

# WHAT ARE THE PROGENITORS OF COMPACT, MASSIVE, QUIESCENT GALAXIES AT $z = 2.3$ ? THE POPULATION OF MASSIVE GALAXIES AT $z > 3$ FROM NMBS AND CANDELS

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## ABSTRACT

Using public data from the NEWFIRM Medium-Band Survey (NMBS) and the Cosmic Assembly Near-Infrared Deep Extragalactic Legacy Survey (CANDELS), we investigate the population of massive galaxies at  $z > 3$ . The main aim of this work is to identify the potential progenitors of  $z \sim 2$  compact, massive, quiescent galaxies (CMQGs), furthering our understanding of the onset and evolution of massive galaxies. Our work is enabled by high-resolution images from CANDELS data and accurate photometric redshifts, stellar masses, and star formation rates (SFRs) from 37-band NMBS photometry. The total number of massive galaxies at  $z > 3$  is consistent with the number of massive, quiescent galaxies (MQGs) at  $z \sim 2$ , implying that the SFRs for all of these galaxies must be much lower by  $z \sim 2$ . We discover four CMQGs at  $z > 3$ , pushing back the time for which such galaxies have been observed. However, the volume density for these galaxies is significantly less than that of galaxies at  $z < 2$  with similar masses, SFRs, and sizes, implying that additional CMQGs must be created in the intervening  $\sim 1$  Gyr between  $z = 3$  and  $z = 2$ . We find five star-forming galaxies at  $z \sim 3$  that are compact ( $R_e < 1.4$  kpc) and have stellar mass  $M_* > 10^{10.6} M_\odot$ ; these galaxies are likely to become members of the massive, quiescent, compact galaxy population at  $z \sim 2$ . We evolve the stellar masses and SFRs of each individual  $z > 3$  galaxy adopting five different star formation histories (SFHs) and studying the resulting population of massive galaxies at  $z = 2.3$ . We find that declining or truncated SFHs are necessary to match the observed number density of MQGs at  $z \sim 2$ , whereas a constant delayed-exponential SFH would result in a number density significantly smaller than observed. All of our assumed SFHs imply number densities of CMQGs at  $z \sim 2$  that are consistent with the observed number density. Better agreement with the observed number density of CMQGs at  $z \sim 2$  is obtained if merging is included in the analysis and better still if star formation quenching is assumed to shortly follow the merging event, as implied by recent models of the formation of MQGs.

*Key words:* galaxies: evolution – galaxies: fundamental parameters – galaxies: high-redshift – galaxies: structure

*Online-only material:* color figures

## 1. INTRODUCTION

The population of galaxies in the Local Universe presents a clear bi-modality, as evidenced by color–magnitude diagrams (e.g., Baldry et al. 2004; Kauffmann et al. 2004), with galaxies either living on the red sequence or in the blue cloud. This bi-modality is further supported by tight correlations between the main physical properties of each class (e.g., Tully & Fisher 1977; Kormendy & Djorgovski 1989). Galaxies on the red sequence typically are massive and quiescent (i.e., with low or no ongoing star formation) with early-type morphologies, while galaxies in the blue cloud are less massive, with higher star formation rates (SFRs) and have spiral or irregular morphologies.

The physical mechanisms driving the onset of the observed bi-modality are one of the main open issues in the study of galaxy formation. At high redshift the observational picture is complicated by the lack of a common definition for massive, quiescent galaxies (MQGs) in the literature (see discussion in Saracco et al. 2012).

Samples selected according to the spectral energy distribution (SED) show that massive (i.e., stellar mass  $M_* \gtrsim 10^{11} M_\odot$ ) and quiescent (i.e., specific star formation rate  $s\text{SFR} \lesssim 10^{-11} - 10^{-10} \text{ yr}^{-1}$ ) galaxies were already in place at

$z \sim 2$  (Franx et al. 2003; Daddi et al. 2005; Kriek et al. 2006; Cimatti et al. 2008). Their number density has grown by almost a factor of 10 since  $z = 3$  (Labbé et al. 2005; Arnouts et al. 2007; Fontana et al. 2009; Taylor et al. 2009; Ilbert et al. 2010; Cassata et al. 2011; Brammer et al. 2011; Domínguez Sánchez et al. 2011; Bell et al. 2012), although most of the evolution occurred at  $z > 1$  (e.g., Pozzetti et al. 2007).

In addition to rapid number density evolution, the sizes of MQGs have evolved dramatically from high redshift to the present day. Most of MQGs at  $z > 1.5$  are also compact systems: the observed effective radii are generally a factor of  $\sim 3$ – $5$  smaller at  $z \sim 2.5$  (Daddi et al. 2005; Longhetti et al. 2007; Toft et al. 2007; Trujillo et al. 2007; van Dokkum et al. 2008; Cimatti et al. 2008; Saracco et al. 2009; van der Wel et al. 2008; Bezanson et al. 2009; Szomoru et al. 2012) than at  $z = 0$ , where such compact galaxies are almost entirely absent (Trujillo et al. 2009; Taylor et al. 2010).

There have been multiple attempts to explain the evolution of these objects and to place them into a broader cosmological context. In the so-called monolithic collapse scenario, MQGs would have assembled almost all of their stellar mass at high redshift, followed by a passive evolution of the stellar population. This class of models, however, foresees little or no evolution in size, in contrast to observations. More recent models describe the formation of MQGs as a two-stage process: gas-rich

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merger events generate compact, massive spheroids at  $z \gtrsim 3$ , while minor, dry (i.e., without formation of new stars) mergers at later cosmic times would increase the size, while responsible for only a small increase in stellar mass (Naab et al. 2007, 2009; Wuyts et al. 2010; Oser et al. 2012). Indeed, Bezanson et al. (2009) showed that the stellar mass density of the inner  $\sim 1$  kpc of  $z \sim 2$  galaxies does not substantially differ from that in present-day MQGs, suggesting that the growth during the second phase progresses from the inner region rapidly toward the external parts (the so-called inside-out growth; see, e.g., van Dokkum et al. 2010).

However, the picture is still far from being completely clear: detailed comparisons with  $\Lambda$ CDM models of dry merging show that some of the models predict descendants of  $z > 2$  too compact compared to the observed local MQGs (Cimatti et al. 2012). Recent studies have also revealed the existence of a large number of MQGs at  $z \sim 1.5$  with sizes similar to those of the local galaxies with comparable mass (Saracco et al. 2009, 2010; Mancini et al. 2010). If the population of MQGs at  $z \gtrsim 2.5$  includes only compact systems, this would imply a size evolution timescale of  $\approx 1$  Gyr, challenging the current models of formation of local MQGs (Saracco et al. 2010).

The main goal of this work is to identify, within an observational framework, the population of galaxies at  $z > 3$  which could give rise to the population of compact MQGs (CMQGs) observed at  $z = 2.3$ . We combine data from two public surveys, the NEWMFIRM Medium-Band Survey (NMBS; Whitaker et al. 2011) and the Cosmic Assembly Near-infrared Deep Extragalactic Legacy Survey (CANDELS; Grogin et al. 2011; Koekemoer et al. 2011). The NMBS provides accurate measurements of photometric redshifts ( $z_{\text{phot}}$ ), stellar masses ( $M_*$ ), and SFR, while robust morphologies and sizes were measured from the high-resolution imaging from CANDELS.

In Section 2, we describe the data sets used in our work, the measurements of the sizes, and the completeness in stellar mass. The results are presented in Section 3. We discuss our results in Section 4, and summarize them in Section 5.

Throughout this work, we use a concordance cosmology with  $H_0 = 70 \text{ Km s}^{-1} \text{ Mpc}^{-1}$ ,  $\Omega_m = 0.3$ , and  $\Omega_\Lambda = 0.7$ . All magnitudes are referred to the AB system.

## 2. DATA

We combined the photometric depth and the accurate measurements of photometric redshifts offered by the NMBS (van Dokkum et al. 2009; Whitaker et al. 2011) with the high-resolution *HST*/WFC3 deep NIR imaging from the CANDELS (Grogin et al. 2011; Koekemoer et al. 2011). These two surveys will be briefly described in the next two sections.

### 2.1. NMBS–COSMOS

The NMBS covers two fields: a  $27''.6 \times 27''.6$  pointing within the COSMOS field (Scoville et al. 2007) and a second pointing, of the same size, overlapping with part of the All-Wavelength Extended Groth Strip International Survey (AEGIS) strip (Davis et al. 2007). Only data from the COSMOS field were used, since the overlap between NMBS–AEGIS and CANDELS is minimal; using both fields the average improvement in cosmic variance would have been just 5%.

NMBS uses five medium-bandwidth filters in the NIR wavelength range 1–1.8  $\mu\text{m}$ . The bluest filter is similar to the *Y* band, the canonical *J* and *H* bands are split into two filters each. Such configuration pinpoints the location of the redshifted Balmer/

4000 Å breaks in  $1.5 < z < 3.5$  galaxies (van Dokkum et al. 2009) and enables photometric redshift measurements with an accuracy of  $\sigma_z/(1+z) \sim 2\%$  for objects in the redshift range  $1.5 < z < 3.5$  (Whitaker et al. 2011).

The full public catalog for the COSMOS field (Whitaker et al. 2011)<sup>6</sup> provides UV-to-24  $\mu\text{m}$  photometry for 31,306 *K*-selected sources based on the de-blended version, along with accurate photometric redshifts, rest-frame luminosities, SFRs, and stellar mass measurements. The redshifts and stellar masses were computed using 37 filters from the COSMOS fields, combining the NIR medium-bandwidth data with existing UV (*Galaxy Evolution Explorer*), visible and NIR (Canada–France–Hawaii Telescope and Subaru Telescope), and mid-IR (*Spitzer*/IRAC) imaging (Whitaker et al. 2011).

The catalog is complete at the 75% detection level for magnitudes brighter than  $K_S = 23.1\text{AB}$  (Whitaker et al. 2011); we selected objects brighter than  $K_S = 23.4$  mag, corresponding to a detection completeness of 50%.

### 2.2. CANDELS

CANDELS is a 902-orbit *Hubble Space Telescope* (*HST*) Multi-Cycle Treasury program aimed at probing the evolution of galaxies and black holes from  $z \sim 1.5$  to 8 and at detecting and studying Type Ia supernovae at  $z > 1.5$  in order to better constrain the nature of dark energy (Koekemoer et al. 2011).

The wide portion of the survey covers a total of  $\sim 800$  arcmin<sup>2</sup> down to  $H \simeq 26.5$  mag, spread over five fields: extended regions around the two GOODS fields, the Extended Groth Strip (EGS; Davis et al. 2007), COSMOS (Scoville et al. 2007), and the UKIDSS Ultra-Deep Survey (UDS; Lawrence et al. 2007).

We used the F160W as the filter for the measurement of the morphological parameters as it is the reddest band available with high-resolution imaging. At redshift  $z \sim 3$ , the F160W filter corresponds to the rest-frame *B* band.

