

1 **Fluid-dynamics of the 1997 Boxing Day volcanic blast on Montserrat, W.I.**

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9 **Abstract.** *Directed volcanic blasts* are powerful explosions with a significant laterally-
10 directed component, which can generate devastating, high-energy pyroclastic density currents
11 (PDCs). Such blasts are an important class of eruptive phenomena, but quantified
12 understanding of their dynamics and effects is still incomplete. Here we use 2D and 3D
13 multiparticle thermofluid dynamic flow codes to examine a powerful volcanic blast that
14 occurred on Montserrat in December 1997. Based on the simulations, we divide the blast
15 into three phases; an initial burst phase lasts roughly 5 s and involves rapid expansion of the
16 gas-pyroclast mixture, a gravitational collapse phase which occurs when the erupted material
17 fails to mix with sufficient air to form a buoyant column and thus collapses asymmetrically,
18 and a PDC phase which is dominated by motion parallel to the ground surface and is
19 influenced by topography. We vary key input parameters such as total gas energy and total
20 solid mass to understand their influence on simulations, and compare the simulations with
21 independent field observations of damage and deposits, demonstrating that the models
22 generally capture important large-scale features of the natural phenomenon. We also
23 examine the 2D and 3D model results to estimate the flow Mach number and conclude that
24 the range of damage sustained at villages on Montserrat can be reasonably explained by the
25 spatial and temporal distribution of the dynamic pressure associated with subsonic PDCs.

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26

27 **1. Introduction**

28 *Directed volcanic blasts* are powerful explosions with a significant laterally-directed
29 component, which can generate devastating, high-energy pyroclastic density currents.
30 Volcanic blasts have had violent consequences at Bezymianny, Russia, in 1956 [Belousov,
31 1996], and Mt. St. Helens, USA in 1980 [Hoblitt et al., 1981; Moore and Sisson, 1981; Waitt,
32 1981; Fisher et al., 1987; Fisher, 1990; Druitt, 1992]. They represent an important and
33 extremely hazardous class of eruptive phenomena, and consideration of blasts and their
34 associated pyroclastic density currents (PDCs) is necessary for modern volcanic hazard
35 zonation at stratovolcanoes [Crandell and Hoblitt, 1986]. However, quantified prediction of
36 their dynamics and effects is still possible only at a generalized level, often involving
37 simplifying assumptions, such as one- or two-dimensional, steady, and/or choked flow [e.g.,
38 Kieffer, 1981; Woods et al., 2002].

39 The term “*directed volcanic blast*” was suggested for the first time by Gorshkov
40 [1959], who studied the eruption of Bezymianny volcano in Kamchatka in 1956. This
41 directed blast was observed only from large distances, and thus the main conclusions about
42 mechanisms of the event were based on interpretations of the effects and deposits of the
43 eruption. The very similar explosive eruption of Mount St. Helens in 1980 [Lipman and
44 Mullineaux, 1981] rekindled a worldwide interest in directed blasts, and the mass and variety
45 of observations, monitoring data, photo-documentation, and detailed geologic studies at
46 Mount St. Helens enabled a quantum improvement in understanding of the basic causative
47 mechanisms. It was observed that the large-scale collapse of the volcanic edifice, which
48 transformed into a debris avalanche, was the event that triggered a directed explosion by
49 suddenly exposing a pressurized body of magma and gas to atmospheric pressure [Voight,
50 1981; Voight et al., 1981, 1983; Glicken, 1998]. This explosion, and the pyroclastic density
51 current that it generated, devastated a large area of complex topography and left deposits
52 closely resembling those of Bezymianny [Hoblitt et al., 1981; Moore and Sisson, 1981;
53 Waitt, 1981; Kieffer, 1981; Walker and McBroom, 1983; Brantley and Waitt 1988; Fisher et
54 al., 1987; Fisher, 1990; Druitt, 1992; Sisson, 1995; Bursik et al., 1998; Belousov et al., 2007].

55 Through deposit studies and field observations, it has been generally recognized that
56 an initially-pressurized lava dome or cryptodome, suddenly depressurized by a slope failure,
57 can create a directed blast. However, controls on the strength, direction and physics of the
58 initial explosion, its subsequent transformation to a PDC, and propagation of the PDC across
59 incised volcanic topography, require further analysis, with 3D analysis required to capture

60 full interaction with topography. This capability has been lacking in the past in
61 computational fluid dynamics modeling of explosive volcanic phenomena.

62 The recent directed blast from the Soufrière Hills volcano (SHV), Montserrat,
63 provides the opportunity to further improve our understanding of blast dynamics. This blast
64 and associated PDC eradicated the village of St. Patricks and substantially damaged much of
65 the southern part of the island, on 26 December (Boxing Day) 1997 (Figures 1, 2). In this
66 case, despite the severity of the event, no lives were lost because a pre-emptive evacuation
67 was enforced, based on recognition of flank instability and the anticipation of a blast [Young
68 et al., 2002]. The resulting deposits and destructive effects have been well studied [Sparks et
69 al., 2002; Ritchie et al., 2002; Voight et al., 2002; Baxter et al., 2005], and thus despite
70 certain limitations, and apart from the images recorded uniquely at Mount St. Helens, the
71 database for this event is unsurpassed for eruptions of this type.

72 Here we perform a preliminary study using a 2D cylindrical-coordinate model, which
73 allows us to efficiently parameterize the effect of the initial dome mass and energy on the
74 blast behavior and to constrain appropriate initial conditions for later implementation in the
75 3D model. We then apply a fully 3D multiphase flow model incorporating realistic 3D
76 topography, using initial conditions constrained by field observations. We compare these
77 runs against the field observations of the Montserrat event, in order to demonstrate broad-
78 scale similarity between natural phenomena and our model results. We also use the 3D
79 results to demonstrate relationships between the flow dynamics and initial conditions,
80 topography, spatial location, and time, within the context of the model assumptions.

81 The effects of gas compressibility and shock waves on the eruption dynamics was
82 first investigated by Nairn [1976] and Nairn and Self [1978] for vertical explosions. Some
83 authors modeled the directed blast at Mount St. Helens as a quasi-steady-state overpressured,
84 supersonic jet, accompanied by internal shock structures and compressibility effects [Kieffer,
85 1981, 1984; Kieffer and Sturtevant 1984, 1988; Wohletz and Valentine, 1990]. Here, we use
86 *directed blast* simply to denote an explosion, caused by decompression of a cryptodome or
87 lava dome, with a significant initial lateral component and an asymmetric deposit distribution
88 due to an asymmetric source geometry and/or edifice morphology. A contested question is
89 whether the preponderance of strong damage observed in volcanic directed blasts should be
90 attributed to air shocks [Wohletz et al., 1984; Wohletz 1998], supersonic flow within an
91 overpressured jet [Kieffer 1981, 1984], or flow dynamic pressure [Sparks et al., 2002; Baxter
92 et al., 2005; Esposti Ongaro et al., 2005] and (possibly) shocks within the energetic collapse
93 and PDC (gravity current) phases. Exploring this issue is an additional goal of this paper.

94

95 **2. Observational constraints on the Boxing Day blast**

96 At Soufrière Hills Volcano (SHV) in December 1997, an andesite dome and talus
97 cone with a volume of $113 \times 10^6 \text{ m}^3$ was growing above the hydrothermally altered and
98 unstable south flank of the volcano. Gravitational collapse of the flank on 26 December
99 triggered an explosive decompression of the dome's interior, to form a violent blast and PDC
100 that traveled >4 km overland, and then continued >3 km over the sea surface [Voight et al.,
101 2002; Sparks et al., 2002; Hart et al., 2004]. The volume of material (dense rock equivalent,
102 DRE) involved in the failure was estimated from the dimensions of the failure scars and by
103 comparison with pre-collapse topography [Sparks et al., 2002; Voight et al., 2002]: c. $20\text{-}30 \times$
104 10^6 m^3 from the south flank hot spring area, c. $5 \times 10^6 \text{ m}^3$ from the old crater rim, c. 25×10^6
105 m^3 from the lava dome that had grown between 6 November and 26 December, and about 30
106 $\times 10^6 \text{ m}^3$ of lava talus. We take the volume of dome lava participating in the blast as $\sim 25 \times$
107 10^6 m^3 (DRE), exclusive of additional materials that may have been incorporated through
108 erosion. The lava volume is relatively well constrained, but the volume of entrained material
109 is not well constrained due to offshore deposition [Hart et al., 2004]. The total duration of
110 strong activity was ~ 11.6 min but occurred in several pulses. The volatile components in the
111 blast came from the andesite, and the material comprising the blast was a complex multiphase
112 vapor-liquid-solid mixture.

113 Seismic data suggest 6 pulses [Sparks et al., 2002], and stratigraphy reveals clearly
114 only two depositional events, and at least two erosional events resulting from relatively large
115 pulses [Ritchie et al., 2002]. Thus two seismic events are not accounted for in the
116 stratigraphy. It is possible they were both largely erosional onshore or perhaps early deposits
117 were eroded by later pulses, leaving no record observed on land. The individual pulses were
118 short lived, lasting but a few minutes. Only $2\text{-}3 \times 10^6 \text{ m}^3$ DRE was deposited on land with the
119 remainder entering the sea or elutriated by co-PDC plumes. Our constraints are poor but we
120 estimate the small pulse volumes to be ~ 1 to $5 \times 10^6 \text{ m}^3$ DRE, with the minimum value
121 bounded by the volume per pulse deposited on land. The large pulses were two or three times
122 the volume of the small pulses, based on seismic magnitudes, with the sum of all pulses being
123 about $25 \times 10^6 \text{ m}^3$ DRE plus eroded and entrained materials. Co-PDC plumes reached a
124 height ~ 15 km asl, with two separate parts, an ash-rich upper part, and an ash-poor lower part
125 rich in condensed steam [Pace et al., 1998; Mayberry et al., 2002]. The latter is inferred to be
126 a consequence of the PDC entering the sea. The airborne ash was about 15-20% of the
127 original PDC volume [Sparks et al., 2002].

