# OSIRIS-REX ORBIT DETERMINATION COVARIANCE STUDIES AT BENNU 

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#### Abstract

The Origins Spectral Interpretation Resource Identification Security Regolith Explorer (OSIRIS-REx) mission is a NASA New Frontiers mission launching in 2016 to rendezvous with the small, Earth-crossing asteroid (101955) Bennu in late 2018, ultimately returning a sample of regolith to Earth. Approximately three months before the encounter with Bennu, the asteroid becomes detectable in the narrow field PolyCam imager. The spacecraft's rendezvous with Bennu begins with a series of four Asteroid Approach Maneuvers, slowing the spacecraft's speed relative to Bennu beginning two and a half months prior to closest approach, ultimately delivering the spacecraft to a point 18 km from Bennu in Nov, 2018. An extensive campaign of proximity operations activities to characterize the properties of Bennu and select a suitable sample site will follow. This paper will discuss the challenges of navigating near a small $500-\mathrm{m}$ diameter asteroid. The navigation at close proximity is dependent on the accurate mathematical model or digital terrain map of the asteroid's shape. Predictions of the spacecraft state are very sensitive to spacecraft small forces, solar radiation pressure, and mis-modeling of Bennu's gravity field. Uncertainties in the physical parameters of the central body Bennu create additional challenges. The navigation errors are discussed and their impact on science planning will be presented.


## INTRODUCTION

In the fall of 2018, NASA's OSIRIS-REx (OREx) spacecraft (S/C) will encounter the small Earth-crossing B-type asteroid, Bennu, with the objective to acquire a sample of the asteroid's regolith and return it to Earth. Activities onboard the S/C will increase 3 months before the encounter when the asteroid finally becomes detectable in the narrow field PolyCam imager. The S/C's rendezvous with Bennu, which is independent of launch date, begins with a series of four Asteroid Approach Maneuvers (AAMs), which slow the S/C's speed relative to Bennu beginning two and one half months prior to closest approach of 18 km on November 18, 2018. During this time, navigation is dependent on star-based Optical Navigation (OpNav) images of the asteroid and 2-way X-band Doppler and range via the Deep Space Network (DSN). During the approach to Bennu, several observations will be devoted to searching for satellites in orbit about the asteroid. If none are found, the mission will proceed with the Navigation Campaign, which will allow the Navigation Team approximately two months to determine the dynamical environment at close proximity to Bennu accurately enough to achieve the Science objectives in subsequent phases and ultimately acquire a sample during the Touch And Go (TAG) event.

[^0]The proximity operations (ProxOps) Navigation Campaign will begin with the Preliminary Survey phase by performing three $7-\mathrm{km}$ hyperbolic flybys of the Northern, Equatorial and Southern regions of Bennu. These flybys allow the Navigation Team to determine the mass of Bennu to within 2\% as shown in Figure 1. After the last flyby, the S/C then performs a series of small burns to enter into a $1.5-$ km terminator orbit about the 512-meter mean-diameter asteroid. The transition from using the star-based OpNavs as the primary navigation observations to the


Figure 1: Improvements to Bennu's GM knowledge during Preliminary Survey and Orbital-A landmark OpNav images using the powerful Stereophotoclinometry (SPC) technique will take place during this orbital mission phase, referred to as Orbital-A. After the transition to landmark navigation, the mission executes the Detailed Survey where the S/C performs a series of maneuvers to target specific science observations of Bennu's surface at several solar longitudes or phase angles with radial distances of $4-5 \mathrm{~km}$. After the last science observation of the Detailed Survey, another series of orbit insertion maneuvers are performed to bring the $\mathrm{S} / \mathrm{C}$ from a $2-\mathrm{km}$ orbit to a $1-\mathrm{km}$ terminator orbit, referred to as Orbital-B, at the end of March. Following completion of Orbit-B science objectives, the S/C performs a series of low-altitude reconnaissance flybys. Each flyby is initiated by an Orbital Departure Maneuver (ODM) to depart the orbit plane and fly across the sunward face of the asteroid over a possible sampling site at altitudes of either 525 m or 225 m . After each of these sorties, the $\mathrm{S} / \mathrm{C}$ is returned to the $1-\mathrm{km}$ terminator orbit. Once the Project determines the sample collection site, two rehearsals of the TAG event are executed. The first rehearsal includes departure from orbit and delivery to the "checkpoint" position 125 m above the sampling site, after which a burn is executed to deliver the $\mathrm{S} / \mathrm{C}$ back to the 1 km home orbit. The second rehearsal includes departure from orbit, execution of the checkpoint maneuver to target the $\mathrm{S} / \mathrm{C}$ on an intercept trajectory with the sample collection site, and the matchpoint maneuver, which is designed to achieve the 10 $\mathrm{cm} / \mathrm{s}$ contact velocity with the surface. The second rehearsal again concludes with a burn to return the S/C back to the 1 km orbit. Finally, in October 2019 the sampling attempt will take place. Berry [2015] gives a thorough description of the TAG design and navigation concept of operations.

Bennu is one of the smallest planetary bodies to be visited to date, and the OSIRIS-REx mission plan brings the $\mathrm{S} / \mathrm{C}$ into very close proximity with Bennu, ultimately including contact with the surface during the sample collection event. Significant uncertainties in the physical parameters of the central body Bennu exacerbate these challenges. This work examines the challenges of navigating in close proximity to a small diameter asteroid. The navigation errors for several ProxOps mission phases are discussed and their impact on science planning. The navigation is dependent on the accurate mathematical model or digital terrain map of the asteroid's shape. Predictions of the $\mathrm{S} / \mathrm{C}$ state are very sensitive to $\mathrm{S} / \mathrm{C}$ small forces, solar radiation pressure (SRP), and mis-modeling of Bennu's gravity field. All of these navigation error sources are discussed and their impact on science planning will be presented.

## ORBIT DETERMINATION PROCESS

Orbit Determination (OD) is the process of estimating the $\mathrm{S} / \mathrm{C}$ 's state (position and velocity) by minimizing in a least squares sense the residuals of tracking data observables and computed observables. The computed observables are based on a dynamical model of the S/C's equations of motion due to gravity, SRP, S/C maneuvers and momentum desaturation events (desats), and other small non-gravitational forces.

During flight operations, OD is geared towards the generation and delivery of certain data products used by the project. The types of products produced by the OD team throughout the mission are given below:

- Maneuver Designs: Prior to a planned maneuver, an estimated trajectory and its uncertainty is predicted forward to the maneuver epoch in order to design the maneuver.
- Knowledge Updates: Prior to a planned mission phase, an estimated trajectory and its uncertainty is predicted forward for use in generating or updating the sequence aboard the S/C.
- Trajectory Reconstructions: At specific times, the data arc is terminated and used to provide an improved estimate of the trajectory and associated uncertainties at points interior to the data arc to assist in science data reduction.
- Maneuver Reconstructions: Data before and after a TCM are used to estimate maneuver parameters with the objective to improve their future designs.
- Tracking Prediction Updates: Trajectory updates given to the DSN for antenna pointing predictions and for proper up-link and down-link tracking of radio frequencies.


