

1     **A dynamic approach to addressing observation-minus-forecast**  
2           **mean differences in a land surface skin temperature data**  
3                   **assimilation system**

4     CLARA DRAPER<sup>1,2</sup>, \* ROLF REICHLE<sup>1</sup>, GABRIELLE DE LANNOY<sup>1,2</sup>

1. *Global Modeling and Assimilation Office, NASA GSFC, Greenbelt, MD, USA*

2. *Universities Space Research Association, Columbia, MD, USA*

5                   BENJAMIN SCARINO<sup>3</sup>

3. *Science Systems and Applications, Inc., Hampton, VA, USA*

---

\* *Corresponding author address:* Clara Draper, Global Modeling and Assimilation Office, NASA GSFC, Code 610.1, Greenbelt, MD, 20771, USA.

E-mail: clara.draper@nasa.gov

## ABSTRACT

7 In land data assimilation, bias in the observation-minus-forecast (O-F) residuals is typically  
8 removed from the observations prior to assimilation by rescaling the observations to have  
9 the same long-term mean (and higher-order moments) as the corresponding model fore-  
10 casts. Such observation rescaling approaches require a long record of observed and forecast  
11 estimates, and an assumption that the O-F mean differences are stationary. A two-stage  
12 observation bias and state estimation filter is presented, as an alternative to observation  
13 rescaling that does not require a long data record or assume stationary O-F mean differ-  
14 ences. The two-stage filter removes dynamic (nonstationary) estimates of the seasonal scale  
15 O-F mean difference from the assimilated observations, allowing the assimilation to correct  
16 the model for synoptic-scale errors without adverse effects from observation biases. The  
17 two-stage filter is demonstrated by assimilating geostationary skin temperature ( $T_{skin}$ ) ob-  
18 servations into the Catchment land surface model. Global maps of the O-F mean differences  
19 are presented, and the two-stage filter is evaluated for one year over the Americas. The two-  
20 stage filter effectively removed the  $T_{skin}$  O-F mean differences, for example the GOES-West  
21 O-F mean difference at 21:00 UTC was reduced from 5.1 K for a bias-blind assimilation to 0.3  
22 K. Compared to independent in situ and remotely sensed  $T_{skin}$  observations, the two-stage  
23 assimilation reduced the unbiased Root Mean Square Difference (ubRMSD) of the modeled  
24  $T_{skin}$  by 10% of the open-loop values.

# 1. Introduction

Within the context of data assimilation, ‘bias’ refers to errors in modeled or observed variables that persist over time and/or space. Standard ‘bias-blind’ data assimilation methods are based on the assumption that neither the forecast model nor the observations are biased, and these methods will produce suboptimal output in the presence of bias (Dee and Da Silva 1998). Unfortunately, the forecast models and observation data sets used in Earth system applications, including for the land surface, typically are biased (Dee and Todling 2000; Reichle et al. 2004). Observation biases can arise from errors in the observing instrument and its calibration, the observation operator, or the retrieval model, as well as representativity errors between the observed state variables and their modeled counterparts. Likewise, forecast biases can arise from errors in the forecast model structure, parameters, initial conditions, and forcing.

Ideally, the cause of observation and forecast biases should be diagnosed and treated at the source. Where this is not possible, these biases can also be addressed in data assimilation by applying an observation bias correction prior to assimilation (e.g., Harris and Kelly, 2001) or by using a ‘bias-aware’ assimilation system explicitly designed to correct either observation biases (e.g., Auligné et al. 2007; Fertig et al. 2009 ) or forecast biases (e.g., Dee and Todling 2000; Keppenne et al. 2005). Bias correction methods require that the bias be observable (Dee and Da Silva 1998), and the ocean and atmosphere examples cited above measure the biases against confident estimates of the true mean state, typically obtained with reference to point-based observations (e.g., ocean buoys, radiosondes). However, the land surface is much more heterogeneous than the ocean and atmosphere, and point-based in situ observations are in general not representative of the coarse resolution states estimated by remote sensors and land surface models (Crow et al. 2012). Consequently, for large domains the true mean land surface states are unknown, since there are large systematic differences between the mean (and variance) of different observed and modeled land surface data sets, none of which can in general be identified as having statistics representative of the true state (Reichle et al.

52 2004).

53 Since observation and forecast biases cannot be observed for land surface states, it is  
54 standard practice to remove the systematic differences between the observed and forecast  
55 estimates from land data assimilation, usually by rescaling the observations to be consis-  
56 tent with the long-term mean (and variance, and sometimes higher order moments) of the  
57 forecasts (e.g., Reichle and Koster 2004; Drusch et al. 2005; Scipal et al. 2008; Crow et al.  
58 2011). This prevents the systematic differences from adversely impacting the model state,  
59 while satisfying the minimum criterion for optimal bias-blind data assimilation that there be  
60 no difference between the mean values of the observed and forecast estimates. The assimi-  
61 lation can then correct the model for random errors developing during each forecast, where  
62 ‘random errors’ are errors persisting over time scales much shorter than the assumed bias  
63 time scale. Data assimilation with observation rescaling has been shown to yield land surface  
64 estimates that are superior to modeled or observed estimates alone (Slater and Clark 2006;  
65 Reichle et al. 2007; Ghent et al. 2010; Crow et al. 2011; Draper et al. 2012; De Lannoy et al.  
66 2012; de Rosnay et al. 2013). This rescaling approach is often referred to as ‘observation  
67 bias correction’, although strictly speaking, it is not the observation bias (defined against  
68 the true mean state) that is corrected, but the lumped observation-bias-minus-forecast-bias.

69 The long data record of observed and forecast state estimates required for estimating  
70 observation rescaling coefficients has slowed the implementation of land data assimilation  
71 in large-scale applications, particularly within atmospheric systems, which are frequently  
72 updated and yet prohibitively expensive to replay over long periods. Consequently, Dharssi  
73 et al. (2011) and de Rosnay et al. (2013) identify the difficulty in obtaining observation  
74 rescaling coefficients as one cause of the limited impact of assimilating remotely sensed soil  
75 moisture observations into atmospheric models. The long data record requirement also pre-  
76 vents the assimilation of new remotely sensed data sets, and necessitates costly reprocessing  
77 of the rescaling parameters after significant updates to assimilated data sets.

78 Consequently, this manuscript presents a method for removing the O-F mean difference

79 (i.e., the lumped observation-bias-minus-forecast-bias) in land data assimilation systems  
80 without access to a long data record, by using a two-stage observation bias and state update  
81 estimation filter. ‘Bias’ is defined subjectively, in terms of the temporal and spatial scales  
82 over which it applies. In seeking a bias correction method that does not require a long data  
83 record, the bias is necessarily defined over shorter time scales, and the presented two-stage  
84 filter dynamically estimates nonstationary O-F mean differences that evolve at seasonal time  
85 scales.

86 There are typically large systematic differences between remotely sensed and modeled  
87  $T_{skin}$  (Ghent et al. 2010; Wang et al. 2014), and if not adequately addressed these differences  
88 will result in a sub-optimal assimilation, potentially leading to degraded flux forecasts (e.g.,  
89 Reichle et al. 2010). Hence, the two-stage observation bias and state estimation scheme has  
90 been demonstrated here by assimilating geostationary  $T_{skin}$  observations into the Catchment  
91 land surface model.

92 The remainder of this manuscript is outlined as follows. In Section 2, the two-stage  
93 observation bias and state estimation scheme is developed, and contrasted to observation  
94 rescaling approaches. The two-stage filter is then demonstrated with an example assimilation  
95 of remotely sensed skin temperature ( $T_{skin}$ ) observations into a land surface model. The  $T_{skin}$   
96 assimilation experiments are outlined in Section 3, before the results are presented in Section  
97 4. Finally, Section 5 presents a summary and conclusions.

## 98 **2. The state and bias filter equations**

99 The two-stage observation bias and state estimation approach introduced here is based  
100 on the on-line two-stage forecast bias and state estimation approach of Dee and Da Silva  
101 (1998), which has been successfully implemented in atmosphere (Dee and Todling 2000),  
102 ocean (Chepurin et al. 2005; Keppenne et al. 2005), and land (Bosilovich et al. 2007; De Lan-  
103 noy et al. 2007; Reichle et al. 2010) data assimilation. Following Friedland (1969), Dee and

104 Da Silva (1998) decouple the forecast bias estimation from the state update, and use a sep-  
105 arate Kalman filter to estimate the forecast bias. The (bias-blind) state update innovations  
106 (i.e., the O-F residuals) are used to measure the forecast bias for the bias update, based on  
107 the assumption that the observations are unbiased, and persistence is used to predict the  
108 forecast bias. Pauwels et al. (2013) recently extended the theory of the two-stage forecast bias  
109 and state estimation filter to also estimate the observation bias. In their approach, demon-  
110 strated with synthetic experiments, the (bias-blind) state update innovation measures the  
111 observation bias plus the forecast bias, and is partitioned into the two separate bias terms  
112 by calibration. However, observations of the true mean state are ultimately required to  
113 partition the sum of the biases.

114 In contrast, we derive the two stage filter as if to estimate the observation biases measured  
115 using the (bias-blind) state update innovations, based on the assumption that the forecasts  
116 are unbiased. However, in the intended land data assimilation applications, it is recognized  
117 that the forecasts are almost certainly biased, so that the estimated ‘observation bias’ really  
118 represents the O-F mean difference (the lumped observation-bias-minus-forecast-bias), to  
119 be used to adjust the observations to have the same mean value as the forecast estimates,  
120 consistent with observation rescaling approaches.

121 Below, the bias-free EnKF equations are reviewed (Section 2a), before the optimal so-  
122 lution for the two-stage observation bias and state estimation filter is derived (Section 2b).  
123 Then, a parameterization of the Kalman gain for the bias update is introduced, to avoid  
124 specifying the unknown prior observation bias uncertainty (Section 2c).

#### 125 *a. The bias-free EnKF*

126 The bias-free EnKF, as implemented by Reichle et al. (2013) for land data assimilation,  
127 consists of a model forecast step and a state update step. For the  $i$ th ensemble member, the  
128 state forecast and update at the  $k$ th assimilation time are:

$$x_{k,i}^- = f(x_{k-1,i}^+, q_{k,i}) \quad (1)$$

$$x_{k,i}^+ = x_{k,i}^- + K_k(y_{k,i}^o + H_k x_{k,i}^-) \quad (2)$$

$$y_{k,i}^o = y_k^o + v_{k,i} \quad (3)$$

130 where  $x$  is the model state vector,  $f(\cdot)$  is the forecast model,  $q$  represents the model error (or  
 131 perturbation vector),  $K$  is the Kalman gain matrix,  $y^o$  is the observation vector,  $H$  is the  
 132 observation operator, and  $v$  is an applied (zero mean, normal) perturbation representative of  
 133 the expected observation errors. For simplicity we assume  $H$  to be linear, however the theory  
 134 is unchanged if this assumption is relaxed. Throughout this manuscript, a super-scripted  
 135 state vector indicates an estimated value, with the  $-$  and  $+$  superscripts indicating the prior  
 136 and posterior estimates, respectively. In contrast, the absence of a superscript for a state  
 137 variable indicates the true state vector.

