

National Aeronautics and Space Administration



# Comparison of Models for Rolling Element Bearing Dynamic Capacity and Life

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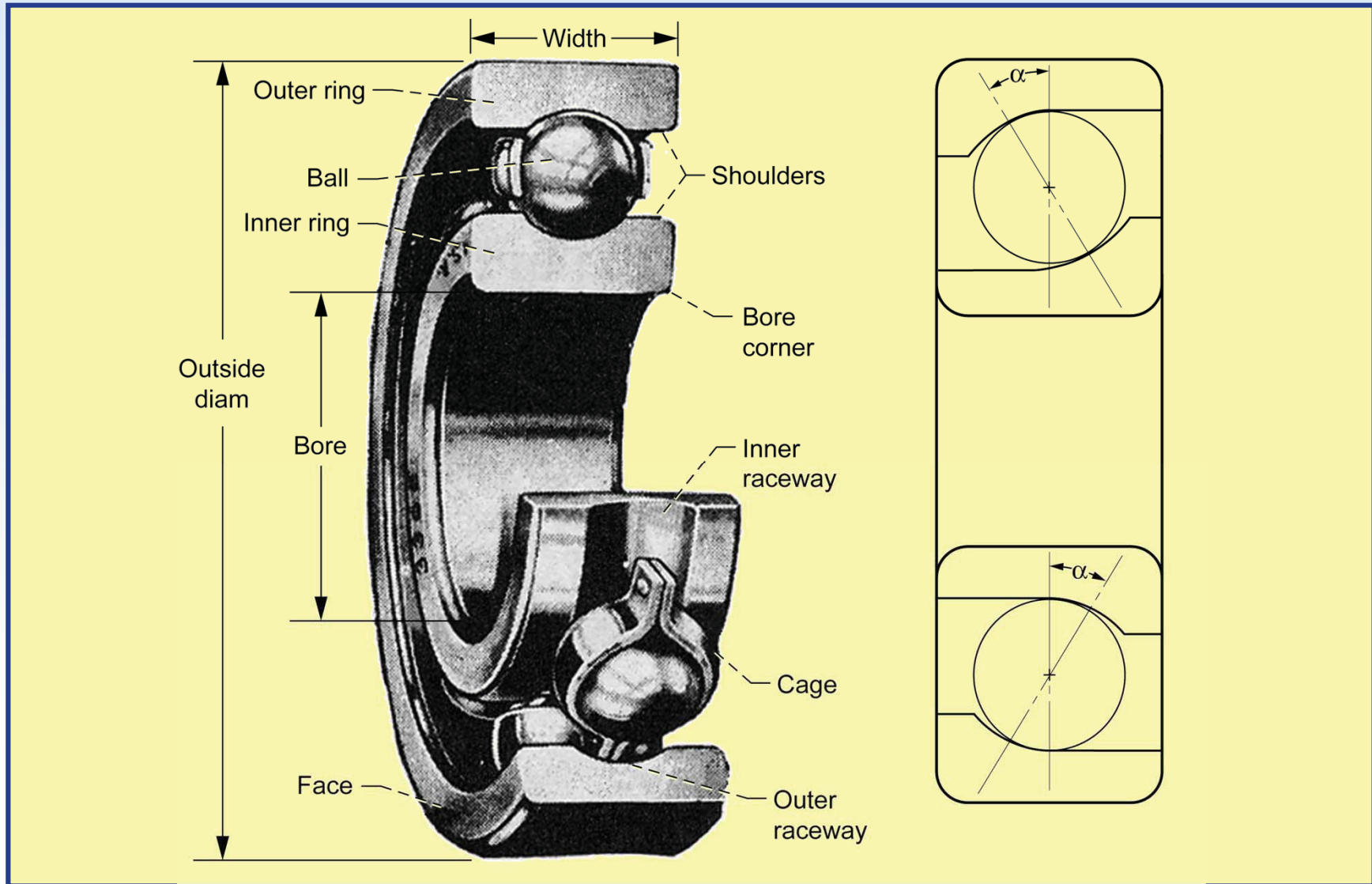
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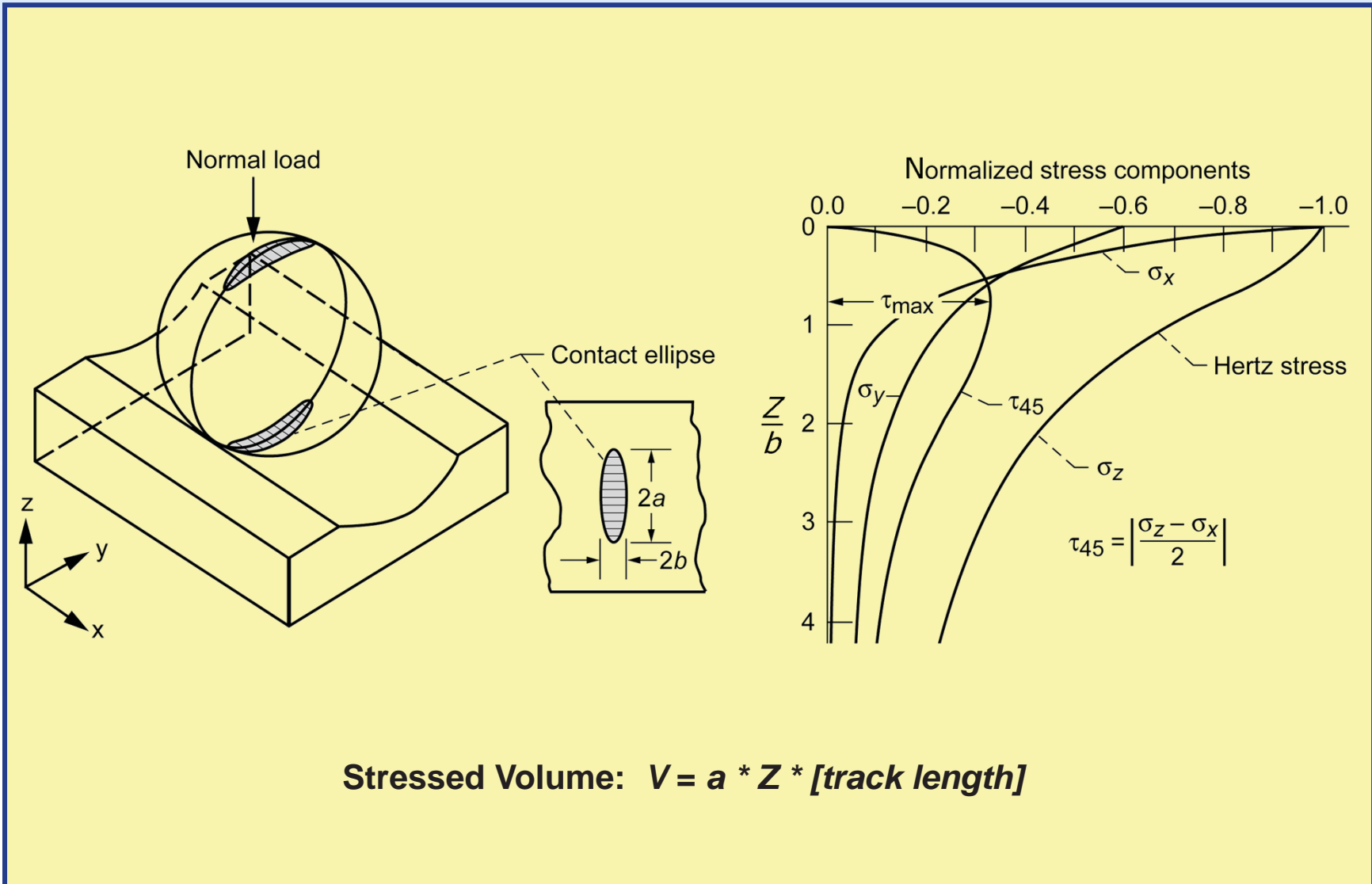
## Objectives