## ProxOps Filter Strategy

Computation and prediction of the S/C's trajectory is accomplished by numerical integration of the equations of motion using the MIRAGE software. The integrated S/C ephemeris and other trajectory-related products are used throughout the mission to support maneuver design and analysis, S/C engineering analysis, sequence development, mission planning, and DSN operations.

In general terms, the dynamics of the trajectory are modeled by a set of nonlinear ordinary differential equations. The acceleration of the $S / C$ in the inertial frame can be represented by

$$
\begin{equation*}
\ddot{\vec{r}}=\ddot{\vec{r}}_{\mathrm{g}}+\ddot{\vec{r}}_{\mathrm{SRP}}+\ddot{\vec{r}}_{\mathrm{NGA}} \tag{1}
\end{equation*}
$$

where $\ddot{\vec{r}}_{g}$ is the S/C acceleration due to gravitational forces, $\ddot{\vec{r}}_{\text {SRP }}$ is the S/C acceleration due to SRP and $\ddot{\vec{r}}_{\mathrm{NGA}}$ is the S/C acceleration due to other small non-gravitational forces caused by factors such as desats, albedo and infrared radiation pressure from the asteroid, thermal re-radiation of the $\mathrm{S} / \mathrm{C}$ and outgassing. Figure 2 shows the major forces acting upon the $\mathrm{S} / \mathrm{C}$ during proximity operations at Bennu.

For the Bennu proximity operations phase, the gravitational forces of Bennu due to oblateness are modeled by a $15 \times 15$ spherical harmonic representation. Initially, this model is derived from a shape model that assumes a constant density. However, throughout ProxOps, the non-spherical gravity model of Bennu will be updated with current best estimates. Note at the $1-\mathrm{km}$ orbit, the trajectory is not sensitive to terms higher than degree and order 4.

A box-wing plate model of the $\mathrm{S} / \mathrm{C}$ has been developed and implemented in MIRAGE for use with SRP modeling and non-gravitational accelerations such as asteroid albedo and infrared radiation pressure. This shape model of the $\mathrm{S} / \mathrm{C}$ uses 10 flat plates representing a 6 -sided Bus and the front and backs of the two solar panels. The 10 -plate model consists of areas and optical


Figure 2: Major forces acting on OREx during early ProxOps (left) and Orbital-B (right)
properties (specular and diffuse coefficients) derived from the $\mathrm{S} / \mathrm{C}$ properties provided by Lockheed Martin (LM) [Olds, 2013]. The SRP magnitude ranges from $65 \mathrm{~nm} / \mathrm{s}^{2}$ at perihelion in January 2019 to $28 \mathrm{~nm} / \mathrm{s}^{2}$ at aphelion in September of 2019.

The acceleration due to small non-gravitational forces can be expressed as

$$
\begin{equation*}
\ddot{\vec{r}}_{\mathrm{NGA}}=a_{R} \hat{u}_{R}+a_{X} \hat{u}_{X}+a_{Y} \hat{u}_{Y} \tag{2}
\end{equation*}
$$

where $a_{R}, a_{X}$, and $a_{Y}$ represent acceleration magnitudes in the corresponding unit directions. The unit vectors $\hat{u}_{R}, \hat{u}_{X}$, and $\hat{u}_{Y}$ are defined in a spacecraft local coordinate system for which the directions are defined as follows: $\hat{u}_{R}$ is in the anti-Sun direction, $\hat{u}_{Y}$ is normal to the plane formed by $\hat{u}_{R}$ and the spacecraft's nominal velocity vector, $\bar{v}_{\text {ref }}$, and $\hat{u}_{X}$ completes the right-handed orthonormal triad.

These parameters are used to approximate small, S/C induced anomalous forces derived from thermal re-radiation, material out-gassing, gas leakage from valves and pressurized tanks, and other small effects. The significance of these accelerations lies in their effect on the OD process and uncertainty predictions. They are typically modeled as random processes due to the fact that the trajectory perturbations due to these phenomena are typically quite small and random in nature. The typical accelerations derived from these processes during ProxOps are assumed to range from 1 to $3 \mathrm{~nm} / \mathrm{s}^{2}$. However, trajectory perturbations at these levels can induce significant downtrack errors when in close proximity to a small asteroid, especially when evaluating the impact on science observations two or more days after the OD data cut off ( DCO ). One of the major challenges will be to characterize these errors below the $3 \mathrm{~nm} / \mathrm{s}^{2}$ level to help with science planning. In addition, since the onboard $\mathrm{S} / \mathrm{C}$ ephemeris is used to target nadir pointing OpNav images, it will be necessary to update the onboard ephemeris to keep Bennu within the NavCam image at least twice per week during the $1-\mathrm{km}$ orbit, because down-track errors could grow over 100 m within 3-4 days.

## Spacecraft Thermal Re-radiation Force

A model of the $\mathrm{S} / \mathrm{C}$ thermal re-radiation has been developed to aid in the predictive accuracy of the trajectories delivered to the project for sequence and Science planning. The force (acceleration) upon the $\mathrm{S} / \mathrm{C}$ in the $\mathrm{S} / \mathrm{C}$ body-fixed frame resulting from the $\mathrm{S} / \mathrm{C}$ 's thermal (infrared) emissive radiation imbalance can be computed to first order as a function of time:

$$
\begin{align*}
\vec{a}_{S / C I R}(t)= & -\frac{2 \sigma}{3 m c}\left(\left[A_{X}\left(\epsilon_{+X} T_{+X}^{4}(t)-\epsilon_{-X} T_{-X}^{4}(t)\right)+A_{S A}\left(\epsilon_{f} T_{f}^{4}(t)-\epsilon_{b} T_{b}^{4}(t)\right) \cos \theta\right] \hat{x}\right. \\
& +A_{Y}\left(\epsilon_{+Y} T_{+Y}^{4}(t)-\epsilon_{-Y} T_{-Y}^{4}(t)\right) \hat{y}  \tag{3}\\
& \left.+\left[A_{Z}\left(\epsilon_{+Z} T_{+Z}^{4}(t)-\epsilon_{-Z} T_{-Z}^{4}(t)\right)-A_{S A}\left(\epsilon_{f} T_{f}^{4}(t)-\epsilon_{b} T_{b}^{4}(t)\right) \sin \theta\right] \hat{z}\right)
\end{align*}
$$

where m is the $\mathrm{S} / \mathrm{C}$ mass, c is the speed of light, $\sigma$ is Stefan-Boltzmann constant, $\theta$ is the solar panel tilt angle, $\mathrm{T}_{\mathrm{f}}$ is temperature on the front of the solar array, $\mathrm{T}_{\mathrm{b}}$ is the temperature on the back of the solar array, and $\mathrm{A}_{\mathrm{i}}, \varepsilon_{i}$, and $\mathrm{T}_{\mathrm{i}}(\mathrm{t})$ are the projected area, area-averaged emissivity and areaaveraged temperature, respectively, on each face of the bus or solar array. The S/C body coordinate frame is used. This assumes each face of the bus can be modeled as flat plates, which are normal to the body-fixed axes.

