



**Minnowbrook VI, August 2009**

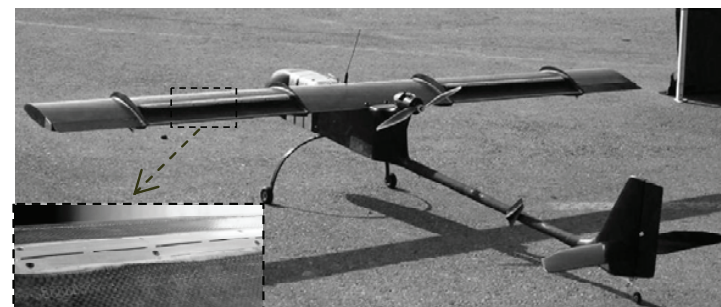
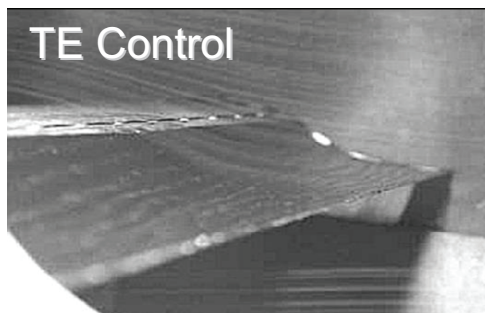
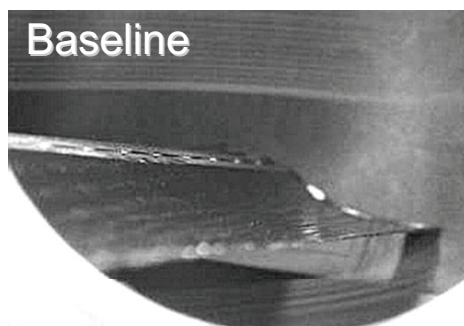


# **Amplitude Scaling of Active Separation Control**

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**School of Mechanical Engineering**

**Faculty of Engineering, Tel-Aviv University, ISRAEL**



## **Acknowledgment:**

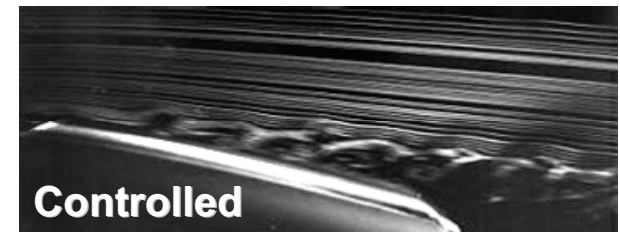
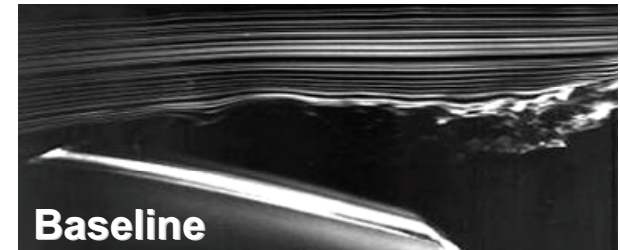
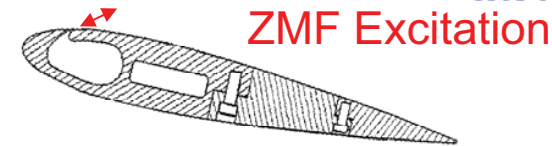
**I. Fono, G. Arwatz, T. Yehoshua, E. Ben-Hamou, I. Dayan  
S. Pasteur, E. Nevo, Kronish, Blas, Meadow Aero Lab members**



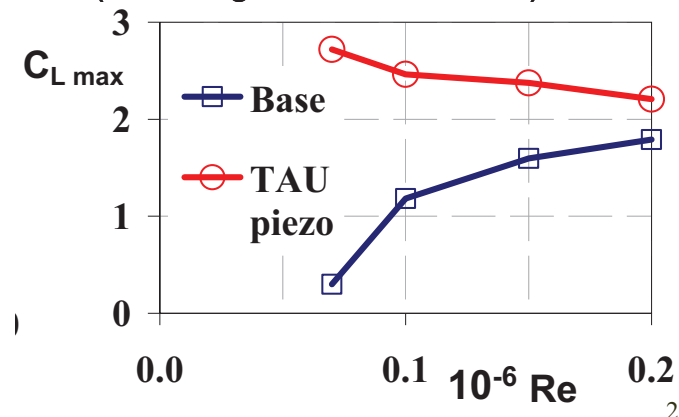
# Motivation



- Active control of boundary layer separation leads to many benefits
- Frequency parameter: Strouhal ( $F^+$ )
- Length scale under controversy
- Amplitude scaling?
- We use  $C_\mu$  – historically, steady blowing
- But does it scale the data?
- Are there other parameters we should consider?
- We revisit here known and define 2 new amplitude scaling parameters
- Check their validity using low Re data ( $Re < 1 \times 10^6$ )



(Neuburger, '89,  $Re < 100k$ )





# Amplitude scaling - 1



- **Velocity Ratio**

$$VR \equiv \frac{U_p}{U_e} \approx \frac{U_p}{U_\infty}$$

- $U_p$ - peak excitation velocity
- $U_e$ - local external velocity
- $U_\infty$ - free-stream velocity
- **Actuator Mach number over free-stream Mach number**
- **Implies linearity**



(Yehoshua)



# Amplitude scaling - 2



- **Momentum coefficient**

$$C_{\mu} \equiv \frac{h}{c} \left( \frac{U_p}{U_{\infty}} \right)^2 = \frac{h}{c} (VR)^2$$

- **Ratio between (incomp., isoth.)**

- Excitation momentum ( $h$ =slot width)

$$hU_p^2$$

- Free stream momentum ( $c$ =chord)

$$cU_{\infty}^2$$

- $U_p$  - peak excitation velocity

- $U_{\infty}$  - free-stream velocity

- $h$  – slot width,  $c$  – airfoil chord

- Follows steady-blowing concept

(Yehoshua)





# Amplitude scaling - 3



- **Reynolds # corrected momentum coefficient**

- **Ratio between**

- **Excitation momentum**

$$\approx hU_p^2$$

- **BL momentum deficit**

$$\approx \theta U_\infty^2$$

- **Laminar momentum thickness**

$$\frac{\theta_{Lam}}{c} \approx Re^{-0.5}$$

- **Turbulent momentum thickness**

$$\frac{\theta_{Turb}}{c} \approx Re^{-0.2} \Rightarrow \theta_{Turb} \approx c Re^{-0.2}$$

$$C_{\mu,Re} \equiv \frac{h U_p^2}{\theta U_\infty^2} \approx \frac{h(VR)^2}{c Re^m} = \frac{h}{c} (VR)^2 Re^{-m}$$



(Yehoshua)



# Vorticity-flux / Circulation - 4



- **Actuator's vorticity flux (blowing, half slot width)**

$$VF \approx \int_0^{T/2} \int_0^{h/2} \omega_z(y,t) U_p(y,t) dy dt$$

$$VF \approx \int_0^{h/2} \int_0^{T/2} U_p(y,t) \frac{dU_p(y,t)}{dy} dt dy$$

$$VF \approx \frac{U_p^2}{h} \frac{hT}{4} \approx \frac{U_p^2 T}{4} \approx \frac{U_p^2}{4f}$$

- **Kutta-Zhukovsky**
- **Circulation**
- **Vorticity-flux coefficient**

$$C_L = \frac{\rho_\infty U_\infty \Gamma}{1/2 \rho_\infty U_\infty^2 c}$$

$$\Gamma = c C_L U_\infty$$

$$C_\Gamma \equiv \frac{\text{Slot\_Vorticity\_Flux}}{\text{Baseline\_Circulation}} \approx \frac{U_p^2 T}{4 \Gamma_{\text{Baseline}}}$$

$$C_\Gamma \approx \frac{U_p^2 T}{4 c C_L U_\infty} = \frac{1}{4 C_L} \left( \frac{U_p}{U_\infty} \right)^2 \frac{1}{S_t} = \frac{(VR)^2}{4 C_L S_t}$$



# Frequency corrected VR - 5



- Nagib et al (2006)
- Proposed to scale AFC effect on lift using
  - Velocity ratio
  - Strouhal number
- For large separated regions
- Low frequencies
- Problematic at  $f \rightarrow 0 \dots$

$$H \equiv \frac{U_p / U_\infty}{\sqrt{fc / U_\infty}} = \frac{VR}{\sqrt{S_t}}$$



(Yehoshua)



# Amplitude Scaling Options



- **Velocity ratio (VR)**

$$VR \equiv \frac{U_p}{U_e} \approx \frac{U_p}{U_\infty}$$

- **Strouhal weighted VR (Nagib et al, 2006)**

$$H \equiv \frac{VR}{\sqrt{S_t}}$$

- **Momentum coefficient**

$$C_\mu \equiv \frac{h}{c} (VR)^2$$

- **Reynolds corrected  $C_\mu$** 
  - $m=0.2$  (Turb.),  $m=0.5$  (Lam.)

$$C_{\mu,Re} \equiv \frac{h}{c} (VR)^2 \text{Re}^m$$

- **Vorticity flux coefficient**

$$C_\Gamma \equiv \frac{(VR)^2}{C_L S_t}$$

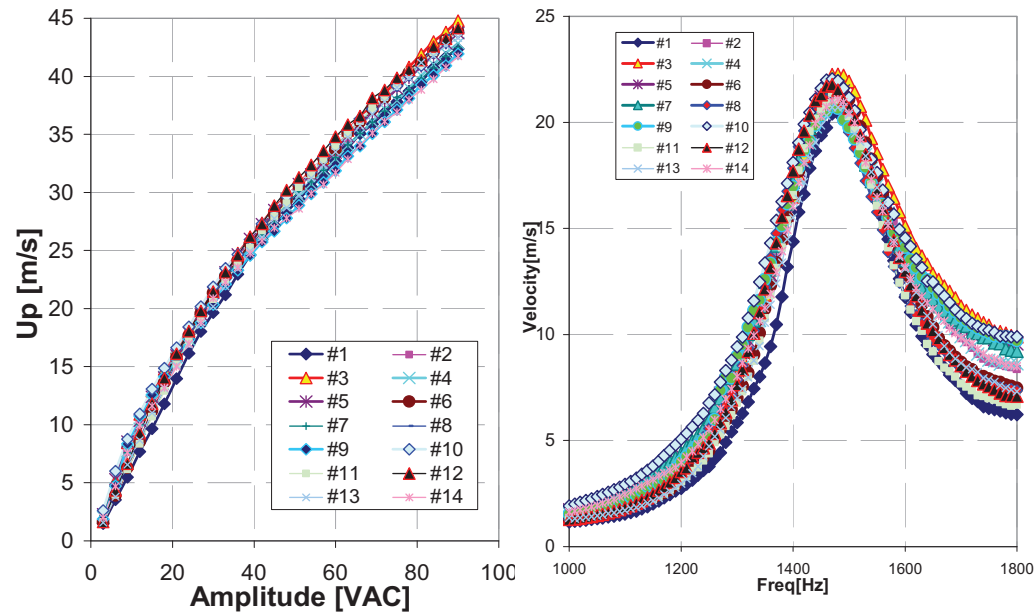
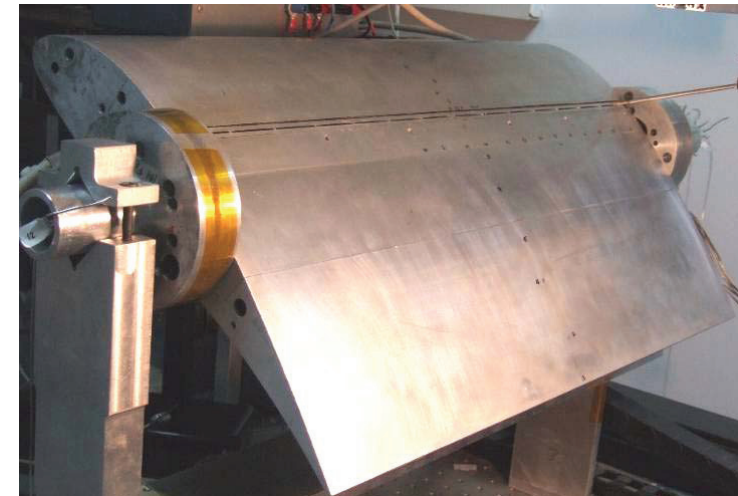
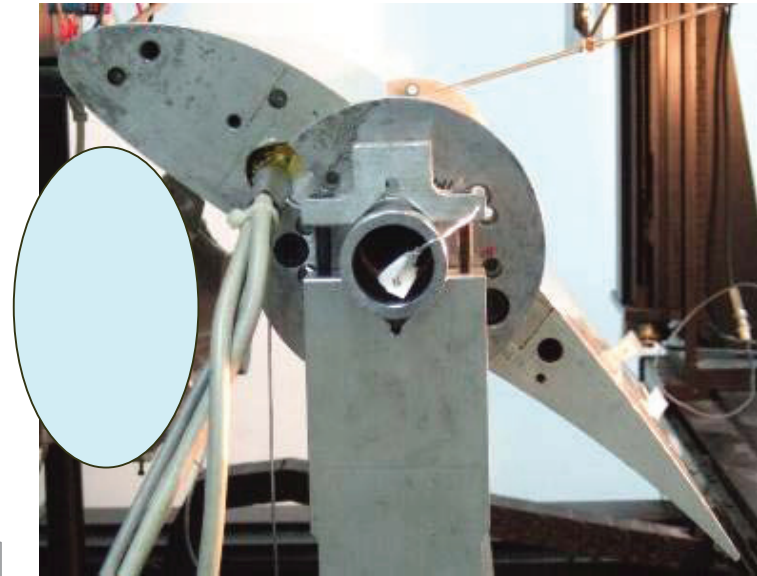




