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# Temporal evolution of long-period seismicity at Etna Volcano, Italy, and its relationships with the 2004–2005 eruption

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## Abstract

Between December 2004 and August 2005, more than 50,000 long-period events (LP) accompanied by very-long period pulses (VLP) were recorded at Mt. Etna, encompassing the effusive eruption which started in September 2004. The observed activity can be explained by the injection of a gas slug formed within the magmatic column into an overlying cavity filled by either magmatic or hydrothermal fluids, thus triggering cavity resonance. Although a large number of LP events exhibit similar waveforms before the eruption, they change significantly during and after the eruption. We study the temporal evolution of the LP-VLP activity in terms of the source movement, change of the waveforms, temporal evolution of the dominant resonance frequencies and the source Q factor and changes in the polarization of the signal. The LP source locations before and after the eruption, respectively, do not move significantly, while a slight movement of the VLP source is found. The intensity of the LP events increases after the eruption as well as their dominant frequency and Q factor, while the polarization of the signals changes from predominantly transversal to pure radial motion. Although in previous studies a link between the observed LP activity and the eruption was not found, these observations suggest that such a link was established at the latter end of the eruptive sequence, most likely as a consequence of a reestablishment of the pressure balance in the plumbing system, **it was undermined** due to discharge of large amounts of resident magma during the eruption. Based on the polarization properties of the signal and geological setting of the area, a fluid-filled crack is proposed as the most likely source geometry. The spectral analysis based on the autoregressive-models (SOMPI) is applied **with the** signals in order to analyse the resonance frequencies and the source Q-factors. The results suggest water and basalt **with the** low gas volume fraction as the most likely fluids involved in the source process. Using theoretical relations for the “slow waves” radiated from the fluid-filled crack, we also estimate the crack size for both fluids, respectively.

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## 1. Introduction

The observation and modelling of seismic waves in volcanic settings is of great importance to enhance our

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understanding of the physical processes in magmatic and hydrothermal systems. Long-period (LP) and very-long-period (VLP) seismicity is of particular interest because it has been widely observed in association with eruptive activity (e.g. Neuberg et al., 1994; Chouet et al., 1994, 1997; Neuberg et al., 1998; Rowe et al., 1998; Matsubara and Yomogida, 2004). It is now well-established that LP events are linked to the resonance of the fluid-filled cracks and conduits (Chouet, 1996a,b, 2003; Neuberg, 2000, and references therein), while VLP activity reflects inertial forces related to the mass transport phenomena within the magmatic and hydrothermal systems (Ohminato et al., 1998; Chouet 2003). The spectral characteristics of both types of signals can be employed to probe the fluid-driven processes in volcanic environments and the state of the fluids involved in such processes.

Although Mt. Etna is the biggest volcano in Europe and one of the most active volcanoes in the world, there was only one report on the LP activity on Mt. Etna (Falsaperla et al., 2002) before the permanent broadband network installation in November 2003. The network includes 8 Nanometrics TRILIUM seismometers with flat amplitude response between 0.025 and 100 Hz, at distance between 1.5 and 9 km from the summit craters (Fig. 1). These instruments have been recording sustained LP activity for the past 3 years, thus encompassing the

‘silent’ effusive 2004–2005 eruption. Along with LP, weak VLP pulses were recorded, usually (but not always) preceding the onset of LP events. Saccorotti et al. (2007) presented accurate locations for both types of events and performed detailed analysis of the LP and VLP wavefield for an extended period preceding the onset of the 2004–2005 eruption (Corsaro and Miraglia, 2005; Burton et al., 2005; Di Grazia et al., 2006). Based on the absence of systematic changes of the activity throughout the analysed time interval, the authors found no obvious link between LP activity and the eruption, a result that is in agreement with the observations by Burton et al. (2005) and Di Grazia et al. (2006) who characterised the eruption as an effusion of the remnant lava stored in the superficial reservoir, triggered by the pure geodynamical forces.

During the eruption, the signature of recorded LP signals started to exhibit significant changes in terms of dominant frequency and attenuation. Since this type of signals can be viewed as the oscillatory response to a fluid-filled resonator triggered by a time-localised excitation, they enable us to determine characteristic properties of the resonator by investigating the resonant frequencies and attenuation of the LP oscillations. Kumagai and Chouet (2000) interpreted these parameters and their temporal variations for various active volcanoes using the acoustic properties of a crack containing magmatic and

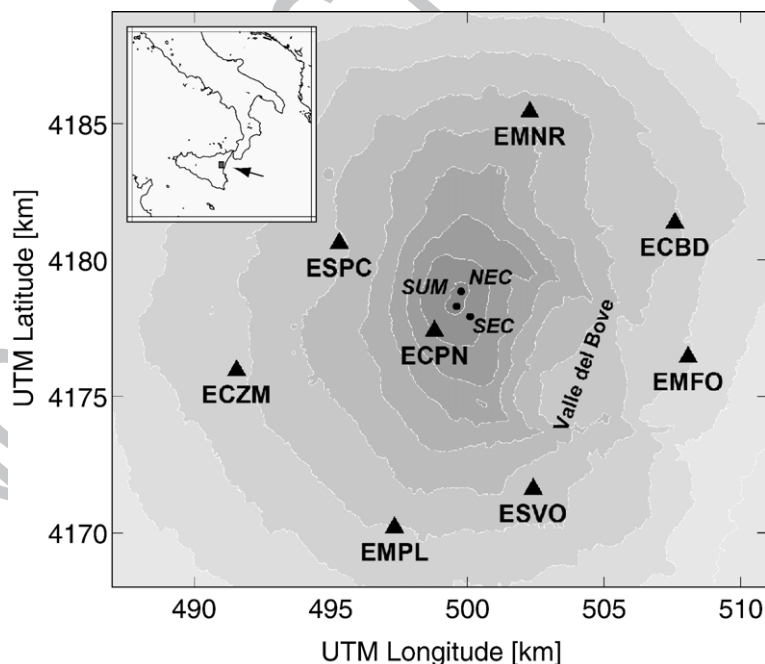


Fig. 1. Topography of Mt. Etna and broad-band seismic network. Triangles represent the seismic stations, while the solid black circles mark the positions of the main craters: SUM — Summit Craters area; NEC — North-East Crater; SEC — South-East Crater. The interval between the contours is 300 m, starting from an elevation of 3200 m a.s.l. (the elevation of the summit of Etna is 3320 m a.s.l.). The inset shows the location of Etna with respect to Italy.

hydrothermal fluids. In this paper, we extend the observations of Saccorotti et al. (2007) to the period after the eruption and study the temporal evolution of LP-VLP activity, in terms of the source movement, change of the signal signature, temporal evolution of the dominant resonant frequencies and the source Q factors and changes in the polarisation of the signal. The observed temporal evolution of the signal can be directly mapped to the temporal evolution of the LP source. Our aim is to establish a dynamical framework for the observed LP activity and find a possible one-way coupling between the eruption and LP activity. We also estimate the size of the LP source.

## 2. LP-VLP activity 2004–2005

### 2.1. Data

Sustained LP activity has been recorded since a permanent broadband network was installed at Mt. Etna in November 2003 (Fig. 1). LP events were detected by an automatic routine based on the spectral correlation between time-windows of the continuous record and a characteristic LP spectrum obtained by averaging spectra from a set of visually-selected events. For each event,

the RMS value of the displacement magnitude (all 3 components) was calculated for the ECPN station (Fig. 2a). Saccorotti et al. (2007) demonstrated a high level of waveform similarity between events recorded before the eruption. Events recorded a few months after the eruption are also found to be similar to each other. This made it possible to analyse only the most energetic signals, denoted by the dark-grey dots in the Fig. 2a, as representative of the complete dataset. Before the analysis the instrument response was removed and the recorded velocity was transformed to displacement. An example of such processed seismograms recorded at the ECPN station a few months before and a few months after the eruption, is shown in Fig. 2b. In both cases, the LP signal is preceded by the VLP pulse which has a peak frequency between 0.03 and 0.05 Hz. However, in some cases VLP signal occurs alone, either like VLP tremor or a single VLP pulse not followed by LP event. Such separate occurrence of these two types of signals suggests that they belong to either different systems (Saccorotti et al., 2007) or systems which are not completely coupled. In the inset boxes of Fig. 2b, 25 seconds long band-passed waveforms ( $f=0.3 - 1.5$  Hz) are shown. LP signals from two different periods look quite different: before the eruption the fundamental mode of oscillation is peaked at about

