

1 **Sensitivity study of forecasted aftershock seismicity**  
2 **based on Coulomb stress calculation and rate- and**  
3 **state-dependent frictional response**

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**Abstract.**

We use the Dieterich (1994) physics-based approach to simulate the spatio-temporal evolution of seismicity caused by stress changes applied to an infinite population of nucleating patches modeled through a rate- and state-dependent friction law. According to this model, seismicity rate changes depend on the amplitude of stress perturbation, the physical constitutive properties of faults (represented by the parameter  $A\sigma$ ), the stressing rate and the background seismicity rate of the study area. In order to apply this model in a predictive manner, we need to understand the impact of physical model parameters and the correlations between them. Firstly we discuss different definitions of the reference seismicity rate and show their impact on the computed rate of earthquake production for the 1992 Landers earthquake sequence as a case study. Furthermore, we demonstrate that all model parameters are strongly correlated for physical and statistical reasons. We discuss this correlation emphasizing that the estimations of the background seismicity rate, stressing rate and  $A\sigma$  are strongly correlated to reproduce the observed aftershock productivity. Our analytically derived relation demonstrates the impact of these model parameters on the Omori-like aftershock decay: the  $c$ -value and the productivity of the Omori law, implying a  $p$ -value smaller or equal to 1. Finally, we discuss an optimal strategy to constrain model parameters for near-real time forecasts.

## 1. Introduction

25 The spatial evolution of seismicity is commonly modeled in terms of coseismic and  
26 postseismic stress changes. Stress perturbations are simulated to model fault interaction  
27 and earthquake triggering (Harris, 1998; King and Cocco, 2001; Freed, 2005; Steacy et al.,  
28 2005a, and references therein). Several papers have pointed out the correlation between  
29 Coulomb stress changes and the seismicity rate changes after moderate-to-large magnitude  
30 earthquakes (Stein, 1999; Toda and Stein, 2003). However, these studies show that, in  
31 order to model the spatial and temporal evolution of seismicity, the fault constitutive  
32 properties have to be taken into account. To this task Dieterich (1992, 1994) proposed  
33 a model to simulate the changes in the rate of earthquake production caused by stress  
34 changes applied to an infinite population on nucleating patches modeled through a rate-  
35 and state-dependent friction law. This model has been discussed by a theoretical point of  
36 view (see Gomberg 2005-a and references therein) and widely applied to different tectonic  
37 areas (Toda et al., 1998 and 2005; Dieterich et al., 2000; Gross, 2001; Toda and Stein,  
38 2003; Catalli et al., 2008; Llenos et al., 2009 among many others).

39 According to the Dieterich model, seismicity rate changes depend on the amplitude  
40 of the stress perturbation, the physical constitutive properties of faults represented by  
41 the parameter  $A\sigma$  (where  $A$  is the constitutive parameter controlling the direct effect of  
42 friction in the rate and state formulation and  $\sigma$  is the effective normal stress), the stressing  
43 rate as well as by the background seismicity rate of the study area.

44 The Dieterich (1994) model has been proposed as a reliable physics-based approach to  
45 forecast seismicity rate changes and to compute earthquake probability changes (Toda

46 and Stein, 2003; Toda et al., 2005). It has also been proposed as the key ingredient  
47 of approaches aimed at evaluating the change in probability of occurrence of a large  
48 earthquake on a specific fault caused by the coseismic stress changes generated by previous  
49 earthquakes occurred nearby (Stein et al., 1997; Parsons et al., 2000). This latter issue  
50 is still controversially debated within the scientific community, since different opinions  
51 exist concerning the actual capability of evaluating the changes in single-fault earthquake  
52 probability through a model assuming an infinite population of nucleation patches (see  
53 Hardebeck, 2004; Gomberg et al, 2005-b).

54 In the present paper we only mention the problem of computing aftershock probability  
55 through seismicity rate changes, because our focus is on computing seismicity rate changes  
56 caused by coseismic stress perturbations. We do not discuss here the problem of the  
57 reliable assessment of time-dependent earthquake probabilities for main shocks through  
58 renewal approaches. Our main goal is to discuss the ability to forecast seismicity rate  
59 changes through a physics-based model, in order to assess its relevance for society.

60 This paper presents the results of research activities matured in the framework  
61 of two projects, namely NERIES (*Network of Research Infrastructures for Euro-*  
62 *pean Seismology*, [www.neries-eu.org](http://www.neries-eu.org)) and SAFER (*Seismic Early Warning for Europe*,  
63 [www.saferproject.net](http://www.saferproject.net)), funded by European Community within the sixth framework pro-  
64 gram. We have faced the challenging task to perform a retrospective testing experiment  
65 to forecast aftershocks patterns using the 1992 Landers earthquake as a case study. While  
66 Hainzl et al. (2009) have studied the problem of aftershock modeling taking into account  
67 the variability caused by uncertainties of computed stress perturbations, the goal of the  
68 present manuscript is to understand the role of the main physical input parameters in



69 forecasting seismicity rate changes through the Dieterich's physics-based model. This  
 70 sensitivity study is particularly important in order to perform a retrospective validation,  
 71 which requires an accurate analysis of the variability and the estimate of best model pa-  
 72 rameters. The result of a retrospective test of stress-based models in comparison to purely  
 73 statistical models is presented in the follow up paper by Woessner et al. (2009) for the  
 74 1992 Landers earthquake sequence.

## 2. Methodology

75 In this section we summarize the methodologies commonly adopted to compute  
 76 Coulomb stress changes and to forecast seismicity rate changes through the Dieterich's  
 77 model. The main goal is to point out the most important physical parameters that have  
 78 to be constrained in order to perform robust applications to real study cases taking into  
 79 account the correlation between the model parameters.

### 2.1. Computing Coulomb stress changes

Coulomb stress changes ( $\Delta CFF$ ) are calculated through the following relation:

$$\Delta CFF = \Delta\tau + \mu \cdot (\Delta\sigma_n + \Delta P) \quad (1)$$

where  $\Delta\tau$  is the shear stress in the direction of slip on the assumed causative fault plane,  $\Delta\sigma_n$  is the normal stress changes (positive for unclamping or extension),  $\mu$  is the friction coefficient and  $\Delta P$  is the pore pressure change (see Harris, 1998; King and Cocco, 2001). The relation used to compute the coseismic pore pressure changes distinguishes the constant apparent friction model from the isotropic poroelastic model (Cocco and Rice, 2002). According to the former model, pore pressure changes depend on the normal stress changes  $\Delta P = -B\Delta\sigma_n$ , where  $B$  is the Skempton coefficient which varies between 0 and

1 (Beeler et al., 2000; Cocco and Rice, 2002 and references therein). Therefore, using this model, equation (1) can be written as

$$\Delta CFF = \Delta\tau + \mu' \cdot \Delta\sigma_n \quad (2)$$

where  $\mu' = \mu(1 - B)$  is usually called the effective friction coefficient. On the contrary, the isotropic poroelastic model assumes that pore pressure changes depend on the volumetric stress changes (first invariant of the stress perturbation tensor)  $\Delta P = -B(\Delta\sigma_{kk}/3)$ , and therefore equation (1) becomes:

$$\Delta CFF = \Delta\tau + \mu \cdot (\Delta\sigma_n - B \frac{\Delta\sigma_{kk}}{3}). \quad (3)$$

80 Thus, in both equations (2) and (3) the values of the friction and the Skempton co-  
 81 efficients have to be adopted in order to compute stress perturbations. Cocco and Rice  
 82 (2002) discussed the difficulties in distinguishing between these two models also in realistic  
 83 complex fault zones with inelastic or anisotropic properties. Beeler et al. (2000) suggested  
 84 using equation (3) because it is more general and applicable to different tectonic areas. This  
 85 represents a first source of variability in computing static coseismic stress changes, which  
 86 is commonly not considered since equation (2) is widely adopted to compute seismicity  
 87 rate changes (see Beeler et al., 2000).

## 2.2. Resolving Coulomb stress changes onto receiver faults

88 The calculation of Coulomb stress changes requires the definition of the geometry and  
 89 the faulting mechanism of the target faults upon which stress perturbations are resolved.  
 90 Two approaches are commonly adopted; the first one relies on resolving stress changes  
 91 onto a prescribed faulting mechanism (that is, to assign strike, dip and rake angles of the  
 92 target faults). This means that fault geometry and slip direction are input parameters

93 of stress interaction simulations. McCloskey et al. (2003) proposed using geological  
94 constraints in order to calculate Coulomb stress perturbations for forecasting the spatial  
95 pattern of seismicity. However, this strategy does not always seem to be applicable, due  
96 to the complexity of fault systems for instance, as pointed out by Nostro et al. (2005)  
97 in their application to the 1997 Umbria-Marche (Italy) seismic sequence. The second  
98 approach relies on the calculation of the optimally oriented planes for Coulomb failure  
99 (often called OOPs). In this case, instead of assigning the strike, dip and rake angles of  
100 the receiver faults, we have to assign the magnitude and the orientation of the principal  
101 axes of the regional stress field  $\sigma_{ij}^r$  (see King and Cocco, 2001, and references therein). The  
102 optimally oriented planes are identified at each grid point of the numerical computation  
103 by finding the values of strike, dip and rake that maximize the total stress tensor defined  
104 as  $\sigma_{ij}^{tot} = \sigma_{ij}^r + \Delta\sigma_{ij}$ , where  $\Delta\sigma_{ij}$  is the coseismic stress perturbation. After assigning the  
105 absolute values of the principal stress components and the orientation of the stress tensor  
106 (trend and plunge of each axis), two equivalent OOPs are obtained at each node of the  
107 3D grid.

108 The predicted focal mechanisms associated with the OOPs strongly depend on the  
109 orientation and magnitude of the regional stress field. Therefore, Coulomb stress changes  
110 computed for OOPs are associated with theoretical focal mechanisms, which might differ  
111 from real fault plane solutions. This might be the case also for stress changes resolved onto  
112 prescribed receiver faults, although in this latter case constraints from structural geology  
113 and a direct control of the expected faulting mechanisms might reduce the variability.