# IAI-Pr8-40 Airfoil AFC Testing



- Chord 360mm, span 609mm
- Actuator at  $x/c=0.38$
- Shallow angle, downstream excitation
- 14 segmented, individually controlled
- Piezo actuators ( $f_{\text{Helmholtz}}=1460\text{Hz}$ )
- Slots: 0.9mm by 40mm
- Power: 1.7w per actuator at 100vac

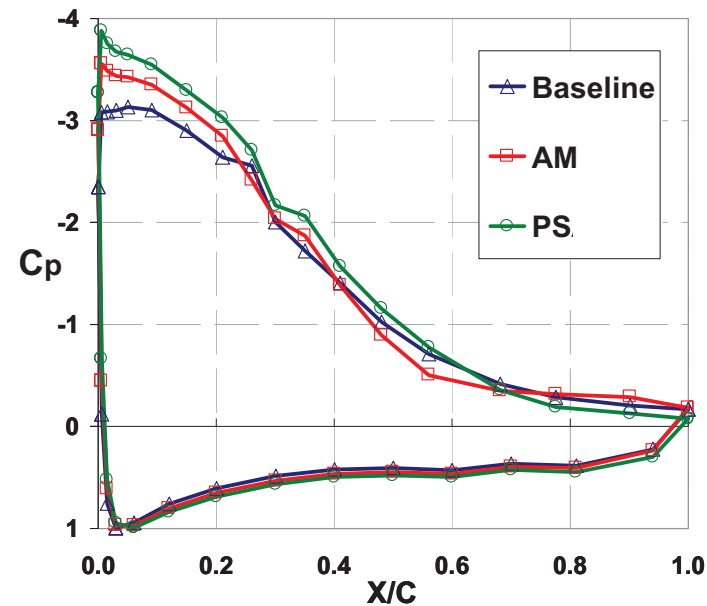
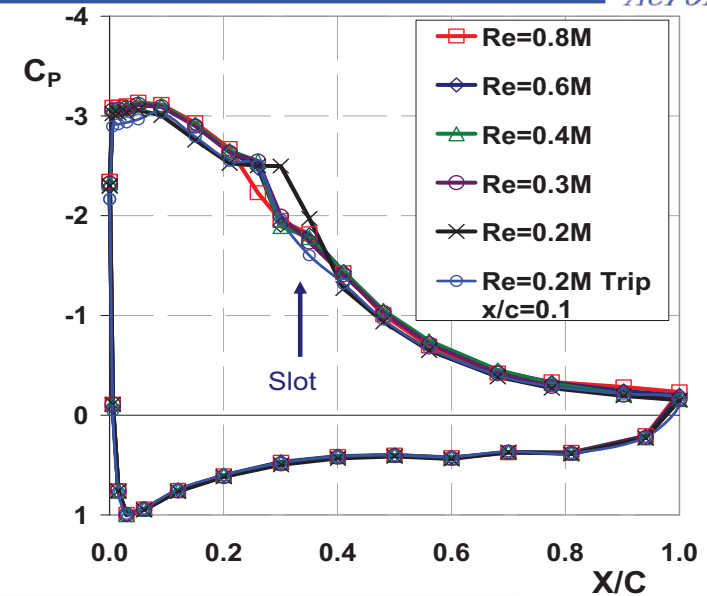
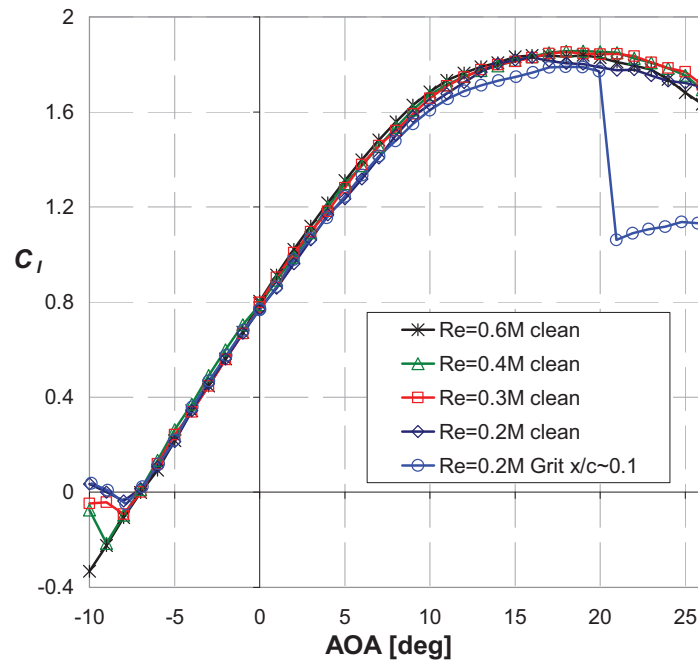




# IAI-Pr8-40 Baseline



- Thick, Efficient, Low Re airfoil
- Mild, trailing edge stall
- Chord 360mm, span 609mm
- Actuator at  $x/c=0.38$
- Shallow angle, downstream excitation
- 14 segmented, individually controlled
- Piezo actuators ( $f_{\text{Helmholtz}}=1460\text{Hz}$ )
- Slots: 0.9mm by 40mm

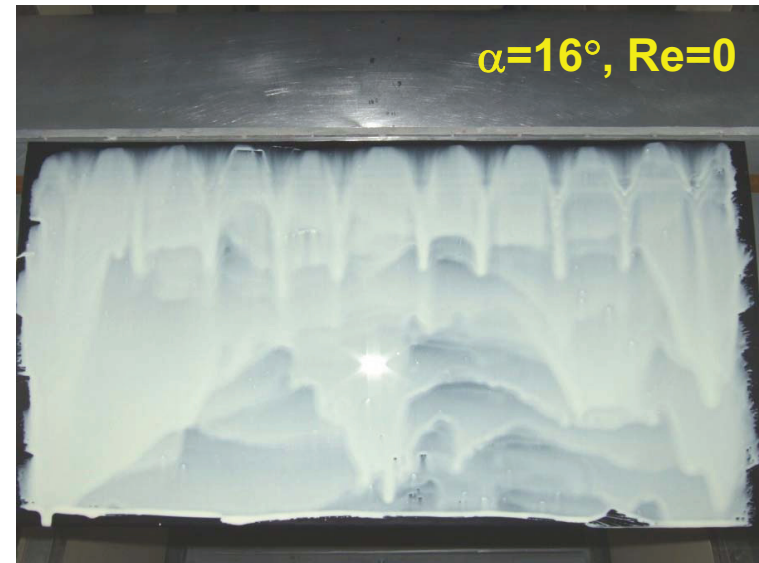
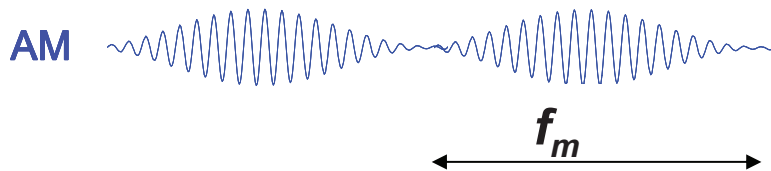




# IAI-Pr8-40 Controlled



- Actuator at  $x/c=0.38$
- Shallow angle, downstream excitation
- 14 segmented, individually controlled
- Piezo actuators ( $f_{\text{Helmholtz}}=1460\text{Hz}$ )
- Slots: 0.9mm by 40mm
- Two modes of operation:
  - Pure sine, Anti-phase,  $F^+>10$
  - AM, In-phase,  $F^+\sim 1$
  - Control of TBL separation
  - Conducted amplitude scans at otherwise fixed conditions
  - Scale lift increment vs amplitude



$\alpha=16^\circ, Re=0.3M$

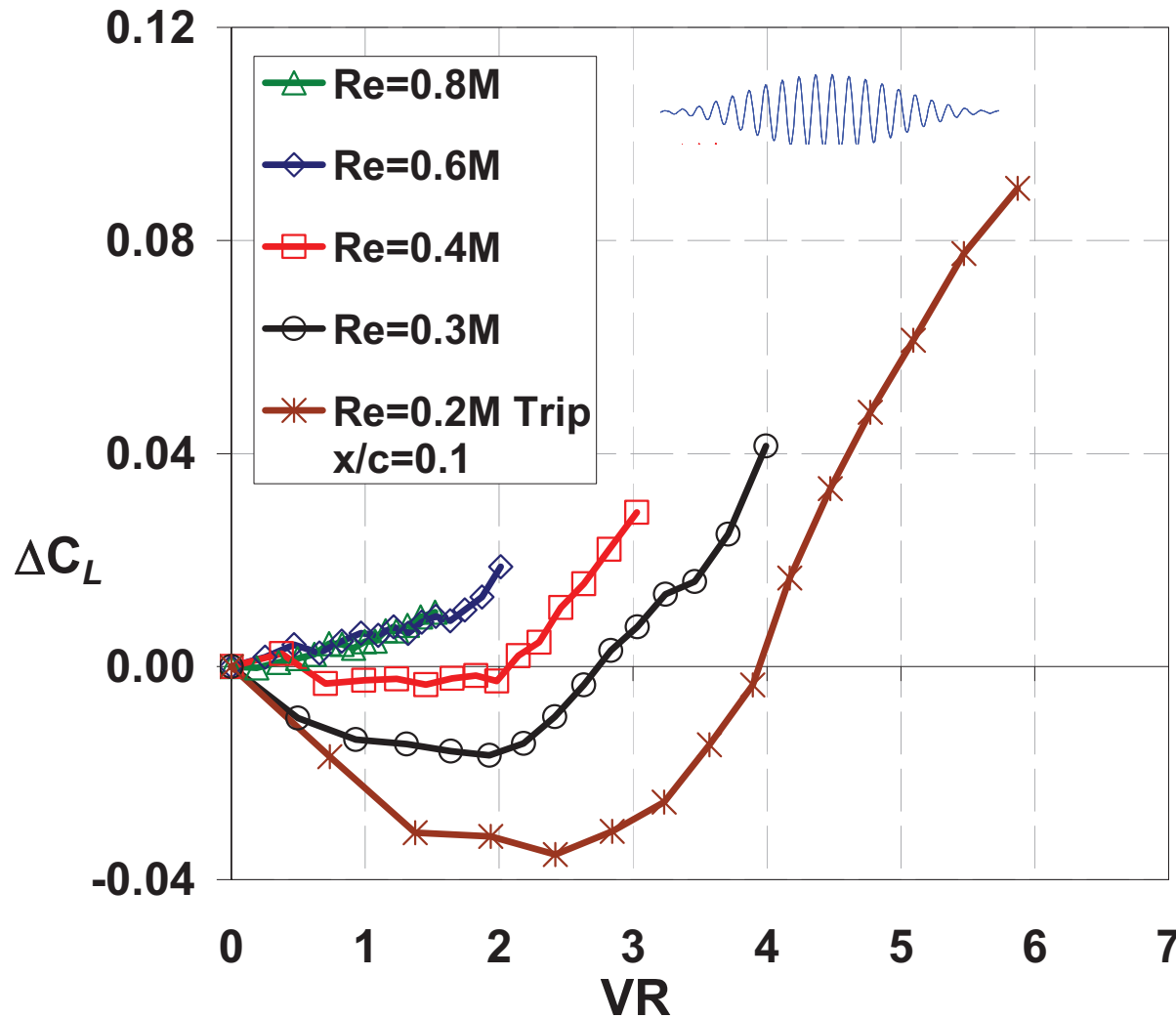


# Low Frequency Amp Scaling



- Velocity ratio (VR)

