

1 **Intraseasonal and interannual variability of the**  
2 **quasi-two day wave in the Northern Hemisphere**  
3 **summer mesosphere**

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4 **Abstract.** This study uses global synoptic meteorological fields from a  
5 high-altitude data assimilation system to investigate the spatial and tem-  
6 poral characteristics of the quasi-2 day wave (Q2DW) and migrating diur-  
7 nal tide during the Northern Hemisphere summers of 2007, 2008, and 2009.  
8 By applying a 2-dimensional fast Fourier transform to meridional wind and  
9 temperature fields, we are able to identify Q2DW source regions and to di-  
10 agnose propagation of Q2DW activity into the upper mesosphere and lower  
11 thermosphere. We find that Q2DW is comprised primarily of westward prop-  
12 agating zonal wavenumber 3 and wavenumber 4 components that originate  
13 from within baroclinically unstable regions along the equatorward flank of  
14 the summer midlatitude easterly jet. Amplitude variations of wavenumbers  
15 3 and 4 tend to be anti-correlated throughout the summer, with wavenum-  
16 ber 3 maximizing in July and wavenumber 4 maximizing in late June and  
17 early August. Monthly mean Q2DW amplitudes between  $30^{\circ}$  –  $50^{\circ}$ N latitude  
18 are largest when diurnal tidal amplitudes are smallest and vice versa. How-  
19 ever, there is no evidence of any rapid amplification of the Q2DW via non-  
20 linear interaction with the diurnal tide. Instead, variations of Q2DW ampli-  
21 tudes during July are closely linked to variations in the strength and loca-  
22 tion of the easterly jet core from one summer to the next, with a stronger  
23 jet producing larger Q2DW amplitudes. Linear instability model calculations  
24 based on the assimilated wind fields find fast growing zonal wavenumber 3  
25 and 4 modes with periods near 2 days in the vicinity of the easterly jet.

## 1. Introduction

26 Wind and temperature observations in the MLT over the last several decades show  
27 that one of the largest recurring features in MLT dynamics is an eastward-propagating  
28 zonal wavenumber 3 disturbance with a period near 48 hours that is commonly referred  
29 to as the quasi-two day wave or Q2DW [e.g. Muller and Nelson, 1978; Harris, 1994; Lima  
30 et al., 2004; Pancheva, 2006; Hecht et al., 2010; Suresh Babu et al., 2011]. Satellite-  
31 based measurements of temperature and long-lived constituents [e.g. Wu et al., 1996;  
32 Limpasuvan and Wu, 2003; Garcia et al., 2005; Tunbridge et al., 2011], in combination with  
33 satellite-based MLT wind observations [Wu et al., 1993; Lieberman, 1999; Limpasuvan and  
34 Wu, 2009], have shown that Q2DW amplitudes peak in the extratropical MLT during both  
35 Southern Hemisphere (SH) and Northern Hemisphere (NH) summer shortly after solstice.  
36 As an example, Figure 1 plots temperature and meridional wind fields at 40°N and 0.02  
37 hPa ( $\sim 75$  km) during July 2009 showing the longitude-time signature of the eastward  
38 propagating Q2DW.

39 The Q2DW is currently understood to originate primarily from baroclinically unstable  
40 regions on the equatorward flank of the summertime mesospheric easterly jet. These  
41 regions produce fast-growing instabilities that can project onto the zonal wavenumber 3  
42 global Rossby-gravity mode [Salby, 1981; Plumb, 1983; Pfister, 1985; Lieberman, 1999;  
43 Rojas and Norton, 2007]. One key aspect of the Q2DW that is not yet well understood is  
44 the cause of its intermittency, i.e., it is often observed in “bursts” throughout the summer  
45 season that vary in duration from several days to several weeks (see, e.g., Fig. 1). As a  
46 result, the observed Q2DW can exhibit a high degree of both intraseasonal and interannual

47 variability as documented by Wu et al. [e.g. 1996]; Limpasuvan and Wu [e.g. 2003]; Garcia  
48 et al. [e.g. 2005]; Tunbridge et al. [e.g. 2011]; Offerman et al. [e.g. 2011].

49 Since conditions for baroclinic instability are extremely sensitive to gradients in back-  
50 ground zonal wind and temperature, the behavior of the summertime extratropical Q2DW  
51 depends on complex interactions with the effects gravity wave drag and solar tides. For  
52 example, Norton and Thuburn [1999] used a global circulation model (GCM) to demon-  
53 strate that the effects of gravity wave drag maintain the meridional and vertical gradients  
54 in the summertime MLT zonal wind distribution that are necessary for the growth of  
55 baroclinically unstable local modes. In addition, Salby and Callaghan [2008] showed that  
56 the presence of the migrating diurnal solar tide in a primitive equation model effectively  
57 can increase the damping of the Q2DW and thus limit its growth under solstice conditions  
58 through nonlinear wave-wave interactions. Under certain conditions, nonlinear interac-  
59 tions between the Q2DW and the migrating diurnal tide can also cause a rapid growth in  
60 Q2DW amplitude and a contemporaneous (albeit smaller) reduction in the diurnal tidal  
61 amplitude. This process was first noted in the observational study by Teitelbaum and  
62 Vial [1991], and later described in several modeling studies [Norton and Thuburn, 1999;  
63 Palo et al., 1999; Salby and Callaghan, 2008; Chang et al., 2011]. Key factors determining  
64 whether or not this rapid amplification of the Q2DW will occur are a strong easterly jet in  
65 the summer upper mesosphere and phase locking of the Q2DW with the diurnal cycle (i.e.,  
66 a 48-hour period) [Walterscheid and Vincent, 1996]. These conditions, and subsequent  
67 Q2DW-tide interactions, have been observed in the SH summer MLT [Hecht et al., 2010;  
68 McCormack et al., 2010], but it is not clear whether or not such processes also contribute  
69 to variability in the Q2DW during NH summer.

70 The goal of this investigation is to examine the roles of both baroclinic instability mech-  
71 anisms and possible Q2DW-tidal interactions in controlling Q2DW intermittency in the  
72 NH summer extratropical MLT. Doing so requires a data set of global winds and tem-  
73 peratures up to the lower thermosphere ( $\sim 90$  km) with sufficient temporal resolution to  
74 separate the Q2DW and tidal signatures. Presently, such information cannot be obtained  
75 from a single set of observations, but can instead be obtained by combining multiple  
76 sets of MLT observations using a high-altitude data assimilation system (HDAS). This  
77 study examines Q2DW and tidal variability using 6-hourly synoptic meteorological anal-  
78 yses of winds and temperature from the surface to 90 km altitude over the June-August  
79 periods of 2007, 2008, and 2009 produced by the Navy Operational Global Atmospheric  
80 Prediction System with Advanced Level Physics-High Altitude (NOGAPS-ALPHA). The  
81 NOGAPS-ALPHA HDAS has been used previously to describe Q2DW variability in the  
82 SH extratropics during January [McCormack et al., 2009], and to provide evidence of non-  
83 linear Q2DW-tidal interactions in the extratropical SH summer MLT region [McCormack  
84 et al., 2010]. This is the first study using HDAS fields to examine the behavior of the  
85 Q2DW and tides in the NH summer.

86 Most studies of the Q2DW to date have focused on the SH summer extratropics, where  
87 its amplitude is largest. Although the amplitude of the Q2DW in the NH is smaller than its  
88 SH counterpart, it has a more complex spatial structure consisting of zonal wavenumbers  
89 2, 3, and 4 whose relative amplitudes vary over the course of the season [Tunbridge et  
90 al., 2011]. We employ space-time spectral analysis of the NOGAPS-ALPHA wind and  
91 temperature fields to discriminate among the different spatio-temporal components of  
92 the Q2DW and the diurnal tide, which is not possible using ground-based data sets or

93 asynoptic satellite records alone given their limitations in spatial and temporal coverage.  
94 This information is used to characterize the seasonal and interannual variability in the NH  
95 Q2DW in relation to the migrating diurnal tide. NOGAPS-ALPHA winds are also used  
96 as input for a linear instability model to diagnose the origin and growth of the Q2DW  
97 throughout the NH summer via baroclinic instability. The results of this investigation  
98 indicate that the strength and location of the midlatitude mesospheric easterly jet core is  
99 the main factor controlling the behavior of the Q2DW during NH summer.

100 The NOGAPS-ALPHA HDAS system and data analysis techniques are described in  
101 Section 2. Section 3 presents the seasonal and interannual variability in the QW2DW and  
102 diurnal migrating tide during NH summer of 2007, 2008, and 2009. Section 4 discusses the  
103 origin and propagation of the Q2DW using diagnostic wave activity calculations. Section  
104 5 presents results from a linear instability model that uses NOGAPS-ALPHA assimilated  
105 winds to examine how the Q2DW arise from baroclinically unstable regions near the  
106 summer easterly jet. Section 6 contains a summary of these results and explores future  
107 research directions.

## 2. Data and Methodology

108 The NOGAPS-ALPHA HDAS assimilates operational meteorological observations in  
109 the troposphere and lower stratosphere in combination with research satellite observations  
110 of middle atmospheric temperature, ozone, and water vapor to provide a comprehensive  
111 analysis of atmospheric state variables from the surface to  $\sim 90$  km. In this section, we  
112 first present a brief overview of the HDAS system. For a comprehensive description of the  
113 production version of NOGAPS-ALPHA, see Eckermann et al. [2009a]. We then discuss

114 the methods used to analyze the behavior of the Q2DW and diurnal migrating tide in the  
115 NH summer MLT.

### 2.1. NOGAPS-ALPHA Description

116 NOGAPS-ALPHA is built upon the framework of the NOGAPS numerical weather pre-  
117 diction and analysis system that originally extended from the surface to 1 hPa ( $\sim 50$  km).  
118 It consists of two main components: a global spectral forecast model [Hogan and Ros-  
119 mond, 1991], and a three-dimensional variational (3DVAR) data assimilation algorithm  
120 [Daley and Barker, 2001]. To expand this system's meteorological analysis capability  
121 through the middle atmosphere, the vertical domain of the NOGAPS-ALPHA forecast  
122 model was raised to  $\sim 100$  km [Hoppel et al., 2008], and a 68-level (L68) hybrid  $\sigma - p$   
123 vertical coordinate was introduced [Eckermann, 2009b], giving  $\sim 2$  km spacing of levels  
124 throughout the stratosphere and mesosphere. In the present study, the forecast model  
125 component of NOGAPS-ALPHA uses a T79 horizontal wave number truncation to give an  
126 effective horizontal grid spacing of  $1.5^\circ$  in longitude and latitude on a quadratic Gaussian  
127 grid. Extending NOGAPS-ALPHA into the middle atmosphere required the addition of  
128 several new physics packages, as described in Eckermann et al. [2009a]. These include  
129 improved shortwave heating and longwave cooling rates [Chou et al., 2001; Chou and  
130 Suarez, 2002], updated parameterizations of sub-grid scale orographic [Palmer et al., 1986]  
131 and non-orographic gravity wave drag [Eckermann, 2011], and linearized photochemi-  
132 cal parameterizations for middle atmospheric ozone and water vapor [McCormack et al.,  
133 2006, 2009], which are both prognostic model variables in NOGAPS-ALPHA.

134 The data assimilation component of NOGAPS-ALPHA is based on the NRL Atmo-  
135 spheric Variational Data Assimilation System (NAVDAS) [Daley and Barker, 2001], a

136 3DVAR system with a 6-hour update cycle that assimilates both conventional ground-  
137 based observations (e.g., wind, pressure, temperature from station reports and radioson-  
138 des) and operational satellite-based observations (e.g., microwave radiances, surface winds,  
139 precipitable water). In addition, NOGAPS-ALPHA assimilates Aura MLS Version 2.2  
140 temperature, O<sub>3</sub>, and H<sub>2</sub>O profile measurements [Hoppel et al., 2008]. The Aura satellite  
141 completes  $\sim 13$  orbits per day with coverage between 82°S–82°N latitude. NOGAPS-  
142 ALPHA also assimilates Version 1.07 temperature profile measurements from the TIMED  
143 SABER instrument, which is a side-viewing instrument whose latitude coverage alter-  
144 nates every two months to view high latitudes in both hemispheres. During NH summer,  
145 TIMED switches from its north-viewing mode (latitude range of 83°N to 52°N) to south-  
146 viewing mode (52°N to 83°S) in mid-July. This change in coverage is not seen to affect the  
147 Q2DW in the NOGAPS-ALPHA analyses, whose amplitude generally maximizes between  
148 30°–40°N latitude.

149 The bulk of the information on the Q2DW and tides in the NOGAPS-ALPHA analy-  
150 ses comes from MLS and SABER temperature profiles that are assimilated between the  
151 32 – 0.002 hPa pressure levels. The vertical resolution of the SABER temperature re-  
152 trieval remains  $\sim 2$  km throughout the stratosphere and mesosphere while the resolution  
153 of the MLS temperature retrieval degrades from  $\sim 3$  km in the stratosphere to  $\sim 13$  km  
154 near the 0.01 hPa level. Global mean systematic biases of 2–3 K between the MLS and  
155 SABER temperatures, have been removed prior to assimilation to avoid introducing spu-  
156 rious spatial variability into the temperature analyses, as described in the work of Hoppel  
157 et al. [2008]. To obtain accurate heating and cooling rates in the middle atmosphere,



158 NOGAPS-ALPHA also assimilates daily MLS H<sub>2</sub>O and O<sub>3</sub> profiles between 220–0.002  
159 hPa and 215–0.02 hPa, respectively [Eckermann et al., 2009a].

160 To investigate the Q2DW in the NH MLT, the present study analyzes global synoptic  
161 zonal and meridional wind fields produced by the NOGAPS-ALPHA HDAS. NOGAPS-  
162 ALPHA does not directly assimilate middle atmospheric wind measurements; instead, it  
163 uses a formulation of the gradient wind approximation in the off-diagonal elements of  
164 the observation error covariance matrix to produce balanced wind and temperature incre-  
165 ments. These increments are integrated forward in time by the forecast model component,  
166 and the resulting middle atmospheric wind fields are further constrained by the physical  
167 parameterizations in the model (e.g., gravity wave drag, diffusion, etc.). As previous  
168 studies have shown [McCormack et al., 2009, 2010] the resulting 6-hourly global wind and  
169 temperature fields have the spatial and temporal resolutions necessary to discriminate  
170 between the Q2DW and diurnal tide in the SH summer MLT; the present study extends  
171 these investigations to the NH summer.

172 A critical test of any assimilation system is verification with independent observations.  
173 For middle atmospheric winds and temperatures, these types of observations consist  
174 mainly of ground-based radar and lidar measurements over a relatively small number  
175 of locations. Eckermann et al. [2009a] and Stevens et al. [2010] show that diurnal and  
176 semi-diurnal variations in the NOGAPS-ALPHA MLT wind and temperature fields agree  
177 well with independent ground-based observations at high northern latitudes during the  
178 2007 summer season. McCormack et al. [2010] also showed good agreement between the  
179 Q2DW in NOGAPS-ALPHA MLT winds and medium-frequency radar winds during Jan-

180 uary 2006 and January 2008. Furthermore, NOGAPS-ALPHA winds compared well with  
181 Tromsø meteor radar winds at 70°N during January 2009 [Coy et al., 2011].

182 To demonstrate that NOGAPS-ALPHA MLT winds used in the present study agree  
183 with ground-based observations during NH summer, Figure 2 compares meridional winds  
184 at 88 km altitude from meteor radar observations over Kühlungsborn (54°N, 12°E) with  
185 corresponding NOGAPS-ALPHA winds at 0.0036 hPa during July and August 2007. To  
186 facilitate the comparison, a 5-point smoothing was applied to the hourly meteor wind  
187 values in order to reduce high-frequency variability. As Fig. 2 shows, there is very good  
188 overall agreement between the NOGAPS-ALPHA analyzed winds and the meteor radar  
189 winds at this location. In particular, both data sets show clear 2-day periodicity during  
190 July (days 196-208). Although additional comparisons are desirable to fully verify the  
191 NOGAPS-ALPHA analyses, results to date clearly demonstrate that the analyzed winds  
192 can capture key features of the Q2DW.