138 In a bias-free EnKF, the errors in  $x^-$  and  $y^o$  are assumed to have vanishing long-term  
 139 mean errors, and to be uncorrelated with each other. Under these assumptions,  $x^+$  provides  
 140 an unbiased estimate of  $x$ , and the optimal (minimum posterior state error variance) Kalman  
 141 gain for the  $k$ th state update,  $K_k$ , is given by:

142

$$K_k = P_k^{x-} H_k^T (R^o + H_k P_k^{x-} H_k^T)^{-1} \quad (4)$$

143 where  $P^{x-}$  is the prior model state error covariance matrix, and  $R^o$  is the observation error  
 144 covariance matrix.  $P^{x-}$  is diagnosed from the ensemble spread, while for land data assimilation  
 145  $R^o$  is typically assumed to be constant in time and have zero off-diagonal terms (e.g.,  
 146 Draper et al. 2012). Applying the above equations in the presence of (unknown) observation  
 147 and/or forecast biases is sub-optimal, and is referred to as ‘bias-blind’ data assimilation (Dee  
 148 and Da Silva 1998).

149 *b. The two-stage observation bias and state estimation*

150 For an observation-bias-aware assimilation, the observation vector is allowed to have a  
 151 nonzero mean error persisting over some extended time period (a bias). The biased obser-  
 152 vations, written  $\tilde{y}_k^o$ , can be partitioned into the bias term,  $b_k$ , and the remaining zero-mean  
 153 error component,  $y_k^o$ :

154

$$\tilde{y}_k^o = b_k + y_k^o \quad (5)$$

155 The observations are then bias-corrected within the state update (equation 2) to remove  
 156 the bias from the innovations, giving an unbiased estimate of  $x^+$ :

157

$$x_{k,i}^+ = x_{k,i}^- + \tilde{K}_k(\tilde{y}_{k,i}^o - b_k - H_k x_{k,i}^-) \quad (6)$$

158 where  $\tilde{K}$  is the Kalman gain for the state update based on the bias corrected observation  
 159 vector.

160 A separate, discrete Kalman filter is then used to estimate the observation bias. The  
 161 observation bias is measured using the mean O-F ( $\langle \tilde{y}_{k,i}^o - H_k x_{k,i}^- \rangle$ , where  $\langle . \rangle$  is the  
 162 ensemble mean). The bias is initialized at zero, and persistence is used as the bias prediction  
 163 model, since the bias is assumed not to change significantly during individual assimilation  
 164 cycles. The persistence model is recognized as an approximation, since a (potentially desir-  
 165 able) feature of the two-stage filter is the nonstationary nature of the bias estimates. The  
 166 observation bias forecast and update equations for the  $k$ th assimilation time are then written:

167

$$b_k^- = b_{k-1}^+ \quad (7)$$

$$b_k^+ = b_k^- + L_k \langle \tilde{y}_{k,i}^o - b_k^- - H_k x_{k,i}^- \rangle \quad (8)$$

168 where  $L_k$  is the Kalman gain for the bias update. Equations 7 and 8 provide an unbiased  
 169 estimate of the observation bias, regardless of the selection of  $L_k$ . Appendix A shows that if



170 the errors in the observations, the prior bias estimate, and the prior state estimate are not  
 171 correlated with each other, and if  $b_k^-$  provides an unbiased estimate of the observation bias,  
 172 the optimal (minimum error covariance) posterior bias estimate is obtained with  $L_k$  equal  
 173 to:

$$L_k = P_k^{b-} (R^o + P_k^{b-} + H_k P_k^{x-} H_k^T)^{-1} \quad (9)$$

175 Here  $R^o$  is unchanged from equation 4 and represents the random errors in the observations  
 176 only, while  $P_k^{b-}$  is the random error covariance matrix for the prior observation bias estimate.

177 Substituting the best estimate of the bias ( $b_k^+$ ; equation 8) into equation 6 then gives the  
 178 state update equation with observation bias correction:

$$x_{k,i}^+ = x_{k,i}^- + \tilde{K}_k (\tilde{y}_{k,i}^o - b_k^+ - H_k x_{k,i}^-) \quad (10)$$

180 Up to this point, the presented derivation of the two-stage observation bias and state  
 181 estimation equations has followed that of Pauwels et al. (2013), with their forecast bias set  
 182 to zero. However, we now diverge from their approach. In Appendix B, we show that if the  
 183 optimal expression for  $L$  is used (equation 9),  $\tilde{K}_k$  in equation 10 is the same as  $K_k$  for the  
 184 bias-free filter (equation 4). That is, the Kalman gain is unchanged by the inclusion of the  
 185 two-stage observation bias estimate in the state update equation. This result parallels that  
 186 of Dee and Todling (2000), who show that for the on-line two-stage forecast bias and state  
 187 estimation filter the state update Kalman gain is unchanged by the inclusion of the forecast  
 188 bias estimate in the state update equation.

189 To summarize the two-stage observation bias and state estimation filter equations pre-  
 190 sented above, equations 1 and 10 are used for the state forecast and update, respectively,  
 191 together with the state update Kalman gain of equation 4. Equations 7 and 8 are used  
 192 for the observation bias forecast and update, respectively, together with the bias update  
 193 Kalman gain of equation 9 (although equation 9 will be replaced by an empirical function in

194 Section c). For illustrative purposes, substituting equation 8 into equation 10, then taking  
 195 the ensemble average gives:

196

$$x_{k,i}^+ = x_{k,i}^- + \tilde{K}_k(\tilde{y}_{k,i}^o - b_k^- - H_k x_{k,i}^-) - \tilde{K}_k L_k \langle \tilde{y}_{k,i}^o - b_k^- - H_k x_{k,i}^- \rangle \quad (11)$$

197 and:

198

$$\langle x_{k,i}^+ \rangle = \langle x_{k,i}^- \rangle + \tilde{K}_k(I - L_k) \langle \tilde{y}_{k,i}^o - b_k^- - H_k x_{k,i}^- \rangle \quad (12)$$

199 Comparing equation 12 to equation 8 for the bias update demonstrates how the two-stage  
 200 filter partitions the innovations  $(\tilde{y}_{k,i}^o - b_k^- - H_k x_{k,i}^-)$  into updates to the bias estimate and  
 201 state estimate.

202 The presented two-stage observation bias and state estimation filter parallels the on-line  
 203 two-stage forecast bias and state estimation of Dee and Da Silva (1998) but differs from the  
 204 original two-stage estimation approach of Friedland (1969) in that the state update equation  
 205 is optimized with the bias correction terms included (i.e., the Kalman gain is obtained by  
 206 optimizing equation 10, rather than equation 2). The resulting two-stage filter is optimal if  
 207 the various assumptions stated above hold. However, in practice the filter is unlikely to be  
 208 optimal, since, for example, the prior state errors and the prior observation bias errors have  
 209 been assumed uncorrelated, yet both contain information (and errors) from past observations.

### 210 *c. Parametrization of the bias gain*

211 The two-stage observation bias correction and state estimation approach outlined above  
 212 requires the specification of the unknown error covariance matrix  $P^{b-}$  for the prior bias  
 213 estimate to calculate the observation bias update Kalman gain,  $L$ , in equation 9. Dee  
 214 and Da Silva (1998) and Pauwels et al. (2013) assumed that the prior forecast bias error  
 215 covariances were proportional to the prior forecast error covariances, and Pauwels et al.

216 (2013) assumed that the prior observation bias error covariances were proportional to the  
 217 forecast observation error covariances. We instead replace  $L$  with an empirical function.  
 218 This approach is made possible because  $P^{b-}$  is not required for the bias-aware state update  
 219 Kalman gain, due to the equivalence of the bias-free and bias-aware Kalman gains noted in  
 220 Section b.

221 For the assimilation of a single observation type at a single location,  $L_k$  becomes scalar.  
 222 For the assimilation of the  $j$ th location and observation type, we approximate  $L_{j,k}$  with a  
 223 function designed to approach one as the time since the last assimilated observation increases:

224

$$\lambda_{j,k} = 1 - e^{-\Delta t_{j,k}/\tau_j} \quad (13)$$

225 where  $\Delta t_{j,k}$  is the number of time steps since the most recent observation of type  $j$  was  
 226 assimilated, and  $\tau_j$  is a user-defined parameter representing the e-folding time scale of the  
 227 bias memory for observation type  $j$ . This function was chosen since it approximates the  
 228 expected behavior  $L_{j,k}$  under two important scenarios. In the first scenario, no observations  
 229 have been recently assimilated, relative to the assumed time scale of the bias, and there is  
 230 little information with which to predict  $b_{j,k}^-$ . Hence,  $L_{j,k}$  is expected to be close to one, as  
 231 predicted by equation 13 for large  $\Delta_{j,k}/\tau_j$ . In the second scenario, observations are being  
 232 assimilated with some regularity, and random errors in  $b_{j,k}^-$  will be dominated by random  
 233 errors in the  $(\tilde{y}_k^o - H_k x_k^-)$  sequence used to update  $b_{j,k}^-$  (since by definition the persistence  
 234 model will not introduce significant errors into the bias estimate), however, the bias filter  
 235 will gradually filter these errors over time. Hence, if  $\Delta t_{j,k}$  is assumed to generalize the recent  
 236 availability of observations, equation 13 will approximate the increased certainty in  $b_{j,k}^-$  (and  
 237 subsequent reduction in  $\lambda_{j,k}$ ) as more observations are assimilated.

238 The empirical  $\lambda_{j,k}$  must adequately account for the first scenario described above, of no  
 239 recent observations, since from equation 12 a large  $L_k$  is necessary in this case to prevent  
 240 the potentially large  $b_{j,k}^-$  errors from being propagated into the model state vector. This  
 241 situation can occur reasonably regularly, since there are often seasonal-scale gaps in land

242 surface observation records, when atmospheric and/or land surface conditions prevent remote  
243 sensing of the land surface. Note the contrast to forecast bias correction, for which one can  
244 fall back on a conservative approach of underestimating the forecast bias (Dee and Todling  
245 2000; Reichle et al. 2010) when the bias estimate is highly uncertain, since the model state  
246 will still be updated towards the true state (defined by the observations in this case).

