaft	constant variable	constant constant	constant variable
Rotor-fixed reference nonrotating shaft rotating shaft	constant variable	variable variable	variable constant

TABLE L--SUMMARY OF EXCITATION OPERATION



Figure 1.-Dynamic Spin Rig Facility.



Figure 3.-Magnetic bearing installed in Dynamic Spin Rig.







Figure 5.-Block diagram for Dynamic Spin Rig excitation system.



Figure 2.-Cutaway drawing of Dynamic Spin Rig.











**Figure 8.---Schematic of top down view of shaft.**







**Figure 9.**-Viscoelastic damped composite plates in **the NASA Dynamic Spin Rig Facility.**





 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$ 

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}^{\text{max}}_{\mathcal{L}}(\mathcal{L}^{\text{max}}_{\mathcal{L}})) \leq \mathcal{L}(\mathcal{L}^{\text{max}}_{\mathcal{L}}(\mathcal{L}^{\text{max}}_{\mathcal{L}}))$ 

 $\label{eq:2.1} \frac{1}{2} \sum_{i=1}^n \frac{1}{2} \sum_{j=1}^n \frac{$ 

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