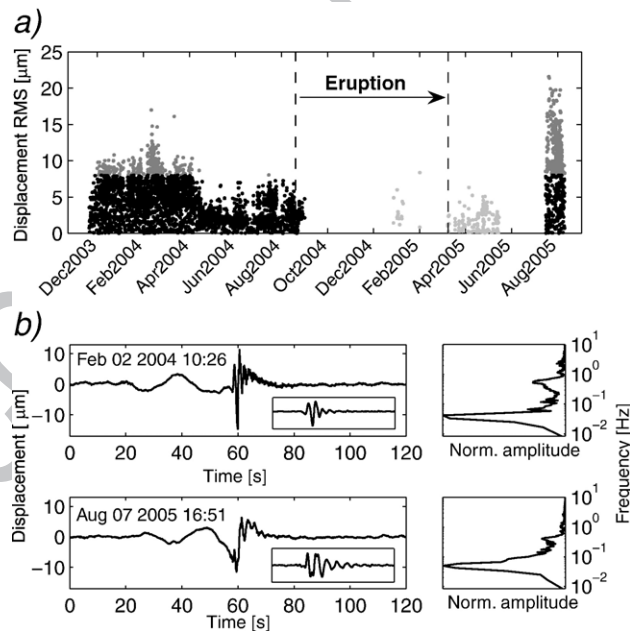



Fig. 2. RMS amplitudes and recorded waveforms. (a) RMS values of displacement recorded at ECPN station. RMS values of the signal magnitude (all 3 components) are calculated for the 6 s long time window encompassing the maximum displacement. Dark grey dots denote signals above the threshold  $RMS=8 \mu m$ , which were analysed in this study. Seismograms recorded during the late eruptive stage and immediately after the eruption are denoted by light grey dots. This subset was analysed in order to have a better insight into the temporal evolution of the signal from pre-eruptive through to the post-eruptive stages. (b) Seismograms and their spectra recorded before (top) and after (bottom) the eruption. Band-pass filtered ( $f=0.3 - 1.5$  Hz), 25 s long waveforms are shown in the inset box. Note that most energy is contained at frequencies below 1 Hz.

136 0.6 Hz, while after the eruption it depicts a frequency of  
137 about 0.4 Hz and a narrower spectral peak.

138 The recorded sequence encompasses the effusive  
139 eruption, which occurred in the period September  
140 2004–March 2005, thus enabling us to examine the  
141 possibility of a connection between the eruption and  
142 LP activity. However, the signals recorded during the  
143 eruption are masked by tremor during the effusive  
144 activity, so we restricted the quantitative part of our  
145 study to the LP activity before and a few months after  
146 the eruption. A subset of 225 events recorded in the  
147 period January–May 2005, during and immediately  
148 after the eruption (denoted by the light-grey dots in the  
149 Fig. 2a), was used only to obtain a qualitative picture of  
150 the temporal evolution of the signals.

## 151 2.2. Locating the events

152 In order to distinguish between source movement and  
153 the activity regime as the possible causes of the temporal  
154 change of the signals, we are interested in relative  
155 locations of the two subsets of events, belonging to pre-  
156 and post-eruptive periods, respectively (referred as *Per-*  
157 *iod I* and *Period II*, hereinafter). Saccorotti et al. (2007)  
158 found absolute locations of the most energetic events from  
159 *Period I*, which they showed to be representative of the  
160 complete pre-eruptive sequence. They used a non-linear,  
161 probabilistic inversion (Tarantola and Vallette, 1982)  
162 acting on reciprocal travel-times calculated using finite-  
163 difference ray tracing for the 3D heterogeneous P-wave  
164 velocity structure of Patanè et al. (2002). Since we are  
165 interested only in relative locations between the two  
166 periods, we relocate events from *Period I* and locate those  
167 from *Period II*, using a simple method which minimizes a  
168 misfit function given by the L1-norm of travel time  
169 residuals for a homogeneous velocity model. The best  
170 estimate for the P-wave velocity, 2.7 km/s, is obtained as  
171 one which minimizes the misfit function obtained for all  
172 the signals and all the stations.

173 In order to define the confidence interval for our  
174 locations, we repeated the location procedure, adding  
175 random noise to simulate incorrect time readings and  
176 waveform arrival-time misalignments. The picking errors  
177 were assumed to be normally distributed with zero mean  
178 and 0.1 s standard deviation, while the error due to the  
179 waveforms misalignment is taken from the uniformly  
180 distributed interval  0.05–0.005 s (time sampling rate).  
181 In this way, for each event the synthetic catalog of 400  
182 travel times was created. We then divided the whole Etna  
183 area to a grid with a cell size of 60 × 60 × 60 m, and divided  
184 the number of locations within each cell by the total  
185 number of synthetic travel times.

At the summit station (ECPN) VLP pulses acting  
contemporaneously with the LP activity were observed.  
These pulses are characterised by the rectilinear motion  
with an angle of incidence between 55 and 65 degrees.  
The free-surface correction angles were obtained from  
numerical simulations, using the volcano topography and  
a homogeneous velocity model, employing the numerical  
scheme described in O'Brien and Bean (2004). For a  
range of source depths between 500 and 2000 m, these  
corrections are found to be less than 2°. The absence of  
the VLP recordings at other stations prevented us from  
locating this type of activity in a conventional way.  
Instead, we corrected the observed incidence angles and  
projected the VLP polarisation vectors onto the plane  
passing in the E–W direction through the centre of the  
LP cluster. Only the data for which rectilinearity of the  
polarisation ellipsoid is greater than 0.9 were used.  
Results for both LP locations and VLP projections are  
given in Fig. 3.

It can be seen from the Fig. 3a that the majority of the  
LP hypocenters are clustered in a small volume at  
elevations of 1700–2900 m, i.e. depths between 400 m  
and 1600 m below the summit craters, which have an  
elevation of about 3300 m. The white dots represent the  
locations of events without added noise. A slight move-  
ment of the centre of the post-eruptive cluster towards the  
west can be observed, but it is negligible once the  
confidence interval is taken into consideration. Thus, the  
temporal changes of the LP waveforms can be attributed to  
different regimes of activity rather than to source  
movement.

Although we cannot determine the exact position of  
VLP source nor its spatial extent from only 1 station, the  
contemporaneous activity of VLP and LP sources  
suggests a common epicentral region for both types of  
activity. Assuming a vertical or inclined conduit, Fig. 3b  
shows a slight downward movement of the VLP source  
between the pre- and post-eruptive stages.

## 3. Data analysis

### 3.1. Temporal evolution of similar events

Although individual unfiltered signals exhibit different  
signatures, one can observe a common shape for the  
waveforms when they are band-pass filtered within the  
frequency band 0.3 – 1.5 Hz. Since this is also the most  
energetic part of signal, it makes it possible to infer the  
main characteristics of the changing source-regime  
through the observation of temporal changes of the  
signal. In order to get a qualitative idea of such changes,  
we performed cross-correlation between all pairs of