128

129 The area devastated on land was $\sim 10 \text{ km}^2$ with some pulses affecting a 70° sector and
130 a much smaller pulse depositing mainly over only a 35° sector (Fig. 2). The damage varied
131 from complete destruction in the central axial region, to lesser physical effects such as blown
132 out windows and roofs, and fire damage, in peripheral areas [Sparks et al., 2002; Baxter et al.,
133 2005]. The destruction was complete in the axial area of the blast near the village of St.
134 Patricks where structures were razed to their foundations, with detached structural
135 components (including building walls) flattened to the ground or carried to the sea along with
136 loose debris. Buildings swept away include stone-built structures and those with poured
137 reinforced concrete walls. Trees with trunks up to 1m in diameter were removed entirely
138 leaving only abraded stumps and roots [Sparks et al., 2002]. Entrained boulders and pieces of
139 destroyed buildings added to the destructive capability of the PDCs in addition to dynamic
140 pressure [Baxter et al., 2005]. East of the axial area of the blast zone and the White River
141 valley, the blast zone is dominated by erosional features across the raised shoulder of an older
142 volcanic edifice. The severity of damage decreases systematically, but with local variability,
143 from the axis of the PDC towards the lateral periphery. One kilometer west of the axial zone,
144 the top floors of houses were blown down and scattered 50 m down slope, impact marks from
145 saltating boulders occur on house walls facing the volcano, and trucks and a bulldozer were
146 flung over a cliff onto the beach [Sparks et al., 2002; Baxter et al., 2005]. Although trees up
147 to 50 cm in diameter were broken a few meters above ground, smaller trees (<10 cm trunks)
148 and shrubs were merely bent over with branches stripped and the trunk tip sharpened by
149 abrasion. Still farther from the axis, house walls were damaged, roofs were partially or
150 entirely removed, and cars were crumpled and displaced tens of meters. At the western lateral
151 limit of damage, 200-m from source, damage was limited to in-blown windows and displaced
152 roof tiles and blown-down wooden sheds [Sparks et al., 2002]. Dynamic pressures estimated
153 from the damage ranged from >25 kPa in the central axial region to 1-3 kPa near the
154 periphery, with local fluctuations of about ~ 1 -5 kPa associated with localized sheltering and
155 topographic effects [Baxter et al., 2005].

156 There are several other constraints on the dynamics of the Boxing Day event. The
157 upper part of the current climbed almost to the summit of South Soufrière Hills (SSH), from
158 the saddle between Galways Mountain and South Soufrière Hills [Fig. 2; Sparks et al., 2002].
159 The trimline representing the upper surface of the current descends the side of Galways
160 Mountain to the saddle at about 600 m a.s.l., where the current collided with the South
161 Soufrière Hills and climbed 150 m further. Converting kinetic to potential energy for the

162 height climbed in the Galways-SSH peripheral zone results in 55 m s^{-1} for the upper part of
163 the current in this region [Sparks et al., 2002].

164 A reliable but limited constraint on dynamics is given by the St Patricks seismic
165 station, MSPT, about 3.4 km from the dome [Voight et al., 2002; Sparks et al., 2002]. The
166 initial collapse began about 03:01.0 LT (the signal is emergent, making it difficult to pick
167 onset time), the first stronger seismic pulses began at 03:01.8 LT and 03:02.8 LT,
168 respectively, and MSPT was destroyed at 03:03.3 LT [Sparks et al., 2002]. If one assumes
169 that the blast pulse that destroyed MSPT began during the first seismic pulse, the implication
170 is that average frontal speeds were $38\text{-}56 \text{ m s}^{-1}$. An alternative interpretation is that the first
171 seismic pulse represented mainly edifice collapse and debris avalanche movement, and that
172 the second, sharp, seismic pulse represented the blast initiation. This interpretation yields an
173 average frontal blast velocity of 113 m s^{-1} . Nevertheless, focusing exclusively on *average*
174 velocities could be misleading since modeling presented here and observations at SHV
175 [Sparks et al., 2002] and Mount St Helens [Voight, 1981; Moore and Rice, 1984; Hickson,
176 1990; Hoblitt, 2000; Belousov et al., 2007] illustrate that velocities were not constant. We
177 therefore discuss temporal and spatial distribution of blast characteristics from both an
178 observational and modeling perspective later in the text.

179 Dynamic pressure estimates for the pyroclastic density current presented above
180 [Sparks et al., 2002] were calculated from building damage following the approach of
181 Valentine [1998a], where dynamic impact pressures in pyroclastic currents were compared
182 with pressures required to damage structures in atomic explosions. The dynamic pressure P_d
183 is half the product of current mixture density and velocity squared, so that velocity can be
184 calculated if current density is known. Sparks et al. [2002] assumed a mass fraction of gas in
185 the flow and calculated a current density of 6 kg m^{-3} . Using this density, about five times that
186 of ambient air, they concluded that maximum velocities could have been $\sim 30\text{-}40 \text{ m s}^{-1}$ in the
187 peripheral area near Kinsale, $>40 \text{ m s}^{-1}$ near Germans Ghaut, and $\gg 60 \text{ m s}^{-1}$ at St. Patricks.

188

189 **3. Blast modeling**

190 Previous steps toward conceptual and quantified understanding of directed blast
191 behavior illuminated many features of the phenomenon. For example, the lateral blast at
192 Mount St. Helens was modeled as a horizontal quasi-steady-state, underexpanded, supersonic
193 jet with perfect coupling between gas and solid phases [Kieffer, 1981]. These results found
194 limited support in numerical simulations by Wohletz and Valentine [1990], who also
195 explored shock effects in vertical explosions. For Montserrat, modeling of decompression

196 and dome fragmentation [Woods et al., 2002] were combined with an analytical 1D ash-flow
197 model to illustrate basic controls on runout distance and dynamic pressure of the directed
198 blast [Sparks et al., 2002]. Here we assume the model of lava dome pressurization presented
199 by Woods et al. [2002], and apply 2D and 3D unsteady multiphase models of pyroclastic
200 dispersal to the rapid decompression of that dome.

201 Our approach builds upon that of Woods et al. [2002] and effectively extends it in
202 several ways. First, flow in volcanic blasts is highly unsteady and the source conditions are
203 reported to be impulsive. We therefore calculate the rapid decompression of a lava dome with
204 finite mass and gas energy, which creates an impulsive source for our blast model. Second,
205 we relax the assumption of perfect coupling between the gas and solid phase (pseudogas
206 assumption) and thus treat the multiphase aspects of the blast (discussed in the model section
207 below). The perfect coupling assumption is reasonable only for particles ≤ 30 microns in
208 diameter [Woods, 1995; Neri et al., 2003], while recent work synthesizing deposit data shows
209 that $\sim 88\%$ of directed-blast clasts exceed 30 microns [Belousov et al., 2007]. Furthermore,
210 high acceleration in the initial phases of blasts is likely to produce high levels of decoupling
211 between solid and gas phases. Both conditions make relaxing the pseudogas assumption
212 desirable and potentially important. Third, we treat the system in 3D allowing the effects of
213 complex topography on flow propagation to be explicitly explored. In a directed-blast the
214 exposed vent and lava- or cryptodome geometry direct much of the momentum at angles
215 highly oblique to the vertical [Voight, 1981; Belousov et al., 2007]. Moreover, flow
216 channeling and azimuthal variations in topography have particular importance in evolution of
217 the flow [Belousov, 1996; Hoblitt et al., 1981; Ritchie et al., 2002]. Evidence of flow
218 channeling at distances from the vent greater than several km was observed at SHV [Sparks
219 et al., 2002; Druitt et al., 2002] and Mount St. Helens [Hoblitt et al., 1981; Kieffer, 1981;
220 Waitt, 1981], revealing that channels allowed dangerous flows to move far from the blast
221 axis, and cause destruction in locations that would not necessarily have been predicted by
222 intuition or by 2D simulations. Furthermore, tree blowdown patterns at MSH [Waitt, 1981;
223 Kieffer, 1981] provide evidence of topography-initiated flow separation and formation of
224 large-scale eddies. As a result of rugged topography, damage was highly variable over
225 relatively short spatial scales.

226

227 **3.1. Physical and numerical model**

228 Motivated by the aforementioned factors, our model describes the dynamics of
229 directed blasts by adopting the multiphase transport theory [Gidaspow, 1994; Valentine

230 1998b; Dartevelle, 2004]. Accordingly, each phase of the mixture (gas, liquid, and solid with
231 specific characteristics) is described separately from the others by solving the corresponding
232 mass, momentum, and energy balance equations. The model thus describes the kinetic and
233 thermal disequilibrium of the gas and particles, and the interphase momentum and energy
234 exchange. In detail, we adopted the PDAC (*Pyroclastic Dispersal Analysis Code*) code
235 [Esposti Ongaro et al., 2007; Neri et al., 2007], which solves the multiphase flow equations
236 on two and three-dimensional domains with topography imported from a digital elevation
237 model (DEM). This code is an evolutionary advance from the KFIX code developed at the
238 Los Alamos National Laboratory (USA) in the mid 70's [Rivard and Torrey, 1977], and
239 further developed along one evolutionary branch at the Illinois Institute of Technology (US)
240 for fluidization engineering studies [Gidaspow, 1994]. The basic model formulation and
241 algorithm derive from the work of Harlow and Amsden [1975], in which classical iterative
242 methods for subsonic flows were extended to the compressible and supersonic regime and to
243 multiphase flows. The details of these models are given by Neri et al. [2003], Dartevelle
244 [2004], and Esposti Ongaro et al. [2007].

245 This approach makes it possible to investigate the dispersal of pyroclasts in the
246 atmosphere and along the volcano flanks without the need of *a priori* assumptions and *ad-hoc*
247 parameterizations of the flow features (e.g., the transient 3D feature allows effective
248 description of flow characteristics in the different regions of the system, the turbulent
249 entrainment is explicitly simulated through the large eddies of the flow and only
250 parameterized at the subgrid scale, the particle settling velocity is computed explicitly by the
251 model as a function of flow properties and need not be specified *a priori*). Moreover, the
252 possibility of using different particle classes gives us the opportunity to investigate the
253 different dispersal pattern of each particle size as well as the effect of their relative proportion
254 on the flow behavior.

255 Nevertheless, several limitations to our model formulation still exist. Present model
256 formulation is limited to solid volume fraction less than about 50 vol.%. Above this
257 threshold, the flow likely enters a frictional regime requiring a different set of constitutive
258 equations. Moreover, although the model describes the sedimentation and stratification
259 within the flow (as well as particle elutriation) through the settling of different particle
260 classes, an explicit deposition model (i.e. particle loss from the ground boundary condition) is
261 not included at this time in the formulation, so that particles are assumed to remain fluidized
262 at all times. A recent study by Dufek and Bergantz [2007] has shown that deposition through
263 a leaky boundary can significantly decrease runout distance, therefore our estimates should

264 be considered liberal in this respect. However, on Montserrat on land, because of the steep
265 slopes there was little deposition and the stronger pulses were erosive. So for the modeling in
266 this paper, the lack of a deposition subroutine seems unimportant. Similarly, erosion and
267 entrainment of substrate material into the density current are not explicitly considered in our
268 model. The thermal interactions between the hot PDCs and the sea surface, and phase
269 changes (condensation) of water vapor, are not specifically treated. However, water vapor
270 condensation is possible only in the upper region of the computational domain, as verified by
271 computing *a posteriori* the water vapour saturation pressure as a function of local pressure,
272 temperature and concentration.

273 Full model verification and validation is an ongoing endeavor, especially for 3D
274 flows, including “validation” against natural events, with new regimes and dynamic
275 conditions being tested continually. To this aim, several applications of the PDAC code in 2D
276 have been successfully carried out in the last decade to assess the model’s ability to capture
277 the behavior of compressible, dilute, turbulent multiphase flows. Neri and Gidaspow [2000]
278 have compared 2D cylindrical and Cartesian model solutions to fluidization experiments in
279 order to test the formulation of the particulate phase. Similarly, the gas turbulence subgrid
280 model has been validated against experiments of gas flow around a bluff-body [Barsotti,
281 2002]. The accuracy of compressible flow simulations was also tested for both one- and two-
282 dimensional shock tubes and supersonic jets by comparison against analytical solutions and
283 well-validated results obtained by other codes [Esposti Ongaro et al., 2006, 2007]. Clarke et
284 al. [2002a,b] compared solutions of PDAC2D against well-documented Vulcanian explosions
285 on Montserrat in 1997.