247 For the assimilation of multiple observation types and locations,  $\lambda_{j,k}$  can be extended  
248 in the obvious way to a matrix,  $\Lambda_k$ , by setting the  $j$ th diagonal element of  $\Lambda_k$  to  $\lambda_{j,k}$ ,  
249 and setting the off-diagonal terms to zero (i.e, disregarding potential spatial correlation, or  
250 cross-correlation between observation types, in the bias updates). A potential weakness of  
251 the above parameterization of  $\lambda_{j,k}$  is that a  $b_{j,k}^-$  estimate based on a single recent observation  
252 would be assigned high confidence. Consequently, observations are excluded from the state  
253 update when the bias estimate is based on less than two observations within the last  $\tau_j/2$   
254 time steps (although these observations are still used to update  $b_{j,k}^-$ ).

#### 255 *d. Comparison to observation rescaling*

256 The two-stage observation bias and state estimation method presented above treats the  
257 systematic differences between observations and forecasts quite differently compared to the  
258 observation rescaling methods currently used in many land data assimilation systems. Ob-  
259 servation rescaling (Reichle and Koster 2004; Drusch et al. 2005; Scipal et al. 2008; Crow  
260 et al. 2011) is designed to remove the long-term systematic differences in the mean and  
261 variance (and possibly higher order moments) of the observed and forecast state estimates,  
262 where ‘long-term’ is defined by the length of the data record used to calculate the rescal-  
263 ing parameters. These systematic differences are typically assumed to be stationary, and a  
264 static set of bias correction parameters is used. Consequently, a (bias-free) data assimilation  
265 with observation rescaling will then adjust the model states to reduce residual differences  
266 between the observations and model forecasts. Such differences include those occurring at  
267 sub-seasonal time-scales, differences in the phase of the seasonal cycle, and also differences in

268 the intra-annual seasonal cycle, if the data record used to estimate the rescaling coefficients  
269 was sufficiently long to sample the climatological inter-annual variability.

270 In contrast, the two-stage observation bias and state estimation method presented here  
271 is designed to remove only the systematic difference in the mean of the observed and fore-  
272 cast state estimates, and this mean difference is not restricted to being stationary. The  
273 filter dynamically estimates the O-F mean differences based only on measurements up to the  
274 current assimilation cycle, with greater weight placed on more recent measurements. The  
275 resulting estimates are then nonstationary, and will evolve at a time scale determined by  
276 the  $\tau$  parameter in equation 13. Specifying  $\tau$  to represent seasonal time scales will result in  
277 the observations being adjusted to match the seasonal cycle of the forecast estimates. The  
278 assimilation will then adjust the model state vector to reduce differences between the obser-  
279 vations and forecasts at sub-seasonal time scales, somewhat consistent with the observation  
280 rescaling approach. Although systematic differences in the variance of the observations and  
281 forecasts are not explicitly removed, as they are in observation rescaling, the component of  
282 variance due to seasonal, or longer, time scale dynamics will be addressed.

283 For a given data assimilation experiment, the suitability of the two-stage filter depends  
284 on the distribution of the systematic differences between the observed and forecast esti-  
285 mates. For  $T_{skin}$ , there can be large differences between the mean values of different model  
286 forecast and observed estimates (Wang et al. 2014), however  $T_{skin}$  variability is reasonably  
287 well constrained, due in part to the tight coupling between  $T_{skin}$  and the (comparatively well  
288 observed) low-level atmospheric temperature. Hence, using the two-stage observation bias  
289 and state estimation to adjust the seasonal cycle of the mean observed  $T_{skin}$  to match that  
290 of the forecast estimates is expected to effectively address the systematic differences between  
291 observed and forecast  $T_{skin}$  in an assimilation. However, for many other land surface vari-  
292 ables this approach may not be sufficient. Most notably, for near-surface soil moisture there  
293 are large systematic differences between the variability of different data sets, including the  
294 sub-seasonal-scale variability (e.g., see Draper et al. (2013), their Figure 2). This is due in

295 part to the absence of global data sets constraining the possible soil moisture range, and  
296 the subsequent uncertainty in the parameters controlling the soil moisture response to at-  
297 mospheric forcing (specifically controlling the total volume of pore space available for water  
298 storage in the soil column).

### 299 **3. Skin temperature assimilation**

300 The two-stage observation bias and state estimation scheme has been demonstrated by  
301 assimilating geostationary  $T_{skin}$  observations into the Catchment land surface model. Two  
302 separate assimilation experiments were performed. First, the  $T_{skin}$  data were assimilated  
303 over the Americas at  $0.3125^\circ \times 0.25^\circ$  longitude by latitude resolution, from 1 June, 2012 to  
304 31 May, 2013. Second, to obtain example global maps of the mean differences between the  
305 observed and forecast  $T_{skin}$ , the  $T_{skin}$  data were assimilated globally, at a coarser resolution  
306 of  $0.625^\circ \times 0.50^\circ$ , from 1 May, to 1 August, 2012.

#### 307 *a. Catchment land surface model*

308 Catchment (Koster et al. 2000) is the land surface modeling component of the Goddard  
309 Earth Observing System Model, version 5 (GEOS-5; Rienecker et al. 2008). The catchment  
310 model equivalent variable to remotely sensed  $T_{skin}$  is the surface temperature ( $T_{surf}$ ), defined  
311 as the average temperature of the canopy and soil surface, and representative of an arbitrarily  
312 thin layer separating the canopy and soil surface from the atmosphere. While the Catchment  
313  $T_{surf}$  is prognostic, it has a very short memory over most land surface types due to its very  
314 low surface specific heat capacity ( $200 \text{ JK}^{-1}\text{m}^{-2}$ , except for broadleaf evergreen vegetation).  
315 The assimilation experiments were performed off-line (i.e., decoupled from the atmospheric  
316 model), using meteorological forcing data from the NASA Modern-Era Retrospective analysis  
317 for Research and Applications (MERRA) (Rienecker et al. 2011) and Catchment model  
318 parameters from the routine GEOS-5 system. The initial land surface state was spun-up

319 from an archived GEOS-5 restart file on 1 January, 2000, by integrating the model forward  
320 (without perturbations) to 1 January 2012, and the model ensemble was then spun up from  
321 1 January, 2012 to the start of the assimilation on 1 June, 2012.

322 *b. Geostationary skin temperature data*

323 The assimilated  $T_{skin}$  observations are retrieved from geostationary Thermal Infrared  
324 (TIR) brightness temperature observations at the NASA Langley Research Center (Scarino  
325 et al. 2013). The  $T_{skin}$  data are retrieved every three hours, and reported on the  $0.3125^\circ \times 0.25^\circ$   
326 GEOS-5 model grid. The geostationary data have been produced in near-real time since  
327 2011, from a constellation of satellites providing global ( $53^\circ$  S to  $53^\circ$  N, after quality con-  
328 trol) coverage: Geostationary Operational Environmental Satellites (GOES)-East, GOES-  
329 West, the second Multifunctional Transport Satellite (MTSAT-2), Feng Yun-2E (FY-2E),  
330 and Meteosat-9 (Met-9). However, for the assimilation experiment over the Americas do-  
331 main, an updated data set from the GOES-East and GOES-West satellites, produced with  
332 the latest retrieval model, has been used. Where observations are available from more than  
333 one geostationary satellite, only the observations from the closest satellite were assimilated.  
334 The observation quality control discards observations with a viewing zenith angle greater  
335 than  $60^\circ$ , a solar zenith angle between  $83^\circ$  and  $90^\circ$ , a grid-cell cloud fraction above 20%, or  
336 if the land modeling system indicates precipitation or a snow-covered surface.

337 Figure 1 shows the coverage of the observation-quality controlled (GOES-West and  
338 GOES-East)  $T_{skin}$  observations assimilated in the Americas experiment, as a fraction of  
339 the total number of possible observation times (eight 3-hourly observation times per day).  
340 There are few observations available during colder periods, due mostly to increased cloudi-  
341 ness. Hence, the coverage is very low ( $< 15\%$  of the maximum possible coverage) at higher  
342 latitudes. The coverage is also low over the Amazon, again due to cloudiness. There is some  
343 diurnal variation in the coverage, with slightly more observations available during the day-  
344 time hours (10% more than nighttime). In Section 4 evaluation statistics are only reported

345 at locations where observations were assimilated for at least 7.5% of the possible observation  
346 times at each time of day ( $\sim 30$  observations).

347 *c. Assimilation system*

348 The state update component of the two-stage filter uses the EnKF (Reichle et al. 2013),  
349 with 12 ensemble members and 3-hourly assimilation of the  $T_{skin}$  observations. The assimila-  
350 tion update vector consists of  $T_{surf}$  and the ground heat content (GHT1) associated with  
351 the near-surface (0-10 cm) soil temperature. The ensemble was generated using the forcing  
352 and model state perturbations in Table 1, which were adapted from Reichle et al. (2010)  
353 to account for the inclusion of GHT1 in the state update vector. Note that the Catchment  
354 model version used in Reichle et al. (2010) had a much higher specific heat capacity for  $T_{surf}$   
355 ( $70,000 \text{ JK}^{-1}\text{m}^{-2}$ ) than is currently used, and  $T_{surf}$  represented a 5 cm layer depth (hence  
356 Reichle et al. (2010) updated only  $T_{surf}$ ). The observation error standard deviations for the  
357  $T_{skin}$  retrievals were set at 1.3 K and 2.1 K during the nighttime and daytime, respectively,  
358 which implies that the model and observations have roughly similar skill.

359 The Catchment model divides each model grid cell into multiple computational elements,  
360 and a 3-D filter (with non-zero horizontal model and observation error correlations, Reichle  
361 and Koster 2003) was used to spread the observations to all model computational surface  
362 elements within each grid cell. For both the observation errors and the (forcing and state  
363 vector) ensemble perturbations in Table 1, relatively short horizontal error correlation scales  
364 with an e-folding distance of  $0.17^\circ$  were applied. Note that preliminary experiments with  
365 increased horizontal error correlation scales (between  $0.5^\circ$  and  $1.0^\circ$ ) degraded the assimila-  
366 tion results, likely because the strong dependence on cloud cover limits the horizontal error  
367 correlations of estimated  $T_{skin}$ .

368 The observation bias update was performed independently at each model grid cell (i.e.,  
369 using a 1-D filter). Since there is a strong diurnal cycle in the observations-minus-forecast  
370 mean difference (as will be shown in Section 4), the observation bias was modeled separately



371 at each of the eight diurnal observation times, following Reichle et al. (2010).