### 2.3. Sample Selection

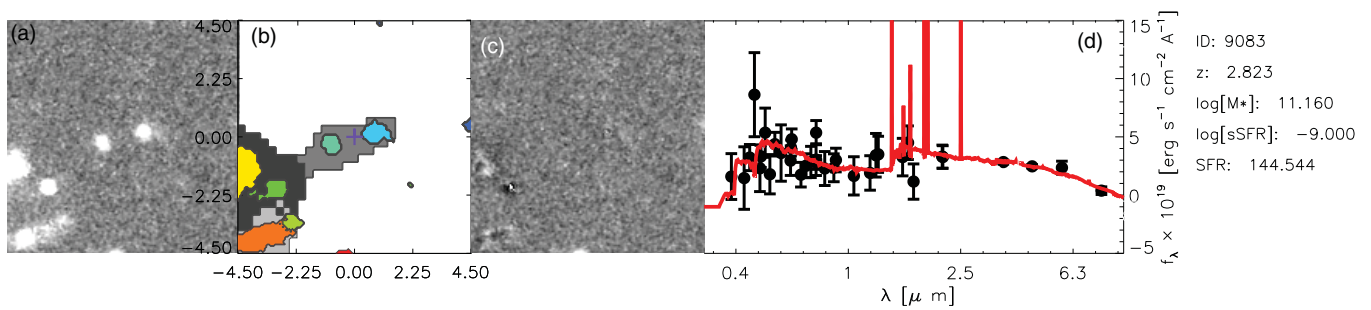
The FWHM of the point-spread function (PSF) on the CANDELS F160W images is  $\text{FWHM} \simeq 0''.17\text{--}0''.19$  (Koekemoer et al. 2011), a factor of  $\sim 6$  better than the *K*-band PSF in NMBS. This fact, together with the higher photometric depth compared to the NMBS survey, translates into a higher surface brightness sensitivity than NMBS.

From the full NMBS catalog we extracted those non-stellar objects and objects with a good quality flag (*star\_flag* = 0 and *use* = 1). We selected galaxies compatible with being at  $z > 3$  at the  $1\sigma$  level (i.e.,  $u_{68} > 3$ ). In this way, we selected a total of 613 galaxies.

The overlap of the CANDELS COSMOS image and the NMBS COSMOS field amounts to 192 arcmin<sup>2</sup>,  $\sim 20\%$  of the original NMBS field. This reduces the sample of  $z > 3$  galaxies available to the measurement of the morphological parameters to 133 sources.

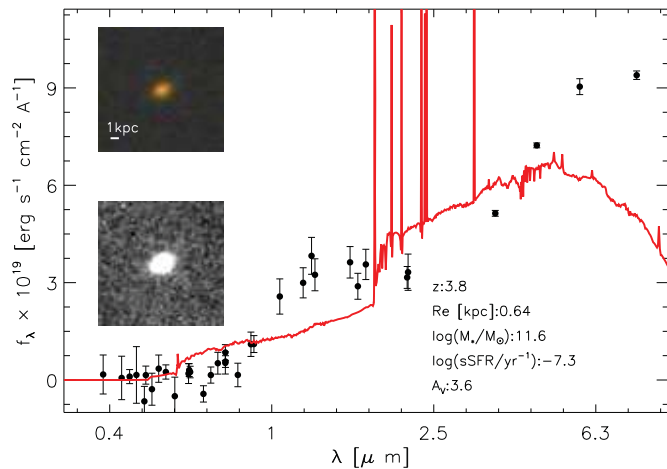
The availability of CANDELS data allowed us to accurately measure the morphological parameters of our  $z > 3$  galaxies and to identify potentially blended objects, which appear as single sources in the NMBS catalog. In Figure 1, we show an example of the importance of high-resolution imaging, which allowed us to identify those cases in which blended and/or very close objects could affect the measurement of the SED, with consequently unreliable photometric redshifts and stellar

<sup>6</sup> Catalogs can be downloaded from [http://www.astro.yale.edu/nmbs/Data\\_Products.html](http://www.astro.yale.edu/nmbs/Data_Products.html).



**Figure 1.** Example of the need for high-resolution images such as those from CANDELS in identifying blended objects in lower resolution images. From left to right: (a) tile from the F160W CANDELS image; (b) segmentation map from NMBS (gray scale) and from the F160W CANDELS frame (colored spots); the purple + indicates the center of the NMBS source, which is the center of the frame; the axis values are in arcseconds relative to the center of the tile; (c) residual image from GALFIT after fitting all sources simultaneously; the pixel scale for the one here plotted were excluded from the analysis. (d) Observed SED from NMBS (black points with error bars) and SED fit from EAZY (solid red line). The blended objects like the one here plotted were excluded from the analysis.

(A color version of this figure is available in the online journal.)



**Figure 2.** Observed SED from NMBS (black points), EAZY best-fitting SED (solid red curve) for a possible AGN. A color cutout created from the F814W, F125W, and F160W CANDELS filters is shown in the top left corner, while a cutout from CANDELS F160W image is presented at the bottom left. The angular size for both cutouts is  $3''.7 \times 3''.7$ . Objects like the one plotted here were excluded from the sample.

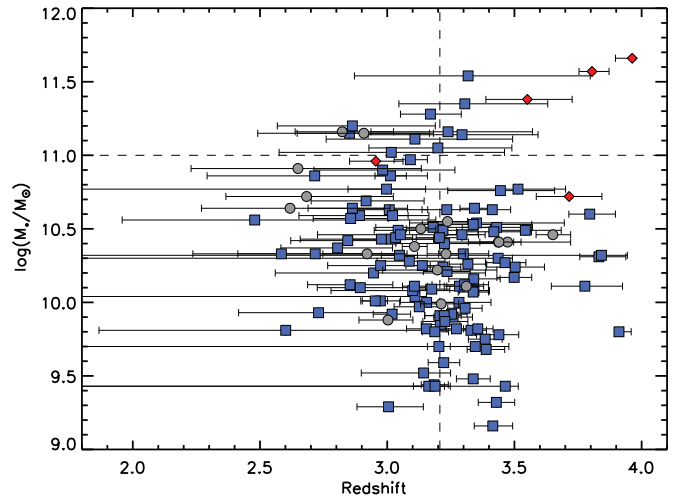
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population properties (e.g., stellar masses, SFRs). For these reasons, blended objects were excluded from our final analysis. We also visually inspected the 133 SEDs of the  $z > 3$  galaxies and excluded from the sample those showing the presence of a possible active galactic nucleus (AGN; an example of which is presented in Figure 2). The fraction of such objects in the whole sample of 133 galaxies summed to 4%.

The final catalog includes 110 galaxies. The distribution of  $M_*$  with  $z_{\text{phot}}$  for the final sample is presented in Figure 3. The median redshift and redshift uncertainty for the full sample are  $z_{\text{tot}} = 3.2$  and  $0.1$ , respectively; similarly, for the  $M_* > 10^{11} M_{\odot}$  subsample, we have  $z_M = 3.2 \pm 0.3$ . The plot also shows that out of the 10 objects with redshift compatible with  $z \sim 2.3$ , none of them has a stellar mass  $M_* > 10^{11} M_{\odot}$ , increasing our confidence in the adopted redshift selection criteria.

#### 2.4. Size Measurement

The luminosity profile of each galaxy was fit by a single Sérsic (1968) profile, using the GALFIT (Peng et al. 2002, 2010) program. This code fits two-dimensional analytic functions directly to images after convolving the profile with a PSF. All size measurements were done on the F160W CANDELS image.



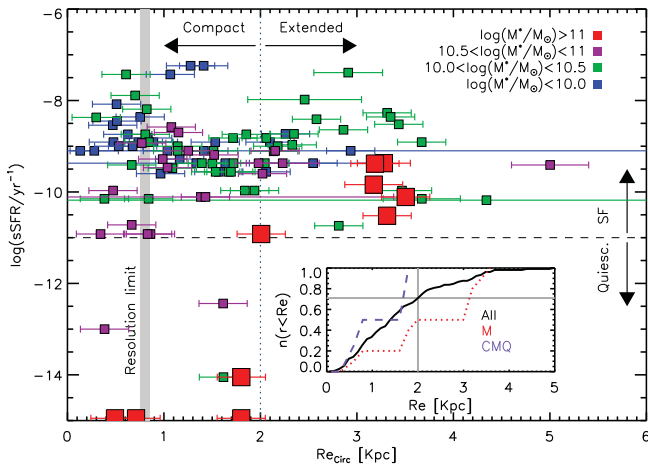
**Figure 3.** Stellar mass as a function of redshift for the 110 galaxies constituting our final sample (blue filled squares), after cleaning for blended objects (gray filled circles), and possible AGNs (red filled diamonds). The error bars in redshift encompass the 68% confidence level, as estimated by EAZY. The median redshift of  $M_* > 10^{11} M_{\odot}$  galaxies is 3.2, and it is marked by the vertical dashed line. All  $M_* > 10^{11} M_{\odot}$  galaxies, selected to possibly lie at  $z > 3$ , have a redshift  $z > 2.5$  at a 68% confidence level. This gives us confidence that our selection is not including  $z \sim 2$  galaxies with very broad redshift probability distributions.

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A zero-order set of morphological parameters was obtained via SExtractor (Bertin & Arnouts 1996) on the F160W image. In order to make the measurements of the morphological parameters with GALFIT as robust and reliable as possible, two fundamental steps were taken into account. The first is the construction of the PSF, while the second is the evaluation of the sky background level.

The PSF was constructed with IRAF/DAOPHOT (Stetson 1987), from a set of unsaturated, bright, and isolated stars, and using a Gaussian analytic function plus a look-up table built by the IRAF psf task from the residuals of the function fitting. This allowed us to take into account the anisotropies of the brightness profile, especially those in the wings of the PSF.

The SExtractor sky measurement is based on thresholding: the sky is measured by determining when the gradient of the flux flattens out enough compared to the background noise. In particular, this means that SExtractor will generally over-predict the sky with the effect of suppressing the Sérsic index, the effective radius, and luminosity. In our analysis, the



**Figure 4.** Specific star formation rate as a function of  $R_e$ . Associated errors on  $R_e$  are from GALFIT. Points are color-coded according to their stellar mass. The sample defined by  $\log(M_*/M_\odot) > 11$  and marked in the plot by the large red filled squares is complete in stellar mass at the 70% level. As such, this is the sample we adopt to draw our conclusions. The vertical gray region marks the limit to which we can resolve objects, determined by fitting stars with a Sérsic (1968) profile. We note that, given the existence of a size–mass relation, the vertical line at  $R_e = 2$  kpc marking the separation between compact and extended galaxies only applies to  $\log(M_*/M_\odot) > 11$  galaxies (see Section 3.2 for a more complete discussion). The inset shows the cumulative fraction of galaxies according to their effective radius  $R_e$  for the full sample (solid black line), for the massive ( $\log(M_*/M_\odot) > 11$ ) galaxies (dotted red line), and for the compact ( $R_e < 2$  kpc), massive, quiescent ( $\log(\text{sSFR}/\text{yr}^{-1}) < -11$ ) sample (dashed purple line). A vertical gray line marks our limit in  $R_e$  for the compact galaxies. Approximately 70% of the galaxies in our (flux-limited) sample have  $R_e < 2$  kpc; 4 out of the 10 massive galaxies are also compact. No extended quiescent galaxies are present, although this could be the result of a surface brightness effect. Star-forming galaxies show no evident correlation between  $R_e$  and sSFR.