- **Update Lundberg-Palmgren (LP) life model**
- **Incorporate Updated LP and Zaretsky (Z) models into ADORE bearing code**
- **Benchmark updated LP and Z life models to contemporary bearing life data**
- **Compare Lundberg-Palmgren with Zaretsky life models**

# Deep Groove and Angular Contact Ball Bearing



# Ball Bearing Stresses Below Contact Patch



**Stressed Volume:  $V = a * Z * [track\ length]$**



## Ball Bearing Life

### 1947 Lundberg-Palmgren Life Model

$$L_{LP} = K_{LP} \left( \frac{1}{\tau_o} \right)^{c/e} \left( \frac{1}{V_o} \right)^{1/e} (Z_o)^{h/e} = K_{LP} \left( \frac{1}{\tau_o} \right)^{9.3} \left( \frac{1}{V_o} \right)^{0.9} (Z_o)^{2.1}$$

where

$L_{LP}$  = Lundberg-Palmgren  $L_{10}$  life

$K_{LP}$  = Material & geometry constant

$\tau_o$  = Maximum orthogonal shear stress

$V_o$  = Stressed volume

$Z_o$  = Depth to maximum orthogonal shear stress

$c, h, e$  ... exponents chosen to fit experimental data



## L-P Model Stress-Life & Load-Life Exponents

for Lundberg-Palmgren model, point contact

$$L_{LP} \sim \left(\frac{1}{\tau_o}\right)^{c/e} \left(\frac{1}{V_o}\right)^{1/e} (Z_o)^{h/e} \sim \left(\frac{1}{S_{\max}}\right)^{9.3} \left(\frac{1}{S_{\max}^2}\right)^{0.9} (S_{\max})^{2.1} \sim \left(\frac{1}{S_{\max}}\right)^n$$

where

$c, h, e, n, p \dots$  exponents

$Q$  = Applied load

$S_{\max}$  = Max. Hertz stress

$$n = \frac{c + 2 - h}{e} = 9.3 + 2(0.9) - 2.1 = 9 \Rightarrow L \sim \left(\frac{1}{S_{\max}}\right)^9$$

$$S_{\max} \sim Q^{1/3} \Rightarrow L \sim \left(\frac{1}{Q}\right)^3$$



## Ball Bearing Life

### 1987 Zaretsky Life Model

$$L_Z = K_Z \left( \frac{1}{\tau_m} \right)^c \left( \frac{1}{V_m} \right)^{1/e} = K_Z \left( \frac{1}{\tau_m} \right)^{10.3} \left( \frac{1}{V_m} \right)^{0.9}$$

where

$L_Z$  = Zaretsky  $L_{10}$  life

$K_Z$  = Material & geometry constant, where  $K_Z \neq K_{LP}$

$\tau_m$  = Maximum shear stress

$V_m$  = Stressed volume

$c, e \dots$  exponents

(exponent 'h' in LP equation  $\rightarrow$  0)



## Zaretsky Model Stress-Life & Load-Life Exponents

for Zaretsky model with point contact

$$L_Z \sim \left(\frac{1}{\tau_m}\right)^c \left(\frac{1}{V_m}\right)^{1/e} \sim \left(\frac{1}{S_{\max}}\right)^{10.3} \left(\frac{1}{S_{\max}^2}\right)^{0.9} \sim \left(\frac{1}{S_{\max}}\right)^n$$