286

287 **3.2 Initial conditions for the multiphase flow model**

288 Initial source conditions are as follows. The dome is represented as a hemisphere on a
289 sloping base with uniform gas volume fraction of 0.1, based on measurements given by
290 Robertson et al. [1998] and Melnik and Sparks [2002]. During the effusive phase, the dome
291 grows as degassed magma reaches the interior or surface of the dome, while the exsolved
292 volatiles separate from the magma and travel through the permeable dome to the atmosphere
293 [Melnik and Sparks, 1999; Sparks et al., 2002]. Models of viscous conduit flow with gas
294 escape show that overpressures of several MPa can develop near the conduit exit, where
295 overpressure is taken as the difference between gas pressure and local lithostatic pressure
296 [Sparks, 1997; Melnik and Sparks, 2002]. The overpressure is only partially dissipated by gas
297 escape through the permeable dome. We use the Woods et al. [2002] permeable hemisphere

298 model to determine initial pressure profiles within the lava dome prior to the blast, for a
299 steady gas (steam) flux of $\sim 400 \text{ kg s}^{-1}$ and dome permeability K . The gas flux is consistent
300 with measured magma extrusion rates of $\sim 8 \text{ m}^3 \text{ s}^{-1}$ for December 1997 [Sparks et al., 1998],
301 and bulk volatile content $\sim 2 \text{ wt}\%$ [Barclay et al., 1998]. No COSPEC measurements were
302 made during December 1997, but this result is conservative with correlated SO_2 flux with
303 magma output, $\sim 680 \text{ g SO}_2$ per tonne of magma [Young et al., 1998] and $\text{H}_2\text{O}/\text{SO}_2$ ratios of
304 200-1000 [Woods et al., 2002]. Measurements of dome rock suggest permeability values in
305 the range $K = 10^{-14}$ to 10^{-12} m^2 , including the effects of pervasive fractures [Melnik and
306 Sparks, 2002]. Gas is assumed to be steam with a temperature of 850° C and vapor viscosity
307 $2 \times 10^{-5} \text{ Pa s}$ [Woods et al., 2002]. These results yield overpressures of the order 5-10 MPa
308 throughout much of the dome for $K = 10^{-12} \text{ m}^2$, and higher values for lower permeability. For
309 the range of permeabilities considered, the mass of solid fraction ranges from 12 to 25×10^9
310 kg, whereas the net mass of exsolved gas (water vapor) in the dome ranges from 3 to 15×10^6
311 kg. This is an important result that constrains the dynamics of the fragmenting mixture. Such
312 pressurized domes have two to three orders of magnitude less exsolved volatiles per mass of
313 magma than is present in a typical Plinian eruption, and this leads to a substantially greater
314 density of the pyroclastic currents produced [Woods et al., 2002].

315 The particle size distribution of the Boxing Day blast deposit was estimated by
316 Ritchie et al. [2002] using well-established sedimentological techniques, although much
317 uncertainty remains in the characterization of pyroclastic mixtures, particularly when large
318 portions of the flow are lost to sea. Based on these deposit studies and additional field work
319 of our own, we use three particle sizes ($5000 \mu\text{m}$; $500 \mu\text{m}$; $50 \mu\text{m}$) to represent particle
320 classes $>2000 \mu\text{m}$, $\sim 125 \mu\text{m}$, and $<125 \mu\text{m}$, respectively, yielding the bulk proportions 25,
321 40, 35 wt%. A density of 2300 kg m^{-3} is used for the largest particle size, otherwise particle
322 density is 2600 kg m^{-3} . Although the three populations cannot cover the full spectrum of
323 grain sizes in the deposits, particularly the coarse tail, our choice was dictated by both
324 computational efficiency and the physical model (constitutive equations) which cannot treat
325 clasts larger than several mm. Furthermore, the model does not treat changes in grain size
326 due to aggregation and secondary fragmentation, processes which have yet to be
327 quantitatively characterized. We refer the reader to previous work which explicitly explores
328 the effects of grain size simplifications on 2D model results [Neri and Macedonio, 1996; Neri
329 et al., 2003] and leave the corresponding 3D study for future work.

330 The volume of dome lava involved in the blast and its associated high-energy PDC
331 was $\sim 25 \times 10^6 \text{ m}^3$ dense rock equivalent (DRE). This value is relatively well constrained, but
332 because the total duration of strong activity was ~ 11.6 min and occurred in several pulses, we
333 partitioned the total volume into smaller quantities representing individual pulses. Our main
334 constraint is on the *total* volume of original dome, which limits the sum of individual pulse
335 volumes, apart from additional materials entrained. For our models we therefore consider
336 representative volumes of ~ 5 and $10 \times 10^6 \text{ m}^3$ DRE, representing relatively small and large
337 pulses, according to arguments outlined in Section 2.

338

339 **4. 2D Simulation results**

340 Before conducting the 3D simulations, we performed a number of 2D sensitivity runs
341 using PDAC. Here we present three of these, illustrating the influence of solid mass (or
342 volume), and gas energy (via the influence of permeability on dome pressurization), on flow
343 evolution. The first comparison between simulations examines the influence of mass released
344 by varying volume DRE (5 and $10 \times 10^6 \text{ m}^3$), independently of permeability, which remains
345 constant at $K = 10^{-12} \text{ m}^2$. The second comparison examines the effects of gas pressure and
346 energy, by varying pre-blast dome permeability ($K = 10^{-12} \text{ m}^2$ and 10^{-14} m^2), while keeping
347 volume constant at $5 \times 10^6 \text{ m}^3$ (Table 1). The computational domain extends 10 km radially
348 and 8 km vertically, with a non-uniform mesh resolution increasing very gradually, from 10
349 m close the left boundary axis of symmetry and above the topography, to 100m on the right
350 edge and the top atmospheric boundaries. The non-uniform mesh allowed us to increase the
351 resolution in the regions near the source and the ground, where we observe the largest
352 gradients in the flow variables. The location of the topographic profile used in all 2D
353 simulations is shown in Fig 2 (A-A') and includes the offshore sea surface. Although the
354 dense basal portion of pyroclastic flows can travel underwater, pyroclastic surges on
355 Montserrat have been observed gliding over the sea [Montserrat Volcano Observatory,
356 unpublished data; Hart et al., 2004].

357

358 **4.1 Large-scale features**

359 Simulation A-2D uses a high permeability value of $K = 10^{-12} \text{ m}^2$ resulting in internal
360 gas pressures from 10 MPa at the base of the dome to atmospheric at the surface. The solids
361 volume $V_{\text{DRE}} = 5 \times 10^6 \text{ m}^3$ assumed for the $\sim 70^\circ$ sector corresponded to a mass per unit angle
362 of $(5 \times 10^6 / 2\pi) \times (360/70) \text{ m}^3/\text{radian}$ for input in the cylindrical coordinate simulation. An

363 estimate of the volatile energy stored in the dome is given by the specific work, and the range
364 of values (see Table 1) correspond to purely adiabatic (lower limit) or purely isothermal
365 (upper limit) expansions [Woods et al., 2002]: $E_s = 320\text{-}490 \text{ J kg}^{-1}$. Simulation B-2D uses a
366 greater dome volume of 2X that of A-2D ($V_{\text{DRE}} = 10 \times 10^6 \text{ m}^3$ for the 70° sector; $E_s = 390\text{-}$
367 610 J kg^{-1}), but is otherwise nearly identical to A-2D. The specific energy is slightly greater
368 in B-2D due to the non-linearity of the pressure distribution within the dome. Simulation C-
369 2D uses $K = 10^{-14} \text{ m}^2$, which results in greater interior pressures and much higher gas energy:
370 $E_s = 1880\text{-}3380 \text{ J kg}^{-1}$. The volume is identical to A-2D.

371 In simulation A-2D (Figure 3), an initial quasi-spherical expansion occurred, reaching
372 maximum gas velocity of $\sim 160 \text{ m s}^{-1}$ at 0.2 s. Corresponding peak particle velocities varied
373 with particle size; 75, 125, and 155 m s^{-1} for particle diameters of 5000, 500, and $50 \mu\text{m}$,
374 respectively. Lateral velocities were greater than vertical by 0.3 s. At 2 s, the vertical mixture
375 speed was $\sim 120 \text{ m s}^{-1}$, and horizontal speed was 170 m s^{-1} . We call this first stage the burst
376 phase, in which the dynamics are primarily controlled by gas expansion and associated
377 particle acceleration, and are strongly affected by the initial total specific gas energy.
378 Velocities in the burst phase are generally higher than the sound speed of the pyroclast
379 mixture, which is much lower than the atmospheric sound speed because of the relatively
380 high particle concentration. Nevertheless, we propose that any leading atmospheric pressure
381 wave was weak [$(p_{\text{after}}/p_{\text{before}}) < 1.5$] for three reasons; the initial velocities of the pyroclast
382 mixture were much less than sound speed in atmosphere, $\sim 330 \text{ m s}^{-1}$ at standard ground
383 conditions, the pressurized fluid was a solid-gas mixture with a low gas volume fraction, and
384 the pressure ratio between the dome's interior and the atmosphere prior to blast initiation was
385 less than 100 [Chojnicki et al., 2006].

386 The erupted material fails to mix with sufficient air to form a buoyant column and
387 thus, at $t > 5 \text{ s}$, collapses below the source, initiating the collapse phase (Fig. 3a). The
388 material then moves parallel to the ground surface in the PDC phase beginning between 15
389 and 20 s after onset (Fig. 4). The transition from initial burst to PDC phase is highlighted by
390 the trajectories of the fluid parcels from 0 to 15 s (Fig. 3b). The trajectories are characterized,
391 in the first seconds, by ballistic paths, where the outermost portions of the dispersed dome
392 pyroclasts reach the maximum height ($>1300 \text{ m a.s.l.}$, 250 m above the dome). We interpret
393 the start of the collapse phase as the point in time when a preponderance of "ballistic" paths
394 have passed peak height and are inclined downward and outward. The phases defined here
395 are to some extent gradational.