372 *d. Evaluation of assimilation output*

373 The results of the assimilation experiment over the Americas have been evaluated by  
374 comparison to independent observations of clear sky  $T_{skin}$ , from the in situ SURFRAD net-  
375 work (Augustine et al. 2005), and from remotely sensed MODIS TIR observations. The six  
376 SURFRAD sites shown in Figure 1 were used (Fort Peck was excluded since the geostation-  
377 ary satellite viewing zenith angle exceeds  $60^\circ$  there). For each of the validation sites, 3-hourly  
378  $T_{skin}$  were calculated from the SURFRAD up-welling and down-welling TIR radiation ob-  
379 servations using the Stefan-Boltzmann equation, and broad-band emissivity calculated from  
380 MODIS Terra monthly narrow-band emissivity observations (MOD11C3), using Wang et al.  
381 (2005). For MODIS, Aqua (MYD11C1) and Terra (MOD11C1) daily clear-sky  $T_{skin}$  data  
382 on the  $0.05^\circ$  Climate Modeling Grid have been averaged up to the GEOS-5 model grid,  
383 and assumed to occur at the geostationary observation time closest to the median MODIS  
384 observation time over the domain for each satellite orbit direction.

385 The skill of the  $T_{skin}$  assimilation experiment in predicting each of the independent data  
386 sets has been compared to the skill of an open-loop (no data assimilation) ensemble, gener-  
387 ated with the same model perturbations as used for the assimilation experiment. For both  
388 cases, instantaneous model  $T_{surf}$  is compared to the independent  $T_{skin}$  observations at times  
389 for which geostationary  $T_{skin}$  observations are available (i.e., for the assimilation experiment  
390 the posterior  $T_{surf}$  is evaluated). There are systematic differences between the mean values  
391 of the  $T_{skin}$  data sets used here, and these differences cannot be attributed to biases in any  
392 particular data set. Hence, the evaluation statistic is the unbiased Root Mean Square Dif-  
393 ference (ubRMSD), calculated at each model grid cell after removing the mean difference  
394 over the full time period (separately at each time of day) between the data sets.

## 4. Results

### a. O-F mean differences

Without bias correction there is a strong diurnal cycle in the mean difference between the observed and forecast  $T_{skin}$ . For example, Figure 2 shows the diurnal cycle in the spatial mean O-F mean difference over the Americas for a bias-blind assimilation of the GOES-East and GOES-West geostationary  $T_{skin}$  observations (using the same observation error covariances and forecast ensemble perturbations as for the bias-aware assimilation experiments). For both GOES-East and GOES-West, the O-F mean differences are more positive after solar noon. The GOES-West O-F mean differences are consistently positive, and larger than those for GOES-East throughout the diurnal cycle, with a maximum value of 5.1 K at 21:00 UTC, compared to values  $< 2$  K during the nighttime. In contrast, the GOES-East O-F mean differences are negative during the nighttime, and positive during the daytime, but with magnitude consistently  $< 1$  K in both cases, except for the 2.8 K maximum at 18:00 UTC. The  $T_{skin}$  data retrieved from the different geostationary satellite are reasonably well calibrated (Minnis et al. 2002), and the differences between the GOES-East and GOES-West O-F mean differences in Figure 2 are almost certainly not related to the sensors themselves, but to the contrasting land covers observed by each. The small spatial mean O-F mean differences for GOES-East are due to cancellation between regions of positive and negative O-F mean differences in the spatial means.

While the effectiveness of the observation bias correction has been analyzed throughout the diurnal cycle, for brevity the focus here is on the results at 21:00 UTC, when the largest O-F mean differences occurred in Figure 2. To demonstrate the influence of  $\tau$  (the time scale of the bias estimate) on the O-F mean differences estimated by the filter (i.e., the  $b^+$ ), Figure 3 compares the  $b^+$  time series at 21:00 UTC, estimated using  $\tau$  values between 10 and 30 days, at the three SURFRAD locations with the greatest observation coverage. The SURFRAD locations are used only for convenience, and no SURFRAD data were used in these plots.

421 For comparison, each panel also includes a smoothed O-F time series, estimated using the  
 422 first two annual Fourier harmonics, following Vinnikov et al. (2008). Recall from Section 2d,  
 423 that selecting  $\tau$  to represent seasonal time scales will allow the assimilation to correct for  
 424 sub-seasonal-scale (e.g., synoptic-scale) errors. The bias filter tracks the expected seasonal-  
 425 scale O-F mean differences, while filtering out the higher-frequency noise in the observed and  
 426 forecast  $T_{skin}$ . As expected, the filtered  $b^+$  time series lag the smoothed time series, with the  
 427 lag increasing as  $\tau$  increases in Figure 3. The minimum time scale of the features resolved by  
 428 the  $b^+$  time series also increases as  $\tau$  increases, and for shorter  $\tau$  values there is more noise  
 429 around the seasonal cycle (particularly for 10 days). The greatest differences between the  $b^+$   
 430 time series with different  $\tau$  (and between the filtered and smoothed time series) occurred at  
 431 Sioux Falls, where the O-F seasonal cycle had the steepest temporal gradient. In particular,  
 432 during the 2012 summer when the O-F decreased rapidly, the  $b^+$  time series are much higher  
 433 than the smoothed time series (likely due to the first two Fourier harmonics in the smoothed  
 434 time series being insufficient to capture the sharp gradient).

435 For a given application the best choice of  $\tau$  for estimating the seasonal-scale O-F mean  
 436 differences will depend on the relative variability of the innovations at seasonal and sub-  
 437 seasonal time scales. For geostationary  $T_{skin}$  assimilation, a compromise value of  $\tau = 20$   
 438 days has been selected, since this produced  $b^+$  time series with reasonably smooth seasonal  
 439 cycles that did not lag the O-F time series by too much (Figure 3).

440 With a  $\tau$  of 20 days, Figure 4 compares histograms of the state update innovations at  
 441 21:00 UTC at the same three locations plotted in Figure 3, for both the bias-blind assim-  
 442 ilation experiments and the two-stage observation bias and state estimation scheme. As  
 443 expected, the innovation distributions for the bias-blind assimilation are biased, with mean  
 444 values between 1.3 K and 8.0 K (Figures 4a-c). The inclusion of the observation bias correc-  
 445 tion reduced the mean innovations to magnitudes less than 0.5 K at each location (Figures  
 446 4d-f). The observation bias correction also changed the shape of the innovation distributions  
 447 in Figure 4, reducing their spread and skew. Consequently, the standard deviation at each

448 site is reduced, with the greatest reductions occurring at Sioux Falls, from 4.0 K for the  
449 bias-blind assimilation to 2.5 K with the observation bias correction. The altered shape of  
450 the innovation distribution is a consequence of the nonstationary bias estimation method  
451 accounting for seasonal-scale evolution of the O-F mean difference. In contrast, if a single  
452 (stationary) correction were applied to the mean over the full time period, the higher order  
453 moments of the innovation distribution would have been unchanged.

454 The histograms in Figure 4 are representative of the performance of the observation bias  
455 correction across the full domain, and throughout the diurnal cycle. For example, for both  
456 satellites in Figure 2, the two-stage filter reduced the spatial mean O-F mean difference to  
457 magnitudes between 0.0 - 0.3 K throughout the day, compared to bias-blind maxima of 5.1  
458 K and 2.8 K, for GOES-West and GOES-East, respectively. Likewise the mean standard  
459 deviation of the innovations across the domain was also reduced throughout the diurnal cycle  
460 (not shown), for example from 3.8 K to 3.1 K for GOES-West, and from 2.7 K to 2.1 K for  
461 GOES-East, both at 21:00 UTC.

462 Finally, in Section 2d it was hypothesized that for the assimilation of  $T_{skin}$ , the vari-  
463 ability of modeled and observed estimates is reasonably well constrained so that adjusting  
464 the mean seasonal cycle of the observations (with the two-stage filter) would be sufficient  
465 to address the systematic differences between the observed and forecast estimates. Compar-  
466 ing the variance of the observed and forecast  $T_{skin}$  confirms that this was the case in the  
467 assimilation experiments performed here. For example, over the Americas at 21:00 UTC,  
468 the spatially averaged temporal standard deviation of the GOES-West observations was 8.0  
469 K, compared to 7.3 K for the model forecasts over the same domain, with a spatial mean  
470 absolute difference between their standard deviations of 1.1 K. Likewise, for GOES-East at  
471 21:00 UTC the mean standard deviation was 5.1 K, compared to 4.9 K for the forecasts,  
472 with a spatial mean absolute difference of 0.9 K. The two-stage observation bias correction  
473 reduced the differences in the variance, and the ‘bias corrected’ observations had spatially  
474 averaged standard deviations very close to the model forecasts, of 7.6 K for GOES-West,

475 with a spatial mean absolute difference of just 0.4 K, and of 5.1 K for GOES-East, giving a  
476 spatial mean absolute difference of 0.3 K.

477 *b. Global O-F mean difference maps*

478 Figure 5 shows maps of the estimated  $b^+$  at 9:00 UTC on June 1, July 1, and August 1,  
479 2012. There is substantial spatial variation in the  $b^+$ , with a clear signal of land surface con-  
480 ditions. There are no obvious discontinuities between the  $b^+$  estimated for adjacent satellites  
481 in Figure 5, although the limited regions of overlapping observations from neighboring satel-  
482 lites (at sufficiently small viewing angles) makes the direct assessment of such discontinuities  
483 difficult. At 9:00 UTC it is daytime over Africa and Europe, and this region has the largest  
484 estimated  $b^+$  in Figure 5, with distinct regions of large positive values ( $> 10$  K) in the drier  
485 regions of Africa, the Arabian peninsula, and western Asia, with a band of negative values  
486 ( $< -5$  K) over equatorial Africa. In contrast, the regions experiencing nighttime generally  
487 have smaller  $b^+$  (magnitude  $< 5$  K), except for the drier regions of western North America  
488 and Australia, with mean differences of 5-10 K. This tendency for very large positive day-  
489 time  $b^+$  over dry regions occurs consistently across the globe, particularly in the summer  
490 hemisphere; the same pattern was evident in Figure 2 for GOES-West, which observes the  
491 arid southwest of the US. In terms of the temporal evolution of the  $b^+$ , the large-scale spatial  
492 patterns are consistent between the three months plotted in Figure 5, although the gradual  
493 evolution of the  $b^+$  estimates is evident.

494 *c. Evaluation against independent  $T_{skin}$  observations*

495 Figures 6 and 7 demonstrate that the two-stage observation bias and state estimation  
496 filter improved the modeled  $T_{surf}$  sub-seasonal-scale variability, compared to independent  
497 observations, albeit by a modest amount. In Figure 6 the mean ubRMSD of the assimilation  
498 estimates versus SURFRAD observations is reduced at each time of day by between 0.05 K

499 - 0.31 K ( $\sim 5\text{-}10\%$ ), with the greatest improvements ( $>0.2$  K) occurring during the first half  
500 of the day (09:00-15:00 UTC). The ubRMSD across all times of day is significantly reduced  
501 (at a 5% level) from 2.1 K to 1.9 K.