where

$c, h, e, n, p \dots$  exponents, and  $h = 0$

$S_{\max}$  = Max. Hertz stress

$Q$  = Applied load

$$n = c + \frac{2}{e} = 10.3 + 2(0.9) = 12$$

$$S_{\max} \sim Q^{1/3} \Rightarrow L \sim \left(\frac{1}{Q}\right)^4$$





## Load-Life Relationship for Point Contact

$$L = \left( \frac{Q_c}{Q} \right)^p$$

where

$L$  =  $L_{10}$  life

$Q_c$  = Dynamic load capacity for  $L_{10} = 10^6$  revolutions

$Q$  = Applied load

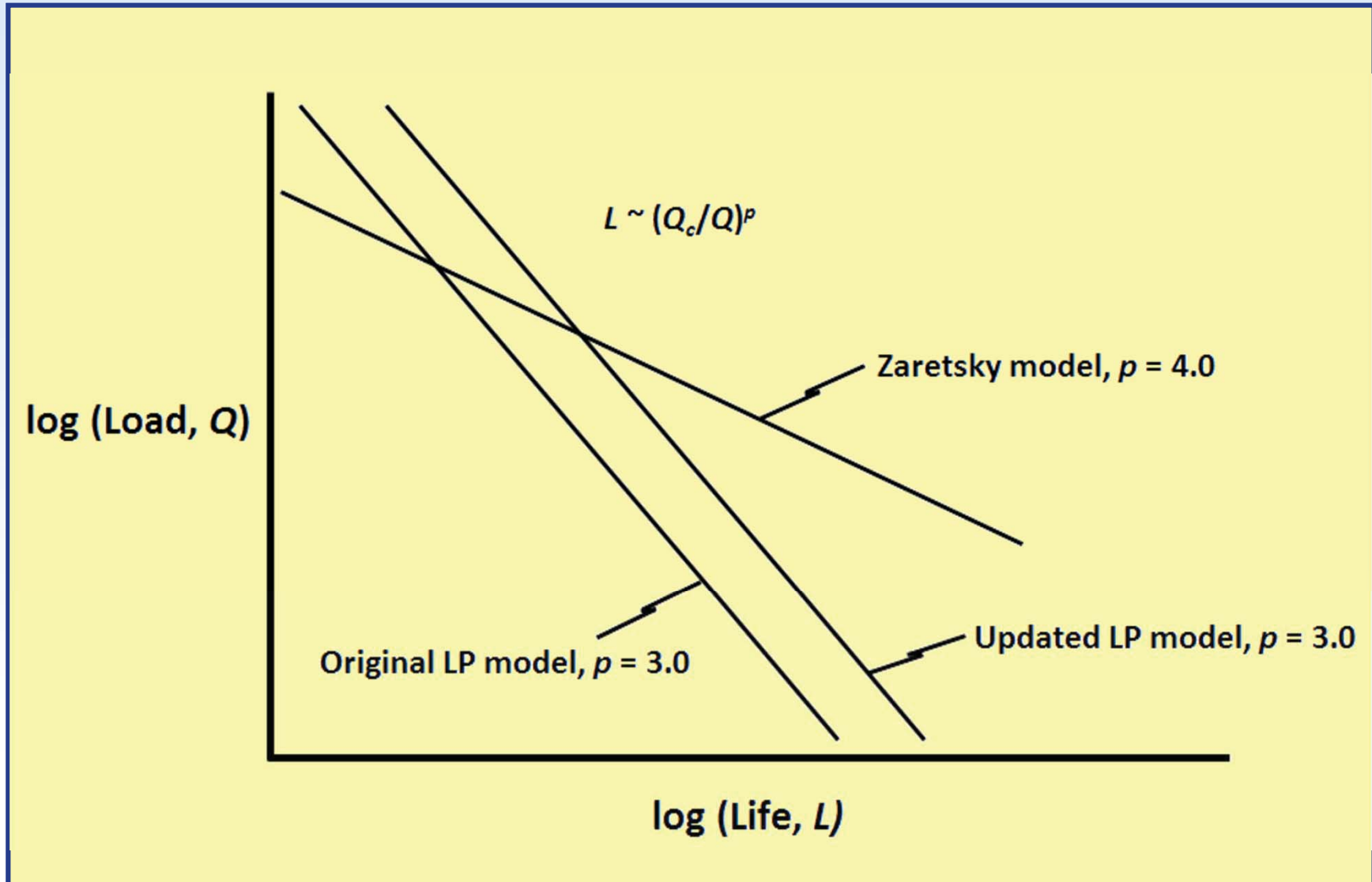
$p$  = Load-life exponent,  $\rightarrow p = n/3$

Lundberg-Palmgren model:  $p = 9/3 = 3$

Zaretsky model:  $p = 12/3 \approx 4$



# Comparison of Load-Life Relationships





## Procedure

### **Update Lundberg-Palmgren life model**

- **Separate material & geometry constants from model**
- **Incorporate into bearing code ADORE**
- **Derive a new geometry constant**
- **Benchmark life model to published life data**
- **Compute new bearing dynamic capacity**

### **Apply similar process to Zaretsky model**

**Compare lives: Orig. LP, Updated LP, Zaretsky Models**



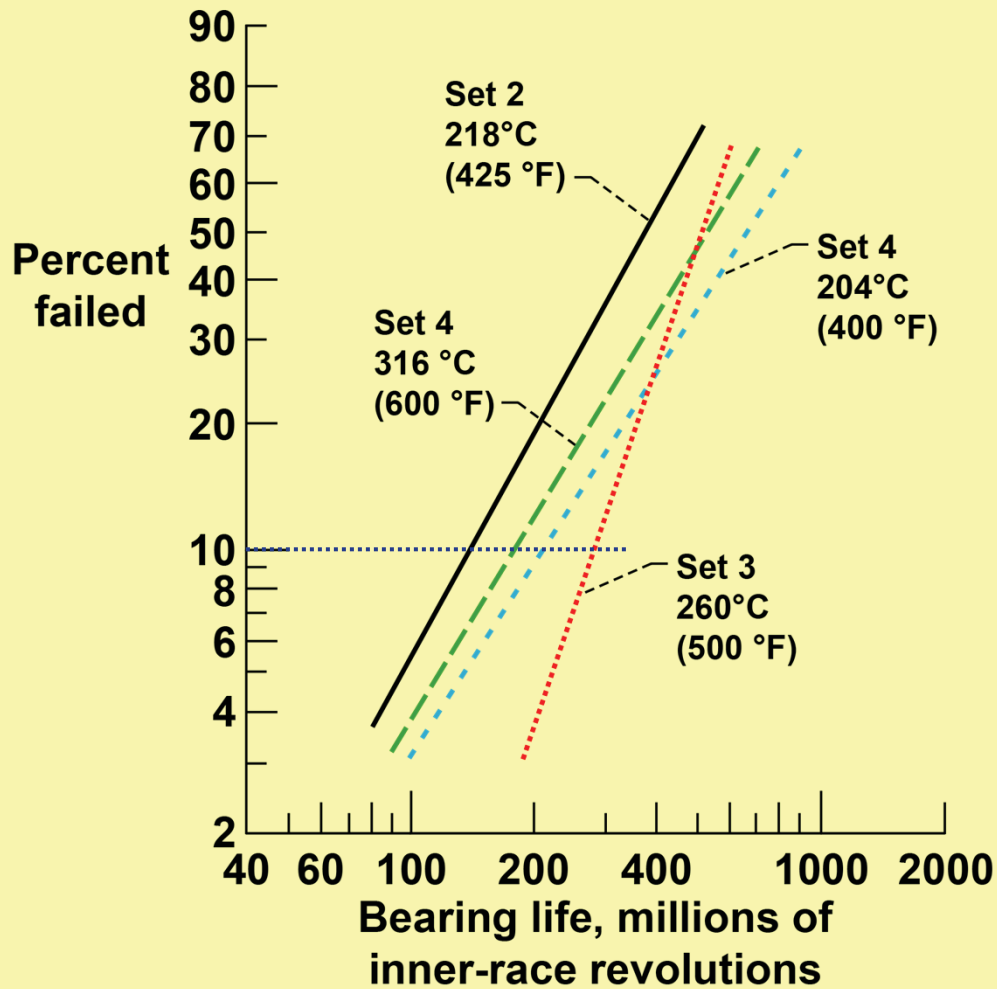
## Bearing Life Database Parameters

- **120-mm bore, 20° angular contact ball bearing**
- **15 balls, 20.6 mm (13/16") dia.**
- **AISI M-50 steel, consumable electrode vacuum melted (CEVM)**
- **Synthetic paraffinic oil (PAO)**
- **Speed 12,000 rpm (1.44 Million DN)**
- **Thrust load 25,800 N (5800 lb)**