114 Therefore, we remark here that resolving stress changes on receiver faults, through  
115 either the identification of prescribed receivers or the calculation of OOPs, requires to

116 assign further input parameters. As we will discuss in the following the choice of one  
 117 of these two simulation strategies will lead to completely different patterns of Coulomb  
 118 stress perturbations, particularly near the causative faults.

### 2.3. Computing the rate of earthquake production

We briefly describe here the Dieterich (1994) model to compute the changes in the rate of earthquake production caused by coseismic stress perturbations. The seismicity rate  $R$  after the application of a stress perturbation is a function of the state variable  $\gamma$ , stressing rate  $\dot{\tau}$  and the background seismicity rate  $r$  (see also Toda and Stein, 2003 and Toda et al., 2005):

$$R = \frac{r}{\gamma \dot{\tau}}. \quad (4)$$

Under a constant stressing rate without stress perturbations, the state variable is at the steady state and takes the value

$$\gamma_0 = \frac{1}{\dot{\tau}}, \quad (5)$$

which according to (4) gives  $R = r$ . This implies that, in absence of any stress perturbation, the seismicity rate at the steady state is given by the background rate of earthquake production. We assume here that the stressing rate does not change before and after the main shock, being equal to  $\dot{\tau}$ . Following Dieterich (1994) the rate  $R$  can be interpreted as a statistical representation of the expected rate of earthquake production in a given magnitude range. An applied stress perturbation to the fault population modifies the seismicity rate through the evolution of the state variable given by:

$$\gamma_n = \gamma_{n-1} \exp\left(\frac{-S}{A\sigma}\right). \quad (6)$$

where  $\gamma_{n-1}$  and  $\gamma_n$  are the values of the state variable just before and after the applied stress change ( $S$ ), respectively.  $A\sigma$  is the constitutive parameter of the rate- and state-dependent law governing fault friction; we remind here that  $\sigma$  is the effective normal stress also named  $\sigma_{eff}$  in the following of the text. The evolution of state variable is governed by the following law:

$$d\gamma = \frac{1}{A\sigma} [dt - \gamma S]. \quad (7)$$

where  $S$  in (6) and (7) is the "modified" Coulomb stress change  $S = \Delta CFF$  and it is given by (Dieterich et al., 2000; Catalli et al., 2008 and references therein):

$$S = \Delta CFF = \Delta\tau + (\mu - \alpha) \cdot \Delta\sigma_{eff} = \Delta\tau + \mu_{eff} \cdot \Delta\sigma_{eff} \quad (8)$$

119 where  $\Delta\sigma_{eff} = (\Delta\sigma_n + \Delta P)$ ,  $\mu_{eff} = (\mu - \alpha)$ , where  $\alpha$  is the positive non-dimensional  
 120 parameter controlling the normal stress changes in the Linker and Dieterich (1992) consti-  
 121 tutive law. This parameter is necessary to account for normal stress changes in the rate-  
 122 and state-dependent frictional approach, and consequently the parameter multiplying the  
 123 effective normal stress changes in (8) is not the friction coefficient as usually assumed in  
 124 Coulomb stress computations [see (1) and also Harris, 1998].

A positive stress perturbation caused by an earthquake occurred nearby will decrease the state variable  $\gamma$ , so that the target fault slips at higher rate. A drop in the state variable results in an increase in the seismicity rate. According to the Dieterich (1994) model, the state variable  $\gamma$  increases with time after the stress changes according to

$$\gamma_{n+1} = \left( \gamma_n - \frac{1}{\dot{\tau}} \right) \cdot \exp\left( \frac{-\Delta t \dot{\tau}}{A\sigma} \right) + \frac{1}{\dot{\tau}}, \quad (9)$$

125 where  $\Delta t$  is the time elapsed after the stress perturbation and  $\gamma_n$  is calculated through  
 126 (6).

### 3. Impact of model parameters

127 The calculation of seismicity rate changes caused by coseismic stress perturbations re-  
128 quires the choice of the following main input parameters: the amplitude of the Coulomb  
129 stress perturbation (which depends on other parameters as described in sections 2.1 and  
130 2.2), the constitutive parameter  $A\sigma$ , the stressing rate  $\dot{\tau}$  and the background seismicity  
131 rate  $r$ . In this section we focus on the last three input parameters describing the rate- and  
132 state-dependent model to forecast seismicity rate changes. Hainzl et al. (2009) have dis-  
133 cussed the impact of uncertainties and variability of coseismic stress change amplitudes.  
134 We solely emphasize here that Coulomb stress changes depend on several "a priori" input  
135 parameters such as the friction and the Skempton coefficients, and the  $\alpha$  parameter of  
136 the rate and state model (see equation 8). According to several authors (see Harris, 1998;  
137 King and Cocco, 2001; and Catalli et al., 2008) the effect of the friction coefficient on  
138 the stress perturbation and the seismicity rate change patterns is usually modest. On the  
139 contrary, the choice of the poroelastic model can be of relevance for computing Coulomb  
140 stress changes (equations 2 and 3). We also point out that, according to equation (8), the  
141 effective normal stress changes are multiplied by an effective coefficient of friction which  
142 depends on both the friction coefficient and the  $\alpha$  parameter.

#### 3.1. The background seismicity rate

143 In this section we discuss the definition of the background seismicity rate as well as its  
144 impact on the computed seismicity rate changes through the Dieterich (1994) model. This  
145 model assumes that before the application of a stress perturbation the state variable  $\gamma$  is at  
146 a steady state, which means that it does not change with time. Indeed, it is assumed that  
147 this initial value ( $\gamma_0$ ) is equal to the inverse of the stressing rate (which is taken constant

148 in time in the most common formulation of the Dieterich model); therefore, according to  
 149 (4) the seismicity rate before the application of the stress perturbation is equal to the  
 150 background rate  $r$ . We describe such a background rate through a stationary seismicity  
 151 rate. The background seismicity rate  $r$  is an important variable in any fault population  
 152 model. The background seismicity rate is the rate of earthquake production in absence  
 153 of any stress perturbation and it is associated with a spatially non-uniform stationary  
 154 process (see for instance Toda et al., 2005). According to this definition, background  
 155 events are expected to occur independently of each other (i.e., the nucleating patches do  
 156 not interact), and therefore the background seismicity rate can be also considered as a  
 157 time independent Poisson process. In the present study, we refer to the "background  
 158 seismicity" rate as a time independent smoothed seismicity rate computed in a prescribed  
 159 time window using a declustered catalog.

Different procedures can be applied for declustering a seismic catalog. In the present  
 study we adopt the background rate measured through the ETAS model (Ogata, 1988;  
 1998) following the method proposed by Zhuang et al. (2002). The ETAS model defines  
 the seismicity rate at time  $t$  and location  $(x, y)$  as the sum of two contributions

$$\lambda(t, x, y) = \mu(x, y) + \sum_{i:t_i < t} \frac{K e^{\tilde{\alpha}(M_i - M_c)}}{(t - t_i + c)^p} \frac{c_{dq}}{[(x - x_i)^2 + (y - y_i)^2 + d^2]^q}. \quad (10)$$

160 where  $\mu(x, y)$  is the time independent spatially non-uniform background seismicity rate,  $K$   
 161 and  $\tilde{\alpha}$  are the productivity parameters related to the numbers of events triggered by each  
 162 earthquake,  $c$  is a time constant and the exponent  $p$  controlling the decay of the sequence.  
 163  $M_c$  is the completeness magnitude, while  $i$  identifies the triggering event occurring at time  
 164  $t_i$  with magnitude  $M_i$ .  $d$  and  $q$  are the parameters characterizing the spatial distribution  
 165 of triggered events,  $\sqrt{(x - x_i)^2 + (y - y_i)^2}$  is the distance between the location  $(x, y)$  and

166 the epicenter of the  $i$ -th earthquake  $(x_i, y_i)$  and  $c_{dq}$  is a normalization factor. Therefore,  
167 using the ETAS model we can measure the spatially non-uniform (i.e., clustered in space)  
168 background seismicity rate as  $r = \mu(x, y)$ .

169 The definition and the measure of a reference or a background seismicity rate is still  
170 controversial (Hainzl and Ogata, 2005; Lombardi et al., 2006; Lombardi and Marzocchi,  
171 2007) and different approaches are used in the literature. Catalli et al. (2008) for instance  
172 adopted a reference seismicity rate computed by smoothing seismicity on a prescribed  
173 time window using a complete (undeclustered) catalog in order to model seismicity rate  
174 changes through the Dieterich approach. We use this definition in the present work and  
175 we refer to the "reference seismicity" rate as a time independent smoothed seismicity  
176 rate computed by using an undeclustered catalog. Thus, contrary to the background, the  
177 reference seismicity rate contains all the sequences and the triggered events within the  
178 selected time window. It is important to point out that in this latter case the reference  
179 seismicity rate cannot be considered as the rate of earthquake production in absence  
180 of any stress perturbation. To estimate in this way a stationary mean rate, the time  
181 period selected for smoothing the seismicity has to be longer than the duration of seismic  
182 sequences within the adopted time interval. The choice of the time window is relevant for  
183 both the computed background and the reference seismicity rates (Marsan, 2003; Marsan  
184 and Nalbant, 2005), but the latter is certainly more affected by this subjective choice and  
185 by the temporal variability of completeness magnitude.

186 Figure 1 shows the calculation of the reference ( $r(x, y)$ , left panel) and background  
187 ( $\mu(x, y)$ , right panel) seismicity rates computed for the area struck by the 1992 Landers  
188 earthquake. The reference seismicity rate has been computed by smoothing the seismicity



189 in the 8 years (1984-1991) preceding the 1992 main shock using the Frankel (1995) algo-  
190 rithm. The minimum magnitude used for smoothing is 3.0, the maximum depth 30 km  
191 and the correlation distance 5 km; the adopted b-value is equal to 0.91. We use in this  
192 study the same values adopted in the retrospective forecasting test described by Woessner  
193 et al. (2009). The mean value of the reference seismicity rate is  $3 \cdot 10^{-6}$  events/day  $\cdot km^2$ .  
194 The background seismicity rate has been computed through equation (10) using the same  
195 minimum magnitude and time period. The mean value of the background seismicity rate  
196 is  $1.5 \cdot 10^{-6}$  events/day  $\cdot km^2$ . It is evident from Figure 1 that both the pattern and the  
197 absolute values of seismicity rates are different and we will show below how this difference  
198 affects the predicted seismicity rate changes.