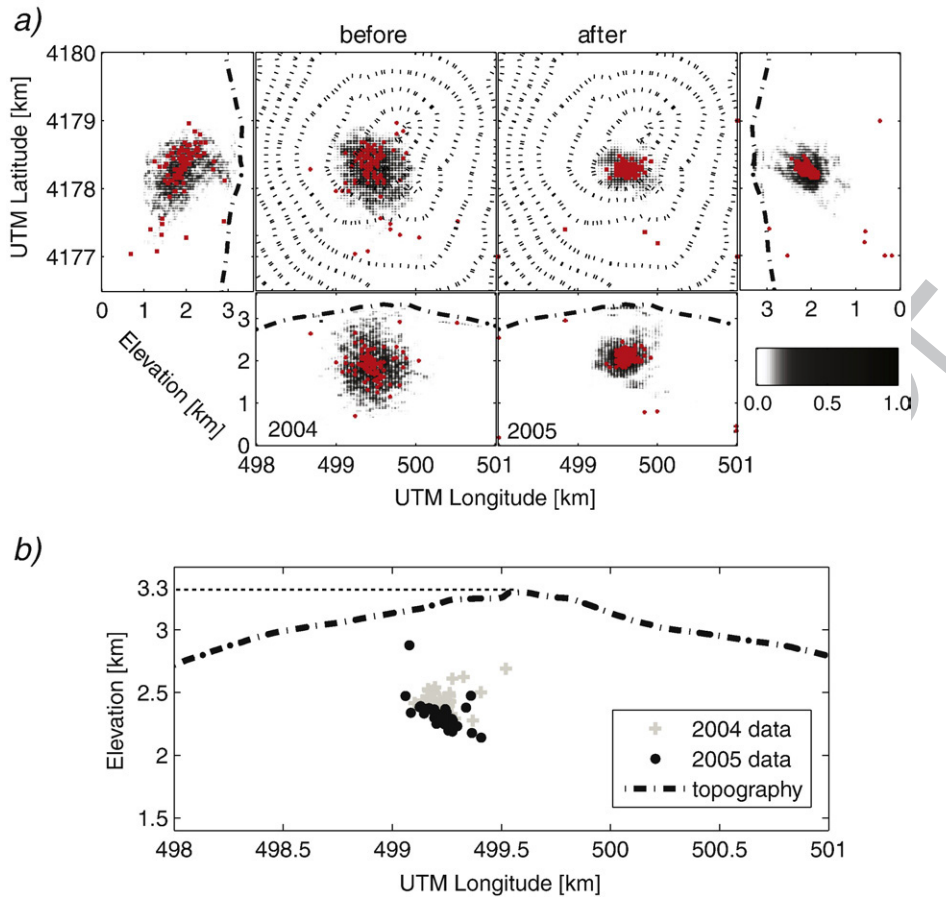


Fig. 3. LP and VLP locations. (a) Locations of the two clusters of LP events (left) before and (right) after the 2004–2005 eruption. The elevation of the summit crater is 3300 m. The red dots (white in the printed version) denote the locations of recorded events. Events are located by using a homogeneous velocity model. The confidence intervals (the shaded area) are calculated from the synthetic catalog of events obtained by adding noise to the arrival times due to the both incorrect reading of the P-wave onset and the finite time sampling. (b) Projection of the VLP polarisation vector onto the E–W vertical plane which passes through the centre of LP clusters. Data recorded before the eruption are represented by the grey crosses, the black circles denote VLP events after the eruption. Only the data for which the rectilinearity of the polarisation ellipsoid is greater than 0.9 are shown.

signals, thus defining clusters of similar events. Then, we used the inter-event time delays measured via correlation analysis to align individual signals, eventually obtaining stacked seismograms representative of each cluster. Saccorotti et al. (2007) demonstrated the similarity of signals within this frequency band for the pre-eruptive period. Their result allows us to use the most energetic event from the *Period I* as representative of the complete pre-eruptive sequence of the LP activity. The same argument holds for *Period II*. In addition to the most energetic events from *Period I* and *II*, we also used a subset of 225 events recorded in the period January–May 2005 (see Fig. 2a). 15 s long signals, encompassing their most energetic part, were cross-correlated. A cluster of similar events was defined as a set of events whose correlation coefficient was higher than 0.85 for all possible event pairs. As we have shown that there is no

significant LP source movement between pre- and post-eruptive stages, this allows us to attribute temporal change of the signal to the different source regimes rather than to the source movement. The stacked signals for the 6 clusters comprising more than 30 events each, along with the temporal distribution of events belonging to each cluster, are shown in Fig. 4. An example of similar events for the cluster 1 before their stack is shown in the Fig. 4a. Although the conservative criterion applied in the cross-correlation analysis resulted in the 6 clusters, the stacked signals reveal the two main regimes of the LP activity, the first one associated with the clusters 1 and 2, and the second with the clusters 3 to 6. Regime 2 is characterised by a lower frequency and longer-lasting signal than regime 1. While the events recorded a few months before and a few months after the eruption, respectively, belong to the different regimes of LP activity, the period during

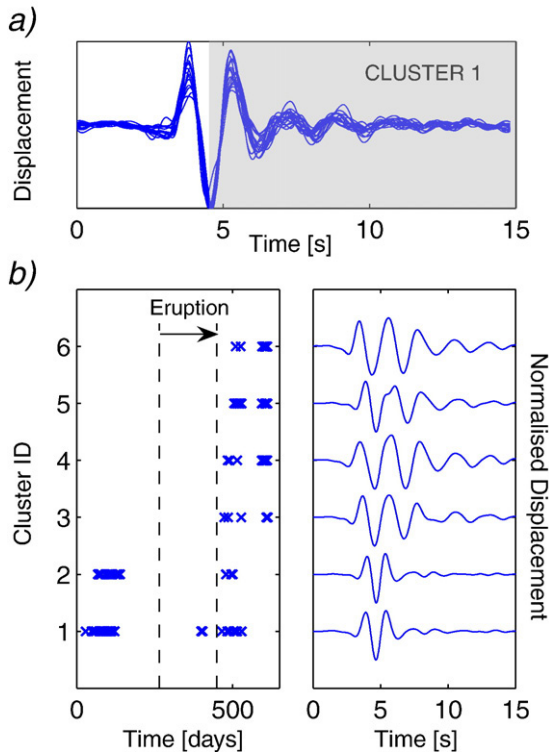


Fig. 4. Temporal evolution of the recorded signal. (a) An example of similar signals (cluster 1) where the correlation coefficient between each pair of events is higher than 0.85. The shaded part of the signal, following the maximum absolute amplitude, was used when performing the polarisation analysis (see the next paragraph). (b) Distribution of similar events over the 6 clusters and their stacked waveforms. Note that events recorded a few months before and a few months after the eruption represent two different regimes of LP activity, while events recorded during and immediately after the eruption can be seen as a transition zone between these two regimes.

269 and immediately after the eruption can be recognised as  
270 the transition zone between the two types of activity.

### 271 3.2. Complex frequency of different source regimes

272 It is known from simplified models of seismo-volcanic  
273 sources (e.g. Chouet, 1986, 1988, 1992) that the resonance  
274 frequency and damping of the system is strongly  
275 influenced by the nature of liquid and gas content. Thus,  
276 information on the change of physical properties of the  
277 fluid-driven source can be inferred by observing the  
278 temporal change of the spectral properties of signal.  
279 Kumagai et al. (2002) and Kumagai (2006) followed the  
280 temporal evolution of fluid-driven sources by the temporal  
281 change of the complex frequencies inferred from  
282 individual signals spanning a time window of a few  
283 months. Here, instead, we analyse the temporal change of  
284 the source regimes, each of which is represented by a stack

of similar signals described above. Although such an  
285 approach cannot reveal subtle changes of the source  
286 within a short time window, we believe that it ensures  
287 a robust analysis of the main source properties. Ideally,  
288 we would like to recover the temporal evolution of the  
289 source resonance (change of the source frequency and  
290 Q factor) from the recorded signals. However, topogra-  
291 phy and soft superficial layers can have a detrimental  
292 effect on signal quality. Ripperger et al. (2003), using  
293 numerical simulations for the case of a homogeneous  
294 model and shallow source, demonstrated a strong  
295

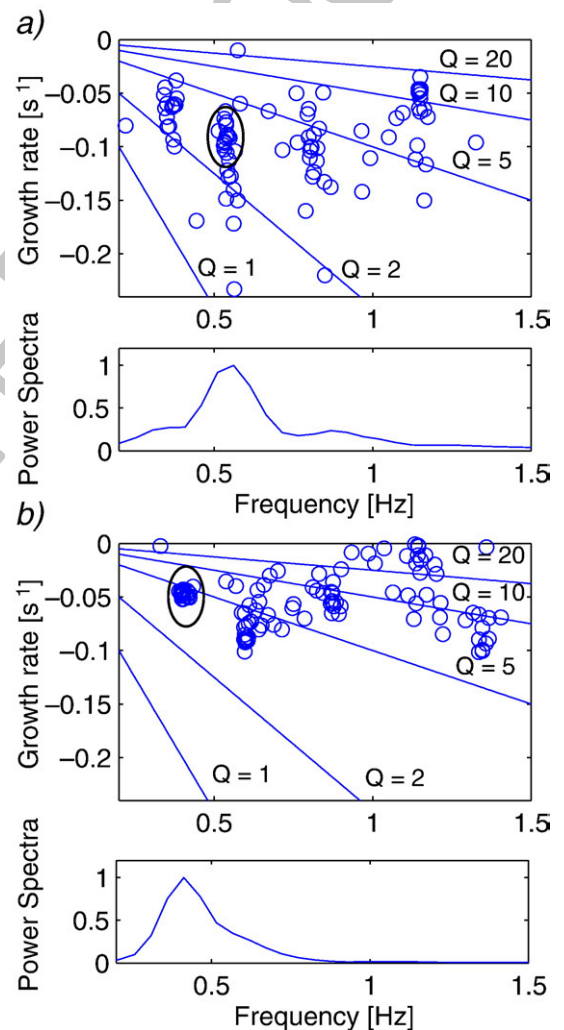


Fig. 5. Complex frequencies obtained from the SOMPI analysis. (a) (top) Complex frequencies of individual wave elements for AR orders 4–70, estimated for the stacked vertical displacement waveform associated with the cluster 1 in Fig. 9. (bottom) Amplitude spectrum of the same waveform. (b) (top) Complex frequencies estimated for the waveform associated with the cluster 6 in Fig. 9. (bottom) Amplitude spectrum of the same waveform.

influence of the volcano topography on the signal duration at the stations situated on the flanks of the Merapi volcano. Only stations very close to the summit reflect the behaviour of the source, while the others are strongly “contaminated” by the topographical surface waves. Using the numerical scheme of O’Brien and Bean (2004), we found that even stronger modification of the waveforms is expected once energy is transmitted through a shallow, soft layer, especially for the stations located on the flanks of a volcano.