## 2.2. Space-Time Spectral Analysis

193 To describe the characteristics of the Q2DW and diurnal migrating tide, we use a two-  
194 dimensional fast Fourier transform (2DFFT) approach following Hiyashi [1971], where  
195 NOGAPS-ALPHA wind and temperature fields at a given latitude and pressure level are  
196 expanded as Fourier series in longitude and time. Following the procedure described in  
197 McCormack et al. [2009], daily zonal means are subtracted from each 6-hourly longitude-  
198 time field and then a cosine taper is applied to the first and last 10% of each record in  
199 time. The resulting space-time power spectrum describes the amount of variance at each  
200 frequency and zonal wave number. The 2DFFT is applied over a 32-day interval to derive

201 results for an individual month. It is also applied over a 90-day interval to obtain results  
202 over the summer period June-August.

203 Figure 3 plots the resulting normalized power spectrum derived for a 32-day period  
204 (128 points) of 6-hourly NOGAPS-ALPHA meridional winds from 30 June – 31 July 2009  
205 at 0.02 hPa and 40°N (see Fig. 1b). The 2DFFT method can identify both westward  
206 and eastward propagating features that are associated, by convention, with positive and  
207 negative frequency values respectively. At this particular level, only westward features  
208 are found and so only positive frequencies are plotted.

209 The results of the 2DFFT in Fig. 3 show that most of the variance in the meridional  
210 winds at this location is found in westward-propagating zonal wavenumbers 3 and 4 with  
211 frequencies between 0.45–0.6 cpd. Similar results are found in the 2DFFT analysis of  
212 NOGAPS-ALPHA temperature at this location (not shown). This combination of waves  
213 3 and 4 at periods near 2 days is consistent with the recent study of MLS temperatures  
214 by Tunbridge et al. [2011], who found the Q2DW throughout the NH summer MLT to  
215 be a complex of waves 2, 3, and 4. Fig. 3 also indicates variance at wave 1 centered on  
216 1 cpd, indicative of the migrating diurnal tide. It should be noted that although spectral  
217 analysis of the 6-hourly NOGAPS-ALPHA output can resolve frequencies down to 2 cpd,  
218 the 3DVAR system’s  $\pm 3$ -hour assimilation window may not be able to fully capture this  
219 high-frequency variability associated with, e.g., the semi-diurnal tide. Therefore, this  
220 study focuses on interactions between the Q2DW and diurnal tide.

221 To study the episodic nature of the Q2DW-tide interactions throughout the NH sum-  
222 mer season, time series of the individual Q2DW and tide components in the wind and  
223 temperature fields are reconstructed by applying appropriate band-pass filters to the in-

verse 2DFFT. Based on the results of the power spectra in Fig. 3, pass bands at zonal  
wavenumbers 3 and 4 from 0.45–06 cpd are chosen for the Q2DW, and at zonal wave  
1 from 0.9–1.1 cpd for the diurnal tide. Eddy heat and momentum fluxes calculated  
from these filtered fields are then used to formulate Eliassen-Palm (EP) flux diagnostics  
of wave activity associated with the Q2DW [Lieberman, 1999]. This technique has been  
applied previously to NOGAPS-ALPHA fields to investigate the evolution of the Q2DW  
and diurnal tide in the SH summer mesosphere [McCormack et al., 2009, 2010]. In the  
present study, we extend this analysis to focus on the behavior of the Q2DW and diurnal  
migrating tide during the NH summers of 2007, 2008, and 2009.

### 3. 2DFFT Results

This section presents detailed information on the latitude and altitude structure of  
the Q2DW and migrating diurnal tide during NH summer obtained from the 2DFFT  
analysis of the NOGAPS-ALPHA temperature and meridional wind fields. This section  
also discusses both the interannual and intraseasonal variability of these features during  
June-August of 2007, 2008, and 2009.

#### 3.1. Interannual variability of the Q2DW

Figure 4 plots monthly mean values of the root-mean-square amplitude for the west-  
ward propagating zonal wavenumber 3 component of the Q2DW in both temperature and  
meridional wind (referred to in terms of its central frequency and wavenumber as [0.5,3])  
for July 2007, 2008, and 2009. In all three years, the spatial structure of the Q2DW is  
consistent with earlier observations of the NH summer [e.g. Tunbridge et al., 2011, their  
Figure 7]. Specifically, we find that the feature exhibits deep vertical extent throughout

244 the mesosphere between 20°N–55°N with a maximum in temperature near 40°N and 0.02  
 245 hPa ( $\sim 75$  km). Fig. 4 also shows that the peak monthly mean temperature amplitudes  
 246 vary from year to year, reaching 3.1 K in 2007, 3.8 K in 2008, and 4.5 K in 2009. A  
 247 secondary maximum in [0.5,3] amplitude is noted in all three years between 50°N–60°N  
 248 above 0.001 hPa ( $\sim 96$  km), reaching 2.9K, 4.9K, and 4.0K in 2007, 2008, and 2009 re-  
 249 spectively. While this secondary temperature maximum appears to be related to the  
 250 [0.5,3] meridional wind component near 95 km, it should be regarded with some caution  
 251 as it lies above the top pressure level of 0.002 hPa where MLS and SABER temperature  
 252 observations are assimilated.

253 The interannual variability in monthly mean meridional wind [0.5,3] amplitudes shown  
 254 in Fig. 4 matches that of the monthly mean temperature amplitudes. Specifically, for the  
 255 three years analyzed the Q2DW in meridional wind is strongest in July 2009 (peak value  
 256 of  $19 \text{ m s}^{-1}$ ) and weakest in July 2007 (peak value of  $15 \text{ m s}^{-1}$ ). The spatial structure of  
 257 the meridional wind [0.5,3] component is also consistent from year to year, and exhibits  
 258 three key features: (1) A broader latitude range compared to the temperature Q2DW,  
 259 extending from the summer hemisphere across the equator to 20°S; (2) a maximum near  
 260 95 km between 40°N– 50°N; and (3) a pronounced poleward tilt with increasing height.  
 261 These features are in good qualitative agreement with model simulations of the [0.5,3]  
 262 feature in meridional wind [Norton and Thuburn, 1999; Palo et al., 1999; Salby and  
 263 Callaghan, 2000; Chang et al., 2011].

264 Figure 5 plots the monthly mean amplitudes of the [0.5,4] component in NOGAPS-  
 265 ALPHA temperatures and meridional winds. While the latitude and altitude dependences  
 266 of the [0.5,4] temperature component are similar to the [0.5,3] component, we find that

267 the peak values of [0.5,4] in temperature are located on average  $\sim 5^\circ$  equatorward and  
268  $\sim 10$ – $12$  km lower than the location of the [0.5,3] temperature peaks. Peak values of the  
269 [0.5,4] meridional wind response are also shifted equatorward by  $\sim 5^\circ$ , on average, relative  
270 to the peak [0.5,3] wind values. One main difference between the zonal wave number 3  
271 and 4 features, however, is that the [0.5,4] meridional wind amplitudes do not exhibit  
272 the sharp increase with height seen in the [0.5,3] wind amplitudes. Another important  
273 difference is that, on average, both the peak temperature and wind amplitudes of [0.5,4]  
274 are 30% less than the amplitudes of [0.5,3].

275 We note here that Tunbridge et al. [2011] found evidence for a westward zonal wave  
276 number 2 feature associated with the Q2DW in NH summer based on analysis of MLS  
277 temperatures. Our 2DFFT analysis of NOGAPS-ALPHA temperatures finds that peak  
278 amplitudes for this [0.5,2] component are typically less than 1.5 K and, unlike the zonal  
279 wave 3 and 4 cases, are found over a broad latitude region from  $10^\circ\text{N}$ – $70^\circ\text{N}$  above  $\sim 80$ km.  
280 The latitude and altitude dependences of the [0.5,2] component in meridional wind (not  
281 shown) are also markedly different from the zonal wave number 3 and 4 cases, showing  
282 peak values of  $\sim 10$  m s $^{-1}$  throughout the upper mesosphere centered over the equator.  
283 Because this apparent wave number 2 Q2DW exhibits spatial characteristics that are fun-  
284 damentally different from [0.5,3] and [0.5,4] results, the present study will focus on the  
285 dynamical factors controlling the growth and evolution of wave number 3 and 4 compo-  
286 nents of the Q2DW in NH summer. Possible relationships between these components and  
287 the zonal wave number 2 Q2DW will be examined in a future study.

288 One distinct advantage of 6-hourly global HDAS output is the ability to discriminate  
289 among the diurnal migrating (or [1,1]) tide and the [0.5,3] and [0.5,4] components of

290 the Q2DW. As discussed in the Introduction, there is both theoretical and observational  
291 evidence that the Q2DW can be influenced by tides, and vice versa. Most of these studies,  
292 however, focus on the SH summer period when Q2DW amplitudes are larger than during  
293 NH summer. We next examine the general characteristics of the [1,1] tide obtained from  
294 the 2DFFT analysis for June–August of 2007, 2008, and 2009.

295 Figure 6 plots the monthly mean [1,1] amplitudes in both temperature and meridional  
296 wind for July 2007, 2008, and 2009. The latitude and altitude structure of the tidal  
297 amplitudes derived from NOGAPS-ALPHA fields are quite similar from year to year, and  
298 are in good agreement with earlier modeling studies [e.g. Norton and Thuburn, 1999;  
299 Chang et al., 2011]. Of the three summers studied here, we find that mean July tidal  
300 amplitudes in temperature and meridional wind are generally smallest in 2009. The  
301 spatial structure of the [1,1] meridional wind amplitudes (Figs. 6b, 6d, and 6f) in the  
302 region between 30°N–40°N, where Q2DW amplitudes are largest, exhibits a pronounced  
303 vertical gradient during both July 2008 and July 2009. This gradient produces a very sharp  
304 “cutoff” in the tidal response below the 0.003 hPa level ( $\sim 90$  km) in these two years. In  
305 contrast, the tidal response in July 2007 between 30°N–40°N has a much weaker vertical  
306 gradient, and there is no corresponding cutoff in tidal amplitudes below 0.003 hPa. As a  
307 result, the [1,1] meridional wind amplitudes between 30°N–40°N in the 85–90 km region  
308 are relatively large ( $\sim 20$  m s $^{-1}$ ) during July 2007. During July 2007 and 2008, on the other  
309 hand, the [1,1] meridional wind amplitudes in this region range from 8–12 m s $^{-1}$ . Overall,  
310 the smallest July Q2DW amplitudes in the Northern subtropical upper mesosphere were  
311 found in 2007, when the corresponding monthly mean tidal amplitudes were largest. This

312 anti-correlation of the Q2DW and tidal amplitudes is generally consistent with previous  
313 studies, and will be examined further in the following section.

314 The interannual variations in tidal amplitudes seen in Fig. 6 can be caused by a variety  
315 of different factors, including variations in the strength of tidal forcing (i.e., latent heat  
316 release and ozone heating), and variations in the strength of the zonal winds in MLT. The  
317 latter is highly dependent on gravity wave drag, and wind variations in the stratosphere  
318 can act as a filter for upward propagating gravity waves. An analysis of TIMED Doppler  
319 Interferometer winds from 2002–2007 by Wu et al. [2008] found that amplitudes of the  
320 migrating diurnal tide tend to be larger during the westerly phase of the stratospheric  
321 quasi-biennial oscillation (QBO). We note that the QBO was in its easterly phase during  
322 July 2007; during July 2008 and 2009, winds in the equatorial lower stratosphere were  
323 westerly. Therefore, it does not appear that the QBO can explain the interannual varia-  
324 tions in the Northern subtropical tidal amplitudes shown in Figure 6. Regardless of the  
325 origin, the results in Figs. 6 and 7 are consistent with the interpretation that strong  
326 tidal amplitudes can limit the growth of the Q2DW, as discussed in the Introduction. We  
327 examine the relationship between the Q2DW and migrating diurnal tide in more detail in  
328 Section 3.3.

### 3.2. Intraseasonal variability

329 We next examine the variability of the  $[0.5,3]$  and  $[0.5,4]$  components over the course of  
330 each summer period (June–August). This is done by applying a band-pass filter at zonal  
331 wavenumber 3 and 4 with limits of  $0.45 - 0.6$  cpd to the inverse 2D Fourier transform of  
332 the NOGAPS-ALPHA fields over a 75-day interval from June 5 to August 20 of each year.  
333 To facilitate comparisons with seasonal Q2DW variability seen in the SH winter reported



334 by McCormack et al. [2010] , we will focus on the seasonal evolution of the Q2DW seen in  
335 NOGAPS-ALPHA meridional wind fields. We note that the time behavior of the Q2DW  
336 in temperature during NH summer (not shown) closely matches the time behavior in  
337 meridional wind.

338 Figure 7 plots [0.5,3] amplitudes in meridional wind at 0.021 hPa ( $\sim 75$  km) as a  
339 function of latitude and time throughout the NH summers of 2007, 2008, and 2009. In  
340 all three cases, the amplitudes exhibit a double-peaked structure during July that can  
341 extend from  $\sim 50^\circ\text{N}$  across the equator to  $20^\circ\text{S}$ . Maximum amplitudes of  $17\text{ m s}^{-1}$ ,  $22\text{ m}$   
342  $\text{s}^{-1}$ , and  $23\text{ m s}^{-1}$  are found between  $30^\circ - 50^\circ\text{N}$  during July of 2007, 2008, and 2009,  
343 respectively. The smaller maximum wind amplitude at this level in 2007 is consistent with  
344 the smaller monthly mean [0.5,3] amplitudes noted in both temperature and meridional  
345 wind throughout the Northern extratropical mesosphere during July 2007 (Fig. 4a,b).  
346 We note that the region of peak [0.5,3] amplitude is more narrowly confined in latitude  
347 during the 2007 summer case than during the 2008 and 2009 cases.

348 Figure 8 plots the [0.5,4] meridional wind amplitude at 0.021 hPa for the NH summers  
349 of 2007, 2008, and 2009. We find that the seasonal behavior of the wavenumber 4 Q2DW  
350 differs considerably from the behavior of wavenumber 3. For example, maximum [0.5,4]  
351 wind amplitudes of  $22\text{ m s}^{-1}$  and  $19\text{ m s}^{-1}$  are found in early August of 2007 and 2009,  
352 respectively. In contrast, in 2008 the maximum amplitude of  $16\text{ m s}^{-1}$  occurs in late June.  
353 Overall, the meridional extent of the [0.5,4] component for all three summers at this level  
354 is narrower in latitude than for [0.5,3].

355 The double-peak structure in the Q2DW amplitudes throughout NH summer are con-  
356 sistent with the results in Tunbridge et al. [2011, their Fig. 10]. This is to be expected,

357 since the NOGAPS-ALPHA assimilates the same MLS temperature observations (in ad-  
358 dition to SABER temperature observations). Offerman et al. [2011] found similar seasonal  
359 behavior of the Q2DW from upper mesospheric OH temperature measurements during  
360 2004-2009, i.e., two peaks in Q2DW amplitude in early and late NH summer, although  
361 this study was not able to distinguish among different wavenumber components of the  
362 Q2DW. Offerman et al. [2011] also reported a peak in Q2DW temperature amplitudes in  
363 April, giving rise to an apparent triple-peak structure throughout the NH spring-summer  
364 period. We do not, however, find any evidence for Q2DW activity during April or May of  
365 2007, 2008, or 2009 in the present analysis of NOGAPS-ALPHA wind and temperature  
366 fields. One possible explanation for this discrepancy may be that the daily sampling rate  
367 of the OH temperatures may result in aliasing of tidal variations that produces a spu-  
368 rious Q2DW signal under equinoctial conditions. Additional direct comparisons between  
369 NOGAPS-ALPHA fields and independent observations are needed to further investigate  
370 this issue.