502 Similar results were obtained by comparison to Terra and Aqua MODIS  $T_{skin}$  observations  
503 over the Americas, as shown in Figure 7. During the night, the open-loop ubRMSD was  
504 already very small, with a spatial mean of 1.9 K for both Terra and Aqua. During the  
505 day, the open-loop ubRMSD was much larger, except over the Amazon, with a spatial mean  
506 of 3.6 K for both Terra and Aqua. For all MODIS overpasses, the assimilation consistently  
507 improved the model fit to the MODIS data across the domain, except over the Amazon where  
508 the open-loop ubRMSD was already very low and the improvement from the assimilation  
509 was weaker, and even slightly negative in places. While the consistency of the positive  
510 improvements in Figure 7 is encouraging, these improvements were significant (at the 5%  
511 level) over only a small fraction ( $<10\%$ ) of the domain. For each MODIS orbit direction  
512 the spatial mean ubRMSD across the domain is shown in Table 2, and in each case the  
513 assimilation reduced the spatial mean ubRMSD by around 10% of the open-loop value, with  
514 ubRMSD reductions of 0.1 - 0.2 K during the nighttime, and 0.2-0.3 K during the daytime.

515 While the above evaluation consistently indicates that the  $T_{skin}$  assimilation has improved  
516 the model  $T_{surf}$ , the improvements are rather modest. This is despite the use of only  
517 assimilation update times in the evaluation, which will have exaggerated the assimilation  
518 impact. There are several reasons for the modest results. Most importantly, the skill of the  
519 model  $T_{surf}$ , in terms of the anomaly behavior assessed here, is already very good. Also, the  
520 Catchment model  $T_{surf}$  has an extremely short memory, associated with its very low heat  
521 capacity, hence the analysis updates do not persist into the subsequent model time step, and  
522 the model has very little memory of improvements previously gained from the assimilation.  
523 Including GHT1 in the state update vector did not increase the  $T_{surf}$  memory of previous  
524 analysis updates, since the  $T_{surf}$  dynamics are dominated by the radiation budget. Finally,  
525 the lack of memory is compounded by the low data volume associated with the lack of

526 TIR observations under cloudy conditions. The modest impact of the assimilation is not  
527 related to the observation bias correction method, since similar results were obtained using  
528 cumulative distribution functions (Reichle and Koster 2004) to rescale the observations (not  
529 shown).

## 530 5. Summary and conclusions

531 A two-stage observation bias and state estimation scheme has been developed for use in  
532 land data assimilation. In this scheme, the observation-minus-forecast (O-F) mean differ-  
533 ences are estimated and removed from the innovations prior to updating the model state.  
534 In applications where the model predictions are bias-free, the two-stage filter could also be  
535 used to correct the observations towards the true mean state. The presented method is com-  
536 putationally affordable, straightforward to implement in an existing assimilation, requires  
537 specification of only a single additional parameter, and can be used to assimilate satellite  
538 radiances or retrieved geophysical variables. In contrast to the observation rescaling meth-  
539 ods currently used in land data assimilation systems, the two-stage filter does not require  
540 a long data record. Hence, it has the potential to facilitate the use and success of land  
541 data assimilation, particularly in atmospheric modeling systems for which long records of  
542 consistently forecast land surface estimates are typically not available.

543 The two-stage filter includes a parameterization of the Kalman gain for the bias update  
544 that introduces an explicit specification of the time scale of the O-F mean differences. Defin-  
545 ing the O-F mean difference over seasonal time scales allows the assimilation to update the  
546 model state vector in response to sub-seasonal-scale (e.g., synoptic scale) differences between  
547 observed and forecast estimates.

548 In experiments assimilating geostationary  $T_{skin}$  observations into the Catchment land  
549 surface model, the two-stage filter effectively removed the O-F mean difference from the  
550 observations, and consequently improved synoptic-scale dynamics in the model  $T_{surf}$  (the

551 model equivalent variable to  $T_{skin}$ ). These improvements were measured using the ubRMSD  
552 with independent estimates of  $T_{skin}$  from the SURFRAD network (at six sites in the US),  
553 and from MODIS satellite observations over the Americas. While modest, the improvements  
554 highlight the potential value of the geostationary  $T_{skin}$  for future modeling efforts.

555 Global maps of the O-F mean differences estimated by the two-stage filter show clear  
556 spatial coherence, with a signal of local land surface conditions. Most prominently, there  
557 is a strong tendency for large positive O-F differences in dry regions during the daytime.  
558 In this study, the O-F mean difference was estimated independently at each model grid  
559 cell. However, the spatial cohesion of the estimates suggests the potential to improve the  
560 two-stage filter design by incorporating horizontal information into the observation bias  
561 estimates. This could be achieved by either including spatial smoothing in the bias forecast  
562 model (assuming correlations between the O-F mean difference in adjacent areas), or by  
563 implementing the bias update using a 3-D filter (assuming correlations between the errors  
564 in the O-F mean difference estimates).

565 In addition to the difficulty of obtaining suitable data records for observation rescaling,  
566 several studies have highlighted other shortcomings arising from the stationary nature of the  
567 observation rescaling approaches for bias correction. For example, the inability of a station-  
568 ary approach (CDF-matching) to distinguish between near-surface soil moisture variability  
569 over seasonal and sub-seasonal time scales can result in inadequate matching of the seasonal  
570 cycles between forecast estimates and CDF-matched observations (Draper et al. 2009). Also  
571 Drusch et al. (2005) argues that uncertainty in the inter-annual variability of the vegetation  
572 characteristics used in both soil moisture retrieval and land surface modeling may necessi-  
573 tate nonstationary observation bias correction methods, based on either frequent updates of  
574 observation rescaling coefficients, or the use of more sophisticated methods. More recently,  
575 Crow et al. (2011) showed that results from the assimilation of remotely sensed soil moisture  
576 into a simple water balance model were improved by using seasonally variable observation  
577 rescaling coefficients for adjusting the mean. The nonstationary nature of filtering may also



578 have practical advantages for the estimation of O-F mean differences, in that the estimates  
579 can respond to step changes, caused for example, by changes in the forecast model, remote  
580 sensor, or retrieval model. Hence, in atmospheric assimilation the ability of variational ob-  
581 servation bias correction schemes to respond to temporal changes in the bias has proven  
582 beneficial (Auligné et al. 2007; Dee and Uppala 2009).

583 Unlike observation rescaling, the two-stage filter presented here does not explicitly ad-  
584 dress systematic differences between higher-order moments of the observations and the model  
585 estimates. For the  $T_{skin}$  assimilation experiments presented here, the two-stage filter proved  
586 sufficient. However, other land surface variables, including near-surface soil moisture, can  
587 have large systematic differences in the sub-seasonal-scale variability of observed and forecast  
588 estimates. Work is underway to expand the two-stage filter to also account for systematic dif-  
589 ferences in the higher order moments, thus providing an alternative to observation rescaling  
590 for soil moisture data assimilation.

591 *Acknowledgments.*

592 The research was supported by the NASA Modeling, Analysis, and Prediction program,  
593 the NASA High-End Computing program, and the NASA Satellite Calibration Interconsis-  
594 tency program. MODIS land surface data were provided by NASA’s Earth Observing System  
595 Data and Information System, and the SURFRAD data were provided by the NOAA Earth  
596 System Research Laboratory.

# APPENDIX

597

598

599

## Appendix A. Derivation of $L_k$ .

600

601

602

603

604

605

606

607

In the bias state update equation (equation 8), the model state, observation bias, and observation estimates can each be partitioned into their true value, a random (zero-mean) error, and for the observations a long term mean error (bias):  $x_k^- = x_k + e^{x-}$ , and  $b_k^- = b_k + e^{b-}$ , and  $\tilde{y}_k^o = \tilde{y}_k + e_k^o = y_k + b_k + e_k^o$ , where  $e$  represents the random error in the superscripted variable. To derive  $L_k$ , minimize the expected error in  $b_k^+$ ,  $P_k^{b+} = E[e^{b+}(e^{b+})^T]$ , where  $E$  is the expectation over time. Substituting equation 8 into  $P_k^{b+}$ , then partitioning each variable into its constituent parts gives:

$$P_k^{b+} = E[(b_k^+ - b_k)(b_k^+ - b_k)^T] \quad (\text{A1})$$

$$= E[(b_k^- + L_k < \tilde{y}_k^o - b_k^- - H_k x_k^- > - b_k)(b_k^- + L_k < \tilde{y}_k^o - b_k^- - H_k x_k^- > - b_k)^T] \quad (\text{A2})$$

$$= E[(e_k^{b-} + L_k < e_k^o - e_k^{b-} - H_k e_k^{x-} >)(e_k^{b-} + L_k < e_k^o - e_k^{b-} - H_k e_k^{x-} >)^T] \quad (\text{A3})$$

608

The derivative of  $P_k^{b+}$  w.r.t  $L_k$  is:

609

$$\frac{\delta P_k^{b+}}{\delta L_k} = 2E[(e_k^{b-} + L_k < e_k^o - e_k^{b-} - H_k e_k^{x-} >)(< e_k^o - e_k^{b-} - H_k e_k^{x-} >)^T] \quad (\text{A4})$$

610

Setting the derivative to zero, and solving for  $L$ , gives the  $P_k^{b+}$  minimum:

611

$$L_k = E[-e_k^{b-} (< e_k^o - e_k^{b-} - H_k e_k^{x-} >)^T (< e_k^o - e_k^{b-} - H_k e_k^{x-} > (< e_k^o - e_k^{b-} - H_k e_k^{x-} >)^T)^{-1}] \quad (\text{A5})$$

612

If  $e_k^o$ ,  $e_k^{b-}$ , and  $e_k^{x-}$  are not cross-correlated with each other, the expectation is:

$$L_k = P_k^{b-} (R^o + P_k^{b-} + H_k P_k^{x-} H_k^T)^{-1} \quad (\text{A6})$$

## 615 Appendix B. Derivation of $\tilde{K}$ , and equivalence to $K$ .

616 To derive  $\tilde{K}$  minimize the expected error  $x_{k,i}^+$ ,  $P_k^{x+} = E[(e_k^{x+})(e_k^{x+})^T]$ . Substituting  
 617 equation 11 into  $P_k^{x+}$ , and as in Appendix A, partitioning each variable into its constituent  
 618 terms, gives:

$$P_k^{x+} = E[(x_k^+ - x_k)(x_k^+ - x_k)^T] \quad (\text{A7})$$

$$\begin{aligned} &= E[(x_k^- + \tilde{K}_k(\tilde{y}_k^o - b_k^- - H_k x_k^-) - \tilde{K}_k L_k \langle \tilde{y}_k^o - b_k^- - H_k x_k^- \rangle - x_k) \\ &\quad (x_k^- + \tilde{K}_k(\tilde{y}_k^o - b_k^- - H_k x_k^-) - \tilde{K}_k L_k \langle \tilde{y}_k^o - b_k^- - H_k x_k^- \rangle - x_k)^T] \end{aligned} \quad (\text{A8})$$

$$\begin{aligned} &= E[(e_k^{x-} + \tilde{K}_k(e_k^o - e_k^{b-} - H_k e_k^{x-}) - \tilde{K}_k L_k \langle e_k^o - e_k^{b-} - H_k e_k^{x-} \rangle) \\ &\quad (e_k^{x-} + \tilde{K}_k(e_k^o - e_k^{b-} - H_k e_k^{x-}) - \tilde{K}_k L_k \langle e_k^o - e_k^{b-} - H_k e_k^{x-} \rangle)^T] \end{aligned} \quad (\text{A9})$$