In such a case, the source Q factor cannot be recovered. To minimise this effect, we restrict our analysis to the ECPN station only, which is situated near the summit crater, closest to the source.

In order to determine the complex frequencies of LP events, the SOMPI method was used (Kumazawa et al., 1990, and references therein). This is a spectral analysis method based on an autoregressive (AR) model, which addresses the problem of resolving the decaying harmonic components of a time series corrupted by noise. Due to its better resolution compared to Fourier-based spectral estimates and ability to determine damping factors as characteristic properties of a linear dynamical system, it is a powerful tool for studies dealing with resonating sources. The force-free tail of the oscillating signal is resolved into a number of harmonic components, each of them described by a complex frequency  $f - ig$ , where  $f$  is frequency,  $g$  is the growth rate, and  $i$  the imaginary unity. A quality factor Q is defined as  $-f/2g$ .

The results of SOMPI analysis of the stacked waveforms associated with the clusters 1 and 6 in Fig. 4

are shown in Fig. 5, along with their corresponding Fourier spectra. ( $f-g$ ) diagrams of the complex frequency represent wave elements for AR orders 4 to 70. Densely populated regions indicate stably resolved harmonic components, while scattered points represent incoherent noise. It can be seen that LP waveforms are characterised by a drop in dominant frequency between the two regimes and a slight increase in Q. Although four oscillation modes are apparent in  $f-g$  diagrams, we analyse the lowest two peaks present in both diagrams, one of which is dominant for each regime (denoted by ellipses). The complex frequency for each waveform along with the corresponding variance is determined from AR order indicated by Akaike’s information criterion (AIC) (Akaike, 1974). We use all 6 stacked waveforms, shown in Fig. 4, and determine the complex frequencies of the two modes from each of them. Finally, these frequencies are used to obtain the mean frequency and Q factor of each mode, respectively, for 2 regimes. We use the formula:

$$x_{rj} = \frac{\sum w_i(x) \cdot x_i}{\sum w_i(x)}, \quad x = f, Q, \quad (1)$$

$$rj = \begin{cases} r1, & i = 1, 2 \quad (\text{regime 1}) \\ r2, & i = 3, 4, 5, 6 \quad (\text{regime 2}) \end{cases}$$

where index  $rj$  denotes different regimes, while index  $i$  is the identification number of clusters 1 to 6. Weights,  $w_i(x)$ , are defined to be proportional to a number of individual waveforms belonging to a certain cluster,  $n_i$ , and inversely

Table 1  
Frequencies and Q factors of the stacked waveforms and their weighted means estimated for the two regimes of the LP activity (see text for details)

Regime 1 (Combining clusters 1 and 2)	Regime 2 (Combining clusters 3 to 6)
<i>Mode 1 (secondary mode):</i>	<i>Mode 1 (dominant mode):</i>
$f_1 = 0.380 \pm 0.020$ Hz, $Q_1 = 2.6 \pm 0.2$ , $n = 76$	$f_3 = 0.403 \pm 0.001$ Hz, $Q_3 = 4.72 \pm 0.1$ , $n = 27$
$f_2 = 0.375 \pm 0.006$ Hz, $Q_2 = 2.2 \pm 0.3$ , $n = 41$	$f_4 = 0.399 \pm 0.001$ Hz, $Q_4 = 4.68 \pm 0.1$ , $n = 63$
	$f_5 = 0.401 \pm 0.002$ Hz, $Q_5 = 4.55 \pm 0.1$ , $n = 47$
	$f_6 = 0.398 \pm 0.001$ Hz, $Q_6 = 4.39 \pm 0.1$ , $n = 36$
<i>Mode 2 (dominant mode):</i>	<i>Mode 2 (secondary mode):</i>
$f_1 = 0.540 \pm 0.010$ Hz, $Q_1 = 3.1 \pm 0.2$ , $n = 76$	$f_3 = 0.597 \pm 0.012$ Hz, $Q_3 = 5.23 \pm 0.6$ , $n = 27$
$f_2 = 0.568 \pm 0.004$ Hz, $Q_2 = 3.0 \pm 0.1$ , $n = 41$	$f_4 = 0.599 \pm 0.009$ Hz, $Q_4 = 3.9 \pm 0.2$ , $n = 63$
	$f_5 = 0.604 \pm 0.010$ Hz, $Q_5 = 4.2 \pm 0.7$ , $n = 47$
	$f_6 = 0.595 \pm 0.006$ Hz, $Q_6 = 3.6 \pm 0.2$ , $n = 36$
<i>Mode 1:</i>	<i>Mode 1:</i>
$f_{r1} = 0.377 \pm 0.002$ Hz, $Q_{r1} = 2.5 \pm 0.2$	$f_{r2} = 0.400 \pm 0.001$ Hz, $Q_{r2} = 4.6 \pm 0.1$
<i>Mode 2:</i>	<i>Mode 2:</i>
$f_{r1} = 0.556 \pm 0.014$ Hz, $Q_{r1} = 3.1 \pm 0.1$	$f_{r2} = 0.599 \pm 0.002$ Hz, $Q_{r2} = 4.0 \pm 0.3$

Both parameters are estimated for all the clusters in Fig. 4, for the first two modes. Note that values of frequency and Q factor increase for both modes between the regime 1 and 2.

352 proportional to the dispersion of frequency and  $Q$  factor  
353 estimated by the SOMPI analysis:

$$354 \quad w_i(x) = n_i \cdot \frac{x_i}{\sigma_i(x)}, \quad x = f, Q, \quad (2)$$

355 where  $\sigma_i(x)$  denotes standard deviations of  $f$  and  $Q$ ,  
356 estimated by the error propagation from the time series to  
357 the characteristic frequencies (Kumazawa et al., 1990).  
358 The standard deviation of the weighted means obtained by  
359 Eq. (1) was calculated using the equation given in De  
360 Vries (1986):

$$361 \quad \sigma_{rj}^2(x) = \frac{\sum w_i(x) \cdot (x_i - x_{rj})^2}{(N-1) \sum w_i(x)}, \quad x = f, Q, \quad (3)$$

$$rj = \begin{cases} r1, & i = 1, 2 & (\text{regime 1}) \\ r2, & i = 3, 4, 5, 6 & (\text{regime 2}) \end{cases}$$

362 where  $N$  is a number of data used for the calculation of  
363 weighted means and standard deviations, and is equal to 2  
364 and 4 for the regimes 1 and 2, respectively. Frequencies,  
365  $Q$ -factors and their standard deviations for all 6 clusters  
366 obtained by the SOMPI analysis, along with the weighted  
367 means and standard deviations for the two different  
368 regimes of LP activity calculated using Eqs. (1)–(3), are  
369 given in Table 1. As seen from the table, for each  
370 individual mode, frequencies for all the clusters within a  
371 certain regime exhibit very small fluctuations and their  
372 standard deviations are also small. Somewhat bigger, but  
373 still small variations of  $Q$  factors can be observed. Bigger  
374 variations in  $Q$  factors with respect to frequency are  
375 usually observed because  $Q$  factors are more sensitive to  
376 the level of noise as well as to the adopted order of the AR  
377 model. However, here we used stacked waveforms with  
378 low noise levels and only the data recorded at the station  
379 which is closest to the source. Therefore, we are confident  
380 that estimated frequencies and  $Q$  factors reflect reason-  
381 ably well the behaviour of the LP source. The most  
382 noticeable feature of the temporal evolution of the  
383 oscillating source is a switching of the dominant and  
384 secondary mode between two regimes, accompanied with  
385 a slight increase in frequency and  $Q$  factor for both of  
386 them, respectively. The same trend in frequency and  
387  $Q$  factor can be observed for the two secondary modes of  
388 oscillation present in Fig. 5, but due to their very low  
389 energy and possible higher contamination by noise, they  
390 were not included in the quantitative analysis.