### 3.3. Q2DW - Tide Relationships

371 Earlier observational studies [Harris, 1994; Lima et al., 2004; Pancheva, 2006; Hecht  
372 et al., 2010; McCormack et al., 2010] found correlations between the Q2DW and diurnal  
373 migrating tide in meridional winds during SH summer, suggesting nonlinear interactions  
374 through which the former grows at the expense of the latter. To determine if there is a  
375 relationship between the intraseasonal behavior of the Q2DW and the migrating diurnal  
376 tide during NH summer, we next examine the temporal variability of the [1,1] component.  
377 Figure 9 plots the [1,1] meridional wind amplitude as a function of latitude and time at  
378 0.0036 hPa ( $\sim 88$  km) for the NH summer period of 2007, 2008, and 2009. This level is of

379 particular interest as it lies near the location of peak amplitude in the [0.5,3] component  
380 of the meridional winds (see Fig. 4).

381 The [1,1] signal in NOGAPS-ALPHA meridional wind at 0.0036 hPa is largely confined  
382 to the subtropical regions of each hemisphere, which is consistent with earlier studies [e.g.  
383 Norton and Thuburn, 1999; Wu et al., 2008; Lieberman, 1999; Chang et al., 2011]. In all  
384 three years, the tidal amplitudes are at a minimum near solstice and tend to increase as  
385 the summer progresses. A comparison of Figures 7 and 9 indicate an inverse relationship  
386 between the amplitudes of the [0.5,3] Q2DW and the diurnal migrating tide that is con-  
387 sistent with earlier observational studies [e.g. Lima et al., 2004; Pancheva, 2006; Hecht  
388 et al., 2010]. Specifically, the [1,1] amplitudes are largest in July 2007 when Q2DW am-  
389 plitudes are smallest. Salby and Callaghan [2008] demonstrated that larger diurnal tidal  
390 amplitudes can locally reinforce the Q2DW, which promotes instability and wave break-  
391 ing that effectively limit the amplification of the Q2DW. GCM studies [e.g Norton and  
392 Thuburn, 1999; Palo et al., 1999; Chang et al., 2011] have also shown that when Q2DW  
393 amplitudes are large, nonlinear interactions can take place between the [0.5,3] and [1,1]  
394 “parent” waves that produce “child” waves whose frequency/wavenumber characteristics  
395 are determined from combinations of the sums and differences of the parent waves. In this  
396 scenario, the cascade of energy to smaller scales causes the amplitude of the child waves  
397 to grow at the expense of the diurnal tide, producing a strong anti-correlation between  
398 the the Q2DW and diurnal tide shortly after summer solstice.

399 To examine the relationships between the Q2DW and diurnal migrating tide in the NH  
400 summer, Figure 10 plots time series of the [0.5,3], [0.5,4], and [1,1] amplitudes derived  
401 from the 2DFFT analysis at 30°N and 0.0036 hPa over the summers of 2007, 2008, and

402 2009. Correlation coefficients computed among these time series are listed in Table 1.  
403 While there appears to be an inverse relationship between the monthly mean amplitudes  
404 of the diurnal migrating tide and the Q2DW from one summer to the next, there is no  
405 evidence of a strong anti-correlation between [1,1] and either [0.5,3] or [0.5,4] throughout  
406 the month of July to indicate that the Q2DW is growing at the expense of the diurnal  
407 migrating tide via nonlinear wave-wave interaction. Of the three months, only July 2008  
408 exhibits a negative correlation between the tide and the Q2DW, and this appears largely  
409 to be due to steady declines in the Q2DW amplitudes that are coincident with a steady  
410 increase in tidal amplitude. Instead, the highest negative correlations during July 2007  
411 and 2009 are found between [0.5,3] and [0.5,4], suggesting that in some circumstances one  
412 component of the Q2DW may be growing preferentially over another. Overall, the lack of a  
413 strong anti-correlation between the Q2DW and tide indicates that year-to-year variability  
414 in the background state of the NH summertime mesosphere, rather than amplification  
415 of the Q2DW due to interaction with the tides, could be responsible for the interannual  
416 differences in the amplitudes of the Q2DW seen in Figs. 4 and 5. Possible explanations  
417 for this behavior will be explored section 5.

418 In summary, the results of the 2DFFT analysis find that the Q2DW in the NH summers  
419 of 2007, 2008, and 2009 is comprised primarily of zonal wavenumber 3 and wavenumber 4  
420 components whose latitude and altitude structures are consistent with previous observa-  
421 tional studies. Monthly mean amplitudes of both [0.5,3] and [0.5,4] components are largest  
422 during July 2009, and smallest during July 2007. In all 3 summers, the [0.5,3] component  
423 exhibits two periods of peak amplitude; once in early July and again 2-3 weeks later.  
424 The [0.5,4] component, on the other hand, tends to exhibit peak amplitudes in late June

425 and early August. To further investigate the origin of the interannual and intraseasonal  
 426 variability in the Q2DW during these NH summers, the following section examines condi-  
 427 tions favoring Q2DW growth via baroclinic instability using NOGAPS-ALPHA wind and  
 428 temperature fields.

#### 4. EP-Flux Diagnostics

429 In this section, we employ a series of diagnostic calculations to examine the origin  
 430 and growth of the Q2DW in the NH summer based on linear quasigeostrophic theory.  
 431 Such an approach has been used previously to study the behavior of the Q2DW near  
 432 the stratopause [Randel, 1994; Orsolini et al., 1997; Limpasuvan et al., 2000] to identify  
 433 regions of baroclinic and/or barotropic instability favoring Q2DW growth and propagation  
 434 using daily stratospheric meteorological fields. In the present work, we extend this type  
 435 of analysis into the upper mesosphere using global synoptic NOGAPS-ALPHA wind and  
 436 temperature fields.

437 A necessary condition for the growth of the Q2DW in the summer extratropical meso-  
 438 sphere via baroclinic instability is a reversal of the meridional gradient in quasigeostrophic  
 439 potential vorticity  $q$  [see, e.g. Plumb, 1983; Pfister, 1985]. In spherical coordinates this is  
 440 computed from the relation

$$441 \quad \bar{q}_\phi = \frac{2\Omega}{a} \cos\phi - \frac{1}{a} \frac{\partial}{\partial\phi} \left[ \frac{1}{a \cos\phi} \frac{\partial(\bar{u} \cos\phi)}{\partial\phi} \right] - (2\Omega \sin\phi)^2 e^{z/H} \frac{\partial}{\partial z} \left[ \frac{1}{N^2} e^{-z/2H} \frac{\partial \bar{u}}{\partial z} \right] \quad (1)$$

442 where  $p$  is pressure in hPa,  $\phi$  is latitude,  $\bar{u}$  is the zonal mean zonal wind speed in  $\text{m s}^{-1}$ ,  
 443  $H$  is the scale height,  $z$  is the log-pressure vertical coordinate,  $N$  is the Brunt-Vaisala  
 444 frequency,  $a$  is the Earth's radius, and  $\Omega$  is the planetary rotation rate. As equation (1)  
 445 shows, reversals in  $\bar{q}_\phi$  (i.e., from positive to negative values) are determined by the curva-

446 ture in the background zonal wind distribution. Consequently, accurate wind analyses are  
 447 needed to diagnose baroclinic instability. Here we use global NOGAPS-ALPHA horizon-  
 448 tal wind and temperature fields on constant pressure surfaces to compute  $q_\phi$  during July  
 449 of 2007, 2008, and 2009. This information shows how variations in baroclinic instability  
 450 from one NH summer to the next may help to explain the observed interannual variations  
 451 in July Q2DW amplitudes shown in Figs. 4 and 5. While reversal of  $\bar{q}_\phi$  is a necessary  
 452 condition for Q2DW growth through baroclinic instability, it is not sufficient. Conditions  
 453 must support the growth of the disturbance in the absence of a critical line, i.e., where  
 454 the speed of the background flow matches the phase speed of the disturbance.

455 Theory states that growth of the Q2DW is related EP flux divergence in baroclini-  
 456 cally unstable regions [e.g. Plumb, 1983]. The EP flux vector can be computed from the  
 457 eddy heat and momentum fluxes associated with the Q2DW using the relation [see, e.g.  
 458 McCormack et al., 2009, equation 4]

$$459 \quad \mathbf{F}_p[\phi, z] = \rho a \cos\phi \left[ -\overline{\langle u'v' \rangle}, \left( f - \frac{1}{a \cos\phi} [\bar{u} \cos\phi]_\phi \right) \frac{R}{HN^2} \overline{\langle v'T' \rangle} \right]. \quad (2)$$

460 The terms  $\overline{\langle u'v' \rangle}$ , and  $\overline{\langle v'T' \rangle}$  represent zonal mean eddy momentum and heat fluxes,  
 461 primes denote deviations from the zonal mean and brackets denote a daily average. These  
 462 quantities are computed from gridded six-hourly NOGAPS-ALPHA zonal wind, merid-  
 463 ional wind, and temperature fields that have been band-pass filtered in order to isolate  
 464 the [0.5,3] or [0.5,4] components of the Q2DW, as described in Section 2.

465 Calculating EP flux from eddy heat and momentum fluxes related to the Q2DW requires  
 466 synoptic horizontal wind and temperature fields throughout the MLT region. Although  
 467 numerous modeling studies have examined EP flux-based diagnostics of the Q2DW, only  
 468 a few studies have used observations to calculate EP fluxes associated with the Q2DW.

469 For example, Lieberman [1999] used High Resolution Doppler Imager (HRDI) wind and  
 470 temperature observations from January 1994 to compute EP flux divergences in the SH  
 471 summer mesosphere. More recently, the study by Offerman et al. [2011] used geostrophic  
 472 winds derived from Microwave Limb Sounder (MLS) temperature measurements to re-  
 473 late the occurrence of baroclinically unstable conditions to the seasonal variability in the  
 474 Q2DW observed from ground-based stations in northern Europe. Here we use output  
 475 from the NOGAPS-ALPHA global HDAS to describe EP flux divergence associated with  
 476 both [0.5,3] and [0.5,4] components of the Q2DW in the NH summer.

477 Figure 11 plots EP flux vectors related to the [0.5,3] Q2DW for three cases: 20 July  
 478 2007 (Fig. 10a), 16 July 2008, and 23 July 2009 (Fig. 10c). These three cases were chosen  
 479 based on the large Q2DW amplitudes observed on these dates (see Fig. 7). Also plotted in  
 480 Fig. 11 is the daily average zonal mean zonal wind distribution for these days, from which  
 481 we calculate values of  $\bar{q}_\phi$ . To illustrate the relationship between baroclinically unstable  
 482 regions and Q2DW growth, shaded regions in Fig. 11 indicate where  $\bar{q}_\phi$  is negative. In all  
 483 three cases, Fig. 9 shows EP flux divergence related to the [0.5,3] component of the Q2DW  
 484 near the core of the easterly jet between 0.05 – 0.1 hPa. The direction of the EP flux  
 485 vectors indicate propagation of wave activity away from the approximate location of the  
 486 critical line for the [0.5,3] wave, which is indicated by the bold red contour. In the lower  
 487 mesosphere the propagation is primarily equatorward, while in the upper mesosphere it  
 488 is primarily poleward and upward.

489 Figure 12 plots the EP fluxes of the Q2DW for three cases where amplitudes of the  
 490 [0.5,4] component were largest during the three NH summers: 4 August 2007 (Fig. 12a),  
 491 22 June 2008 (Fig. 12b), and 4 July 2009 (Fig. 12c). Wave activity associated with the

492 [0.5,4] component originates just equatorward of the easterly jet core between 0.1 – 0.2  
493 hPa and propagates away from the estimated location of the critical line (blue contour in  
494 Fig. 12), mainly in the upward and poleward direction. It is interesting to note how the  
495 locations of the critical lines in Figs. 11 and 12, which are determined by the curvature of  
496 the zonal mean zonal wind, can affect the upward propagation of the Q2DW. For example,  
497 in the 2007 case (Fig. 11a) the summer easterly jet is weaker and exhibits a poleward  
498 tilt with increasing altitude between 40°–65°N, which leads to a gradual sloping of the  
499 critical lines upward and poleward, away from the source regions. In the 2008 and 2009  
500 cases, the jet is stronger and its core is centered between between 40°–50°N, producing a  
501 “bull-nose” shape in the location of the critical lines where the equatorward edge of the  
502 critical lines extend higher in altitude than in the 2007 case. In particular, the higher  
503 extent of the critical lines in the 2009 case (see Fig. 11c and Fig. 12c) appears to direct  
504 more Q2DW activity upward into the region above the 0.01 hPa level.

505 To further examine the relationship between the location of the Q2DW critical line  
506 and vertical wave propagation during NH summer, Figure 13 plots the time evolution of  
507 zonal mean zonal winds over the NH extratropics during July of 2007, 2008, and 2009 at  
508 0.021 hPa. Superimposed upon the wind contours are regions where  $q_\phi$  is negative (gray  
509 shading). Also plotted in Fig. 12 are values of the eddy heat flux (heavy black contours),  
510 that are proportional to the vertical component of the EP-flux (equation 2). During July  
511 2007 (Fig. 13a) the location of the [0.5,3] critical line retreats poleward as the month  
512 progresses due to the weakening easterly jet. In contrast, the stronger easterly jet during  
513 July 2008 and 2009 (Fig. 13b and 13c) maintains the position of the [0.5,3] critical line



514 near  $40^{\circ}\text{N}$  throughout the month. As a result, there are more sustained periods of high  
515 eddy heat flux during July 2008 and 2009.

516 These results indicate that the larger monthly mean Q2DW amplitudes in July during  
517 2008 and 2009 as compared to July 2007 can be attributed to the characteristics of the  
518 summer easterly jet. Specifically, a stronger and more sustained jet core near the Q2DW  
519 source region acts to focus more wave activity upward through a smaller area by nature of  
520 the critical line's location. A weaker jet core, on the other hand, results in the critical line  
521 sloping away from the source region that allows upward wave activity to spread throughout  
522 a much wider area. Figure 14 summarizes this relationship, plotting time series of the  
523 zonal mean zonal winds at  $40^{\circ}\text{N}$  and 0.1 hPa from 1 June to 31 August of 2007, 2008, and  
524 2009. The zonal mean easterly flow was strongest throughout the summer of 2009, when  
525 Q2DW amplitudes were largest. During summer 2007, when Q2DW amplitudes were  
526 smallest, the easterly jet briefly peaks in early July and is relatively weak both before and  
527 after that time. In 2008, the peak winds were somewhat weaker than in 2007, but they  
528 were more sustained, coincident with monthly mean Q2DW amplitudes that were larger  
529 than 2007.

530 The EP-flux diagnostics based on the NOGAPS-ALPHA meteorological fields indicate  
531 that the Q2DW originates from baroclinic instabilities near the equatorward flank of the  
532 mesospheric summer easterly jet. The interannual variability of the Q2DW amplitudes  
533 in NH summer over the 2007 – 2009 period closely follows interannual variability in the  
534 strength and position of the summer easterly jet core, which determines the locations of  
535 the critical lines for the [0.5,3] and [0.5,4] components of the Q2DW. As the results in  
536 section 3 show, both wavenumber 3 and wavenumber 4 components of the Q2DW are of

537 comparable magnitude in NH summer, and they both exhibit a high degree of variability  
 538 throughout the summer season. In the next section, we use a linearized instability model  
 539 to examine this intraseasonal variability in more detail

## 5. Instability Model Results

540 The results in the preceding sections show that both wavenumber 3 and wavenumber  
 541 4 components of the Q2DW arise from baroclinically unstable regions near the summer  
 542 easterly jet at midlatitudes in the the NH mesosphere. As Figures 7 and 8 illustrate, am-  
 543 plitudes of the [0.5,3] component are typically largest in July, while the largest amplitudes  
 544 of the [0.5,4] component generally occur in late June or early August. This variability  
 545 is consistent with an earlier study of the NH Q2DW by Tunbridge et al. [2011], which  
 546 showed that in some years the amplitude of the [0.5,4] component surpasses the amplitude  
 547 of the [0.5,3] component in August.