$\alpha=16^\circ$ , AM,  $F^+=1$



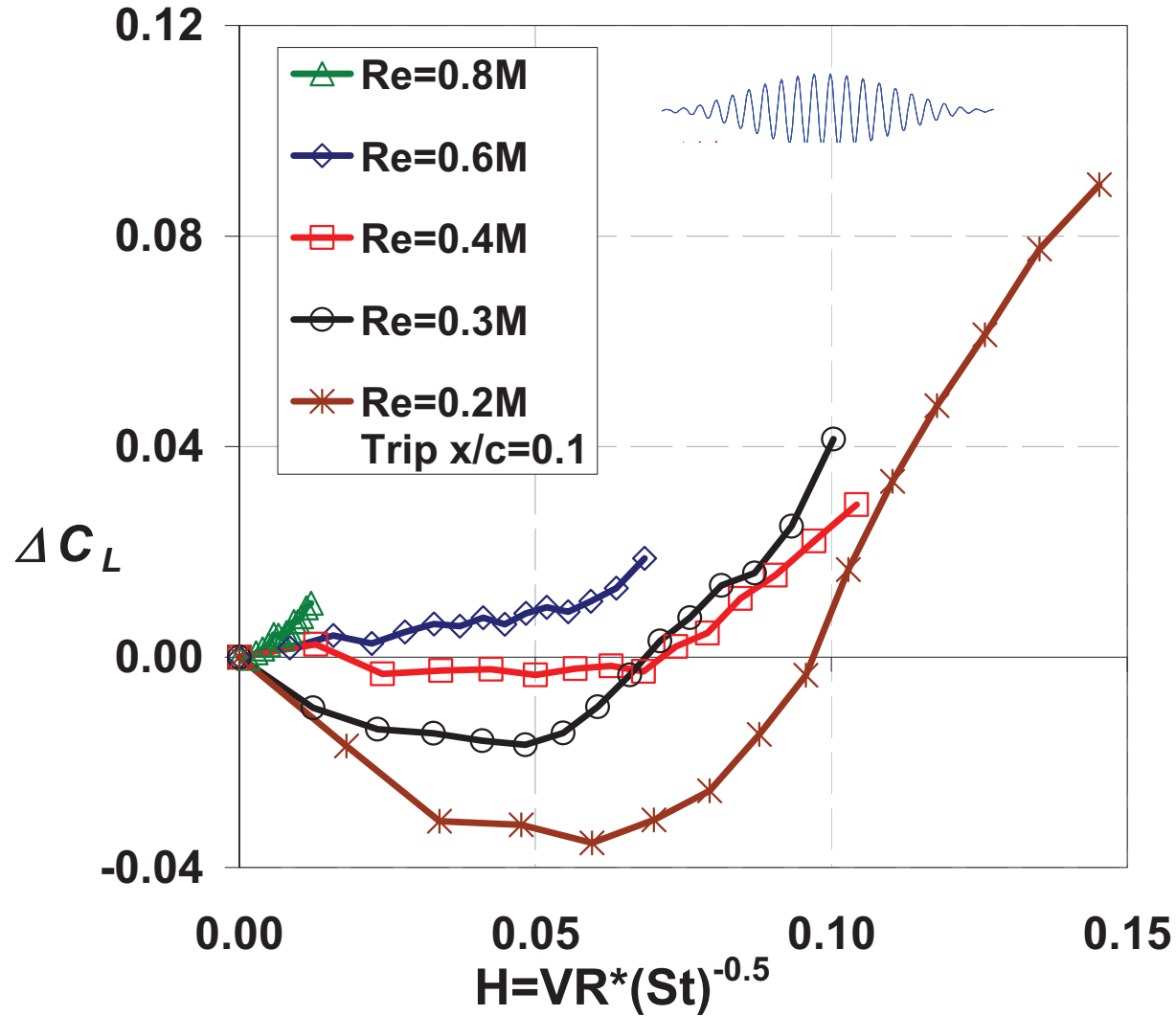


# Low Frequency Amp Scaling



- St corrected VR

$\alpha=16^\circ$ , AM,  $F^+=1$



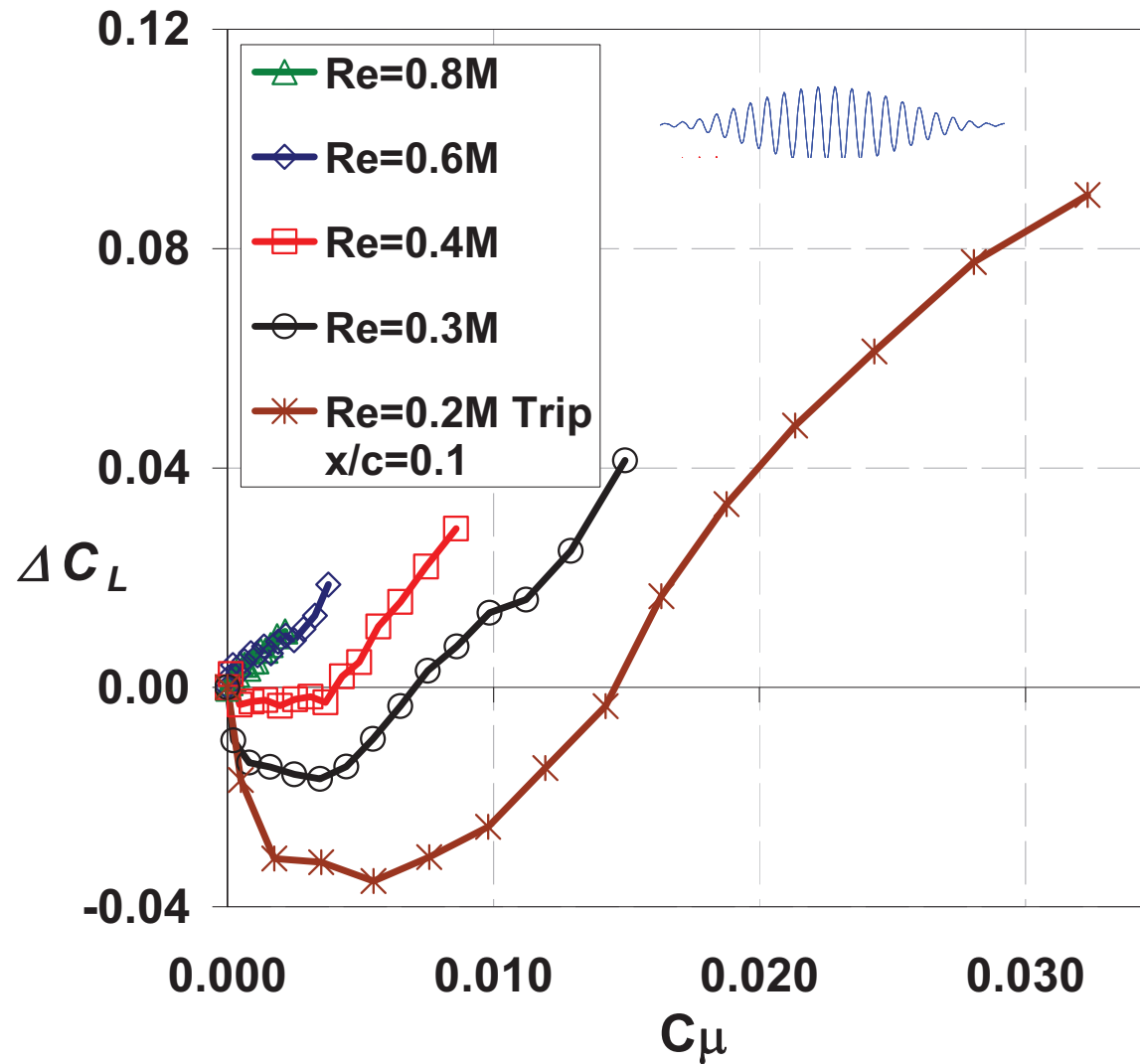


# Low Frequency Amp Scaling



- Momentum Coefficient

$\alpha=16^\circ$ , AM,  $F^+=1$



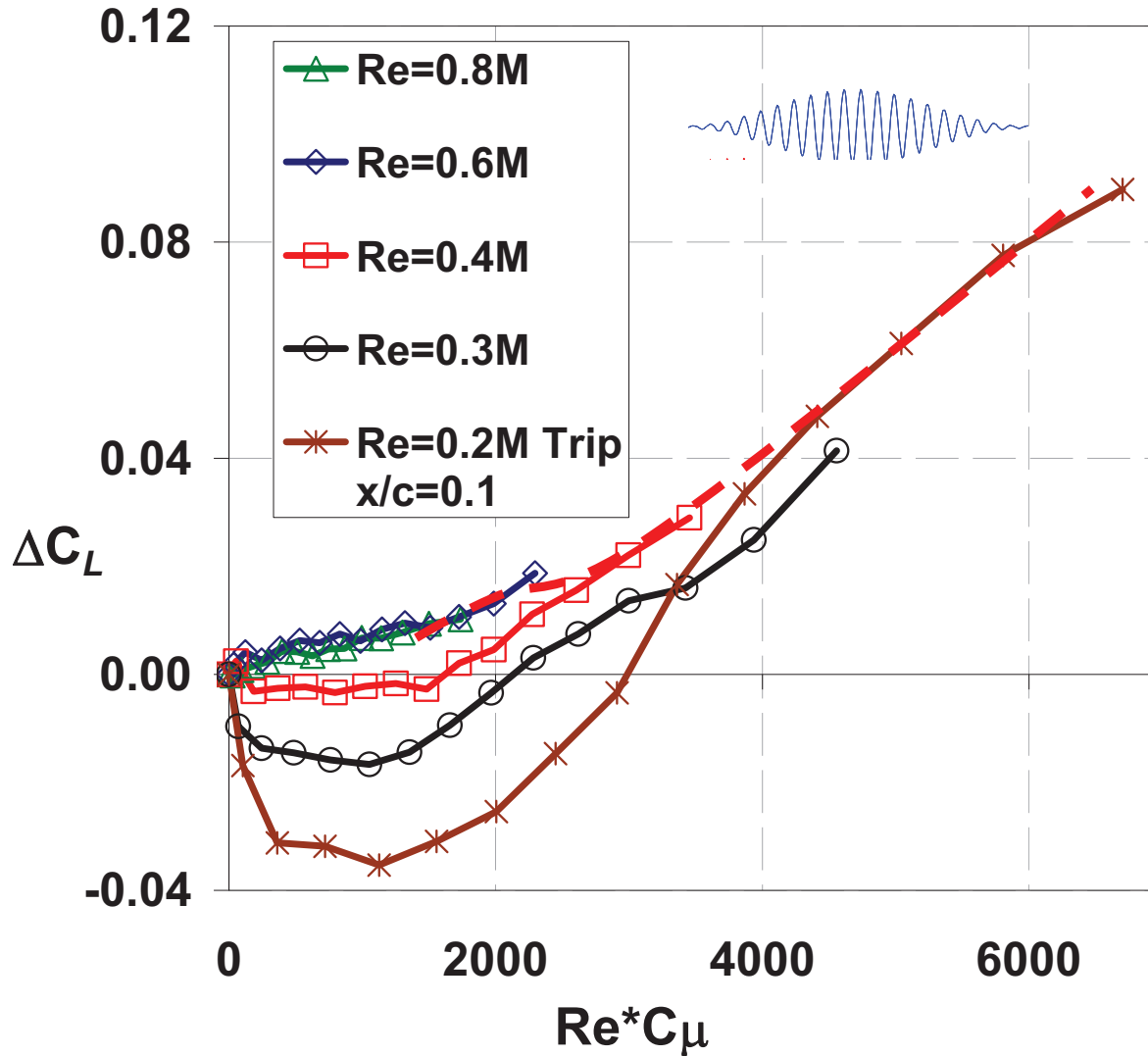


# Low Frequency Amp Scaling



- Reynolds corrected Momentum Coefficient

$\alpha=16^\circ$ , AM,  $F^+=1$

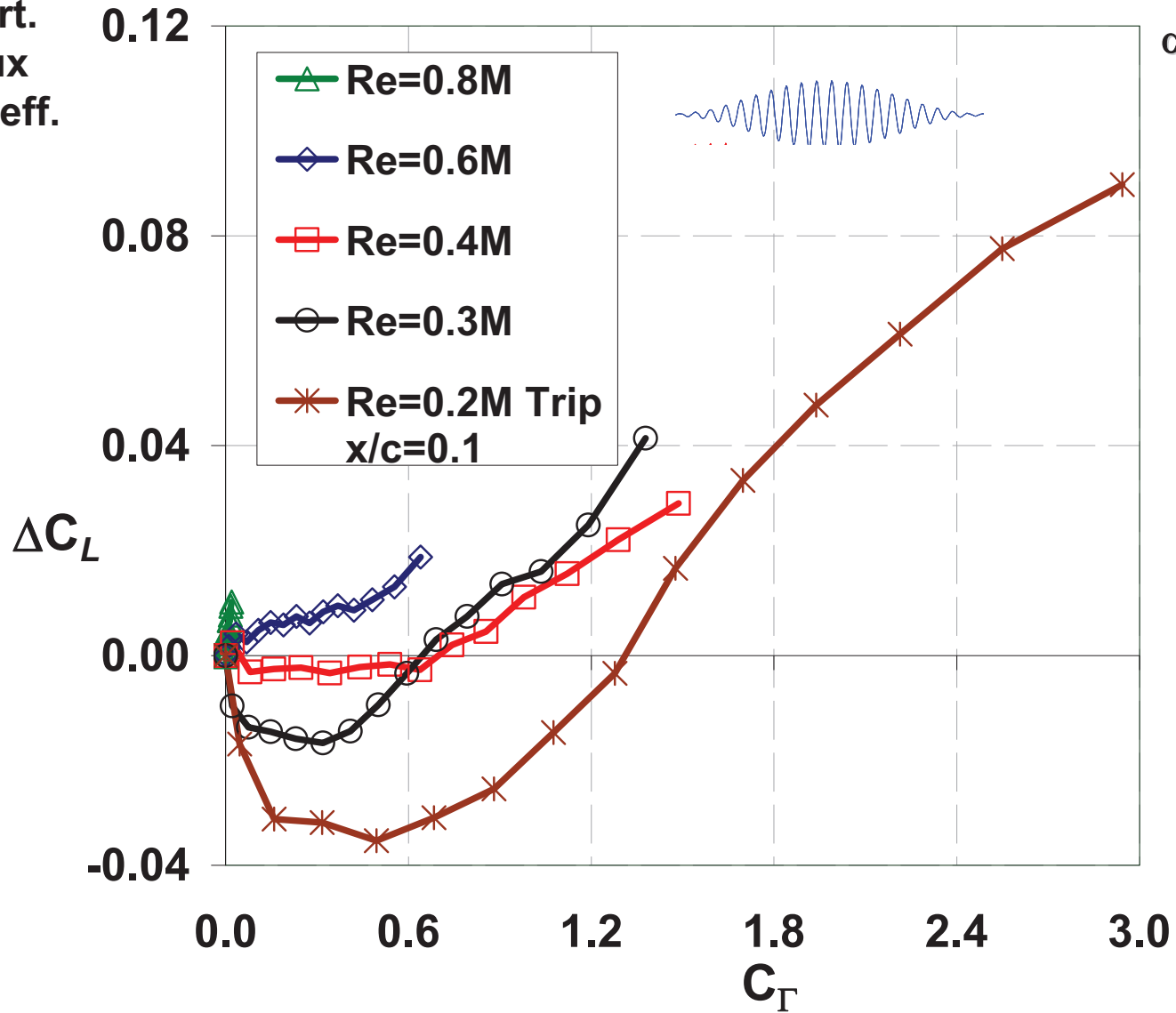




# Low Frequency Amp Scaling



- Vort. Flux Coeff.