### 391 3.3. Polarisation analysis

392 Chouet (1986) investigated far-field radiation pat-  
393 terns of P and S waves radiated from an oscillating fluid-  
394 filled crack. In Chouet (1988), he expands his study

showing a few profiles of seismograms recorded in the 395  
near- and intermediate-field, where standing waves 396  
patterns of the oscillating crack surface are clearly 397  
observed. He suggests that such an observation should 398  
provide a powerful tool to define the extent of the source 399  
by analysing the relative content of energy belonging to 400  
different modes of resonance, provided that the 401  
observation is made using a small-aperture array. 402  
However, our observations show that for either of two 403  
regimes the source oscillates with predominantly one 404  
frequency. In such a monochromatic case, even one 405  
near-to-intermediate-field station could enable us to gain 406  
an idea about the nature of the resonance. Therefore, we 407  
performed polarisation analysis of recorded signals, 408  
using the covariance-matrix method of Kanasewich 409  
(1981). We calculated all 3 axes of the polarisation 410  
ellipsoid for a 5 seconds window for each signal, 411  
starting from its maximum absolute amplitude (shaded 412  
region in the Fig. 4a). We plotted projections of the 413  
obtained axes onto horizontal, radial-vertical and 414  
transverse-vertical planes passing through the receiver 415

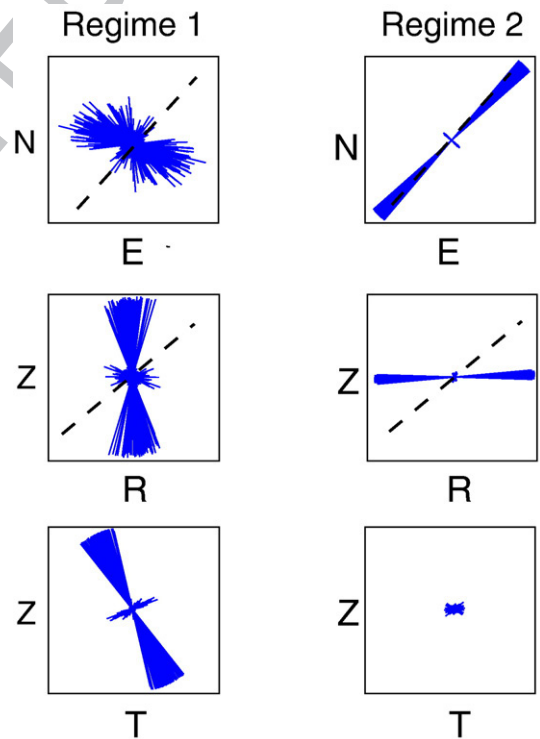


Fig. 6. Main axis of polarisation ellipsoid of the signal projected to the (top) horizontal, (middle) radial-vertical and (bottom) transversal-vertical plane. Polarisation of the signals belonging to the regime 1 and 2 is shown on the left and right panels, respectively. Note the absence of the major radial motion before the eruption, while after the eruption the particle motion is predominantly radial.



416 position, for both regimes, respectively. Results are  
 417 shown in Fig. 6. The dashed line in the figure denotes  
 418 source–receiver direction. While particle motion before  
 419 the eruption was characterised by predominantly  
 420 transverse and vertical motion, after the eruption it  
 421 turns into horizontal–radial motion. For the case of a  
 422 single source, this observation eliminates a spherical  
 423 cavity as a possible source candidate and implies a non-  
 424 isotropic source, in agreement with Saccorotti et al.  
 425 (2007). The main question arising here is if it is possible  
 426 that longitudinal and transverse modes of the crack  
 427 resonance excite different radiation patterns. Detailed  
 428 discussion on this matter follows in the next section.

#### 429 4. Discussion

430 Saccorotti et al. (2007) analysed a sequence of LP  
 431 activity occurring from November 2003 to the onset of  
 432 the effusive eruption on September 7th 2004. Observed  
 433 non-destructive repetitive LP activity accompanied by  
 434 VLP pulses was explained as a resonance of a cavity  
 435 filled by magmatic or hydrothermal fluids at a poor gas  
 436 volume fraction, triggered by injection of gas exolved  
 437 from the nearby magmatic column. The same authors  
 438 suggest that there is no connection between the LP  
 439 activity and the eruption. Due to the absence of typical  
 440 seismological precursors (Di Grazia et al., 2006), and  
 441 geochemical properties of extruded lavas (Burton et al.,  
 442 2005), the eruption was characterised as an effusion of  
 443 the remnant lava stored in the superficial reservoir,  
 444 triggered by geodynamical forces associated with steep  
 445 topography on the eastern flank of the volcano.  
 446 However, our current observations of temporal changes  
 447 of the seismological parameters during and after the  
 448 eruption seem to suggest the possibility of one-way  
 449 coupling between the eruption and LP activity. These  
 450 observations can be summarised as follows:

- 451 • No movement of the LP source within confidence
- 452 intervals
- 453 • Slight movement of the VLP source
- 454 • Increase in intensity of LP events
- 455 • Increase in resonance frequency and source Q-factor
- 456 • Change in the polarisation of the signal

457  
 458 In the next section, we propose a model for the  
 459 link between the eruption and the change of the LP  
 460 regime, which explains the observations outlined above.  
 461 Then we discuss the link between the longitudinal/  
 462 transverse mode of a vibrating crack and the polarisa-  
 463 tion of the observed signal. Finally, we estimate the  
 464 of the source.

#### 465 4.1. Link between eruption and LP regime

466 Both this study and that of Saccorotti et al. (2007) 466  
 467 determine a shallow source at elevations mainly be- 467  
 468 tween 1700 m and 2900 m, i.e. depths between 400 and 468  
 469 1600 m below the summit crater (3300 m a.s.l.). Based 469  
 470 on seismic wave attenuation and velocity tomography, 470  
 471 two groups of authors (De Gori et al., 2005; Martínez- 471  
 472 Arévalo et al., 2005) suggest that the upper part of this 472  
 473 region consists of fractured, fluid-filled hot rock 473  
 474 surrounding the molten material. Although little atten- 474  
 475 tion has been given to the presence of water in the upper 475  
 476 parts of Etna volcano, a few recent studies, using dipole 476  
 477 geoelectric, magnetotelluric and self-potential methods 477  
 478 (e.g., Mauriello et al., 2004; Della Monica et al., 2004; 478  
 479 Manzella and Zaja, 2006) as well as phreatomagmatic 479  
 480 activity at the Piano del Lago site at 2570 m a.s.l. during 480  
 481 the 2001 eruption reported by Behncke and Neri (2003), 481  
 482 suggest the existence of groundwater within the first 482  
 483 500 m below ground level. The deformation study 483  
 484 conducted by Macorso and Davis (2004) describes 484  
 485 two classes of final magma penetration at Mt. Etna: 485  
 486 dykes that propagate horizontally and vertically. Fol- 486  
 487 lowing these authors, the first class of dykes propagate 487  
 488 from the summit craters to the eruption point, thus 488  
 489 supplying magma to the flanks from the deeper magma 489  
 490 reservoir through the summit conduit zone. Their 490  
 491 extension is mostly in a NW–SE direction at a typical 491  
 492 depth of 500–1000 m. In summary, we can suggest that 492  
 493 the LP activity originates in the region with the fol- 493  
 494 lowing characteristics: 494

- 495 1) possible interaction between magmatic and fractured 495  
 496 hydrothermal system, 496
- 497 2) bending point of the magma transport from depth 497  
 498 towards the flanks, and 498
- 499 3) presence of the fractured region towards the SE 499  
 500 flanks where the 2004 eruption occurred. 500

501  
 502 Features 1) and 2) support the LP model suggested by 502  
 503 Saccorotti et al. (2007), outlined in Section 1. Moreover, 503  
 504 the different time delays and amplitude correlation 504  
 505 between VLP and LP signals observed by the same 505  
 506 authors suggest that they are inter-related but represent 506  
 507 different mechanisms, which supports the interpretation of 507  
 508 the interaction between two systems. The presence of the 508  
 509 proposed fracture zone at Mt. Etna between the source 509  
 510 position and the eruption site opens a possibility of 510  
 511 depressurisation of the source region due to the void left by 511  
 512 the erupted magma. According to Sturton and Neuberg 512  
 513 (2003), decompression of magma can move the bubble 513  
 514 nucleation level deeper in the system by a few hundred 514

515 metres. This will increase the size of the gas slug arriving at  
 516 the terminal part of the magmatic column. In such a case,  
 517 the apparent VLP source location will move downwards,  
 518 as observed here (Fig. 3b). Since the gas slug reaching the  
 519 terminal part of the magmatic column is more energetic  
 520 than in the period before the eruption, an increase in size of  
 521 LP events is expected, as observed (Fig. 2a).

