

1 **A fast Visible-Infrared Imaging Radiometer Suite simulator for cloudy atmospheres**

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26 **Key Points:**

- 27 • Correlated k-distribution models for the VIIRS bands are developed
- 28 • A fast VIIRS instrument simulator is developed
- 29 • A case study is performed to validate the simulator

30

31 **Abstract**

32 A fast instrument simulator is developed to simulate the observations made in cloudy
33 atmospheres by the Visible Infrared Imaging Radiometer Suite (VIIRS). The correlated *k*-
34 distribution (CKD) technique is used to compute the transmissivity of absorbing
35 atmospheric gases. The bulk scattering properties of ice clouds used in this study are based
36 on the ice model used for the MODIS Collection 6 ice cloud products. Two fast radiative
37 transfer models based on pre-computed ice cloud look-up-tables are used for the VIIRS
38 solar and infrared channels. The accuracy and efficiency of the fast simulator are quantify
39 in comparison with a combination of the rigorous line-by-line (LBLRTM) and discrete
40 ordinate radiative transfer (DISORT) models. Relative errors are less than 2% for simulated
41 TOA reflectances for the solar channels and the brightness temperature differences for the
42 infrared channels are less than 0.2 K. The simulator is over three orders of magnitude faster
43 than the benchmark LBLRTM+DISORT model. Furthermore, the cloudy atmosphere
44 reflectances and brightness temperatures from the fast VIIRS simulator compare favorably
45 with those from VIIRS observations.

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48 **1. Introduction**

49 The Visible Infrared Imaging Radiometer Suite (VIIRS) on board the Suomi National
50 Polar-orbiting Partnership (Suomi NPP) satellite provides critical data for accurately
51 determining cloud and aerosol properties, ocean color, sea and land surface temperatures,
52 ice motion and temperature, fires, and Earth's albedo [Lewis et al., 2010; Lee et al., 2010;
53 Hillger et al., 2013]. VIIRS includes 16 moderate-resolution channels (referred to as M-
54 bands) at 0.75-km spatial resolution and 5 higher-resolution imagery channels (I-bands) at
55 0.375-km resolution. With central wavelengths from approximately 0.4 to 12 μm , the
56 sensor was designed to be the next-generation global weather and climate imager for
57 afternoon polar orbiting observations. To infer cloud properties from the VIIRS
58 observations, an accurate and efficient forward radiative transfer model (RTM) is
59 invaluable for generating simulated reflectances or brightness temperatures for a variety of
60 atmospheric cloud and surface conditions, and can be used for retrieval error analyses and
61 instrument calibration efforts.

62 Many rigorous radiative transfer schemes, such as the line-by-line radiative transfer
63 model (LBLRTM) [Clough et al., 1992, 2005], the adding-doubling (AD) algorithm
64 [Twomey et al., 1966; Hovenier, 1969; Hansen, 1971; de Haan et al., 1987], and the
65 discrete ordinates radiative transfer (DISORT) method [Chandrasekhar, 1960; Liou, 1973;
66 Stamnes et al., 1988; Thomas and Stamnes, 1999], have been developed and widely applied
67 under different circumstances. For remote sensing problems involving hyperspectrally
68 resolved or channel-averaged radiances, a rigorous approach is needed to independently
69 and efficiently perform large numbers of simulations for each wavelength/wavenumber

70 due to the significant spectral variations exhibited by molecular absorption, and, in the case
71 of channel-averaged simulation, to conduct subsequent spectral integration. Performing
72 hundreds or even thousands of monochromatic simulations is extremely time-consuming;
73 thus, rigorous RTMs are significantly limited in satellite remote sensing applications
74 because of the large number of spatial and temporal observations. Developing
75 computationally efficient RTMs for specific satellite-based instruments is critical for
76 operational retrievals of atmospheric profiles as well as for the advancement of more
77 sophisticated cloud or aerosol property retrievals [Dubuisson et al., 1996, 2005; Weisz,
78 2007; Garnier et al., 2012, 2013; Chen and Huang, 2014].

79 One approach to achieve computational efficiency is to relax the accuracy constraints
80 for each individual simulation; models using two streams [Meador and Weaver, 1980], low
81 orders of scatterings [Natraj and Spurr, 2007], or pre-computed look-up-tables [Wang et
82 al., 2012] are typical examples of such approximations. These models normally keep the
83 same number of single simulations, but accelerate each individual simulation. Other
84 approximate approaches for hyperspectral or band-average calculations such as the
85 correlated k-distribution (CKD) method [Arking and Grossman, 1972; Lacis and Oinas,
86 1991; Fu and Liou, 1992; Kratz, 1995; Shi et al., 2009], the principal component method
87 [Liu et al., 2006, 2009], and the optimal spectral sampling method [Moncet et al., 2008],
88 are designed to minimize the computational effort by reducing the number of individual
89 radiative transfer simulations within a spectral band. Instead of considering each
90 wavenumber within a band, such models conduct rigorous radiative transfer calculations
91 at only a small number of representative monochromatic wavenumbers. The two types of
92 approaches have been applied to remote sensing, radiative transfer, and GCMs in both the

93 solar and IR spectral regions. In this study, we combine the two approaches to maximize
94 computational efficiency.

95 This study develops a fast RTM, i.e., an instrument simulator for cloudy atmospheres,
96 and uses both of the previously described methodologies to minimize the computational
97 time. While the emphasis here is in simulating the VIIRS solar and infrared channels, the
98 approach can be easily extended to other imagers. To obtain top-of-atmosphere (TOA)
99 reflectances or brightness temperatures, the atmospheric gaseous transmissivity and cloud
100 optical properties are essential parameters for a RTM, and will be carefully considered in
101 the fast model. Section 2 describes the development of the CKD models to determine
102 gaseous transmissivity, and Section 3 discusses the cloud optical properties. The fast
103 radiative transfer models (FRTMs) for VIIRS solar and IR channels, respectively, are
104 described in Section 4. Section 5 validates the simulator and compares the simulated results
105 with VIIRS observations, and Section 6 summarizes the study.

106

107 **2. Determination of gas transmissivity**

108 As an approximate technique to line-by-line calculations such as those of LBLRTM
109 [Clough et al., 1992, 2005], the CKD is a highly efficient model to account for gaseous
110 absorption, and can be easily incorporated into calculations of multiple scattering in
111 aerosols and clouds. The CKD model replaces the integral of gas transmissivity over highly
112 variable spectral space by one over a much smoother absorption coefficient space.

113 The transmissivity of a single gas at constant pressure and temperature within a small
114 spectral interval of interest, e.g., the interval of a VIIRS channel, is defined as:

$$115 \quad T_{ch}(u) = \frac{1}{\Delta\nu} \int_{\Delta\nu} e^{-k(v)u} dv, \quad (1)$$

116 where $k(\nu)$ is the gas spectral absorption coefficient at wavenumber ν , and u is the gas
 117 path-length . To accurately obtain the transmissivity, the line-by-line calculation must be
 118 performed over a very fine wavenumber grid. This calculation requires significant
 119 computational time because the absorption coefficient is a highly variable function in
 120 spectral space. However, the transmissivity does not depend on the ordering of the spectral
 121 absorption coefficient within a given spectral interval, and, thus, instead of integrating over
 122 the spectral space, Eq. (1) can be expressed as:

$$123 \quad T_{ch}(u) = \frac{1}{\Delta\nu} \int_{\Delta\nu} e^{-k(\nu)u} d\nu = \int_{k_{min}}^{k_{max}} e^{-ku} f(k) dk, \quad (2)$$

