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A Foundation for Multi-Level Modelling

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Abstract. Multi-level modelling allows types and instances to be mixed in the same model, however there are several proposals for how meta-models can support this. This paper proposes a meta-circular basis for meta-modelling and shows how it supports two leading approaches to multi-level modelling.

1 Introduction

Contemporary and future engineering of information systems place an increasing emphasis on the use of models, either directly to aid design and implementation, in a more formal sense for code generation or as the backbone to model-driven engineering (MDE) [27]. Models must be described using a language that itself may be defined in many ways but typically using a meta-model e.g., [26, 20]. That meta-model must itself be defined, by a meta-meta-model. Together with the instances conformant to the model, this leads to an identification of four abstraction levels of interest to the modeller and meta-modeller. Although in use for almost two decades, a four-layer architecture like that of the Object Management Group (OMG) raises some concerns both theoretically and pragmatically; a prime problem being the use of strict meta-modelling [5, 4] that constrains the instance-of relation to only be permitted between pairs of conterminous layers and never within a layer (see also [5]). This led several researchers (e.g., [7, 6]) to seek a way of describing models and modelling languages without the use of this ‘strict meta-modelling’ hierarchy of the OMG.

A foundation for meta-modelling should be unifying and complete in the sense that it supports the development of both general-purpose and domain-specific languages and also integrates their representation so that tools can work across multiple languages. Leading approaches include: strict meta-modelling: The OMG strict meta-modelling architecture has been criticized, especially when applied to processes and methodologies (see summary in [18]) since the traditional strict meta-modelling approach is unable to support enactment e.g., [2]; it defines attributes at level M2, thus giving them values at M1 by virtue of the prevailing type-instance semantics, when what is actually needed is values at M0. This enactment support is provided by the architecture used by ISO/IEC 24744 but at the expense of relying on power-type patterns, which do not accord
with the philosophy of strict meta-modelling. **Clabjects**: Potency is associated with the notion of deep instantiation, [8, 12, 13], and introduces the idea of an entity with both a class facet and an object fact, entity given the name clabject [5]. **OCA**: Two different kinds of meta-model structures have been identified: ontological meta-modelling in contrast to the linguistic meta-modelling utilized in a strict meta-modelling architecture. This was later called the Orthogonal Classification Architecture (OCA) [9]. In [22] we describe these ideas and relate them to some more recent concerns raised by the application of language use theory to this approach. More recently, Atkinson and colleagues have extended the OCA in their description of the Pan Level Model (PLM) and the Level-agnostic Modeling Language (LML) [7]. **Powertypes**: The need to provide access to, and control over, the meta-types of elements in a model when designing languages led to proposals for powertypes [17, 23]. This is a methodological approach that uses standard classes both conventionally and as meta-classes by disciplined use of instance-of associations. The approach allows the modeller to control attribute definitions at M2 that affect the properties in model elements at M1.

Our claim is that none of the approaches above are complete as a basis for meta-modelling. In particular, such a basis must achieve the following features: **Meta-Circularity**: Self description is key to achieving virtually all of the desirable features for language engineering. Just as it is possible to embed a \(\lambda\)-calculus interpreter in itself and thereby characterize an infinite tower of operational languages, we seek to construct a self describing basis for an infinite tower of modelling languages. **Uniformity**: Any basis for meta-modelling that is self-describing implies a precisely defined relation between representations for type and instance. A system that achieves the conflation of these representations, *i.e.*, uses the identity relationship, is minimal in the family of such relationships. Furthermore, a uniform representation is essential if we are not to encounter limitations on the type of languages that can be defined, for example where we need to mix instances and types. Therefore, we seek to provide a single representation for types and instances at any level. **Extensibility**: We assume that any family of modelling languages will use type-based extension (sub-classes, inheritance, etc.), and that new languages are based on extending existing languages. Meta-circularity and extensibility implies that languages can be extended at both type and meta-type levels and therefore the question arises as to whether there is a limit to the levels over which extension can be applied. We seek a basis that places no restriction on the number of levels of both extensibility and instantiation. **Views**: Languages should support multiple modes of interaction that are defined at the meta-level. Although we will use multiple language views, we will not consider this aspect further.

