National Aeronautics and Space Administration



Fast Kalman Filtering for Relative Spacecraft Position and Attitude Estimation for the Raven ISS Hosted Payload

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Spacecraft Servicing

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Want to service existing spacecraft:

- Inspect
- Repair
- Refuel
- Relocate

Existing spacecraft present navigation challenges:

- No laser retroreflectors
- No visual fiducials

Unmanned servicing spacecraft must perform rendezvous and docking autonomously!

- Communication delays preclude
 ground control
- Must have accurate navigation solution with sufficient bandwidth for closed loop control



Notional robotic servicing operation rendering

Raven: Relative Navigation Testbed



- ISS hosted payload
 - Anticipating June 2016 launch as part of the DoD Space Technology Program (STP-H5)
 - Mount on port nadir side of ISS
 - Next to solar array rotation joint
 - ISS provides power and comm
- Mission objectives
 - Track ISS resupply vehicles
 - Collect resupply vehicle imagery
 - Visual
 - Infrared
 - LIDAR

• Challenges

- Command and telemetry outages require autonomous pan/tilt tracking
- Raven gets no real-time data from ISS
 - No ISS navigation state
 - No GPS measurements
 - We DO get a clock pulse
- 16 months from project authorization to hardware delivery





- Resupply vehicles provide relative navigation solution for their prox ops maneuvers, monitored by ISS mission control and ISS crew
- Resupply vehicles must use their own relative navigation sensor suite and associated computation, incurring cost and design complexity
- ISS does not produce its own relative navigation solution
- Raven is a prototype of a new paradigm:
 - Air traffic control uses local radars to monitor airspace
 - A relative navigation sensor suite would allow ISS to monitor its nearby space and even provide relative navigation solutions to visiting vehicles

Raven Location



- Multiplicative Extended Kalman Filter (MEKF) formulation tracks relative pose = translation and orientation
 - MEKF formulation explicitly maintain quaternion constraints
 - Extension of MEKF to pose is similar to Junkins, Geller, Tweddle
- Raven includes a GSFC SpaceCube 2.0 flight processor
 - fast and powerful multi-core flight computer with FPGA
- Demanding filter rates
 - Pointing controller requires frequent filter estimate updates
 - Pose measurements from computer vision available at high rate
- Information available:
 - Relative pose from optical sensors
 - Inertial attitude and rate from star tracker and gyro
 - NO orbital information in real-time (neither ISS solutions nor raw GPS)
- Focus on what information is available
 - No orbital information precludes a Clohessy/Wiltshire or higher fidelity dynamics model
 - Relative pose measurements are frequent and well modeled
 - Account for camera rotation using star tracker and gyro (separate filter)

RNF Block Diagram





RNF Translation States



Filter State





Combining the above yields:

$$\dot{\boldsymbol{v}} pprox -2\boldsymbol{\omega}_{_{RVN}/_{ECI}}^{^{RVN}} imes \boldsymbol{v} + W_{_{tran}} \boldsymbol{w}_{_{tran}}$$

RNF Rotation States



Filter State

Definition



$$oldsymbol{q}_{_{VV}/_{RVN}} = oldsymbol{q}_{_{VV}/_{ECI}} \otimes oldsymbol{q}_{_{RVN}/_{ECI}}^{^{-1}}$$

Kinematics

 \dot{q}

Dynamics

$${}^{ECI} \frac{d}{dt} \boldsymbol{\omega}_{VV/ECI}^{VV} = J^{-1} \left(\left(J \boldsymbol{\omega}_{VV/ECI}^{VV} \right) \times \boldsymbol{\omega}_{VV/ECI}^{VV} \right) + W_{rot} \boldsymbol{w}_{rot}$$

$$W_{_{rot}} \boldsymbol{w}_{_{rot}} \sim \mathcal{N}\left(\boldsymbol{0}, W_{_{rot}} W_{_{rot}}^{^{T}}
ight)$$

RNF Measurement Bias States



Each sensor bias is assumed to be an independent first order Gauss Markov process

$$\dot{b}_{_{j}} = -\frac{1}{\tau_{j}}b_{_{j}} + \sigma_{_{j}}w_{_{j}} \qquad \qquad \sigma_{_{j}}w_{_{j}} \sim \mathcal{N}\left(0,\sigma_{_{j}}^{^{2}}\right)$$

Linearized Error State Dynamics





Linearized Error State Dynamics derived in paper (linear time varying system)

$$\Delta \dot{\boldsymbol{x}} = F \Delta \boldsymbol{x} + W \boldsymbol{w}$$

First order approximation used to compute error state transition matrix

$$\Phi(\Delta t) = \mathbb{I} + \Delta tF + \frac{\Delta t^2}{2!}F^2 + \dots$$
$$\approx \mathbb{I} + \Delta tF$$

Process noise matrix preserves kinematic constraints

$$Q(\Delta t) = E\left\{\left[\int_{t-\Delta t}^{t} \Phi\left(t-\epsilon\right) W \boldsymbol{w}(\epsilon) d\epsilon\right] \left[\int_{t-\Delta t}^{t} \Phi\left(t-\eta\right) W \boldsymbol{w}(\eta) d\eta\right]^{T}\right\}$$