396 The transformation to the PDC was mostly complete by 15-20 s, with the flow front
397 ~1 km from source, and PDC velocity about 70 m s^{-1} . The evolution of the PDC is illustrated
398 by the isocontours of the total particle volumetric fraction at selected times in Fig. 4. At 40 s
399 the PDC head has reached a distance of about 2700 m from the source where particles start to
400 be elutriated by vertical convection. Mixing of the PDC with the atmospheric air occurs
401 mainly through the entrainment at the flow head, as evidenced by the thickened nose. At 90s
402 the flow head has reached 5 km and has grown by air entrainment and expansion. A vertical
403 convective plume is rising above the vent and small co-PDC clouds are developing where
404 topographic slope abruptly changes and because of vortex instability in the tail. At 180s the
405 elutriation of particles by co-PDC plumes is more developed, while the velocity of the PDC
406 head is greatly reduced, and now consists of a dilute ash current overlying a dense basal flow.
407 Nevertheless, it is worth recalling that the boundary condition at the bottom does not account
408 for the interaction of the PDC with the sea surface or for the loss of particles by deposition so
409 that the run-out of this thin basal flow could be overestimated, especially using a coarse mesh
410 [Neri et al., 2003; Darteville et al., 2004; Appendix]. At 240 s the PDC head has stopped and
411 an intense co-PDC plume develops at 6 km, while a dense basal flow has reached the distance
412 of 10 km. The animation of the results better represents the temporal evolution of the burst
413 and PDC propagation and can be seen on Movie S1 in the on-line auxiliary material.

414 In simulation A-2D, more than 95% of the total solid mass fed into the PDC. A small
415 fraction (less than 5%) of the mass fed the plume above the dome (Fig 4 at 90s). Co-PDC
416 plumes developed downslope after ~80 s, reflecting gravity segregation of fine versus coarse
417 particles in the PDC, and development of mixture buoyancy by air entrainment; the plumes
418 elutriated about 50% of $50 \mu\text{m}$, 20% of $500 \mu\text{m}$, and a negligible fraction of $5000 \mu\text{m}$
419 particles. The mass in the PDC was computed by integrating the particle bulk density in the
420 sub-domain where $R > 1 \text{ km}$ and $Z < 0.9 \text{ km}$, whereas elutriation by the co-PDC was
421 calculated over the sub-domain where $Z > 0.9 \text{ km}$.

422 Simulation B-2D begins with double the dome volume of A-2D, with parameters
423 otherwise the same. B-2D produced the longest runout PDC of all 2D simulations due to its
424 higher mass. Initial quasi-spherical expansion in the burst phase achieved peak gas velocities
425 $\sim 160 \text{ m s}^{-1}$ at 0.2 s, but peak particle velocities varied with particle size. The burst phases of
426 A-2D and B-2D are very similar, because the specific gas expansion energy is of the same
427 order of magnitude (Table 1). At 2 s, vertical mixture speed was $\sim 115 \text{ m s}^{-1}$, and horizontal
428 speed was 200 m s^{-1} (Fig. 5a). The erupted material failed to become buoyant and at $t > 5 \text{ s}$,

429 and collapsed below the vent. The current then moved parallel to the ground surface in the
430 PDC phase at $t > 10$ s, with the flow front ~ 1 km from source, and slope-parallel velocities of
431 roughly 80 m s^{-1} . The trajectories of the fluid particles are similar to A-2D, with a very short
432 expansion phase followed by the sudden collapse of the stream (Fig. 5b).

433 The temporal evolution of the B-2D PDC is similar to A-2D up to 90s (Fig. 6 and
434 Movie S2 in auxiliary material), although the flow front moves faster due to higher inertia.
435 The main differences can be observed after 130s when the flow head does not significantly
436 slow down while the co-PDC plumes begin to develop in the flow tail. Instead, at 180s the
437 PDC head structure is preserved without showing significant deceleration and has reached a
438 distance of 10 km. The elutriation of particles occurs only in the PDC tail, so that it exerts a
439 negligible effect.

440 Next we examine simulation C-2D, which begins with a dome volume identical to A-
441 2D but K has been reduced to 10^{-14} m^2 . The lower permeability results in greater interior
442 pressures of several tens of MPa and much higher gas energy than A-2D. Because these
443 magnitudes exceed previous estimates of conduit pressures [Clarke et al., 2002a,b; Voight et
444 al., 1999], we consider this an extreme upper-bound case but useful to explore the effects of
445 high dome overpressures on the blast. As a consequence of the higher gas energy (compared
446 to A-2D) the initial quasi-spherical expansion reached a maximum gas velocity of 175 m s^{-1} ,
447 with corresponding peak particle velocities of 80, 145, and 175 m s^{-1} for particle diameters of
448 5000, 500, and $50 \mu\text{m}$, respectively. At 2 s, vertical speed was $\sim 140 \text{ m s}^{-1}$ and horizontal
449 speed was 188 m s^{-1} , and at 5 s, the average speeds were 106 m s^{-1} vertically, and 150 m s^{-1}
450 horizontally (Fig.7a). The erupted material again failed to mix with sufficient air to form a
451 buoyant column and thus, in the gravity collapse phase at $t > 5$ s, collapsed downslope in a
452 stream of ash, blocks, and gas. The material then moved parallel to the ground surface in the
453 PDC phase at $t > 20$ s (Fig. 9). The burst phase of C-2D is characterized by a violent radial
454 expansion of the mixture, with fluid parcels following almost ballistic trajectories up to 10 s
455 and greater than 500 m above the dome (Fig. 7b). Despite the high internal dome pressure,
456 even in this case the atmospheric pressure perturbation rapidly decays with distance from
457 source. Perturbations of the atmospheric pressure in the first 10 s at different distances from
458 the dome are shown in Figure 8. Values are sampled at 5 m above the ground. The plots
459 clearly identify the arrival of the pressure wave caused by the burst. The overpressure is
460 about 15 kPa at 1 km, creating a weak pressure wave of strength $(p_{\text{after}}/p_{\text{before}}) < 1.2$, and
461 decreases to only a few kPa at 3.5 km. Overpressures > 2 kPa are sufficient to cause tree

462 blowdown [Valentine, 1998a], although the interior dome pressures assumed for C-2D are
463 extreme.

464 The transition from collapse phase to PDC phase occurs at ~15-20 s. PDC front
465 speeds are $\sim 90 \text{ m s}^{-1}$ at the transition. The temporal evolution of the PDC (Fig. 9, Movie S3
466 in auxiliary material) is similar to A-2D except that co-PDC plume development is more
467 vigorous due to the greater initial expansion of the mixture associated with higher dome
468 pressure. An intensely buoyant co-PDC plume develops from the flow head at a distance of 5
469 km at about 150 s and is then pulled vent-ward by the strong vertical convection above the
470 vent (Figure 9, 180 s). At 240s the co-PDC plume extends to about 4 km from the source
471 while a dense, thin basal flow has reached the distance of 10 km. The co-PDC plumes
472 elutriated about 65% of $50 \mu\text{m}$, 30% of $500 \mu\text{m}$ and $<5\%$ $5000 \mu\text{m}$ particles.

473

474 **4.2. PDC dynamics**

475 Figure 10 shows the PDC front positions vs. time and the PDC front velocity vs.
476 distance from the source. The front is tracked by measuring the most advanced part of the
477 PDC, without distinguishing between the flow head and the thin basal layer. The “low
478 energy” blasts (A-2D and B-2D) display nearly parallel trends, with B-2D’s flow velocity
479 systematically higher than that of A-2D. The slight change in slope of the A-2D distance-time
480 curve occurs where the current becomes positively buoyant and decelerates as a result. The
481 more energetic blast (C-2D), on the contrary, attains the highest initial PDC velocity of all
482 three 2D simulations (Fig. 10b) but decelerates rapidly due to extensive entrainment of
483 atmospheric air and subsequent development of positive buoyancy in portions of the flow. As
484 a result, the final PDC run-out is comparable with that of A-2D.

485 The trends of the front velocity vs. distance (Fig. 10b) are very similar for A-2D and
486 B-2D even though the former shows more pronounced changes in the front velocity at 4 km
487 (corresponding to the break-in-slope) and 6 km (where the co-PDC plume forms). On the
488 other hand, the PDC front of C-2D developed a very high lateral velocity in the burst phase
489 (please note that the front velocity does not necessarily coincide with the maximum flow
490 velocity) while it decreased more rapidly corresponding to breaks-in-slope and subsequent
491 entrainment.

492 Figure 11 compares mixture density, mixture velocity, and dynamic pressures, as a
493 function of time, at 10 m above the ground surface at sampling positions 2, 3, and 4 km from
494 the source. The left plots refer to simulations with lower dome volume (A-2D and C-2D),

495 whereas the right plots refer to the higher volume (B-2D). The dynamic pressure is computed
 496 from the mixture density $\rho_m = \varepsilon_g \frac{P\bar{\mu}}{RT_g} + \sum_s \varepsilon_s \rho_s$ and the horizontal and vertical mixture
 497 velocity components $(u_m, v_m) = \frac{1}{\rho_m} \left[\varepsilon_g \frac{P\bar{\mu}}{RT_g} (u_g, v_g) + \sum_s \varepsilon_s \rho_s (u_s, v_s) \right]$, according to
 498 $P_d = \frac{1}{2} \rho_m \sqrt{(u_m^2 + v_m^2)}$. In the preceding equations, $\bar{\mu}$ is the averaged molecular weight of
 499 the gas mixture, P and T_g are the gas pressure and temperature, R is the universal gas
 500 constant, ρ_s is the density of the pyroclasts, ε is the volumetric fraction of a phase and the
 501 subscripts g and s refer to the gas and solids, respectively.

502 Mixture density plots (Fig. 11) show a peak corresponding with the passage of the
 503 flow head. This peak decreases in magnitude with distance from source, which we interpret
 504 to indicate flow head dilution. However, at later times (e.g., 100 s), the PDC mean density is
 505 controlled by the competing effects of intra-current sedimentation of particles and elutriation
 506 via a buoyant gas stream. For A-2D, peak densities of ~ 57 , 19, and 18 kg m⁻³ occurred at the
 507 three sampling positions at times ~ 50 , 70, and 100 s. For C-2D, very similar values are
 508 reached about 10 s earlier. In contrast, B-2D produced peak densities of ~ 118 , 38, and 30 kg
 509 m⁻³ at the same locations, roughly double the values of the other two runs. Nevertheless, it is
 510 worth noting that the exact values of the density in the basal cells can be affected
 511 significantly by the mesh resolution. The sedimentation process is influenced by the vertical
 512 mesh size and deposition, as discussed above, and deposition is not explicitly treated by the
 513 model. The sensitivity of model results to grid resolution is discussed in detail in the
 514 appendix.

515 Mixture velocity also decreases with the distance from the vent and after the passage
 516 of the flow head. Please notice that mixture velocity 10 m above the ground is generally
 517 much lower than the front velocity (compare Fig. 11 to Fig. 10b), due to flow stratification.
 518 For A-2D, maximum velocities of 46, 40, and 34 m s⁻¹ occurred at 2, 3, and 4 km at times
 519 ~ 35 , 60, and 75 s, respectively. For C-2D, maximum velocities at 2, 3, and 4 km, 10 m above
 520 ground, are 72, 44, and 33 m s⁻¹, at 23, 50, and 60 s, respectively. Apart from higher speed at
 521 the 2 km position, the values are close to those of A-2D, but occur 10-15 s earlier. For B-2D,
 522 peak velocities were 66, 43, 40 m s⁻¹, at times of 26, 50, and 65 s. Peaks in velocity always
 523 occur earlier than peaks in density, indicating that the arrival of the dilute ash cloud precedes
 524 the arrival of the dense basal layer. The large oscillations after about 110 s reflect the
 525 development of convective co-PDC plumes.