Our approach (subsuming those above) is to use simple objects together with two simple relations: **Type** A relation that exists between every object and its class and can be applied an arbitrary number of times to define the meta-classifications of instance, class and meta-class; **Extension** A relation that exists between classes that provides a minimal basis for incremental addition of features. The approach is based on existing proposals for meta-classes provided
by languages such as Smalltalk [16] and ObjVLisp [10]. Although Smalltalk was
the first language to introduce meta-classes (and thereby three-levels of meta-
class, class and instance), each meta-class is restricted to having a single instance
which severely limits its use as the basis for language engineering where meta-
properties are reused across multiple languages.

The approach to object classification and
the instance-of relation is shown in Fig. 1
where circles represent sub-sets of the set O
of objects. Consider the set A that denotes
a set of objects representing animals. In or-
der for an element of A to be well-formed, it
must have an instance-of link to an object in
the set C of all classes. Note that elements of
C are objects (everything is an object), but
they are objects that satisfy some criteria for
class-hood. Since the element of C that rep-
resents the class Animal is itself an object, it
must have an instance-of link to an object that
represents its class. Such an object is a meta-
class and is a member of the set of objects M (perhaps the class called Class). A
meta-class is just an object that satisfies the constraint for membership of M.
This means that it must have an instance-of link to a meta-meta-class in MM. It
should be stressed at this point, that there is no limit to the instance-of regress.
In addition to objects that satisfy Animal-hood. There are objects that are used
to group objects: snapshots that are members of the set S. Snapshots contain
objects that are all instances of related classes: packages that are members of the
set P. Finally, classes can be related by extension so that there are two classes
Animal and Herbivore in C that designate the rules for membership of the sets
A and H. Of course, since every element of M is also in C, the extension relation
can be defined between meta-classes that will designate different sub-sets of C.

Our basis for meta-modelling is defined as a self-describing object-oriented
kernel. The Kernel is essentially a logic. However, unlike a traditional logic
that consists of boolean valued formulas whose sub-expressions denote values
drawn from a collection of predefined types, the Kernel can only denote ob-
jects. Some objects are designated classes because they conform to a particular
object-interface that includes boolean valued expressions (or constraints) that
characterize objects designated as well-formed instances of the class. Such a self-
describing logic might lead to doubts related to Russell’s Paradox, although the
use of types and identities as described below, together with an implementation
of the approach that supports a collection of real-world applications (including
itself), gives us confidence that this is not a problem. Our claim is that this
approach is novel and that it subsumes existing approaches to meta-modelling.
Our contribution is the definition of a meta-circular foundation for model-based
language engineering in the form of a kernel language that is validated in terms
of an implementation as a toolkit that has been used for a variety of real-world
applications. In addition we show that other approaches to multi-level modelling can be represented in the Kernel.

2 A Meta-Modelling Kernel

Our proposal is to set up a system whereby everything is an object [21] and where a simple set of rules governs the ability to construct configurations of objects that constitute self-describing languages. The system consists of an object representation and then sugarings that are convenient language structures defined to de-sugar into the basic representation.

Figure 2(a) shows the proposed kernel language as a diagram. Fundamentally, everything is an object and a partial view of the Kernel as a collection of objects and slots is shown in figure 2(b). An object has a unique id, some slots, and a type. The type of an object is a class. Classes are organised into packages whose instances are snapshots that are assemblies of objects. Since classes are just objects that conform to some structural conditions, packages can be similarly viewed as snapshots with appropriate conditions. Collections of objects are organised as sequences in terms of pairs and null. Since types are always implemented as classes, there is a special class called listof whose instances are lists. There is no need to special types of atomic value such as integers and booleans because we can designate special objects via their identities as being members of these data types. Expressions are objects that can be asked to evaluate themselves in a supplied context. Constraints are special types of expressions that always return boolean values. Constraints are important because they are used in classes to classify objects that are considered to be instances. Classes have operations, that are objects used to handle messages sent to instances of the class. Note that there is no notion of side-effect, operations are purely functional.