548 To better understand the origins of this behavior, we use a simple linear instability  
 549 model to examine the characteristics of the fastest-growing unstable modes in the MLT  
 550 region near the NH summer easterly jet. This approach has been used to study other  
 551 types of free traveling planetary waves in the MLT [e.g. Hartmann, 1983; Manney and  
 552 Randel, 1993]. The model is based on the linearized quasi-geostrophic potential vorticity  
 553 equation for frictionless, adiabatic flow on a  $\beta$ -plane centered at midlatitudes [see, e.g.  
 554 Andrews et al., 1987, their equation 3.4.5]:

$$555 \quad q'_t + \bar{u}q'_x + v'\bar{q}_y = 0. \quad (3)$$

556 Here the potential vorticity is derived from the NOGAPS-ALPHA horizontal wind  
 557 fields. Formulating the zonal wind and potential vorticity distributions in terms of the

558 geostrophic stream function and assuming periodic solutions as functions of both latitude  
 559 and time allows equation (3) to be cast as an eigenvalue problem of the form

$$560 \quad \mathbf{A}x = c\mathbf{B}x \quad (4)$$

561 where  $x$  is the state vector represented by gridded values of the streamfunction and the  
 562 complex phase speed  $c$  is the eigenvalue. The operator  $\mathbf{A}$  is determined from  $\bar{u}$  and  $\bar{q}_y$ ,  
 563 the operator  $\mathbf{B}$  is determined from the finite-differenced potential vorticity equation; both  
 564  $\mathbf{A}$  and  $\mathbf{B}$  depend on the zonal wavenumber.

565 To simplify the calculation, the daily averaged values of NOGAPS-ALPHA zonal wind  
 566 fields are subsampled onto the instability model domain, which consists of a uniform grid  
 567 with 20 points in latitude extending from  $20^\circ - 60^\circ$  N latitude and 26 points in altitude  
 568 extending from 65 – 90 km. For a given day,  $\mathbf{A}$  and  $\mathbf{B}$  are constructed from using the  
 569 geostrophic streamfunction and potential vorticity using these subsampled daily averaged  
 570 zonal winds. Standard numerical codes are then used to solve the eigenvalue problem  
 571 and obtain  $\mathbf{x}$  (i.e., the wave modes) and  $\mathbf{c}$  (i.e., phase speeds) for zonal wavenumbers 1  
 572 through 6. The fastest growing modes are evaluated in terms of their  $e$ -folding times,  
 573 which are determined from the inverse of the imaginary component of the phase speed  
 574 for each zonal wavenumber. The periods of the unstable modes are determined from the  
 575 real component of the phase speed (positive values indicate westward propagation). In  
 576 addition, each mode's spatial structure contains wind and temperature information from  
 577 which EP fluxes can be computed.

578 In this discussion, we focus on the summer of 2009 when the Q2DW was most prominent.  
 579 We first examine model output for two individual cases: 10 July and 5 August. These

580 cases were chose to highlight the development of the [0.5,3] and [0.5,4] components of the  
581 Q2DW, respectively, during the NH summer of 2009. Figure 15a plots the zonal wind  
582 and  $\bar{q}_y$  distributions over the model domain for the 10 July case. We find that zonal  
583 wavenumbers 3, 4, and 5 exhibit the fastest growth rates, with  $e$ -folding times of  $\sim 8$ – $9$   
584 days (Fig. 15b). The normalized streamfunction amplitudes of waves 1–4 (Fig. 15c-e)  
585 have maxima in the region between  $30^\circ - 40^\circ\text{N}$  and  $60$ – $70\text{km}$ , which closely resembles the  
586 observed spatial structure of the [0.5,3] temperature Q2DW in Figure 4. In general, the  
587 period of the fastest growing modes decreases with increasing horizontal scale. On this  
588 particular day, the zonal wavenumber 3 (Fig. 14e) solution has a period of 2 days, and  
589 the wavenumber 4 solution has a period of 1.5 days.

590 Figure 16 plots instability model results for the 5 August 2009 case. We find that the  
591 fastest growing modes are again at zonal wavenumbers 3, 4, and 5 (Fig. 16b). However,  
592 the  $e$ -folding times of 3–4 days are much shorter than the July case. The spatial structure  
593 of the waves in this case now exhibits two maxima (Figs. 16c-e) centered near  $35^\circ\text{N}$  and  
594  $45^\circ\text{N}$ . For this August case, the zonal wavenumber 3 (Fig. 16e) solution has a period of  
595 3.1 days and the wavenumber 4 solution has a period of 2.3 days.

596 In order to determine the direction of wave propagation for the instability model solu-  
597 tions related to the Q2DW, Figure 17 plots EP fluxes calculated from the streamfunctions  
598 of the zonal wavenumber 3 and 4 eigenvectors for the July and August cases, respectively.  
599 For both cases, the EP-flux vectors derived from the model solutions indicate that most  
600 of the upward-propagating wave activity originates near the intersection of the critical  
601 line for the Q2DW (blue contour) and the region where  $\bar{q}_y$  is negative (enclosed by the  
602 red contour). This result is consistent with the EP-flux vectors derived directly from the

603 assimilated winds and temperatures plotted in Figs. 11 and 12, and lends support to the  
604 idea that the variability of the NH Q2DW is closely linked to the characteristics of the  
605 summer midlatitude easterly jet.

606 The results from these two cases show that the growth time of the Q2DW decreased  
607 by a factor of 2–3 between early July and early August 2009. To determine if this is a  
608 systematic effect, the stability model was applied to daily average NOGAPS-ALPHA zonal  
609 wind throughout the period from 5 June–10 August 2009. Figure 18 plots the resulting  
610 values of the period and growth time for both wavenumber 3 and 4 solutions. For plotting  
611 purposes, these time series have been smoothed using a 3-point running average. During  
612 much of June and early July, both wavenumbers have periods near 2 days (Fig. 18a).  
613 Starting in mid-July, the periods increase sharply and then vary in the 3–7 day range  
614 thereafter. By late summer, the period of wavenumber 4 is consistently 1–2 days shorter  
615 than wavenumber 4. The growth time of wavenumber 4 is shorter than wavenumber 4  
616 throughout most of the summer (Fig. 18b), and the growth times of wavenumbers 3 and  
617 4 both decrease sharply during late-July and early August. These calculations have also  
618 been performed for the summers of 2007 and 2008, and similar decreases in growth times  
619 from July to August were found in each case (not shown).

620 As previous studies have shown, the results from these types of model calculations can be  
621 highly sensitive to the curvature of the zonal wind fields, and thus averaging or smoothing  
622 of the input dynamical fields can affect the results. We present these calculations to  
623 better understand, in a qualitative sense, possible factors that contribute to the observed  
624 intraseasonal variability of the NH Q2DW. From these results, we can conclude that the  
625 baroclinically unstable region along the equatorward flank of the NH summer easterly jet

626 produces the fastest-growing modes at wavenumbers 3, 4, and 5. During June and July,  
627 the periods of the wavenumber 3 and 4 modes most closely match the 2-day period of the  
628 Rossby normal mode, and these grow preferentially over other modes.

629 These results alone do not explain why the observed [0.5,3] component of the Q2DW  
630 is larger during July while the [0.5,4] component is larger in June and August. Nor do  
631 they account for the sporadic behavior of the Q2DW which tends to produce the double  
632 peaked structure observed in, e.g., Figure 7. However, based on the observational and  
633 model results presented here, we speculate that one possible explanation for this behavior  
634 may be that the faster-growing wavenumber 4 unstable mode tends to emerge initially  
635 in June, only to be overtaken by the slower-growing wavenumber 3 mode. The observed  
636 anti-correlation between the [0.5,3] and [0.5,4] components of the Q2DW during July 2009  
637 suggests that wavenumber 3 may in fact grow at the expense of wavenumber 4 through  
638 some nonlinear interaction. When the Q2DW amplitudes and associated EP fluxes grow  
639 large enough to become unstable and dissipate, they modify the vertical shear structure in  
640 the background zonal wind such that it no longer produces fast-growing unstable modes  
641 at zonal wavenumbers 3 and 4 with periods near 2 days. This would be consistent with  
642 the sudden increase in the period of the unstable wave 3 and wave 4 modes in mid-July  
643 2009 (Fig. 18a). As baroclinically unstable regions near the easterly jet reform after the  
644 Q2DW dissipates, another fast-growing zonal wave 4 mode can emerge in late July or  
645 early August. However, by this time the effects of a weakening easterly jet (Fig. 14)  
646 and increasing tidal amplitudes (Fig. 9) will combine to limit growth of the slower [0.5,3]  
647 mode. Fully interactive GCM simulations are needed to test this hypothesis by studying

648 the origin and growth of these various unstable modes in concert with fluctuations in the  
649 strength and curvature of the easterly jet for realistic conditions.

## 6. Summary and Discussion

650 Global synoptic meteorological analyses of the MLT from the NOGAPS-ALPHA data  
651 assimilation system have provided, for the first time, a comprehensive description of  
652 Q2DW behavior during the NH summers of 2007, 2008, and 2009. Unlike the SH case,  
653 where the Q2DW is primarily a westward propagating zonal wavenumber 3 feature, we  
654 find that the Q2DW in NH summer is comprised primarily of westward propagating zonal  
655 wavenumber 3 and wavenumber 4 components that are comparable in magnitude, con-  
656 sistent with earlier observational studies. Wavenumber 3 tends to maximize during July,  
657 while wavenumber 4 tends to maximize in late June and early August. We did not find  
658 evidence for significant Q2DW activity in the NH extratropics outside of the June–August  
659 period. At latitudes between  $30^{\circ} - 50^{\circ}\text{N}$ , where the Q2DW amplitudes are largest, the  
660 wavenumber 3 and wavenumber 4 components are often anti-correlated throughout the  
661 NH summer season. Of the three summer periods examined here, the monthly mean  
662 wavenumber 3 Q2DW amplitudes are largest in July 2009 and smallest in July 2007,  
663 whereas the monthly mean amplitudes of the diurnal migrating tide at  $30^{\circ}\text{N}$  are largest  
664 in July 2007 and smallest in 2009.

665 Diagnostic calculations based on NOGAPS-ALPHA output indicate that the Q2DW  
666 originates from baroclinically unstable regions on the equatorward flank of the summer  
667 easterly jet near the 0.1 hPa level ( $\sim 65\text{--}70$  km). The vertical propagation of the Q2DW  
668 activity appears to be controlled by the location of the critical line. The large wavenumber  
669 3 amplitudes observed during July 2009 coincide with a relatively strong and well-defined

670 easterly jet core that directed more wave activity upward compared to July 2007, when  
671 the jet core was smaller and weaker.

672 Results from a linearized instability model using daily NOGAPS-ALPHA winds for  
673 summer 2009 as input show that the baroclinically unstable region near the summer  
674 easterly jet supports growth of both zonal wavenumber 3 and 4 disturbances with periods  
675 near 2 days. The growth times of these disturbances are typically in the range of 10–  
676 20 days during July, but approach  $\sim 5$  days in early August. Using a similar modeling  
677 approach based on winds from a mechanistic global circulation model (GCM), Rojas  
678 and Norton [2007] found evidence for two zonal wavenumber 3 modes with growth times  
679 between 3–5 days: a faster growing mode with period of 35 hours and a slower growing  
680 mode with a period of 42 hours. In this study, the faster growing mode quickly reached  
681 saturation at relatively small amplitude while the slower growing mode continued to grow  
682 to much larger amplitude and then began to interact with the background flow. In the  
683 present study, qualitatively similar behavior can be seen in the anti-correlation between the  
684 faster growing [0.5,4] and slower growing [0.5,3] components of the Q2DW (e.g., Fig. 10).  
685 We plan to pursue this subject further by conducting free-running model simulations using  
686 the NOGAPS-ALPHA meteorological fields as initial conditions to determine whether  
687 the [0.5,3] component interacts with the [0.5,4] components as it grows, or if the two  
688 components grow independently from one other.

689 Although the results of the 2DFFT analysis suggest an anticorrelation between the  
690 monthly mean amplitudes of the Q2DW and diurnal migrating tide during July, we do  
691 not find direct evidence for the type of interaction that can sometimes lead to rapid  
692 amplification of the Q2DW in SH summer [e.g. Norton and Thuburn, 1999; Palo et al.,



1999; McCormack et al., 2010; Hecht et al., 2010; Chang et al., 2011; Yue et al., 2012]. This is likely due to the smaller amplitudes and more broad band nature of the Q2DW in NH summer compared to SH summer, which reduces the chances for the type of interaction described by Walterscheid and Vincent [1996]. A modeling study of the SH Q2DW in January by Chang et al. [2011] found that nonlinear advection of momentum by the Q2DW itself may introduce variations in the background flow and, by extension, in tidal amplitudes that can also account for anti-correlation between the Q2DW and migrating diurnal tide. Other factors controlling the year-to-year variations in the strength and location of the NH summer easterly jet such as gravity wave activity may also play a role in controlling the behavior of both the Q2DW and tides. While the Q2DW-tide relationship in the SH summer has been the subject of numerous studies, there has been relatively little study of this relationship in the NH summer. To further investigate the nature of possible Q2DW-tidal coupling in NH summer, a targeted series of global circulation model (GCM) experiments capable of accurately simulating the evolution of the background zonal flow throughout the NH summer MLT is needed. Recently, Sassi et al. (*submitted*, 2013) used a GCM driven by NOGAPS-ALPHA meteorological fields in the lower atmosphere to generate a Q2DW in the the SH summer MLT internally through baroclinic instability processes, rather than through means of an imposed forcing. This approach will be extended to the NH summer cases of 2007, 2008, and 2009 in order to further investigate the nature of the Q2DW-tidal relationships presented here.