Translation Measurement Component



Pose measurements from sensor CAM are denoted $\left(\tilde{r}_{_{VV}/_{_{RVN},CAM}}^{_{VV}}, \tilde{q}_{_{VV'}/_{_{RVN},CAM}} \right)$

The translation component is modeled as:

 $\tilde{\boldsymbol{r}}_{VV/_{RVN},CAM}^{VV} = \boldsymbol{r}_{VV/_{RVN}}^{VV} + \boldsymbol{b}_{CAM,tran} + M_{CAM,tran} \boldsymbol{m}_{CAM,tran}$ measurement true FOGM bias Gaussian white noise

Where the First Order Gauss Markov Bias is as given before:

$$\dot{b}_{_{CAM,tran}} = -\begin{bmatrix} 1/\tau_{_{1}} & & & \\ & 1/\tau_{_{2}} & & \\ & & & 1/\tau_{_{3}} \end{bmatrix} b_{_{CAM,tran}} + \begin{bmatrix} \sigma_{_{1}} & & & \\ & \sigma_{_{2}} & & \\ & & & \sigma_{_{3}} \end{bmatrix} w_{_{b,CAM,tran}}$$

Resulting in the translation component innovation:

$$\begin{split} \Delta \boldsymbol{r}_{\scriptscriptstyle CAM}^{\scriptscriptstyle innov} &= \boldsymbol{\tilde{r}}_{\scriptscriptstyle VV/_{\scriptstyle RVN}, CAM}^{\scriptscriptstyle VV} - \boldsymbol{\hat{r}} - \boldsymbol{\hat{b}}_{\scriptscriptstyle CAM, tran} \\ &= \Delta \boldsymbol{r} + \Delta \boldsymbol{b}_{\scriptscriptstyle CAM, tran} + M_{\scriptscriptstyle CAM, tran} \boldsymbol{m}_{\scriptscriptstyle CAM, tran} \end{split}$$



Rotation Measurement Component



Pose measurements from sensor CAM are denoted $\left(\tilde{r}_{_{VV}/_{RVN},CAM}^{_{VV}}, \tilde{q}_{_{VV'}/_{RVN},CAM}^{_{VV}} \right)$

The rotation component is modeled as:

$$\tilde{\boldsymbol{q}}_{_{VV'}/_{RVN},CAM} = \boldsymbol{q} \left(\boldsymbol{b}_{_{CAM,rot}} + \boldsymbol{M}_{_{CAM,rot}} \boldsymbol{m}_{_{CAM,rot}} \right) \otimes \boldsymbol{q}_{_{VV}/_{RVN}}$$

measurement FOGM bias Gaussian white noise

Where the First Order Gauss Markov Bias is as given before:

$$\dot{\boldsymbol{b}}_{_{CAM,rot}} = -\begin{bmatrix} 1/\tau_{_{4}} & & & \\ & 1/\tau_{_{5}} & & \\ & & & 1/\tau_{_{6}} \end{bmatrix} \boldsymbol{b}_{_{CAM,rot}} + \begin{bmatrix} \sigma_{_{4}} & & & \\ & \sigma_{_{5}} & & \\ & & & \sigma_{_{6}} \end{bmatrix} \boldsymbol{w}_{_{b,CAM,rot}}$$

The orientation component innovation is a bit more involved:

$$\begin{split} \Delta \boldsymbol{q}_{CAM}^{innov} &= \boldsymbol{q}^{-1} \left(\boldsymbol{\hat{b}}_{CAM,rot} \right) \otimes \boldsymbol{\tilde{q}}_{VV'/_{RVN},CAM} \otimes \boldsymbol{\hat{q}}_{VV/_{RVN}}^{-1} \\ &= \boldsymbol{q}^{-1} \left(\boldsymbol{\hat{b}}_{CAM,rot} \right) \otimes \boldsymbol{q} \left(\boldsymbol{b}_{CAM,rot} + \boldsymbol{M}_{CAM,rot} \boldsymbol{m}_{CAM,rot} \right) \otimes \Delta \boldsymbol{q} \\ \Delta \boldsymbol{g}_{CAM}^{innov} &= \boldsymbol{g} \left(\Delta \boldsymbol{q}_{CAM}^{innov} \right) \approx \Delta \boldsymbol{g} - \Delta \boldsymbol{b}_{CAM} + \boldsymbol{M}_{CAM,rot} \boldsymbol{m}_{CAM,rot} \end{split}$$