526 For A-2D, dynamic pressure peaks of ~44, 13, and 7 kPa occurred at the sampling
527 positions at times of ~45, 65, and 90 s, about 15-20 s after the arrival of the PDC front.
528 Similar values for C-2D occur almost 10 s earlier, because of the larger initial velocity of the
529 burst phase. For B-2D, dynamic pressure peaks of ~75, 28, and 14 kPa, occurred at the
530 sampling positions at times ~48, 65, and 80 s, about 20 s after the arrival of the PDC front.
531 The A-2D and C-2D simulated peak dynamic pressure in the region of severe damage at St.
532 Patricks and Morris (at about 3.4 km from the source) were between 10 and 15 kPa, values
533 less than those estimated to explain the damage observed [Sparks et al., 2002; Baxter et al.,
534 2005]. On the contrary, for B-2D, simulated dynamic pressure in the same region was as
535 much as 25 kPa, consistent with the minimum value (>25 kPa) proposed by Sparks et al.
536 [2002] and Baxter et al. [2005] to explain the damage observed. The reader is cautioned that
537 these near-ground (~10 m) dynamic pressures could be significantly underestimated due to a
538 grid size effect (see Appendix, Fig. A2). Nevertheless, the general conclusion appears to be
539 sustained.

540 An interesting feature of these simulations is that velocities in the region of severe
541 damage between 3 and 4 km appear to be similar for A-2D, C-2D and B-2D, i.e. 33-43 m s⁻¹,
542 whereas doubling the mass approximately doubled the peak mixture density, and doubled the
543 dynamic pressure. We therefore conclude that damage potential on Montserrat may be linked
544 more closely with high mixture densities than with unusually high current speeds.

545 Modeled mixture temperatures were also recorded at 2, 3, and 4 km positions, 10 m
546 above ground. For all runs, and in all cases, peak values are roughly ~800°C, close to the
547 initial temperature of the lava dome. These high peak values indicate that the basal layer of
548 the PDC can keep high temperatures despite the intense air entrainment in the overlying ash
549 cloud. At 90 s convective plumes increase entrainment and plume temperatures drop to 200-
550 400°C. Erosion and entrainment of cold substrate material on Montserrat undoubtedly
551 contributed to temperature reduction, but are not treated in these simulations. Nevertheless,
552 high temperatures of the ash in the Boxing Day event caused rapid ignition of furniture and
553 combustibles, and was a major source of damage even at the periphery of the impacted area
554 [Baxter et al., 2005].

555 Fig. 12 shows the dynamic pressure at R = 3.4 km (the distance relevant for damage
556 observed at St. Patricks) at 10 m above ground. For A-2D, the onset of the jump in dynamic
557 pressure associated with the arrival of the PDC front at SPT seismic station (at R = ~3.4 km)
558 occurred at ~60 s, whereas the peak dynamic pressure occurred at ~70 s. For B-2D the flow
559 front arrived at ~50 s with a peak at ~70 s. For C-2D the flow front arrival and peak dynamic

560 pressure roughly coincide at ~50-55 s. Given that the initial dome radius is 230 m, the
561 average velocity for A-2D was $(3400-230 \text{ m})/60 \text{ s} = 53 \text{ m s}^{-1}$, whereas for B-2D and C-2D,
562 the velocity was approximately 63 m s^{-1} . These values are close to the average velocities of
563 $38-56 \text{ m s}^{-1}$ inferred from the timing of the first seismic pulse, but <50% of the velocity
564 inferred from the second seismic pulse (113 m s^{-1}). Our models therefore support the
565 hypothesis that the first pulse destroyed the station, although we must emphasize that average
566 velocities fail to capture the complex velocity vs. distance estimates discussed in previous
567 sections. The main 2D simulation results are summarized in Table 2.

568

569 **5. 3D simulation results**

570 Guided by the 2D parametric runs, the 3D PDAC code was applied over a Digital
571 Elevation Model (DEM) with a 20-m grid. The DEM represents conditions just before the
572 blast, with topography from a debris avalanche deposit filling much of the original White
573 River valley. The 3D computational domain is extended 9 km in longitude (from $X=76160$ to
574 $X=85060$ on the UTM map), 9 km in latitude (from $Y=41560$ to $Y=50460$) and 6 km
575 vertically. The horizontal mesh resolution varies, very gradually, from 20 m near the source
576 up to 200 m on the lateral boundaries. The vertical resolution varies from 20 m over the first
577 800 m, and gradually increases to 200 m at the top of the domain. The non-uniform mesh
578 allowed us to increase the resolution in the regions near the source and the ground, where we
579 observe the largest gradients in the flow variables. The initial dome is represented by a
580 hemisphere centered at coordinates [$X=80690\text{m}$; $Y=46550\text{m}$; $Z=710\text{m}$] on the summit flank,
581 sloping to the south [see topography Figure 13]. Two 3D simulations are presented here, A-
582 3D ($V_{\text{DRE}} = 5 \times 10^6 \text{ m}^3$), and B-3D ($V_{\text{DRE}} = 11 \times 10^6 \text{ m}^3$). For both cases, $K=10^{-12} \text{ m}^2$. We
583 compared the simulation results against one another, and against maps of deposits and
584 destruction and observational data [Sparks et al., 2002; Ritchie et al., 2002; Baxter et al.,
585 2005].

586

587 **5.1. Large-scale features**

588 The results of the 3D runs are shown in Figure 13 and 14. Fig. 13 (vertical slice
589 through the dome center, parallel to PDC propagation direction) shows the initial *burst* phase
590 for simulations A-3D (a) and B-3D (b). The simulation is characterized, as in the 2D cases,
591 by an initial expansion phase at $t < 5\text{s}$, when the pyroclastic mixture expands into the
592 atmosphere forming a quasi-spherical shell. The subsequent collapse of the cloud at $t \sim 10 \text{ s}$
593 produces a PDC which travels down slope. The asymmetry of the collapse is due, in 3D, to

594 the source topography that provides an initial tilted flank on which the source rests, and an
595 impediment to the propagation toward the Northern sector. The blast phase is very similar for
596 A-3D and B-3D since the initial specific energy is nearly identical (Table 1).

597 Fig. 14a shows simulations A-3D propagating over a 20-m DEM of southern
598 Montserrat viewed to the north. The evolution of the blast and blast-generated PDC is
599 illustrated by color contours that represent total volume particle fraction, decreasing from
600 dark (10^{-2}) to light (10^{-6}). The figure illustrates important effects associated with local
601 topography, including accelerations affected by steep slopes, non-radial motions caused by
602 obliquely-orientated topographic elements, particle-size segregation better developed in
603 channels than on interfluves, and topography-influenced formation of buoyant plumes near
604 the source and above the PDCs. At 10 s (not shown) early gravitational collapse feeds the
605 PDC, followed by topographic segregation into two distinct PDC lobes. By 30 s the PDC is
606 spreading over a broad sector of the landscape, with its main axis directed through St Patricks
607 village, and segregation into local channels is shown by the development of several lobes.
608 There is a weak rise of near-source buoyant plumes. Just after 60 s only one lobe exists, in the
609 White River valley. By 90 s, multiple buoyant plumes are evolving above the source region,
610 while the densest portion of the main lobe verges on St Patricks village, and the more dilute
611 front extends over a 70° sector and to nearly 2 km offshore.

612 The second 3D simulation, B-3D (Fig. 14b), is representative of the higher-volume
613 destructional/erosional pulses. The PDC flow features are generally similar to, but more
614 strongly developed than, the previous run of Fig. 14a. At 10 s (not shown), early gravitational
615 collapse feeds the PDC, followed by topographic segregation. By 30 seconds the PDC has
616 spread over a 60° sector, centered about a main axis aligned to the southwest. Two lobes have
617 developed, concentrating most of the mass in the White River channel; the current also
618 moves in places over interfluves, aided in some cases by runup at channel bends. The densest
619 portions of the two lobes remain beyond 60 s. By 90 s, the densest portion of the PDC occurs
620 as a single lobe, and the PDC front has bypassed St Patricks and extends 3 km offshore, while
621 multiple co-PDC plumes are rising above the source region.

622 Further details of the 3D simulations are illustrated by contours log of the particle
623 volume fraction 10 m above the topographic surface and along a longitudinal (LL') and a
624 transverse (PP') section (Figure 15). The particle maps (Fig. 15a,d) show, in both cases, a
625 channelized flow to the east, in Dry Ghaut, recognized also in the field [Fig. 2; Druitt et al.,
626 2002]. The model blast-affected sector is roughly 70° in both simulations and compares well
627 with the mapped distribution (Fig. 2 and bold line in Fig. 15a,d). In both A-3D and B-3D,

628 particles concentrate near the base of the flow whereas co-PDC plumes generally develop at
629 slope breaks and are significantly more dilute (Fig. 15b,c,e,f). The highest particle
630 concentration occurs in channels and decreases with height above the surface (Fig. 15b,c,e,f),
631 and laterally away from the centerline of the deepest channels (Figs. 15c,e). In general,
632 current velocities are greater in the 3D simulations due to channeling effects, but some
633 general trends are similar to the 2D runs. For example, doubling the dome mass (Simulation
634 B-3D) also increases the PDC density, dynamic pressure and velocity, and decreases the
635 elutriation rate (as in 2D).

636 Field studies of the SHV deposits provide evidence that mobile dense basal flows
637 drained into channels which did not directly connect with the primary source area (secondary
638 flows), including ravines west of St Patricks and Dry Ghaut to the east of the vent. They
639 were immediately recognized as representing an important, but puzzling and hitherto
640 underestimated hazard around active lava domes [Druitt et al., 2002]. The 3D simulations
641 presented here strongly suggest that this type of hazardous flow can form in blast-type
642 eruptions by PDCs which cross interfluves. Particle velocity vector maps (Fig. 16) augment
643 the maps of particle distributions and compare well to blowdown features in the blast-
644 affected area [Sparks et al., 2002; Baxter et al., 2005], as well as illustrate development of
645 these secondary flows (originating near the summit, flowing to the East in Dry Ghaut). On
646 the other hand, simulation B-3D produced a northward directed PDC lobe, which was able to
647 overtop the summit. This type of PDC was not observed in the natural event, and we
648 attribute the inconsistency mainly to the weak constraint to northerly motion provided by the
649 modeled source topography. Animated results from three oblique views of both 3D models
650 runs display the dynamic evolution of the phenomena mentioned above, and can be viewed
651 on on-line auxiliary material (Movies S4 to S6).

652 In both 3D models (map not shown) high temperatures in the basal part of the currents
653 extended even to the periphery of the PDC, where dynamic pressures were low. This is
654 consistent with field observations that temperatures were high and rapid ignition was a
655 primary source of building damage along the periphery of the affected zone [Baxter et al.,
656 2005].