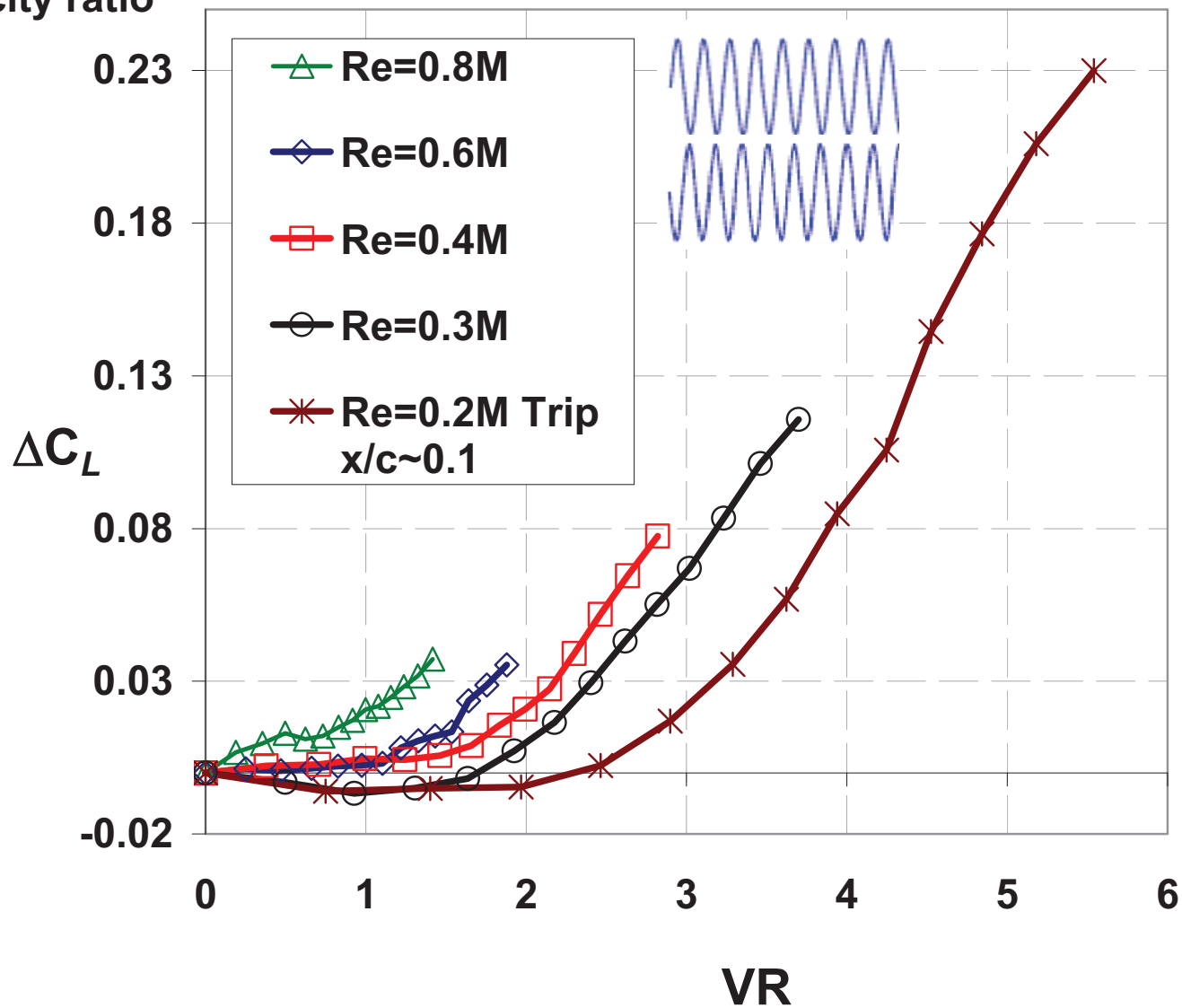




# High Frequency Amp Scaling



- Velocity ratio

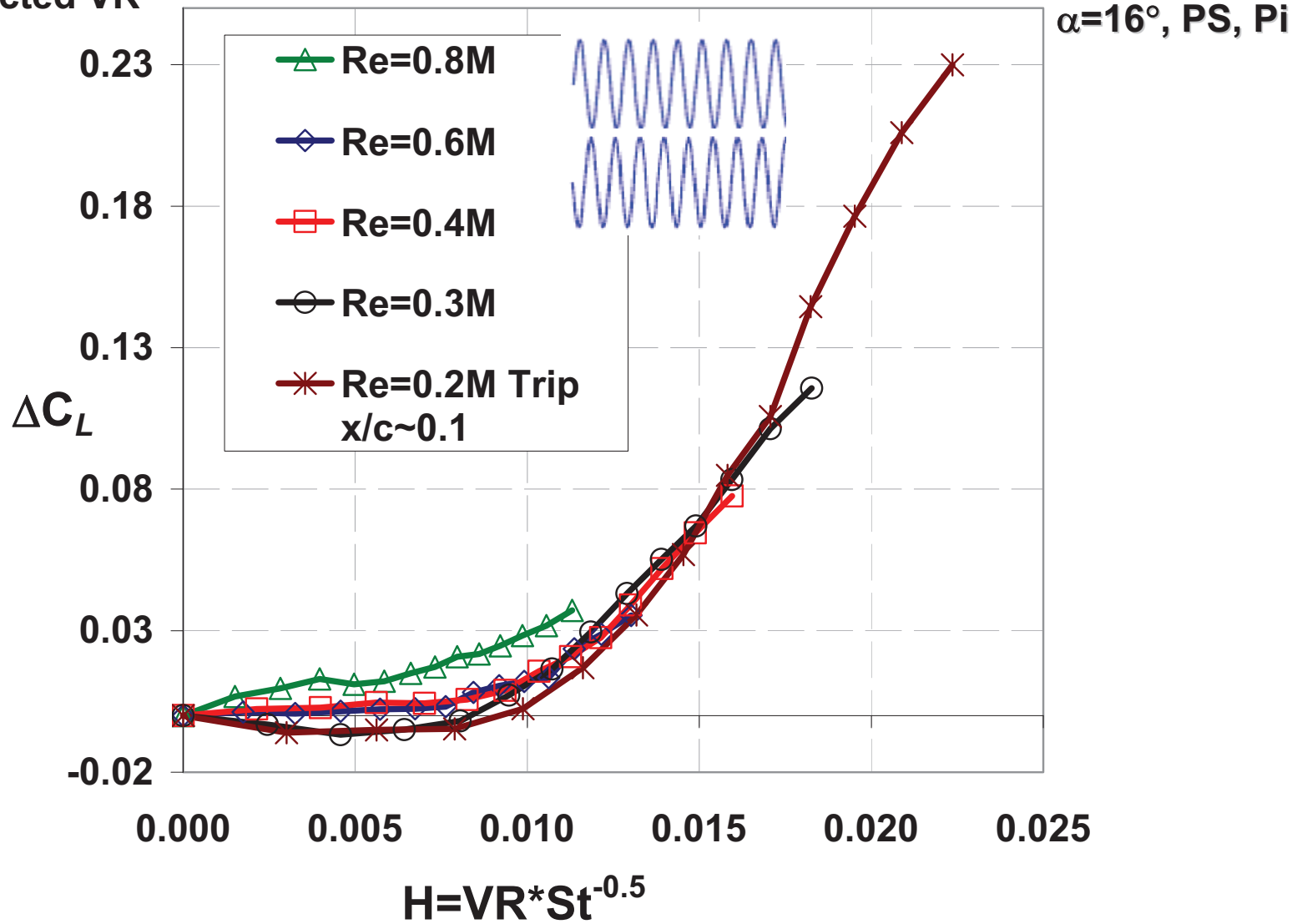




# High Frequency Amp Scaling



- St corrected VR

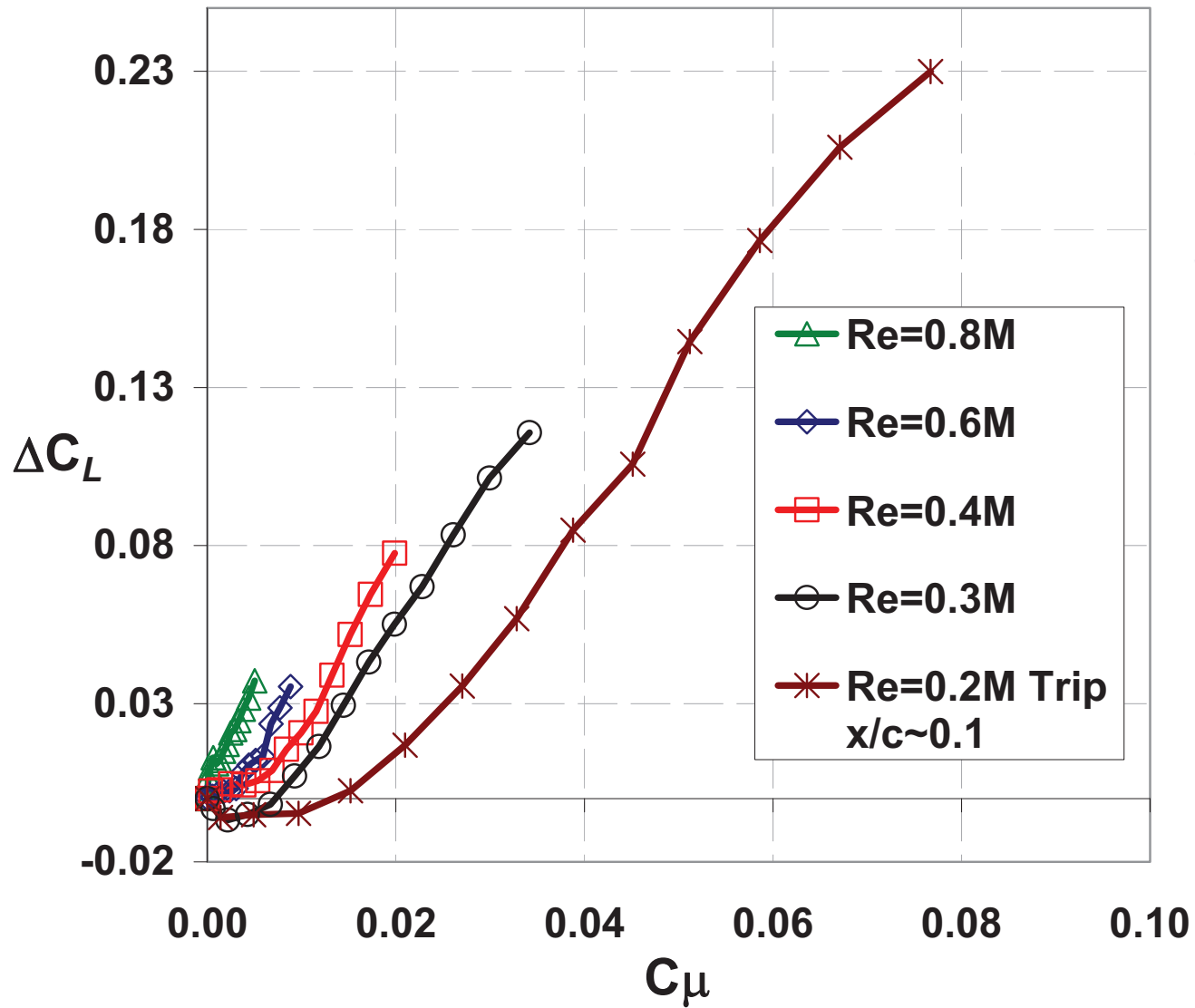




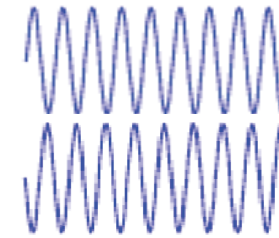
# High Frequency Amp Scaling



•  $C_\mu$



$\alpha=16^\circ$ , PS, Pi

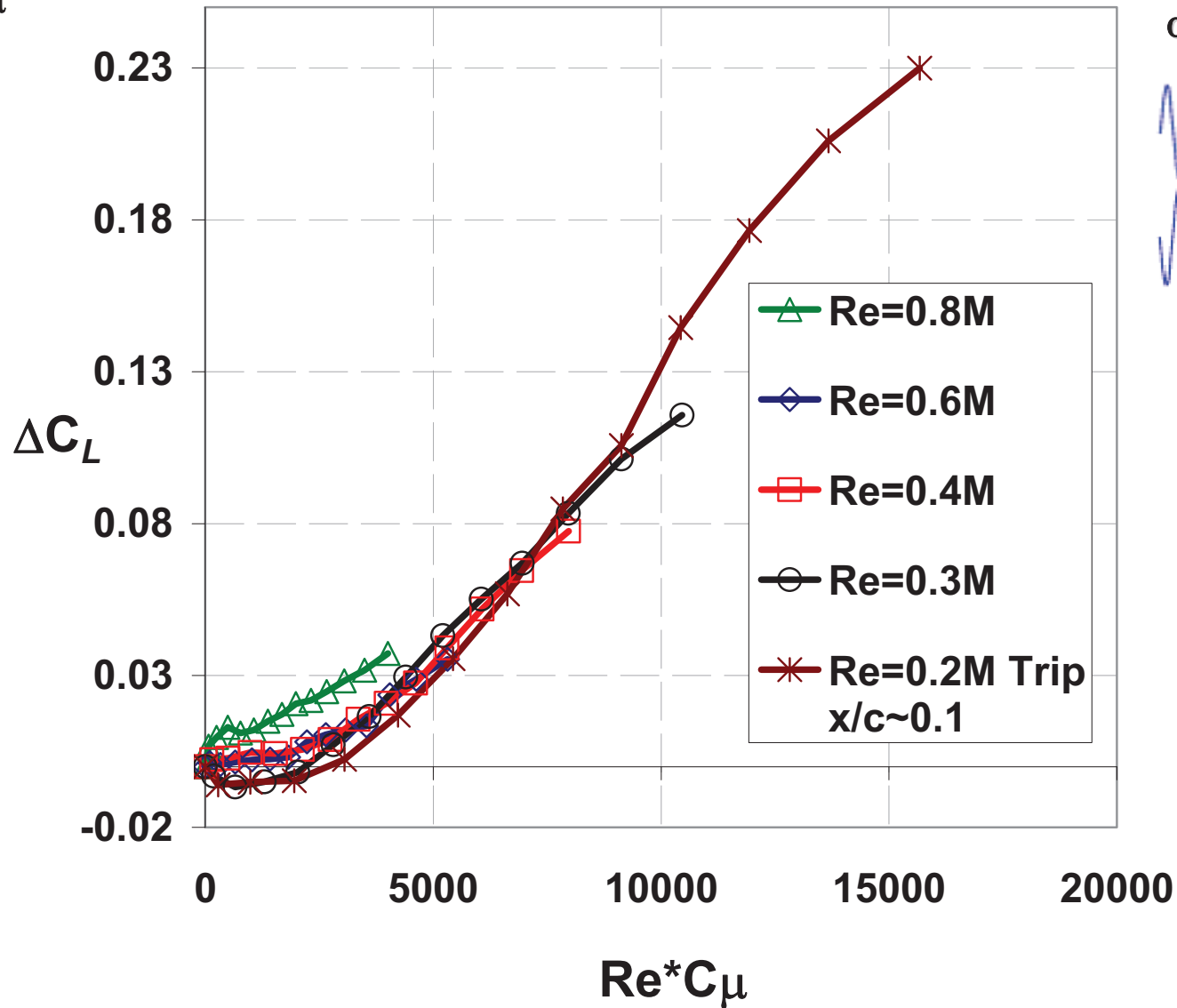




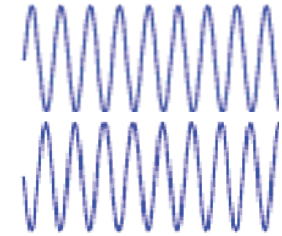
# High Frequency Amp Scaling



•  $Re \cdot C_{\mu}$



$\alpha=16^\circ$ , PS, Pi

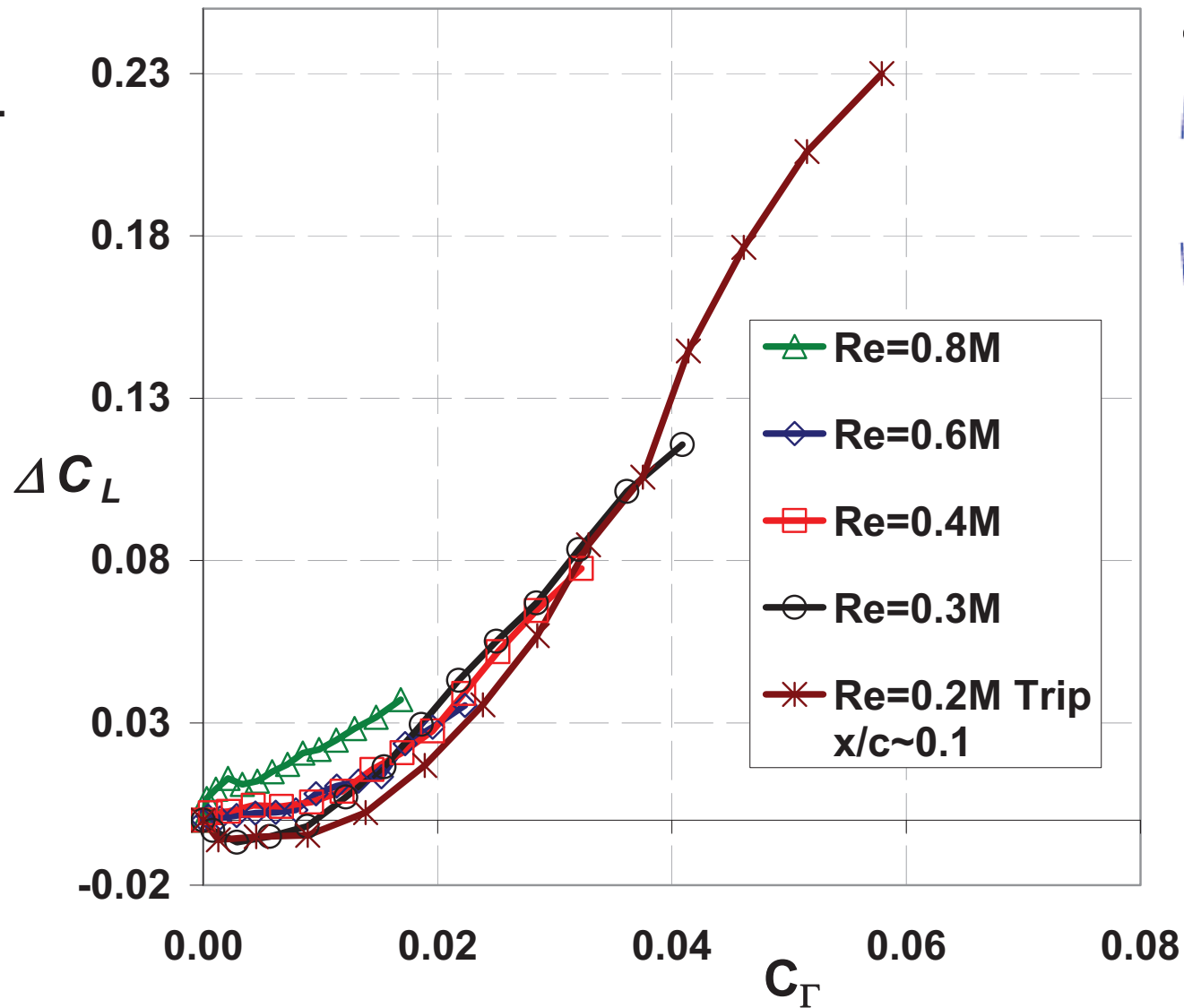




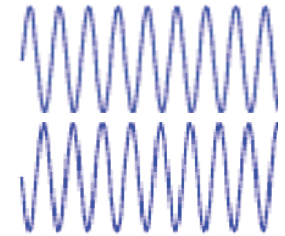
# High Frequency Amp Scaling



- Vort. Flux Coeff.



$\alpha=16^\circ$ , PS, Pi





# Amplitude Scaling Summary



		$F^+=1$	$F^+>10$
<ul style="list-style-type: none"> <li>Velocity ratio (VR)</li> </ul>	$VR \equiv \frac{U_p}{U_e} \approx \frac{U_p}{U_\infty}$	X	X
<ul style="list-style-type: none"> <li>Strouhal weighted VR (Nagib et al, 2006)</li> </ul>	$H \equiv \frac{VR}{\sqrt{S_t}}$	X	✓
<ul style="list-style-type: none"> <li>Momentum coefficient</li> </ul>	$C_\mu \equiv \frac{h}{c} (VR)^2$	X	X
<ul style="list-style-type: none"> <li>Reynolds corrected <math>C_\mu</math> <ul style="list-style-type: none"> <li><math>m=0.2</math> (Turb.), <math>m=0.5</math> (Lam.)</li> <li>used <math>m=1...</math></li> </ul> </li> </ul>	$C_{\mu,Re} \equiv \frac{h}{c} (VR)^2 Re^m$	~ ✓	✓
<ul style="list-style-type: none"> <li>Vorticity flux coeff.</li> </ul>	$C_\Gamma \equiv \frac{(VR)^2}{C_L S_t}$	X	✓



# Conclusions



- **Three existing and two new excitation magnitude scaling options for active separation control at Reynolds numbers below one Million.**
- **The physical background for the scaling options was discussed and their relevance was evaluated using two different sets of experimental data.**
- **For  $F^+ \sim 1$ , 2D excitation:**
  - The traditional  $VR$  and  $C_\mu$  - do not scale the data
  - Only the  $Re \cdot C_\mu$  is valid
- **This conclusion is also limited for positive lift increment.**
- **For  $F^+ > 10$ , 3D excitation, the  $Re$  corrected  $C_\mu$ , the  $St$  corrected velocity ratio and the vorticity flux coefficient, *all* scale the amplitudes equally well.**
- **Therefore, the Reynolds weighted  $C_\mu$  is the preferred choice, relevant to both excitation modes.**