# Bearing Life Database

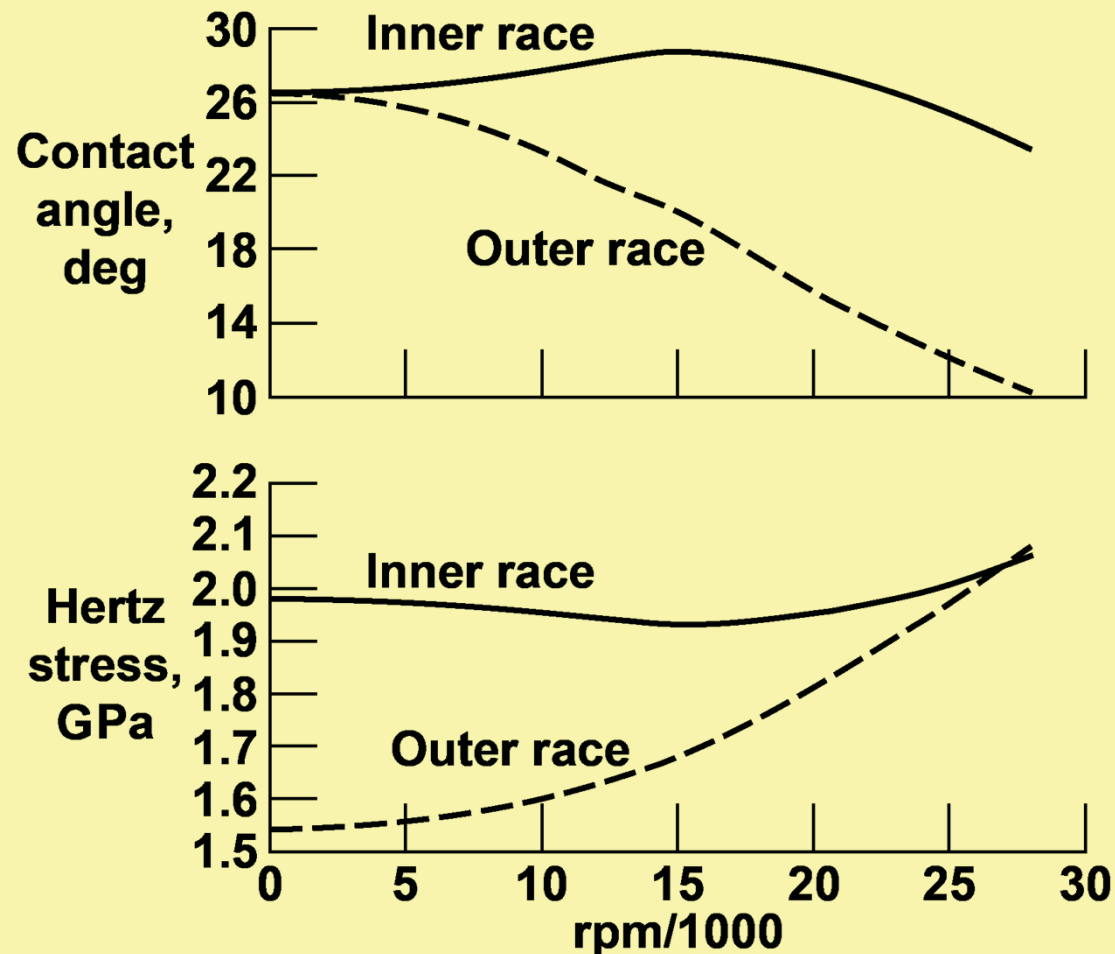
120-mm bore, 20° contact angle, CEVM, AISI M-50 Steel,  
PAO oil @ 12,000 rpm, 25,800 N (5,800 lb) thrust load





## Speed Effect on Hertz Stress and Contact Angle

120-mm bore, 24° contact angle, VIM-VAR, AISI M-50 Steel,  
 @ 25,800 N (5,800 lb) load, MIL-L-23699 oil @ 218 °C (425°F)