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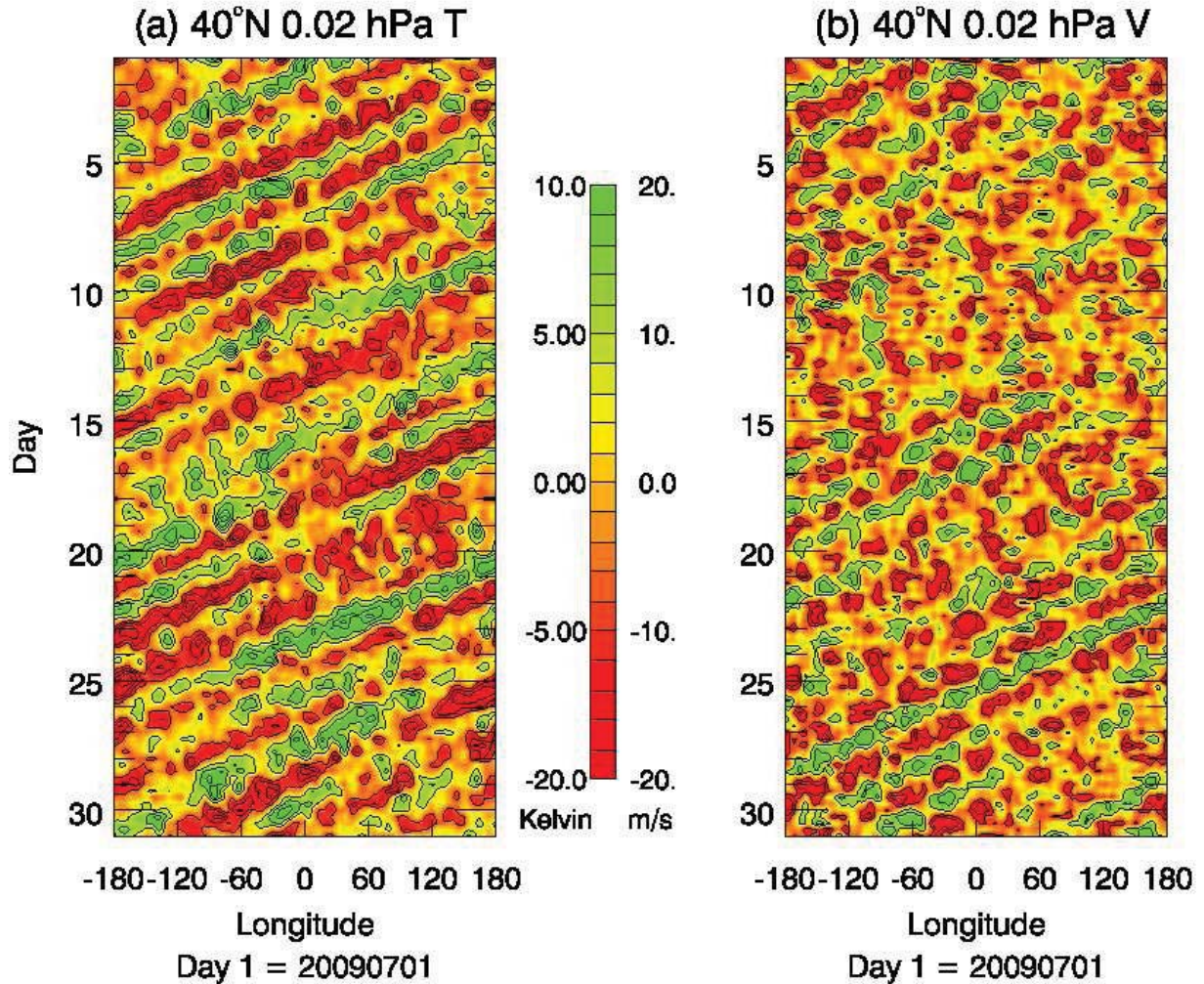
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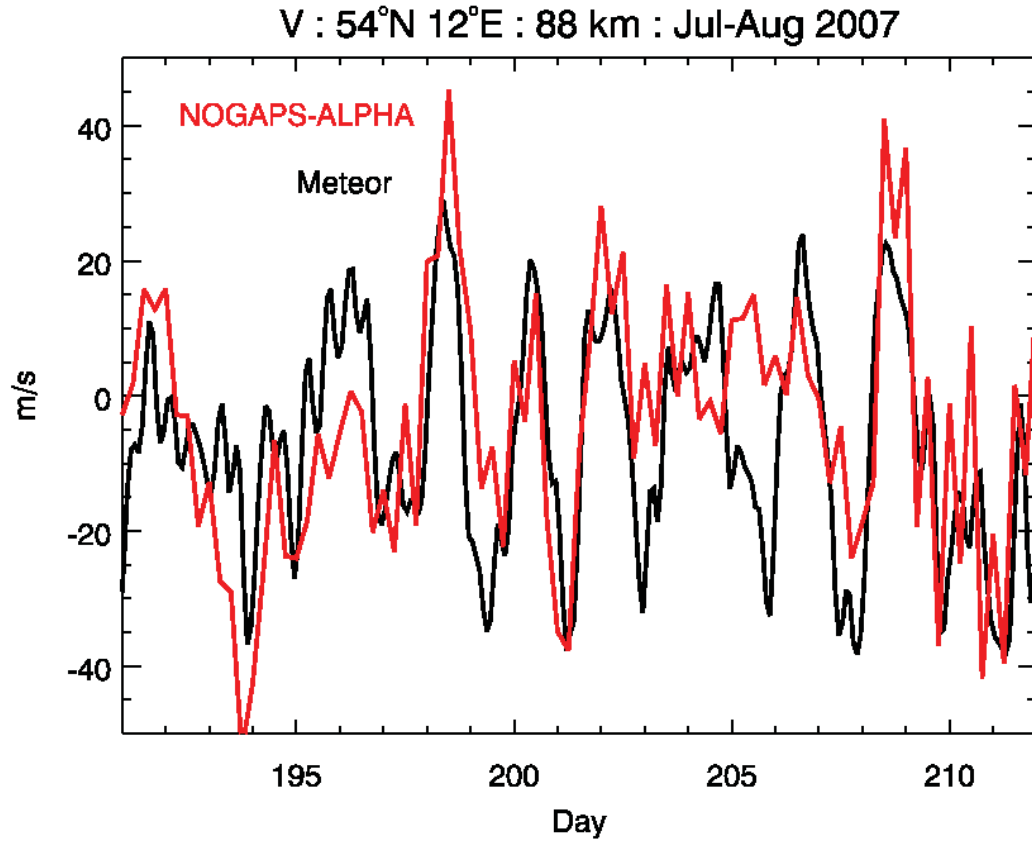


**Table 1.** Correlation coefficients among [1,1], [0.5,3] and [0.5,4] meridional wind amplitudes at 30°N and 0.0036 hPa during July.

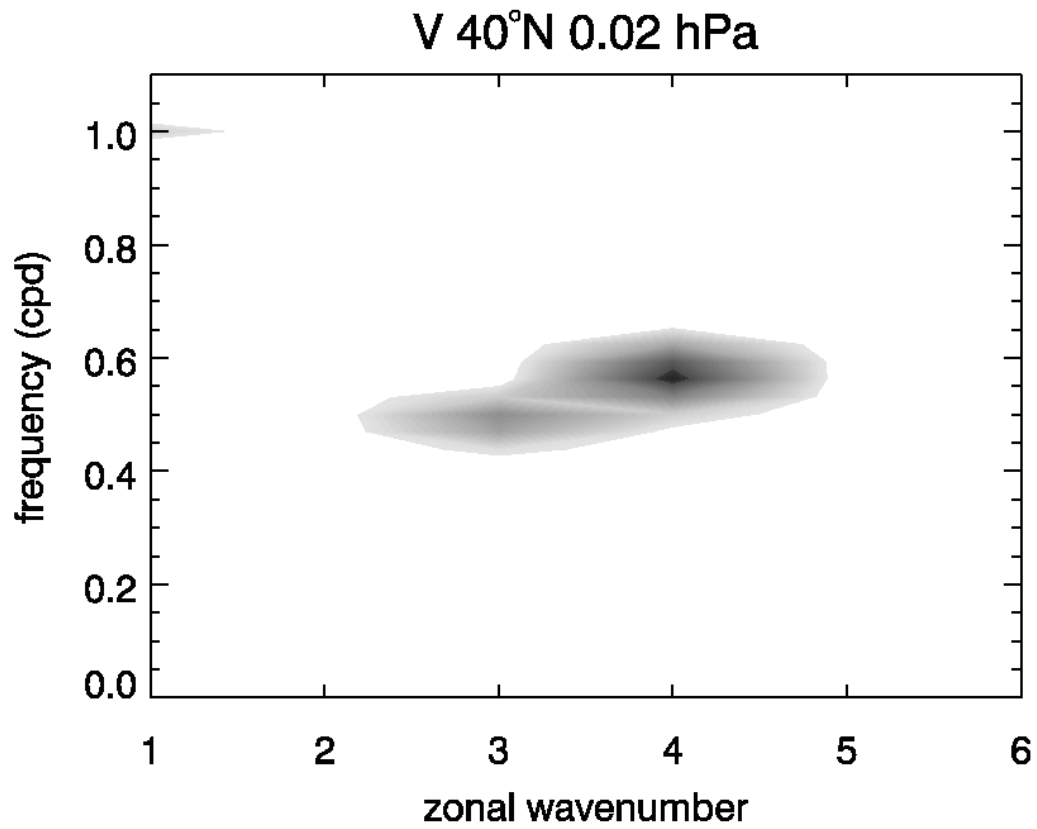
Year	[1,1] vs. [0.5,3]	[1,1] vs. [0.5,4]	[0.5,3] vs. [0.5,4]
2007	0.16	0.26	-0.47
2008	-0.35	-0.44	0.2
2009	0.00	0.1	-0.42



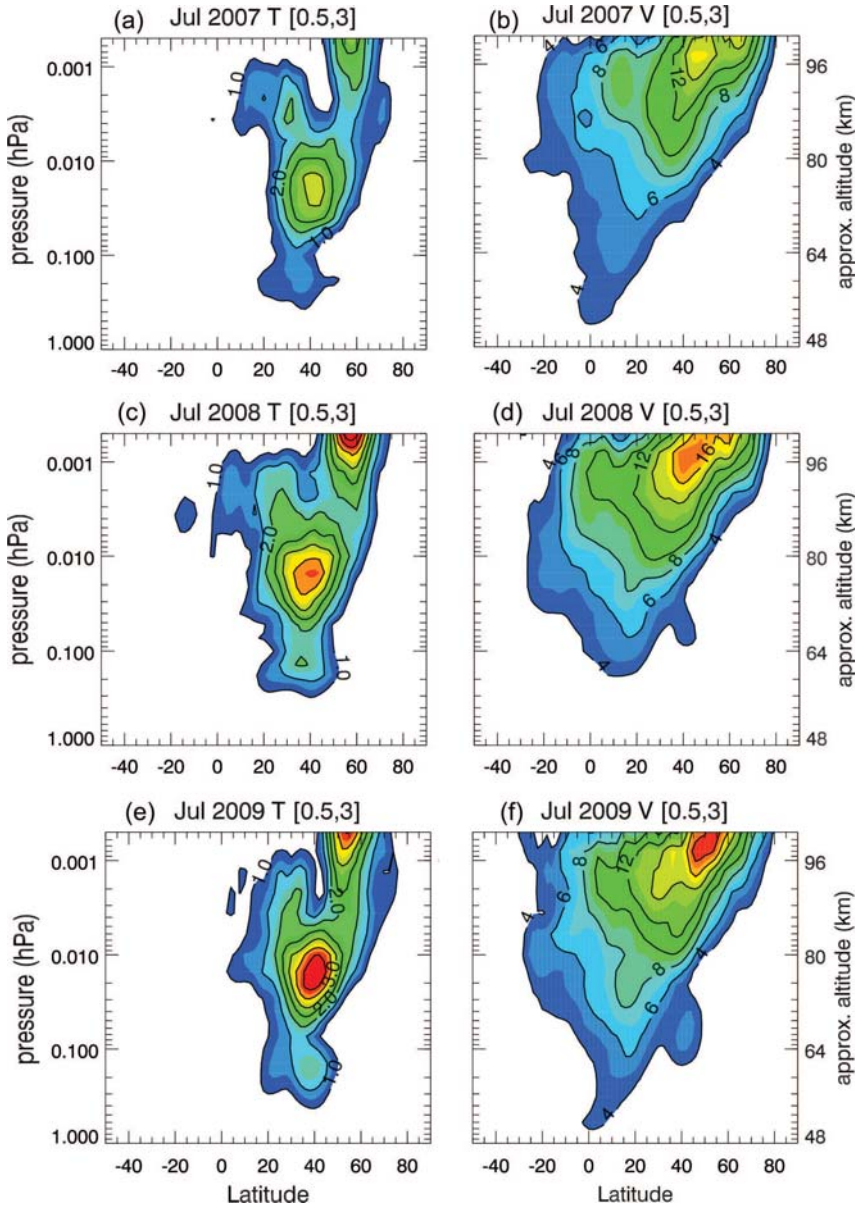
**Figure 1.** Hovmöller plot of NOGAPS-ALPHA (a) temperature and (b) meridional wind anomalies at 40°N and 0.02 hPa for July 2009.



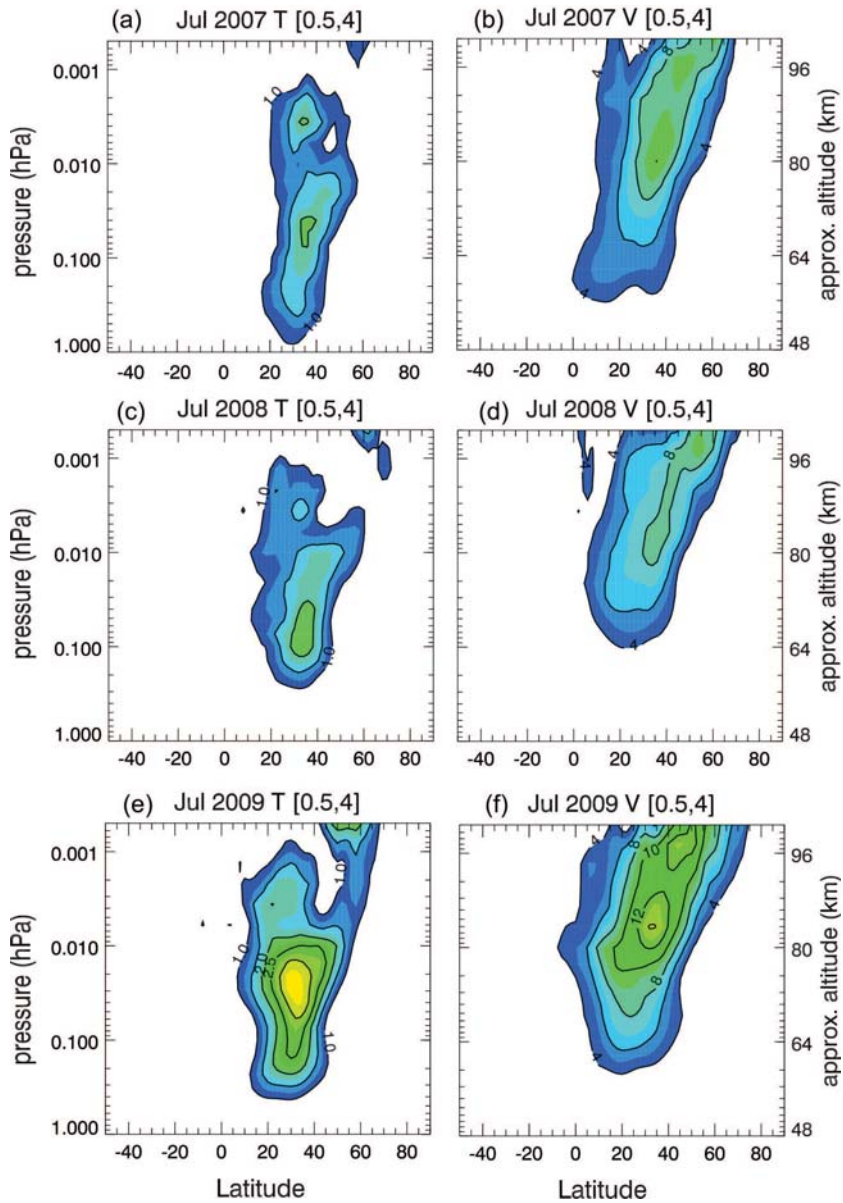
**Figure 2.** Time series of meridional winds from meteor radar observations over Kühlungsborn at 88 km (black curve) and from coincident NOGAPS-ALPHA analyses at 0.0036 hPa (red curve) during July – August 2007.