- **Incidence also considered, using  $U_e$  from local  $C_p$**



# Vorticity flux ratio - 4



- **Actuators also generate vorticity flux and alter circulation**

$$C_{VF} \equiv \frac{\left[ U_p(t, y) \frac{dU_p(t, y)}{dy} \right]_{\max}}{\left[ U_{BL}(y) \frac{dU_{BL}(y)}{dy} \right]_{\max}} \approx \frac{U_p^2 \theta}{h/2 U_e^2} = \frac{2\theta}{h} \left( \frac{U_p}{U_e} \right)^2 \approx \frac{0.01c}{h} \left( \frac{U_p}{U_e} \right)^2$$

- **While the momentum coefficient**
- **For**  $h/c = 0.005$  (and  $\theta/c = 0.005$ )

$$C_\mu \equiv \frac{2h}{c} \left( \frac{U_p}{U_e} \right)^2$$

- **So the ratio**  $C_{VF}/C_\mu \equiv \frac{0.01c}{h} \bigg/ \frac{2h}{c} = \frac{0.005c^2}{h^2} \approx \frac{5 \times 10^{-3}}{2.5 \times 10^{-5}} = 200$
- **Is very large; define *Vorticity Flux Coefficient***

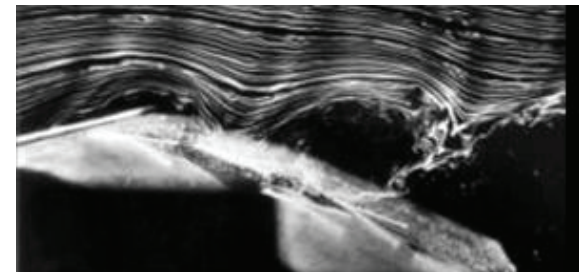




# AFC Open Forum: **Actuators Comparison Criteria**

**Avraham “Avi” Seifert**

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Faculty of Engineering, Tel-Aviv University, ISRAEL**



## **Acknowledgment:**

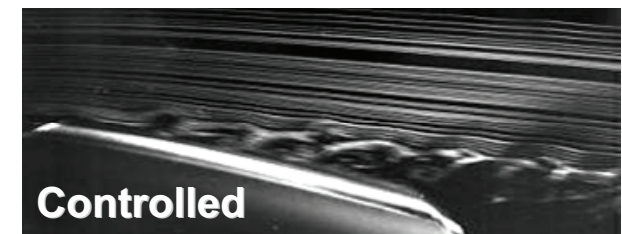
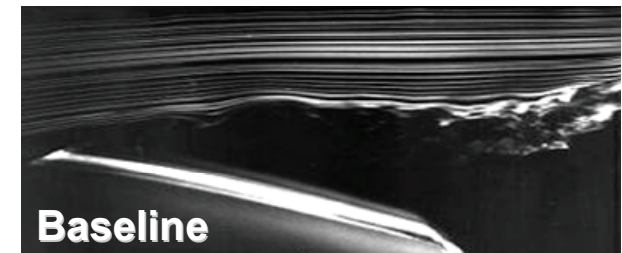
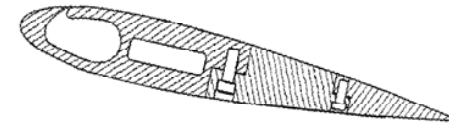
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I. Dayan, S. Paster, E. Nevo, Meadow Aero Lab members**



# Motivation



- **Active control of boundary layer separation**
- **Actuation: key enabling technology**
- **Many actuator types exist**
- **No accepted criteria for actuator comparison**
- **Rare to find:**
  - **Energy, efficiency, weight, cost data**



(Neuburger, '89,  $Re < 100k$ )



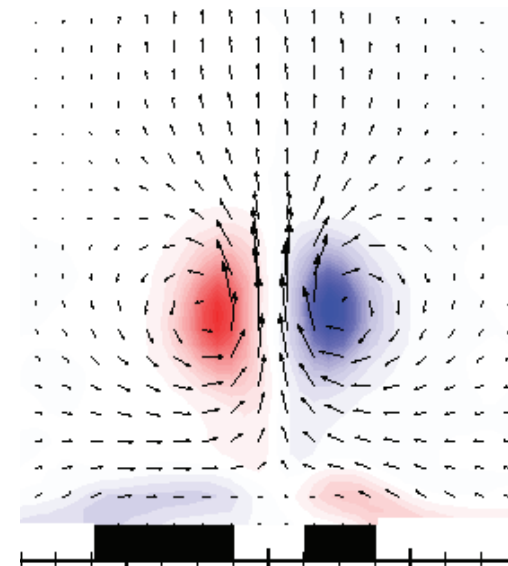
# Comparison criteria: OFM



- **Overall Figure of Merit**
- **Actuator operates in still air**
- $F_a$  – force generated
- When not/can not be measured could be estimated by
- With  $C$  from 0.25 to 0.5 (blowing only, velocity profile)
- $U_p$  - peak generated velocity
- $W_a$  – actuator weight
- $P$  – actuator energy consumption
  - Electric, fluidic, combined

$$OFM \equiv \frac{F_a^2 U_p}{W_a P}$$

$$F_a \approx C \rho A_a U_p^2$$



(Yehoshua) <sup>27</sup>



# Comparison criteria: AFM-1



- **Aerodynamic Figure of Merit (1)**

$$AFM1 \equiv \frac{U_{\infty} L_c / (U_{\infty} D_c + P)}{\left( \frac{L}{D} \right)_{baseline}}$$