620 The derivative of  $P_k^{x+}$  w.r.t  $\tilde{K}_k$  is:

$$\begin{aligned} \frac{\delta P_k^{x+}}{\delta \tilde{K}_k} &= 2E[(e_k^{x-} + \tilde{K}_k(e_k^o - e_k^{b-} - H_k e_k^{x-}) - \tilde{K}_k L_k \langle e_k^o - e_k^{b-} - H_k e_k^{x-} \rangle) \\ &\quad (e_k^o - e_k^{b-} - H_k e_k^{x-} - L_k \langle e_k^o - e_k^{b-} - H_k e_k^{x-} \rangle)^T] \end{aligned} \quad (\text{A10})$$

622 If  $e^o$ ,  $e^{x-}$ , and  $e^{b-}$  are not cross-correlated with each other, setting the derivatives to zero  
 623 to minimize  $P_k^{x+}$ , and taking the expectation gives:

$$\tilde{K}_k (I - L_k) = P_k^{x-} H_k^T (R^o + P_k^{b-} + H_k P_k^{x-} H_k^T)^{-1} \quad (\text{A11})$$

625 Substituting equation 9 into A11 gives:

626

$$\tilde{K}_k(I - P_k^{b-}(R^o + P_k^{b-} + H_k P_k^{x-} H_k^T)^{-1}) = P_k^{x-} H_k^T (R^o + P_k^{b-} + H_k P_k^{x-} H_k^T)^{-1} \quad (\text{A12})$$

$$\tilde{K}_k(R^o + P_k^{b-} + H_k P_k^{x-} H_k^T - P_k^{b-}) = P_k^{x-} H_k^T \quad (\text{A13})$$

$$\tilde{K} = P_k^{x-} H_k^T (R^o + H_k P_k^{x-} H_k^T)^{-1} \quad (\text{A14})$$

627 which is the same as equation 4 for the Kalman gain for the bias-free EnKF state update.

628 This demonstrates that the inclusion of the observation bias estimate from the two-stage

629 state and bias estimation does not change the expression of the solution for the Kalman gain

630 for the state update in equation 10 (assuming that equation 9 is used for  $L_k$ ).

## REFERENCES

- 633 Augustine, J., G. Hodges, C. Cornwall, J. Michalsky, and C. Medina, 2005: An up-  
634 date on SURFRAD: The GCOS Surface Radiation Budget Network for the continen-  
635 tal United States. *Journal of Atmospheric Oceanic Technology*, **22**, 1460–1472, doi:  
636 10.1175/JTECH1806.1.
- 637 Auligné, T., A. McNally, and D. Dee, 2007: Adaptive bias correction for satellite data  
638 in a numerical weather prediction system. *Q. J. R. Meteorol. Soc.*, **133**, 631–642, doi:  
639 10.1002/qj.56.
- 640 Bosilovich, M., J. Radakovich, A. da Silva, R. Todling, and F. Verter, 2007: Skin tempera-  
641 ture analysis and bias correction in a coupled land-atmosphere data assimilation system.  
642 *Journal of the Meteorological Society of Japan*, **85A**, 205–228, doi:10.2151/jmsj.85A.205.
- 643 Chepurin, G., J. Carton, and D. Dee, 2005: Forecast model bias correction in ocean data  
644 assimilation. *Mon. Wea. Rev.*, **133**, 1328–1342, doi:10.1175/MWR2920.1.
- 645 Crow, W., M. van den Berg, G. Huffman, and T. Pellarin, 2011: Correcting rainfall using  
646 satellite-based surface soil moisture retrievals: The Soil Moisture Analysis Rainfall Tool  
647 (SMART). *Water Resources Research*, **47**, W08 521, doi:10.1029/2011WR010576.
- 648 Crow, W., et al., 2012: Upscaling sparse ground-based soil moisture observations for the  
649 validation of coarse-resolution satellite soil moisture products. *Reviews of Geophysics*, **50**,  
650 RG2002, doi:10.1029/2011RG000372.
- 651 De Lannoy, G., R. Reichle, K. Arsenault, P. Houser, S. Kumar, N. Verhoest, and V. Pauwels,  
652 2012: Multi-scale assimilation of AMSR-E snow water equivalent and MODIS snow cover  
653 fraction in northern Colorado. *Water Resources Research*, **48**, W01 522.

- 654 De Lannoy, G., R. Reichle, P. Houser, V. Pauwels, and N. Verhoest, 2007: Correcting  
655 for forecast bias in soil moisture assimilation with the ensemble Kalman filter. *Water*  
656 *Resources Research*, **43**, W09 410, doi:10.1029/2006WR005449.
- 657 de Rosnay, P., M. Drusch, D. Vasiljevic, G. Balsamo, C. Albergel, and L. Isaksen, 2013:  
658 A simplified Extended Kalman Filter for the global operational soil moisture analysis at  
659 ECMWF. *Quarterly Journal of the Royal Meteorological Society*, **139**, 1199–1213, doi:  
660 10.1002/qj.2023.
- 661 Dee, D. and A. Da Silva, 1998: Data assimilation in the presence of forecast bias. *Q.J.R.*  
662 *Meteorol. Soc.*, **124**, 269–295, doi:10.1002/qj.49712454512.
- 663 Dee, D. and R. Todling, 2000: Data assimilation in the presence of forecast bias: The  
664 GEOS moisture analysis. *Mon. Wea. Rev.*, **128**, 3268–3282, doi:{10.1175/1520-0493(2000)  
665 128<3268:DAITPO>2.0.CO;2}.
- 666 Dee, D. and S. Uppala, 2009: Variational bias correction of satellite radiance data in the  
667 ERA-Interim reanalysis. *Q. J. R. Meteorol. Soc.*, **135**, 1830–1841, doi:10.1002/qj.493.
- 668 Dharssi, I., K. Bovis, B. Macpherson, and C. Jones, 2011: Operational assimilation of AS-  
669 CAT surface soil wetness at the Met Office. *Hydrology and Earth System Sciences*, **15**,  
670 2729–2746, doi:0.5194/hess-15-2729-2011.
- 671 Draper, C., J.-F. Mahfouf, and J. Walker, 2009: An EKF assimilation of AMSR-E soil mois-  
672 ture into the ISBA land surface scheme. *Journal of Geophysical Research*, **114**, D20 104,  
673 doi:10.1029/2008JD011650.
- 674 Draper, C., R. Reichle, R. de Jeu, V. Naeimi, R. Parinussa, and W. Wagner, 2013: Esti-  
675 mating root mean square errors in remotely sensed soil moisture over continental scale  
676 domains. *Remote Sensing of Environment*, **137**, 288–298, doi:10.1016/j.rse.2013.06.013.

- 677 Draper, C., R. Reichle, G. De Lannoy, and Q. Liu, 2012: Assimilation of passive and active  
678 microwave soil moisture retrievals. *Geophysical Research Letters*, **39**, L04 401, doi:10.1029/  
679 2011GL050655.
- 680 Drusch, M., E. Wood, and H. Gao, 2005: Observation operators for the direct assimilation  
681 of TRMM microwave imager retrieved soil moisture. *Geophysical Research Letters*, **32**,  
682 L15 403, doi:10.1029/2005GL023623.
- 683 Fertig, E., et al., 2009: Observation bias correction with an ensemble Kalman filter. *Tellus*  
684 *A*, **61**, 210–226, doi:10.1111/j.1600-0870.2008.00378.x.
- 685 Friedland, B., 1969: Treatment of bias in recursive filtering. *IEEE Transactions on Automatic*  
686 *Control.*, **14**, 359–367, doi:10.1109/TAC.1969.1099223.
- 687 Ghent, D., J. Kaduk, J. Remedios, J. Ardö, and H. Balzter, 2010: Assimilation of land  
688 surface temperature into the land surface model JULES with an ensemble Kalman filter.  
689 *Journal of Geophysical Research*, **115**, D19 112, doi:10.1029/2010JD014392.
- 690 Harris, B. and G. Kelly, 2001: A satellite radiance-bias correction scheme for data assimila-  
691 tion. *Q.J.R. Meteorol. Soc.*, **127**, 1453–1468, doi:10.1002/qj.49712757418.
- 692 Keppenne, C., M. Rienecker, N. Kurkowski, and D. Adamec, 2005: Ensemble Kalman filter  
693 assimilation of temperature and altimeter data with bias correction and application to  
694 seasonal prediction. *Nonlinear Processes in Geophysics*, **12**, 491–503.
- 695 Koster, R., M. Suarez, A. Ducharne, M. Stieglitz, and P. Kumar, 2000: A catchment-based  
696 approach to modeling land surface processes in a general circulation model: 1. model struc-  
697 ture. *Journal of Geophysical Research*, **105**, 24 809–24 822, doi:10.1029/2000JD900327.
- 698 Minnis, P., L. Nguyen, D. Doelling, D. Young, W. Miller, and D. Kratz, 2002: Rapid  
699 Calibration of Operational and Research Meteorological Satellite Imagers. Part II: Com-

700 parison of Infrared Channels. *J. Atmos. Oceanic Technol.*, **19**, 1250–1266, doi:10.1175/  
701 1520-0426(2002)019<1250:RCOOAR>2.0.CO;2.

702 Pauwels, V., G. De Lannoy, H.-J. Hendricks Franssen, and H. Vereecken, 2013: Simul-  
703 taneous estimation of model state variables and observation and forecast biases us-  
704 ing a two-stage hybrid kalman filter. *Hydrol. Earth Syst. Sci.*, **17**, 3499–3521, doi:  
705 10.5194/hess-17-3499-2013.

706 Reichle, R., G. De Lannoy, B. Forman, C. Draper, and Q. Liu, 2013: Connecting satellite  
707 observations with water cycle variables through land data assimilation: Examples using the  
708 NASA GEOS-5 LDAS. *Surveys in Geophysics*, **35**, 577–606, doi:0.1007/s10712-013-9220-8.