522 In a state of equilibrium, the pressure within a fluid-  
 523 filled crack is equal to the ambient pressure of the source  
 524 region. When gas is injected, this pressure exceeds the  
 525 ambient pressure and the excess of a gas–fluid mixture  
 526 is discharged into surrounding area, which triggers the  
 527 LP oscillations. This discharge explains the observed  
 528 dilatation at the onset of recorded signals (Fig. 4). Fluid  
 529 discharges through the crack edge determined by the  
 530 local stress conditions. Thus, a change in these  
 531 conditions can change the direction in which the crack  
 532 is discharged, which leads to the change of the principal  
 533 mode of the crack resonance. However a detailed  
 534 analysis of the geodynamical stress field is out of the  
 535 scope of this study.

536 Another observation which also supports the proposed  
 537 model is the increase in frequency and source Q-factor for  
 538 both modes of the source resonator, respectively (see  
 539 Fig. 5 and Table 1). Using Henry’s law for the liquid–gas

solution, Kumagai (2006) showed that gas volume  
 540 fraction in the gas–liquid mixture increases with decreas-  
 541 ing pressure. The same author, using the crack model of  
 542 Chouet (1986), showed that for basalt–gas mixture a very  
 543 slight increase in frequency and a larger increase in Q-  
 544 factor is expected for an increased volume fraction of gas  
 545 in the mixture (Fig. 6 in Kumagai, 2006). Similar  
 546 behaviour is expected for the bubbly water, but with a  
 547 higher increase in frequency, as shown by Kumagai et al.  
 548 (2002) in Fig. 7. 549

#### 4.2. Mode of oscillation and particle motion 550

Crack opening/closing can be described by a system  
 551 of equivalent forces for which, in the case of a vertical  
 552 crack oriented as in Fig. 7a, the moment tensor has a  
 553 form (Aki and Richards [47], equation 3.21): 554

$$M \propto \pm \begin{bmatrix} \lambda + 2\mu & 0 & 0 \\ 0 & \lambda & 0 \\ 0 & 0 & \lambda \end{bmatrix}, \quad (4) \quad 555$$

where  $\lambda$  and  $\mu$  are Lamé’s constants, and signs “+” and  
 556 “–” denote crack opening and closing, respectively. The  
 557 set of equations (4.29) from Aki and Richards (2002), re-  
 558

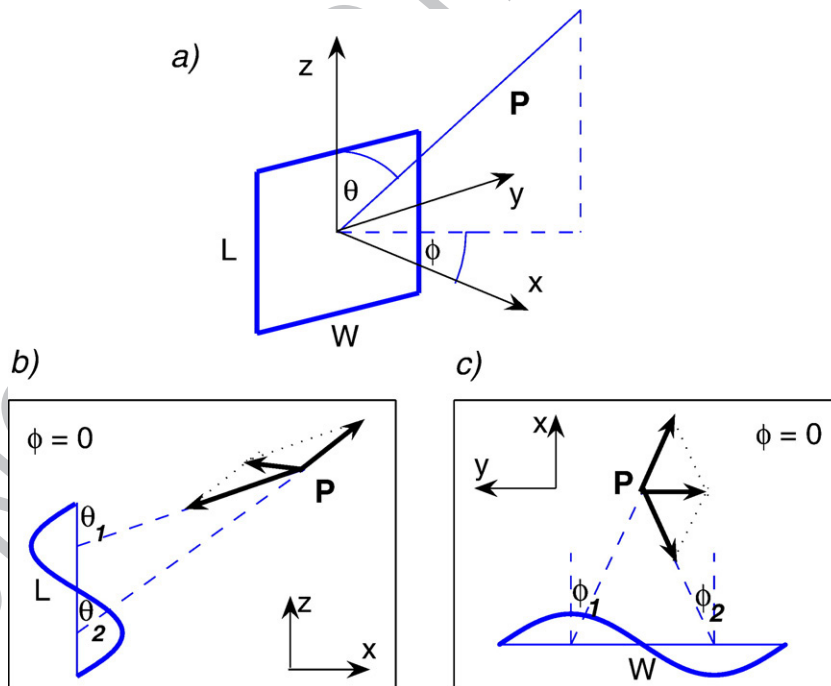


Fig. 7. Schematic of the P-wave radiation from the longitudinal and transversal crack resonance, respectively. (a) Spherical coordinate system with the origin in the centre of the vertical crack. (b) Longitudinal mode of resonance for a source–receiver azimuth  $\phi=0^\circ$ . Note that particle motion always remains polarised in the P–SV plane. (c) Transversal mode of resonance viewed from above. Motion in the transversal direction is created. For simplicity, only one crack wall is shown in the figure.

559 written in the spherical coordinate system (see Fig. 7a)  
 560 and by taking  $\lambda = \mu$ , gives a displacement field due to a  
 561 moment-tensor defined by Eq. (4) as follows:

$$\begin{aligned}
 562 \quad u^r &= (P^F - P^I + 2S^I - 6N) + 2\sin^2\theta\cos^2\phi \\
 &\quad \times (P^F + 4P^I + 3S^I + 9N) \\
 u^\theta &= \sin 2\theta\cos^2\phi \cdot (2P^I + 3S^I + S^F - 6N) \\
 563 \quad u^\phi &= -\sin\theta\sin 2\phi \cdot (-2P^I + 3S^I + S^F - 6N)
 \end{aligned} \quad (5)$$

563 where  $P^F$ ,  $S^F$ ,  $P^I$ ,  $S^I$  and  $N$  are functions of travel-  
 564 time, source–receiver distance, properties of the  
 565 medium, seismic-moment and the source time-history.  
 566  $P^F$  and  $S^F$  denote far-field P- and S-waves,  $P^I$  and  $S^I$   
 567 intermediate-field P and S terms and  $N$  stands for the  
 568 near-field term. Note that the dependence of  $u^r$ ,  $u^\theta$  and  
 569  $u^\phi$  on direction of propagation is common for the far-  
 570 intermediate- and near-field disturbance propagating  
 571 through the medium. This property of the source  
 572 mechanism described by Eq. (4) makes the following  
 573 discussion more general.

574 For the fluid-filled crack, at the time  $t=0$ , when  
 575 resonance is triggered, the initial pulse propagates  
 576 through the medium at P- and S-wave velocities and a  
 577 displacement field given by Eq. (5) is recorded at the  
 578 receiver. At the same time slow interface waves start to  
 579 propagate along the crack walls with a velocity slower  
 580 than the acoustic velocity of fluid (Chouet, 1986;  
 581 Ferrazzini and Aki, 1987), thus sustaining the oscillation  
 582 of the crack. According to Ferrazzini and Aki (1987),  
 583 these waves cannot be directly observed at distances  
 584 greater than a wavelength, which for the case of the  
 585 fundamental mode of resonance, is equal to the crack  
 586 length. However, due to the finite dimensions of the  
 587 crack, the strong horizontal motion in the fluid layer can  
 588 provide an important source of radiation which can be  
 589 observed at large distances. Chouet (1988) showed that  
 590 this type of disturbance can be recorded at near and  
 591 intermediate distances. For the fundamental mode of  
 592 the crack resonance,  $\lambda=L$ , where  $\lambda$  is the wavelength  
 593 of the fundamental mode and  $L$  is the crack length,  
 594 and the source-receiver azimuth  $\phi=0$ , a schematic of  
 595 the P-wave propagation for the longitudinal and trans-  
 596 versal mode of the crack oscillation is given in the  
 597 Fig. 7b and c, respectively. Similar considerations can  
 598 be undertaken for SV and SH waves. Note that although  
 599 Eqs. (5) give  $u^\phi=0$  for a vertical crack observed at an  
 600 azimuth  $\phi=0$ , transverse motion is generated. Such an  
 601 oscillating crack can be described by two simulta-  
 602 neously acting, closely spaced sources whose mechan-  
 603 isms are given by Eq. (4), but have opposite signs. In the  
 604 case considered in this study, the seismic station is in

close proximity to the source (see Fig. 1). Following this  
 simple deduction we suggest that different polarisations in  
 the wave train before and after the eruption can be  
 explained by the excitation of perpendicular modes of  
 source resonance. This interpretation is qualitative, and a  
 full moment-tensor inversion needs to be performed to  
 obtain the source mechanism and its orientation. This is a  
 subject of further work.

An important implication of the observation outlined  
 above is that the moment-tensor solution could be  
 sensitive to the direction of the slow waves propagating  
 along the crack walls. However, future work is required  
 to confirm this hypothesis.