(A color version of this figure is available in the online journal.)

background level was estimated from its median value in 30 non-overlapping boxes 50 pixels ( $3''$ ) wide, distributed across a region of 400 pixels ( $24''$ ) around the central object, and free from any other source, as probed by the SExtractor segmentation map. The region size is wide enough to grant robust statistics and at the same time it is small enough to mitigate possible gradients in the sky background. The boxes were kept to an additional distance of  $0''.6$  from the segmentation map, increasing the confidence in excluding contamination from the outskirts of objects.

All objects in a box of 150 pixels ( $9''$ ) around each galaxy were simultaneously fit, in order to take into account possible contamination of the brightness profile from neighboring objects, which could bias the measured size and Sérsic index.

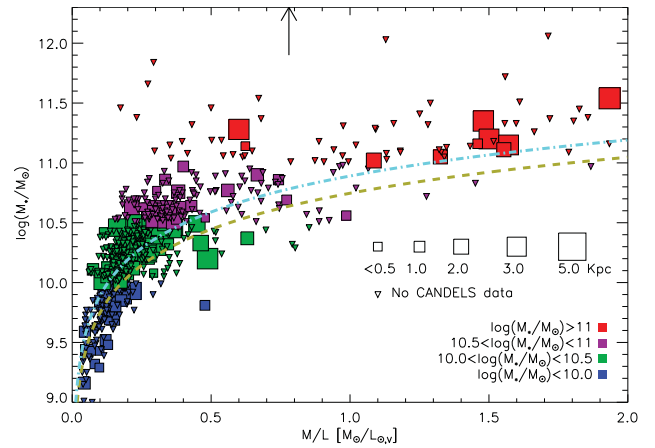
The effective radii were finally circularized and converted to physical units using the adopted cosmology.

The resulting distribution of  $R_e$  as a function of the sSFR for the galaxies of our sample is presented in Figure 4.

### 2.5. Stellar Mass Completeness

Consistent statistical measurements of intrinsic physical quantities rely on the accurate characterization of the selection effects, i.e., on the completeness of the sample.

The galaxy stellar mass completeness for a flux-limited sample not only directly depends on the limiting flux itself but also on the mass-to-light ratio ( $M/L$ ) of each galaxy. All else being the same, galaxies with lower  $M/L$  values will be probed to lower mass limits; similarly, it is possible to probe only the higher stellar mass region for those objects with higher  $M/L$  ratios (see, e.g., Marchesini et al. 2009).



**Figure 5.** Stellar mass as a function of the rest-frame  $V$ -band mass-to-light ratio for all the NMBS galaxies with redshift compatible with being at  $z > 3$ . Points are color-coded according to their stellar mass. Objects covered by the CANDELS F160W frame which allowed for size measurement are marked by larger symbols, with the symbol size proportional to  $R_e$ . The 50% completeness level, computed adopting the  $K$ -band detection completeness curve from Whitaker et al. (2011), is marked by the yellow dashed curve, while the 80% completeness level by the cyan dash-dotted curve. The vertical arrow marks the  $M/L$  of a single stellar population passively evolved to  $z = 3.2$ , smaller than the maximum value we observe for the massive population, increasing our confidence on our completeness analysis. The completeness of the  $M_* > 10^{11} M_\odot$  galaxies is  $> 70\%$ .

(A color version of this figure is available in the online journal.)

The above effect makes the measurement of the stellar mass completeness a non trivial task; common approaches involve either Single Stellar Population (SSP) modeling (Dickinson et al. 2003) and/or comparing the galaxy populations to existing deeper data (Marchesini et al. 2010).

The average PSF on NMBS frames is  $\sim 1''.1$ , corresponding to an  $R_e$  of  $\sim 0''.6$ , or  $\sim 5$  kpc at  $z = 3.2$ . In particular, this means that objects with  $R_e < 5$  kpc are essentially point sources on the NMBS frames. The inset in Figure 4 shows that the totality of the galaxies in our sample has  $R_e < 5$  kpc. We therefore adopt for each galaxy the  $K$ -band completeness curve measured for point sources for the NMBS survey and presented in Whitaker et al. (2011).

The completeness of the  $z > 3$  sample as a function of stellar mass was analyzed for different ranges in  $M/L$  ratio. Objects with  $\log(M_*/M_\odot) > 11$  are complete at the  $\sim 70\%$  level. A graphical representation is plotted in Figure 5, which shows the  $\log(M_*/M_\odot)$  versus  $M/L$  ratio diagram for all NMBS galaxies at  $z > 3$ , as well as the 50% and 80% completeness curves of the stellar mass as a function of  $M/L$  ratio derived from the  $K$ -band detection completeness curve from Whitaker et al. (2011). Figure 5 shows that for galaxies with  $\log(M_*/M_\odot) > 11$ , the completeness is  $\gtrsim 70\%$ . Also plotted is the  $M/L$  at  $z = 3.2$  of a passively evolving single stellar population formed at  $z_{\text{form}} = 20$ . Its value, equal to  $0.78 M_\odot/L_{\odot,V}$ , well below the maximum value we observe for the massive sample, provides additional confidence in the adopted completeness limits in stellar mass. We furthermore note that the completeness in stellar mass as a function of redshift is fairly flat over the redshift range targeted in our work, changing by, e.g.,  $\sim 0.1$  dex from  $z = 4$  to  $z = 3$  for a single stellar population formed at  $z_{\text{form}} = 10$ . In our analysis we then selected only those galaxies with  $\log(M_*/M_\odot) > 11$  (for a total of 10 objects) for which small completeness corrections are required; specifically, the correction for incompleteness ranged from 1.05 to 1.5.

In subsequent sections, we will evolve our  $z \sim 3$  sample to  $z \sim 2$  to assess its correspondence to the  $z \sim 2$  observed population. In principle, we should also estimate completeness levels in stellar mass for this evolved population. This could be done in a way similar as that implemented for the  $z > 3$  sample. In particular, this means that for each object the final completeness correction for the  $z \simeq 2$  sample would be the product between the completeness correction at  $z \simeq 3$  and that at  $z \simeq 2$ . However, as shown by Brammer et al. (2011), the stellar mass completeness at  $z \simeq 2$  is 95% or better for galaxies with stellar mass  $\log(M_*) \gtrsim 11$ , which coincides with our stellar mass selection limit. This implies that no further correction is needed for the massive  $z \simeq 2$  sample.

### 2.6. Cosmic Variance

Given the small region of overlap between the NMBS–COSMOS and CANDELS–COSMOS fields, the statistical uncertainties associated with fluctuations of the large-scale density (i.e., the cosmic variance) play a non-negligible role. We measured such effects following the recipe by Moster et al. (2011). A halo distribution model is used to relate the stellar mass to the dark matter halo as a function of redshift; the galaxy bias is then estimated via dissipationless  $N$ -body simulations. The cosmic variance is first computed on dark matter halos and then converted to galaxy cosmic variance by applying the galaxy bias. The average relative error due to cosmic variance for the  $z > 3$  massive sample is 35%. This value was added in quadrature to the Poisson errors in the number densities we computed.

### 2.7. The Sample

Our primary sample is composed by those galaxies brighter than  $K_s = 23.4\text{AB}$ , whose redshift is compatible with  $z > 3$ , with stellar mass  $M_* > 10^{11} M_\odot$ , and which lie on the CANDELS–COSMOS frame. This selection yields 10 galaxies. Given that their associated completeness is  $\sim 70\%$ , this is the only sample that allows us to perform a quantitatively robust analysis. Specifically, all number densities quoted in this work are based on the above sample. Their SEDs are shown in Figure 6, together with the F160W and color cutout.

## 3. RESULTS

### 3.1. Massive $z > 3$ Galaxies

The distribution of the specific star formation rate (sSFR =  $\text{SFR}/M_*$ ) as a function of the effective radius  $R_e$  for the  $3 < z < 4$  sample is shown in Figure 4. Points are color-coded according to their stellar mass. The effective radius from a Sersic profile fit to the point-source objects is  $0''.11 \pm 0''.01$ ; its projection to  $3 < z < 4$  corresponds to  $\sim 0.8$  kpc and is marked by the solid gray region, identifying a limit for the PSF-convolved Sersic profile. This marks an empirically determined limit below which we cannot robustly determine the size. Given our stellar mass completeness measurement, galaxies satisfying the 70% completeness limit coincide with those whose stellar mass  $M_* > 10^{11} M_\odot$ , identified by the red squares.

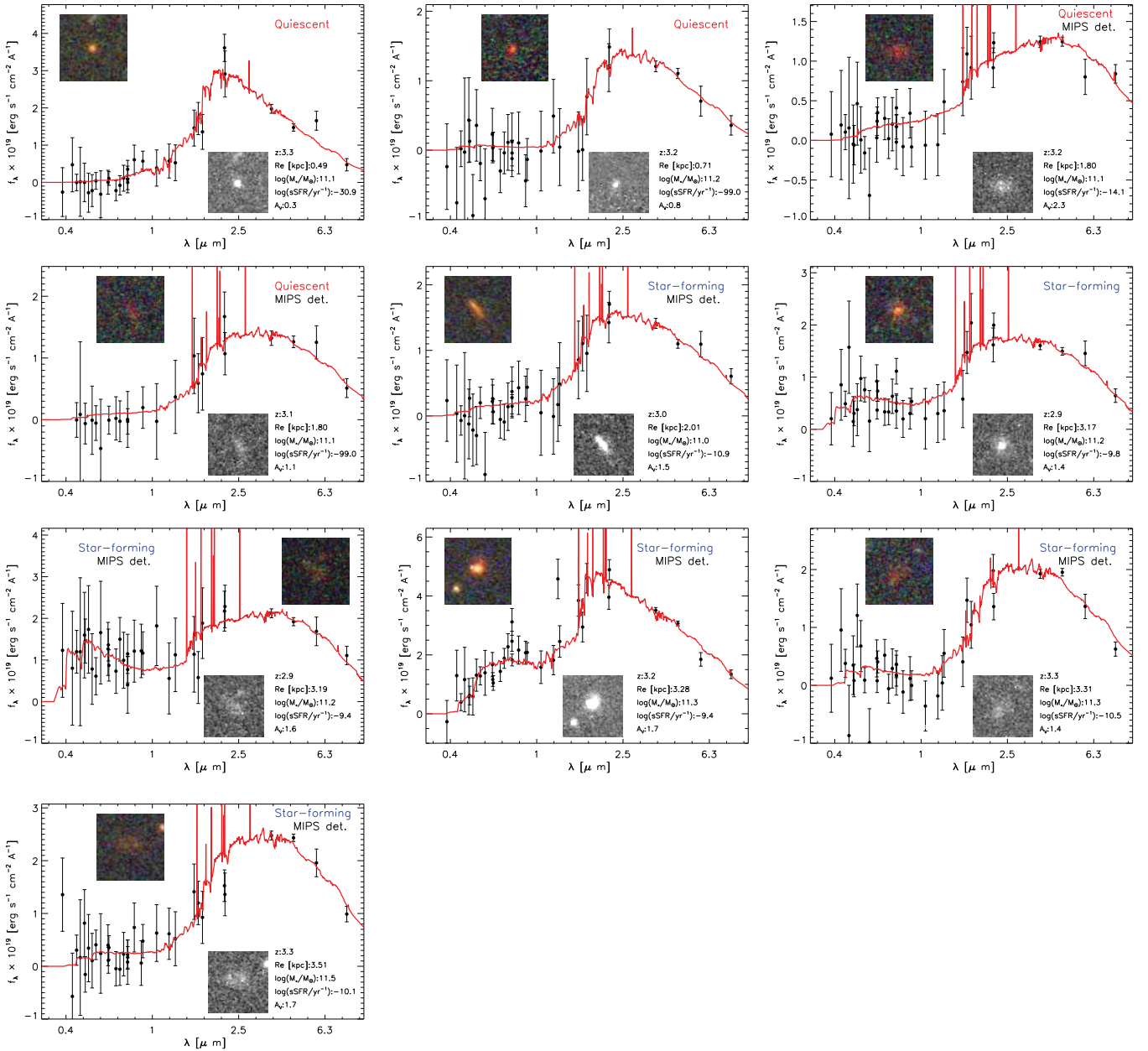
In the following, if not otherwise specified, we refer to *massive* galaxies as those with stellar mass  $M_* > 10^{11} M_\odot$ ; we define *compact* galaxies as those with  $R_e < 2$  kpc and *quiescent* galaxies as those whose  $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$ . Our definition of quiescent galaxies is based on the work of Kriek et al. (2006), where a population of MQGs is spectroscopically identified at  $z \sim 2.3$ . In their sample, the average sSFR is  $4 \times 10^{-12} \text{ yr}^{-1}$ ,