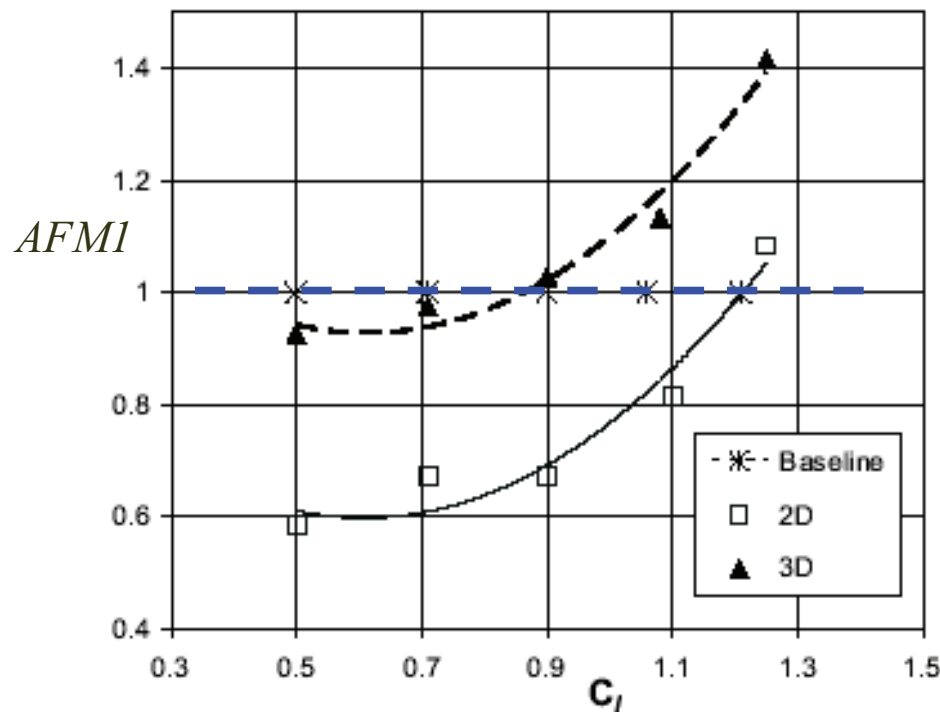
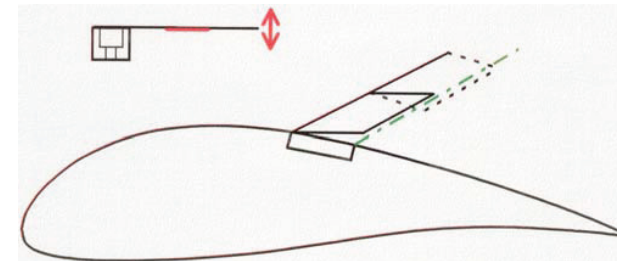
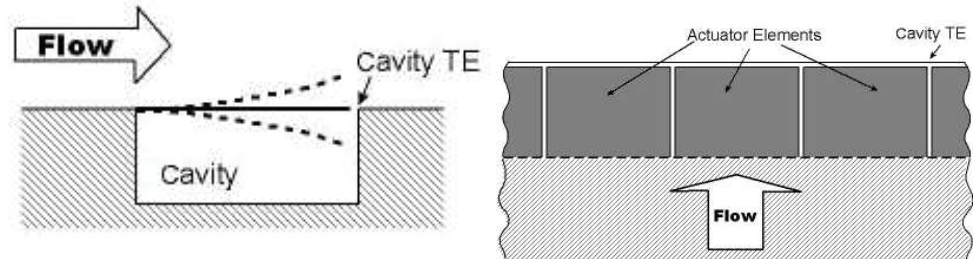
- **Application, actuators and flow condition dependent**
- $U_{\infty}$  – Free-stream velocity
- $L$  – lift (baseline or controlled)
- $D$  – Drag (baseline or controlled)
- $P$  – actuator energy consumption
- **Situation:** Have system and actuators
- **Question:** Direct energy into power-plant or actuators?
- **Answer:** Only when  $AFM1 > 1$  operate actuators



# AFM-1 Example: 3D PZE



- Low Re Control of separation
- TAU Developed piezo-benders
- Considered energy efficiency
- Found that 3D excitation more effective than 2D



$$AFM1 \equiv \frac{U_\infty L_c / (U_\infty D_c + P_a)}{\left(\frac{L}{D}\right)_{baseline}}$$

(Seifert et al, '99)



# Comparison criteria: AFM-2



- **Aerodynamic Figure of Merit (2)**

$$AFM2 \equiv \frac{U_{\infty} (L_c - W_a) / (U_{\infty} D_c + P)}{\left(\frac{L}{D}\right)_{baseline}}$$

- **Application, actuators and flow condition dependent**
- $U_{\infty}$  – Free-stream velocity
- $L$  – lift (baseline or controlled)
- $D$  – Drag (baseline or controlled)
- $W_a$  – weight of actuation system (incl. drivers, cables...)
- $P$  – actuation SYSTEM energy consumption
- **Situation:** Scaled  $AFM1 > 1$  and actuation system weight known (or predicted)
- **Question:** Should we include actuation in system?
- **Answer:** only when  $AFM2 > 1$  (probably 1.1 minimum)



# Actuation Methods



**(Not a tutorial nor a comprehensive review)**

- **External**
  - Speakers on tunnel walls
  - Speakers in cavities
  - Mechanical rotary
  - Mechanical – pneumatic
  - Ribbons + shakers
- **Internal...**

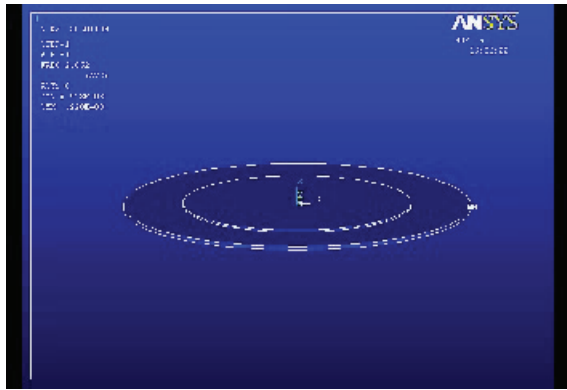




# ZNMF Piezo Actuator Operation

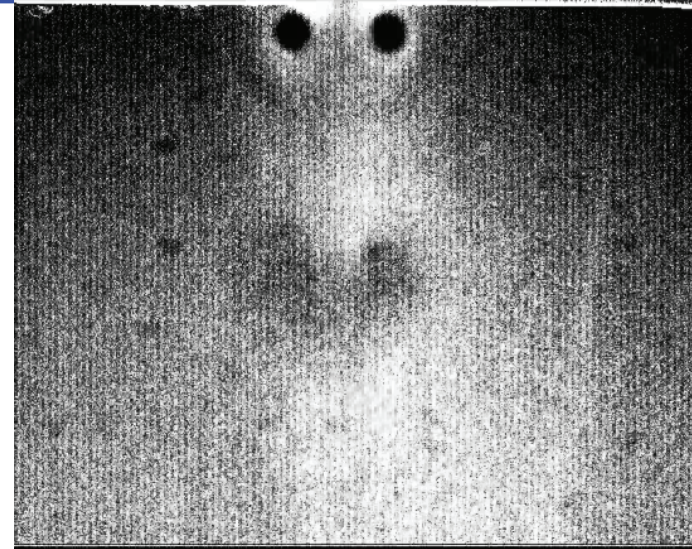


1St mode - Membrane

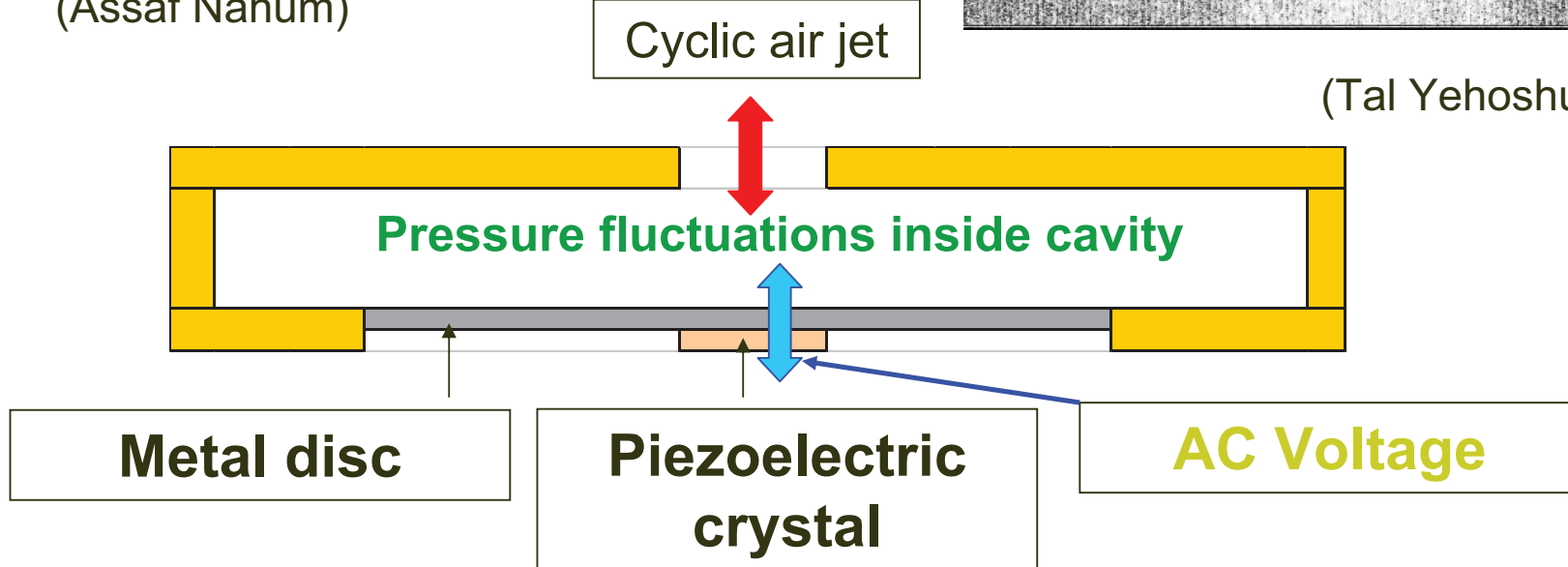


(Assaf Nahum)

**Zero  
Net  
Mass  
Flux**



(Tal Yehoshua)



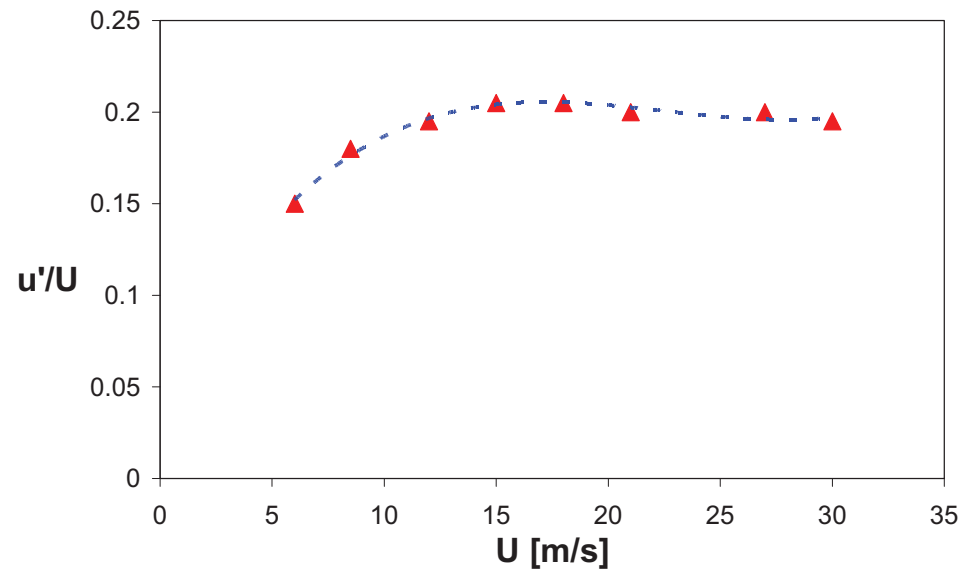
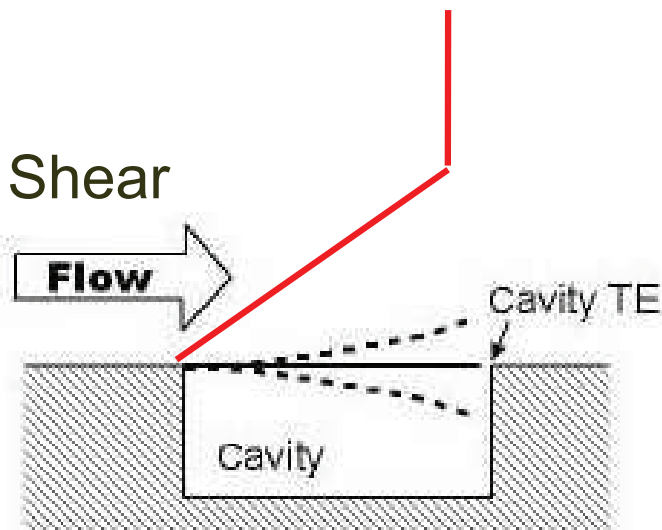




# Surface Mechanical Actuators



- Requirement: Sufficient control authority (...any type)
- Type (affecting method and feasibility of characterization)
- Mechanical: Amplitude, Mode shape...
- Micro balloons, micro flaps...