Research on this force (Ref. Sugimoto [2010], Shoemaker [2012], Antreasian [1992], Vique [1994], and Fahnestock [2012]) for vehicles in the 1 AU solar distance range generally show that the resultant force can be as much as $10 \%$ of the SRP affect. The above equation for the thermal force depends on the on-orbit temperatures of the S/C. The computation of the expected temperatures in close proximity to Bennu was performed by the Lockheed-Martin thermal engineer, C. May, using a full thermal-finite-element analysis of the S/C. The thermal model of the S/C contains over 6000 external nodes. Each node is represented by a projected area and optical properties (reflectivity, emissivity). Temperature histories were computed during the $1-\mathrm{km}$ Orbital-B orbit assuming the nominal Z-to-nadir, X-to-Sun attitude (see Figure 3 (a)) and during a time that assumes a 5 -hour High Gain Antenna (HGA)-to-Earth (X-to-Earth) pointing attitude. The solar arrays are rotated $45^{\circ}$ about the +Y -axis for both attitudes. At each point in the orbit, the contribution of energy imbalances of each node are summed along each S/C body-fixed axes to determine the acceleration due to thermal re-radiation.

Two thermal models were received from Lockheed Martin: 1) the first model was evaluated during late Orbital-B at the time of TAG in October 2019 when Bennu is near aphelion at 1.3 AU ; and 2) the second model was evaluated during early Orbital-B (March 2019) when Bennu just passes perihelion at 0.98 AU . The data included temperatures, emissivities and areas for each external node on each side of the S/C bus and solar arrays for four locations in the $1-\mathrm{km}$ sunterminator orbit. The locations include Bennu's North Pole, South Pole, and equator crossings at sunrise and sunset for nominal attitude and one point for HGA-to-Earth point attitude when the Sun-probe-Earth (SPE) angle is $\sim 72.5^{\circ}$. Since model 1 was evaluated at Bennu's aphelion when temperatures are generally lower, these numbers are considered to be near the lower bound of the expected thermal force during ProxOps. And because model 2 incorporated higher temperatures during perihelion, this model represents the expected upper bound to the $\mathrm{S} / \mathrm{C}$ thermal force.

Figure 3 (a) illustrates the orbital positions and attitudes evaluated in model 2. Figure 3 (b) shows the thermal accelerations from model 2 . These values are compared to model 1 in Table 1. The total X or Z-axis force includes the contribution of the solar array in the last columns. The forces during perihelion are roughly 2-3 times those during aphelion. The forces along the S/C X and Z -axes during the nadir-point attitude, which are in respectively, the sun (orbit normal) and radial directions are not expected to perturb the orbit's down-track position. The force along the Y-axis, which is primarily in the orbit transverse direction during nadir-point attitude, is two orders of magnitude lower than the totals in the X or Z directions. If this level of imbalance proves to be accurate in operations, then the assumed down-track non-gravitational errors are conservative.


Figure 3: a) Orbital locations, attitudes evaluated for model 2. b) S/C thermal accelerations during Orbital-B March 2019

In operations, temperature telemetry will be available at various locations on the S/C bus. These bus temperatures, however, will be internal to outside blankets and therefore, further computations are needed to determine the

Table 1: S/C Thermal accelerations along S/C body-fixed directions

| Thermal Model | Solar Dist | Attitude | Along Each S/C Axis (Face only) |  |  |  | Total |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\underset{\left(\mathrm{nm} / \mathrm{s}^{2}\right)}{\mathrm{X}}$ | $\begin{gathered} \mathrm{Y} \\ \left(\mathrm{~nm} / \mathrm{s}^{2}\right) \end{gathered}$ | $\underset{\left(\mathrm{nm} / \mathrm{s}^{2}\right)}{\mathrm{Z}}$ | Solar Arrays ( $\mathrm{nm} / \mathrm{s}^{2}$ ) | $\begin{aligned} & +\mathrm{X}+\mathrm{SA} \\ & \left(\mathrm{~nm} / \mathrm{s}^{2}\right) \end{aligned}$ | $\begin{aligned} & +\mathrm{Z}+\mathrm{SA} \\ & \left(\mathrm{~nm} / \mathrm{s}^{2}\right) \end{aligned}$ |
| Model 1 | 1.35 | Nadir | -2.58 | -0.04 | -0.02 | -0.90 | -3.22 | -0.80 |
|  |  | HGA | -1.46 | -0.03 | 2.63 | -0.72 | -1.97 | 2.12 |
| Model 2 | 0.93 | Nadir | -6.47 | -0.05 | 0.31 | -2.78 | -8.44 | -1.65 |
|  |  | HGA | -2.33 | -0.03 | 7.71 | -3.83 | -5.04 | 5.00 | temperatures on the outside blankets based on the thermal conductivity of the blankets. Further work will be performed by the thermal engineer to calibrate the full-up thermal model in operations.

The MIRAGE pseudo-epoch state batch processor will be used throughout the mission to process radiometric tracking and optical navigation observables to estimate the S/C's state. The baseline parameters that will always be estimated in the filter will include the $\mathrm{S} / \mathrm{C}$ 's state (position and velocity), maneuvers, desat events, SRP parameters, and small forces. The Bennu ephemeris, GM and gravity harmonics up to degree and order 4 will also be estimated during proximity operations at Bennu. Other parameters will be added throughout the mission as well as the uncertainties of other consider parameters. Appendix A lists the filter parameters estimated and considered for ProxOps as well as data weights and a priori uncertainties.

## OpNav Tracking

OpNav imaging is a vital contributor to the OD during asteroid proximity operations. While DSN radiometric ranging and Doppler is necessary for OD throughout the duration of the mission, these data types provide limited information when orbiting unknown bodies due to uncertainties in their ephemeris and physical properties. Thus, it is necessary to supplement radiometric data with an observation that allows for direct characterization of the unknown body. Optical images provide such information and their use in navigation near small bodies like Bennu is essential to ensure accurate orbit determination of the $\mathrm{S} / \mathrm{C}$ during the course of proximity operations.