709 Reichle, R. and R. Koster, 2003: Assessing the impact of horizontal error correlations in  
710 background fields on soil moisture estimation. *Journal of Hydrometeorology*, **4**, 1229–1242,  
711 doi:10.1175/1525-7541(2003)004<1229:ATIOHE>2.0.CO;2.

712 Reichle, R. and R. Koster, 2004: Bias reduction in short records of satellite soil moisture.  
713 *Geophysical Research Letters*, **31**, L19 501, doi:10.1029/2004GL020938.

714 Reichle, R., R. Koster, J. Dong, and A. Berg, 2004: Global soil moisture from satellite  
715 observations, land surface models, and ground data: Implications for data assimila-  
716 tion. *Journal of Hydrometeorology*, **5**, 430 – 442, doi:10.1175/1525-7541(2004)005<0430:  
717 GSMFSO>2.0.CO;2.

718 Reichle, R., R. Koster, P. Liu, S. Mahanama, E. Njoku, and M. Owe, 2007: Comparison  
719 and assimilation of global soil moisture retrievals from the Advanced Microwave Scanning  
720 Radiometer for the Earth Observing System (AMSR-E) and the Scanning Multichannel  
721 Microwave Radiometer (SMMR). *Journal of Geophysical Research* , **112**, D09 108, doi:  
722 {10.1029/2006JD008033}.

723 Reichle, R., S. Kumar, S. Mahanama, R. Koster, and Q. Liu, 2010: Assimilation of satellite-



724 derived skin temperature observations into land surface models. *Journal of Hydrometeo-*  
725 *rology*, **11**, 1103–1122, doi:10.1175/2010JHM1262.1.

726 Rienecker, M., et al., 2008: The GEOS-5 Data Assimilation System - Documentation of  
727 Versions 5.0.1, 5.1.0, and 5.2.0. *Technical Report Series on Global Modeling and Data*  
728 *Assimilation*, **27**.

729 Rienecker, M., et al., 2011: MERRA - NASA's Modern-Era Retrospective Analy-  
730 sis for Research and Applications. *Journal of Climate*, **24**, 3624–3648, doi:10.1175/  
731 JCLI-D-11-00015.1.

732 Scarino, B., P. Minnis, R. Palikonda, R. Reichle, D. Morstad, C. Yost, B. Shan, and  
733 Q. Liu, 2013: Retrieving clear-sky surface skin temperature for numerical weather pre-  
734 diction applications from geostationary satellite data. *Remote Sensing*, **5**, 342–366, doi:  
735 10.3390/rs5010342.

736 Scipal, K., M. Drusch, and W. Wagner, 2008: Assimilation of a ERS scatterometer derived  
737 soil moisture index in the ECMWF numerical weather prediction system. *Advances in*  
738 *Water Resources*, **31**, 1101–1112, doi:10.1016/j.advwatres.2008.04.013.

739 Slater, A. and M. Clark, 2006: Snow Data Assimilation via an Ensemble Kalman Filter. *J.*  
740 *Hydrometeor.*, **7**, 478–493, doi:10.1175/JHM505.1.

741 Vinnikov, K., Y. Yu, M. Rama Varma Raja, D. Tarpley, and M. Goldberg, 2008: Diurnal-  
742 seasonal and weather-related variations of land surface temperature observed from geosta-  
743 tionary satellites. *Geophysical Research Letters*, **35**, L22 708, doi:10.1029/2008gl035759.

744 Wang, A., M. Barlage, X. Zeng, and C. Draper, 2014: Comparison of land skin temperature  
745 from a land model, remote sensing, and in-situ measurement. *Journal of Geophysical*  
746 *Research*, **119**, doi:10.1002/2013JD021026.

747 Wang, K., Z. Wan, P. Wang, M. Sparrow, J. Liu, X. Zhou, and et al., 2005: Estimation of  
748 surface long wave radiation and broadband emissivity using Moderate Resolution Imaging  
749 Spectroradiometer (MODIS) land surface temperature/emissivity products. *Journal of*  
750 *Geophysical Research*, **110**, D11 109, doi:10.1029/2004JD005566.

## 751 **6. Figures**



753 **List of Tables**

754	1	Ensemble Generation Perturbation Parameters for Forcing and Model Prog-	
755		nostic Variables.	36
756	2	Spatial Mean of the ubRMSD (K) with MODIS $T_{skin}$ Reported in Figure 7.	37

TABLE 1. Ensemble Generation Perturbation Parameters for Forcing and Model Prognostic Variables.

	(A)dditive, or (M)ultiplicative	Standard Deviation	AR(1) Time Scale	Perturbation cross-correlation			
				GHT1	T2m	SW	LW
$T_{surf}$	A	0.2 K	12 hours	0.7	0	0	0
GHT1	A	50,000 J	12 hours	-	0	0	0
2m air temp (T2m)	A	1 K	24 hours		-	0.4	0.4
SW radiation	M	0.3	24 hours			-	-0.6
LW radiation	A	20 $\text{Wm}^{-2}$	24 hours				-

TABLE 2. Spatial Mean of the ubRMSD (K) with MODIS  $T_{skin}$  Reported in Figure 7.

Experiment	MODIS overpass			
	Nighttime		Daytime	
	Terra	Aqua	Terra	Aqua
Open-loop	1.89	1.94	3.62	3.60
$T_{skin}$ assimilation	1.70	1.79	3.36	3.42
Difference	0.19	0.15	0.27	0.18

## 757 List of Figures

- 758 1 Coverage of the assimilated GOES-West and GOES-East  $T_{skin}$  observations  
759 from 1 June, 2012 to 31 May, 2013, as a fraction of the maximum possi-  
760 ble coverage (eight observations every day). The locations of the SURFRAD  
761 measurement stations are marked as DRA (Desert Rock), TBL (Table Moun-  
762 tain), SXF (Sioux Falls), GWN (Goodwin Creek), BON (Bondville), and PSU  
763 (Penn State). The plotted meridians demark the GOES-West and GOES-East  
764 domains. 40
- 765 2 Diurnal cycle of the  $T_{skin}$  O-F mean difference, averaged over the Americas, for  
766 a bias-blind assimilation (solid) and the two-stage observation bias and state  
767 estimation bias-aware assimilation with  $\tau = 20$  days (dashed), for GOES-West  
768 (black) and GOES-East (grey). 41
- 769 3 The  $T_{skin}$  O-F residuals [K] at 21:00 UTC (black crosses) at the a) Goodwin  
770 Creek, b) Sioux Falls, and c) Desert Rock SURFRAD sites. Black lines show  
771 the smoothed O-F time series using the first two annual Fourier harmonics.  
772 Dots show the bias estimates from the two-stage observation bias correction  
773 scheme using (dark blue)  $\tau = 10$  days, (light blue)  $\tau = 20$  days, and (pink)  
774  $\tau = 30$  days. 42
- 775 4 Histograms of the state update innovations at 21:00 UTC, for the assimila-  
776 tion of geostationary  $T_{skin}$ , at the Goodwin Creek (GWN), Sioux Falls (SXF),  
777 and Desert Rock (DRA) SURFRAD sites, for a bias-blind assimilation (up-  
778 per), and for the two-stage observation bias and state estimation bias-aware  
779 assimilation with  $\tau = 20$  days (lower). 43

- 780 5 Observation-minus-forecast  $T_{skin}$  mean difference, estimated at 09:00 UTC on  
781 first a) June, b) July, and c) August, 2012. Values are shown only where the  
782 observation bias estimate is considered valid for use in the state update equa-  
783 tion. The plotted meridians demark the domain of each satellite:  $[-175^\circ, -105^\circ]$   
784 GOES-West,  $[-105^\circ, -37^\circ]$  GOES-East,  $[-37^\circ, 54^\circ]$  MTSAT-2,  $[54^\circ, 90^\circ]$  FY-2E,  
785 and  $[90^\circ, -175^\circ]$  Met-9. 44
- 786 6 ubRMSD with SURFRAD  $T_{skin}$ , calculated separately for each SURFRAD  
787 site and each observation time, for the assimilation of geostationary obser-  
788 vations with the two-stage filter (filled circles), and the open-loop (unfilled  
789 circles). The mean ubRMSD at each time of day for the assimilation (open-  
790 loop) is indicated by the solid (dashed) line. 45
- 791 7 ubRMSD with MODIS  $T_{skin}$  for the open-loop (upper), and the improvement  
792 in the ubRMSD gained from the assimilating geostationary  $T_{skin}$  with the  
793 two stage filter (lower:  $\Delta$  ubRMSD=ubRMSD of open-loop - ubRMSD of  
794 assimilation), separately for each Terra and Aqua overpass direction. Grey  
795 indicates  $< 30$  coincident geostationary and MODIS  $T_{skin}$  observations. The  
796 plotted meridians demark the GOES-West and GOES-East domains. 46



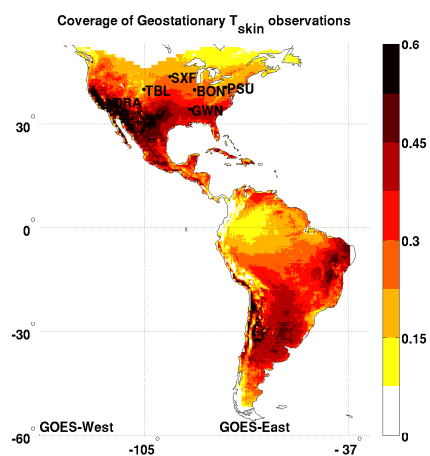


FIG. 1. Coverage of the assimilated GOES-West and GOES-East  $T_{skin}$  observations from 1 June, 2012 to 31 May, 2013, as a fraction of the maximum possible coverage (eight observations every day). The locations of the SURFRAD measurement stations are marked as DRA (Desert Rock), TBL (Table Mountain), SXF (Sioux Falls), GWN (Goodwin Creek), BON (Bondville), and PSU (Penn State). The plotted meridians demark the GOES-West and GOES-East domains.

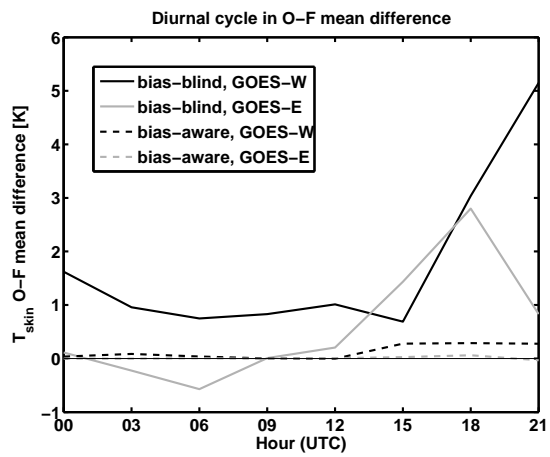


FIG. 2. Diurnal cycle of the  $T_{skin}$  O-F mean difference, averaged over the Americas, for a bias-blind assimilation (solid) and the two-stage observation bias and state estimation bias-aware assimilation with  $\tau = 20$  days (dashed), for GOES-West (black) and GOES-East (grey).