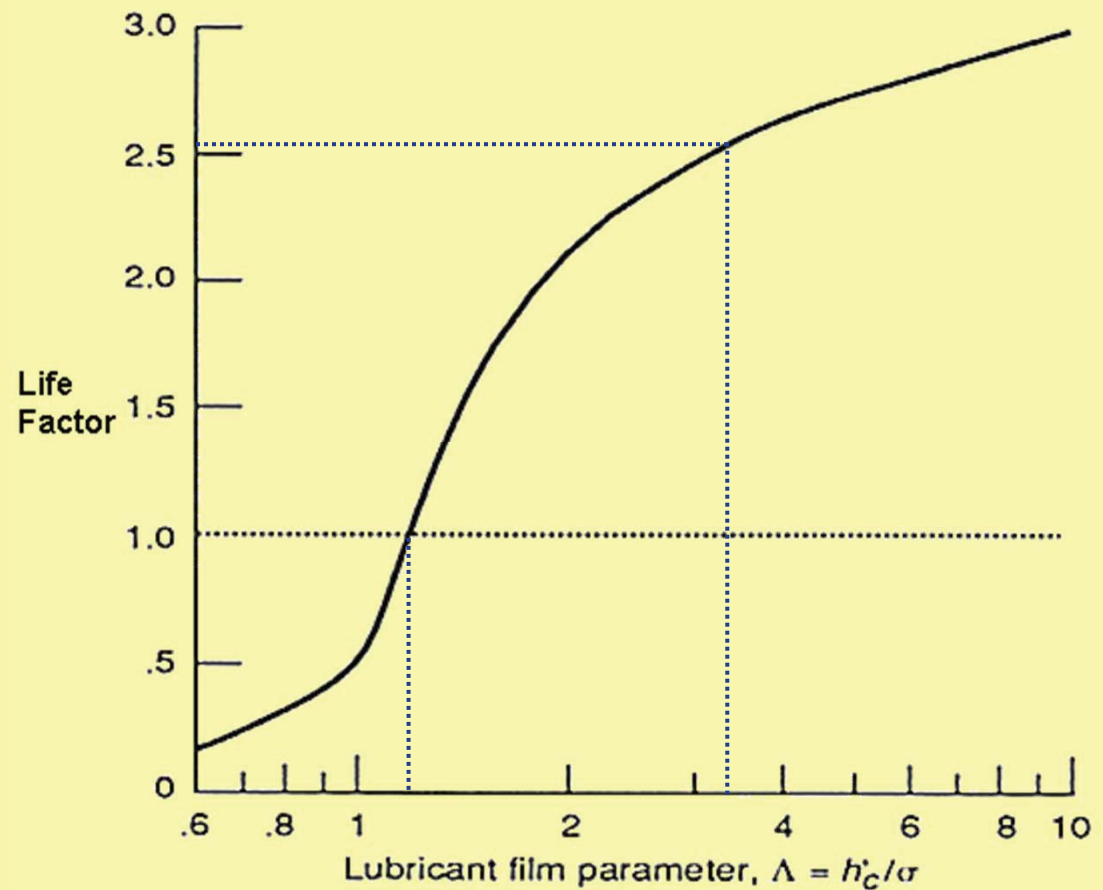




## STLE Life Factors Applied

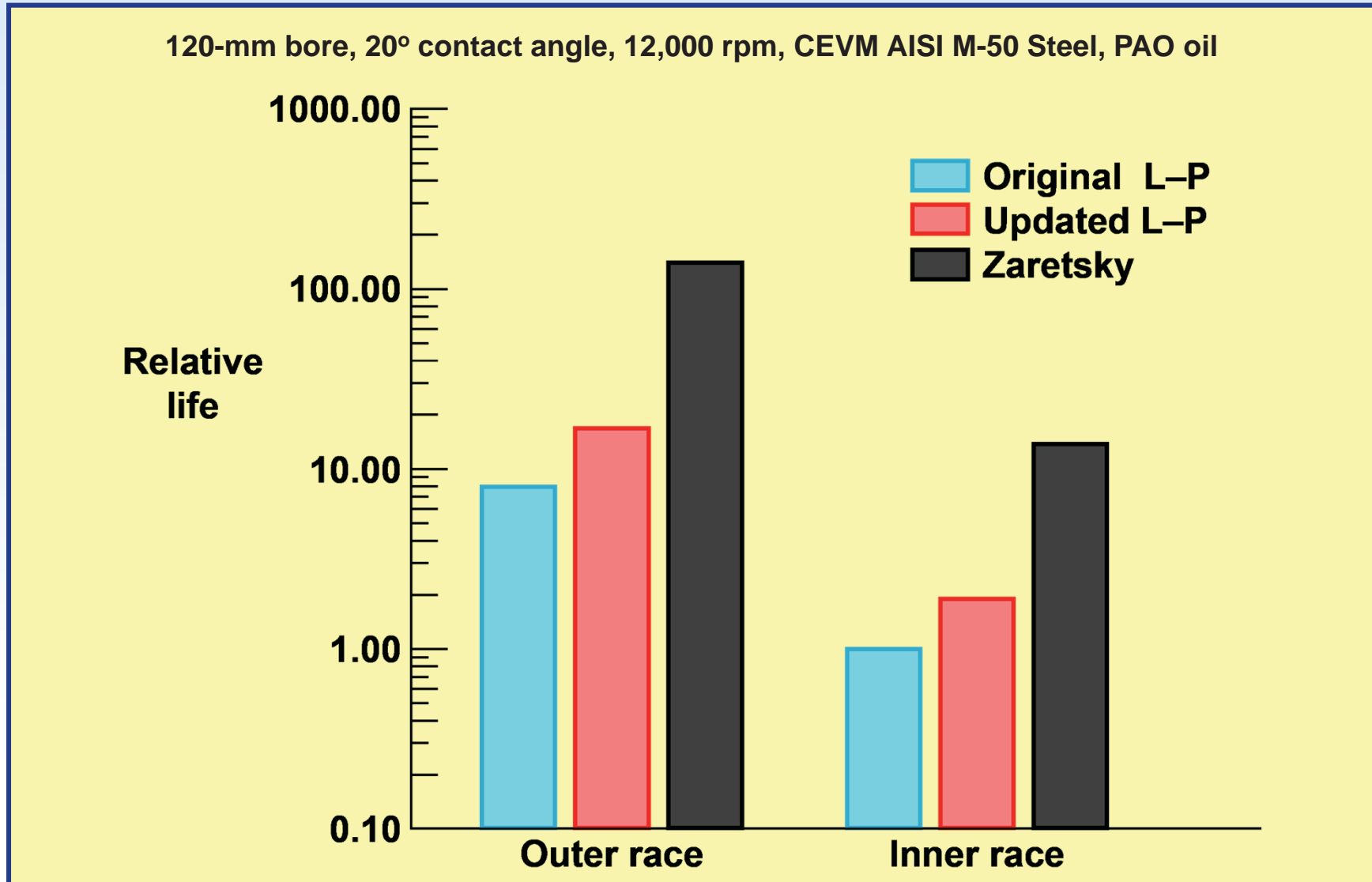
120-mm bore, 24° contact angle, VIM-VAR, AISI M-50 Steel, @ 12,000 rpm,  
MIL-L-23699 oil @ 218 °C (425°F), Film parameter  $\Lambda = 3.38$

Material (AISI M-50)	2.00
Steel Processing (VIM-VAR)	6.00
Hardness ( $R_C=62$ )	1.05
Lubrication	2.52
Life Factor Product	31.75