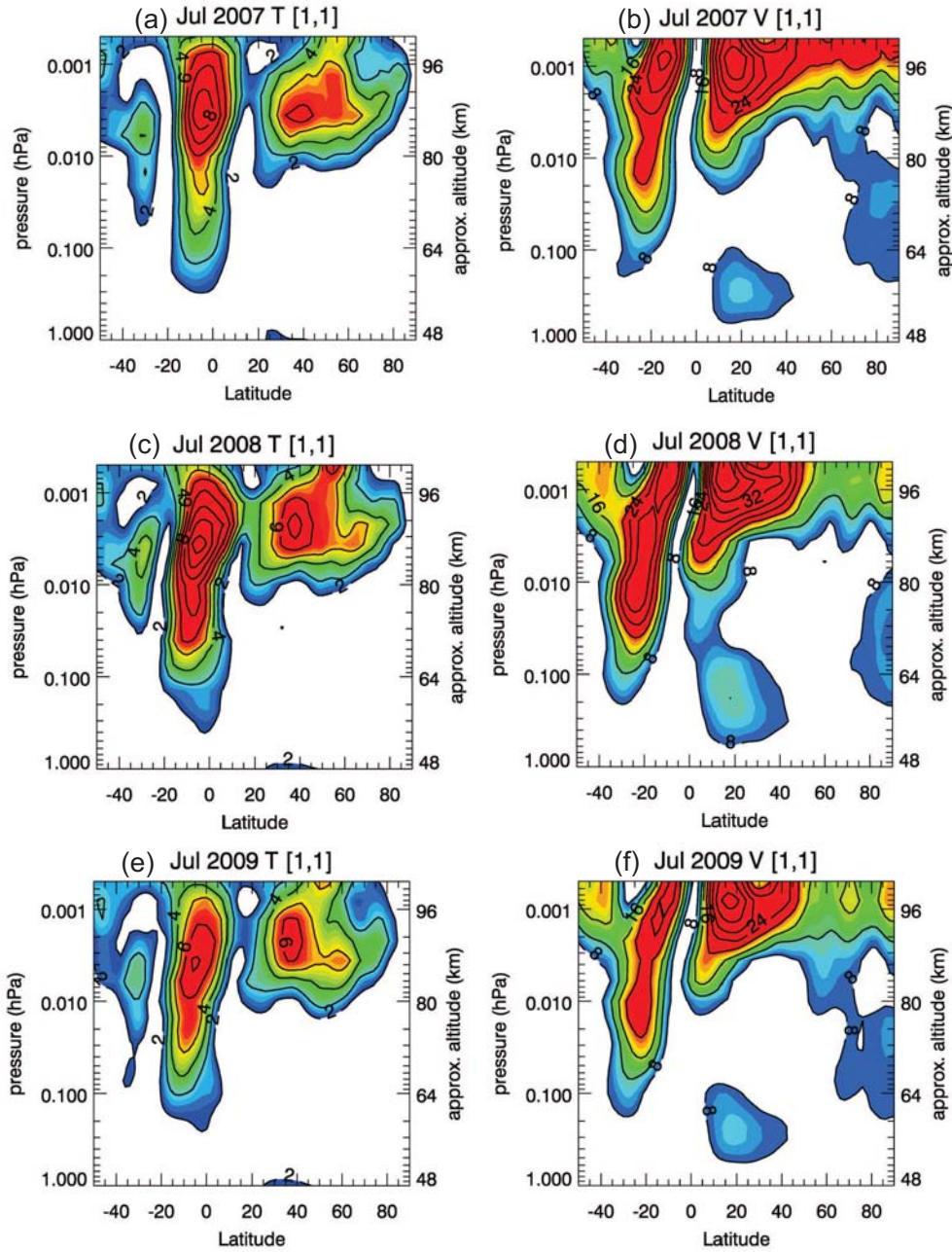
**Figure 3.** Normalized power spectrum obtained from 2DFFT of NOGAPS-ALPHA meridional winds at 40°N and 0.021 hPa. Positive frequencies denote westward propagation.



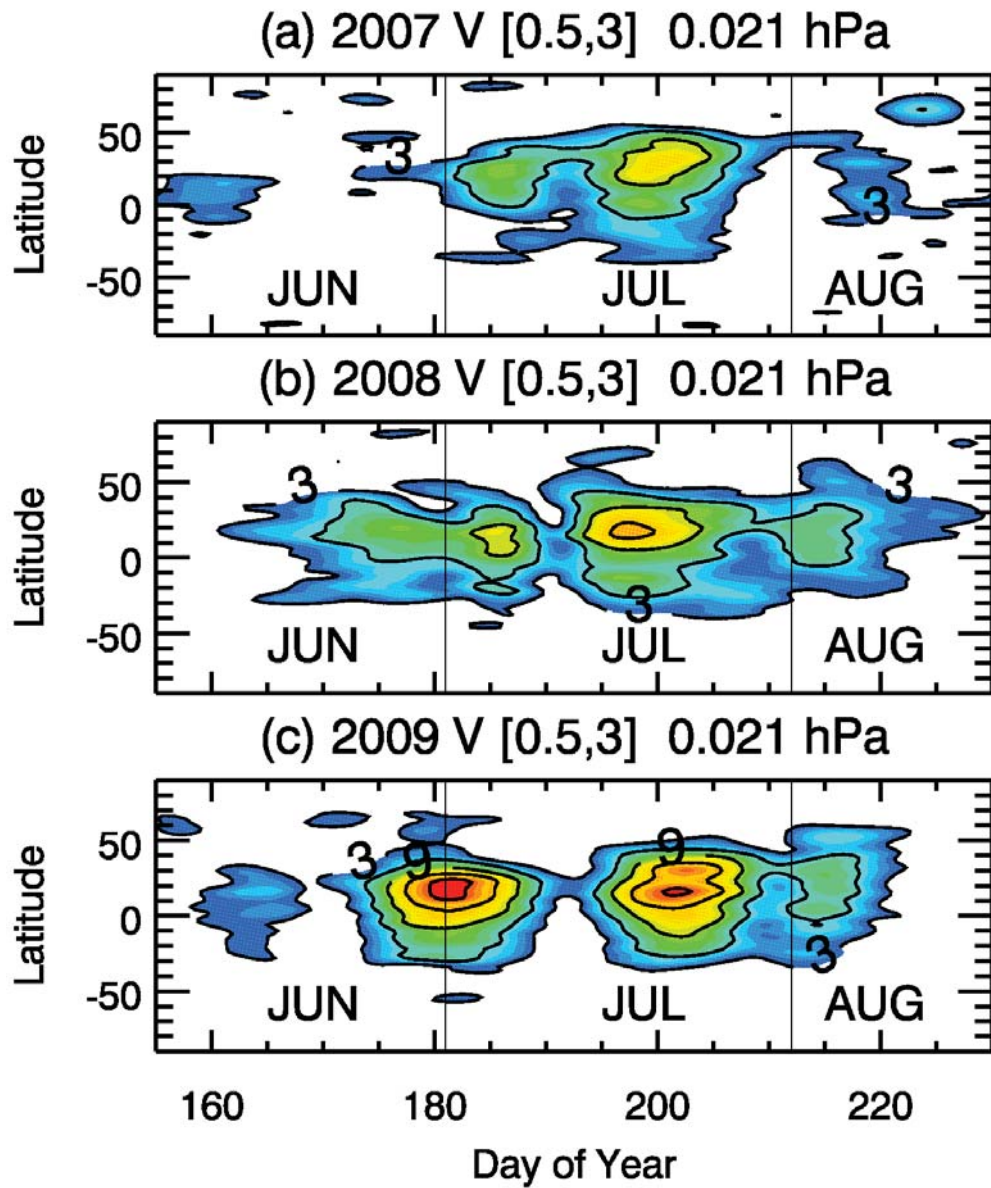
**Figure 4.** Monthly mean amplitudes of the [0.5,3] Q2DW component in temperature and meridional wind for July 2007, 2008, and 2009. Contour intervals are 0.5 K and  $2 \text{ m s}^{-1}$ .



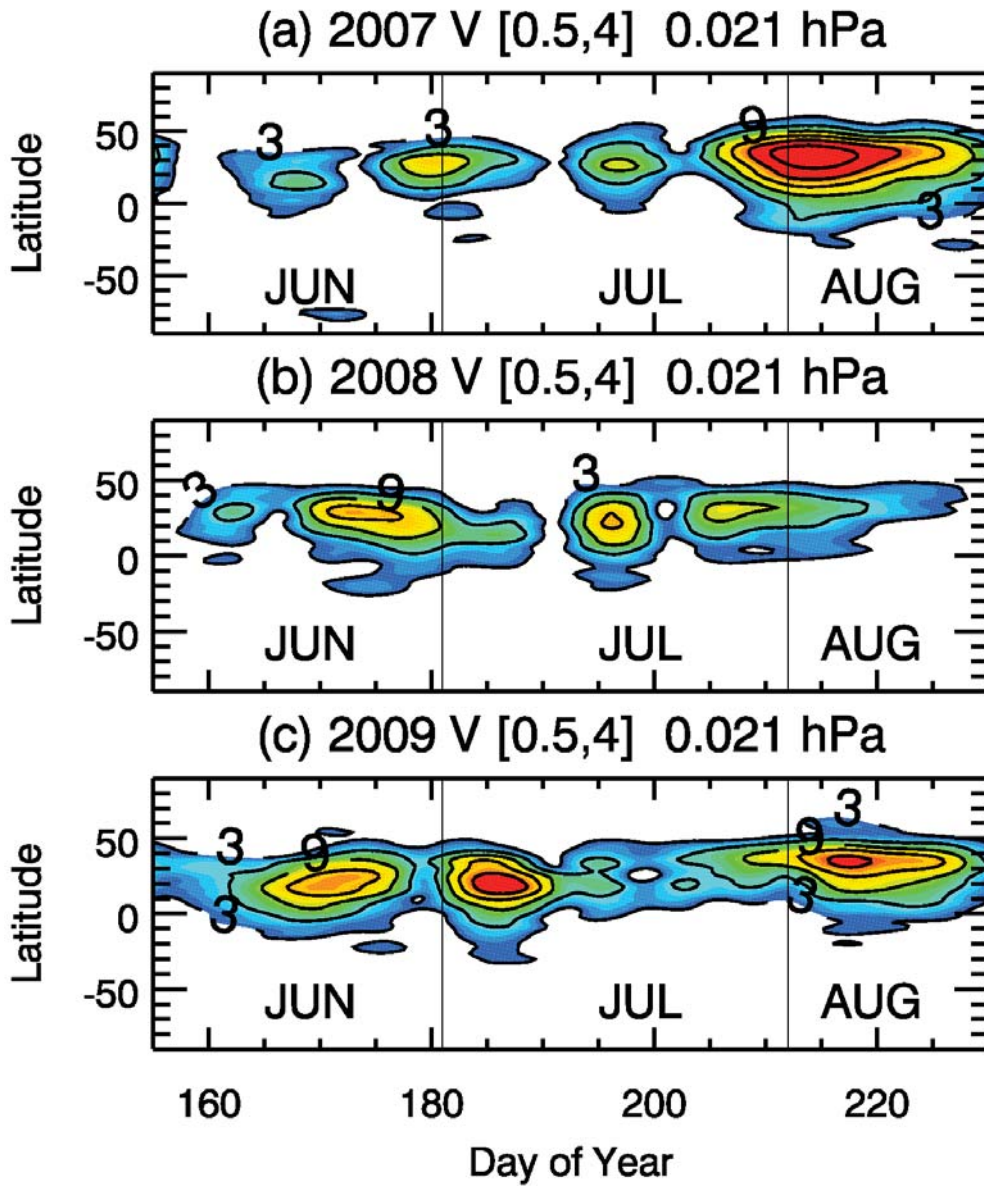
**Figure 5.** Monthly mean amplitudes of the [0.5,4] Q2DW component in temperature and meridional wind 1428 for July 2007, 2008, and 2009. Contour intervals are 0.5 K and  $2 \text{ m s}^{-1}$ .



**Figure 6.** Monthly mean amplitudes of the [1,1] migrating diurnal tide in temperature and meridional wind 1428 for July 2007, 2008, and 2009. Contour intervals are 1 K and 4 m s<sup>-1</sup>.

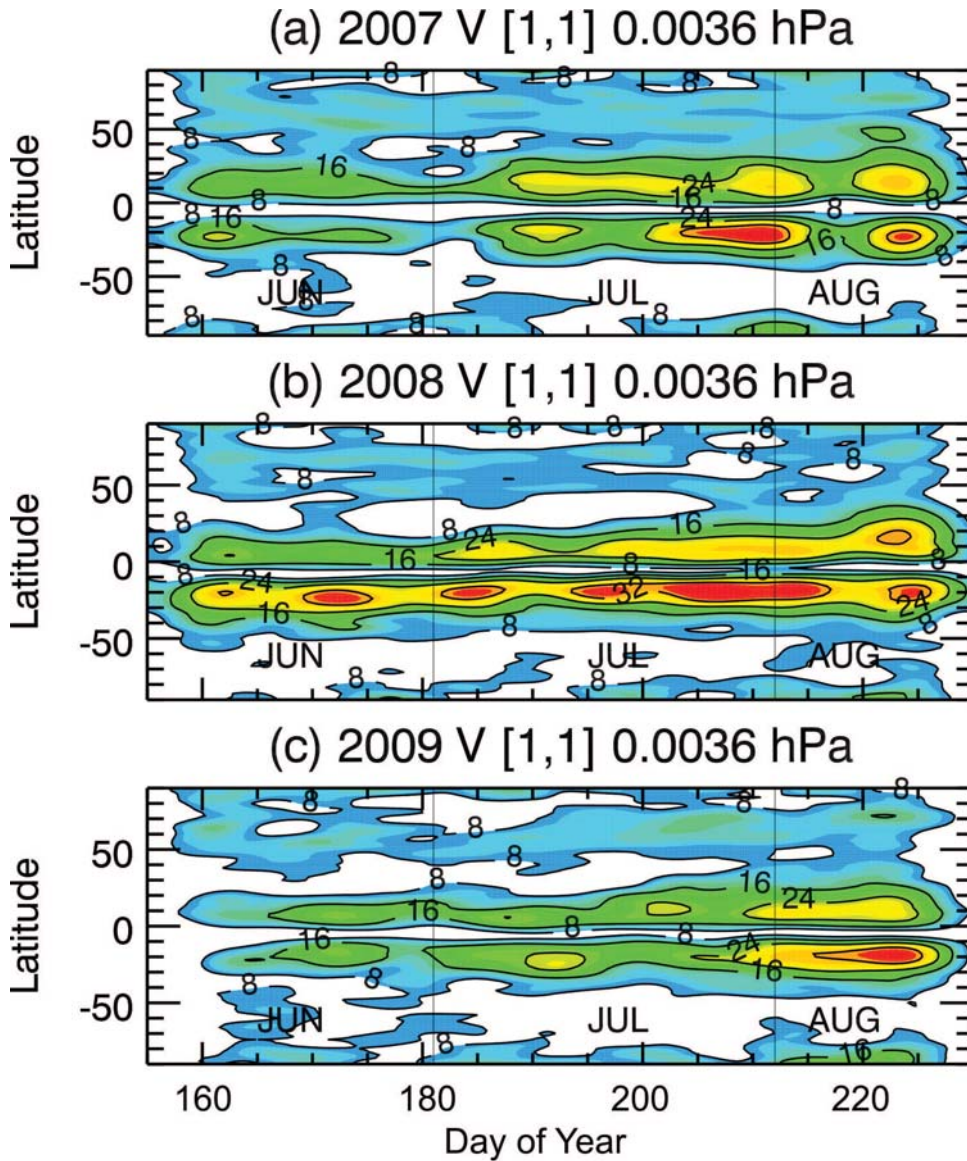


**Figure 7.** Latitude-time section of [0.5,3] Q2DW amplitudes at 0.021 hPa for the June–August period of (a) 2007, (b) 2008, and (c) 2009. Contour interval is 3 K.