Two OpNav techniques will be employed throughout proximity operations at Bennu. The first method is a star-based OpNav method whose objective is to determine the position of the target body's center through a series of images. This is a two-step process. First the camera pointing errors must be removed through imaging of the background stars and using their locations to solve for the pointing errors. Next, the target body is imaged resulting in a set of images that can be used to obtain the center of the target body. KXIMP is the primary star-based OpNav software used for OSIRIS-REx. KXIMP was developed by KinetX and was used successfully on the New Horizons mission to Pluto. This software will be used extensively from Approach through Or-bital-A [Jackman, et al., 2016].

Star-based OpNav will treat Bennu as an unresolved object until its diameter exceeds a few pixels. The center of Bennu will be estimated by cross-correlating the observed image with a Gaussian Point Spread Function model. When the diameter exceeds a few pixels, star-based OpNav will transition to treating Bennu as an extended body. The center will be estimated by cross-correlating the observed image against the a priori shape model of the body, thus providing improved information on the ephemeris of the $\mathrm{S} / \mathrm{C}$ and that of the asteroid.

The second optical navigation method is landmark-based OpNav; a technique that becomes possible as Bennu becomes better characterized and a three-dimensional shape model is developed. Landmark OpNav uses defined features on the body's surface to solve for both the body and $\mathrm{S} / \mathrm{C}$ positions in the presence of pointing knowledge errors. In situations where the pointing knowledge uncertainties are large, a camera with a large field of view (FOV) is required to capture enough spread between the landmarks to break the degeneracy between pointing and positioning errors. Landmark OpNav for OSIRIS-REx utilizes software called SPC. SPC was developed by Dr. Robert Gaskell with heritage from the Dawn mission and was used as a verification tool for Hayabusa and other small body missions [Gaskell, 2012]. SPC will be used in a limited capacity during Orbital-A to allow for transition from star-based OpNav to landmark OpNav. Landmark-based OpNav will be the primary optical observables used during Detailed Survey through TAG.

## Table 2: Camera Specifications

|  | PolyCam | MapCam | SamCam | NavCam |
| :--- | :---: | :---: | :---: | :---: |
| FOV (deg) | 0.8 | 4 | 21 | $33 \times 44$ |
| \# pixels | $1024 \times 1024$ | $1024 \times 1024$ | $1024 \times 1024$ | $2592 \times 1944$ |
| Focal Length (mm) | 625 | 125 | 24 | 7.6 |
| F-number | 3.125 | 3.4 | 5.6 | 3.5 |
| Aperture (cm) | 20 | 3.78 | 0.428 | 0.22 |
| microrad/px | 13.6 | 68 | 354.17 | 289.5 |
| Pixel Size (microns) | $8.5 \times 8.5$ | $8.5 \times 8.5$ | $8.5 \times 8.5$ | $2.2 \times 2.2$ |

Table 2 lists the OSIRISREx science Camera Suite (OCAMS) (PolyCam, MapCam and SamCam) and Navigation Camera (NavCam) specifications. Throughout the mission, the primary OpNav imager is the NavCam; however, there are periods during which the range to Bennu is great enough that long-range imaging must take place with narrower field of view cameras. PolyCam and MapCam will be used for these transitional periods until ranges are close enough for the wide FOV NavCam. Table 3 describes the range criteria for imager usage through the mission.

Table 3: Guideline for imager usage for OpNav imaging technique

| Range $(\mathrm{km})$ | Instrument | Technique |
| :---: | :---: | :---: |
| $>165$ | PolyCam | Star-based |
| $30-165$ | MapCam | Star-based |
| $<30$ | NavCam | Star-based |
| $33-165$ | PolyCam | Landmark $(75 \mathrm{~cm})$ |
| $7.6-33$ | MapCam | Landmark $(75 \mathrm{~cm})$ |
| $<7.6$ | NavCam | Landmark $(75 \mathrm{~cm})$ |

The Science Team Altimetry group is responsible for the development and delivery of the asteroid shape model at various resolutions throughout the mission. A 75 cm resolution shape model, referred to as a Digital Terrain Map (DTM), and associated maplets/landmarks will be made available by the end of Preliminary Survey to allow for the transition period from star-based OpNav to landmark-based OpNav to occur during Orbital-A. The delivery of the 75 cm resolution DTM will enable the use of 100 "navigation landmarks" for OpNav processing. Since Or-bital-A is a less intensive mission phase due to the reduced number of maneuvers and ephemeris updates, resources can be focused on the OpNav transition.

The weights for the landmarks are limited by the accuracy of the DTM. Prior to the Orbital-B Phase, the second DTM to be delivered to the project is expected to be accurate to 30 cm . The weights of each landmark data will depend on the resolution of the camera, $\mathrm{R}=\mathrm{r} * \mathrm{iFOV}$, where r is the range to the asteroid surface ( 1 km ) and iFOV for NavCam is $289.48 \mu \mathrm{rad}$. The nominal optical weights are:

$$
\begin{equation*}
\mathrm{W}=\left(\mathrm{W}^{2}{ }_{\text {min }}+(\mathrm{S} / \mathrm{R})^{2}\right)^{1 / 2} \tag{4}
\end{equation*}
$$

where $\mathrm{W}_{\text {min }}=$ minimum weight $=1.0$ pixel, $\mathrm{S}=\mathrm{DTM}$ error $(\mathrm{rms})=75 \mathrm{~cm}$ (or 30 cm ). For this Orbital-B scenario, the nominal optical weights applied range from 3.3 to 3.5 pixels. All analyses discussed in this paper assumed the DTM error of 75 cm .

## ORBIT DETERMINATION KNOWLEDGE AND PREDICTIVE UNCERTAINTIES

## Approach

The approach phase of the OSIRIS-REx mission begins in August of 2018 with the initial attempt to optically acquire Bennu at 60 days prior to rendezvous with the asteroid. The timeline in Figure 4 indicates the activities during the approach phase. PolyCam is used during this phase to acquire Bennu when the $\mathrm{S} / \mathrm{C}$ is more than 2 million km out from Bennu. During this timeframe, DSN tracking passes are increased to two per week while being augmented with two DeltaDifferential One-way Range (DDOR) baselines per week. These early PolyCam images are used with the star-based OpNav technique and the DSN's radiometric tracking data to determine the S/C's state relative to Bennu and refine the ephemeris of Bennu. The first of the two AAMs slows the approach rate to approximately $5.2 \mathrm{~m} / \mathrm{s}$. AAM-3 further slows the approach rate to $10 \mathrm{~cm} / \mathrm{s}$. AAM-4 is used to perform final targeting (and clean up of previous targeting errors) to Bennu at 18.5 km to begin the Preliminary Survey.

Two satellite-search observations will take place, the first prior to AAM-3, followed by a 10cm search prior to AAM-4. In response to a detection of natural satellites, the start of proximity operations about Bennu will be delayed using the contingency braking maneuver on Nov 16, 2018 to accommodate re-planning and provide additional opportunities to observe and develop ephemerides of any natural satellites greater than 10 cm in diameter.