124 where $f(k)$ is the normalized probability distribution function for $k(\nu)$. To obtain $f(k)$,
 125 the range of the absorption coefficient $k(\nu)$ ($[k_{min}, k_{max}]$) and the spectral interval are
 126 divided into N and M uniform subintervals, respectively, with width $\delta k = \frac{k_{max}-k_{min}}{N}$, and
 127 $\delta\nu = \frac{\Delta\nu}{M}$. We define $k_0 = k_{min}$, $k_n = k_{n-1} + \delta k$, and $\nu_m = (m - 0.5)\delta\nu$. Thus, the
 128 probability function $f(k)$ can be numerically represented by:

$$129 \quad f(k_i) = \frac{1}{\Delta\nu} \sum_{m=1}^M \frac{\delta\nu}{\delta k} W(k_{i-1} < k(\nu_m) \leq k_i), \quad (3)$$

130 where W is the weighting function equal to unity if its argument condition is satisfied and
 131 zero otherwise. By defining the cumulative probability function $g(k) = \int_{k_{min}}^k f(k') dk'$, or
 132 in the discrete format,

$$133 \quad g(k_i) = \frac{1}{\Delta\nu} \sum_{m=1}^M \delta\nu W(k(\nu_m) \leq k_i) = \sum_{j=1}^i f(k_j) \delta k, \quad (4)$$

134 Eq. (1) can be further simplified as:

$$135 \quad T_{ch}(u) = \int_0^1 e^{-k(g)u} dg, \quad (5)$$

136 where g ranges from 0 to 1, and $k(g)$ is a monotonically increasing and smooth function
 137 of g . Thus, the spectral integration in Eq. (5) can be evaluated with fewer points in g space

138 between zero and unity compared to the number of wavenumber points required for Eq.
 139 (1). This approximation is known as the k -distribution method and can be given by:

$$140 \quad T_{ch}(u) = \int_0^1 e^{-k(g)u} dg = \sum_{i=1}^P e^{-k(g_i)u} \Delta g_i. \quad (6)$$

141 To extend the k -distribution method to realistic inhomogeneous atmospheres, the CKD
 142 method assumes that the ordering of absorption lines with respect to their strengths is the
 143 same at different temperature and pressure levels, and

$$144 \quad \begin{aligned} T_{ch}(u) &= \frac{1}{\Delta v} \int_{\Delta v} \exp \left[- \int_{z_1}^{z_2} k(v, P(z), T(z)) \rho dz \right] dv \\ &= \int_0^1 \exp \left[- \int_{z_1}^{z_2} k(g, P(z), T(z)) \rho dz \right] dg \end{aligned} \quad (7)$$

145 where $P(z)$ and $T(z)$ are the pressure and temperature of the atmospheric layer between z_1
 146 and z_2 .

147 While the CKD method has been widely used, the spectral k 's from multiple gases
 148 have typically been treated as uncorrelated so that a product rule approximation
 149 could be used. Edwards and Francis [2000] suggested an approach to treat overlapping
 150 lines from different gases as a “single gas” by combining the absorption coefficients of
 151 multiple absorption gases. The equivalent absorption coefficient for a given mixture of
 152 (N+1) gases is defined as:

$$153 \quad K(v, R_1, R_2, \dots, R_N) = k_0(v) + \sum_{i=1}^N k_i(v) R_i, \quad (8)$$

154 where $k_i(v)$ is the absorption coefficient of the i th gas, and R_i is the density ratio of the i th
 155 gas to the reference gas, i.e., the gas with absorption coefficient of $k_0(v)$. The dominant
 156 gas can be regarded as the reference gas, and, through Eq. (8), the absorption of (N+1)
 157 gases is converted into a single-gas case with equivalent absorption coefficient
 158 $K(v, R_1, R_2, \dots, R_N)$. This process can be repeated for a finite number of gas mixture density

159 ratios for a fixed set of constituent gases, such that $K(v)$ for any given mixture of these
 160 gases can be found by interpolation.

161 To consider an instrument channel's (i.e., VIIRS) spectral response function (SRF, i.e.
 162 $s(v)$), the spectral transmissivity given by Eq. (1) is rewritten as:

$$163 \quad T_{ch}(u) = \frac{1}{S} \int_{\Delta v} s(v) e^{-k(v)u} dv, \quad (9)$$

164 where the normalization factor is $S = \int_{\Delta v} s(v) dv$. To include the SRF in the CKD model,
 165 the approach given by Edwards and Francis [2000] is used, and Eqs. (3) and (4) are
 166 modified as:

$$167 \quad f_s(k_i) = \frac{1}{S} \sum_{m=1}^M \frac{s(v_m) \delta v}{\delta k} W(k_{i-1} < k(v_m) \leq k_i), \quad (10)$$

168 and

$$169 \quad g_s(k_i) = \frac{1}{S} \sum_{m=1}^M s(v_m) \delta v W(k(v_m) \leq k_i) = \sum_{j=1}^i f_s(k_j) \delta k. \quad (11)$$

170 In Eqs. (10) and (11), the uniform weighting δv is changed into $s(v_m) \delta v$ for each spectral
 171 subinterval. TOA solar spectral irradiance variations in the channel can also be included in
 172 the normalization factor in a manner similar to the SRFs.

173 Fig. 1 illustrates the treatments of overlapping absorption lines, SRF, and solar spectral
 174 irradiance for the VIIRS M10 channel centered at a wavelength of 1.61 μm . The gas
 175 spectral absorption coefficients of CO_2 , H_2O , and CH_4 are plotted in (a), (b), and (c),
 176 respectively, with (d) showing the effective absorption coefficient of a mixture with mass
 177 density ratios of H_2O and CH_4 to CO_2 of 0.1 and 0.001, respectively. Following Eqs. (10)
 178 and (11), the effective coefficient of the mixture gas is weighted with the corresponding
 179 SRF (e) and solar spectral irradiance (SI) (f). Fig. 1(g) shows the sorted effective absorption

180 coefficient as a function of g (blue line); results without considering either the SRF or solar
 181 spectral irradiance is illustrated for comparison (red line). In g space, the absorption
 182 coefficient becomes a smooth function, and only 4 intervals (shown by the dashed lines in
 183 (g)) in this channel are used to determine the transmissivity following Eq. (6). Furthermore,
 184 differences are obvious for results with and without consideration of the SRF, as shown in
 185 Fig. 1g.

186 Based on the theories and techniques described, we construct a CKD model for each of
 187 the VIIRS channels, considering only up to the three most absorptive gases. The parameters
 188 used to construct the CKD models follow the work done by Ding et al. [2012] for the
 189 Geostationary Operational Environmental Satellite R (GEOS-R) Advanced Baseline
 190 Imager (ABI) solar channels. To build the CKD model for each of the VIIRS channels, the
 191 absorption coefficients of the gases of interest are obtained from the LBLRTM, and the
 192 molecular absorption line parameters are based on the 2008 edition of the High Resolution
 193 Transmission (HITRAN) molecular spectroscopic database [Rothman et al., 2008]. The
 194 absorption coefficients are calculated at 19 pressure levels and 3 temperatures (i.e., 200K,
 195 260K, and 320K) using the LBLRTM, and each set of absorption coefficients are sorted
 196 and binned following the same distribution as that of the reference pressure and
 197 temperature, chosen as 261 hPa and 260 K, respectively. Each of the VIIRS channels is
 198 divided into 4 to 16 intervals in g -space, the number of which is determined by the degree
 199 of the gas absorption and the complexity of the overlapping gaseous absorption.

200 At a given g and pressure level P_o , the absorption coefficient at temperature T is given
 201 by:

$$202 \quad \ln[k(g, P_o, T)] = a(g, P_o) + b(g, P_o)(T - 260) + c(g, P_o)(T - 260)^2, \quad (12)$$

203 where the coefficients a , b and c are regression coefficients derived from absorption
204 coefficients obtained at the three temperature values of 200 K, 260 K, and 320 K for the
205 corresponding g values at the 19 pressure levels. In practice, the absorption coefficient at
206 an arbitrary temperature and pressure, $k(g, P, T)$, is found first by solving Eq. (12) first, then
207 by linear interpolation between values at the two neighboring pressures.