(Seifert et al., 1998, *AIAA J.*, V. 36, N. 8.)



# Combustion actuator

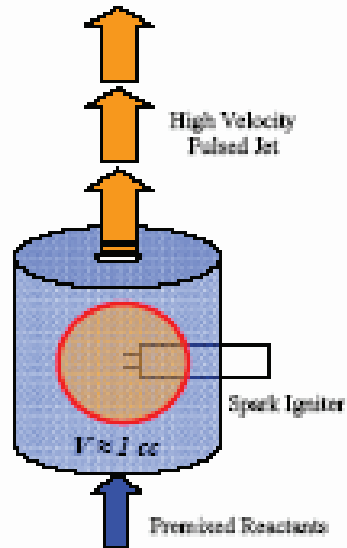
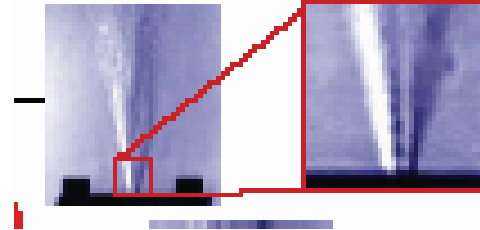


Figure 1. Schematic illustration of combustion-driven jet actuator



## Microfabricated, Combustion-Driven Jet Actuators for Flow Control Applications

T. Crittenden and A. Glezer

*Woodruff School of Mechanical Engineering*

*801 Ferst Drive N.W.*

E. Birdsell and M. Allen

*School of Electrical and Computer Engineering*

*777 Atlantic Drive N.W.*

*Georgia Institute of Technology, Atlanta, GA, USA 30332*



# Surface Plasma actuator

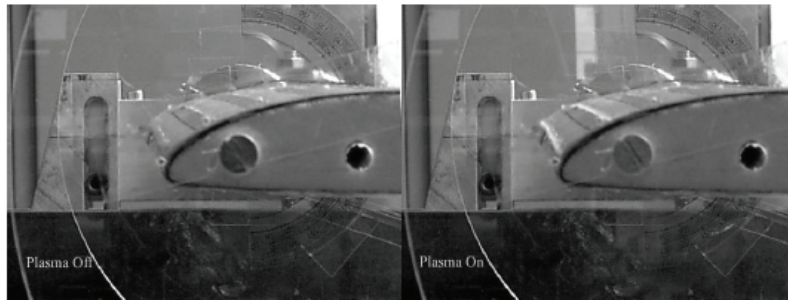
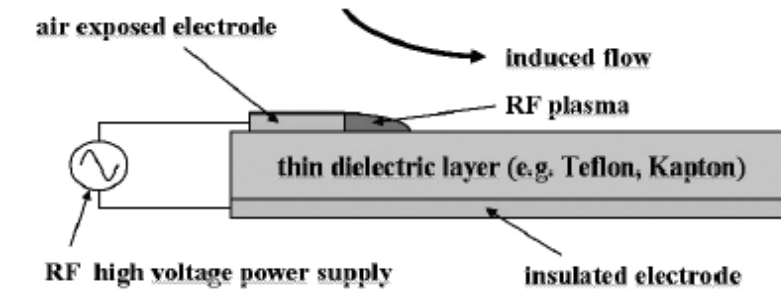


Figure 4 Two activated plasma actuators with 180° phase shift on the leading edge

Actu power – 17W/m

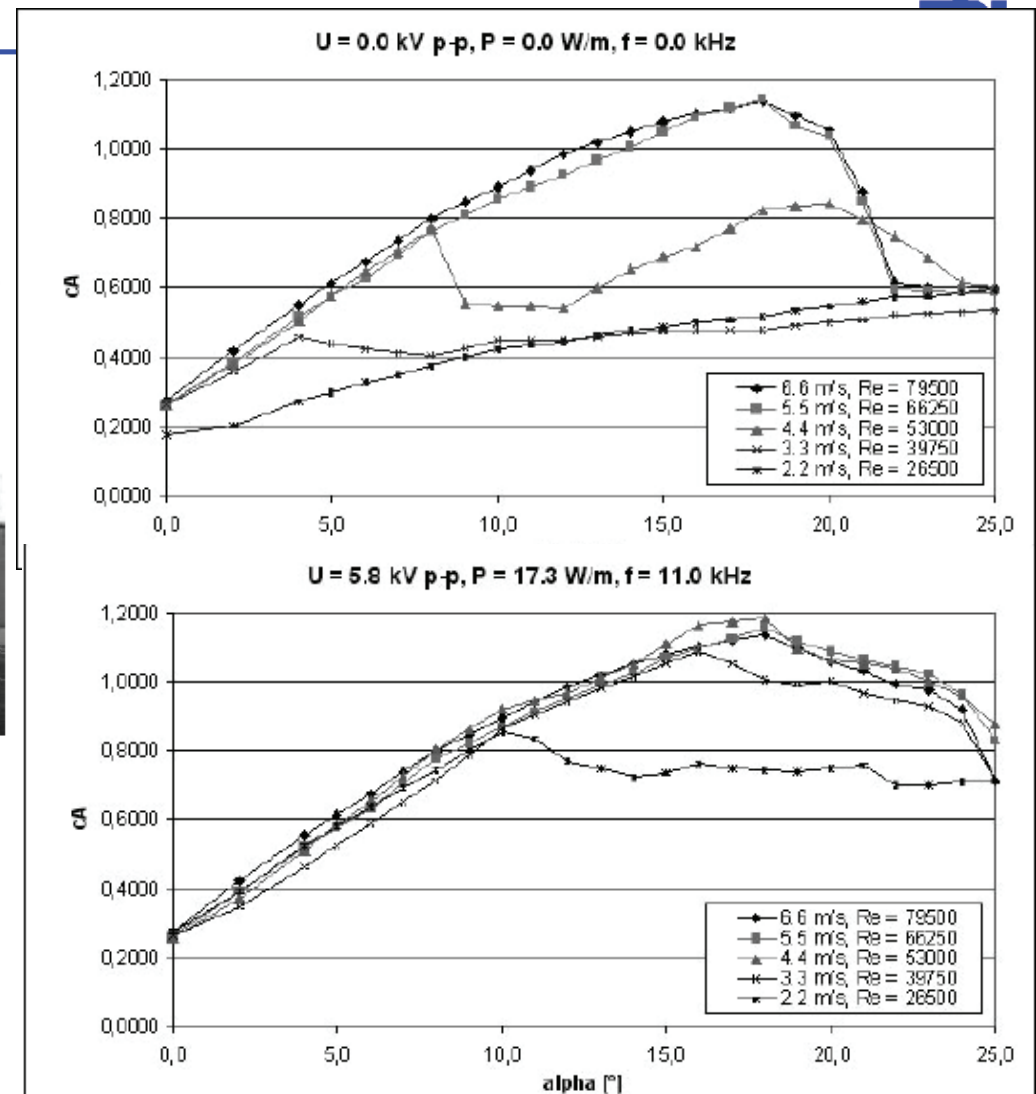
$U_{inf}=2-6\text{m/s}$

Plasma  $U_p=2-4\text{m/s}$

Lift recovery for  $Re \leq 50k$

No drag data

$1/2\rho U^3=4.4\text{Watt}$



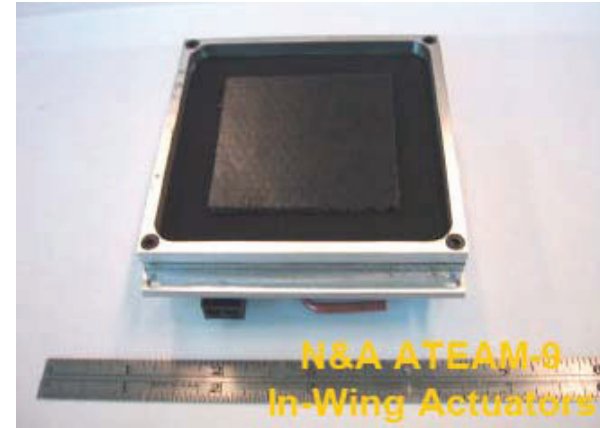
Active Flow Control by Surface Smooth Plasma Actuators

B. GÖKSEL, I. RECHENBERG, TUB

# Electro Magnetic actuator (XV-15)



NASA/CP-2010-216112



Actu power – 1000W/m  
Up=80m/s  
Wa>3kg



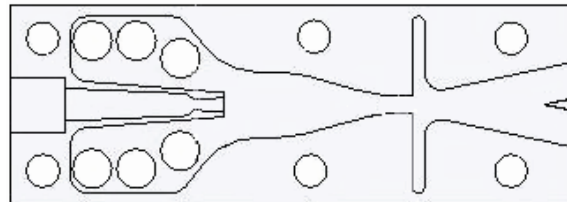
[http://fdrc.iit.edu/research/docs/MAFC\\_XV\\_15\\_Briefing\\_Final.pdf](http://fdrc.iit.edu/research/docs/MAFC_XV_15_Briefing_Final.pdf)

340



# TAU

## Suction and Oscillatory Blowing (SaOB) Actuator

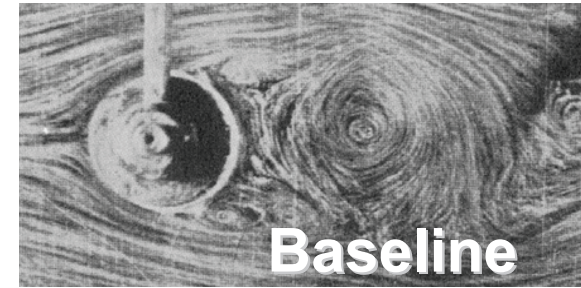




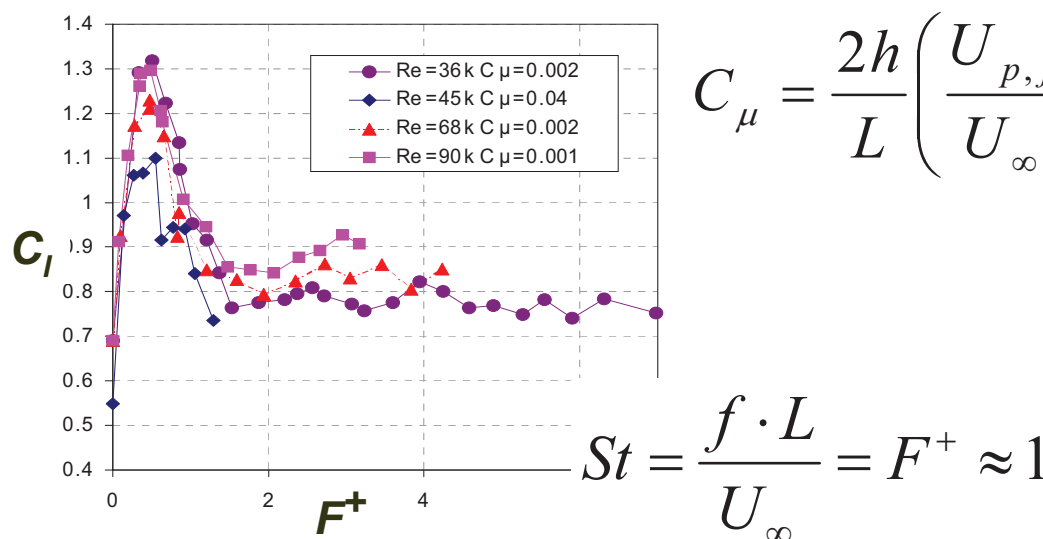
# Background



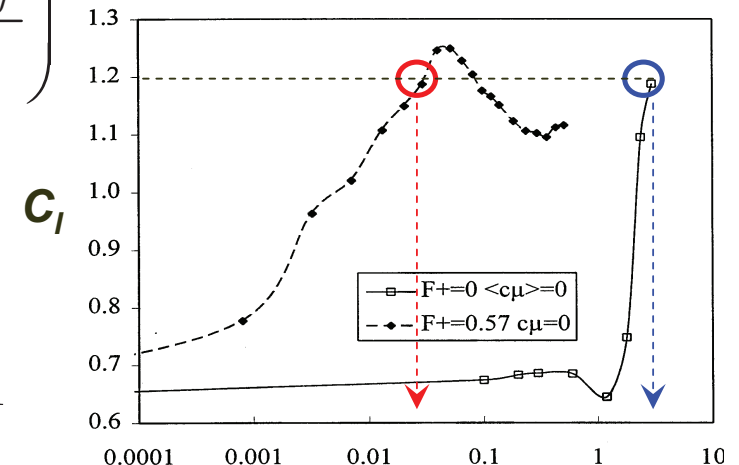
- Boundary layer separation control by steady suction (note date...)
- Steady, wall tangential blowing
- Oscillatory blowing (directed ZMF)
- The importance of flow instability for efficient AFC



(Prandtl, 1904)



(Yom-Tov & Seifert, '05)