Figure 4: Bennu approach timeline in Fall of 2018


Figure 5: S/C current state errors (1 $\sigma$ ) (a) presented in the Radial-Transverse-Normal components relative to Bennu and corresponding trajectory pointing errors (b) during final approach phase

Figure 5 (a) shows the S/C current state Radial-Transverse-Normal (RTN) uncertainties relative to Bennu during Approach. Each point in these plots includes all tracking data up to that point to determine the state. The daily OpNavs are shown in this figure to bring the state errors down substantially; however, the non-gravitational, desat or maneuver errors continue to disperse S/C's state. The small non-gravitation errors are shown to have a more pronounced effect on the state errors as the S/C's position becomes known to the tens to hundreds of meters range. Corresponding pointing errors relative to Bennu in the Transverse and Normal directions are shown in Figure 5 (b).

## Detailed Survey

This science sub-phase begins with a maneuver that puts the $\mathrm{S} / \mathrm{C}$ on a 3.5 km closest approach hyperbolic flyby to allow for imaging of the Northern hemisphere of Bennu. This is followed by another 3.5 km closest approach hyperbolic flyby that targets the Southern hemisphere of Bennu. Both of these flybys target specific solar phase angle stations of Bennu at $\pm 40$ degrees latitude. Figure 6 (a) shows the trajectory and solar phase angle stations of Bennu for this mission phase.

(a) Mid-Latitude Survey
(b) Equatorial Survey

Figure 6: OSIRIS-REx baseline trajectory for Detailed Survey


Figure 7: Mid-latitude survey predicted uncertainties for Latitude (left) and Longitude (right) of the first (blue) and second (green) survey stations
During this mid-latitude survey, the $\mathrm{S} / \mathrm{C}$ 's position must be known to $61 \mathrm{~m}(2 \sigma)$ in latitude and $33 \mathrm{~m}(2 \sigma)$ in longitude. This phase of Detailed Survey has regular HGA and Low Gain Antenna (LGA) contacts with the DSN, as well as landmark-based OpNav campaigns between DSN passes. The tracking schedule around the observations can be seen in Figure 7. Due to planning and scheduling of the science survey periods, the S/C's trajectory and uncertainties must be predicted out $\sim 30$ hours after the data cut-off. Figure 7 shows the predicted latitudinal and longitudinal uncertainties ( $2 \sigma$ ) predicted over the two survey stations of the Northern Hemisphere. Notice that the longitudinal error requirement is not met for all observations.

With the completion of the mid-latitude survey, an equatorial survey phase begins. This sequence consists of seven equatorial hyperbolic flybys that achieve an altitude of 4.7 km above Bennu's surface. The S/C will take 4 days to traverse from south to north for each equatorial station with observations being collected for 4.5 hours centered on the equatorial crossing.

Each flyby occurs at different sun illumination conditions in order to map the global texture, geological features, mineralogy, and chemistry of Bennu. Figure 6 (b) shows the trajectory for and equatorial stations for this portion of Detailed Survey. During this sub-phase, regular HGA and LGA contacts with the DSN are made, as well as landmark-based OpNav campaigns between



Figure 8: Equatorial survey predicted uncertainties for Latitude (left) and Longitude (right) of all survey stations

DSN passes. Similar to the mid-latitude survey phase, the S/C's trajectory and associated uncertainties must be predicted out $\sim 30$ hours prior to the survey. In addition, a desat is performed $\sim 5$ hours prior to the start of the survey period. The size of this desat greatly influences the latitudinal and longitudinal predicted uncertainties. Figure 8 shows the predicted latitudinal and longitudinal uncertainties ( $2 \sigma$ ) predicted over all seven-survey stations relative to the observation period. The predicted uncertainties are consistent for all survey stations. Several iterations with the LM Guidance, Navigation, and Control team were conducted to determine the current best estimate of desat delta-V expected to be imparted on the $\mathrm{S} / \mathrm{C}$ during this timeframe. The results shown take into account these updated desat performance levels. As with the Mid-latitude survey, the longitudinal requirement cannot be met with the current assumptions for all observations. Discussions are currently underway with the Science Team to determine a resolution since optimistic filter assumptions cannot meet these longitude requirements. The current assumptions for these equatorial observations can meet $2-\sigma$ accuracies better than 50 m whereas the Mid-latitude survey can meet accuracies below 100 m .


Figure 9: OSIRIS-REx baseline trajectory for Orbital-B insertion (left) and science (right)

## Orbital-B

The completion of Detailed Survey leads into the reestablishment of a stable orbit around Bennu known as Orbital-B as shown in Figure 9. The goal of this science sub-phase is to gather global science data and to map in detail twelve candidate sample sites. The duration of this phase is roughly 60 days. The orbit insertion sequence which takes place over 1 week is similar to that of Orbital-A; first a $2-\mathrm{km}$ orbit is established using a set of 3 maneuvers (target insertion to terminator orbit, capture into orbit, then cleanup/trim to 2 km ), then the $1-\mathrm{km}$ orbit is achieved with another set of 2 maneuvers. This will be a challenging period for the Navigation Team as the maneuvers are separated by roughly 48 hours. Following a successful stable orbit insertion, nine days of quiescent time is dedicated for Radio Science to acquire minimally perturbed observations for gravity field recovery. This is accomplished by allowing the S/C's trajectory to naturally evolve without any maneuvers during the data arc. During this timeframe, the $\mathrm{S} / \mathrm{C}$ is in a Sunpointed attitude. OpNav imaging is acquired when Bennu is visible in this attitude configuration. Orbit Laser Altimeter ranging to the asteroid surface is also acquired during this science subphase providing detailed measurements of the global shape and topography.

A covariance analysis was performed for the week leading up to the TAG event in midOctober 2019 to determine the state errors at the time of ODM assuming a DCO 24 hours beforehand; these errors are then used to perturb the ODM epoch state in the Monte Carol TAG analysis performed by Berry [2015]. The baseline RTN state errors predicted 1 day after the DCO are presented in Table 4 assuming the nominal Bennu GM $\left(5.2 \mathrm{~m}^{3} / \mathrm{s}^{2}\right)$. The challenge for performing the