208 Table 1 lists parameters of the CKD model for each VIIRS channel, including the
209 central wavelength, wavelength range, absorbing gas species considered, and the number
210 of g values. Gases considered in this study include H₂O, O₂, O₃, CO₂, CH₄, and N₂O. Up
211 to three different absorbers are considered for each channel, and the O₃ continuum
212 absorption (designated as “cont.” in the table) is included in the IR channels by using the
213 equations given by Roberts et al. [1976].

214 The CKD is employed to produce the transmissivity of the atmosphere, and Fig. 2
215 compares the band-averaged transmissivity and weighting profiles with results from the
216 LBLRTM to illustrate the accuracy of the model for clear sky calculations. Results for four
217 VIIRS channels centered at wavelengths 0.555 μm , 1.61 μm , 3.7 μm , and 10.763 μm , are
218 shown. In the simulations, the US standard atmospheric profile is divided into 50 layers,
219 each being 1 km thick, and the volume mixing ratios of O₂, CO₂, CH₄, and N₂O are assumed
220 to be uniform with values of 0.21, 3.8×10^{-4} , 1.8×10^{-6} , and 3.2×10^{-7} . From left to right in
221 Fig 2, the three columns correspond to the transmissivity in each layer, relative
222 transmissivity error, and weighting function profiles of the CKD models. Fig. 2 indicates
223 that the relative errors in transmissivity are less than 0.1% for the four VIIRS channels,
224 which, from a practical application perspective, are sufficiently accurate for simulating
225 TOA reflectance and brightness temperatures under cloudy conditions.

226

227 **3. Determination of cloud optical properties**

228 For cloudy sky applications, channel-averaged cloud bulk-scattering properties, for
229 both liquid and ice phases, are required to determine the absorption, scattering, and
230 emission of cloud layers. Here, single-scattering calculations are performed at discrete
231 sizes and wavelengths, and averaged over the assumed particle size distribution and the
232 SRF for each VIIRS channel. For the solar channels, the solar spectral irradiance is also
233 considered. For the IR bands, the Planck function representing the thermal IR emission
234 from an opaque cloud at 233 K is used. The details for obtaining the channel-averaged
235 properties can be found in Baum et al. [2005].

236 For liquid phase clouds, the single-scattering properties are obtained using the Lorenz-
237 Mie theory [Mie, 1908]. The cloud droplet size distributions are assumed to be Gamma
238 distributions [Hansen and Travis, 1974] with an effective variance of 0.1, and the bulk-
239 scattering properties are calculated for effective radii ranging from 2 to 50 μm .

240 For ice phase clouds the model choice is critical, because the microphysical and optical
241 properties of ice clouds are very sensitive to particle habits, especially the optical properties
242 in solar reflectance channels. The ice cloud model used for deriving the MODIS Collection
243 6 cloud products is applied in this study. This model consists of a single ice habit, i.e., a
244 severely roughened aggregate with eight solid hexagonal columns, that provides excellent
245 spectral consistency (i.e., between optical thicknesses inferred from solar reflectance and
246 IR channels) and close agreement with the polarization properties from the PARASOL
247 observations [Baum et al. 2014]. The column aggregate single-scattering properties are
248 obtained from the ice crystal database developed by Yang et al. [2013]. The Gamma size

249 distribution with an effective variance of 0.1 is assumed for the ice clouds, and the effective
250 diameter ranges from 10 to 180 μm in 10 μm steps.

251

252 **4. VIIRS simulator**

253 This study considers both the VIIRS solar reflectance and infrared channels. For solar
254 channels, cloud multiple scattering plays a much more significant role than the gaseous
255 absorption and emission, because absorption is relatively weak at most VIIRS solar
256 channels (except the M9 channel with strong water vapor absorption), and emissions at
257 these wavelengths are negligible. However, gaseous absorption and emission become as
258 important as cloud and aerosol effects (scattering, absorption, and emission) in the infrared
259 channels. Thus, the VIIRS solar and infrared channels use different fast radiative transfer
260 models (FRTMs).

261 The FRTM developed by Wang et al. [2013a] is chosen to calculate visible through
262 shortwave infrared spectral reflectance. This FRTM uses six independent radiative transfer
263 equations to approximate the full radiative transfer processes for a combination of cloud,
264 aerosol, or molecular layers; the adding-doubling algorithm implemented on a twisted
265 icosahedral mesh is incorporated to account for overlapped cloud/aerosol layers. To further
266 improve the FRTM efficiency, the bidirectional reflectance and transmittance distribution
267 functions (BRDF and BTDF) of cloud layers with different optical thicknesses and
268 effective particle sizes are pre-calculated using the 128-stream DISORT, and the optical
269 properties of water and ice clouds, discussed in the previous section, are included.
270 Generally, the FRTM is approximately two orders of magnitude faster than the 128-stream
271 DISORT, and obtains TOA reflectance with relative errors normally less than 5%.

272 For the infrared channels, the simulator uses the FRTM developed by Wang et al.
273 [2011, 2013b] to obtain the TOA brightness temperature. Similar to the FRTM used for the
274 solar channels, the effects of cloud layers are efficiently considered by pre-calculated look-
275 up-tables at various optical thicknesses and effective particle sizes, which include the
276 reflectance, transmittance, emissivity, and effective temperature. The CKD model
277 discussed in Section 2 is used to account for atmospheric gas absorption. The TOA
278 brightness temperature differences (BTDs) given by the fast model and the rigorous
279 DISORT are less than 0.15 K. Furthermore, the FRTM is more than three orders of
280 magnitude faster than the corresponding a DISORT implementation with 32 streams.

281 The most current DISORT code (DISORT 2.0 beta) is used to calculate the look-up-
282 tables for both FRTMS based on the band-averaged optical properties. In DISORT, the
283 cloud phase functions are defined in terms of their Legendre polynomial expansion
284 coefficients and, for large ice particles, thousands of Legendre polynomial terms are
285 needed to represent a phase function that has a strong forward peak. The number of
286 expansion terms can be greatly reduced, however, by truncating the forward peak of the
287 phase function. The δ -fit method [Hu et al., 2000] is used here for the solar channels, such
288 that only 128 terms are sufficient to reconstruct the phase function, significantly decreasing
289 computational time in the DISORT simulations. Corresponding scaling adjustments are
290 made to the optical thickness and single-scattering albedo to account for the truncated
291 forward energy.

292 The solar and IR FRTMs are combined with the CKD method to maximize the
293 efficiency of the simulator. For each simulation, the FRTM is performed with the

294 transmissivity obtained under each g value, and the TOA radiance of a given channel is
 295 obtained by:

$$296 \quad I_{ch,simulator} = \sum_{i=1}^M I[T(g_i)]\Delta g_i, \quad (13)$$

297 where $T(g_i)$ refers to the transmissivity of the i th g value, and $I[T(g_i)]$ is the
 298 corresponding TOA radiance given by the FRTM.

299 The accuracy and efficiency of the simulator, i.e., the model based on the combination
 300 of the CKD and FRTMs, are evaluated by comparing the simulated band-averaged
 301 reflectance or BT at the TOA with the rigorous solutions given by the combination of the
 302 LBLRTM and DISORT. The spectral resolution of the LBLRTM+DISORT simulation is
 303 chosen to be 1.0 and 0.1 cm^{-1} for the solar and infrared channels, respectively, and the TOA
 304 upwelling radiances are then averaged over the spectrum considering the SRF:

$$305 \quad I_{ch,std} = \frac{\int_{\Delta\nu} s(\nu)I(\nu)d\nu}{S}, \quad (14)$$

306 where $I(\nu)$ is the radiation at wavenumber ν given by the DISORT. With the TOA
 307 radiance, obtaining the corresponding reflectivity and brightness temperature is
 308 straightforward.

309 A set of comparisons at solar channels is implemented between the fast simulator and
 310 the rigorous approach, with the relative errors of TOA reflectance as a function of the
 311 viewing zenith angle shown in Fig. 3. Three VIIRS channels (M4, M10, and M11) are
 312 considered for the comparison, and three solar zenith angles values (10° , 30° and 50°) are
 313 used. The left panels are for an optical thickness of 5, and the right panels are for a value
 314 of 20. For all cases, the simulator yields relative errors less than 1.5% with respect to the

315 rigorous approach. The relative errors slightly increase as the solar zenith angle increases,
316 and show little dependence on the cloud optical thickness.