Fig. 2. Two Views of the Kernel
Fig. 3 shows the complete textual definition of the Kernel. It uses a number of external definitions and notational conventions that are outlined as follows: classes define a predicate \( ? \) that is used to determine instance-hood; operations use \( \lambda \)-notation where arguments are patterns; objects are \( (C,i)[s \mapsto v] \) where \( C \) is the class of the object, \( i \) is the id, \( s \) is a slot name and \( v \) is the corresponding value; \texttt{intern} maps a class and slots to an object; lists are \( [v_1,\ldots,v_n] \) and can be appended using \( + \); \( :: \) is used to dereference names in a name-space; \( \uparrow \) is an inheritance relationship between classes.

Since the Kernel is essentially a logic we need something equivalent to OCL. We use the following shorthand where \( l \) is a list: \( l.\forall(p) \) is \textit{true} when the predicate \( p \) returns \textit{true} for each element in the list \( l \); \( l.\exists(p) \) is \textit{true} when the predicate \( p \) returns \textit{true} for any element in the list \( l \); \( l.\approx(x) \) is true when the element \( x \) is contained in the list \( l \); \( l.\equiv(p,a,y) \) is the result of applying operation \( a \) to the first element \( x \) of \( l \) for which \( p(x) \) is \textit{true} and \( y \) if no such element exists; \( l.\texttt{flatten()} \) expects \( l \) to be a list of lists and returns a list formed by appending all elements of \( l \) in order. \# maps a list to its length. It is convenient to be able to construct and manipulate lists using \textit{comprehension} expressions. For example, if \( l \) is the list \( [2,3,4] \) then \( [x*2 | x \leftarrow l] \) is the list \( [4,6,8] \). Predicates may be used to filter lists as in \( [x | x \leftarrow l,?\text{even}(x)] = [2,4] \).

In order for this to be meta-circular, we require that and Kernel.?(Kernel) holds. This is difficult to establish without tooling since all the objects in the definition must be checked against their classes, and, since the classes themselves are part of the package, this requires the classes to be self-describing. The Kernel has been implemented as part of the XModeler toolkit and has been used to implement the rest of the tools including diagram tools, model browsers, model editors, model transformers and libraries. The XModeler Kernel contains many more classes than the language described in this article, but the essential features are the same. XModeler can be instructed to apply the Kernel-defined constraints to itself (over 100 classes) and to produce a report that shows that it is self-consistent.

### 3 Validation

Section 1 describes a list of features that we claim to be characteristic for any language that is used as a basis for meta-modelling. We have introduced such a language and used it to build a model of itself. This section analyses the Kernel language with respect to the characteristic features: **type**: In Kernel everything is an object and all objects have an intrinsic type property. **meta-circularity**: This property is essential for multi-level modelling and in order to be able develop tools (such as serializers) that are language-level agnostic [25]. The XModeler tool can be shown to establish that Kernel.?(Kernel). **uniformity**: We have used a single representation (with a small number of externally defined conventions and rules) for all data in Kernel. **extensibility**: Extension is supported through class relationships that are then used by constraints in order to place conditions
class Object {
    id : Object;
    type : Class;
    slots : [Slot]
    constraints { type.(self) }
    operations {
        dot(n) = slots.(λ(n' → .)(n' → v).v.error)
        send(n, args) =
        λ(n' → (Operation){args → args'}).n' and args' = args'.
        λ(_, → f) f.invoke(self,args),
        error
    }
}
class Slot { name : Str; value : Object }

class Operation {
    class 
    Slot { name : Str; value : Object }
    class 
    Constraint { name : Str; value : Object }
    class 
    Pair { head : Object; tail : Object }
    class 
    Null {} 
    class Exp {} 
    class Arg { name : Str }
}