199 Figure 2 displays the map of the difference at each grid point between the computed  
200 reference (left panel) or background (right panel) seismicity rate and their average value  
201 measured for the whole area. This figure shows that both the background and the reference  
202 seismicity rates are larger than their associated average values in nearly the same area.  
203 As expected the variability of the reference seismicity rate is larger than that of the  
204 background rate. This figure depicts that in both cases the Big Bear aftershock lies in  
205 the area of largest positive difference between spatially non-uniform seismicity rates and  
206 their average values. On the contrary, east of the causative fault system, where the Hector  
207 Mine earthquake occurred in 1994, this difference is negative, which means that the non-  
208 uniform rates are smaller than their mean values (note that we are analyzing here the  
209 seismicity before the 1992 Landers main shock). This raises the question if a uniform  
210 background seismicity rate is a good assumption to forecast seismicity rate changes. The

211 resulting average rates for the whole area correspond to 0.176 and 0.086 events/day for  
212 the reference and the background seismicity rate, respectively.

213 In many studies and applications (see Gomberg et al., 2005-a; Toda and Stein, 2003,  
214 among many others) the background seismicity rate is assumed spatially uniform. We have  
215 computed the seismicity rate changes caused by the 1992 Landers main shock and the Big  
216 Bear largest aftershock using the mean values of both the reference and the background  
217 seismicity rates given above. In this case, the ratio between the forecasted cumulative  
218 number of triggered earthquakes for both models (we have kept all the other parameters  
219  $A\sigma$  and  $\dot{\tau}$  fixed and equal to 0.04 MPa and  $5.6 \cdot 10^{-6}$  MPa/day; these values are consistent  
220 with those proposed by Toda et al. 2005) is nearly equal to the corresponding ratio  
221 between the values of the estimated background and reference seismicity rates (see Figure  
222 3 dashed curves). A different application performed by using spatially inhomogeneous  
223 seismicity rates shows that the difference between the seismicity rate forecast performed  
224 by using  $r(x, y)$  for the Landers and Big Bear shocks is significantly larger than that  
225 obtained by using the non-uniform background rate  $\mu(x, y)$  (see Figure 3 solid curves)  
226 as well as those inferred by adopting the spatially uniform mean values (dashed curves).  
227 However, it is important to emphasize that this result cannot be extrapolated to other  
228 areas.

229 We have performed similar calculations to study the 1997 Kagoshima (Japan) earth-  
230 quake pair (see Toda and Stein, 2003). Two strike slip earthquakes ( $M \sim 6$ ) struck the  
231 Kagoshima prefecture (Japan) in 1997; they were just 4 km and 48 days apart and pro-  
232 vided a good test to study stress interactions and one of the first attempts to estimate  
233 aftershock probabilities (Toda and Stein, 2003). We have computed the background seis-

234 micity rate by applying the ETAS approach to the seismic catalog provided by JMA  
235 and the reference seismicity rate by smoothing the seismicity in the 10 years preceding  
236 the first Kagoshima main shock. The minimum magnitude and the maximum depth for  
237 smoothing seismicity are 2.3 and 40 km, respectively. The adopted b-value for this area is  
238 0.9. Figure 4 shows the spatial distribution of the reference (left panel) and background  
239 (right panel) seismicity rates for the Kagoshima area, which displays evident differences.  
240 The mean value of the reference seismicity rate is  $7.5 \cdot 10^{-6}$  events/day  $\cdot km^2$  and that  
241 one of the background seismicity rate is  $2.5 \cdot 10^{-6}$  events/day  $\cdot km^2$ . We have computed  
242 the predicted seismicity rate changes caused by the two main shocks using both the mean  
243 and the spatially variable reference and background rates. The results of the numerical  
244 simulations for Kagoshima reveal just the opposite outcome than those for Landers (see  
245 Figure 5). The seismicity rate forecast performed by using the uniform reference rate is  
246 larger than that obtained for the non-uniform reference rate and the opposite is found for  
247 forecasted seismicity rate changes inferred by using the background rates (constant and  
248 spatially non-uniform).

249 This apparent paradox can be explained by considering that the signs of the Coulomb  
250 stress changes affect the computed cumulative number of triggered aftershocks. A high  
251 reference seismicity rate in a stress shadow area will not produce any enhanced seismicity  
252 rate changes. On the contrary, a higher reference rate in a region of enhanced Coulomb  
253 stress will produce a significant increase of seismicity rate. Therefore, the expected seis-  
254 micity rate change will strongly depend on the spatial correlation between applied stress  
255 changes and the background or reference seismicity rates. In particular, high seismicity  
256 rate changes are expected for positive correlations, but irrelevant changes of the rate of

257 earthquake production for anti-correlations. Therefore, the opposite results found for the  
258 1992 Landers and the 1997 Kagoshima earthquakes depend on the different correlation  
259 between the spatial pattern of Coulomb stress changes and seismicity rate changes.

260 Figure 6 shows the map of Coulomb stress changes computed at 7.5 km depth (mid of  
261 the seismogenic layer) after the 1992 Landers main shock (left panel) and after the main  
262 shock and the Big Bear aftershock (right panel) using equation (2) and resolving stress  
263 changes onto prescribed target vertical faults striking N330° (dip 90°) with a rake angle of  
264 180°. The slip distribution for the Landers earthquake used for these calculations is taken  
265 from Wald and Heaton (1994), while for the Big Bear earthquake is taken from Jones and  
266 Hough (1995). The stress changes are computed for:  $\alpha = 0.25$ ,  $\mu = 0.75$  and  $B = 0.47$   
267 (which yields  $\mu' = 0.4$ ). Using these stress changes we have calculated the seismicity rate  
268 changes through equations (4), (6) and (9). A visual comparison between figures 2 and 6  
269 reveals that a large area with high background or reference seismicity rates lies in stress  
270 shadows.

271 Although non-uniform background seismicity can be expected from a physical point  
272 of view, the application of inhomogeneous reference or background models should be  
273 taken with care. First, an appropriate estimation of the spatial seismicity fluctuations  
274 requires a better data coverage than is available in many applications. Second, because  
275 of the above mentioned dependence on the spatial correlation, non-uniform background  
276 models are more sensitive to the calculated stress changes, which are known only with  
277 large uncertainties due to uncertain slip distribution, fault geometry and small-scale stress  
278 heterogeneities (see Sudhaus and Jónsson, 2009; Hainzl et al., 2009, for further discussion).

### 3.2. $A\sigma$ and the stressing rate

The effects of individual input parameters in the Dieterich model have been previously discussed in the literature (see Belardinelli et al., 1999; Toda and Stein, 2003; Catalli et al., 2008, and references therein). Indeed, it is well known that  $A\sigma$  controls the instantaneous increase of the seismicity rate: the smaller the  $A\sigma$  value the larger the seismicity rate change. Equations (6) and (7) show that this parameter controls both the instantaneous change and the following evolution of the state variable  $\gamma$ . Console et al. (2006) and Catalli et al. (2008) have shown that the total number of triggered events over infinite times does not depend on  $A\sigma$ . Indeed, the time integral of the net rate of promoted seismicity  $R'(t) = R(t) - r$  over infinite times is given by

$$N_\infty = \int_0^{+\infty} R'(t)dt = \frac{r}{\dot{\tau}}S. \quad (11)$$

279 According to this relation the net number,  $N_\infty$ , of promoted earthquakes over infinite  
 280 times depends only on the background rate, the stressing rate and the Coulomb stress  
 281 perturbation.

The role of the stressing rate on the predicted seismicity rate changes has been already discussed in the literature (see Toda et al., 2002; Llenos et al., 2009). It is evident from equations (5) and (9) that the stressing rate  $\dot{\tau}$  controls the state variable evolution before and after the stress perturbation. The stressing rate is of particular importance for modeling the seismicity rate changes and the Omori-like aftershock decay because it controls for a given  $A\sigma$  the duration of the aftershock sequence. Indeed, one of the relevant implications of the Dieterich (1994) approach is that the aftershock duration  $t_a$

does not depend on the magnitude of the main shock and it is controlled by

$$t_a = \frac{A\sigma}{\dot{\tau}}. \quad (12)$$

Thus, the rate-and-state dependent friction model for seismicity rate changes can equiv-  
 alently be stated by the three parameters  $r, A\sigma, t_a$  instead of  $r, A\sigma, \dot{\tau}$ . Finally, despite  
 equation (11) predicts that the total number of triggered events over infinite times does  
 not depend on  $A\sigma$ , we emphasize that for time periods shorter than  $t_a$ , the adopted  $A\sigma$   
 value affects the cumulative number of triggered earthquakes.

#### 4. Correlations between parameters

The model parameters are strongly correlated for physical and statistical reasons. Based  
 on the the balance of seismic moment release, Catalli et al. (2008) deduced an analytically  
 approximate relation to link the stressing rate to the reference seismicity rate, under  
 the assumption that  $r$  accounts for all the events in a given magnitude range without  
 declustering:

$$\dot{\tau} \cong \frac{rM_0^*}{W_{seis}} \frac{b}{1.5 - b} (10^{(1.5-b)(M_{max}-M^*)} - 1) \quad (13)$$

where  $r$  is the reference seismicity rate,  $M_0^*$  the seismic moment of the magnitude  $M^*$   
 earthquake,  $W_{seis}$  the thickness of the seismogenic zone (Catalli et al., 2008),  $b$  is the  
 parameter of the Gutenberg-Richter distribution,  $M_{max}$  and  $M^*$  are the maximum and  
 minimum magnitudes, respectively. Note that in (13) the reference seismicity  $r(x, y)$  must  
 include all the earthquakes in the given magnitude range to estimate the stressing rate  
 through the proposed approximate relation. We emphasize that this relation suggests the  
 input parameters  $\dot{\tau}$  and  $r$  of the physics-based model to be linearly correlated. According  
 to (12) and(13) a spatially variable stressing rate (inferred from a spatially non-uniform

reference seismicity rate) implies a spatially variable aftershock duration time  $t_a$ . This in  
turns impacts the forecasted seismicity rate changes.