with all galaxies having  $\log(\text{sSFR}/\text{yr}^{-1}) < -11$ . For galaxies of  $\log(M_*/M_\odot) = 11$ , this corresponds to  $\text{SFR} < 1 M_\odot \text{ yr}^{-1}$ . While galaxies with  $\text{sSFR} > 10^{-10} \text{ yr}^{-1}$  can be reasonably considered star forming, those with intermediate sSFR ( $-11 < \log(\text{sSFR}/\text{yr}^{-1}) < -10$ ) are galaxies with suppressed star formation activities (relative to their stellar masses) with respect to the star-forming sequence observed at  $z \sim 2$  (e.g., Whitaker et al. 2012; Szomoru et al. 2012), although not necessarily quiescent. We therefore adopt a more conservative definition of quiescent galaxy (i.e.,  $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$ ) in place of  $\text{sSFR} < 10^{-10} \text{ yr}^{-1}$  sometimes used in the literature. We also checked *Spitzer*/MIPS 24  $\mu\text{m}$  data relative to each massive galaxies. All but one star-forming galaxies are detected at more than  $3\sigma$ . No significant MIPS detection is found for two of the four MQGs, consistently with their quiescent nature from SED modeling. However, two quiescent massive galaxies have significant MIPS fluxes ( $\sim 80$  and  $\sim 140 \mu\text{Jy}$ ), which would imply large SFRs ( $700\text{--}900 M_\odot \text{ yr}^{-1}$ ; Whitaker et al. 2012) if the 24  $\mu\text{m}$  emission were associated with dust-enshrouded star formation. We note, however, that at  $z > 3$ , the MIPS 24  $\mu\text{m}$  band samples rest-frame wavelengths shorter than 6  $\mu\text{m}$ , i.e., emission from hot dust. As such, the conversion from mid-IR fluxes to SFRs is very uncertain, especially at the high redshifts targeted in our work. Moreover, additional contamination due to the emission from the dusty torus of an AGN can potentially contaminate the MIR fluxes probed by the MIPS 24  $\mu\text{m}$  band. For these reasons, we will use the SFRs derived from the SED modeling throughout the paper, noting that half of the subsample of MQGs could actually be highly obscured, star-forming galaxies. Observations in the far-IR (e.g., ALMA) are needed to robustly quantify the level of obscured star formation and to confirm the quiescent nature of these galaxies.

The data show that at  $z > 3$ ,  $M_* > 10^{11} M_\odot$  galaxies that are quiescent tend to be compact, while those that are star forming are more extended, similar to the distribution found at  $z \sim 2$ . Most of the galaxies ( $\sim 70\%$ ; see the inset in Figure 4) are characterized by  $R_e < 2$  kpc, with a median of 1.5 kpc. However, we caution that these values refer to the full sample that is not complete in stellar mass. The average size for the MQGs in the stellar mass complete sample is 1.2 kpc (0.6 kpc if the two galaxies with MIPS 24  $\mu\text{m}$  detection are excluded); the corresponding value for the massive, star-forming sample is 3.1 kpc.

The plot also shows a lack of extended ( $R_e > 2$  kpc) quiescent galaxies, indicating that the massive quiescent (elliptical) galaxies observed in the Local Universe were not yet completely formed when the universe was  $\lesssim 2$  Gyr old. This could also be a surface brightness selection effect, although the width of the NMBS PSF compared to the CANDELS PSF causes all objects with  $R_e < 5$  kpc to be detected as point sources; the selection effect should then act only on the very extended objects.

The plot in Figure 4 shows that MQGs were already present at  $z > 3$ , confirming previous results (see, e.g., Guo et al. 2012 and Marchesini et al. 2010, who first characterized the properties of a mass-complete sample of  $3 < z < 4$  galaxies, finding both quiescent and star-forming galaxies). For  $M_* > 10^{11} M_\odot$  and  $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$  we count four galaxies, corresponding to a completeness-corrected number density of  $n_Q = 5.2_{-3.1}^{+4.6} \times 10^{-6} \text{ Mpc}^{-3}$  ( $n_Q = 3.6_{-2.4}^{+4.0} \times 10^{-6} \text{ Mpc}^{-3}$  if the two galaxies with MIPS 24  $\mu\text{m}$  detection are excluded). The comoving volume was computed assuming a redshift range  $2.8 < z < 4.0$ . The upper and lower error bars were computed following the recipe by Gehrels (1986); cosmic variance was finally added in quadrature.



**Figure 6.** Observed SED from NMBS (black points) together with EAZY best-fitting SED (solid red curve) of our sample of galaxies with  $\log(M_* M_\odot) > 11$ . A color cutout centered on the object and based on the F814W, F125W, and F160W filters from CANDELS, with color scheme following Lupton et al. (2004), is presented in the upper part of each plot, while a cutout from the F160W filter is shown at the bottom of each plot. The *MIPS det.* label indicates those objects with a  $3\sigma$  MIPS detection (see the text for details). The angular size of each cutout is  $3''.7 \times 3''.7$ .

(A color version of this figure is available in the online journal.)

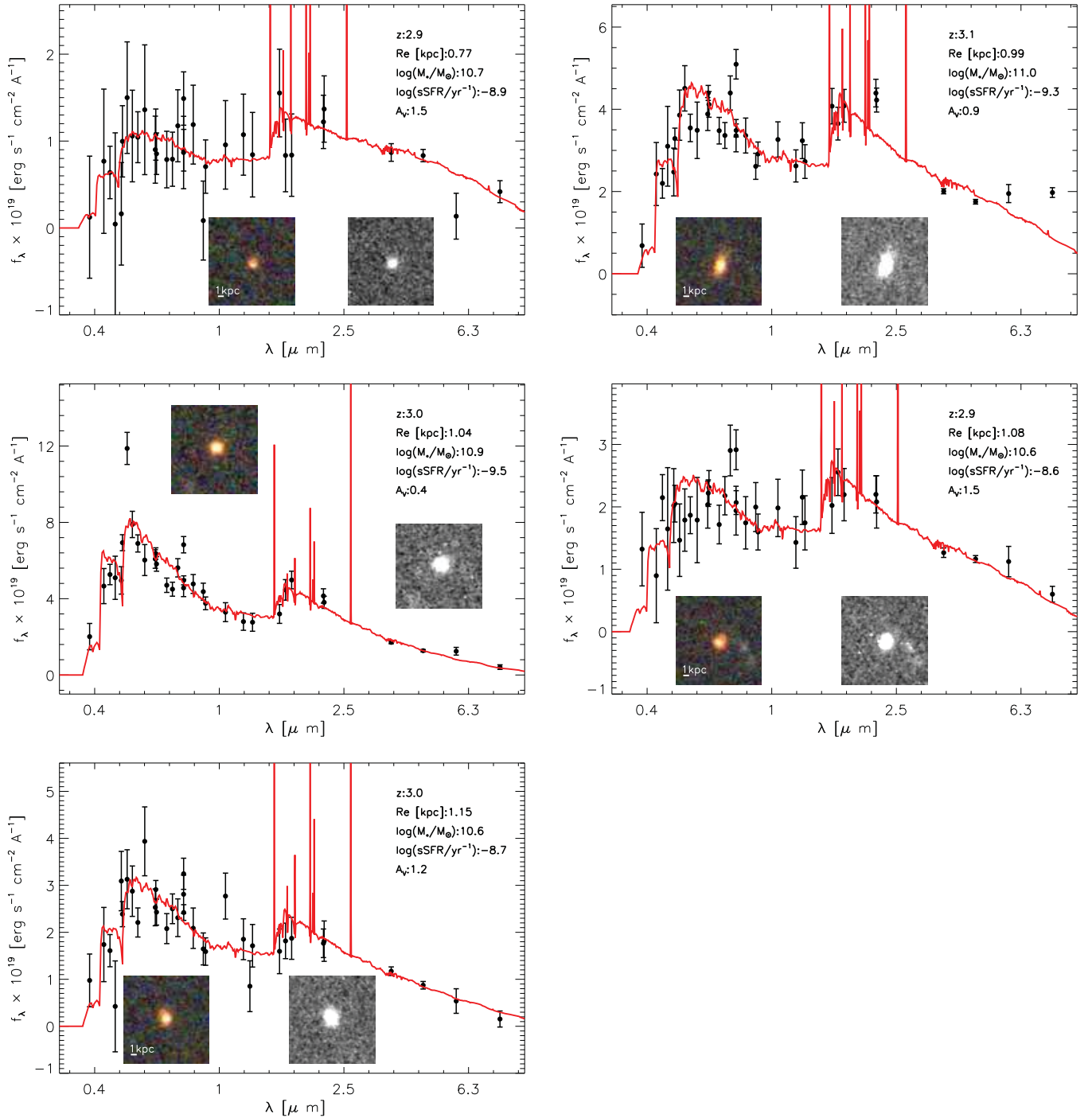
Figure 4 clearly shows that CMQGs were already present at  $z > 3$ . This is one of the main results of this work. Studies so far have found this population of galaxies up to  $z \sim 2$  (see, e.g., Kriek et al. 2006; Bezanson et al. 2009). Our data allow us to push back in time the appearance of CMQGs from when the universe was  $\approx 3$  Gyr old to an age of less than 2 Gyr.