#### 4.3. Slow waves and source size

Quasi-monochromatic long-period seismograms,  
 such as observed on Etna, can be successfully explained  
 by the existence of slow waves propagating along the  
 fluid–solid interface between the fluid-filled resonator  
 and surrounding medium, with a velocity lower than the  
 acoustic velocity of fluid. These waves were first  
 detected in the models of Chouet and Julian (1985)  
 and Chouet (1986), who found that the resonance period  
 of the fluid-filled crack can be much longer than that  
 expected from the acoustic properties of fluid and size of  
 the resonator. Chouet (1986) called them “crack waves”.  
 He also found that the phase velocity of the crack wave  
 rapidly decreases with increasing values of a non-  
 dimensional parameter called the crack stiffness,  $C$ ,  
 originally introduced by Aki et al. (1977):

$$C = \frac{bL}{\mu h} \quad (6)$$

where  $b$  is the bulk modulus of the fluid,  $\mu$  is rigidity,  
 $L$  is the length of the crack and  $h$  its aperture. Since the  
 crack wave velocity depends on the crack stiffness, it is  
 a crucial parameter for estimating the size of a fluid-  
 filled resonator. Following the work of various authors,  
 Chouet (1988) gives estimates for possible in-situ values  
 of the crack stiffness. Thus, for dykes filled with basalt  
 this parameter is estimated to be between 10 and 500,  
 while for hydrofractures values range from  $10^3$  to  $10^4$ .  
 Saccorotti et al. (2007) showed that the low values of the  
 source Q factor estimated from our signals support both  
 types of fluids when low gas volume is involved in the  
 source process. Therefore, we estimate the crack size for  
 the case of basalt and water, respectively. Although an  
 assumption about the crack geometry of the source  
 may not seem completely justified, we believe that this  
 is a realistic case because of the non-isotropic source

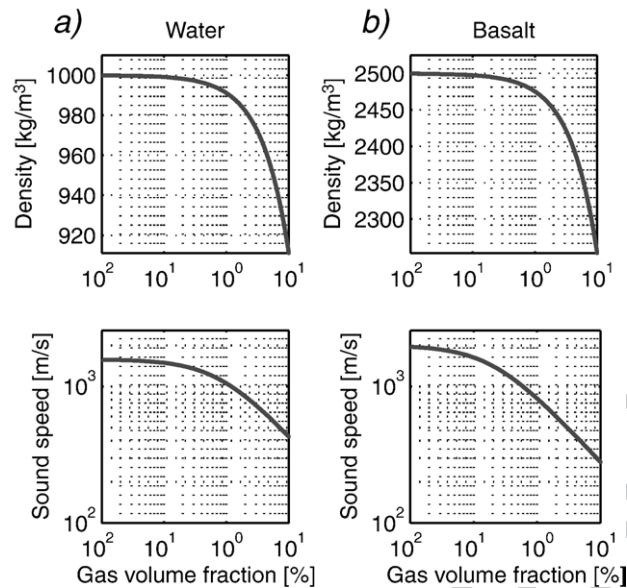


Fig. 8. Density and speed of sound in (a) water and (b) basalt for a 0.01 – 10% of the gas volume fraction in a fluid–gas mixture. The speed of sound was calculated using the model of Commander and Prosperetti (1989). The temperature of water was set to 120 °C and initial speed to 1580 m/s, while these values for basalt were 1100 °C and 2000 m/s, respectively.

radiation observed by Saccorotti et al. (2007), the change of polarisation of the mode of oscillation and geological setting of the source region. This is also the most natural geometry satisfying mass transport beneath a volcano (Kumagai et al., 2002).

Apart from the crack stiffness, values of the acoustic velocity and density of the fluid are needed for an estimation of the crack size. In our calculations, we allowed a gas volume fraction in fluid to lie within the range 0.01%–2%. We obtained velocities for bubbly basalt and water with a bubble radius of 1 mm from the model for bubbly liquids of Commander and Prosperetti (1989), using equations (75)–(86) in Chouet (1996a,b) and neglecting the surface tension of the bubbles. The initial values in the model, for pure basalt at a pressure of 20 MPa and a temperature of 1100 °C, were: velocity  $c=2000$  m/s (Chouet [9]), and density  $\rho=2500$  kg/m<sup>3</sup>. At the same pressure and a temperature of 120 °C, for pure water we used  $c=1580$  m/s (Benedetto et al., 2005) and  $\rho=1000$  kg/m<sup>3</sup>. Following Saccorotti et al. (2001), variation in the density of the fluid–gas mixture with the gas volume fraction was calculated using the following set of equations:

$$\begin{aligned} \rho &= n\rho_g + (1-n)\rho_f \\ \rho_g &= \frac{p}{RT}, \end{aligned} \quad (7)$$

where  $\rho$  is the density of the mixture,  $n$  the gas volume fraction,  $\rho_g$  density of the gas,  $\rho_f$  the density of the pure fluid,  $p$  pressure,  $R$  the individual gas constant and  $T$  temperature. Both variations of velocity and density for basalt and water at poor gas volume fraction are given in Fig. 8. It can be seen that for a gas volume fraction in a range 0.01% – 2%, the acoustic velocity in basalt takes values between 1500 m/s and 600 m/s, in water between 1300 m/s and 800 m/s, while the drop of densities is much lower. Assigning a P-wave velocity in the host rock to 3000 m/s (Patane et al., 2001), the estimated impedance contrast between the host rock and basalt ranges between 1.6 and 5.4, thus overlapping with the 1.5–7.5 range for andesite, used by Neuberg et al. (2000) in their modelling of LP activity at Montserrat. Slightly higher impedance contrast for andesitic volcanoes could be explained by the lighter and gas-richer andesitic magmas. However, the estimated ranges of values overlap significantly, thus suggesting that similar parametrisation can be used for modelling of resonant sources on both types of volcanoes.

We estimate the velocity of the crack waves sustaining the source resonance from the theoretical dispersion curves. According to Ferrazzini and Aki (1987), who first analytically described the existence of the slow waves at the fluid–solid interface, the

703 dispersion relation for the slow wave velocity, for a  
704 Poisson's ratio  $\sigma=0.25$ , can be written as:

$$705 \coth \left[ \sqrt{1 - \left(\frac{v}{a}\right)^2} \cdot \left(\frac{\pi h}{\lambda}\right) \right]$$

$$= -\frac{\rho_s \sqrt{1 - \left(\frac{v}{a}\right)^2}}{\rho_f \left(\frac{v}{\beta}\right)^4} \cdot \left[ \frac{\left(2 - \left(\frac{v}{\beta}\right)^2\right)^2}{\sqrt{1 - \left(\frac{v}{a}\right)^2}} - 4\sqrt{1 - \left(\frac{v}{\beta}\right)^2} \right] \quad (8)$$

706 where  $v$  is the slow wave velocity,  $a$  the acoustic  
707 velocity,  $h$  is the channel thickness,  $\lambda$  is wavelength,  $\beta$  is  
708 the S-wave velocity in the solid, and  $\rho_f$  and  $\rho_s$  are the  
709 densities of the fluid and solid, respectively. By taking  
710  $\beta=1730$  m/s (e.g. Patanè et al., 2002),  $\rho_s=2650$  kg/m<sup>3</sup>,  
711 and assuming the fundamental mode of the crack  
712 oscillation,  $\lambda=L$ , combining Eqs. (6) and (8) gives the  
713 dependence of the ratio  $v/a$  on the crack stiffness,  $C$ , as  
714 shown in Fig. 9. Note that dispersion curves depend only  
715 slightly on the velocities and densities of fluid within our  
716 range of interest (see also Chouet, 1996a,b, Fig. 14).  
717 Therefore, only the curves calculated for the average  
718 velocities and densities are given in the diagram.  
719 Ferrazzini and Aki (1987) showed that for the calculation  
720 of the fundamental mode of resonance ( $\lambda=L$ ), one half  
721 of the value of the ratio  $v/a$  given by theoretical curve  
722 should be used. Thus, for the range of values of the  
723 crack stiffness marked in the diagram ( $C=100$ – $500$  for  
724 basalt, and  $C=10^3$ – $5 \cdot 10^3$  for water), we estimated the  
725 ratio  $v/a=0.15$ – $0.07$  for basalt and  $v/a=0.048$ – $0.024$

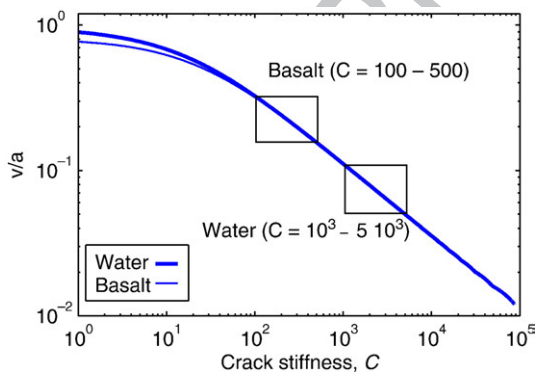


Fig. 9. Theoretical dependence of the slow wave velocity in a crack of infinite length on the crack stiffness defined as  $C=(b/\mu)(\lambda/h)$ , for water and basalt. For the crack of finite dimensions, the value  $v/c$  for the fundamental mode of resonance is about one half of the value obtained from the diagram. Realistic values of the crack stiffness for the crack filled by basalt and water, respectively, are shown in the figure.