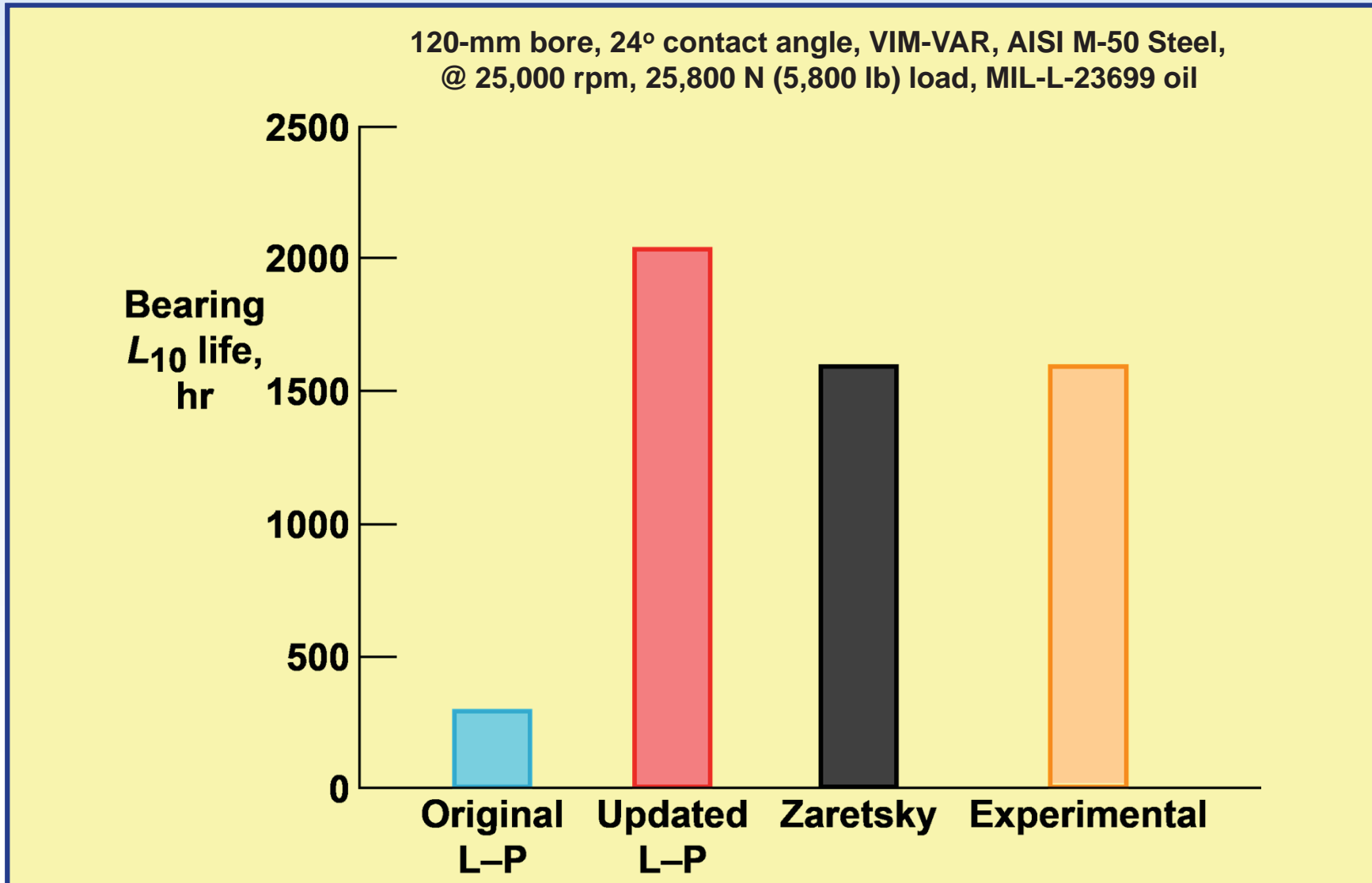
## Relative Life for Three Models





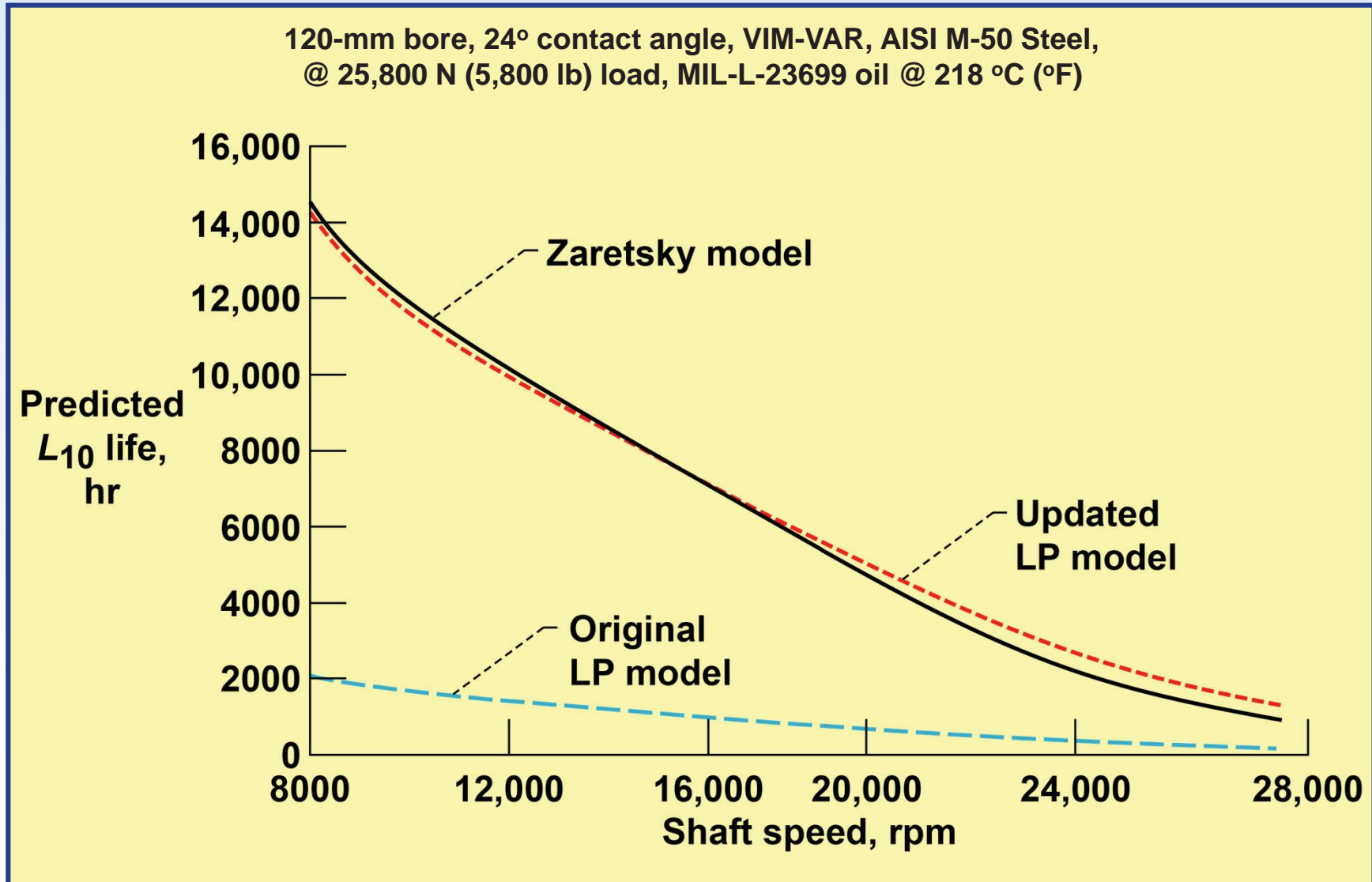


## Analysis applied to 3 Million DN Bearing