As we will show in Section 4.3, these objects do not exist in significant enough numbers to explain the abundance of CMQGs at  $z \sim 2$ .

### 3.2. Compact, Star-forming Galaxies at $z \sim 3$

The existence of a relation between  $M_*$  and  $R_e$  (see, e.g., Shen et al. 2003; Mosleh et al. 2011) implies that we cannot consider

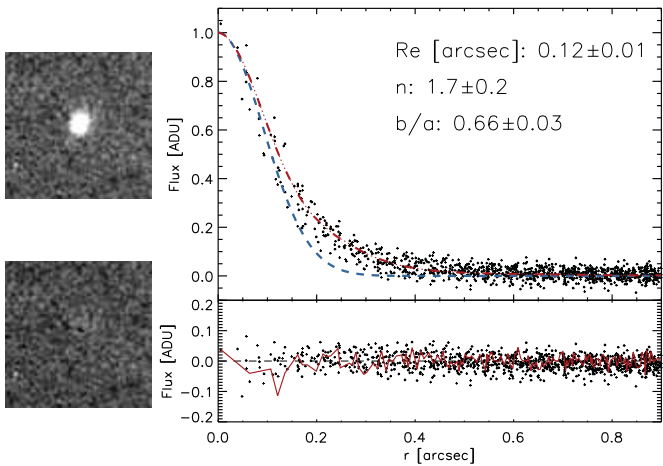
a single value for the  $R_e$  when selecting compact galaxies at different stellar mass ranges. Assuming  $R_e \propto M_*^{0.32}$ , valid for galaxies at  $2.5 < z < 3.5$  (Mosleh et al. 2011), an  $R_e = 2.0$  kpc for a  $\log(M_*/M_\odot) = 11$  galaxy scales to  $R_e = 1.4$  kpc for  $\log(M_*/M_\odot) = 10.5$  and  $R_e = 1.0$  kpc for  $\log(M_*/M_\odot) = 10.0$ . Figure 4 then shows that there are a number of compact star-forming galaxies spanning the whole range of stellar masses. In particular, and more interestingly, in our sample there are five galaxies with high sSFR ( $\log(\text{sSFR}/\text{yr}^{-1}) \sim -9$ ), stellar mass  $10.6 < \log(M_*/M_\odot) < 11$ , and with  $R_e < 1.4$  kpc (i.e., they are compact). Their redshift is above  $z = 2.6$  with 68% confidence level, excluding contamination from low-redshift galaxies with broad probability distributions of photometric redshifts. From Figure 5, the stellar mass completeness



**Figure 7.** Observed SED from NMBS (black points), EAZY best-fitting SED (solid red curve), color cutout built from F814W, F125W, and F160W CANDELS frames, and F160W cutout for our sample of compact, star-forming galaxies with  $10.6 < \log M_*/M_\odot < 11.0$ . The angular size of each cutout is  $3''.7 \times 3''.7$ . (A color version of this figure is available in the online journal.)

of  $\log(M_*/M_\odot) \sim 10.6$  galaxies is lower than 50% for  $M/L > 0.9 M_\odot/L_{\odot,V}$ , i.e., we could possibly be missing star-forming galaxies with significant dust absorption. In Figure 7, we present their SEDs along with F160W and color cutouts. We note, however, that one out of the five objects has both 5 and 8  $\mu\text{m}$  excess that could be the imprint of a Type 2 AGN. However, there is no evidence for this AGN in the rest-frame optical SED and we therefore do not think that it is causing a significant bias in our sizes, although obscured AGNs are a potential source of uncertainty.

To determine if there is a faint extended component in the compact star-forming galaxies and to better assess our size measurements, we directly stacked the images for the five objects. We normalized each image tile to its peak flux to prevent any single object from dominating the stack. The brightness profile of the stacked image was analyzed using GALFIT and a Sérsic profile, obtaining  $R_e = 0''.53 \pm 0''.02$  and  $n = 3.5 \pm 0.2$ . Assuming an average redshift of  $z \sim 3$ , this corresponds to  $R_e \sim 7.7$  kpc. However, we note that visual inspection of the images of the individual objects shows that the aspect ratio and



**Figure 8.** Panels on the left show the stacked image for three out of the five compact star-forming galaxies with high stellar mass at  $z > 3$ , obtained after excluding the two galaxies with very different aspect ratio and position angle (top) and the residual image resulting from the fit (bottom). The panels on the right show on top the circularized radial profile (arbitrary units) of the stacked image indicated by the black points. The triple-dotted dashed red curve marks the PSF-convolved Sersic profile recovered by GALFIT, while the blue dashed line represents the profile of the PSF. The bottom panel shows the residuals measured directly from the GALFIT residual image (black points) and smoothed difference between the PSF-convolved analytic profile and the original input image (solid red line). The light profile closely resembles that of the PSF and it does not show evidence for a faint extended halo. (A color version of this figure is available in the online journal.)

position angle of two galaxies are very different from the other three, causing significant broadening of the profile. We therefore repeated the stacking excluding these two sources, obtaining  $R_e = 0''.12 \pm 0''.01$  (0.9 kpc at  $z \sim 3$ ) and  $n = 1.7 \pm 0.2$ , further supporting their compact configuration. The stacked image and its surface brightness profile for this second analysis are shown in Figure 8.

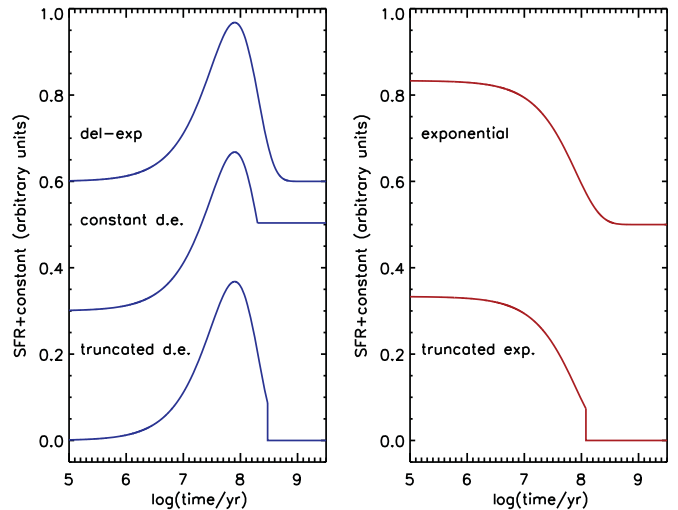
These compact, star-forming galaxies with stellar mass  $10.6 < \log(M_*/M_\odot) < 11$  are likely candidates for being the progenitors of the CMQGs observed at  $z \simeq 2$ , as recent works have shown (see, e.g., Patel et al. 2013; Barro et al. 2013). However, as we will show in Section 4.1, the evolution of the stellar mass of this sample of objects does not increase above  $\log(M_*/M_\odot) = 11$  by  $z = 2.3$ . Therefore, the net result is that the compact, star-forming galaxies with  $10.6 < \log(M_*/M_\odot) < 11$  at  $z \sim 3$  will not directly contribute to the number density of the more massive CMQGs at  $z \sim 2$ .

#### 4. WHAT WERE THE PROGENITORS OF THE $z \sim 2.3$ COMPACT, MASSIVE, AND QUIESCENT GALAXIES?

##### 4.1. Evolving $z > 3$ Galaxies to $z = 2.3$

In this section, we describe the evolution of the  $z > 3$  population of massive ( $M_* > 10^{11} M_\odot$ ) galaxies down to  $z = 2.3$ , paying specific attention to the progenitor population of the massive, quiescent ( $sSFR < 10^{-11} \text{ yr}^{-1}$ ) galaxies at  $z \sim 2.3$  (Kriek et al. 2006; van Dokkum et al. 2008; Bezanson et al. 2009). We used the stellar masses and SFRs from the public NMBS catalog. These were computed using the FAST code (Kriek et al. 2009), adopting a Kroupa (2001) initial mass function (IMF), a delayed-exponential star formation history (SFH) and solar metallicity.

The stellar mass and the SFR of each  $z > 3$  galaxy were evolved to  $z = 2.3$  using the GALAXEV program from the



**Figure 9.** Examples of the SFHs resulting from the different evolution scenarios assumed in this work. Left panel: from top to bottom are the delayed-exponential SFH, the constant delayed-exponential SFH, and the truncated delayed-exponential SFH. Right panel: from top to bottom, the exponential and truncated exponential SFH (see Section 4.1 for descriptions of the SFHs used here). The adopted parameters are representative of the average  $z > 3$  population for all but the truncated exponential SFH:  $e$ -folding time ( $\tau$ ) of  $8 \times 10^7$  yr and age of  $3 \times 10^8$  yr. The age of the truncated exponential SFH corresponds to  $2 \times 10^7$  yr. Arbitrary normalization and offset were applied in order to increase readability.

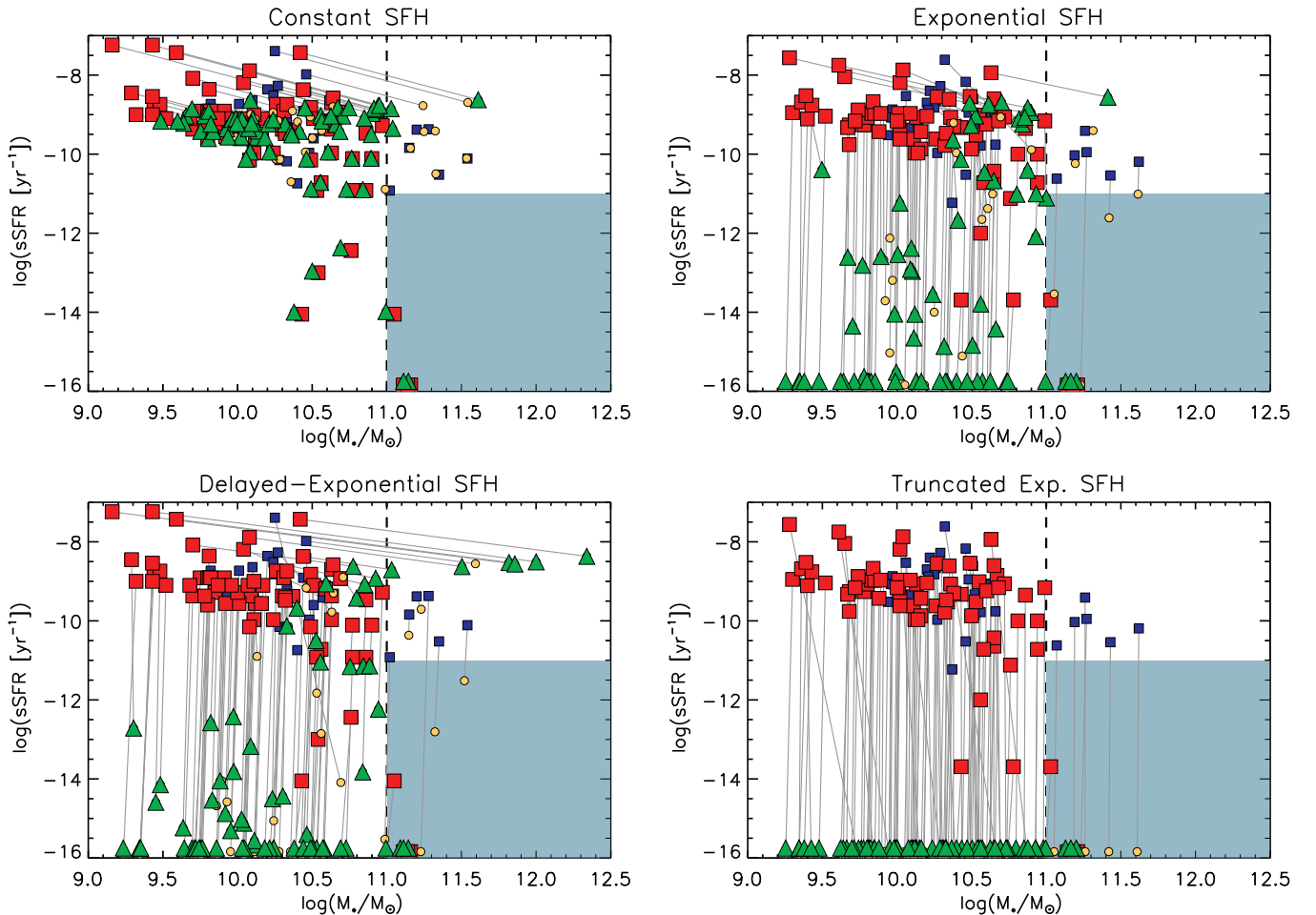
(A color version of this figure is available in the online journal.)