317 To validate the simulator at the IR channels, Fig. 4 illustrates the brightness temperature
318 differences (BTDs) given by the simulator and the LBLRTM+DISORT at three IR
319 channels (M14, M15, and M16). The BTD is defined as:

$$320 \quad \text{BTD} = \text{BT}_{\text{Simulator}} - \text{BT}_{\text{LBLRTM+DISORT}}. \quad (15)$$

321 Each panel of Fig. 4 shows the comparison of simulation results based on a surface
322 emissivity of 1 and viewing zenith angle of 20° under different cloud conditions. The BTD
323 is expressed as a function of optical thickness, and cloud particle effective diameters and
324 top temperatures used for the simulations are listed in the figure. The errors in the BTDs
325 are smaller than 0.2 K and decrease to less than 0.1 K for optically thick clouds.

326

327 **5. Comparison with VIIRS observations**

328 We developed a fast radiance simulator to calculate TOA reflectances or brightness
329 temperatures of a cloudy atmosphere based on a combination of the CKD and FRTMs for
330 the VIIRS solar and infrared channels. This section highlights a case study to assess the
331 performance of the simulator by comparing simulated TOA reflectances and brightness
332 temperatures with those from VIIRS observations.

333 As discussed in the previous sections, the forward model requires atmospheric profiles
334 and cloud properties as input parameters. For this comparison, atmospheric profile data is
335 obtained from the Modern Era Retrospective-analysis for Research and Applications
336 (MERRA) [Rienecker et al., 2008] instantaneous 3-hour vertical atmospheric profile
337 product (i.e., inst3_3d_asm_Cp) that provides temperature, geopotential height, water

338 vapor, and ozone concentrations at 42 pressure levels on a 288×144 mesh grid with a 1.25°
339 $\times 1.25^\circ$ resolution. The cloud input to the simulator, including cloud thermodynamic phase,
340 top pressure, optical thickness, and effective particle size, is from the operational MODIS
341 Collection 6 cloud products (i.e., the Aqua MODIS MYD06_L2 product), and the 1 km-
342 resolution geolocation is obtained from the MYD03 dataset. The atmospheric profiles and
343 cloud properties are collocated with the VIIRS observations, with VIIRS solar and sensor
344 view geometries used as simulator inputs.

345 A flowchart summarizing the fast VIIRS radiance simulator process is shown in Fig.
346 5. The atmospheric profile is input into the CKD models to generate transmissivity of
347 absorption gases, and also provides the temperature profile for the IR simulator. The
348 gaseous transmissivity and cloud properties are used by the FRTMs to calculate
349 reflectances or brightness temperatures of given VIIRS solar-satellite geometries, and the
350 simulated results are compared with the corresponding VIIRS measurements to assess the
351 performance of the simulator.

352 To avoid uncertainties associated with satellite-based cloud retrievals due to larger
353 surface reflectances over land, only observations over ocean are considered for the present
354 case study, specifically, the VIIRS granules taken over the South Pacific Ocean from
355 00:38:47.4 to 00:41:38.2 UTC on 3 January 2014. The collocated MODIS granule is taken
356 at 00:45 UTC, approximately 4 to 6 minutes behind the VIIRS observations. Fig. 6 shows
357 the true color images of the (a) MODIS and (b) VIIRS granules, with the MODIS cloud
358 optical thickness and effective particle radius shown in (c) and (d), respectively. The red
359 boxes in the RGBs show the region of the simulation, which is largely covered by ice

360 clouds. In the simulation region, the cloud optical thickness ranges from a few to over 50,
361 and the effective particle radius shows values from 5 to approximately 40 μm .

362 Fig. 7 compares the observed (left panels) and simulated (right panels) reflectances at
363 VIIRS 0.86- and 2.25- μm channels (M7 and M11). The reflectance values at the 0.86- μm
364 channel are larger than those at the 2.25- μm channel, which is mainly due to the significant
365 differences in the scattering properties of ice clouds at the two channels (e.g., ice clouds
366 are much more absorptive at the 2.25- μm channel). The patterns of the reflectances given
367 by the fast simulator are almost the same as the VIIRS observations at each channel.
368 Furthermore, the agreement indicates the performance of the MOD06 product that is used
369 as the input parameters. However, note that the liquid water and ice cloud radiative models
370 used in the FRTM were specifically chosen to match the models used in MYD06_L2 (see
371 Sect. 3).

372 Fig. 8 is the same as Fig. 7 but for brightness temperatures at three VIIRS IR channels
373 (i.e., 8.55-, 10.76-, and 12.01- μm channels (M14, M15, and M16) from upper to lower
374 panels). The simulated brightness temperatures show close agreement with the
375 observations. However, noticeable differences exist in some regions of the granules, and
376 this may be due to the uncertainties in either atmospheric profiles or cloud height. The ice
377 cloud properties, which are retrieved from MODIS solar-channel observations, may also
378 yield significant errors when applied to IR channels, because the cloud optical thickness
379 and effective particle radius inferred from the solar and IR channels can be quite different
380 [Baum et al., 2014]. The case study indicates the exceptional performance of the VIIRS
381 simulator for both solar and IR channels.

382

383 **6. Summary**

384 This study developed a computationally efficient simulator for the VIIRS solar and IR
385 channels in cloudy atmospheres that can be used in cloud property evaluations and
386 retrievals. The absorption of atmospheric gases and overlapping gas absorption is
387 accounted for using a VIIRS-specific CKD that considers both the spectral response
388 function and solar spectral irradiance. The accuracy of the transmissivity profile is
389 estimated by comparing with the exact line-by-line results, and the relative errors in
390 transmissivity are less than 0.1% for all VIIRS channels. Two fast RTMs are used to
391 consider absorption, scattering, and emission of cloud layers. The channel-averaged bulk-
392 scattering properties of roughened hexagonal columns are used for ice cloud, and the
393 properties of water cloud are given by the Lorenz-Mie theory. By comparing with the
394 rigorous DISORT results, the relative errors for TOA reflectance at VIIRS solar channels
395 are less than 1.5%, and the differences in brightness temperatures at the IR channels are
396 less than 0.25K. The present simulator is more computationally efficient than the standard
397 LBLRTM+DISORT by over three orders of magnitude. With collocated MERRA
398 atmospheric profiles and cloud optical thickness and effective particle diameter from the
399 MODIS cloud product as input, the reflectances and brightness temperatures calculated by
400 the fast simulator show close agreement with concurrent VIIRS solar and IR observations.
401 Considering the accuracy and efficiency provided, the simulator can be used directly for
402 cloud property retrievals related to VIIRS observations. While our fast radiative transfer
403 model (FRTM) used in this study was applied to VIIRS channels, the FRTM can also be
404 developed for MODIS and other satellite or airborne imagers with similar spectral
405 coverage.