TAG event is to determine the S/C state given the available optical and radiometric data and accurately predict the state relative to Bennu at the time of the ODM one day later. A requirement is levied on Flight Dynamics that 24-hour predictions of the S/C state shall have in-track position errors less than $85 \mathrm{~m} 3 \sigma$; the current $3 \sigma$ baseline down-track state error is less than 58 m . Note this error is slightly larger than that presented by Berry [2015] of 53 m , where the OD filter did not include OpNav pointing errors. In order to determine the pre-ODM S/C state within the requirements, all the forces affecting the $\mathrm{S} / \mathrm{C}$ 's motion must be well calibrated. Of particular importance is the calibration of small non-gravitational forces $\left(<100 \mathrm{~nm} / \mathrm{s}^{2}\right)$ such as SRP, Bennu albedo and Infrared radiation pressure, and the force imparted from the $\mathrm{S} / \mathrm{C}$ 's thermal energy imbalance. Activities that would disturb the orbit such as desats and science observation slews are reduced or eliminated during this time. This orbit is referred to as the safe-home orbit. Two filter strategies were evaluated for the Orbital-B safe-home orbit. These include a baseline case and current-best-estimate (CBE) case. Both cases assumed a priori gravity coefficient uncertainties based on the analog of Kaula's rule for Bennu, [McMahon, 2015]. The baseline case assumed that the NavCam pointing can be determined to at least the current best estimate of the S/C (S/C CBE) pointing performance of $1.15 \mathrm{mrad}(1 \sigma)$ with respect to the boresight direction and 1.01 mrad $(1 \sigma)$ in roll about the boresight. The CBE case assumed the SPC process would resolve the image pointing error within the $1-\sigma$ SPC-post-fit pointing errors of 0.42 mrad and 0.40 mrad , respectively with respect to the boresight and roll axes. These errors were set as the process noise to a white-noise-stochastic model with no time correlation between direction and opnav images. The CBE filter case also assumed improved determination of the along-track and radial components of the non-gravitation stochastic acceleration to $1 \mathrm{~nm} / \mathrm{s}^{2}$, better 2-way Doppler performance and more available landmarks in each image. Appendix A lists the parameter settings for the baseline and CBE filter strategies.

Table 2: Predicted 1-o RTN State errors in Orbital-B

| Case | Desats in predict | Map Time | $\begin{gathered} \mathrm{R} \\ (\mathrm{~km}) \end{gathered}$ | $\begin{gathered} \mathrm{T} \\ (\mathrm{~km}) \end{gathered}$ | $\begin{gathered} \mathrm{N} \\ (\mathrm{~km}) \end{gathered}$ | $\begin{gathered} \text { DR } \\ (\mathrm{km} / \mathrm{s}) \end{gathered}$ | $\begin{gathered} \text { DT } \\ (\mathrm{km} / \mathrm{s}) \end{gathered}$ | $\begin{gathered} \mathrm{DN} \\ (\mathrm{~km} / \mathrm{s}) \end{gathered}$ | Downtrack Timing Errort | Downtrack Pt Error (deg) $\dagger$ | Crosstrack Pt Error (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| At DCO |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 10-Oct-19 12:00 | 0.00077 | 0.00050 | 0.00059 | $6.67 \mathrm{E}-08$ | $3.27 \mathrm{E}-08$ | $8.38 \mathrm{E}-09$ | . 1 min | 0.0 | 0.0 |
| CBE | None | 10-Oct-19 12:00 | 0.00037 | 0.00026 | 0.00018 | $3.31 \mathrm{E}-08$ | $1.39 \mathrm{E}-08$ | $4.87 \mathrm{E}-09$ | . 1 min | 0.0 | 0.0 |
| Baseline | Desats | 10-Oct-19 12:00 | 0.00064 | 0.00055 | 0.00038 | $5.84 \mathrm{E}-08$ | $9.33 \mathrm{E}-08$ | $3.90 \mathrm{E}-08$ | . 1 min | 0.0 | 0.0 |
| CBE | Desats | 10-Oct-19 12:00 | 0.00046 | 0.00029 | 0.00031 | $3.50 \mathrm{E}-08$ | 7.67E-08 | $3.13 \mathrm{E}-08$ | . 1 min | 0.0 | 0.0 |
| Predict 1 day |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 11-Oct-19 12:00 | 0.00422 | 0.01915 | 0.00128 | $1.42 \mathrm{E}-06$ | $1.72 \mathrm{E}-07$ | $1.26 \mathrm{E}-08$ | 4.4 min | 1.1 | 0.1 |
| CBE | None | 11-Oct-19 12:00 | 0.00156 | 0.00848 | 0.00126 | $6.23 \mathrm{E}-07$ | $6.19 \mathrm{E}-08$ | 6.93E-09 | 2. min | 0.5 | 0.1 |
| Baseline | Desats | 11-Oct-19 12:00 | 0.00714 | 0.06534 | 0.00192 | $4.50 \mathrm{E}-06$ | $2.40 \mathrm{E}-07$ | $1.91 \mathrm{E}-08$ | 15.1 min | 3.7 | 0.1 |
| CBE | Desats | 11-Oct-19 12:00 | 0.00397 | 0.04358 | 0.00365 | $2.92 \mathrm{E}-06$ | $1.27 \mathrm{E}-07$ | $1.50 \mathrm{E}-08$ | 10.1 min | 2.5 | 0.2 |
| Predict 2 days |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 12-Oct-19 12:00 | 0.00827 | 0.07797 | 0.00129 | $5.64 \mathrm{E}-06$ | $3.11 \mathrm{E}-07$ | $3.58 \mathrm{E}-08$ | 18. min | 4.5 | 0.1 |
| CBE | None | 12-Oct-19 12:00 | 0.00284 | 0.02849 | 0.00127 | $2.06 \mathrm{E}-06$ | $1.07 \mathrm{E}-07$ | $1.42 \mathrm{E}-08$ | 6.6 min | 1.6 | 0.1 |
| Baseline | Desats | 12-Oct-19 12:00 | 0.00987 | 0.15630 | 0.00177 | $1.10 \mathrm{E}-05$ | $3.40 \mathrm{E}-07$ | $4.79 \mathrm{E}-08$ | 36.1 min | 9.0 | 0.1 |
| CBE | Desats | 12-Oct-19 12:00 | 0.00443 | 0.09716 | 0.00350 | $6.65 \mathrm{E}-06$ | $1.40 \mathrm{E}-07$ | $2.63 \mathrm{E}-08$ | 22.5 min | 5.6 | 0.2 |
| Predict 4 days |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 14-Oct-19 12:00 | 0.01246 | 0.26360 | 0.00128 | $1.90 \mathrm{E}-05$ | $4.76 \mathrm{E}-07$ | 1.17E-07 | 60.9 min | 15.1 | 0.1 |
| CBE | None | 14-Oct-19 12:00 | 0.00421 | 0.09100 | 0.00127 | $6.57 \mathrm{E}-06$ | $1.60 \mathrm{E}-07$ | 4.06E-08 | 21. min | 5.2 | 0.1 |
| Baseline | Desats | 14-Oct-19 12:00 | 0.01659 | 0.46600 | 0.00652 | $3.27 \mathrm{E}-05$ | $6.76 \mathrm{E}-07$ | $3.32 \mathrm{E}-07$ | 107.7 min | 26.7 | 0.4 |
| CBE | Desats | 14-Oct-19 12:00 | 0.01114 | 0.33810 | 0.00688 | $2.33 \mathrm{E}-05$ | $5.03 \mathrm{E}-07$ | $3.01 \mathrm{E}-07$ | 78.1 min | 19.4 | 0.4 |
| Predict 1 week |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 17-Oct-19 12:00 | 0.01299 | 0.65639 | 0.00126 | $4.74 \mathrm{E}-05$ | 7.01E-07 | $2.97 \mathrm{E}-07$ | 2.53 hr | 37.6 | 0.1 |
| CBE | None | 17-Oct-19 12:00 | 0.00431 | 0.22273 | 0.00123 | $1.61 \mathrm{E}-05$ | $2.34 \mathrm{E}-07$ | $1.00 \mathrm{E}-07$ | . 86 hr | 12.8 | 0.1 |
| Baseline | Desats | 17-Oct-19 12:00 | 0.01544 | 1.08200 | 0.00799 | $7.71 \mathrm{E}-05$ | $1.04 \mathrm{E}-06$ | $8.32 \mathrm{E}-07$ | 4.17 hr | 62.0 | 0.5 |
| CBE | Desats | 17-Oct-19 12:00 | 0.00970 | 0.81300 | 0.00750 | $5.75 \mathrm{E}-05$ | $8.27 \mathrm{E}-07$ | $7.52 \mathrm{E}-07$ | 3.13 hr | 46.6 | 0.4 |
| Predict 2 weeks |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 24-Oct-19 12:00 | 0.05982 | 1.98251 | 0.00298 | $1.47 \mathrm{E}-04$ | $9.73 \mathrm{E}-07$ | $9.27 \mathrm{E}-07$ | 7.64 hr | 113.6 | 0.2 |
| CBE | None | 24-Oct-19 12:00 | 0.02007 | 0.66615 | 0.00133 | $4.93 \mathrm{E}-05$ | $3.36 \mathrm{E}-07$ | $3.10 \mathrm{E}-07$ | 2.57 hr | 38.2 | 0.1 |
| Baseline | Desats | 24-Oct-19 12:00 | 0.09809 | 2.97300 | 0.01878 | $2.19 \mathrm{E}-04$ | $1.66 \mathrm{E}-06$ | $1.78 \mathrm{E}-06$ | 11.45 hr | 170.3 | 1.1 |
| CBE | Desats | 24-Oct-19 12:00 | 0.07545 | 2.20400 | 0.01841 | $1.62 \mathrm{E}-04$ | $1.74 \mathrm{E}-06$ | $1.45 \mathrm{E}-06$ | 8.49 hr | 126.3 | 1.1 |
| Predict 4 weeks |  |  |  |  |  |  |  |  |  |  |  |
| Baseline | None | 7-Nov-19 12:00 | 0.33541 | 6.77591 | 0.01586 | $6.01 \mathrm{E}-04$ | 1.37E-06 | 3.85E-06 | 26.1 hr | 388.2 | 0.9 |
| CBE | None | 7-Nov-19 12:00 | 0.11252 | 2.26719 | 0.00296 | $2.01 \mathrm{E}-04$ | $6.43 \mathrm{E}-07$ | $1.45 \mathrm{E}-06$ | 8.73 hr | 129.9 | 0.2 |
| Baseline | Desats | 7-Nov-19 12:00 | 0.50120 | 8.98400 | 0.04247 | $8.04 \mathrm{E}-04$ | $4.05 \mathrm{E}-06$ | $6.05 \mathrm{E}-06$ | 34.61 hr | 514.7 | 2.4 |
| CBE | Desats | 7-Nov-19 12:00 | 0.34060 | 6.10400 | 0.04374 | $5.46 \mathrm{E}-04$ | $5.39 \mathrm{E}-06$ | $6.73 \mathrm{E}-06$ | 23.51 hr | 349.7 | 2.5 |
|  | * Desats <br> † Assum | are approx. 3-4 d es circular orbit fo | begin on 10 apping trans | $19 \text { 12:00, }$ <br> se error di | $12 / 1912: 0$ <br> tly into tim | $10 / 15 / 19$ <br> g and dow | $: 00,10 / 18 /$ <br> rack pointin | $12: 00,10 /$ <br> errors | 21/19 12:00, | 10/24/19 12: |  |