Bruzual & Charlot (2003) SSP models using a set of different SFHs. Specifically, we adopted five distinct SFHs: a constant delayed-exponential SFR (CSF), an exponentially declining SFR (E), an exponentially declining with quenching of star formation 100 Myr after the observed redshift SFR (TE), a delayed-exponential SFR (DE), and its quenched version 100 Myr after the observed redshift (TDE). We allowed each SFH to progress starting at the mass and SFR given by FAST. The adopted SFHs are schematically presented in Figure 9. We note that the constant delayed-exponential SFH is the result of a delayed-exponential SFH, from the formation of the galaxy until the epoch of observation at  $z > 3$ , and of a pure constant SFH, for the following evolution.

The  $z > 3$  sample and its evolution at  $z = 2.3$  are shown in the  $sSFR-M_*$  plane in the four panels of Figure 10 (we omit the truncated delayed-exponential case as its results resemble those from the truncated exponential SFH).

The panels in Figure 10 show that galaxies with  $sSFR < 10^{-9} \text{ yr}^{-1}$  do not significantly increase their stellar mass with time due to their low SFRs, but instead they keep approximately the same value, or slightly decrease it, due to the return of stellar mass to the gas phase in the ISM. This is valid also for the sample of compact, star-forming ( $\log(sSFR) \sim -9$ ) galaxies with stellar masses  $10.6 < \log(M_*/M_\odot) < 11$  presented in the previous section. Specifically, there is only one galaxy at  $z \sim 3$  with  $10.6 < \log(M_*/M_\odot) < 11$  that will evolve to  $M_* > 10^{11} M_\odot$  at  $z = 2.3$ . This mass evolution occurs for two out of the five chosen SFHs (exponentially declining and constant delayed exponential), but only for the exponential SFH is the  $sSFR < 10^{-11} \text{ yr}^{-1}$  at  $z = 2.3$ . Therefore, galaxies with  $10.6 < \log(M_*/M_\odot) < 11$  at  $z \sim 3$  will not enter the CMQ population at  $z \sim 2$  in great numbers, unless they grow their stellar masses through merging and/or further quenching of their SFRs. Overall, the largest contribution to the change in number density in the evolution of the population of MQGs





**Figure 10.** Evolution of the  $z > 3$  galaxy sample in the  $\text{sSFR}-M_*$  plane to  $z = 2.3$  for four different SFHs (left to right, top to bottom: constant delayed-exponential, exponential, delayed-exponential, and truncated exponential SFHs). The large red squares mark compact (i.e.,  $R_e < 2$  kpc)  $z > 3$  galaxies, while the blue smaller squares indicate the remaining  $z > 3$  galaxies. The position of each galaxy after evolution is indicated by the green triangles and yellow circles for descendants of compact and extended galaxies, respectively. The filled area marks the selection criteria adopted for the massive ( $M_* > 10^{11} M_\odot$ ) and quiescent ( $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$ ) sample at  $z = 2.3$ . The vertical dashed line indicates the stellar mass limit corresponding to our 70% completeness. Barring significant size evolution, the descendants of the red squares that fall within the shaded box indicate the number of predicted  $z \sim 2$  compact, massive, quiescent galaxies. The number of galaxies in the shaded box is possibly a lower limit as they are the result of evolving the full  $z > 3$  sample and not only those galaxies from the stellar mass complete sample. In particular, there may be galaxies with stellar masses below our completeness limit at  $z \sim 3$  which could nonetheless grow above the limit by  $z \sim 2.3$ . The largest contribution to the change in number density in the evolution of the population of massive quiescent galaxies comes mainly from the decreased value of the SFR at  $z = 2.3$ , rather than from an increase in stellar mass with cosmic time.

(A color version of this figure is available in the online journal.)

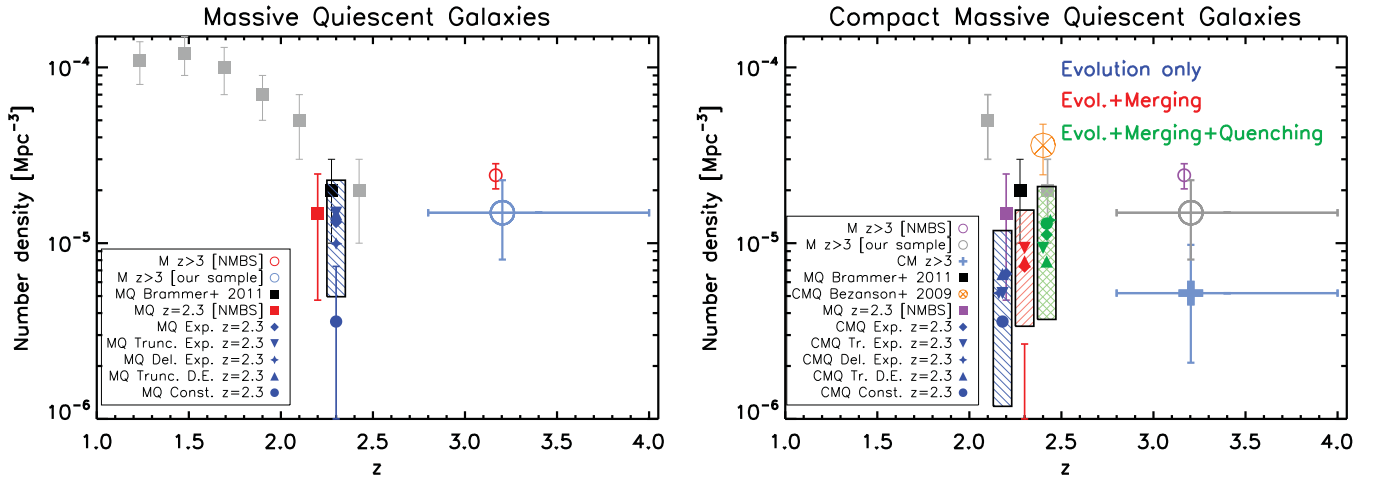
comes mainly from the decreased value of the SFR at  $z = 2.3$ , rather than from an increase in stellar mass with cosmic time.

In the following section, we present the number densities of MQGs; the number densities of the compact, massive, quiescent population are discussed in Section 4.3. As a further and more consistent source of comparison, the number density of  $z > 3$  massive galaxies and of  $z = 2.3$  MQGs was also computed using the full NMBS catalog. These two populations were selected according to the same limits in stellar mass and SFR used for the other samples, i.e.,  $\log(M_*/M_\odot) > 11$  and  $\log(\text{sSFR}/\text{yr}^{-1}) < -11$ . The full list of the number densities computed for the different choices of SFH can be found in Table 1. The comoving volume was computed assuming a redshift range  $2.8 < z < 4.0$ . We used upper and lower error bars from Gehrels (1986) and added in quadrature the cosmic variance. Figure 3 shows that there are six objects with  $z < 2.8$ , although all of them have stellar masses  $M_* < 10^{11} M_\odot$ . We repeated our analysis excluding the six objects with  $z < 2.8$  and obtained results quantitatively similar to those presented here.

#### 4.2. The Evolution of Massive $z > 3$ Galaxies to $z \sim 2$

In order to explore how our results depend on different SFH in SED modeling, we adopt a different SFH for the past and future history of galaxies in each panel of Figure 10. Specifically, for the exponential and truncated exponential SFH, we used stellar masses and SFRs computed adopting an exponential SFR and a Salpeter (1955) IMF, and converting the SFRs and stellar masses to a Kroupa IMF by subtracting 0.2 dex. The location of the starting galaxies does not depend much on the SFH used to compute the stellar masses and SFRs, meaning that the choice of SFH primarily affects the evolved galaxies.

The number density  $n_M$  of massive ( $M_* > 10^{11} M_\odot$ )  $z > 3$  galaxies from our sample is  $n_M = 14.9_{-6.8}^{+7.9} \times 10^{-6} \text{ Mpc}^{-3}$ ; Figure 11 shows that it is fully compatible with the number density of  $z \sim 2.2-2.5$  quiescent galaxies from Brammer et al. (2011). In particular, this implies that, in the absence of external processes able to trigger new star formation or increase the stellar mass (e.g., galaxy mergers), the whole population of