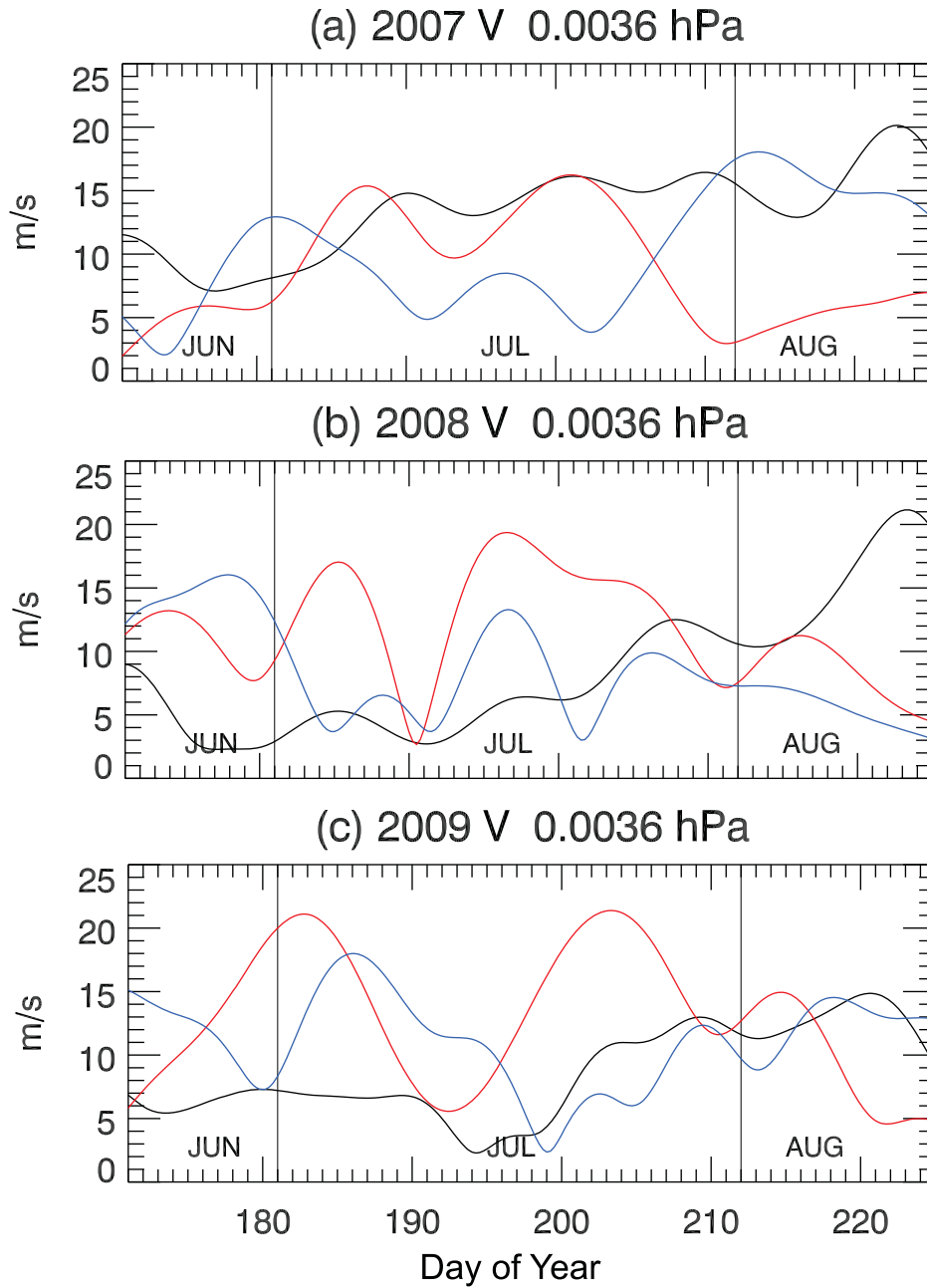


**Figure 8.** Latitude-time section of [0.5,4] Q2DW amplitudes at 0.021 hPa for the June–August period of (a) 2007, (b) 2008, and (c) 2009. Contour interval is 3 K.

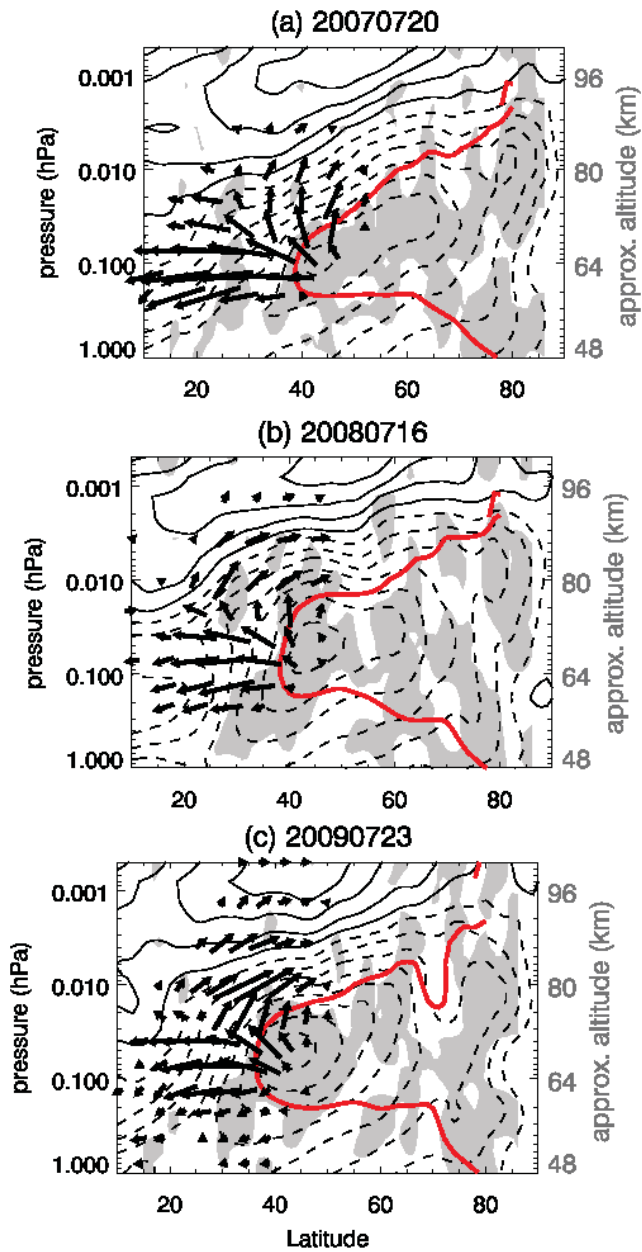




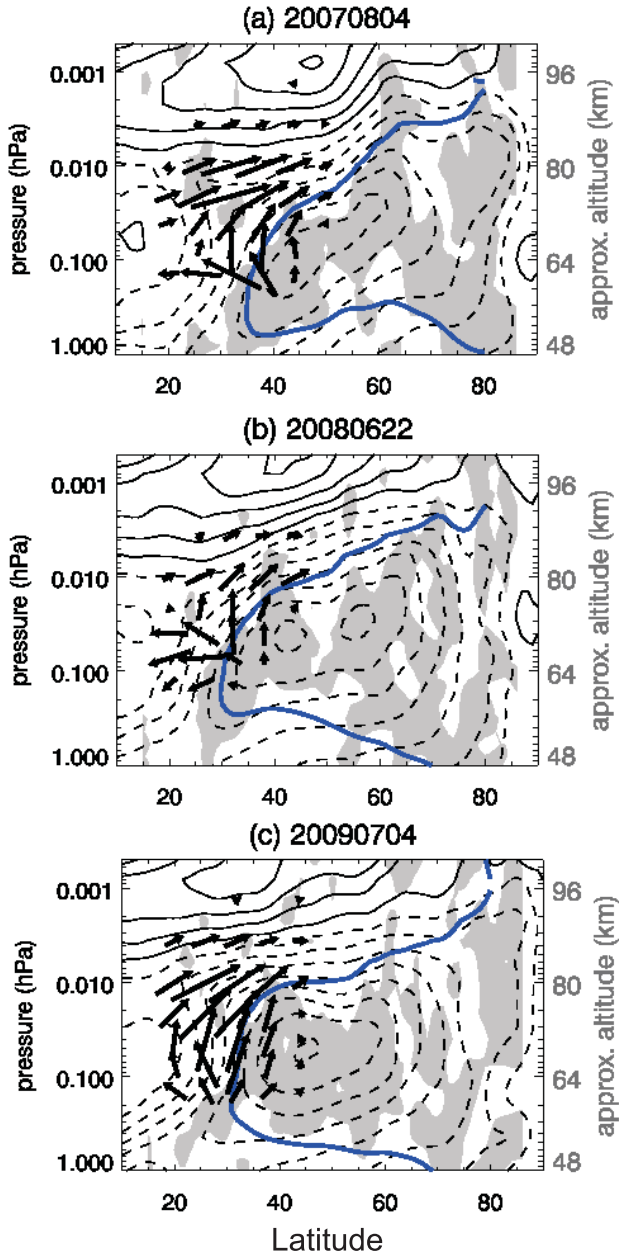
**Figure 9.** Latitude-time section of [1,1] tidal amplitudes at 0.0036 hPa for the June–August period of (a) 2007, (b) 2008, and (c) 2009. Contour interval is 8 m s<sup>-1</sup>.



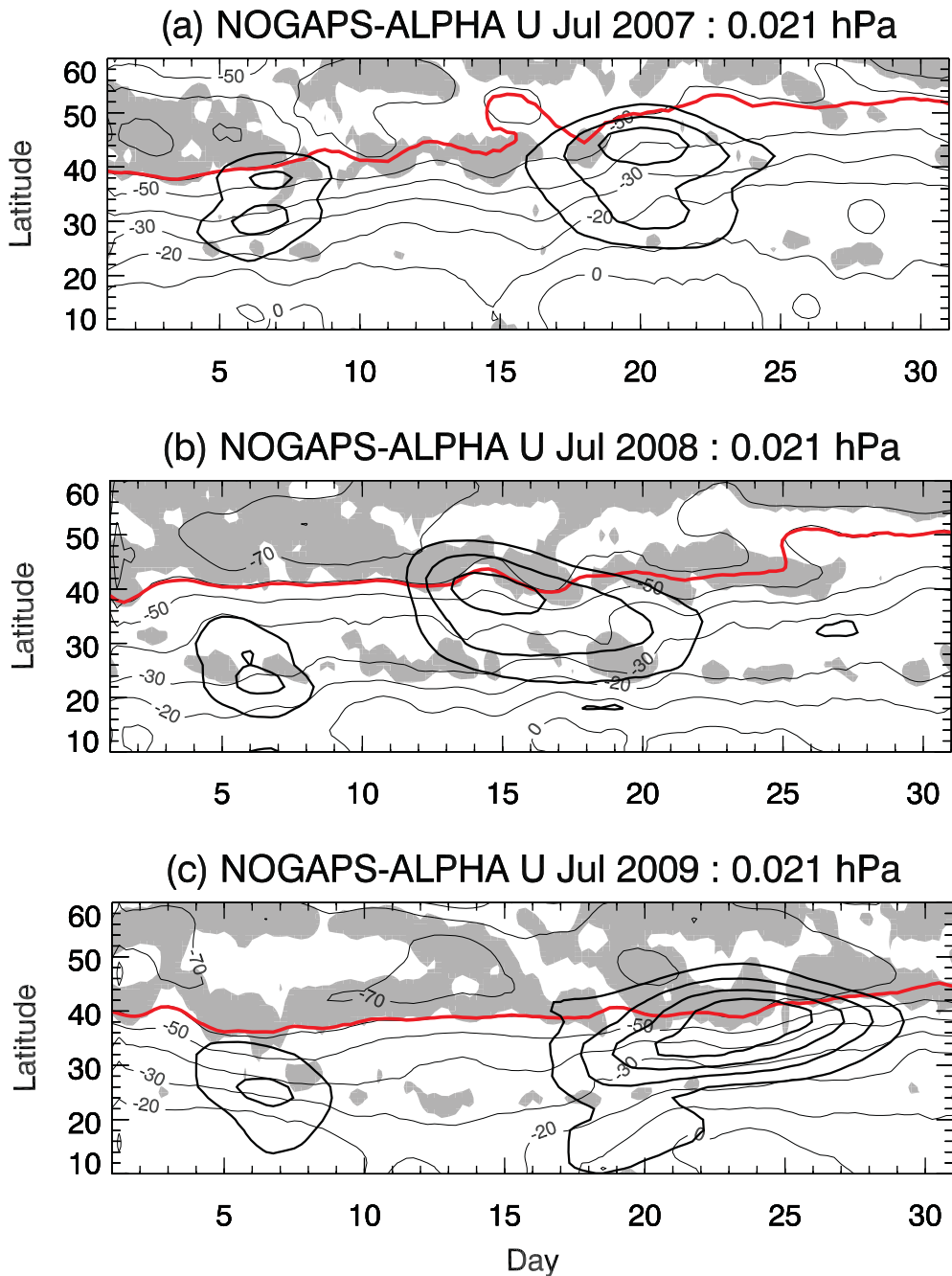
**Figure 10.** Time series of the [0.5,3] (red), [0.5,4] (blue), and [1,1] (black) amplitudes at  $30^{\circ}\text{N}$  and 0.0036 hPa during June–August of (a) 2007, (b) 2008, and (c) 2009.



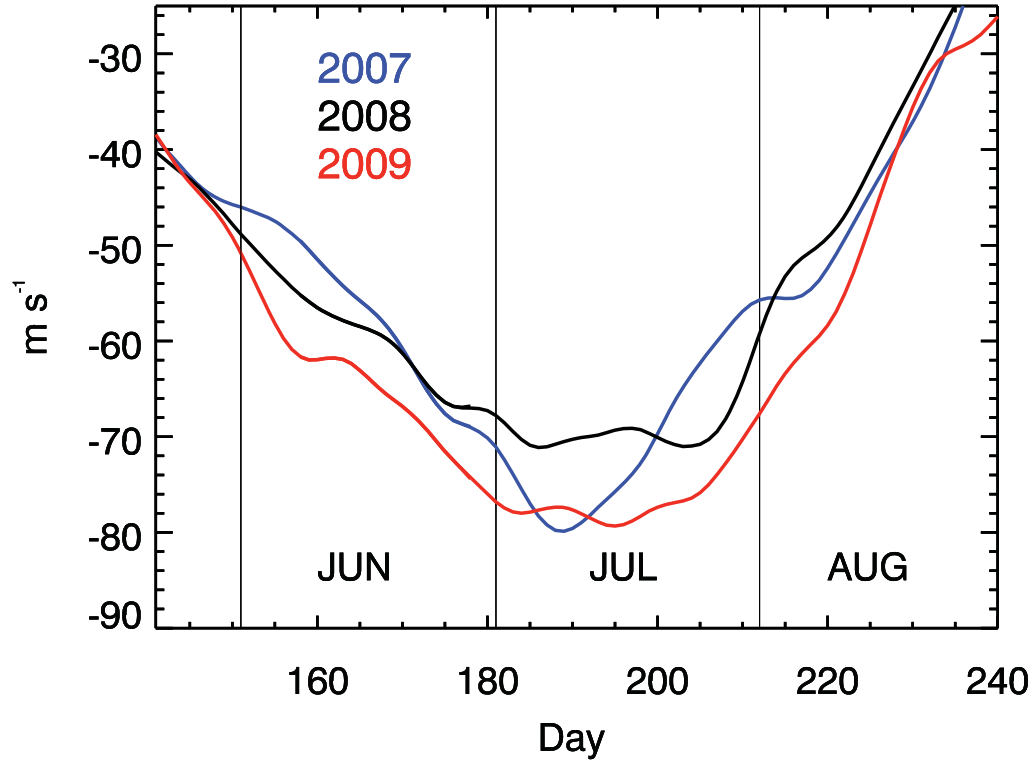
**Figure 11.** Contour plots of daily averaged NOGAPS-ALPHA zonal mean zonal winds for (a) July 20, 2007, (b) July 16, 2008, and (c) July 23, 2009. Contour interval is  $10 \text{ m s}^{-1}$ ; dashed contours represent easterly winds. Shaded regions indicate where meridional gradient in quasi-geostrophic potential vorticity is negative. Red contour indicates approximate location of critical line for  $[0.5,3]$  Q2DW. Arrows represent EP-fluxes associated with the  $[0.5,3]$  Q2DW.