true

EKF Measurement Update Procedure

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for k=1,2,3,... do **Propagate State Estimate to Measurement Time** $\hat{x}_{k}^{-} = \hat{x}_{k-1}^{+} + \int_{t_{k-1}}^{t_{k}} f(x(\tau), \tau) d\tau$ (note $\Delta \hat{\boldsymbol{x}}_{\mu_{-1}}^{+} = \boldsymbol{0}$, so $\Delta \hat{\boldsymbol{x}}_{\mu_{-1}}^{-} = \Phi_{\mu} \Delta \hat{\boldsymbol{x}}_{\mu_{-1}}^{+} = \boldsymbol{0}$) **Propagate State Covariance to Measurement Time** compute Φ_{μ} and Q_{μ} $P_{\mu}^{-} = \Phi_{\mu}P_{\mu}^{+}, \Phi_{\mu}^{T} + Q_{\mu}$ Perform Measurement Update compute H_{μ} $K_{k} = P_{k}^{-}H_{k}^{T} \left(H_{k}P_{k}^{-}H_{k}^{T} + R_{k}\right)^{-}$ $P_{k}^{+} = (I - K_{k}H_{k})P_{k}^{-}(I - K_{k}H_{k})^{T} + K_{k}R_{k}K_{k}^{T}$ $\Delta \hat{\boldsymbol{x}}_{_{k}}^{+} = \Delta \hat{\boldsymbol{x}}_{_{k}}^{-} + K_{_{k}} \left(y_{_{k}} - \boldsymbol{h} \left(\hat{\boldsymbol{x}}_{_{k}}^{-}, t_{_{k}} \right) \right)$ Transfer Information to State Estimate, Reset Error Estimate $\hat{\boldsymbol{x}}_{\mu}^{+} = \hat{\boldsymbol{x}}_{\mu}^{-} + \Delta \hat{\boldsymbol{x}}_{\mu}^{+}$ $\Delta \hat{\boldsymbol{x}}_{L}^{+} = \boldsymbol{0}$ end

EKF Measurement Update Procedure

NASA

for k=1,2,3,... do **Propagate State Estimate to Measurement Time** $\hat{x}_{k}^{-} = \hat{x}_{k-1}^{+} + \int_{t_{k-1}}^{t_{k}} f(x(\tau), \tau) d\tau$ (note $\Delta \hat{\boldsymbol{x}}_{\mu_{-1}}^{+} = \boldsymbol{0}$, so $\Delta \hat{\boldsymbol{x}}_{\mu_{-1}}^{-} = \Phi_{\mu} \Delta \hat{\boldsymbol{x}}_{\mu_{-1}}^{+} = \boldsymbol{0}$) **Propagate State Covariance to Measurement Time** compute Φ_{μ} and Q_{μ} $P_{\mu}^{-} = \Phi_{\mu}P_{\mu}^{+}, \Phi_{\mu}^{T} + Q_{\mu}$ Perform Measurement Update compute H_{μ} $K_{k} = P_{k}^{-} H_{k}^{T} \left(H_{k} P_{k}^{-} H_{k}^{T} + R_{k} \right)^{T}$ $P_{k}^{+} = \left(I - K_{k}H_{k}\right)P_{k}^{-}\left(I - K_{k}H_{k}\right)^{T} + K_{k}R_{k}K_{k}^{T}$ $\Delta \boldsymbol{\hat{x}}_{_{k}}^{^{+}} = \Delta \boldsymbol{\hat{x}}_{_{k}}^{^{-}} + K_{_{k}}\left(y_{_{k}} - \boldsymbol{h}\left(\boldsymbol{\hat{x}}_{_{k}}^{^{-}}, t_{_{k}}
ight)
ight)$ Transfer Information to State Estimate, Reset Error Estimate $\hat{\boldsymbol{x}}_{k}^{+} = \hat{\boldsymbol{x}}_{k}^{-} + \Delta \hat{\boldsymbol{x}}_{k}^{+} \\ \Delta \hat{\boldsymbol{x}}_{k}^{+} = \boldsymbol{0}$ end equivalent $egin{aligned} \hat{m{x}}_{k}^{+} &= \hat{m{x}}_{k}^{-} + K_{k}\left(m{y}_{k}^{-} - m{h}\left(\hat{m{x}}_{k}^{-}, t_{k}^{-}
ight)
ight) \end{aligned}$

MEKF Measurement Update Procedure



- Same paradigm as the (cumbersome version) of an EKF
- Quaternion update makes this an MEKF a la Lefferts, Markley, and Shuster
- Inclusion of translation states in an MEKF already in the literature
 - Kim, Crassidis, Cheng, Fosbury, Junkins
 - Woffinden, Geller
 - Tweddle, Saenz-Otero
- We augment with biases



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- Can't instantaneously solve for all sensor biases AND relative pose

IR Camera

VIS Camera

LIDAR















- Relative dynamics aren't "rich enough" to correctly solve over time
- Instead, only solve for N-1 sensor biases

Observability Issue Resolved

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- Relative dynamics aren't "rich enough" to correctly solve over time
- Instead, only solve for N-1 sensor biases



Raven Development Montage









Raven_dragon_rend_gn firTrack_fov35.mp4 goes here, shows GNFIR tracking synthetic imagery of SpaceX Dragon in complicated lighting

Questions?



- Raven_fsp_CDR_viscam.mp4 goes here
 - Freespace rendering showing third person perspective as well as Raven perspective
 - SpaceX Dragon rendezvous
 - Synthetic imagery shows ISS shadow on Dragon