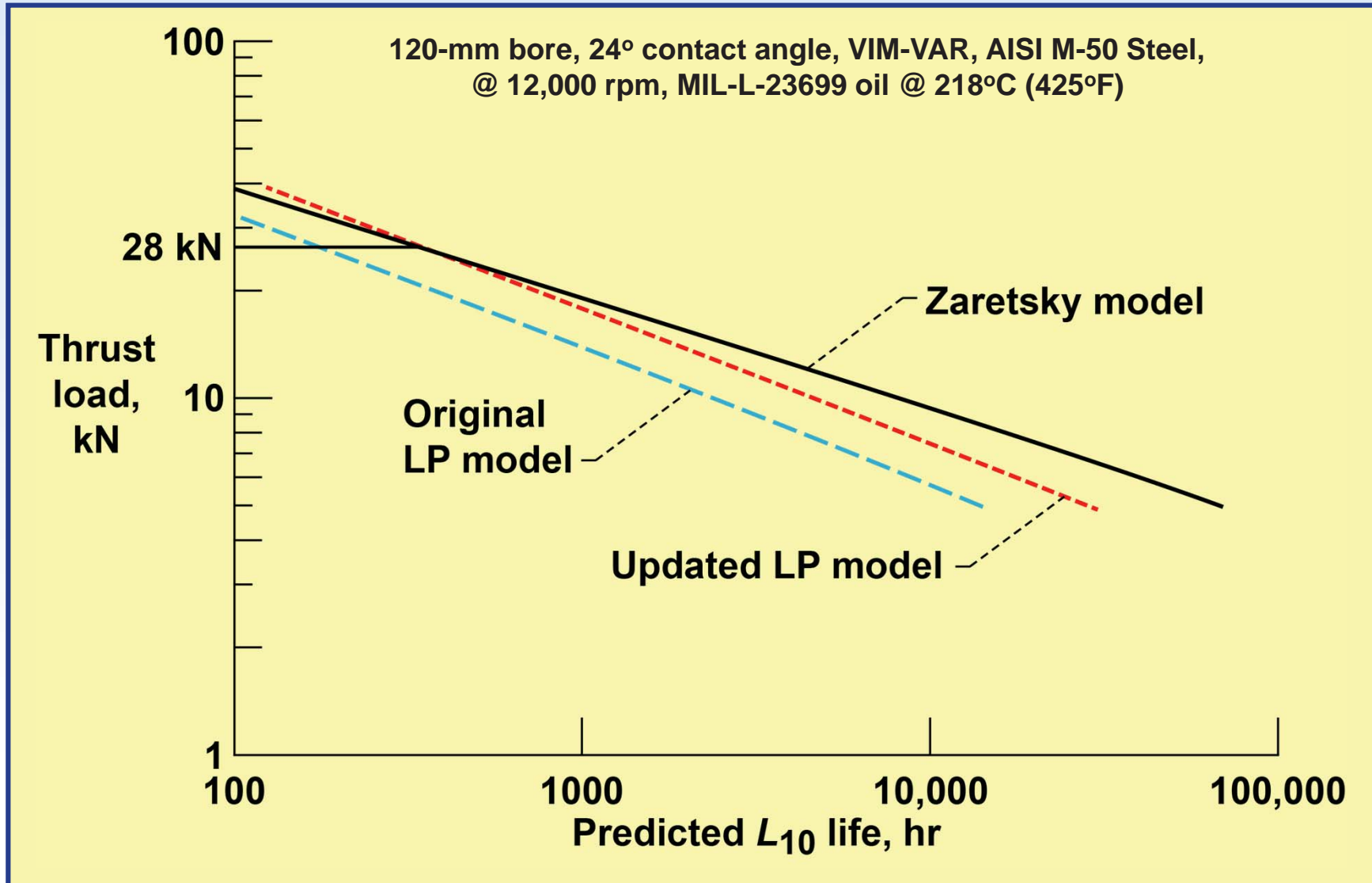


## Effect of Speed on $L_{10}$ Life





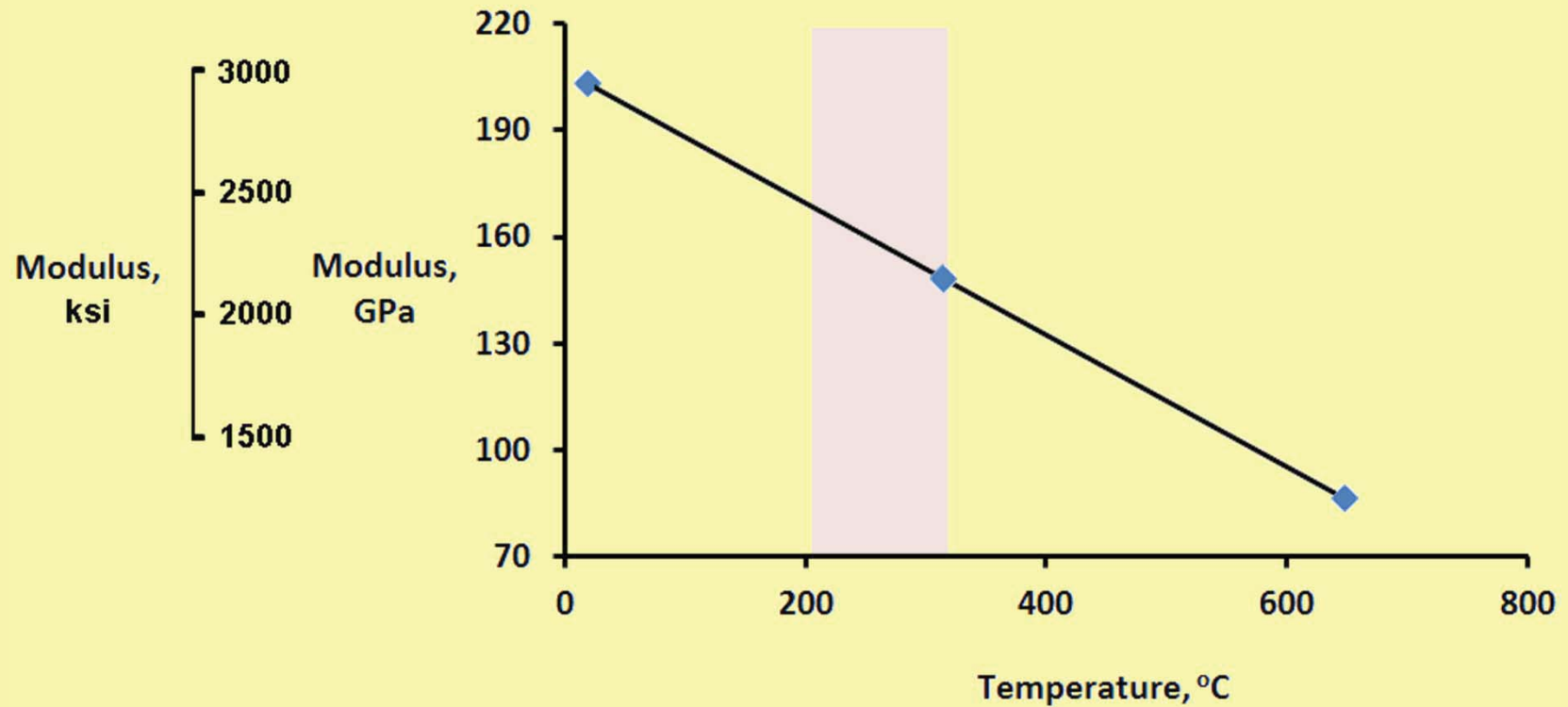
## Effect of Thrust Load on $L_{10}$ Life





