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A new and simple water retention model for root-permeated soils

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ABSTRACT

Vegetation affects the soil hydrology through not only evapotranspiration (ET) but also changes in soil water retention curve (SWRC). There are only limited models which are able to predict root-induced change in SWRC. These models often contain many empirical parameters that are not easy to be obtained and calibrated. This letter proposes a new and simple model with only one root parameter, namely root volume ratio $R_v$, needed for predicting SWRC of a root-permeated soil. The new model considers void ratio change through the volume reduction of air void of soil due to the presence of roots. The modified void ratio of a root-permeated soil is then fed into a void ratio-dependent SWRC model to predict any resulted change in SWRC. The performance of this new model is validated against three case studies. Good agreement between measurements and predictions is obtained, with discrepancies of degree of saturation less than 13% for a given suction.

KEY WORDS: Partial saturation; Suction; Vegetation
INTRODUCTION

The presence of vegetation is known to affect the hydrology and, hence, stability of some major civil infrastructure such as man-made slopes/embankments (Osman and Barakbah, 2011; Scanlon et al., 2011; Smethurst et al., 2015; Ng et al., in press). Past studies have been carried out to investigate the effects of plant evapotranspiration (ET) on the changes in soil moisture content or soil suction through field monitoring (Lim et al., 1996; Simon & Collison, 2002; Pollen-Bankhead and Simon, 2010; Leung & Ng, 2013; Leung et al., 2015a), laboratory studies (Fan and Su, 2009; Ng et al., 2013, 2014; Garg et al., 2015; Leung et al., 2015b; Veylon et al., 2015) and numerical or/and analytical modelling (Indraratna et al., 2006; Zhu & Zhang, 2014; Ng et al., 2015).

In addition to plant ET, some existing studies suggest that the presence of plant roots in soil could directly affect soil hydraulic properties. Field and laboratory tests (Gabr et al., 1995; Huat et al., 2006; Aravena et al., 2011; Ng et al., 2014; Leung et al., 2015b) have evidently showed that vegetated soil has lower water infiltration rate and enhanced water retention capacity than bare soil. The root-induced change in soil hydraulic properties is arguably attributed to the alteration of soil structures, predominantly due to occupancy of roots in soil pore space (Scanlan & Hinz, 2010; Scholl et al., 2014; Leung et al. 2015b), which consequently leads to changes in soil pore size and, hence, soil water retention curve (SWRC; Romero et al., 1999; Ng & Pang, 2000; Ng & Leung, 2012). However, it should be noted that such soil-root-water interaction might be different in fine-grained soils. Veylon et al. (2015) revealed that root growth in clayey soils influences the frequency and magnitude of drying-wetting cycles and consequently the formation of soil aggregates.

Quantifying root-induced modification in soil hydraulic properties, including SWRC, are vital to more correctly predict the hydrology and, hence, assess the stability of the civil infrastructure.
subjected to rainfall. Such root-induced modification is especially prominent for the case under high relative humidity (RH; i.e., low vapour pressure deficit) and cloudy condition (i.e., minimal supply of radiation), during which any suction induced by plant ET and root osmotic action are practically negligible (Sidle et al., 1985; Snyder et al., 2003). To date, there are only a few models, which may capture root-induced change in SWRC. Scanlan (2009) and Scanlan & Hinz (2010) proposed a conceptual model to capture the reduction in soil pore size by idealising soil pore throats as a bundle of cylindrical tubes containing plant roots. Their model considers that the presence of a root reduces the effective diameter of a pore throat and this, in turn, increases the height of capillary water and enhances matric suction. This model requires 13 parameters, some of which are empirically-based and cannot be easily obtained in a test. Scholl et al. (2014) determined a set of pore size parameters to deduce root-induced change in SWRC through inverse analyses of column tests, where changes in soil moisture and suction of vegetated soil were monitored. Physical meaning of the back-analysed SWRC parameters is not clear, because these parameters can be heavily affected by the subjective choices of their initial values and the parameter searching algorithm of the inverse analysis.

This letter proposes a new and simple model of SWRC for root-permeated soils. This model was then validated by three case studies.

**NEW WATER RETENTION MODEL FOR ROOT-PERMEATED SOIL**

The new model considers that plant roots occupy some soil pore space and, hence, reduce soil pore size. Considering the mass-volume relationship and phase diagram of an unsaturated soil where part of its air void is occupied by plant roots (Fig.1), the void ratio of a root-permeated soil may be expressed by the following equation:
\[ e = \frac{e_0 - R_v(1+e_0)}{1 + R_v(1+e_0)} \]  

(1)

where \( e_0 \) is the void ratio of bare soil [-], \( R_v \) is the root volume ratio [\( \text{mm}^3/\text{mm}^3 \)], which is defined as the total volume of roots per unit volume of soil. \( R_v = 0 \) means that there are no plant roots in the soil (i.e., bare soil). \( R_v \) is less than \( e_0/(1+e_0) \), as total root volume cannot be larger than the total soil pore size. Depending on the plant type, \( R_v \) is a function of depth within root zone. It should be noted that it is not the intention of this study to model any effects of root decay, and the associated formation of macro-pores (Ghestem et al., 2011), on the change in soil void ratio. Furthermore, for simplicity, the proposed model does not consider any change of soil microstructure (i.e., micro-cracks development and aggregates formation) during drying-wetting cycles. The proposed model is thus more suitable for low plasticity soils such as sands and/or silts.