**Figure 11.** Left panel: number density of the massive  $z > 3$  sample with overlap with the CANDELS field (blue open circle), and computed from the full NMBS catalog (red open circle). The filled red square marks the number density of  $z \sim 2.3$  massive quiescent galaxies computed using the full NMBS catalog. We note that, while the Brammer et al. (2011) number density refers to quiescent galaxies selected via the  $UVJ$  diagram, our measurement of the  $z \sim 2.3$  massive quiescent population is obtained applying an  $sSFR < 10^{-11} \text{ yr}^{-1}$  cut. The blue hashed box at  $z \sim 2.3$  encompasses the range in number density of massive quiescent galaxies as predicted by four of our SFH scenarios (DE, TDE, E, and TE) for evolving all galaxies from  $z > 3$  to lower redshift. The vertical extent of the bar also takes into account the expected cosmic variance. It is clear from this that there are enough massive galaxies at  $z > 3$  to account for the full massive quiescent galaxy population at  $z \sim 2$ . The blue filled circle at  $z = 2.3$  represents the number density and total error from the CSF model. The total number density of  $\log(M_*/M_\odot) > 11$  galaxies at  $z > 3$  is consistent with the population of massive quiescent galaxies at  $z \sim 2$ ; all except the CSFH are plausible SFHs in reproducing the evolution to  $z \sim 2$ . Right panel: number density of the original massive  $z > 3$  sample (open gray and magenta circles for the measurement obtained using our sample and the full NMBS catalog, respectively) and of the compact massive  $z > 3$  sample (thick blue plus sign), which encompasses the same objects as the  $z > 3$  MQ sample, and hence has the same number density. The colored boxes at  $z \approx 2.3$  mark the number densities of evolved compact, massive, quiescent galaxies under different scenarios. The blue box represents pure evolution in the SFHs with no merging. The red box and points represent the evolution after galaxies have been allowed to merge once randomly. The green box includes the effect of the SFH, a random merger, and a post-merger truncation of the SFH. The blue and green bars and the associated points have been shifted by an arbitrary value in  $z$  to improve readability and should be considered at  $z = 2.3$ . The Brammer et al. (2011) data are plotted only for  $z > 2$ , i.e., where the vast majority of massive quiescent galaxies are also compact. Also plotted is the number density of  $2.2 < z < 2.4$  massive, quiescent galaxies from the full NMBS catalog (red filled square). The number density of the compact, massive, quiescent population of galaxies obtained with pure SFH evolution to  $z = 2.3$  is only marginally consistent with previous determinations; a simple merging model produces number densities in better agreement with previous determinations. Agreement at the  $1\sigma$  level is found with the number density of  $z \sim 2$  massive, quiescent galaxies computed from the full NMBS data set for the simple evolution scenario; the simple merging model increases the level of agreement of the number densities. We caution, however, that the number densities of the evolved samples are perhaps lower limits since they are the result of evolving all galaxies at  $z > 3$  and not just those for which we are mass complete. Specifically, there may be galaxies below our completeness limit at  $z \sim 3$  which could nonetheless grow above the limit by  $z \sim 2.3$ .

(A color version of this figure is available in the online journal.)

**Table 1**  
Number Densities for the Galaxy Populations and SFHs Adopted in This Work

Redshift	Population <sup>a</sup>	Number density <sup>b</sup> ( $10^{-6} \text{ Mpc}^{-3}$ )				
$z > 3$	M	$14.9^{+7.9}_{-6.8}$				
	M (Full NMBS)	$24.3^{+3.5}_{-3.3}$				
	MQ	$5.2^{+4.6}_{-3.1}$				
Redshift	Population	Number density ( $10^{-6} \text{ Mpc}^{-3}$ )				
$z = 2.3$	MQ (Full NMBS)	$14.7^{+12.1}_{-10.5}$				
Redshift	Population	E ( $10^{-6} \text{ Mpc}^{-3}$ )	TE ( $10^{-6} \text{ Mpc}^{-3}$ )	DE ( $10^{-6} \text{ Mpc}^{-3}$ )	TDE ( $10^{-6} \text{ Mpc}^{-3}$ )	CSF ( $10^{-6} \text{ Mpc}^{-3}$ )
$z = 2.3$	MQ	$13.2^{+7.3}_{-6.2}$	$14.9^{+7.9}_{-6.8}$	$9.9^{+6.2}_{-5.0}$	$14.6^{+7.8}_{-6.7}$	$3.6^{+4.0}_{-2.4}$
	CMQ	$6.7^{+5.1}_{-3.7}$	$5.2^{+4.6}_{-3.1}$	$5.2^{+4.6}_{-3.1}$	$6.7^{+5.1}_{-3.7}$	$3.6^{+4.0}_{-2.4}$
Merging						
$z = 2.3$	CMQ	$6.7^{+5.1}_{-3.7}$	$9.8^{+6.2}_{-4.9}$	$7.0^{+5.2}_{-3.8}$	$9.1^{+5.9}_{-4.7}$	$0.2^{+2.6}_{-0.2}$
Merging+Quenching						
$z = 2.3$	CMQ	$12.3^{+7.0}_{-5.9}$	$9.8^{+6.2}_{-4.9}$	$15.3^{+8.0}_{-7.0}$	$9.1^{+5.9}_{-4.7}$	$11.1^{+6.6}_{-5.4}$

**Notes.**

<sup>a</sup> Symbols refer to: M, massive galaxies ( $\log(M_*/M_\odot) > 11$ ); C, compact galaxies ( $R_e < 2 \text{ kpc}$ ); Q, quiescent galaxies ( $\log(sSFR/\text{yr}^{-1}) < -11$ ); and combinations thereof.

<sup>b</sup> The comoving volume for the  $z \gtrsim 3$  and  $z = 2.3$  populations is computed adopting the redshift range  $2.8 < z < 4.0$ .

massive  $z > 3$  galaxies needs to have its SFR quenched to  $\log(sSFR/\text{yr}^{-1}) < -11$  by  $z \sim 2$ . We will explore how mergers might influence the growth of stellar mass in Section 4.3.1.

The comparison of the number density of  $z > 3$  massive galaxies with  $z = 2.3$  MQGs, both computed using the full NMBS catalog, confirms the above result.

This is further supported by our SFH predictions. The blue bar in the left panel of Figure 11 represents the number density of galaxies which, evolved from their observed redshifts, are massive and quiescent by  $z = 2.3$ . The box takes into account the spread in values from four of the five adopted SFHs (excluding the CSF) and cosmic variance. The blue box is in good agreement with measurements of quiescent galaxies from Brammer et al. (2011) at  $z \sim 2-2.5$ . Overplotted are also the values from the individual SFHs. In general, apart from the constant delayed-exponential SFH case, it is not possible to discriminate among the SFHs, mainly due to the high cosmic variance errors ( $\approx 0.35$  relative error). As shown in the left panel of Figure 11, four out of five of the SFHs do equally well in reproducing the number counts of MQGs at  $z \sim 2.3$ . The only exception is the CSF that underpredicts the observed number density of MQGs at  $z \sim 2$  by a factor of  $\sim 4$ . This suggests that the only valid SFHs are the declining or truncated SFHs and that the constant delayed-exponential SFH is not a valid option in this range of redshift. On the other side, given that the number densities of massive, star-forming galaxies at  $z \sim 2$  is approximately the same as that of MQGs (Brammer et al. 2011), the fact that the CSF SFH underpredicts the number densities of MQG means that the CSF SFH would also underpredict the number density for the massive star-forming galaxies at  $z \sim 2$ . Considered together with the low number of star-forming galaxies with CSF SFH that cross the  $\log(M_*/M_\odot) = 11$  threshold (see the top left panel of Figure 10), the above result suggests that high-redshift massive star-forming galaxies might be characterized by rising SFHs, in agreement with recent works (e.g., Maraston et al. 2010; Papovich et al. 2011).

Interestingly, Bell et al. (2012) found a similar result when comparing  $z \sim 1$  galaxies to the  $z = 0$  quiescent population, with the local population of MQGs approximately as numerous as the entire massive population at  $z \sim 1$ . This could suggest that mechanisms for quenching, either the same over the history of the universe or of different nature at different epochs, are ongoing more or less continuously since  $z \sim 4$ .

#### 4.3. The Progenitors of $z \sim 2$ Compact, Massive, Quiescent Galaxies

Several works have demonstrated that the vast majority of massive quiescent  $z \sim 2$  galaxies are also compact (see Szomoru et al. 2012 and references therein). This allows us to directly compare our number densities for CMQGs to the number densities at  $z = 2-2.5$  from Brammer et al. (2011) and Bezanson et al. (2009) and to the number density of MQGs at  $z = 2.3$  we measured using the full NMBS sample.

Bezanson et al. (2009) published an estimate of the number density of CMQGs, based on the stellar mass function of Marchesini et al. (2009). The corresponding value is marked in Figure 11 by the crossed-circle symbol. We increased the original error bar to take into account the effects of cosmic variance using the Moster et al. (2011) recipe and adding it in quadrature. The final error bar is a factor of  $\approx 1.5$  the error bar quoted in the original work, but more representative of the true uncertainties.

As is seen in the right panel of Figure 11, the number density  $n_C$  of massive galaxies that are compact at  $z > 3$  (specifically, the number density of compact galaxies at  $z > 3$  with  $\log(M_*/M_\odot) > 11$  and  $\log(\text{sSFR}/\text{yr}^{-1}) < -11$ , which also corresponds to the number density  $n_Q$  of MQGs at  $z > 3$ ) is a factor of  $\sim 3$  smaller compared to the number density of all massive galaxies. Nonetheless,  $n_C$  is consistent within  $1\sigma$  with

the number density of MQGs computed from the NMBS. This agreement is mostly the consequence of the large error bars, as the number density of  $z > 3$  CMQ galaxies is systematically smaller than the number densities of MQ galaxies we adopted as reference at  $z \sim 2$ . The evolution to  $z = 2.3$  of the compact, massive galaxies using our chosen SFHs (blue box) produces a number density which is approximately a factor of  $\gtrsim 4$  smaller than the number density of MQGs from Brammer et al. (2011) and consistent only at a  $2\sigma$  level. We can explain the decrease in number density between  $z \sim 3$  and  $z \sim 2$  in the context of our evolution models: the increase with cosmic time of the fraction of mass returned to the ISM decreases the stellar mass. One possible source of the discrepancy between our measured number density and that of Brammer et al. (2011) could be the different criteria adopted by Brammer et al. (2011) to select the quiescent population (the *UVJ* color selection; Williams et al. 2009). In a recent work, Szomoru et al. (2012) showed that the fraction of quiescent galaxies selected at  $z \gtrsim 2$  using the *UVJ* method is equivalent to an  $\text{sSFR} < 10^{-10} \text{ yr}^{-1}$  criterion.<sup>7</sup> It is worth noting that we do not find  $z > 3$  compact, massive, star-forming galaxies, and specifically compact, massive galaxies with  $-11 < \log(\text{sSFR}/\text{yr}^{-1}) < -10$  which, following our evolutionary models, would eventually become compact, massive, quiescent by  $z \sim 2$ . This means that our measurement of the number density of CMQGs at  $z \sim 2.3$  does not change if we use an sSFR that is compatible with that for a *UVJ* cut.

When we compare the expected number density of CMQGs that have been evolved from  $z \sim 3$  with the measured sample of  $z = 2.3$  MQGs from NMBS (nearly all of which are compact), we find that the two agree to within  $1\sigma$ .

The plot also shows that the number density from Bezanson et al. (2009) is higher than our measurements, and compatible only with the upper end of Brammer et al. (2011). One possible reason for this discrepancy could be that Bezanson et al. (2009) assume the fraction of MQGs to be 0.5, which is likely a too optimistic choice (e.g., Domínguez Sánchez et al. 2011).

Similar to the left panel, in the right panel of Figure 11 the number densities from the individual SFHs are marked. For the compact massive galaxies, the number density from the CSFH is compatible with the measurements from the other SFHs, in agreement with recent works (see, e.g., González et al. 2010; Reddy et al. 2012).