## Variation of Elastic Properties with Temperature

Lower modulus means lower stress, longer life

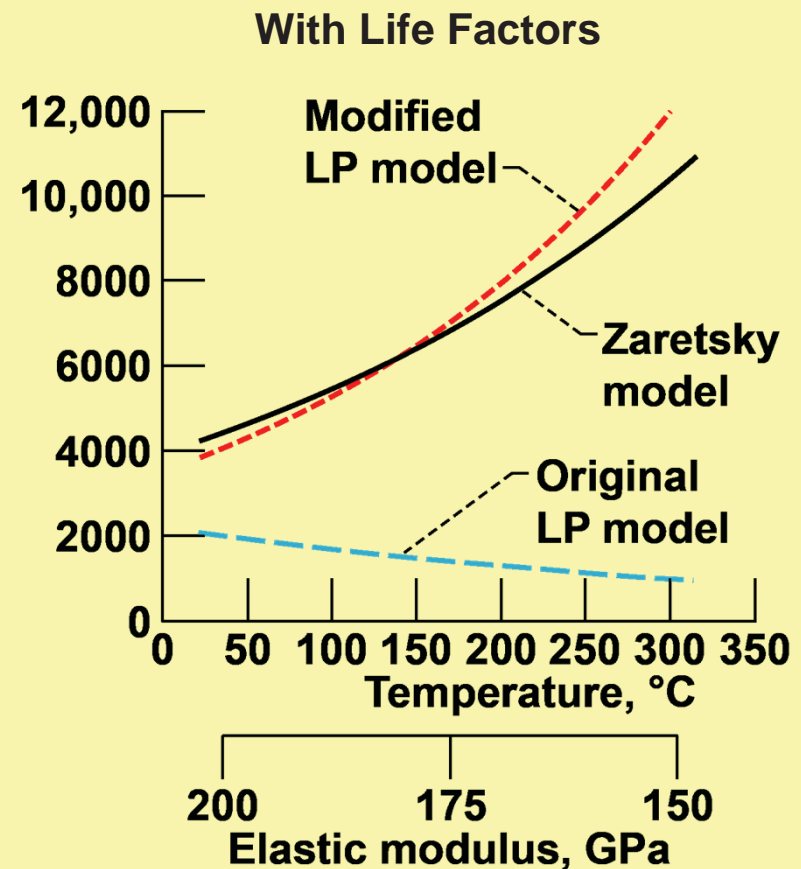
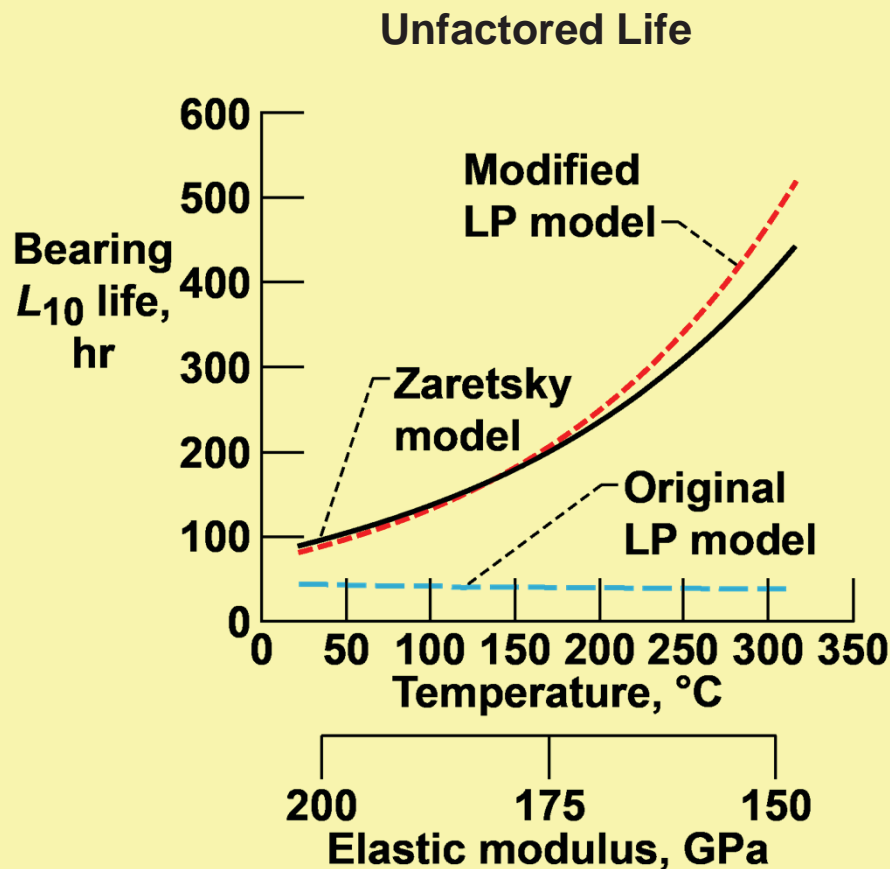


Source: MatWeb, Online Materials Information Resource  
<http://www.matweb.com/>



## Effect of Variation of Elastic Properties on Life

120-mm bore, 24° contact angle, VIM-VAR, AISI M-50 Steel,  
@ 12,000 rpm, 25,800 N (5,800 lb) load, MIL-L-23699 oil





## Summary of Results

- **Variation of elastic modulus with temperature has significant effect on life. Higher temperatures → longer life**
- **Updated Lundberg-Palmgren model → 7 times life, primarily due to modulus change @ elevated temperature.**
- **Updated Lundberg-Palmgren & Zaretsky models give similar results. Zaretsky model shows shorter life at high speed.**
- **Zaretsky model predicts longer life at light loads and greater life reduction as loads increase.**