406

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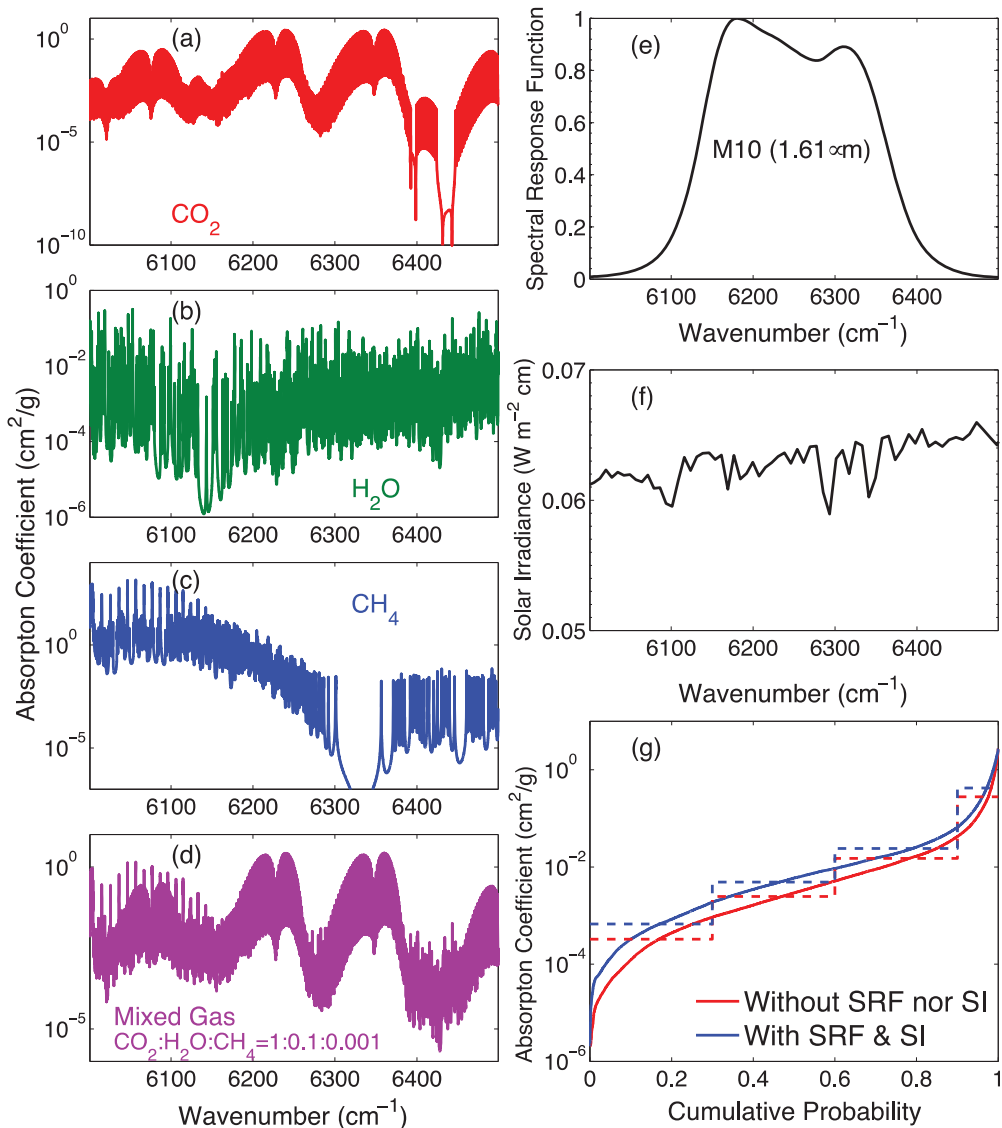
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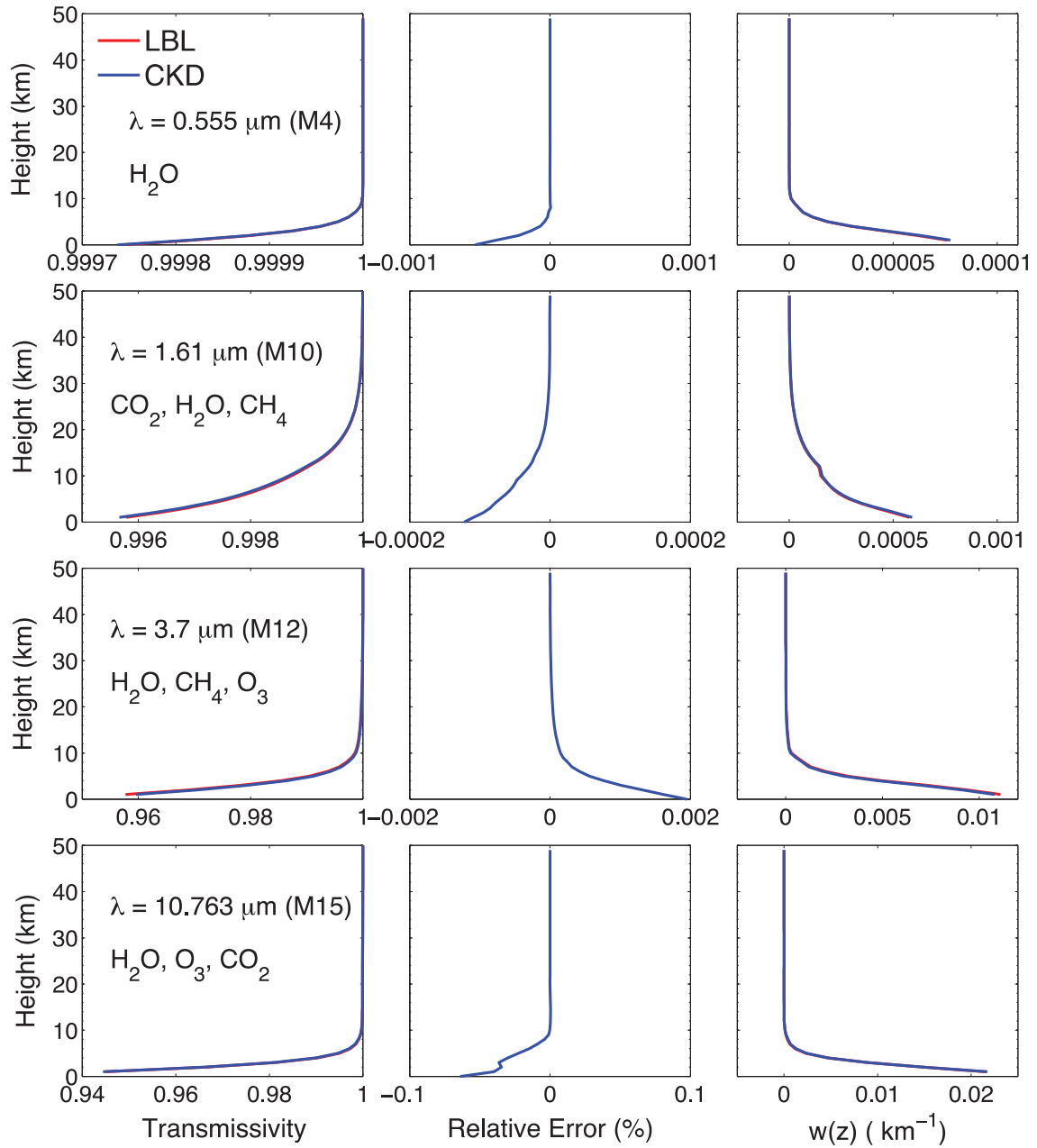
534 **TABLE 1.** CKD model parameters for the VIIRS channels.

VIIRS Channels	Central Wavelength (μm)	Wavelength Range (μm)	Gas Considered	Number of g values
M1	0.412	0.402-0.422	H ₂ O	4
M2	0.445	0.436-0.454	H ₂ O	4
M3	0.488	0.478-0.488	H ₂ O	16
M4	0.555	0.545-0.565	H ₂ O	4
M5	0.672	0.662-0.682	H ₂ O, O ₂ , O ₃	8
M6	0.746	0.739-0.754	H ₂ O, O ₂	8
M7	0.865	0.846-0.885	H ₂ O, O ₂	8
M8	1.240	1.23-1.24	H ₂ O, O ₂ , CO ₂	8
M9	1.378	1.371-1.386	H ₂ O	12
M10	1.61	1.58-1.64	H ₂ O, CO ₂ , CH ₄	4
M11	2.25	2.23-2.28	CH ₄ , H ₂ O, N ₂ O	4
M12	3.7	3.61-3.79	H ₂ O, CH ₄ , O ₃	4
M13	4.05	3.97-4.13	CO ₂ , H ₂ O, N ₂ O	16
M14	8.55	8.4-8.7	H ₂ O, N ₂ O, O ₃ , cont.	8
M15	10.763	10.26-11.26	H ₂ O, CO ₂ , O ₃ , cont.	4
M16	12.013	11.54-12.49	H ₂ O, CO ₂ , O ₃ , cont.	8
I1	0.64	0.60-0.68	H ₂ O, O ₂	4
I2	0.865	0.85-0.88	H ₂ O, O ₂	8
I3	1.61	1.58-1.64	H ₂ O, CO ₂ , CH ₄	4
I4	3.74	3.55-3.93	H ₂ O, N ₂ O, CH ₄	4
I5	11.45	10.5-12.4	H ₂ O, CO ₂ , O ₃ , cont.	16