In order to model the effects of the presence of roots on the change in water retention ability of a soil, the void ratio-dependent SWRC equation proposed by Gallipoli et al. (2003) may be adopted:

\[ S_r = \left[ 1 + \left( \frac{se^{s_\infty}}{m_4} \right)^{m_2} \right]^{-m_1} \]  

(2)

where \( S_r \) is the degree of saturation of soil; \( s \) is the matric suction; and \( m_1 [-], m_2 [-], m_3 [\text{kPa}], m_4 [-] \) are the model parameters. \( m_1 \) and \( m_2 \) control the shape of a SWRC (van Genuchten, 1980), while \( m_3 \) and \( m_4 \) are related to the air-entry value (AEV) of the parent soil. Considering that the void ratio has negligible effects on SWRC at high suction range, the product, \( m_1 m_2 m_4 \), can be set to 1 (Gallipoli et al., 2003). Therefore, by knowing the SWRC of the parent soil and the root parameter, \( R_v \), SWRC of root-permeated soil can be predicted.

**VALIDATION OF THE NEW MODEL**
In order to validate the new SWRC model, field and laboratory tests are conducted to obtain all necessary parameters. In addition, the laboratory test data reported by Leung et al. (2015b) is also selected for validation. Although there are some limited case studies that also show the SWRCs of both bare and root-permeated soil (Rahardjo et al., 2014; Yan & Zhang, 2015), the root parameter, $R_v$, is not reported. These case histories thus cannot be used for validation of this study.

**Test plan and procedures**

The field tests were double-ring infiltration tests conducted at a site called Eco-Park in Hong Kong (Fig. 2(a)). A flat soil bed was constructed by compacting a 2 m-thick layer of completely decomposed granite (CDG; silty sand), until a relative compaction of 95% (i.e., dry density of 1777 kg/m$^3$) was reached. Two rings with diameters of 0.6 and 0.3 m were inserted into the ground by 150 and 75 mm depth, respectively. Any gapping between the ground and the two rings was sealed with cement paste. Inside both rings, 19 seedlings of *Schefflera heptaphylla* were transplanted to the soil bed in the uniform pattern and were irrigated every two days for four months for root establishment prior testing (Wang et al., 2007). The leaf area index, which is a dimensionless index indicating the total area of leaves over the projected planar area of plant canopy, of this species was $1.8 \pm 0.2$. Three pairs of moisture probes and tensiometers were installed at 100, 250 and 400 mm depths at the middle of the rings for monitoring the responses of soil moisture content and suction, respectively. When plant roots were established, a constant ponding head of 100 mm was applied inside both rings. Changes in soil moisture and suction were monitored continuously until the steady state was reached. The vegetated soil bed was then allowed for natural evapotranspiration, during which the changes in soil water content and suction at 100 mm (i.e., within the root zone) were measured to determine the
SWRC of root-permeated soil. After testing, the plant roots were excavated to obtain \( R_v \) using an image-based analysis (Himmelbauer et al., 2004). The root zone was divided into several horizontal layers along root depth. An average \( R_v \) value was determined for each layer. In order to account for any plant variability, three repeated tests (i.e., 57 seedlings in total) were conducted. The above test procedures were repeated for soil bed without vegetation, for determining SWRC of bare soil.

The laboratory tests were carried out at a temperature- and humidity-controlled plant room. The same type of CDG was compacted in a steel drum in 15 layers (600 mm in diameter; see Fig. 2(b)), until a relative compaction of 95% (i.e., dry density of 1777 kg/m\(^3\)) was reached. In total, 13 seedlings of \( S. \) heptaphylla were transplanted to the compacted CDG uniformly. The method of root establishment, instrumentation and the test procedures to obtain SWRCs were identical with the field tests described above. Three test replications for bare and vegetated soils were examined (i.e., 39 seedlings in total).

Leung et al. (2015b) conducted a similar laboratory test to those carried out in this study, using the identical soil type and plant type. The tests were performed in the same plant room. The only differences were that in Leung et al. (2015b), (i) the tests were for one single tree, and (ii) the relative compaction of the soil adopted was 80%. Similarly, three test replications were performed.