The epoch of the data arc begins October 6, 2019. The date of the ODM which places the $\mathrm{S} / \mathrm{C}$ along the TAG trajectory was October 11, 2019 at 12:00 UTC and the DCO for this maneuver is 24 hours beforehand (Oct 10, 2019 12:00 UTC). Daily HGA telecom passes are assumed, where the S/C will slew to point the HGA towards Earth while keeping the Sun within the S/C's X-Z plane. In the safe-home orbit, these Earth contacts will be limited to 5 hours or less to ensure as stable thermal


Figure 10: Comparing the $1-\sigma$ filtered and predicted transverse state errors conditions as possible. This covariance analysis also evaluated the growth in the state errors in Table 4 from 1 day to 4 weeks after the DCO for both the baseline and CBE filter strategies assuming either no desat errors or with desats ( $\Delta \mathrm{V}$ errors of $0.5 \mathrm{~mm} / \mathrm{s}$ ) every 3 days over the predicted time. Since the transverse errors at the map time of 4 days or greater in the linear covariance analysis can be larger than the orbit radius, it is assumed that these errors map directly into orbit down-track timing or true anomaly errors in the $1-\mathrm{km}$ circular orbit. Thus, it will be a challenge to plan specific science observations 4 weeks ahead, since the predicted transverse errors approach the circumference of the $1-\mathrm{km}$ orbit of 6.3 km , which corresponds to a true anomaly error of $360^{\circ}$, i.e. the $\mathrm{S} / \mathrm{C}$ 's location in orbit is unknown after 4 weeks. The adopted strategy for targeting specific science observations requires late OD updates similar to ODM with DCO of 24-30 hours from the start of the observations. The CBE no-desat case improves the state errors by a factor of 2-3 of the baseline. Desat errors nearly double the baseline or triple the CBE no-desat case predicted transverse errors. Figure 10 compares the $1-\sigma$ transverse position and velocity filtered and predicted errors for the baseline and CBE filter cases. The baseline-filtered cases generally show position errors less than 1 m , while the CBE no-destat state errors are less than 50 cm . The reconstructed velocity errors for all cases are generally less than $0.1 \mathrm{~mm} / \mathrm{s}$.