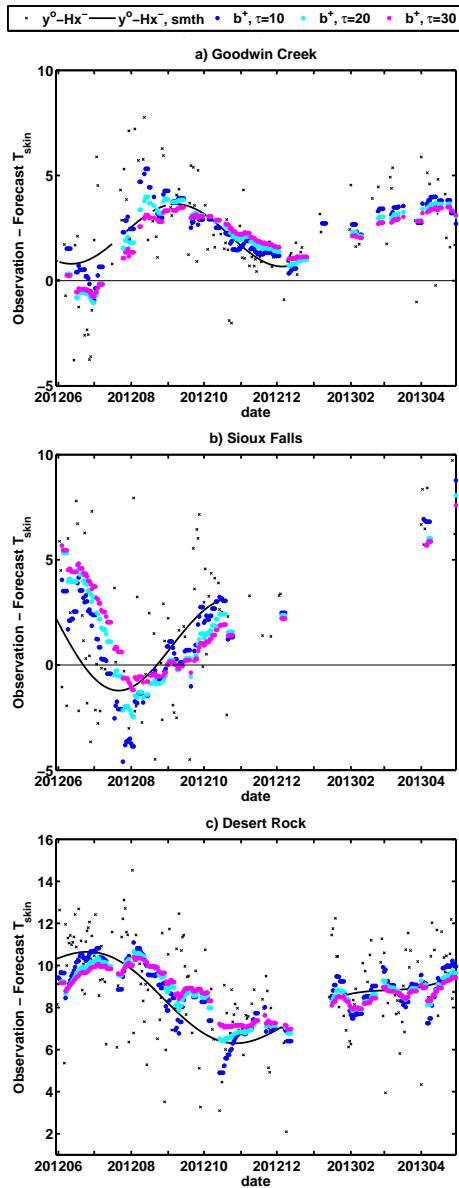


FIG. 3. The  $T_{skin}$  O-F residuals [K] at 21:00 UTC (black crosses) at the a) Goodwin Creek, b) Sioux Falls, and c) Desert Rock SURFRAD sites. Black lines show the smoothed O-F time series using the first two annual Fourier harmonics. Dots show the bias estimates from the two-stage observation bias correction scheme using (dark blue)  $\tau=10$  days, (light blue)  $\tau = 20$  days, and (pink)  $\tau=30$  days.

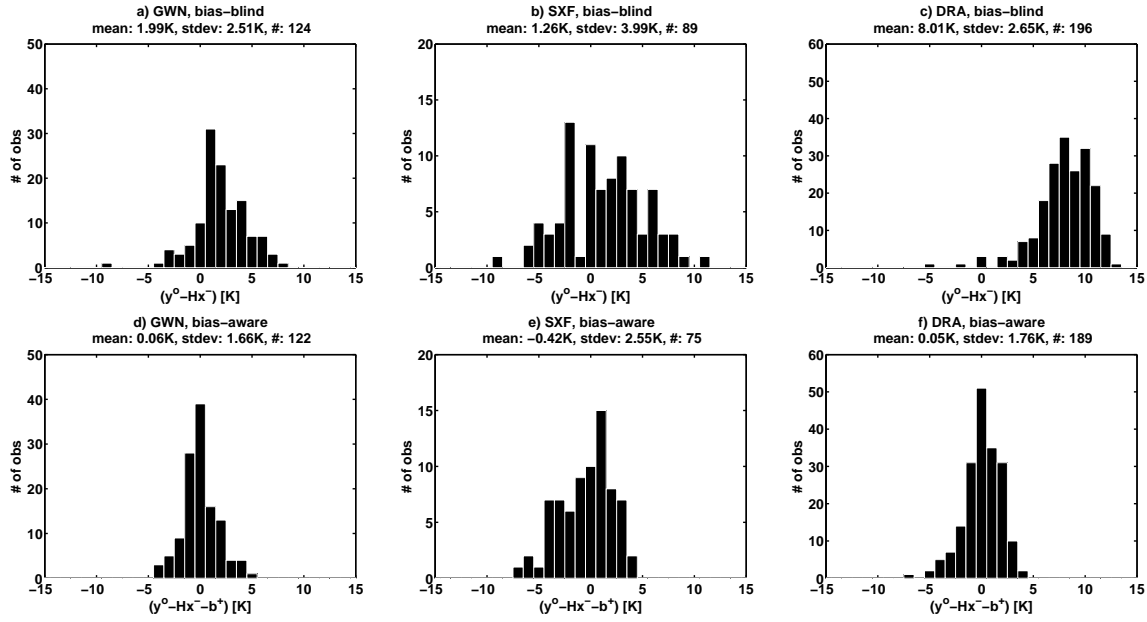


FIG. 4. Histograms of the state update innovations at 21:00 UTC, for the assimilation of geostationary  $T_{skin}$ , at the Goodwin Creek (GWN), Sioux Falls (SXF), and Desert Rock (DRA) SURFRAD sites, for a bias-blind assimilation (upper), and for the two-stage observation bias and state estimation bias-aware assimilation with  $\tau=20$  days (lower).

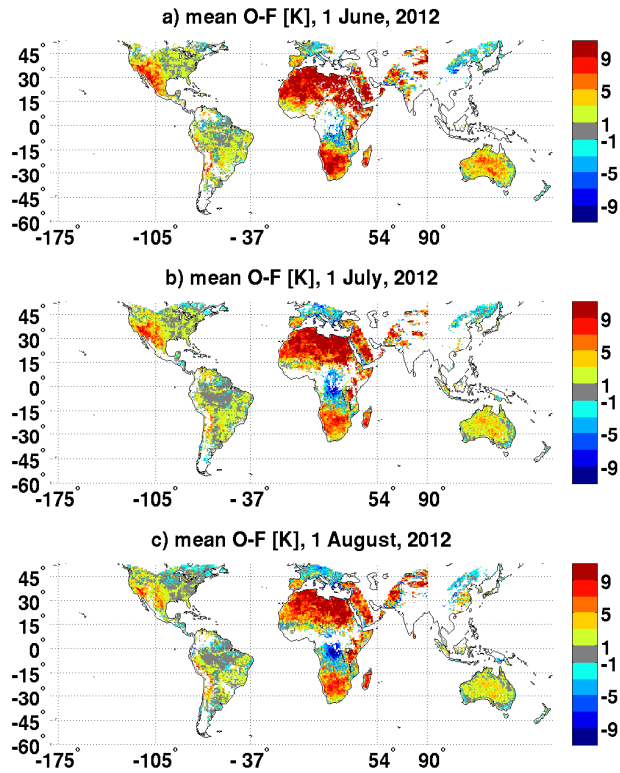


FIG. 5. Observation-minus-forecast  $T_{skin}$  mean difference, estimated at 09:00 UTC on first a) June, b) July, and c) August, 2012. Values are shown only where the observation bias estimate is considered valid for use in the state update equation. The plotted meridians demark the domain of each satellite:  $[-175^{\circ}, -105^{\circ}]$  GOES-West,  $[-105^{\circ}, -37^{\circ}]$  GOES-East,  $[-37^{\circ}, 54^{\circ}]$  MTSAT-2,  $[54^{\circ}, 90^{\circ}]$  FY-2E, and  $[90^{\circ}, -175^{\circ}]$  Met-9.

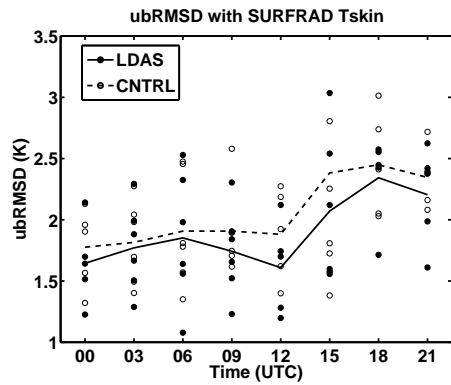


FIG. 6. ubRMSD with SURFRAD  $T_{skin}$ , calculated separately for each SURFRAD site and each observation time, for the assimilation of geostationary observations with the two-stage filter (filled circles), and the open-loop (unfilled circles). The mean ubRMSD at each time of day for the assimilation (open-loop) is indicated by the solid (dashed) line.

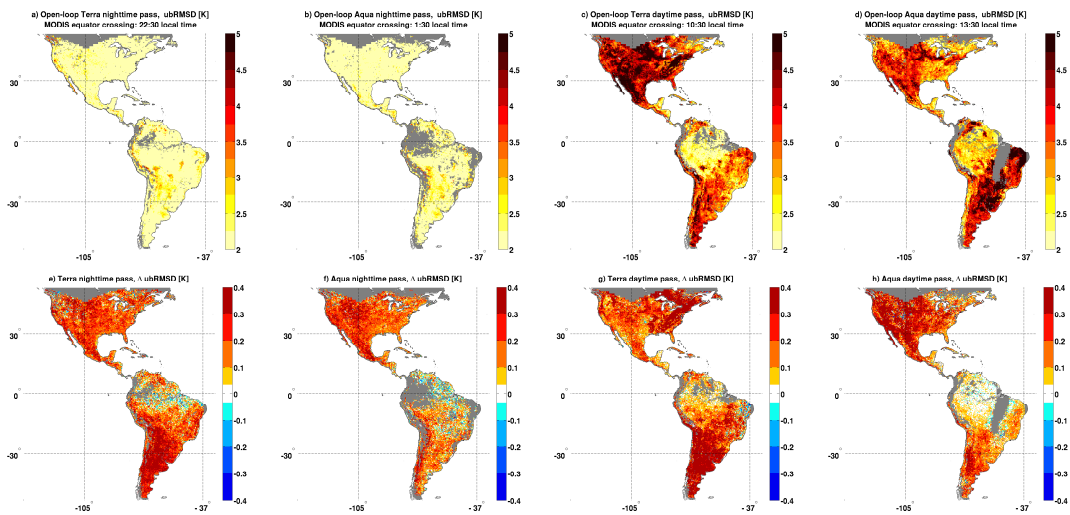


FIG. 7. ubRMSD with MODIS  $T_{skin}$  for the open-loop (upper), and the improvement in the ubRMSD gained from the assimilating geostationary  $T_{skin}$  with the two stage filter (lower:  $\Delta$  ubRMSD=ubRMSD of open-loop - ubRMSD of assimilation), separately for each Terra and Aqua overpass direction. Grey indicates  $< 30$  coincident geostationary and MODIS  $T_{skin}$  observations. The plotted meridians demark the GOES-West and GOES-East domains.