**Observed root characteristics**

Overview of the root systems of some typical tree seedlings tested in the field and laboratory studies is shown in Fig. 3. It can be generally seen that the roots growing from the bottom of tree stem are predominantly fresh roots, which is displayed as whitish colour (MaCrady & Comerford, 1998). No observable decayed roots are found. These root characteristics satisfy the conditions and assumptions
stated in the proposed SWRC model and, hence, can be used for validation.

Fig. 4 shows the measured distribution of $R_v$ of the *S. heptaphylla* obtained from the three cases. Note that the vertical axis is the depth normalised with the maximum root depth in each corresponding case. It can be seen that the $R_v$ for both the field and laboratory tests conducted in this study distributes non-linearly along depth, exhibiting a parabolic shape. A peak value of $R_v$ of about 0.032 and 0.034 mm$^3$/mm$^3$ is identified near the mid-depth of the root zone. On the contrary, the distribution of $R_v$ obtained from Leung *et al.* (2015b) is rather different and it is approximately linear, with a peak value of about 0.065 mm$^3$/mm$^3$ near the soil surface. The SWRC of root-permeated soil in each case is evaluated at the depth, where the instruments were installed. The depth of evaluation and the corresponding value of $R_v$ in each case are summarised in Table 1.

**Performance of the new model**

Figs 5(a) to (c) show the measured SWRC of bare soil tested in each case. Each SWRC is fitted with Eq. (2) to calibrate the coefficients, $m_1$, $m_2$, $m_3$ and $m_4$ (see Table 1). Based on these coefficients and the root parameter $R_v$, SWRC of root-permeated soil is predicted and compared with the respective measurements (including all replicates). Good agreement between the measurement and prediction can be generally seen in all three cases. At any given suction, the maximum discrepancy of $S_r$ is less than 13%. It can be consistently seen that in all three cases, the presence of roots caused an increase in air-entry value (AEV), while the desorption rate does not show significant change. The AEV increased from 1 to 3 kPa for both the field and laboratory tests conducted in this study. Similarly, Leung *et al.* (2015b) also reported an increase in AEV by 4 kPa in their laboratory study. The similar SWRC change due to the presence of roots is also found in the test data presented by Rahardjo *et al.*
(2014) and Yan & Zhang (2015), who report an increase in AEV by 4 kPa in silty soils and 3 kPa in sandy soils, respectively. The observed increase in AEV, from both the measurements and prediction, is an indication of the increase in water retention capacity due to the presence of roots in soil pore space. This is in line with the experimental observation made by Romero et al. (1999) and Ng & Pang (2000), who also show that a decrease in void ratio of bare soil (i.e., denser soil) would possess a higher AEV.

CONCLUSIONS

A new and simple SWRC model was developed for root-permeated, low plasticity soils such as sands and silts, which do not show significant soil microstructural changes during drying-wetting cycles. This model can capture the reduction of soil void ratio due to the presence of roots in the air void of soil. Totally the model requires five parameters: four for describing the SWRC of the parent soil (without any vegetation) and one for characterising a root property, namely root volume ratio. The performance of this new model is verified by a laboratory test reported in literature and two new additional field and laboratory studies. The model illustrates its capability of predicting SWRC of silty sand vegetated with a tree species, S. heptaphylla, reasonably well. Moreover, it is able to capture a substantial increase in soil air-entry value (AEV) due to the presence of roots. The maximum discrepancy of degree of saturation is less than 13%, for a given suction.

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LIST OF NOTATIONS

AEV  Air entry value
CDG  Completely Decomposed Granite
ET   Evapotranspiration
SWRC Soil Water Retention Curve

$R_v$  Root volume ratio
$S_r$  Degree of saturation
$e$    Void ratio
$e_0$  Void ratio of bare soil

$m_1$  Fitting parameter in Gallipoli’s equation (Gallipoli et al., 2003)
$m_2$  Fitting parameter in Gallipoli’s equation (Gallipoli et al., 2003)
$m_3$  Fitting parameter in Gallipoli’s equation (Gallipoli et al., 2003)
$m_4$  Fitting parameter in Gallipoli’s equation (Gallipoli et al., 2003)

$s$   Suction

$\theta$ Volumetric water content
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Fig. 4. Measured distributions of $R_v$ with depth

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<table>
<thead>
<tr>
<th>Test</th>
<th>Parameters for Eq. (2)</th>
<th>Depth</th>
<th>$R_v$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$m_1$ [-]</td>
<td>$m_2$ [-]</td>
<td>$m_3$ [kPa]</td>
</tr>
<tr>
<td>This study (Field)</td>
<td>0.11</td>
<td>2.5</td>
<td>0.30</td>
</tr>
<tr>
<td>This study (Laboratory)</td>
<td>0.15</td>
<td>1.9</td>
<td>0.18</td>
</tr>
<tr>
<td>Leung et al. (2015b)</td>
<td>0.04</td>
<td>8.6</td>
<td>0.70</td>
</tr>
</tbody>
</table>
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