538

539 **FIG. 1.** Example of the treatment of overlap absorption lines, spectral response function
 540 (SRF), and solar irradiance (SI) based on the CKD algorithm for the VIIRS 1.61- μm
 541 channel. (a)-(c) Absorption coefficient as a function of wavenumber for H_2O , CO_2 , and
 542 CH_4 . (d) Absorption coefficient for a mixed case with the ratio of the three gases being
 543 1:0.1:0.001. (e) Spectral response function. (f) Solar irradiance at the top of atmosphere.
 544 (g) Absorption coefficient as a function of cumulative probability for the mixed gas with
 545 and without the inclusion of the spectral response function and solar irradiance.



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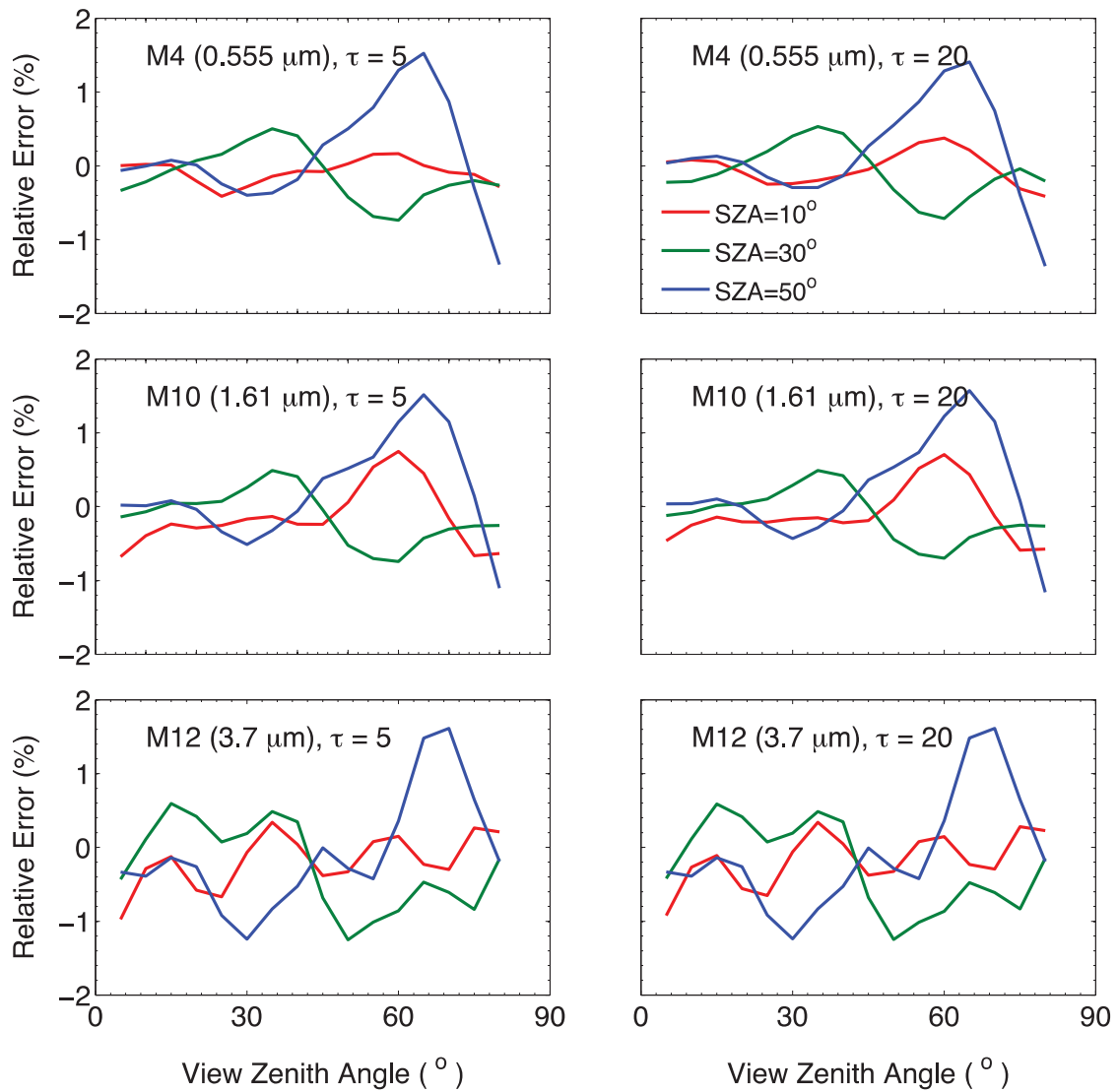
547 **FIG. 2.** Band-averaged transmissivity (left) calculated from the LBLRTM and CKD

548 models for VIIRS 0.555-, 1.61-, 3.7-, and 10.763- μm channels. Corresponding relative

549 errors (middle) and weight function (right) profiles of the CKD models. The U.S. standard

550 atmospheric profile is used in the calculations.

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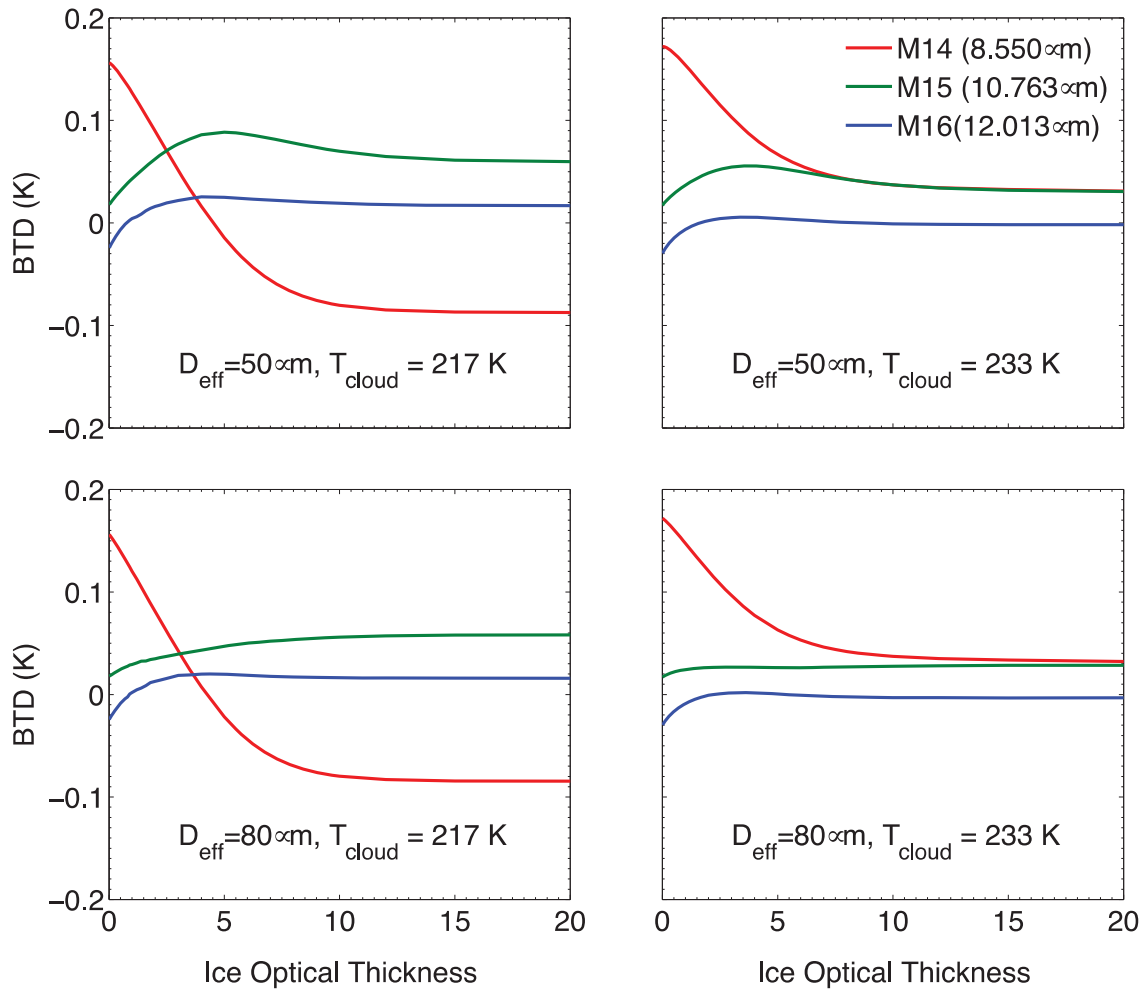