657

658 **5.2 PDC dynamics**

659 The dynamic pressure, mixture density and mixture velocity at fixed probe locations
660 (shown by dots in Fig. 16) through time show that the dynamic pressure decreases with total
661 mass erupted as in 2D (Fig. 17). For example, consider the dynamic pressure along the flow

662 axis for the two runs at 2.2 km from source (Fig. 17, top two panels, solid lines). Doubling
663 the dome mass more than doubles the dynamic pressure, which can be attributed largely to an
664 increase in PDC density (Fig. 17, middle two panels), and, to a much lesser degree, to
665 changes in PDC velocity (Fig. 17, bottom two panels). This comparison agrees with the 2D
666 calculations which suggest that the dynamic pressure is roughly proportional to the erupted
667 mass and increases largely due to an increase in flow density, rather than to an increase in
668 flow velocity. Dynamic pressure also decreases significantly with distance from source and
669 with distance from the PDC axis towards the flow periphery, again with changes in flow
670 density causing the bulk of the changes in P_{dyn} (Fig. 17). For instance, the dynamic pressure
671 of A-3D at 2.2 km from source along the flow axis is nearly six times the dynamic pressure
672 along the flow periphery at the same distance from source, and is roughly three times the
673 dynamic pressure along the flow axis at 3.2 km (Fig. 17, top left panel).

674 The maximum dynamic pressure recorded at 10 m above the ground, 90 s into
675 simulation A-3D, is mapped in Fig. 18a. The map further illustrates that maximum dynamic
676 pressure decreases steeply with distance from source and with distance from the main and
677 secondary flow axes. The longitudinal (Fig. 18b) and transverse (Fig. 18c) sections show the
678 steep decay in more detail. The maximum dynamic pressure calculated by A-3D near St.
679 Patricks is about ~ 7 kPa, compared to estimates of >25 kPa required for the complete
680 destruction at this axial locality [Sparks et al., 2002; Baxter et al., 2005]. And, for A-3D,
681 peripheral areas experienced slowly-building peak pressures <5 kPa. Therefore, simulation
682 A-3D suggests that dynamic pressures resulting from a collapse of ≤ 5 million cubic meters
683 are probably too small to explain the most severe damage observed. Although these simulated
684 near-ground dynamic pressures could be underestimated by a factor of about two because of
685 the grid size effect (Appendix, Fig. A2), the general conclusion appears to be robust.

686 The maximum dynamic pressure achieved by B-3D near St. Patricks is about 16 kPa
687 (Fig. 18d,e,f). This value underestimates the actual dynamic pressure by a factor of about
688 two because of the grid size effect (Fig. A2), so we conclude that this result is roughly
689 consistent with estimates of >25 kPa based on field observations [Sparks et al., 2002; Baxter
690 et al., 2005]. The much lower dynamic pressures in peripheral areas are also consistent with
691 field-based estimates from damage. Therefore the dynamic pressures calculated for the B-3D
692 case can account for the destruction observed both along the main axis and peripheral areas.

693 A further aspect of dynamic pressure is related to the ability of a PDC to pick up and
694 entrain large rocks, trees, concrete slabs, etc., with these “missiles” themselves having the
695 capability to cause severe damage [Esposti Ongaro et al., 2002; Sparks et al., 2002; Baxter et

696 al., 2005]. Following the analysis by Wills et al. [2002], dealing with missiles transported by
697 heavy winds, in a steadily increasing current the condition for flight of a loose object is,

$$698 \quad P_d C_D > \rho_s L g,$$

699 Where P_d is dynamic pressure, C_D is the drag coefficient, ρ_s is density of the object, L is the
700 characteristic dimension of the object, and g is gravitational acceleration. The maximum size
701 of the object is thus proportional to the dynamic pressure and inversely proportional to
702 density of the object.

703 Applying this relation to the PDC dynamics at St. Patricks, we calculate maximum
704 size L of a loose lava block borne by the PDC. Assuming C_D is approximately one for a bluff
705 body, $P_d = 25$ kPa, and $\rho_s = 2000$ kg m⁻³, yields a maximum block dimension $L = 1.3$ m,
706 which is consistent with the meter-sized blocks observed embedded in heavily impacted
707 houses on Montserrat [Sparks et al., 2002, Fig. 16c].

708 Damage due to such objects can be related to their kinetic energy K , given by

$$709 \quad K = \frac{1}{2} \rho_s V (\vartheta u)^2,$$

710 where V = volume, ϑ = fraction of the current speed attained by an object before impact, u =
711 current speed. Assuming $V = L^3 = (1.3 \text{ m})^3 = 2.2 \text{ m}^3$, $\vartheta = 0.36$ (based on wind-tunnel tests for
712 cubes [Wills et al., 2002]), and $u = 45 \text{ m s}^{-1}$ (sampled at 10 m above ground, Fig. 16), the
713 kinetic energy is about 580,000 J. Since kinetic energies of a few tens of J are sufficient to
714 seriously damage building components [Minor, 1994], such missiles can be considered an
715 important hazard process related to PDC dynamics on Montserrat and elsewhere.

716 We finally note that dynamic pressures calculated for the 3D simulations represent a
717 lower bound for the given volumes, because not all energy was focused directly to the south.
718 For example, if the source boundary were changed to a quarter-sphere (with the same total
719 volume as the hemisphere), with an east-west trending vertical back-boundary, the burst
720 phase would be directed entirely to the south and would likely have been more damaging. We
721 will explore the specific effects of source geometry in a future study.

722

723 **6. Discussion**

724 In general terms, the modeling results presented here have led to several scientific
725 insights about the sudden decompression and subsequent destruction of a lava dome.
726 According to our model results, the directed volcanic blast can reasonably be described by
727 three main phases; the *burst*, *collapse* and *PDC* phases. It appears that dome permeability
728 and source pressure distribution can influence blast characteristics, mostly affecting the burst

729 phase and co-PDC plume development, and asserting lesser influence on asymmetric collapse
730 characteristics and PDC velocity, density, dynamic pressure, and runout distance. On the
731 other hand, total dome mass appears to exert the greatest control on PDC runout and dynamic
732 pressure, which largely determine whether or not an event will be highly destructive.
733 Comparison between 2D and 3D results indicates that topography strongly influences the
734 dynamics of the PDC. For example the 3D results capture the evolution of enigmatic high-
735 concentration mobile dense basal flows in several channels not directly connected with the
736 primary source area [Druitt et al., 2002] and simulate the steep decline in dynamic pressure
737 with lateral distance from PDC axes. From these comparisons, we conclude that 3D
738 modeling with topography is essential for full analysis of directed volcanic blasts, especially
739 for exploring the effects of channeling on the distribution of pyroclastic deposits.

740 Given that the observed damage and deposit characteristics are the primary evidence
741 of the Boxing Day blast characteristics and dynamics, we made broad comparisons between
742 model results and estimates made from field analysis. From these comparisons, we suggest
743 several conclusions specific to the 1997 Boxing Day event at SHV. The 3D simulations
744 generally capture the geometry of the mapped sector of the Boxing Day event, as well as
745 numerous other basic characteristics of the distribution of the eruptive products, including the
746 development of multiple PDC lobes with the highest concentrations occurring along channel
747 axes, and the formation of secondary pyroclastic flows in lateral channels. High-volume
748 simulations (in both 2D and 3D) calculate PDC dynamic pressures consistent with field
749 observations of structural damage, while dynamic pressures associated with low-volume
750 simulations appeared insufficient to explain observations, providing evidence that the
751 observed severe damage was likely caused by high-volume pulses, rather than low-volume
752 pulses. A systematic decrease in peak PDC dynamic pressure with distance from source and
753 from lobe axes was also reproduced, in accordance with the observed damage. Modeled
754 temperatures are high over the extended region of the PDC even at the periphery where
755 dynamic pressures were low, consistent with ignition being the major source of observed
756 damage in those areas [Baxter et al., 2005]. The relatively sharp rise in dynamic pressure at
757 St Patricks ($R = \sim 3.4$ km; $t = \sim 50$ s) suggests average 2D model speeds of $53\text{-}63$ m s⁻¹. These
758 average speeds are reasonably consistent with estimates of $38\text{-}56$ m s⁻¹ inferred by assuming
759 that the first seismic pulse destroyed seismic station MSPT, but are roughly half of the
760 velocity estimated by assuming that the second seismic pulse destroyed the station,
761 supporting the hypothesis that the first pulse destroyed the station. These comparisons
762 suggest that the model presented here, along with its simplifying assumptions, captured the

763 essence of the large-scale dynamics of the lateral blast at SHV, and could be useful for
764 understanding hazards associated with blasts in general.

765 For the 1980 Mount St Helens blast, Kieffer [1981, 1984] developed the hypothesis
766 that the most severe zone of damage could be explained by supersonic flow (Mach number
767 >3) within a shock wave-constrained flow field. Kieffer also proposed that the boundary
768 between the ‘direct blast zone’ and the ‘channelized blast zone’ north of the vent
769 corresponded to a transition from supersonic to subsonic flow marked by a Mach disk shock
770 at ~ 11 km from source. Wohletz [1998], for the MSH blast specifically, calculated leading
771 shock wave overpressures of 40 kPa and dynamic pressures of 1 kPa at 10 km using the full
772 thermal energy (7 Mt) released during lateral propagation of the blast, and assuming that the
773 energy release time and empirical relations were similar to surges driven by a surface nuclear
774 explosion [Glasstone and Dolan, 1977]. We discuss supersonic flow and shock waves below
775 within the context of the Boxing Day event on Montserrat.

776 Under the assumption of mechanical equilibrium between the phases, no heat transfer
777 between them, and no compressibility effects in the solid phases, the sound speed in a
778 multiphase gas-particle mixture can be computed by the formula:

$$779 \quad c = \left(\frac{\gamma_g RT_g}{Y} \right)^{\frac{1}{2}} \left(Y + (1-Y) \frac{\rho_g}{\rho_s} \right)$$

780 where Y is the mass fraction of gas in the multiphase mixture, ρ_g and ρ_s are the gas and solid
781 densities, T_g is the gas temperature, γ_g is the ratio of specific heats for the gas phase, and R is
782 the perfect gas constant [Wallis, 1969; Dobran et al., 1993, Gidaspow, 1994]. Depending on
783 the transformation, γ_g can be equal to 1.4 (adiabatic expansion of gas) or 1 (isothermal
784 expansion). Due to the multiparticle nature of the mixture and therefore to the different
785 degrees of equilibrium between gas and particles we tested both adiabatic and isothermal
786 conditions. Nevertheless, the large exchange area between gas and particles, together with
787 the high concentration of solids at the base of the PDC, favor (as shown by simulation
788 results) an isothermal expansion. Therefore we prefer the value $\gamma_g = 1$. Moreover, as a first-
789 order estimate, we did not include a slip velocity correction due to its relatively small value
790 compared to the horizontal flow speed. The above equation has been validated by Gidaspow
791 and Driscoll [2007] by showing it appropriately describes the propagation of pressure waves
792 through a fluidized bed over a wide range of void fractions. According to it, the sound speed
793 of the mixture decreases with increasing particle volume fraction until a minimum is reached

794 at a void fraction of 0.5. Similar estimates of the sound speed of the eruptive mixture can be
795 obtained by using the pseudogas approximation; for instance Kieffer [1981] assumed $\gamma_{\text{mix}} =$
796 1.04 and obtains soundspeed values within a difference of few percent of our values. The
797 associated Mach number is defined as $M = \frac{\sqrt{u_m^2 + v_m^2}}{c}$, where u_m and v_m are the mixture
798 horizontal and vertical velocity components, respectively. Because the sound speed can be
799 quite low in our gas-particle mixtures, we now explore the Mach numbers in C-2D and B-2D,
800 the simulations most likely to exhibit supersonic flow. Simulation C-2D has the highest burst
801 velocities, whereas B-2D exhibits the highest PDC velocities and has the lowest mixture
802 sound speeds due to high particle concentration. Figures 19 shows Mach number contours for
803 these two simulations.