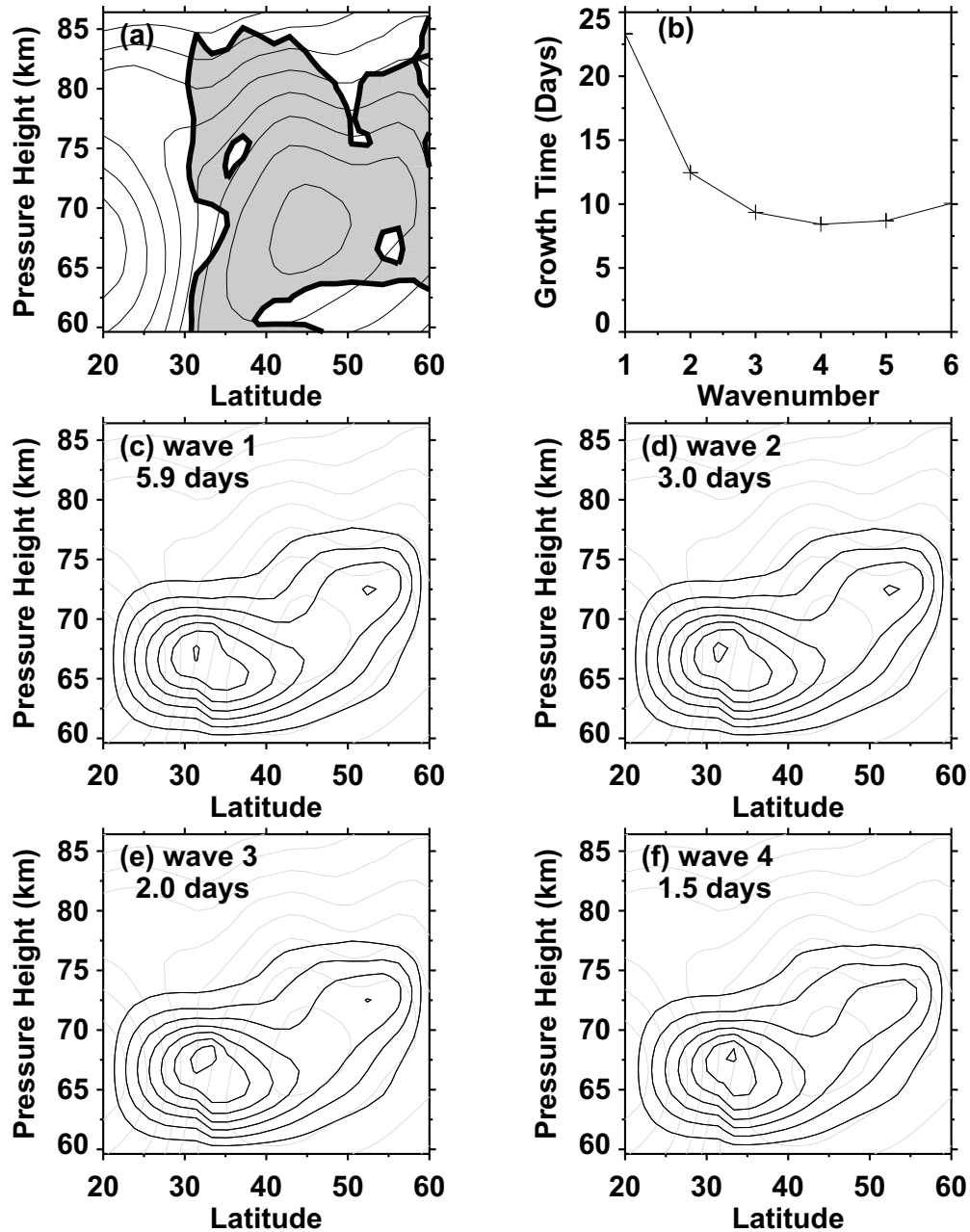
**Figure 12.** Contour plots of daily averaged NOGAPS-ALPHA zonal mean zonal winds for (a) August 4, 2007, (b) June 22, 2008, and (c) July 4, 2009, as in Fig. 11. Blue contour indicates approximate location of critical line for  $[0.5,4]$  Q2DW. Arrows represent EP-fluxes associated with the  $[0.5,4]$  Q2DW.



**Figure 13.** Latitude-time sections of daily averaged NOGAPS-ALPHA zonal mean zonal winds at 0.021 hPa during July of (a) 2007, (b) 2008, and (c) 2009. Shaded regions indicate where meridional gradient in quasi-geostrophic potential vorticity is negative. Red contour indicates approximate location of critical line for  $[0.5,3]$  Q2DW. Heavy black contours indicating positive  $[0.5,3]$  Q2DW eddy heat flux are drawn at values of 10, 15, 20, 25  $\text{K m s}^{-1}$



**Figure 14.** Time series of zonal mean zonal wind speed at  $40^\circ\text{N}$  and  $0.1 \text{ hPa}$  during NH summer of 2007 (blue curve), 2008 (black curve), and 2009 (red curve).



**Figure 15.** Linear instability model results for July 10, 2009 case. (a) Latitude-altitude distribution of zonal winds (contour interval of  $10 \text{ m s}^{-1}$ ), shaded regions indicate where  $q_y > 0$ ; (b)  $e$ -folding times for westward-propagating unstable modes as function of zonal wavenumber; (c)-(f) normalized amplitudes of the geostrophic streamfunction solutions, and the period of each solution, for wavenumbers 1 through 4.

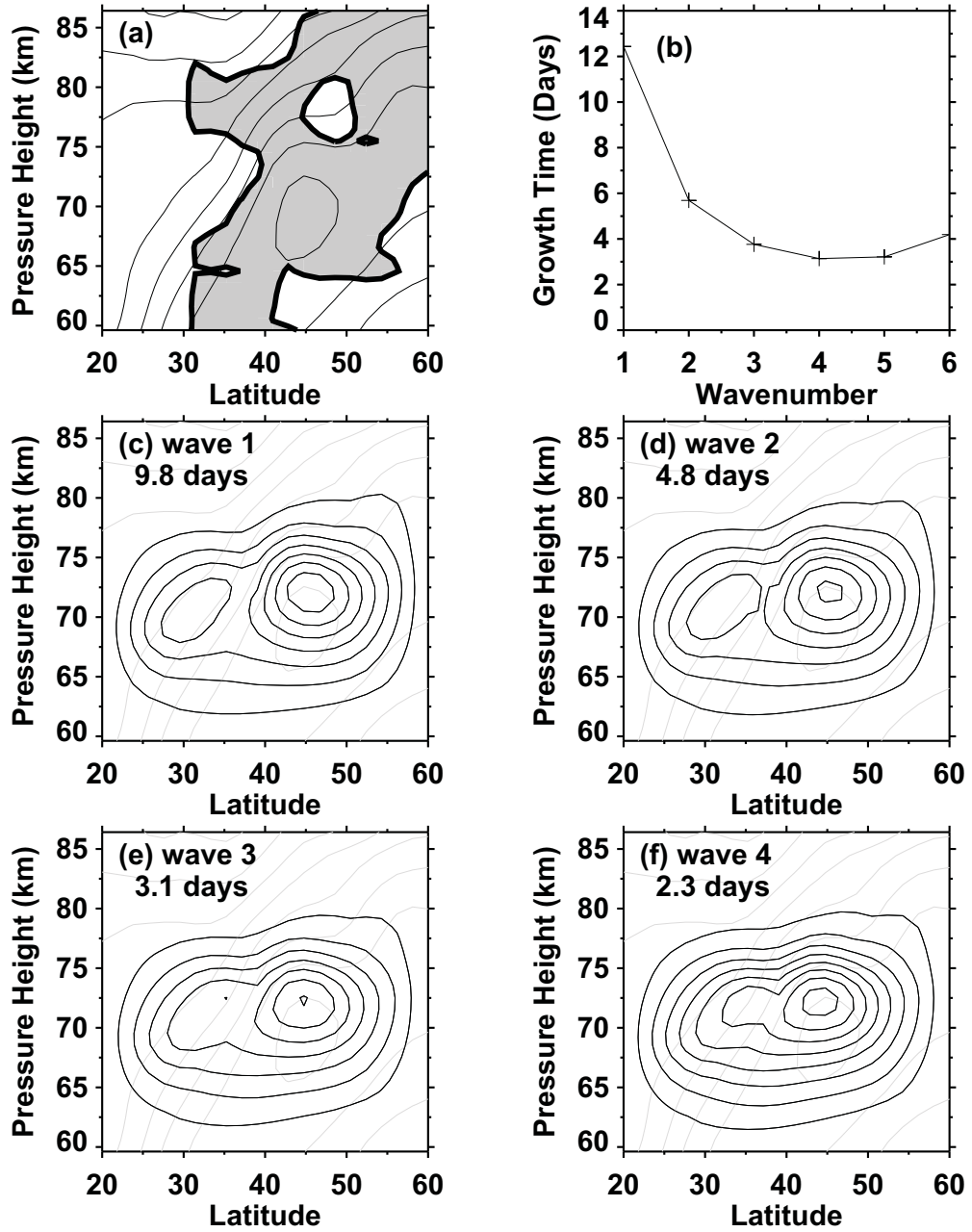
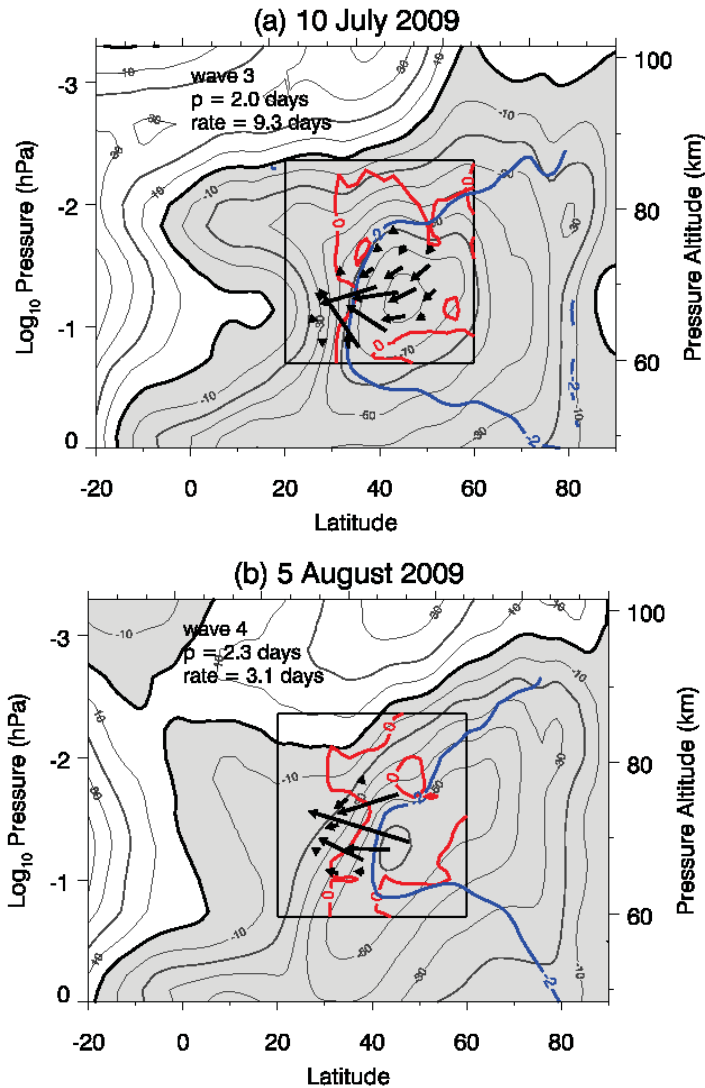
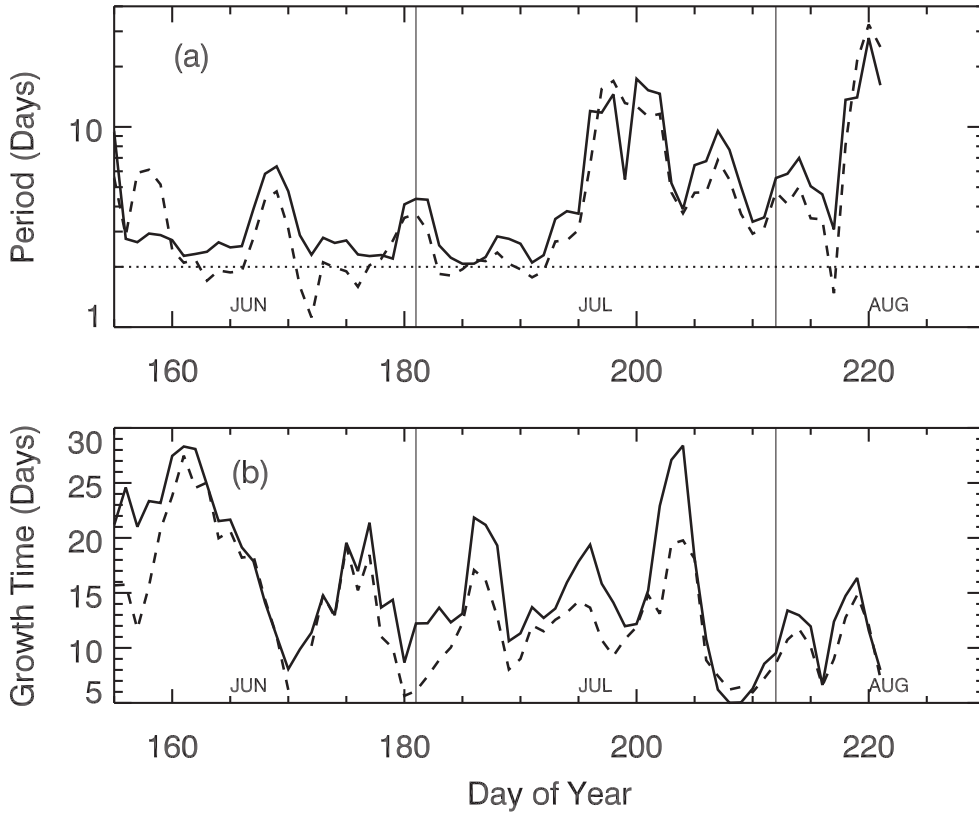


Figure 16. As in Figure 15, but for the August 5, 2009 case.





**Figure 17.** Daily averaged NOGAPS-ALPHA zonal mean zonal winds for (a) July 10 2009 and (b) August 5, 2009. Shaded regions indicate easterly flow. The domain of the linear instability model is indicated by the box extending from 20°–60°N and 60–86 km. Red contour encloses region where  $q_y > 0$ , blue contour indicates approximate location of critical line for wave solution with period closest to 48 hours. Arrows represent EP-flux vectors derived from zonal wavenumber 3 and 4 solutions of the linear instability model



**Figure 18.** Time series of (a) period and (b) *e*-folding time for zonal wavenumber 3 (solid curve) and wavenumber 4 (dashed curve) instability model solutions during summer 2009. Dashed line drawn at 2 days.