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553 **FIG. 3.** Relative errors of TOA reflectance at M4 (0.555 μm), M10 (1.61 μm), and M12

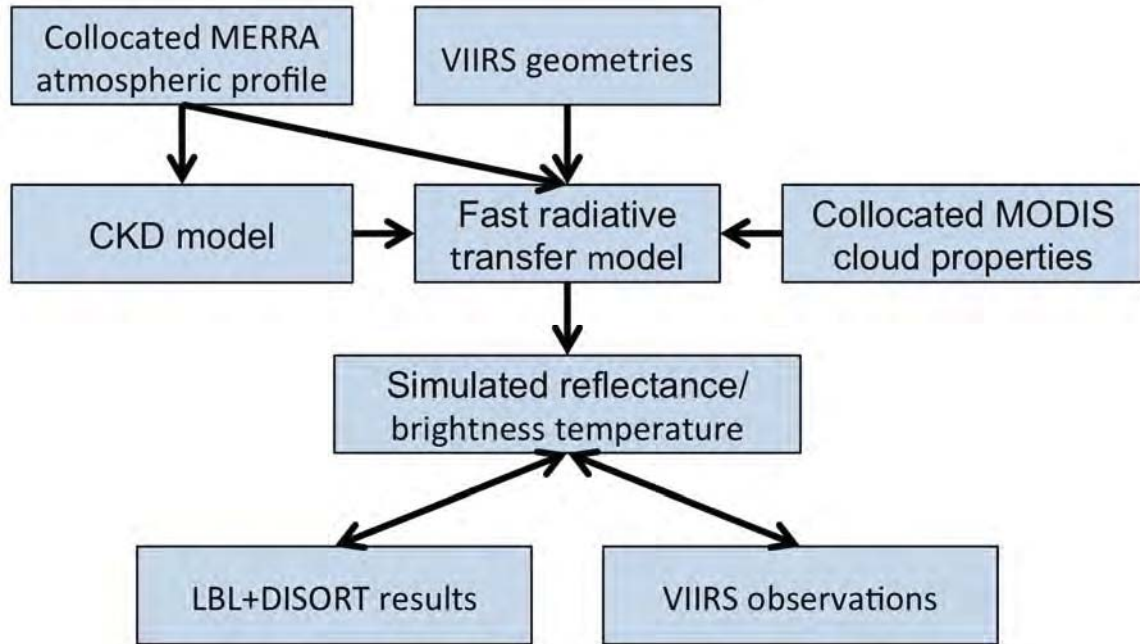
554 (3.7 μm) channels by the VIIRS simulator in comparison with the benchmark model.

555



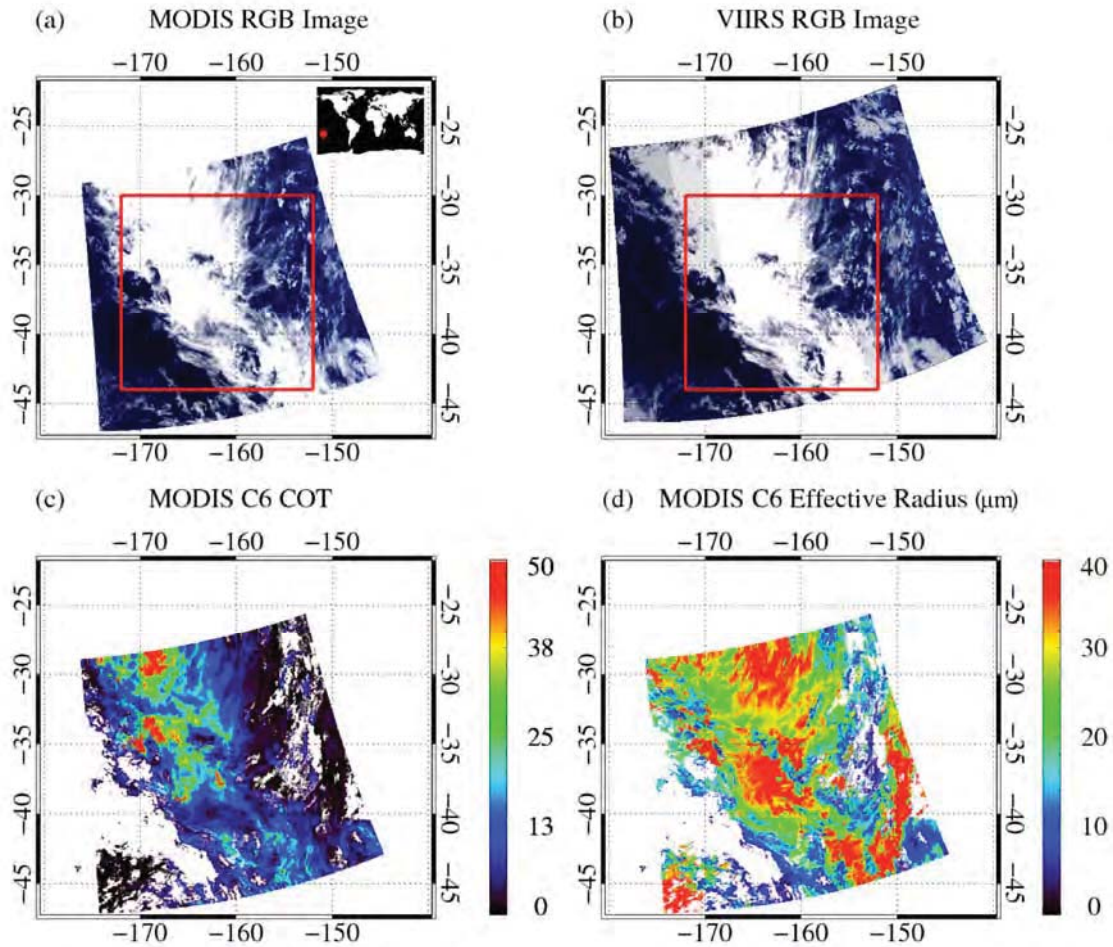
556

557 **FIG. 4.** Brightness temperature difference (CKD+FRTM – LBL+DISORT) as a function
 558 of ice optical thickness for a viewing zenith angle of 20° at three VIIRS infrared channels
 559 (8.55-, 10.763-, and 12.013- μm).