class Class {
    name : Str;
    supers : [Class];
    attributes : [Attribute];
    operations : [Binding];
    constraints : [Constraint]
    operations {
        supers() = [self] +
        [c | p ← supers +
        c ← p.supers()].remDups()
        ∀(c) = supers().∋(c)
        atts() =
        [a | c ← supers(), a ← c.attributes]
        ops() =
        [b | c ← supers(), b ← c.operations]
        cond() =
        [a | c ← supers(), a ← c.constraints]
        ::= (a,d) =
        atts().∩(λ(n' → a)n'≡n,λ(n → a)a,
        ops().∩(λ(n' → e)n≡n,λ(n → e)o,o))
        ?(o) = o.type.∋(self) and
        atts().∩(λ(a)o.sLOTS.∃(λ(a)
        s.name = a.name and
        a.type.∋(s.value)) and
        cond().∩(λ(c) c.eval([self → o] +
        [s.name → s.value | s ← o.sLOTS]))
    }
}
class Package extends Snapshot,Class {
    constraints {
        objects.∩(λ(?Class));
        attributes.∩(λ(a objects.∋(a.type)));
        parents.∩(λ(p) p.type.∋(Package))
    }
    operations {
        ::= (a,d) = obj.(λ(a) o≡n,λ(o) o,d)
        obj() = objects +
        [p.objects | p ← parents].flatten()
        ?(p) = objects.∩(λ(c) Φ(a).∩(λ(c') c'.∋(c')))
        ?(o) = o.type.∩(Snapshot) and
        o.package.∩(self) and
        o.objects.∩(λ(a)
        objects.∋(λ(c) c'.∋(c')) and
        Class::?(int(self,o.sLOTS))
    }
}
class Snapshot extends Object {
    package : Package;
    objects : [Object];
    bindings : [Slot]
    constraints {
        package.∋(self);
        bindings.∩(λ(b)objects.∋(b.value))
    }
    operations {
        ::= (k,d) = bindings.(λ(s)
        λ(s)s.name=k,λ(s)s.value=d)
    }
}
class Null {} 

Fig. 3. Definition of Kernel

The model in figure 4(a) shows the use of type facets that allow classes to have properties. These can be implemented by including a potency as part of an attribute definition. The potency is an integer value indicating the number of type-levels (3 are shown in the model) spanned by the relationship between objects that are instances of a sub-class. The definitions are Class::? and Package::? in Fig. 3.

Our claim is that the Kernel is a suitable basis for multi-level modelling. In order to validate this claim we present the definition of two different languages, each based on independent approaches, both defined in the Kernel. Models written in the languages are shown in Fig. 4.

on objects that are instances of a sub-class. The definitions are Class::? and Package::? in Fig. 3.
an attribute and its corresponding slots. The model defines a language (Domain Metatypes) of engines. The class `Engine` defines a type facet called `max_speed` that results in a slot at the domain type (model) level, and an instance facet called `inertia` that becomes a slot at a remove of two type-levels.

The model in figure 4(b) shows the power-type pattern where a class (in this case `Vehicle`) is classified by another class (`VehicleKind`). Instances of `VehicleKind` are used to partition subclasses of `Vehicle` as shown in the ellipse, forming a `class`-ject. The result is that an object is contributing to the type-level information in a class that will eventually affect instances of the class.

Each language definition takes the form of a package that is both an instance and an extension of `Kernel`. By the definition of `Package::?`, an instance of a package `P` should be a snapshot whose contents are all instances of classes in `P`. By the definition of `Package::extends?`, a package `P` extends a package `Q` when every class in `P` extends some class in (or inherited by) `Q`. Therefore, by extending and instantiating `Kernel` a package is a well-formed language definition in its own right, that can, by the definition of extension, modify the basic definition of `Class::?`. Such a modification might place extra conditions on instance-hood, or even relax existing conditions.

Fig. 5 contains the definition for the language and models shown in figure 4(a). The class `CAtt` extends `Attribute` with an attribute for potency-level. The class `CClass` modifies `atts` so that it gathers together all attributes that apply to this level. This is achieved using a counter that is incremented when the type-level is traversed. A concrete-syntax for potency-level in attributes is used in the definition of the package `DomainMetaTypes`, and slots are permitted in class definitions due to potency-levels becoming 0 in `DomainTypes`. The snapshot `DomainInstances` contains a single object whose slots correspond to attributes from different type-levels as defined by their respective potency-levels.