$C_\mu$  [%] (Seifert et al, '96)<sub>B8</sub>

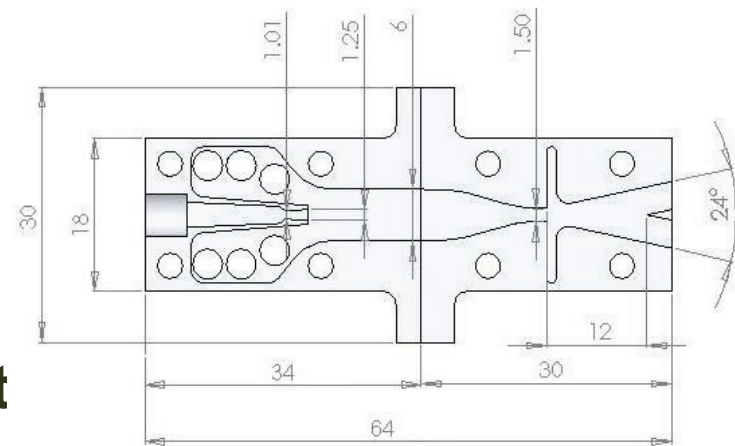




# The SaOB actuator concept



- G. Arwatz (MSc), I. Fono, London MEMS IUTAM, Sep '06
- Available ZNMF devices limited to  $M=0.3$
- Suction and oscillatory blowing – high potential for efficient AFC
- **Combination of *steady suction and oscillatory blowing in one device***
- High velocity, near sonic, output
- Wide range of output frequencies
- Enables 3D excitation
- Frequency proportional to flow rate
- No moving parts
- Low power consumption



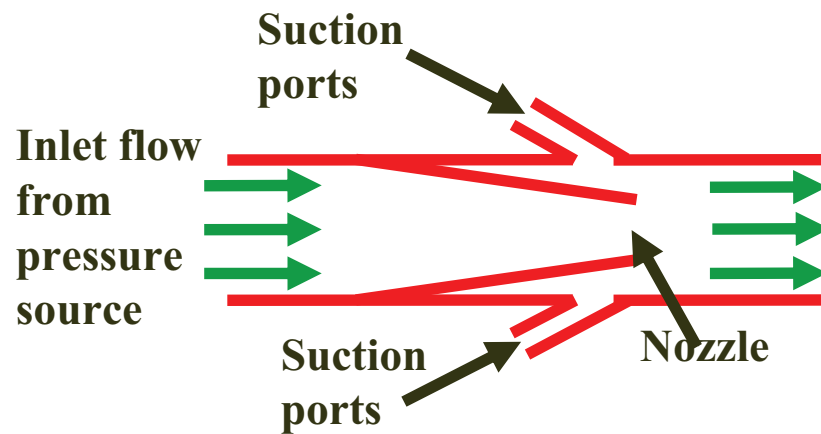


# The SaOB actuator concept

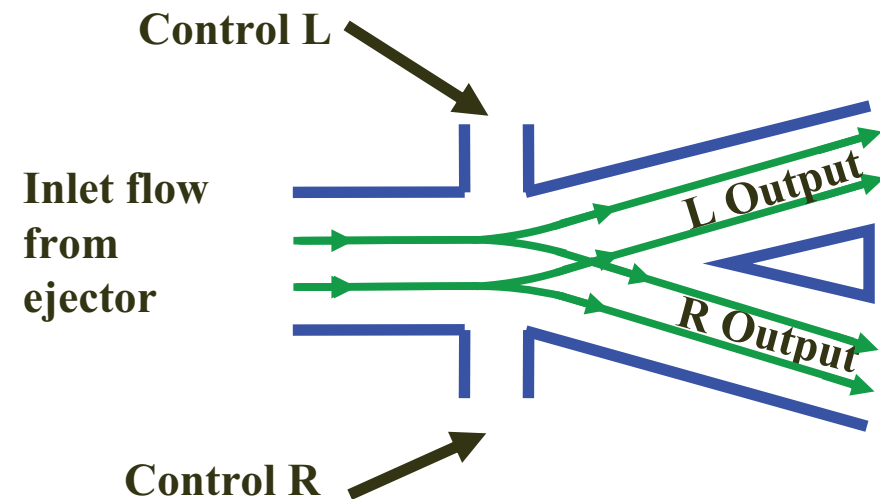


- Combination of ejector and switching valve

## Ejector (steady suction)



## Bi-stable fluidic amplifier (oscillatory blowing)



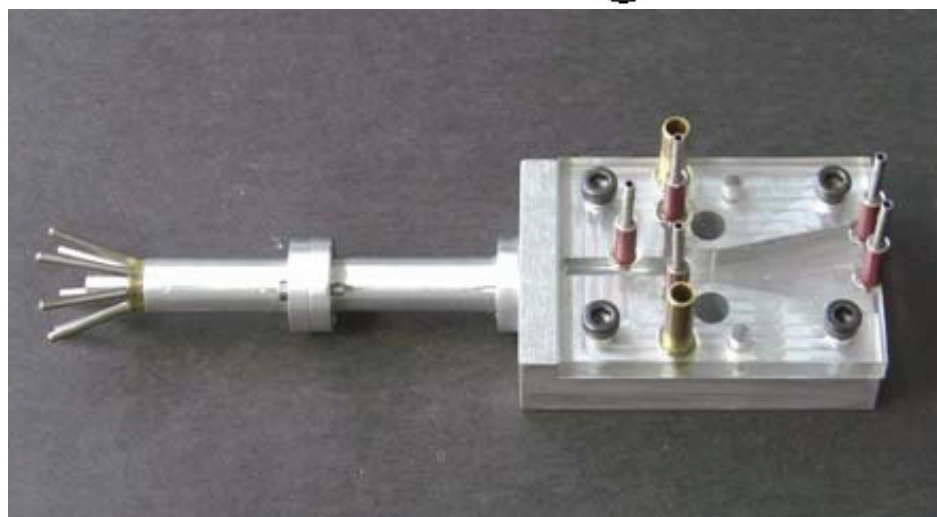
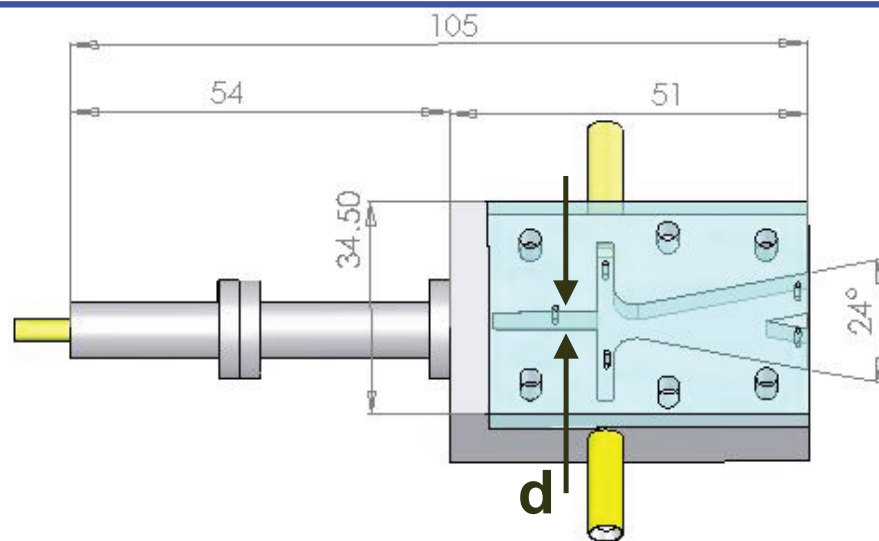




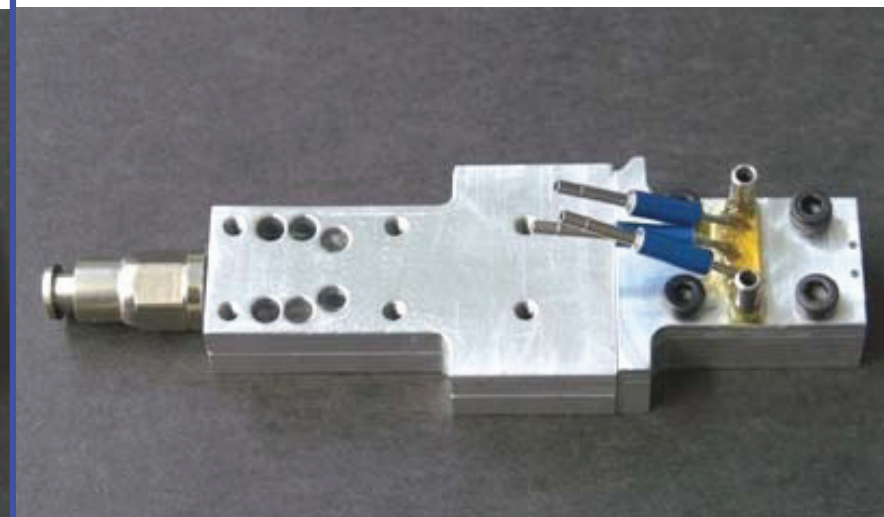
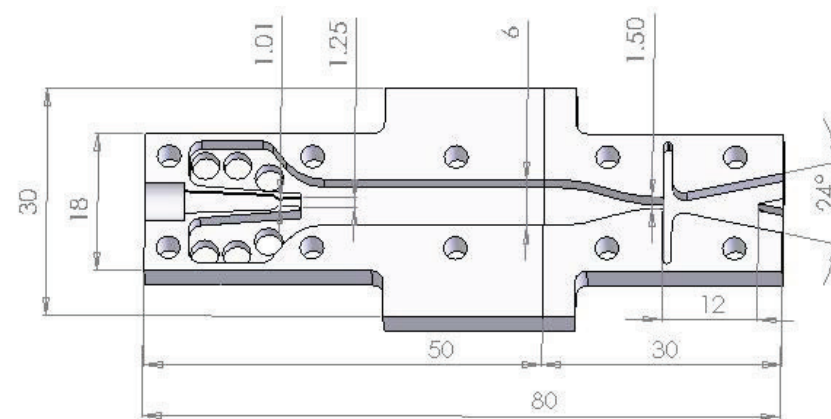
# Valve generations, 2nd & 3rd



## Medium scale $d=3\text{mm}$



## Small scale $d=1.5\text{mm}$





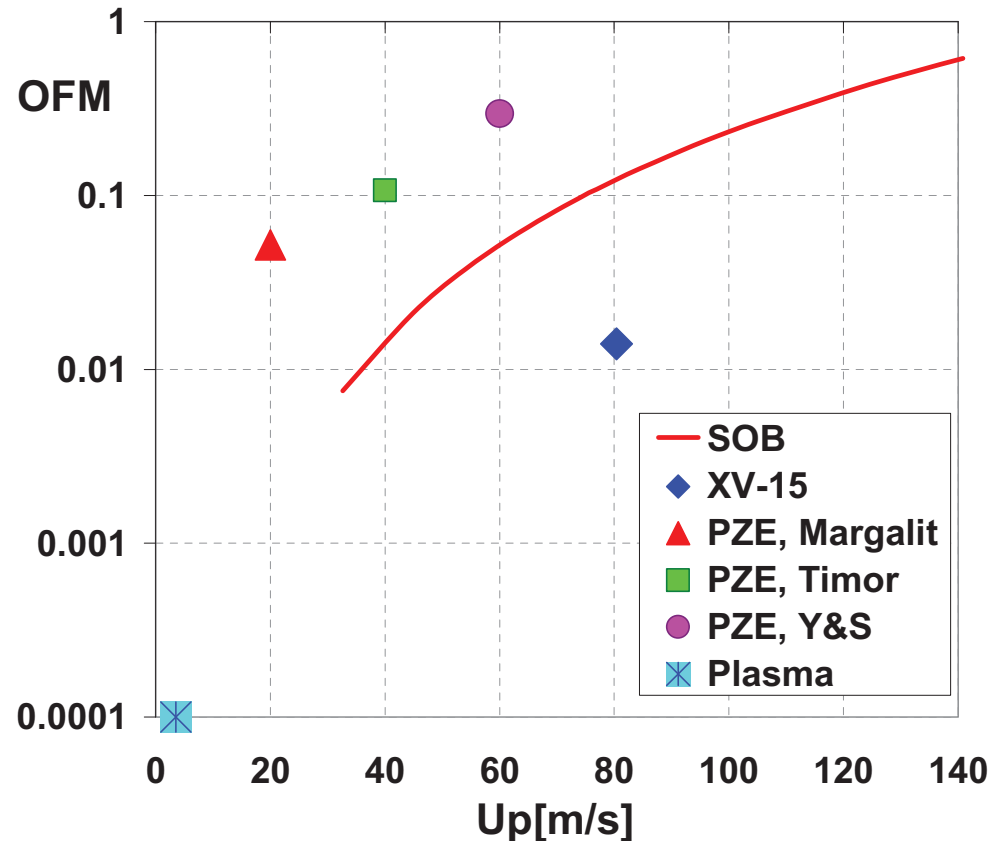
# Actuators' Efficiency



- Overall Figure of Merit

$$OFM = \frac{F_a^2 U_p}{W_a P_a}$$

- Still air operation
- SaOB weight - 15 gm
- Thrust-suction+blowing
- Note: OFM Log scale



# Summary (Actuators)



- **Actuator comparison criteria suggested**
- **Overall and Aerodynamic figures of merit**
- **New actuator for steady suction and oscillatory blowing was developed, modeled and characterized**
- **OFM for ZNMF, Plasma and SaOB actuators compared**
- **Rare to find data for AFM (Need: Weight, power, Up, L, D)**
- **Please measure and publish**