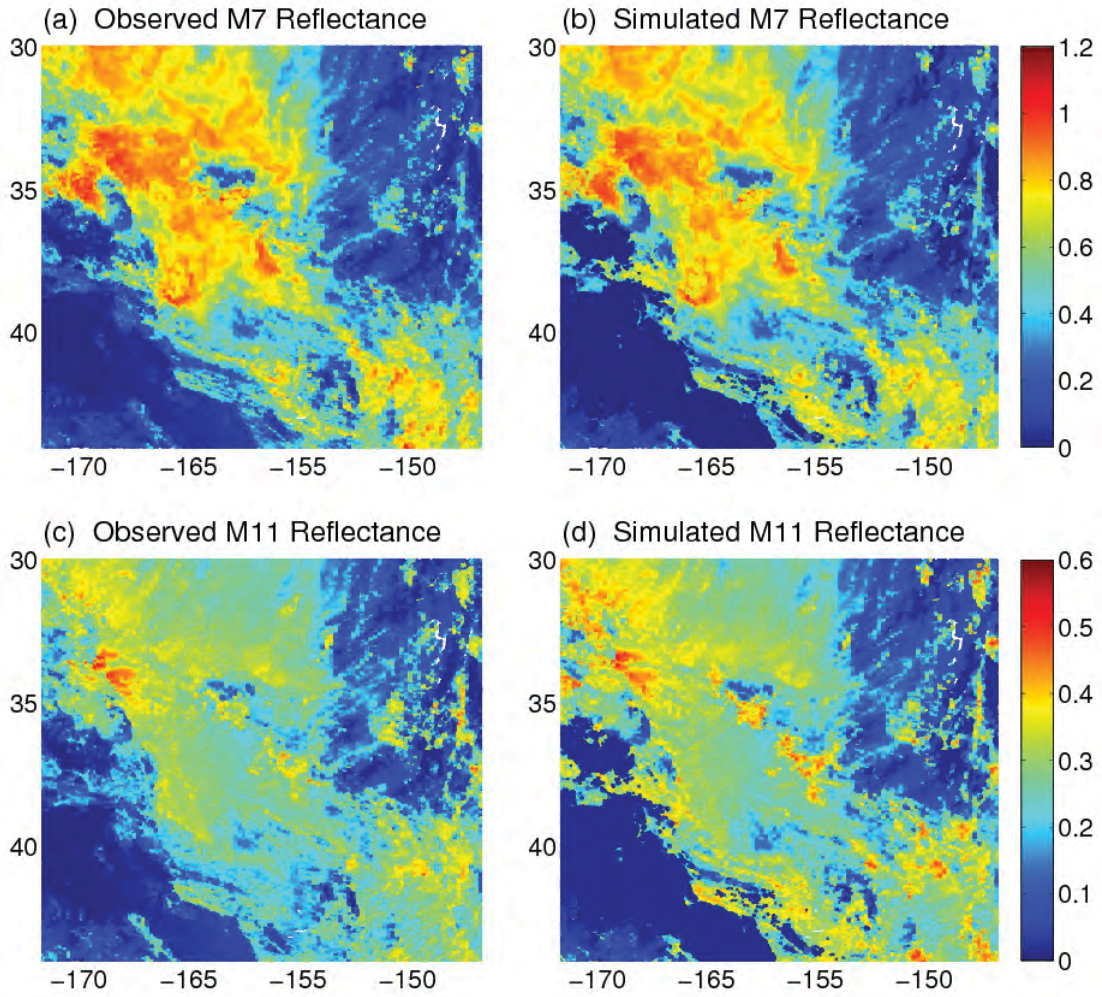
560

561 **FIG. 5.** Flowchart outlining the fast VIIRS radiance simulator using the collocated
 562 MERRA atmospheric profile and MODIS retrieved ice cloud thickness and effective
 563 particle size.



564

565 **FIG. 6.** (a) MODIS RGB image for a granule on 3 January 2014 at 0:45 UTC taken over
 566 the South Pacific Ocean. (b) RGB image of the corresponding VIIRS granules from
 567 00:38:47.4 to 00:41:38.2 UTC of the same day. (c) and (d) are the MODIS Collection 6
 568 cloud optical thickness and particle effective radius of ice clouds.

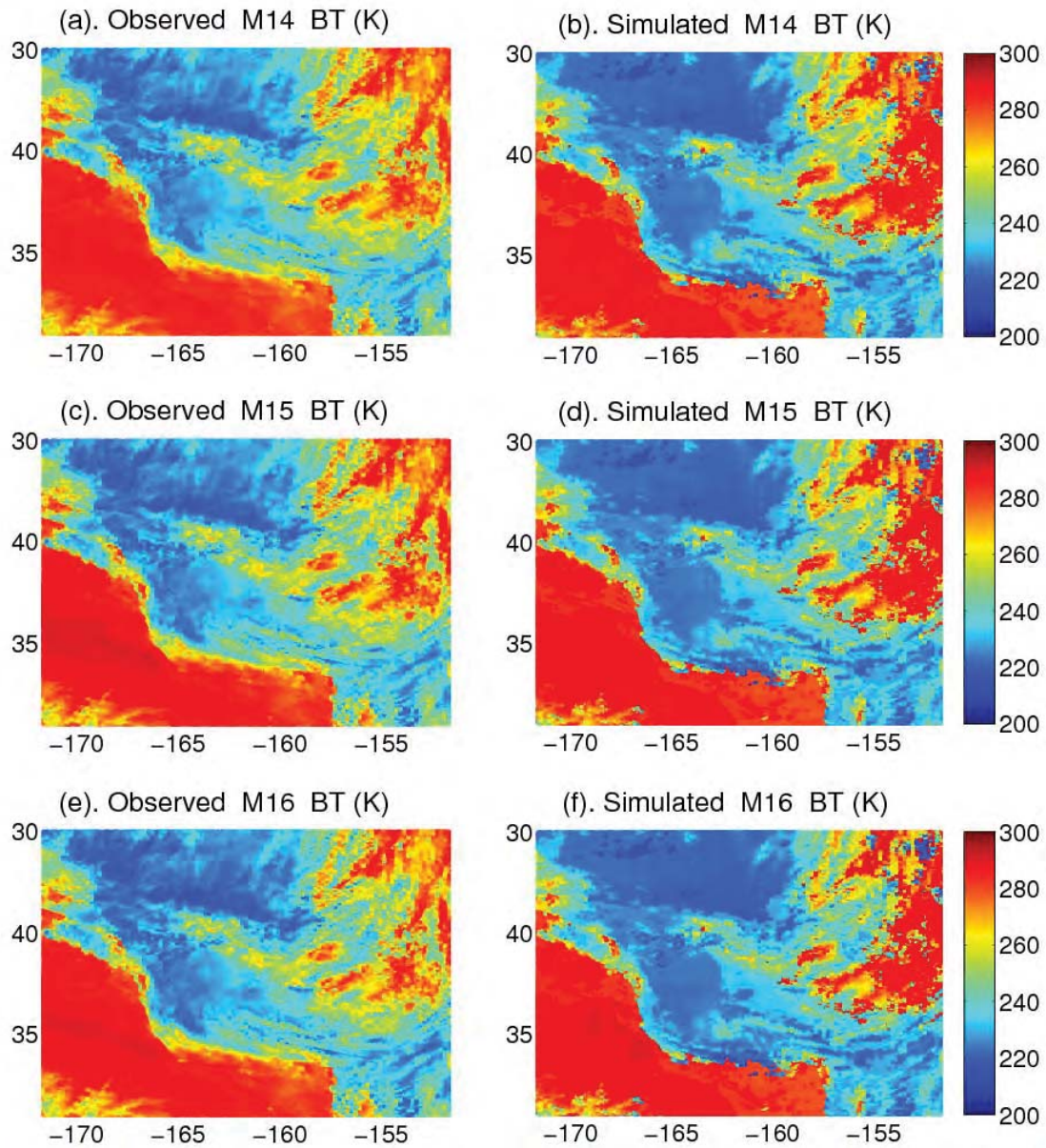


569

570 **FIG. 7.** Comparison between the observed (left panels) and simulated (right panels)

571 reflectances at the VIIRS M7 (0.865 μm) and M11 (2.25 μm) channels.

572



573

574 **FIG. 8.** Comparison between the observed (left panels) and simulated (right panels)

575 brightness temperatures at the VIIRS M14 (8.55 μm), M15 (10.763 μm), and M11 (12.013

576 μm) channels.

577