Fig. 6 contains the definition for the language and models shown in figure 4(b). The meta-class `PowClass` defines an attribute `classifier` and the constraint on `PartClass` requires that all its descriptor objects are instances of the classifier inherited by a parent power-class. The package `Vehicles` contains a single power-class `Vehicle` that is classified by `VehicleKind` and a partitioned-class `Boat`
package CKernel:Kernel extends Kernel {
    level:Integer;
}
class CAtt extends Attribute {
    level: Integer;
}
class CClass extends Class {
    operations {
        atts() = catts(1, self)
        catts(n,c=(_c))[] = []
        catts(n,c) = [a | a ← c.atts(),
                      ?a.type=CAtt, a.level = n] +
        catts(n+1, c. type)
        constraints (atts.∀(λ(a)a.type=CAtt))
    }
    }
}
snapshot DomainInstances:DomainTypes {
    (DType) [ inertia ↦→ 0.28; ECU_version ↦→ 7.3]
    }
}

package DomainMetaTypes:CKernel {
    class Engine: CClass extends CClass {
        inertia[2]: Float;
        max_speed[1]: Integer
    }
    class DieselEngine: CClass extends Engine {
        preheat_time[1]: Float
    }
    class OttoEngine: CClass extends Engine {
        ignition_alpha[1]: Float
    }
    }
}

package DomainTypes: DomainMetaTypes {
    class DType: DieselEngine {
        ECU_version[1]: Float;
        max_speed = 5000;
preeheat_time = 1.5
    }
    }
}

package PKernel: Kernel extends Kernel {
    class PowClass extends Class {
        classifier: Class
    }
    class PartClass extends Class {
        descr:[Object]
        constraints {
            supers().∀(λ(c) PowClass?(c));
            descr.∀(λ(a)
                supers().∃(λ(c)
                    c.classifier.?/(a)))
        }
    }
    snapshot ABoat: Vehicles {
        (Boat)[beam ↦→ 9; weight ↦→ 185]
    }
}

package Vehicles:PKernel {
    class Vehicle: PowClass {
        classifier=VehicleKind
        weight: Int
    }
    class VehicleKind {
        name: Str;
        canTravelOnWater: Bool
    }
    class Boat: PartClass extends Vehicle {
        descr=[(VehicleKind)[
            name='Boat';
canTravelOnWater ↦→ true]]
        beam: Int
    }
    }
}

Fig. 5. Definition and use of CKernel

that includes an instance of VehicleKind as its descriptor. The snapshot ABoat is governed by the classes defined in the package Vehicles which in turn are governed by the language PKernel therefore, ABoat is constrained by the clabject Boat and Boat.descr.

Fig. 6. Definition and use of PKernel

The examples described above contribute evidence that Kernel can define different languages and is not restricted to a fixed number of type-levels, and that objects, classes and meta-classes can be mixed. This is possible because of the uniformity of representation, the unrestricted access to type-level information and meta-circularity. Although outside the scope of this paper, the formulation of Kernel makes it possible to write level-agnostic tools, such as those for model-management, that can be used on any type-level.

4 Conclusion

Our aim is to produce a meta-circular level-agnostic basis for model-based language engineering. We have reviewed the current proposals for such a basis and
argued that they are not optimal by providing a new language definition that is
self-describing and can be used to embed the competing approaches. The Kernel
language is simple and can be implemented as demonstrated by the XMF and
XModeler toolkit [11] that is capable of both describing and reasoning about
itself. The toolkit was reported as a leading technology for Software Engineering
[19] and has been used for a variety of applications including modelling languages
for aerospace applications, telecoms applications [1], and is currently being used
to implement aspects of the MEMO enterprise modelling language [24, 14].

In [15], the authors show how the OMG levels M0-M3 can be represented
on a single object-diagram. This allows OCL constraints to range over all levels
and thereby support clabjects and potency. This is consistent with our approach,
although OCL is just one of the languages that could be used with our approach
(as a view of models and constraints) and the authors of [15] do not claim to be
a foundation for model-based language engineering.

Our intention is that the Kernel language defined in this article provides a
basis for ourselves and others to experiment with language definitions. Because
all such kernel-defined languages are based on a single object representation, it
is feasible to build a collection of tools that work against well defined sub-sets
of objects (as shown in figure 1) and thereby incrementally develop a shared
library.

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