804 For B-2D, the transformation from the burst phase to collapsing stream occurs in the
805 first few seconds and the transformation from collapse phase to PDC phase is largely
806 complete by 10 s (Fig. 19a). The PDC displays a local supersonic basal region, enhanced by
807 topography. For instance at 30 s (Fig. 19b), isolated regions with $M > 1.6$ occur in front of
808 local steep areas that promoted acceleration. By 50 s (Fig. 19c), $M > 1$ occurs in a thin basal
809 zone limited to 1.6 - 2.3 km from source, whereas the PDC has spread to 3.6 km, and
810 dynamic pressures >15 kPa (and rising) already occur in the subsonic region at 3 km (see Fig.
811 11 above).

812 C-2D shows the development of a concentric region of supersonic flow at 1 s in the
813 burst phase (not shown), grading to a broader and gradually less concentric region of
814 supersonic flow (with $M > 2$) in the laterally-directed collapsing stream (Fig. 19d at 10s). By
815 30 s the flow is subsonic nearly everywhere, except a very narrow region ($R \sim 1$ km) where M
816 > 1 in the PDC body (Fig. 19e). At later stages the flow Mach number decreases due to
817 deceleration. At 50s (Fig. 19f) the maximum Mach number is roughly 0.8 at 3-4 km from the
818 source.

819 The distribution of the mixture Mach number (over the dispersal sector at 10 m above
820 the ground) is shown for simulation B-3D at 50s (Figure 20). The mixture sound speed is
821 computed from the same relation used above, and ranges from 40 m s^{-1} at the base of the
822 PDC (where the particle concentration is the highest) to about 400 m s^{-1} in the dilute ash-
823 cloud, where the ash concentration is low but the temperature is still high. Maximum Mach
824 number of approximately 1.0 occurs in a small patch along the main channel, where the
825 velocity and the flow density are the highest, but apart from this the PDC is internally

826 subsonic. Along longitudinal (Fig. 20b) and transverse sections (Fig. 20c), the distribution of
827 the Mach number is very similar to that observed in 2D, with the highest values occurring in
828 the basal layer of the PDC. The Mach numbers in run A-3D (not shown) are everywhere
829 subsonic, suggesting that in the simulated events, supersonic effects are of very local
830 occurrence and of minor importance. To summarize, our model results suggest that the flow
831 is only locally supersonic (in correspondence with the regions with high particle
832 concentrations) and strongly transient, so that we can reasonably exclude any important effect
833 due to strong, persistent internal shock waves, beyond the burst phase and region (up to 2 s
834 after onset and distances < 1 km).

835 For the 1980 Mount St. Helens blast, it was hypothesized that an overpressured jet
836 horizontally emanated from a vent, resulting in a strong (Mach disc) shock normal to the blast
837 direction [Kieffer, 1981]. In such an underexpanded jet, the flow accelerates due to the
838 decompression and is supersonic in an extended region between the vent and the shock.
839 Based on our Montserrat simulations, we cannot exclude the possibility that increasing the
840 scale (total mass and energy) of the eruption to the size of the MSH blast could lead to the
841 formation of a short-lived overpressured jet. Nevertheless, according to the simulations
842 presented here, the strongly transient behavior of a blast and the generally low Mach numbers
843 in the corresponding PDC make us skeptical that a supersonic, underexpanded quasi-steady
844 horizontal jet of wide extent existed during the Boxing Day event.

845 The severe damage at St. Patricks appears to have been caused by the high dynamic
846 pressure of subsonic PDCs (>25 kPa), and impacts of large missiles (also related to dynamic
847 pressure), rather than by shock waves associated with supersonic flow, given that calculated
848 Mach number never exceeds unity in the region of damage. The existence of local regions of
849 $M > 1$ implies that perturbations of the flow pressure (e.g., due to sudden changes in the
850 topographic profile) can generate internal shock waves. Nevertheless, no discontinuities
851 were calculated in these model runs at the mesh scale (a recent application of the PDAC code
852 to the simulation of the shock wave propagation in supersonic volcanic jets [Esposti Ongaro
853 et al., 2006] has demonstrated that the code is able to accurately capture the flow
854 discontinuities in the compressible regimes even using a relatively coarse mesh of more than
855 10 m). This conclusion, however, does not exclude the possibility of localized generation of
856 internal shock waves in isolated regions, or of damage by supersonic flow in the very
857 proximal area. We also note that with some alternative source conditions, the burst phase
858 could be more focused to the south.

859

860 **7. Conclusions**

861 Based on our model simulations we are able to separate the transient directed-blast at
862 SHV into three main parts, the *burst phase*, the *collapse phase*, and the *PDC phase*. In the
863 burst phase, the pressurized mixture is driven by kinetic energy of the gas phase, expanding
864 rapidly into the atmosphere, with much of the expansion having an initial lateral component
865 because of the geometry of the pressure release surface. The erupted material fails to mix
866 with sufficient air to form a buoyant column and thus, in the collapse phase, falls beyond the
867 source as a stream of gas and pyroclasts. The material then moves parallel to the ground
868 surface as a density current in the mainly subsonic PDC phase. Local supersonic flow is
869 possible in the PDC phase, but it likely results from high mixture density, rather than
870 extremely high velocities. This idealization of directed blasts contrasts with some previous
871 models (Kieffer, 1981, 1984; Wohletz, 1998].

872 Our modeling results also indicate that the total mass in the PDC has great control on
873 inertia and runout, and can largely determine whether or not an event will be highly
874 destructive. Further, source permeability and source pressure distribution can strongly
875 influence burst-phase characteristics and co-PDC plume development, but affects only minor
876 control over asymmetric fountain characteristics and PDC propagation. Topography strongly
877 influences the dynamics of PDC evolution, and only 3D models incorporating 3D topography
878 can capture the effects of channeling on the distribution of PDC deposits. Despite the
879 complexity of the phenomena, our simulation results were consistent with field observations
880 of depositional features, structural damage, and damage due to fires ignited by the pyroclastic
881 event. In particular our calculations suggest that the severe damage observed in the St
882 Patricks area on Montserrat can reasonably be explained by high dynamic pressures and
883 missile impact loading within subsonic PDCs generated by high-volume pulses.

884

885 **Appendix**

886 **Numerical resolution on rectilinear meshes**

887

888 The PDAC code solves the multiphase transport equations on a rectilinear mesh in 2D
889 (cylindrical or Cartesian) and 3D (Cartesian) [Esposti Ongaro et al., 2007; Neri et al., 2007].
890 The discretization schemes adopted in the PDAC code are accurate to the second order in a
891 Taylor expansion on a uniform mesh. In the simulations performed we adopted non-uniform
892 meshes in order to reduce the number of cells and, consequently, the execution time of each
893 run. The use of a non-uniform mesh allowed us to increase the resolution in the regions near

894 the source and the ground, i.e. in the regions where we observe the largest gradients in the
895 flow variables. In 2D, the computational domain extended 10 km horizontally and 8 km
896 vertically and was discretized into 400×200 computational elements. The horizontal mesh
897 size was uniform in the first 600 m with a resolution of 20 m, then increased radially up to
898 100 m at 6 km and then was left constant at 100 m up to 10 km. Vertically, the mesh size was
899 uniform in the first 1500 m with a resolution of 10 m, then was increased gradually up to 60
900 m. In 3D, the computational domain was extended over a 9 km × 9 km area and up to 6 km
901 vertically and was discretized into 128×128×100 cells. In this case, we adopted a horizontal
902 resolution of 20 m, in a box of 500 m enclosing the source, and increased this gradually to
903 100 m beyond the 500-m boundaries. The vertical mesh resolution was uniform at 20 m for
904 the first 800 m, and then increased up to 200 m. To reduce the numerical error, in both 2D
905 and 3D, we limited the radial cell-size increase rate to 1.05, as is the common practice in
906 numerical modeling. The numerical error strongly depends on the diffusion properties of the
907 numerical scheme adopted and also on the flow Reynolds number. We therefore performed
908 several sensitivity tests to evaluate the effects of the horizontal mesh non-uniformity and
909 vertical mesh resolution on the numerical solutions.

910 Figure A1 presents the isocontours from -8 to -1 of the \log_{10} of the total particle
911 volumetric fraction in the atmosphere at 90 and 180 s for simulation A-2D and for various
912 computational meshes, both uniform and non-uniform. The results show a minor effect of the
913 mesh features on the large-scale dynamics of the PDC propagation. In particular, the effect of
914 the horizontal cell stretching is negligible at 90 s (Figure A1, a and b), when the flow is
915 almost entirely in the uniform region of the computational domain. At 180 s (Figure A1, e
916 and f) some difference in the PDC runout can be observed, due to the different horizontal
917 resolution (20 m vs. 100 m). The effect of the vertical resolution on the large-scale
918 propagation of PDCs is also quite limited, as demonstrated by comparing the runout of PDCs
919 at 90 s with a mesh of 6, 10, and 20 m (Figure A1, c, b, and d). At 180 s the difference is
920 slightly more pronounced but still within a 10% tolerance. Similar results were obtained and
921 discussed by Dobran et al. [1993] and Neri et al. [2003]. Similarly, in 3D, the comparison
922 between maps of the total particle volumetric concentration at 90 s obtained with a uniform
923 (50 m) and non-uniform (20-100 m) horizontal discretization (not shown) confirms the
924 relatively minor effect of cell stretching on the solutions of explosion dynamics.