In addition, relation (13) and equation (11) predict that the total number of triggered  
earthquakes over infinite times only depends on the stress change amplitude. This implies  
that assessing the variability of Coulomb stress changes is extremely important (Hainzl  
et al., 2009).

Even stronger correlations between the parameters are obtained from a statistical point  
of view if early aftershock data are available and are used to constrain input parame-  
ters for forecasting attempts. We demonstrate in the following that in the case of an  
observationally constrained aftershock decay, the background rate  $r$  and the aftershock  
relaxation time  $t_a$  are strongly correlated to determine the aftershock productivity. This  
implies that according to (12) and (13) all the three main input parameters of the rate  
and state approach are correlated.

According to the Dieterich (1994) model, the seismicity rate changes caused by a stress  
perturbation  $S$  (at time  $t = 0$ ) can be also written in the following way, which is equivalent  
to (4),

$$R = \frac{r}{1 + \left[ \exp\left(-\frac{S}{A\sigma}\right) - 1 \right] \cdot \exp\left(-\frac{t}{t_a}\right)}. \quad (14)$$

Using relation (12) and defining  $\psi = \exp\left(-\frac{S}{A\sigma}\right)$ , we can write (14) as

$$R = \frac{r}{1 + (\psi - 1) \cdot \exp\left(-\frac{t}{t_a}\right)}, \quad (15)$$

which for  $t \ll t_a$  becomes

$$R \approx \frac{r}{1 + (\psi - 1) \cdot \left(1 - \frac{t}{t_a}\right)} = \frac{r}{\psi - (\psi - 1) \cdot \left(\frac{t}{t_a}\right)}. \quad (16)$$

After simple rearrangements (16) is written as

$$R \approx \frac{\frac{rt_a}{1-\psi}}{\left[\frac{\psi t_a}{1-\psi} + t\right]}, \quad (17)$$

which is the Omori law with a  $p$ -value equal to 1, the  $c$ -value is given by

$$c = \psi t_a / (1 - \psi) \quad (18)$$

and the productivity by

$$K = rt_a / (1 - \psi) \quad (19)$$

308 These equations show that the productivity depends not only on the stressing rate (see  
 309 Llenos et al., 2009), but also on the background rate and the parameter  $A\sigma$ . However,  
 310 if equation (13) holds and  $\dot{\tau}$  is linearly proportional to  $r$ ,  $\frac{r}{\dot{\tau}}$  becomes constant and the  
 311 productivity only depends on  $A\sigma$ .

312 If the stress jump is large compared to the parameter  $A\sigma$ , then  $1 - \psi \approx 1$  and the  
 313 Omori parameters become  $c \simeq \exp(-\Delta S/A\sigma) \cdot t_a$  and  $K \simeq rt_a$  (see Dieterich, 1994). For  
 314  $c < t \ll t_a$ , the rate decays according to  $R \approx K/t$  and thus if the  $t_a$  is changed by a  
 315 factor  $\kappa$ , the background rate  $r$  has to be changed by a factor  $1/\kappa$  to fit the same observed  
 316 decay. To get a similar fit on short time scales ( $t \ll t_a$ ), the  $c$ -value should be also the  
 317 same. Our calculations imply that for a spatially uniform background rate  $r$  and tectonic  
 318 loading  $\dot{\tau}$ , the aftershock duration  $t_a$  is also uniform but not the productivity  $K$  and the  
 319  $c$ -value. The latter parameter defines the delay before the onset of the  $1/t$ -decay. The  $c$   
 320 parameter and the productivity depend on the  $\Delta CFF$ -value of the stress changes which  
 321 will be spatially non-uniform and distance dependent. This implies that  $K$  and  $c$  will  
 322 depend on the spatial coordinates (i.e., spatially variable) due to the spatial fluctuations  
 323 of  $(1 - \psi)$  around 1 and  $\psi$  above zero, respectively. The superposition of aftershock



324 sequences with  $c$ -values differing in this way has previously shown to result in apparent  
 325  $p$  values  $< 1$  for an exponential stress distribution [Helmstetter & Shaw 2006]. Smaller  
 326  $p$ -values at the beginning of aftershock sequences have been reported in several previous  
 327 studies that use high-resolution waveform data to quantify early aftershocks (Peng et al.,  
 328 2006, 2007; Enescu et al., 2007; 2009).

Using the constraints from observations of the earliest aftershocks, namely the  $K$  and  
 $c$ -value, the only free parameter that remains in (14) is  $t_a$ . Taking equations (18) and (20),  
 we can express  $r$  and  $\psi$  as a function of the aftershock duration time  $t_a$ ,  $\psi = c/(c + t_a)$   
 and  $r = K/(c + t_a)$ , and we get

$$R(t) = \frac{K}{c + t_a - t_a \exp\left(-\frac{t}{t_a}\right)}, \quad (20)$$

329 which holds for  $t < t_a$ .

330 Figure 7 summarizes the correlation between input parameters for the rate and state  
 331 model. Indeed, this figure shows that, locally (i.e., for a given value of stress perturba-  
 332 tion), almost the same decay caused by a positive or a negative stress step on short and  
 333 intermediate time scales is achieved for different combinations of input parameters which  
 334 follow the functional dependencies:  $r \cdot t_a = \text{const}$  and  $\psi \cdot t_a = \text{const}$ .

335 Thus, if early aftershock observations are available to constrain the seismicity decay, the  
 336 frictional parameters should not be set independently but rather in accordance with the  
 337 above mentioned relations. Aftershock forecasts that take these correlations implicitly into  
 338 account by maximizing the likelihood function for the earliest aftershocks are discussed  
 339 for the Landers case by Hainzl et al. (2009).

## 5. Forecasting seismicity rate changes

340 In this section we present as an example simulations of the rate of earthquake production  
341 caused by the 1992 Landers earthquake. We compare and discuss the model predictions  
342 based on stress changes calculated by resolving stress onto prescribed receivers as well  
343 as onto OOPs. Figure 8 displays the predicted seismicity rate changes computed from  
344 mean Coulomb stress perturbations, averaged between stress changes estimated at 7 and  
345 11 km depth, both immediately after the main shock (panels a and b) and 30 days after  
346 it (panels c and d); thus, the latter includes also the stress perturbations caused by the  
347 Big Bear aftershock. The calculations are performed using the Dieterich (1994) model  
348 resolving stress changes onto prescribed receivers oriented as those used for Figure 4 (a  
349 and c) as well as onto OOPs associated with a horizontal  $\sigma_1$  oriented  $N7^\circ$ , a vertical  $\sigma_2$   
350 and a horizontal  $\sigma_3$  (b and d). Here we have assumed the uniform background seismicity  
351 rate (0.086 events/day, corresponding to  $1.5 \cdot 10^{-6}$  events/day  $\text{km}^2$ ) shown in Figure 1,  
352 a constant stressing rate ( $2 \cdot 10^{-6}$  MPa/day) and a value for  $A\sigma$  equal to 0.02 MPa. As  
353 discussed in the previous section several combinations of these parameters can yield the  
354 same forecasts of seismicity rate if the proposed scaling is respected.

355 This figure confirms that when the only difference is resolution of stress perturbations  
356 onto prescribed receivers or OOPs a completely different pattern of forecasted rate of  
357 earthquake production may result. This is evident close to the causative faults, where  
358 seismicity shadows predicted by the model for stress perturbations resolved onto pre-  
359 scribed receivers become enhanced seismicity rates for OOPs model. In order to further  
360 point out this finding, we have shown in Figure 9 the difference between the seismicity

361 rate changes computed for the prescribed receivers and the OOPs models. As expected  
362 the largest difference is found around the causative faults.

363 The difference between forecasted rates of earthquake production computed adopting  
364 OOPs and prescribed receivers is evident also in the aftershock decay following the main  
365 shock. Figure 10 shows the decay rate of aftershocks predicted through mean stress  
366 changes (averaged between values estimated at 7 and 11 km depth, as in Figure 8) resolved  
367 onto OOPs (red curves) and onto prescribed receivers (blue curves). Dashed curves display  
368 the aftershock decay in areas which experienced mean stress changes smaller than 0.5 MPa,  
369 while solid curves show the whole aftershock decay for unconstrained stress perturbations.  
370 This figure suggests that the difference decreases for increasing time after the main shock.  
371 The peak in the aftershock decay shown in Figure 10 is the seismicity rate change caused  
372 by the Big Bear aftershock.

373 In some previous studies (Toda et al., 2003; Steacy et al., 2004) the authors proposed  
374 excluding seismicity close to the causative faults in order to improve the forecasted seis-  
375 micity rate changes. Figure 10 shows the consequences of limiting the computed Coulomb  
376 stress changes, which indirectly corresponds to excluding near-fault regions. This figure  
377 suggests that the choice of this simulation strategy has important implications on the  
378 predicted temporal decay of early aftershocks.

## 6. Discussions and conclusive remarks

379 The application of physics-based models to near real-time forecast attempts requires a  
380 robust validation through retrospective modeling and statistical tests. In order to perform  
381 these applications the input model parameters have to be constrained a priori based on the  
382 available data and information for the target study area. Previous studies constrain model

383 parameters with different strategies and sometimes without a comprehensive analysis  
384 of their correlation. In this study we aim to understand the impact of physical model  
385 parameters in forecasting seismicity rate changes.

386 We use the Dieterich (1994) model which is widely used to simulate the changes in the  
387 rate of earthquake production caused by stress changes. In this study we focus on the  
388 main input parameters of the Dieterich's approach: the physical constitutive properties of  
389 faults (represented by the parameter  $A\sigma$ ), the stressing rate and the reference seismicity  
390 rate of the study area. Hainzl et al. (2009) have discussed the effect of the variability of  
391 the amplitude of stress perturbations as well as the effect of small-scale heterogeneities  
392 characterizing the stress change pattern near the causative faults (see also Marsan, 2006;  
393 Helmstetter and Shaw, 2006).