##### 4.3.1. The effects of mergers

In the previous sections, we showed that the assumed evolution models allow us to reproduce within  $1\sigma$  the number density of (compact) MQGs at  $z \sim 2$ . Despite being consistent within the errors, the pure-evolution measurements are still systematically below the number density of MQGs at  $z = 2.3$ , indicating that pure evolution might just be barely enough. Merging and quenching after merging are also plausible processes in this range of redshift (see, e.g., Khochfar & Silk 2006; Cameron & Pettitt 2012). In order to try to understand the possible mechanisms that could be responsible for the buildup of the compact, massive, quiescent population at  $z \sim 2$ , we then implemented a very simple statistical model for how mergers could affect the evolution in the observed number densities. Our toy model consists of randomly choosing pairs of galaxies among the 110

<sup>7</sup> We also selected quiescent galaxies in the full NMBS data set using the *UVJ* color-color technique. The sSFRs for quiescent galaxies at  $2 < z < 2.5$  and with  $\log(M_*/M_\odot) > 11$  are lower than  $\log(\text{sSFR}/\text{yr}^{-1}) = -9.84$ , with a 75% upper limit  $\log(\text{sSFR}/\text{yr}^{-1}) = -10.3$  and a median  $\log(\text{sSFR}/\text{yr}^{-1}) = -11.11$ .

galaxies with  $z > 3$  and with a measurement of the  $R_e$  and leaving the SFH of each galaxy to evolve independently of its companion. The stellar mass of the merged pair was finally considered as the algebraic sum of the two components; the sSFR was computed as the mass-weighted sum of each component (or, equivalently, as the sum of the two SFRs divided by the total stellar mass), while we assumed for the  $R_e$  of the merged pair the  $R_e$  of the more massive companion.

The effect of merging on the number density evolution is represented in the right panel of Figure 11 by the red box; the result is an agreement between the observed number density of compact MQGs at  $z \sim 2$  and that from our models, for all the SFH but the CSF. In the CSF case, in fact, the number density is even smaller than the number density of the population without merging. In the framework of our toy model, this is due to the high probability that each pair contains a galaxy with high SFR. The end product is then biased toward high sSFR galaxies at the end of the merging process.

Given the potential effect of a starburst or an AGN that is triggered by the merger, we also examined a scenario in which the SF is quenched following the merger. This is supported by recent hydrodynamical simulations in which mergers play an important role in the gravitational heating of the halo gas, and consequently in the suppression of star formation (Johansson et al. 2009). However, we note that this last process does not improve the agreement significantly, except for the CSF case, for which the number density falls well within the values from the other SFH.

Good agreement between the expected and observed number densities for our evolved, merged, and quenched model is also found when we compare the expected number densities to those calculated from the full NMBS sample using a  $\log(\text{sSFR}/\text{yr}^{-1}) < -11$  cut. This comparison is useful as the full NMBS catalog has a higher precision than our sample that is limited to the area with CANDELS overlap. Although the merging model appears to be in better agreement with the data, it is clear that even a simple evolution model with no merging provides an adequate match to the data. Therefore, merging and quenching, which are both likely processes that are occurring in the galaxy population, are not required to explain the number densities.

If the two quiescent galaxies with MIPS detections indeed have the extreme SFRs implied by the rest-frame  $5.6 \mu\text{m}$  fluxes, our results on the potential importance of merging would remain qualitatively unchanged. This is because these two galaxies are only 13%–20% of the whole sample of galaxies that would be classified as massive at  $z \sim 2.3$ . If the truncated post-merger SFH is correct then the results will also remain quantitatively similar as the prompt quenching of star formation assumed in this model would turn them into MQGs by  $z \sim 2.3$ .

## 5. DISCUSSION

According to current semi-analytic models for the formation of MQGs, the bulk of the stellar mass was formed as a compact, massive spheroid at  $z > 3$  through gas-rich merger events (e.g., Oser et al. 2010). Specifically, in the redshift range between  $z = 5$  and  $z = 3$ , the models predict that the central galaxy would still be building up from gas flows which would feed the formation of stars in the central region of the galaxy directly, forming the concentrated stellar system (Naab et al. 2009). In a second stage, quenching mechanisms such as major merger or feedback from AGNs or from star formation would convert the full population of massive galaxies into the population

of quiescent massive galaxies observed at later cosmic times. Subsequent minor dry mergers would be responsible for the increase in size (Naab et al. 2009; Oser et al. 2012), while keeping the gain in stellar mass to a factor of  $\lesssim 2$  (van Dokkum et al. 2010).

Understanding *what* are the physical mechanisms of star formation quenching, *when* they started to act, and *how long* they took to completely quench star formation is then a central key in our knowledge of formation and evolution of local MQGs. While our analysis does not provide us with significant information on the physical mechanisms, it allows us to put new constraints on both when star formation quenching could have happened and on how fast it could be.

In fact, the compatibility of the number density of massive  $z > 3$  galaxies with the number density of  $z \sim 2$  MQGs from the literature suggests that the population of MQGs at  $z \sim 2$  can be completely accounted for by the observed  $z > 3$  population of massive galaxies that is subsequently quenched. Specifically, when evolving our sample of  $z > 3$  galaxies to  $z = 2.3$ , a good agreement is obtained introducing quenching of star formation after merging, a process which is supported by recent hydrodynamical simulations.

Second, our observations of CMQGs at  $3 < z < 4$  push back in time the appearance of this class of objects to when the universe was  $\sim 2$  Gyr old.

Finally, considering that, according to models, massive galaxies should still be actively forming stars at  $3 < z < 5$ , then the observation of compact massive galaxies that are already quiescent by  $3 < z < 4$  imposes that the quenching of star formation should be a rapid mechanism in massive galaxies, acting on timescales of less than 1 Gyr in the early universe, in agreement with recent determinations (e.g., Barro et al. 2013).

## 6. CONCLUSIONS

In this work, we used two overlapping public sets of data in a region of the COSMOS field to identify the progenitors at  $z \gtrsim 3$  of the CMQGs observed at  $z \sim 2$ . Stellar masses, sSFRs, and photometric redshifts were taken from the NMBS. The sizes were measured on high-resolution CANDELS F160W images. The population of  $z \gtrsim 3$  galaxies was evolved to  $z = 2.3$  using the Bruzual & Charlot (2003) models following five different SFHs (constant delayed exponential, delayed exponential, truncated delayed exponential, exponential, and truncated exponential). All the number densities were computed assuming a comoving volume corresponding to  $2.8 < z < 4.0$ . Our main results can be summarized by the following points.

1. We discovered four compact, massive ( $M_* > 10^{11} M_\odot$ ) quiescent (SED-based  $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$ ) galaxies at  $z \gtrsim 3$ , corresponding to a completeness-corrected number density of  $n_Q = 5.2^{+4.6}_{-3.1} \times 10^{-6} \text{ Mpc}^{-3}$ . If the two galaxies with MIPS detection were excluded, the resulting completeness-corrected number density would be  $n_Q = 3.6^{+4.0}_{-2.4} \times 10^{-6} \text{ Mpc}^{-3}$ .
2. For a complete sample of 10 galaxies with  $\log M_*/M_\odot > 11$ , we found that the quiescent ( $\text{sSFR} < 10^{-11} \text{ yr}^{-1}$ ) galaxies are compact ( $R_e \sim 1.2 \text{ kpc}$ ), while the star-forming galaxies are extended ( $R_e \sim 3.1 \text{ kpc}$ ), qualitatively similar to what is found at lower redshifts ( $z \sim 2.3$ ). If the two quiescent galaxies with MIPS  $24 \mu\text{m}$  detection were considered star forming, the averaged sizes of the quiescent and star-forming galaxies would be  $R_e = 0.6 \text{ kpc}$  and  $R_e = 2.8 \text{ kpc}$ , respectively.

3. We found five compact ( $R_e < 1.4$  kpc), star-forming (sSFR  $\sim 10^{-9}$  yr $^{-1}$ ) galaxies at  $z \sim 3$  with stellar masses  $10^{10.6} < \log(M_*/M_\odot) < 10^{11.0}$ . The small effective radius was confirmed by a Sersic (1968) profile fitting of the stacked image.
4. The number density of massive  $z > 3$  galaxies is comparable to the number density of  $z \sim 2$  MQGs from the literature. The evolution of the number density of the  $z > 3$  galaxy population to  $z \sim 2$  can be accounted for with a family of decaying or truncated SFHs. The CSF SFH does not fit the observed number densities. A model with quenching of the SFR between  $z = 2.3$  and 3 does.
5. When we evolve our compact  $z > 3$  galaxies to  $z = 2.3$ , we find that the predicted number density of CMQGs is consistent at the  $1\sigma$  level for all of our adopted SFHs. An even better agreement is obtained if we quench the star formation after the merging event. Such a rapid truncation is supported by recent simulations (e.g., Johansson et al. 2009).

The above results lead to the following conclusions.

1. The number density of MQGs at  $z \sim 2$  can be completely accounted for by the observed  $z > 3$  population of massive galaxies that is subsequently quenched. Similarly, the number density of CMQGs at  $z \sim 2$  is consistent with the number density of compact, massive galaxies at  $z > 3$ , implying that most CMQGs at  $z > 3$  must be quenched by  $z \sim 2$ . Despite the good agreement within the large error bars, the number density of  $z > 3$  CMQGs is systematically lower than the number density of MQGs at  $z \sim 2$ , most of which are compact. This implies the potential need for an additional channel for the creation of CMQGs at  $z \sim 2$ , which may include galaxy merging.
2. The existence of CMQGs at  $3 < z < 4$  pushes back in time the appearance of this class of objects to when the universe was  $\sim 2$  Gyr old.
3. Since galaxy formation models predict that at  $3 < z < 5$  galaxies should still be building up from gas flows, the existence of compact, massive galaxies that are quiescent already at  $3 < z < 4$  implies that the quenching of star formation should be a rapid mechanism, acting on timescales of less than 1 Gyr in the early universe.

We note that half of the subsample of massive and quiescent galaxies is detected in MIPS, implying large SFRs if the MIR emission were associated with dust-enshrouded star formation. Since the MIPS band probes rest-frame wavelengths shorter than  $6 \mu\text{m}$  at  $z > 3$  (i.e., emission from hot dust), SFRs derived from MIPS are very uncertain and can potentially be contaminated by emission from a dusty torus of an AGN. Observations in the far-IR (e.g., ALMA) are needed to robustly quantify the level of obscured star formation and to confirm the quiescent nature of these galaxies.

The analysis presented in this work is based on a sample size of about one hundred objects, resulting from the intersection of two catalogs, CANDELS and NMBS on the single COSMOS field. Recent projects like the 3D-HST survey (van Dokkum et al. 2011; Brammer et al. 2012) will provide accurate redshift for  $\sim 7000$  objects at  $1 < z < 3.5$  over a total area a factor of  $\sim 5$  larger than the one available for this work. This will reduce by a large amount both the Poisson noise and the uncertainties due to the cosmic variance. Additionally, the increase in photometric depth from both CANDELS and the 3D-HST with respect to the currently available data sets will also allow us to probe

the population of galaxies down to smaller stellar masses. These improvements will contribute significantly in the near future to further understanding the buildup and evolution of massive galaxies.

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