## CONCLUSIONS

The mission plan for the OSIRIS-REx mission will require unprecedented levels of navigation performance, and will require the Operations teams to execute a rapid cadence of maneuvers and observation plans. This mission requires the OD-predicted S/C state errors during proximity operations with Bennu to be on the order of tens of meters. Requirements at these levels are a challenge to meet, especially since these are at least $1-2$ orders of magnitude lower than previous planetary or small body missions. It will also be challenging to meet the demanding ProxOps operations schedule, which requires frequent OD updates for maneuver designs or late science updates. Furthermore, at close range to Bennu, the on-board ephemeris needs frequent updates from the OD Team (at least twice per week) to ensure the asteroid remains within the FOV of the NavCam. It has been shown that the Detailed Survey longitudinal requirements are not yet met, even with CBE levels of non-gravitational forces or improved desat performance. The Navigation

Team is in discussions with the Science Team to better understand the impact of relaxing these requirements on the science observations planned during each Detailed Survey pass. The primary challenge during the Orbital-B phase is to characterize the non-gravitational forces at or below the $3 \mathrm{~nm} / \mathrm{s}^{2}$ level. Given that we can determine the non-gravitational errors to this level, the state errors predicted 24 hours after the DCO for the ODM have been shown to be within the requirements, which ensures a successful TAG attempt.

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## APPENDIX A: FILTER STRATEGY

| Error Source | Estimate, Consider or Observable | A Priori Uncertainty (10) | Correl ation Time | Update Time or Frequency | Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Tracking Data <br> X-Band 2-way Doppler ( $\mathrm{mm} / \mathrm{s}$ ) <br> X-Band Range (m) | Obs Obs | $\begin{gathered} \text { Baseline: } 0.1 \\ \text { CBE: } 0.073 \\ 3.333 \end{gathered}$ | - | - | $0.1 \mathrm{~mm} / \mathrm{s}=0.0055 \mathrm{~Hz}$, data deweighted for solar conj. (sep < 10 deg ) <br> $23.3 \mathrm{RU}(1 \mathrm{~m}=7.0 \mathrm{RU})$, data deweighted <br> for solar conj. (sep < 10 deg ) |
| OPNAV (Landmarks) Line/Pixel (pix) | Obs | $\mathbf{W}=\left(\mathbf{W}_{\text {min }}^{2}+(\mathbf{S} / \mathbf{R})^{2}\right)^{1 / 2}$ <br> Orbit-B Safe-home 3.3-3.6 | - | - | $\mathrm{W}_{\text {min }}=1 \mathrm{pix}, \mathrm{S}=75 \mathrm{~cm}$ (shape model error), $\mathbf{R}=$ camera resolution |
| Spacecraft Trajectory Models Epoch state position (km) Epoch state velocity (km/s) | Estimate Estimate | $\begin{gathered} 5000 \\ 0.5 \end{gathered}$ | - |  | Earth, Sun or Bennu-Centered ICRF Cartesian |
| Solar Radiation Pressure Coefficient (\% of total) | Estimate | 20 | - | - | GR (or SOLCOF) |
| Non-Grav Acceleration (km/s ${ }^{\text {2 }}$ ) | Estimate | Baseline: 3.00E-12 per axis CBE: $3 \mathrm{e}-12$ in sun dir, 1e-12 radial, transverse | 0 | 1 day | Baseline: assumes $8 \%$ SRP in all axes CBE: assumes calibration of transverse and radial components |
| AMD Event $\Delta \mathbf{V}$ ( $\mathrm{mm} / \mathrm{s}$ ) | Estimate | $2 \mathrm{~mm} / \mathrm{s}$ for $\mathbf{1 0 - d a y}$ freq. <br> $0.5 \mathrm{~mm} / \mathrm{s}$ for 3 -day freq. <br> CBE used in DS: $<0.1 \mathrm{~mm} / \mathrm{s}$ | - | - | Per axis, Impulsive $\Delta \mathbf{V}$ |
| Data biases and other info Range Bias (m) | Estimate | 4 | 0 | Per pass | RSS of DSN and S/C errors |
| Number of landmarks (in view of opnav) |  | Baseline: 7-10 CBE: 17-21 | - | - | Total landmarks in simulation: Baseline:40 CBE: 100 |
| Camera Pointing (deg) | Estimate | Baseline: $\mathrm{S} / \mathrm{C}$ 's CBE(1sig): 1.1 mrad boresight 1.01 mrad roll CBE: Post-SPC( 1 sig): 0.42 mrad boresight 0.47 mrad roll | - | Per OpNav image | Assume Rayleigh distribution for per axis errors (3-sig boresight error/3.439), Scale RA error by $1 / \cos (\mathrm{dec})$ |
| Ephemerides <br> Earth/Moon Barycenter Ephemeris | Consider | JPL DE425 Covariance | - | - | Set III parameters |
| Bennu Ephemeris Epoch state position (km) Epoch state velocity (km/s) | Estimate <br> Estimate | JPL Soln \#76 correlated covariance | - | - | Set III parameters <br> ( 1 X formal statistics). Formal position error on approach $\sim 10 \mathrm{~km}$. |
| Gravity <br> Earth GM ( $\mathbf{k g}^{\mathbf{3}} \mathbf{k m}^{2}$ ) <br> Lunar GM ( $\mathbf{k g}^{3} / \mathbf{k m}^{2}$ ) <br> Bennu GM ( $\mathbf{k g}^{\mathbf{3}} / \mathbf{k m}^{2}$ ) <br> Earth Gravity Field Lunar Gravity Field Bennu Gravity Field | Consider Consider <br> Estimate <br> Consider Consider <br> Estimate | $1.40 \mathrm{E}-03$ <br>  <br> Prelim. Survey, 10\% afterwards $(5.2 \mathrm{e}-9-5.2 \mathrm{e}-10)$ <br> 4x4, Kaula power law based on Bennu |  |  | Nominal GM =5.2 e-9 kg3/km2 <br> Correlated covariance from JGM-3 <br> Correlated covariance from LP150Q <br> Based on current range of errors in shape <br> model. [McMahon, 2015] |
| Measurement Models <br> Station Locations (km, deg, km) <br> Earth Pole X, Y (cm) <br> UT1 (cm) <br> lonosphere - day / night (cm) <br> Troposphere - wet / dry (cm) | Consider <br> Consider <br> Consider <br> Consider <br> Consider | JPL 2003 full correlated Covariance $\begin{gathered} 10.0 / 10.0 \\ 10 \\ 55.0 / 15.0 \\ 1.0 / 1.0 \\ \hline \end{gathered}$ |  |  | Stations 15, 45, 65 used in cov studies (2-5 cm each axis) <br> 15 nanoradians <br> 0.256 msec <br> S-band values (MIRAGE input) eqv to 15, 4 cm for X-band |
| ```Bennu Orientation Model (Principal axis rotation) Pole RA, Dec (deg) Prime Meridian (deg) Spin (deg/s)``` | Estimate Estimate Estimate | $\begin{gathered} 10,10 \\ 100 \\ 1.20 \mathrm{E}-03 \end{gathered}$ |  |  | 100 deg/day |


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