394 A number of input parameters have to be constrained to compute stress perturbations  
395 and the associated seismicity rate changes. These model parameters are strongly corre-  
396 lated. Our inferred correlations demonstrate that different sets of model parameters can  
397 yield the same rate of aftershock decay. In particular, the rate-and-state dependent fric-  
398 tion model for seismicity rate changes can equivalently be formulated in terms of the three  
399 parameters  $r, A\sigma, \dot{\tau}$ , as well as  $r, A\sigma, t_a$ . One relevant implication is that the inferred cor-  
400 relations do not allow the physical interpretation of adopted values of model parameters.  
401 In other words, it is difficult to compare values of  $A\sigma$  parameter inferred from modeling  
402 the rate of earthquake production with those resulting from laboratory experiments of  
403 rock friction. At the same time, it is difficult to constrain  $A\sigma$  from the aftershock decay  
404 parameter  $t_a$ , as commonly done in the literature, because this estimate depends on the  
405 correlation with the stressing rate  $\dot{\tau}$ .

406 An important choice is the definition of the background seismicity rate, in particular,  
407 the use of declustered or non-declustered precursory seismicity and its spatial variability.  
408 Despite the use of spatially variable reference or background seismicity rates is physically  
409 reasonable and corroborated by observations (see Toda and Stein, 2003; Zhuang et al.,  
410 2002; Toda et al., 2005, among many others), the application of these models is not  
411 straightforward because of the spatial correlation between seismicity rate and the pattern  
412 of calculated stress perturbations. Indeed, spatially non-uniform background models are  
413 more sensitive to the uncertainties of slip distribution as well as to the heterogeneity of  
414 stress patterns. This can discourage the adoption of non-uniform reference or background  
415 seismicity rates to forecast the rate of earthquake production.

416 Assuming a constant background seismicity rate has also implications on the stressing  
417 rate. Catalli et al. (2008) have used spatially variable stressing rate patterns inferred  
418 from non-uniform reference seismicity rates through relation (13). However, this choice  
419 implies: (i) a dependence on the maximum magnitude for the study area, (ii) a spatially  
420 variable  $t_a$ , (iii) the lack of a depth dependence (since  $\dot{\tau}$  is computed from seismicity  
421 in the whole seismogenic layer) and, finally, (iv) a correlation between two out of three  
422 input parameters of the Dieterich model ( $r$  and  $\dot{\tau}$  or  $t_a$ ). For these reasons, a constant  
423 stressing rate seems to be preferable together with a spatially uniform reference seismicity  
424 rate. These considerations also suggest to conclude that using the background seismicity  
425 rate instead of the reference rate is a more effective assumption to forecast the rate of  
426 earthquake production. This will also guarantee to better satisfy the assumption of a  
427 stationary seismicity rate before the application of the stress perturbation.

428 Llenos et al. (2009) discuss the effect of temporal changes of stressing rate caused by  
429 aseismic deformation and their effect to the background and the aftershock rates. In  
430 agreement with these authors, we have shown in this study that the aftershock productiv-  
431 ity depends on the stressing rate (see equations 17 and 20). Llenos et al (2009) analyzed  
432 the rate of earthquake production during several seismic swarms and concluded that the  
433 stressing rate transients increase the background seismicity rate without affecting the  
434 clustered (i.e., triggered) seismicity rate. This contradicts the predictions of the Dieterich  
435 (1994) model, when background seismicity and stressing rates are assumed to be uncor-  
436 related (as in numerous applications published in the literature). In the present study,  
437 we investigate the rate of earthquake production following a large earthquake. We as-  
438 sume that the stressing rate does not change before and after the application of the stress  
439 perturbation. This also allows the use of Coulomb stress changes (instead of shear stress  
440 perturbations) to model the evolution of the gamma variable. Our results suggest that  
441 for aftershock sequences the productivity depends on both the background seismicity and  
442 the stressing rates (see equation 17) and that, because of the correlation between model  
443 parameters, it is impossible to separate their contributions by analyzing aftershock decay  
444 rates in real sequences.

445 The analysis of correlations among model parameters discussed in this study (equations  
446 16 and 17) relies on the assumption that  $t \ll t_a$ . The inferred correlations are relevant  
447 for near-real time (i.e., short term) forecast attempts. Indeed, we have shown that these  
448 correlations hold at short time scales. However, the definition of "short" time scale de-  
449 pends on  $t_a$ . It has to be noted, however, that the predicted aftershock decay for longer  
450 times (that is, when  $t \ll t_a$  does not hold) might deviate from the expected Omori law.

451 Finally, we emphasize that two alternative modeling strategies to resolve Coulomb stress  
452 changes on target receivers (OOPs or prescribed receivers), which are both likely choices  
453 for near real time applications, yield very different predictions of seismicity rate changes  
454 (see Steacy et al., 2005b). In particular, these authors and Hainzl et al. (2009) concluded  
455 that models that incorporate the regional stress field (i.e., OOPs) tend to produce stress  
456 maps that best fit the observed spatial aftershock distribution. We emphasize, however,  
457 that the improved ability to forecast seismicity rate changes may be achieved renouncing  
458 to match the aftershock focal mechanisms. We also point out here that the expected  
459 variations in modeled Coulomb stress changes through equations (2) and (3) represent a  
460 further contribution to the uncertainties in stress perturbation amplitudes. This further  
461 suggests the need to include uncertainties and variability of stress amplitudes in forecasting  
462 seismicity rate changes.

463 The results of the present study are of relevance to: (i) identify reliable strategies for  
464 constraining model parameters for forecasting attempts; (ii) interpret the result of the  
465 retrospective statistical tests (see Woessner et al., 2009); (iii) emphasize the necessity of  
466 reducing the "a priori" choices to compute Coulomb stress perturbations.

467 Most of applications constrain model parameters from seismicity before the origin time  
468 of the causative main shock, thus analyzing the background seismicity rate. However, the  
469 results of this study suggest that early aftershocks, when available, can also be used to  
470 constrain model parameters. This can be done, for instance, by computing background  
471 stationary seismicity rate through the ETAS approach. This strategy is novel and original  
472 and relies on the acknowledgment that model parameters have to be constrained taking  
473 into account their correlations and the scaling relations proposed in this study.

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599 **Figure Captions**

600 **Figure 1.** Reference  $r(x, y)$  (a) and background  $\mu(x, y)$  (b) seismicity rates computed  
 601 for the study area. Red dots show the epicenter of the 1992 Landers mainshock and the  
 602 Big Bear aftershock. The reference seismicity rate is computed in the 8 years preceding  
 603 the 1992 main shock (1984-1991) using the Frankel algorithm for smoothing the seismicity  
 604 of a complete (undeclustered) catalog (see text for the details of these calculations). The  
 605 background seismicity rate has been computed through equation (10) and the ETAS  
 606 approach. The black dots in this figure indicate the epicenters of earthquakes occurred  
 607 before the 1992 Landers main shock, while the gray dots depicts the aftershock locations.

608

609 **Figure 2.** Difference between the spatially non-uniform seismicity rate and the average  
 610 value measured for the whole area: (a) displays the difference for the reference seismicity  
 611 rate, while (b) shows that one for the background seismicity rate. Red and blue colors  
 612 indicate a local value larger or smaller than the average value, respectively.

613 **Figure 3.** Cumulative number of events calculated through the Dieterch (1994) model  
 614 assuming a spatially non-uniform reference and background seismicity rates (solid curves)  
 615 and a constant reference and background seismicity rates corresponding to their average  
 616 values (dashed curves). For all these calculations the stressing rate is constant  $\dot{\tau} =$   
 617  $5.6 \cdot 10^{-6}$  MPa/day and  $A\sigma = 0.04$  MPa. Blue curves identify the calculations performed

618 by adopting the reference seismicity rates and green curves shows those performed by  
 619 using the background seismicity rate.

620 **Figure 4.** Reference  $r(x, y)$  (a) and background  $\mu(x, y)$  (b) seismicity rates computed  
 621 for the 1997 Kagoshima prefecture (Japan) earthquake. The red dots show the epicenter  
 622 of the two strike slip earthquakes ( $M \sim 6$ ) occurred 48 days apart from each other. The  
 623 background seismicity rate is computed by applying the ETAS approach to the seismic  
 624 catalog provided by JMA, while the reference seismicity rate by smoothing the seismicity  
 625 in the 10 years preceding the first Kagoshima main shock (see text for the details of these  
 626 calculations). The black dots in this figure indicate the epicenters of earthquakes occurred  
 627 before the first main shock, while the gray dots depicts the aftershock locations.

628 **Figure 5.** Cumulative number of events calculated through the Dieterch (1994) model  
 629 assuming a spatially non-uniform reference and background seismicity rates (solid curves)  
 630 and a constant reference and background seismicity rates corresponding to their average  
 631 values (dashed curves) for the 1997 Kagoshima earthquake. For all these calculations the  
 632 stressing rate is constant  $\dot{\tau} = 3.0 \cdot 10^{-6}$  MPa/day and  $A\sigma = 0.04$  MPa (Toda and Stein,  
 633 2003). Blue curves identify the calculations performed by adopting the reference seismicity  
 634 rates and green curves shows those performed by using the background seismicity rate.