726 for water. For the fundamental longitudinal mode, the  
727 crack length and its aperture can be estimated from the  
728 following relations:

$$729 L = \frac{v}{f} = \frac{v}{a} \cdot \frac{a}{f}, \quad (9)$$

where  $f$  is frequency, and

$$730 h = \frac{bL}{\mu C}. \quad (10) \quad 731$$

732 The same approach can be used for estimation of the  
733 crack width, by defining the transverse crack stiffness,  
734  $C_t$ , as follows: 735

$$736 C_t = \frac{bW}{\mu h}, \quad (11)$$

737 where  $W$  denotes the crack width,  $h$  its aperture,  $\mu$  is  
738 rigidity and  $b$  is the bulk modulus of the fluid. For the  
739 case of basalt, our estimated crack length varies between  
740 105 and 563 m, while its aperture takes values between  
741 0.02 and 3.9 m. If the fluid is water, these values are  
742  $L=48$ – $179$  m and  $h=1$ – $38$  mm. The ratio between the  
743 width and the length of the crack is about  $W/L=0.85$  for  
744 both cases.

745 We have used the mode with wavelength  $L$  to  
746 estimate the crack size. There is no clear justification  
747 for the choice of the mode  $L$ , except that it is the  
748 fundamental mode for a crack excitation triggered by a  
749 pressure step applied at its perimeter (Fig. 1 and Table 2  
750 in Chouet, 1986), a scenario suggested by our proposed  
751 model. If we used instead the next higher mode,  $2L/3$ ,  
752 which is at the same time the lowest dominant mode for a  
753 crack excitation triggered at the centre of the crack  
754 (Kumagai and Chouet, 2000; Kumagai et al., 2002), the  
755 estimated crack size would be about twice as big as  
756 for the mode  $L$ . Although based on a host of assumptions,  
757 the estimated dimensions seem quite realistic for both  
758 types of fluid involved in the source process. In theory,  
759 moment-tensor inversion may help us to distinguish  
760 between these two possibilities, based on the estimated  
761 expected amplitudes at seismic stations for the resolved  
762 source orientation and its volumetric change. However,  
763 as seen above, the estimated source size values overlap,  
764 thus producing an overlapping range of values for the  
765 displacement at the source for the two types of fluids. For  
766 instance, a volumetric change of  $150$  m<sup>3</sup>, estimated by  
767 Saccorotti et al. (2007) for the VLP source, gives a  
768 displacement of the crack walls between  $0.6$  mm and  
769  $1.6$  cm for basalt, i.e. between  $6$  mm and  $8$  cm for water.  
770 Neglecting the radiation pattern of the source and  
771 assuming geometrical spreading as a primary factor

772 influencing the amplitude decay, then expected ampli- 820  
773 tude at ECPN station can be roughly estimated by:

$$774 A_{\text{ECPN}} = A_0/r^b, \quad (12)$$

775 where  $A_{\text{ECPN}}$  denotes amplitude of displacement at  
776 ECPN station,  $A_0$  is the amplitude at the source and  $r^b$  is  
777 the geometrical spreading factor with  $b$  taking values of  
778 0.5, 1 or 2, for surface waves, far-field body waves and  
779 near-field term, respectively. Applying the Eq. (12) to the  
780 whole estimated range of values of displacement at the  
781 source (0.6 mm–8 cm), and putting  $r=1.5$  km, the  
782 exponent  $b$  needs to take values between 0.6 and 1.2 in  
783 order to produce an average displacement of 10  $\mu\text{m}$   
784 recorded at ECPN station (Fig. 2). Since the wavefield is  
785 recorded in the near-field, where all types of waves are  
786 intertwined, it is impossible to a priori assign a value of  
787  $b$ . Moreover, the situation is further complicated by a  
788 number of factors, such as the scattering of the wave-  
789 field on the pronounced topography, uncertainties in  
790 the shallow part of the velocity model responsible for  
791 amplification of the signal, the wide range of amplitudes  
792 recorded at the surface and the finite dimensions of the  
793 source. All these suggest that, without a detailed velocity  
794 model of the upper part of the volcano and extensive  
795 numerical simulations, seismological techniques alone  
796 are not enough to distinguish between the types of fluids  
797 involved in the LP source process at Etna. This work will  
798 be the subject of further investigations.

## 799 5. Concluding remarks

800 In this paper we have analysed the temporal evolution  
801 of LP–VLP activity which occurred at Etna Volcano  
802 from November 2003 to August 2005, thus encompass-  
803 ing the effusive eruption taking place between Septem-  
804 ber 2004 and March 2005. We extended the work of  
805 Saccorotti et al. (2007) who analysed a pre-eruptive  
806 sequence of LP activity and proposed a model where the  
807 gas slug formed within the magmatic column being  
808 injected into an overlying cavity filled with either  
809 magmatic or hydrothermal fluids. Although they did  
810 not find a link between the observed LP activity and the  
811 eruption, this work suggests that such a link was  
812 established at the latter end of the eruptive sequence,  
813 most likely as a consequence of a reestablishment of the  
814 pressure balance in the plumbing system, after it was  
815 undermined due to discharge of large amounts of  
816 resident magma during the eruption. Such a scenario  
817 successfully explains the observed increase of the  
818 recorded displacement after the eruption as well as an  
819 increase of both frequency and  $Q$  factors of the source

820 resonance. Furthermore, due to the non-isotropic source  
821 radiation observed by Saccorotti et al. (2007), a change  
822 of polarisation of the mode of oscillation and geological  
823 setting of the source region inferred from a number of  
824 geophysical studies, a crack represents the most like  
825 source geometry. This is also the most natural geometry  
826 satisfying mass transport beneath a volcano (Kumagai  
827 et al., 2002). In this context, the observed difference in  
828 the polarisation of signal before and after the eruption  
829 can be explained by the transition from longitudinal to  
830 transversal crack resonance due to the newly established  
831 equilibrium between the lithostatic pressure and the local  
832 stress field after the eruption. The estimated size of the  
833 basalt- and water-filled cracks, respectively, seems to  
834 be within a realistic range of values expected for Etna  
835 volcano.

We can summarize our interpretation as follows: 836

- 837 1) pressure drop due to the void left by the erupted 837  
838 material 838
- 839 2) this pressure drop leads to a deeper gas nucleation 839  
840 level (a larger gas slug arrives to the terminal part of 840  
841 the conduit (we see it as a deeper VLP source) 841
- 842 3) as a consequence of 2), more gas is injected into the 842  
843 crack (bigger events in Period II than in Period I 843  
844 (which we observe) 844
- 845 4) a new stress regime established by the eruption 845  
846 changes the direction in which the crack is dischar- 846  
847 ging into the surrounding medium (changing the 847  
848 polarisation of the signal) 848

849  
850 Despite both location results and waveform similarity  
851 indicating negligible source movement, the polarisation  
852 attributes change markedly. We attribute this change to a  
853 modification of the way in which the crack discharges  
854 fluid, as a consequence of a changing stress regime. This  
855 aspect suggests that, under particular conditions, LP  
856 could also act as possible stress gauges.

857 This study reveals a different concept for the  
858 generation of LP events, to one described in Falsaperla  
859 et al. (2002) where the LP activity is explained as a  
860 consequence of dyke pressurization due to the collapse  
861 of the crater floor. Also, our model is different from the  
862 Stromboli case, where, as opposed to the interaction  
863 between the two systems suggested here, VLP and LP  
864 oscillations originate in the same system, representing  
865 the volumetric deformation and LP oscillation of a  
866 shallow crack, respectively (Chouet et al., 2003). This  
867 indicates that a wide variety of phenomena can cause the  
868 same type of seismological observations and puts an  
869 imperative on the closer cooperation between different  
870 geophysical and geological disciplines involved in the

871 widening our knowledge about the complex physical  
872 processes beneath volcanoes.

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