635 **Figure 6.** Static Coulomb stress changes computed at 7.5 km depth immediately after  
 636 the 1992 Landers main shock (left panel) and after the Big Bear aftershock (right panel;  
 637 thus including both the main shock and the aftershock) using the constant apparent



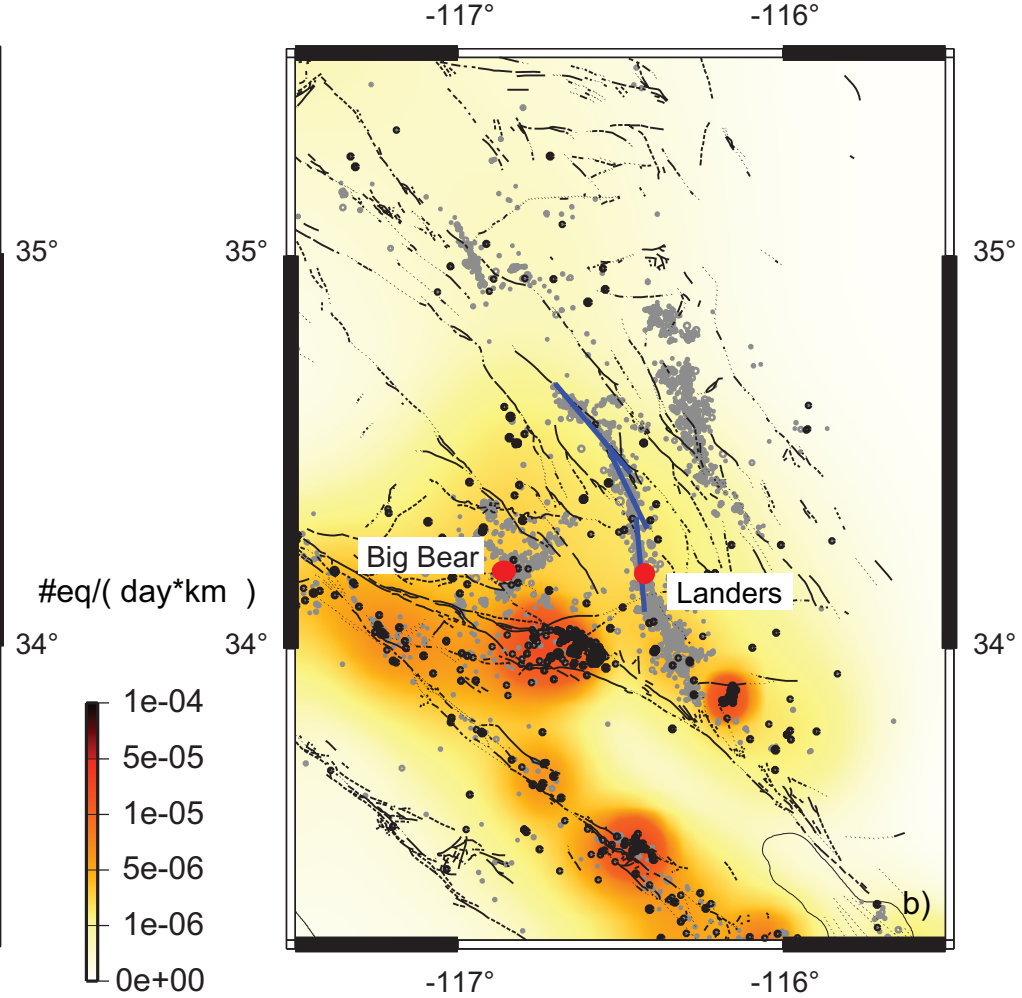
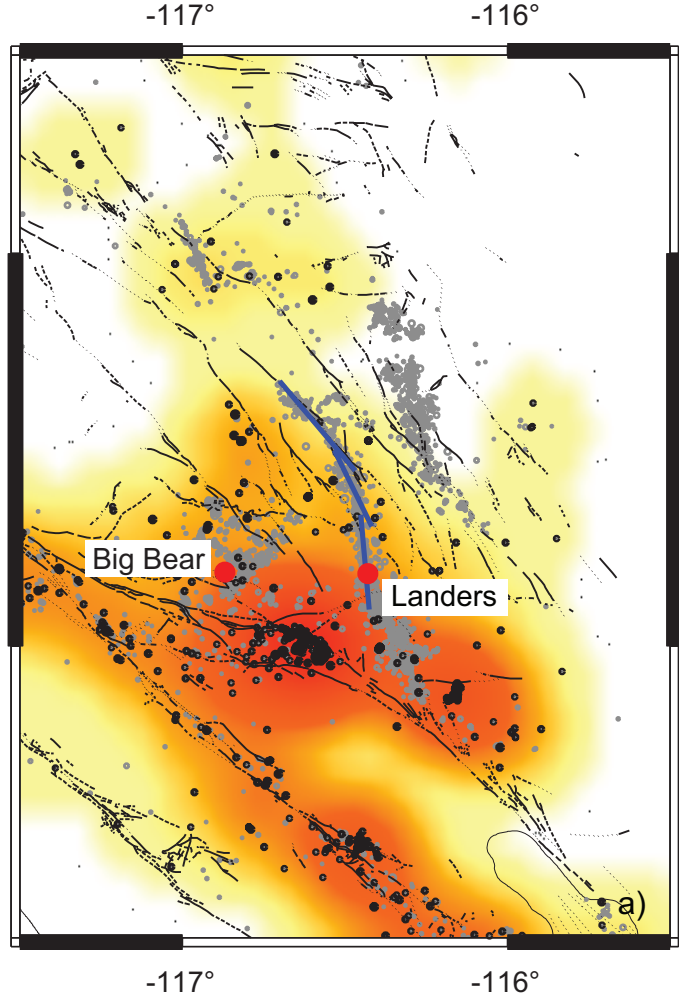
friction model (equation 2,  $\mu' = 0.4$ ) and resolving stress changes onto prescribed vertical strike slip faults striking  $N330^\circ$  (rake angle  $180^\circ$ ). The slip distribution and the fault geometry for the 1992 Landers earthquake are taken by Wald and Heaton (1994), while for the Big Bear aftershock from Jones and Hough (1995).

**Figure 7.** Rate of aftershock production in a log-log scale caused by a positive (left panel) and a negative (right panel) stress perturbations. These simulations have been performed using a stress step of 0.3 MPa. Colors indicate different combinations of the aftershock duration  $t_a$ , background rate  $r$  and  $A\sigma$  parameter. The same rate decay in the first days after the stress perturbation is obtained by different combinations of input parameters. This figure suggests an inverse correlation between background seismicity rate and aftershock duration  $r \sim \frac{1}{t_a}$ .

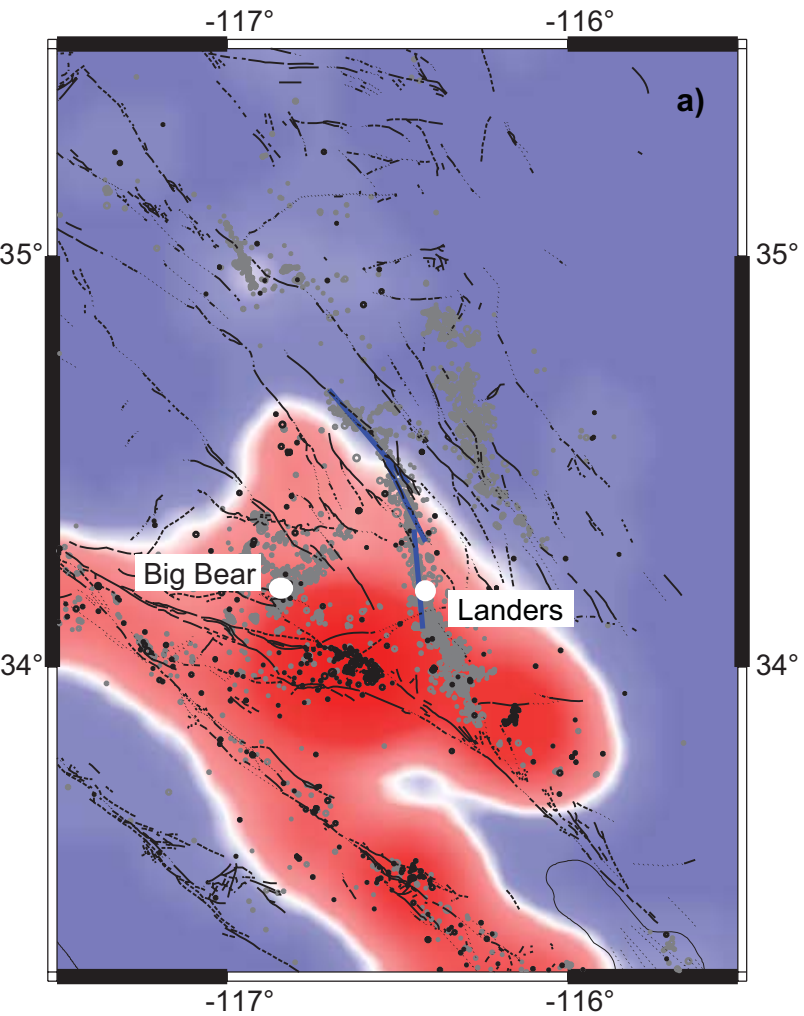
**Figure 8.** Spatial distribution of predicted seismicity rate changes computed immediately after the 1992 Landers earthquake (panels a, b) and 30 days after the main shock (panels c, d). Panels on the left (a and c) displays the calculations performed for prescribed receivers oriented as those used for Figure 4, while panels on the right (b and d) shows those performed for OOPs associated with a horizontal  $\sigma_1$  oriented  $N7^\circ$ , a vertical  $\sigma_2$  and a horizontal  $\sigma_3$ . The parameters adopted for computing Coulomb stress perturbations are those used for Figure 4. Coulomb stress perturbations are computed by averaging stress changes estimated at 7.0 km and 11 km depth. Seismicity rate changes shown in panels (b) and (d) are caused by both the Landers main shock and the Big Bear aftershock.

658 **Figure 9.** Spatial distribution of the difference between the seismicity rate changes  
659 computed from prescribed receivers and OOPs. The left and the right panels show the  
660 seismicity rate difference from stress changes calculated immediately after the 1992 Lan-  
661 ders earthquake and 30 days after the main shock, respectively.

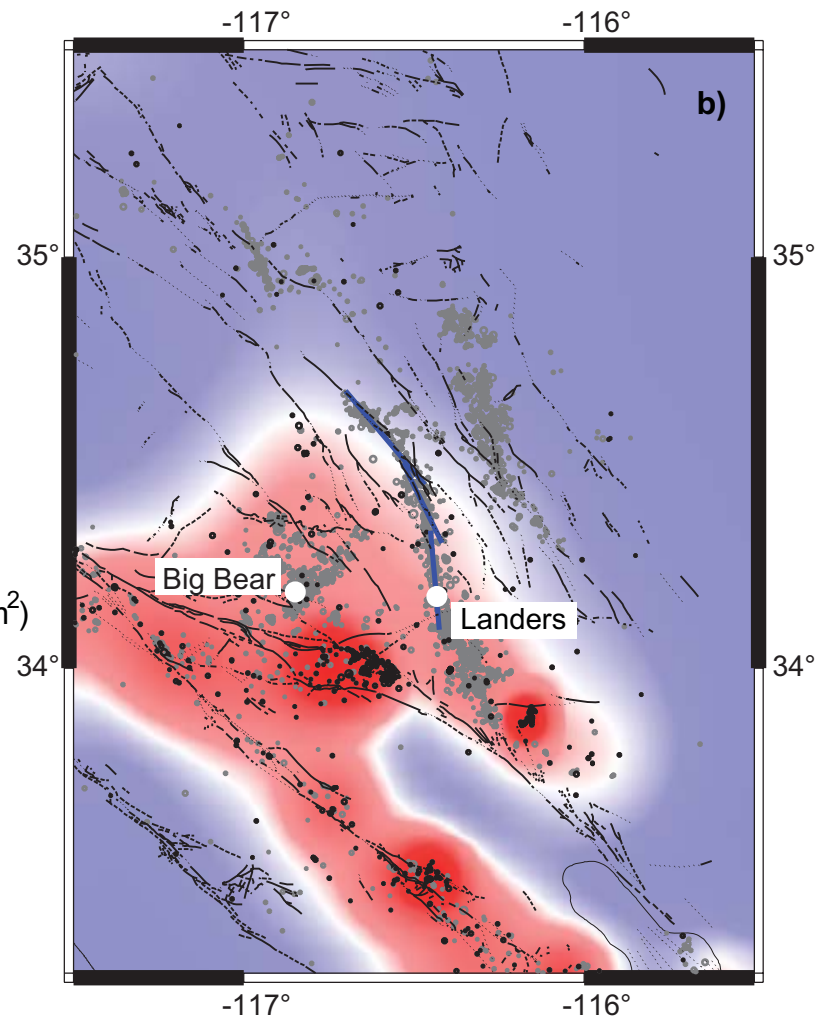
662 **Figure 10.** Temporal decay of the normalized seismicity rate changes  $\frac{R}{r}$  computed  
663 for OOPs (red curves) and for prescribed receivers (blue curves). Dashed lines indicate  
664 the aftershock rate decay in areas that experienced stress changes less than 0.5 MPa,  
665 while solid curves illustrate the decay rate for unrestricted stress perturbations. Input  
666 parameters for these calculations are those used for Figure 8. Seismicity rate changes  
667 are computed from mean Coulomb stress changes averaged from stress perturbations  
668 estimated at 7 and 11 km depth.

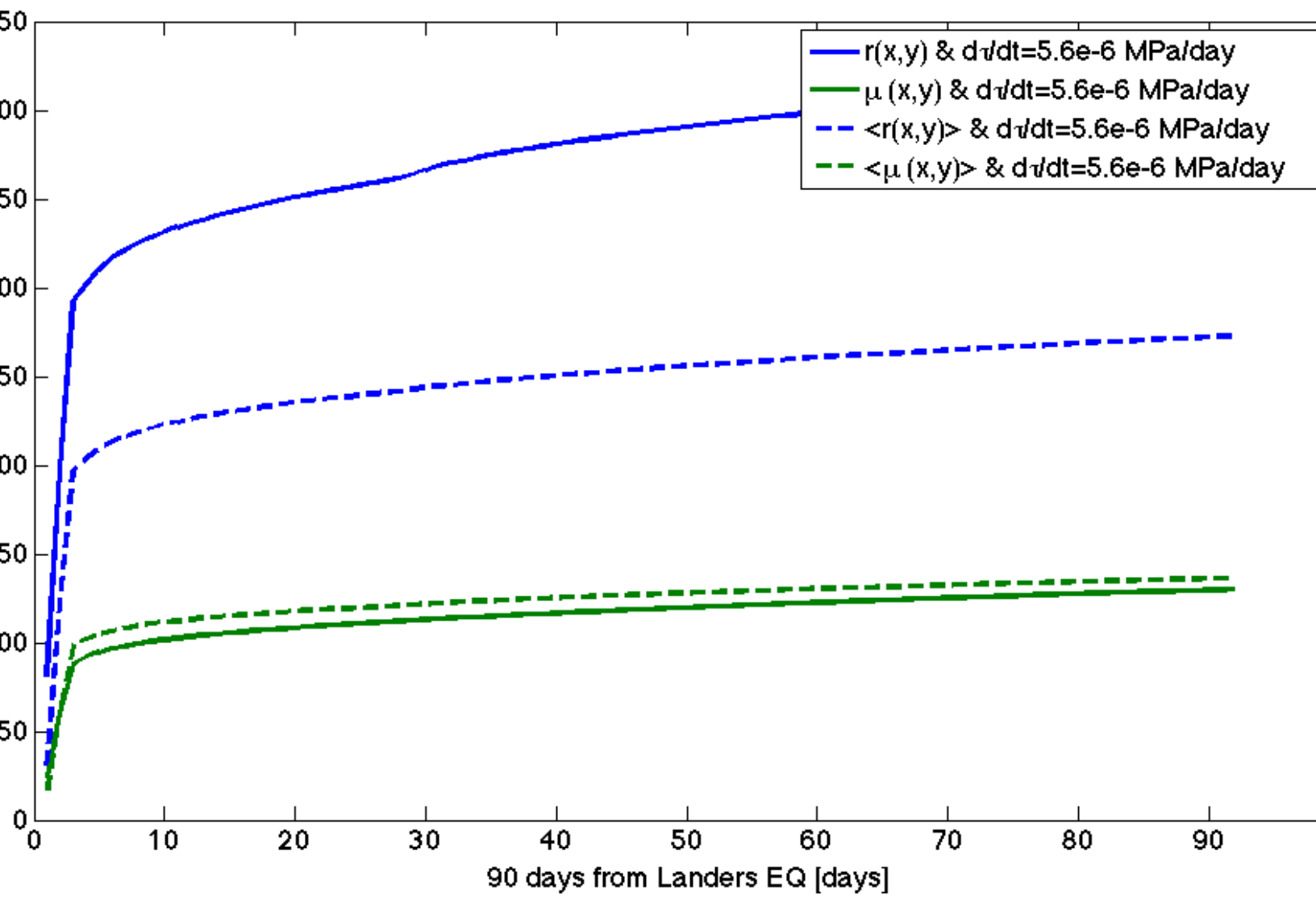


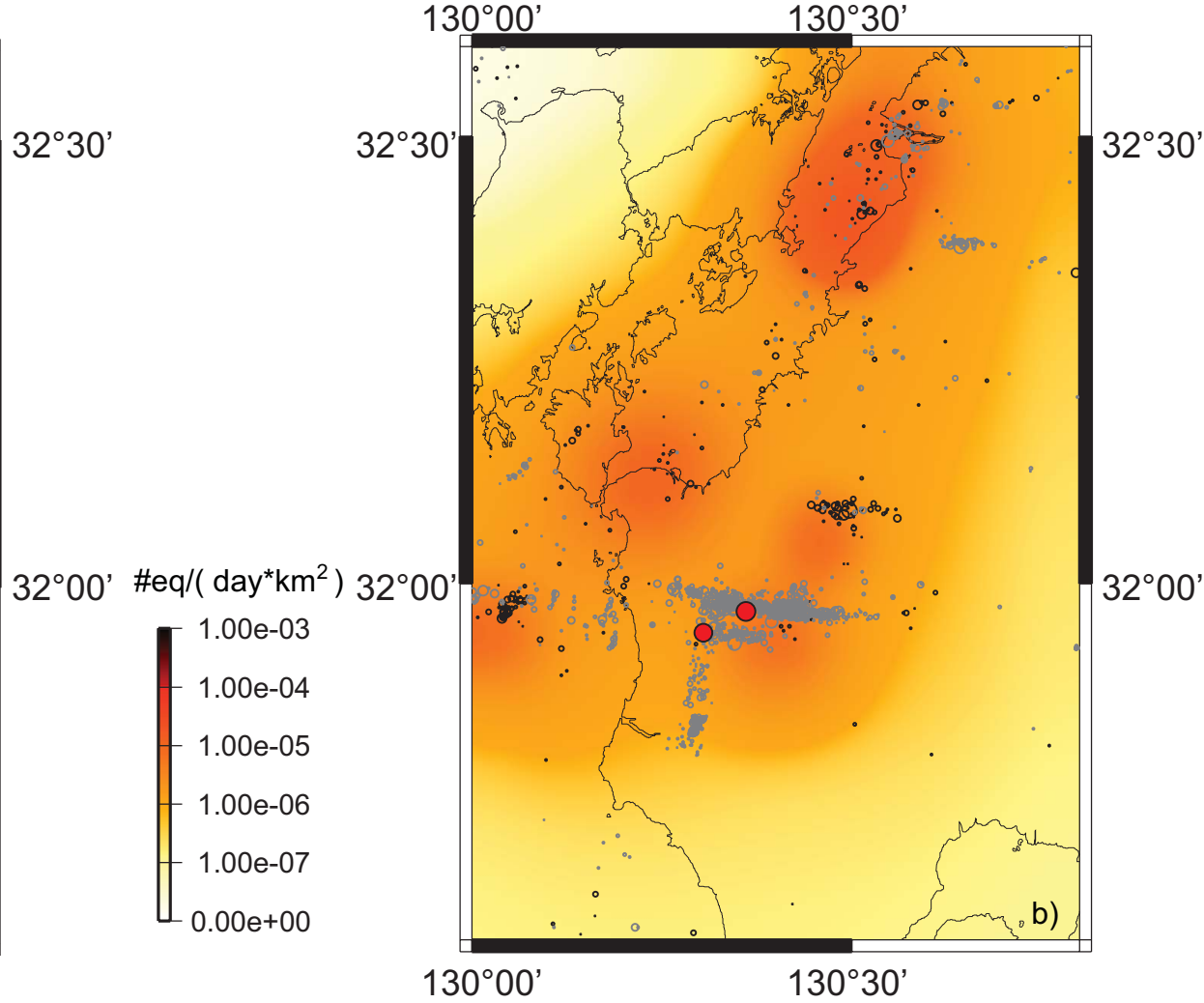
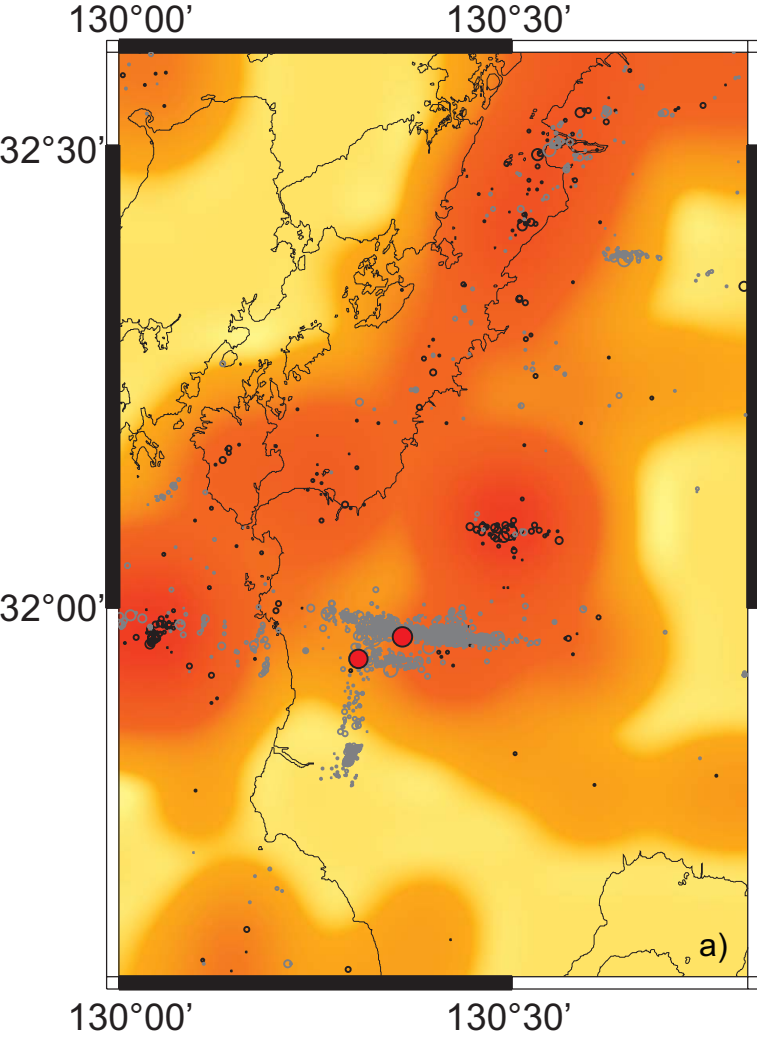
# Reference seismicity

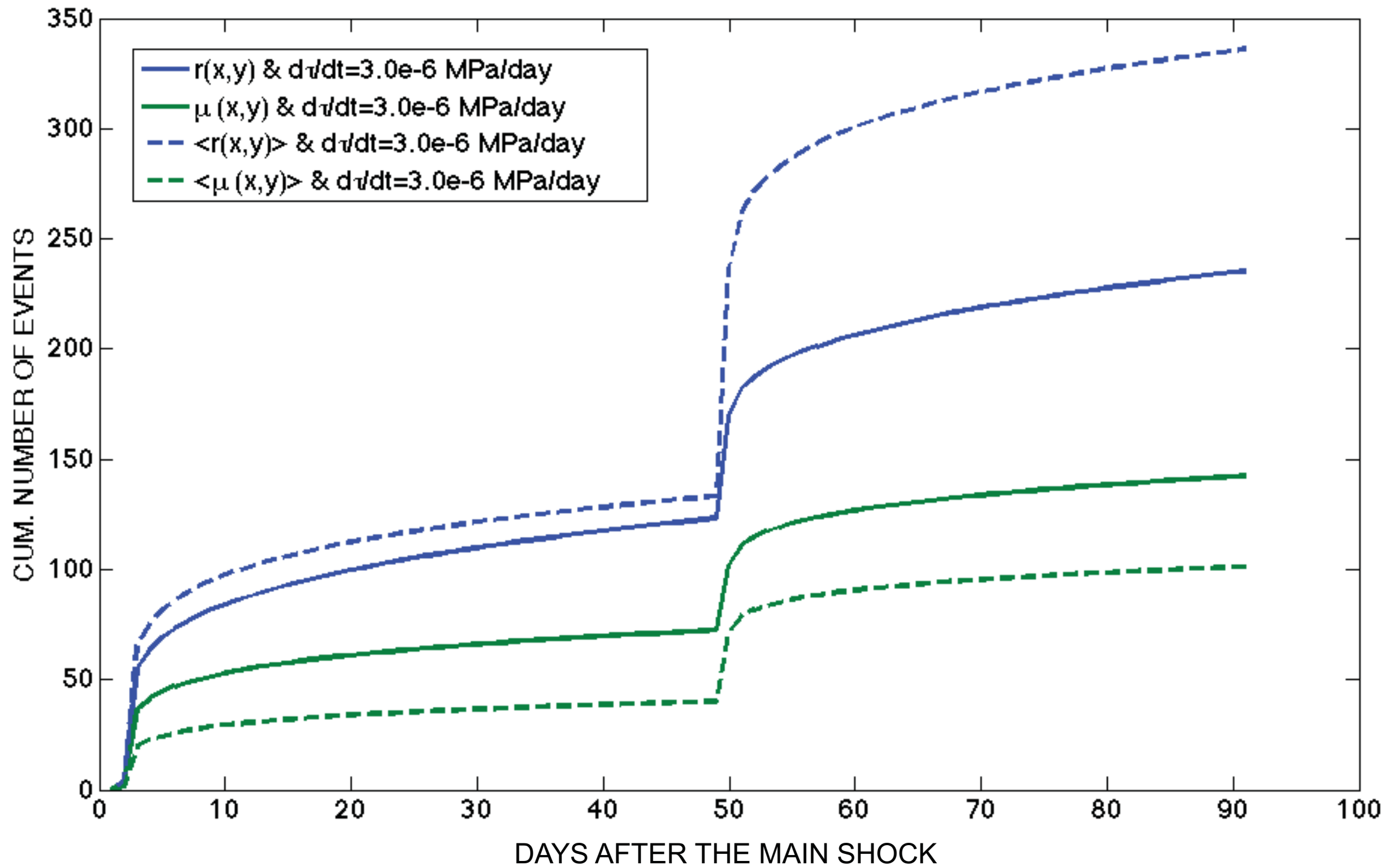


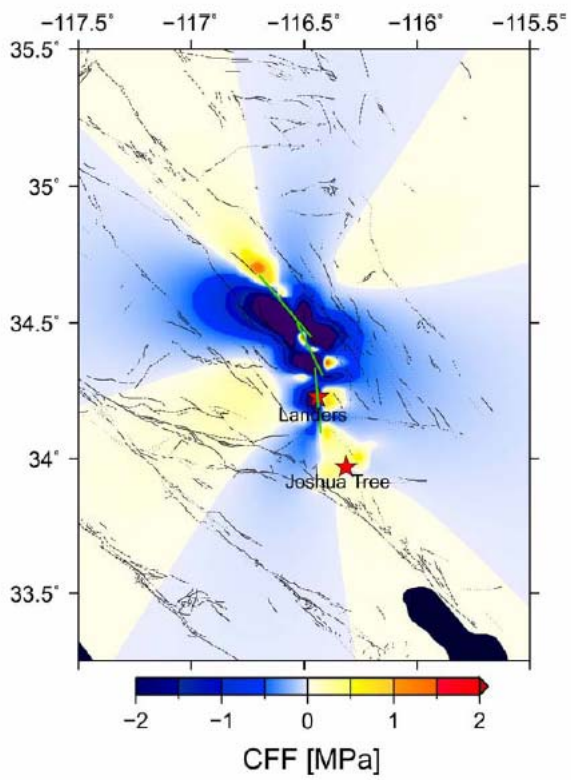
# Background seismicity



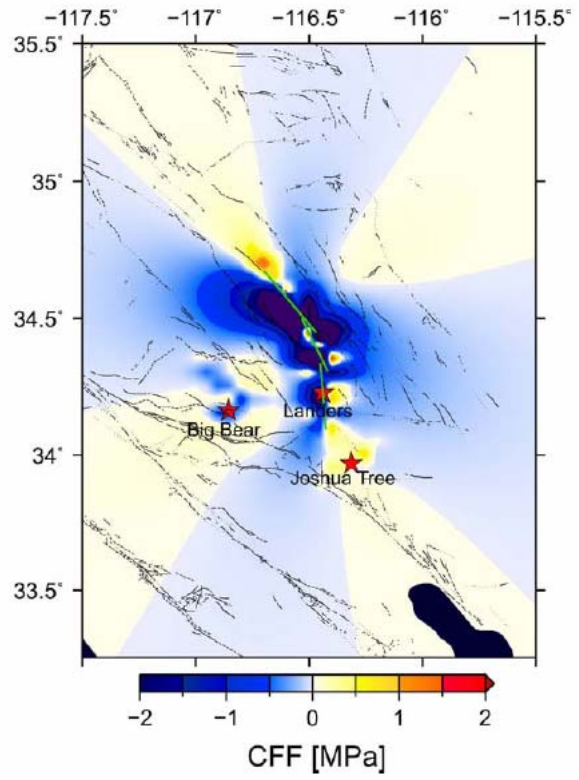








Map of CFF after Landers occurrence.



Map of CFF after Landers and Big Bear occurrences.