925 Because PDCs show strong vertical density and velocity gradients close to the
926 ground, the influence of the vertical mesh resolution on dynamic pressure is more significant
927 at the base of the flow. As a consequence, flow sedimentation and stratification computed by

928 the model significantly depends on grid size, as already noted in multiparticle simulations by
929 Neri et al. [2003]. For example, Figure A2 shows the influence of mesh size on vertical
930 profiles of mixture density, velocity, and dynamic pressure for the PDC of simulation A-2D.
931 From the plots one can see that the solutions begin to converge on a single solution as vertical
932 grid size decreases (compare the change from the 20 m to 10 m grid to the change from the
933 10 m to 6 m grid). Generally speaking the smallest grid spacing, in this case 6 m, produces
934 the most accurate solution. Results obtained with the 6 and 10 m meshes produce similar
935 solutions and flow gradients. In detail, they produce similar velocity profiles with maxima
936 about 50-60 m above the ground (Fig. A2, b and e), and nearly identical density profiles (Fig.
937 A2, a and d). The resulting peak in dynamic pressure is approximately 20-30 m above the
938 ground (Fig. A2 c and f). The similarity between the solutions on the 6 m and 10 m grids
939 suggests that a resolution of 10 m is adequate to quantitatively describe the primary flow
940 features. On the other hand, the solutions on the 20 m mesh significantly underestimate the
941 maximum value of dynamic pressure (relative to the 6 m grid) and do not capture patterns
942 close to the ground. Unfortunately, a 10 m mesh resolution is difficult to achieve in 3D
943 simulations, because of the substantial increase in the total number of computational elements
944 and associated computing time, and therefore a 20 m minimum grid size was adopted in our
945 main 3D simulations. This choice does not significantly affect the large-scale dynamics of the
946 explosion and PDC propagation (see Figure A1 above and similar analyses reported in Neri et
947 al., 2003), but likely underestimates the PDC dynamic pressure by roughly a factor of two
948 (Fig. A2c,f). Our results show that the dynamic pressure profile of the PDC is characterized,
949 at least under the conditions considered in our simulations, by a sharp gradient from the
950 ground to its maximum value at approximately 20-30 m above the surface. As a consequence,
951 the estimate of dynamic pressure at 10 m above ground or lower may be subject to
952 considerable uncertainty, due to the grid size effect and also the complex effect of the ground
953 boundary condition on the flow behavior [Dufek and Bergantz, 2007].

954 Finally, it should be noted that mesh resolution also affects the accuracy of the
955 topographic description. To reduce errors associated with inaccurate descriptions of
956 topography we adopted a new immersed-boundary technique [De' Michieli Vitturi et al.,
957 2007] suited to compressible multiphase flows in order to accurately describe, even with the
958 relatively coarse mesh adopted, the no-slip condition at the interface between the fluid and
959 the irregular 2D and 3D topography.

960

961 The computational grids used to date included up to 300 thousand cells in 2D and 2.5 million
962 cells in 3D and required the challenging solution of several billions of algebraic equations.
963 The parallelization strategy that allowed such an accomplishment was based on the
964 decomposition of the domain among the computational processors by adapting the numerical
965 solution algorithm to the parallel environment [Esposti Ongaro et al. 2007]. A parallel
966 communications layer based on the Message Passing Interface (MPI) protocol and a friendly
967 input/output interface make the new PDAC code portable on most parallel (shared- and
968 distributed-memory) architectures and transparent to the programmers and the users. The new
969 code is thus able to exploit the peak performance of large supercomputers and workstation
970 clusters. In detail the code was run on a Linux cluster with 66 AMD Opteron CPUs at 1 GHz
971 and 52 GB RAM, interconnected with a low-latency Myrinet network. On this machine, 3D
972 runs took about 2500 total CPU hours.

973

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982

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Table captions

Table 1. List of the main parameters used in 2D and 3D simulations. κ is the porous dome permeability, V_{DRE} is the Dense Rock Equivalent volume of the dome, R_d is the resulting dome radius, M is the solid mass in the dome, α the porosity (void fraction) and E is the expansion energy per unit mass assuming an adiabatic or isothermal expansion (see text). The total mass in the 2D runs is multiplied by a factor accounting for the asymmetric distribution of the deposit over a sector of 70° .

Table 2. List of the main simulation outputs from 2D simulations. H_b is the maximum burst height above the dome (see Figs. 3, 5, 7), $U_{b,g}$ is the gas *burst* velocity, $U_{b,p}$ is the three particles *burst* velocity, U_f is the average velocity of the PDC after collapse, T_p is the time at which the phoenix cloud form from the PDC front, E is the percentage of pyroclasts elutriated at the final simulation time, $R_{m_{max}}$, $U_{m_{max}}$, Pd_{max} are the maximum mixture density, velocity and dynamic pressure at 10m and 2, 3 and 4 km from the vent (see Fig. 11), Pd_{SP} is the maximum dynamic pressure at St. Patrick village ($R=3.4$ km, see Fig. 12).

Figure captions

Figure 1. The area affected by the 1997 Boxing Day lateral blast on Montserrat, view from south. a) before: foreground, St. Patricks village (left) and White River valley; background, SHV. b) after, showing debris avalanche deposit in and near the valley, and widespread blanket of PDC deposits over 70° sector. St. Patricks at lower left is completely destroyed.

Figure 2. Distribution of 1997 Boxing Day deposits (from Sparks et al., 2002). A-A' marks the profile used in 2D runs A, B & C.

Figure 3. a) Initial expansion of 2D simulation A-2D ($V_{DRE} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). Contours are \log_{10} of particle volume fraction. Initial condition, 2 s, 5 s and 12 s into simulation. By 12s the plume exhibits the collapse phase. b) Trajectories of fluid particles from 0 to 15s defining the burst phase and collapse phase of eruption.

Figure 4. Simulation A-2D ($V_{DRE} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). Contours are \log_{10} of particle volume fraction (color map as in Fig. 3a). At 10s the burst phase has ceased and the PDC moves along the volcanic slope. At 20s the PDC head forms by the effect of the air entrainment at 1.5 km. At 40s in the PDC phase, the leading edge has thickened and most of the solid mass has entered the PDC. By 90s the PDC has progressed beyond the shoreline and further thickening of the leading edge is evident. By 180 s the PDC has reached 8 km and segregated fines are forming a co-PDC plume, with minor plumes at the trailing edge. At 240s, co-PDC plumes are well-developed and vertical motion dominates. Animated contours can be viewed on Movie S1 in the on-line auxiliary material.

Fig 5. a) Initial expansion of simulation B-2D ($V_{DRE} = 10 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). Contours are \log_{10} of particle volume fraction. Initial condition, 2 s, 5 s and 12 s into simulation. By 12s the plume exhibits the collapse phase. b) Trajectories of the fluid particles from 0 to 15s, defining the burst phase and collapse phase of eruption. The initial phase is not greatly affected by total mass (compare to Fig. 3a and 3b).

Figure 6. Results of B-2D ($V_{DRE} = 10 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). Contours are \log_{10} of particle volume fraction (color map as in Fig. 5a). From 0 to 40s the dynamics is similar to A-2D, but the PDC front is more advanced. At 40s in the PDC phase, the leading edge has thickened. By 90 s the

PDC has progressed well beyond the shoreline with further thickening and broadening of the leading front. At 180s the increased dome mass and inertia results in high-speed runout beyond the computational limit of 8 km (PDC motion continues). Deposition is offshore. Buoyant co-PDC plumes are in the early stages of development. Animated contours can be viewed on Movie S2 in the on-line auxiliary material.

Figure 7. a) Initial expansion of 2D simulation C-2D ($V_{DRE} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-14} \text{ m}^2$). Contours are \log_{10} of particle volume fraction. Initial condition, 2 s, 5 s and 12 s into simulation. The initial phase is strongly affected by initial total specific gas energy (compare Fig. 3). b) Trajectories of fluid particles from 0 to 10s, defining the burst phase and collapse phase of eruption (please notice the change in the axis scale with respect to Figs. 3b) and 5b).

Figure 8. Pressure perturbation at ground level and different radial distances (from 1 to 3.5 km) produced by the exploding dome in simulation C-2D.

Figure 9. Results of C-2D ($V_{DRE} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-14} \text{ m}^2$). Contours are \log_{10} of particle volume fraction (color map as in Fig. 5a). At 10s the pyroclastic material is expanding in the atmosphere (burst phase) by the effect of the high initial gas overpressure. At 20s the erupting material is collapsing to the ground forming a PDC. At 40s in the PDC phase, the leading edge has thickened. By 90 s the PDC has progressed past the shoreline with further thickening and broadening of the leading front. By 180 s the PDC has passed 6 km but has stalled and segregated fines are forming a co-PDC plume, with minor plumes at the trailing edge. At 240s, co-PDC plumes are well-developed onshore and vertical motion dominates. Animated contours can be viewed on Movie S3 in the on-line auxiliary material.

Figure 10. a) Front position versus time, and b) Front velocity versus position of simulations A-2D (solid line), B-2D (dashed) and C-2D (dotted). The front is tracked by following the most advanced part of the flow, irrespective of its shape (expanded flow head or thin basal flow).

Figure 11. Time-wise variation of the mixture density (top), mixture velocity (middle) and flow dynamic pressure (bottom) at 2 km (red), 3 km (green) and 4 km (blue) from the source. Values are sampled 10m above the ground level. Plots on the left are results from an erupted mass of $V_{DRE} = 5$

$\times 10^6 \text{ m}^3$ and different dome permeabilities (A-2D: 10^{-12} m^2 - solid line; C-2D: 10^{-14} m^2 - dashed line). Plots on right are results from a higher erupted mass: B-2D ($V_{\text{DRE}} = 10 \times 10^6 \text{ m}^3$) and high dome permeability (10^{-12} m^2).

Figure 12. Flow dynamic properties at St Patricks, 3.4 km from source, resulting from simulations A-2D (solid line), B-2D (dashed) and C-2D (dotted). a) Time-wise variation of the flow dynamic pressure. Values are sampled 10m above the ground level. b) Vertical flow profile at the time of maximum dynamic pressure reported in the legend.

Figure 13. Isocontours [-8:0:-1] of the Log_{10} of the total particle fraction at $t=0\text{s}$, $t=5\text{s}$ and $t=10\text{s}$ across a vertical section parallel to the Y axis in 3D simulations [$X=80700$]. The dark solid contour indicates the initial volume of the exploding dome at [$X=80690\text{m}$; $Y=46550\text{m}$; $Z=710\text{m}$]. A) Simulation A-3D ($V_{\text{DRE}} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$); B) B-3D ($V_{\text{DRE}} = 11 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). The sequences can be compared with those in 2D in Fig. 3 and 5 (but the initial position of the dome is somewhat different; see text).

Figure 14. Temporal evolution of 3D pyroclastic dispersal process at 30, 60 and 90s. View from South on 20-m grid DEM. The isosurfaces correspond to the total particle concentrations of 10^{-6} (outer, light brown) and 10^{-2} (inner dark) a) Simulation A-3D ($V_{\text{DRE}} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$); b) Simulation B-3D ($V_{\text{DRE}} = 11 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). Animated contours can be viewed on Movie S4 to S6 in the on-line auxiliary material.

Figure 15. Left panels: Simulation A-3D ($V_{\text{DRE}} = 5 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$); Right panels: Simulation B-3D ($V_{\text{DRE}} = 11 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). a,d) Map of the log_{10} of total particle concentration at 10m above ground (the basal cell) at 90 s. Note channelized flow to the east, in Dry Ghaut, which was also recognized in the field. The bold line indicates the boundary of the debris avalanche and blast deposits. b,e) Longitudinal LL' section of the log_{10} of total particle concentration along the flow direction (seen from NW). c-f) Transversal PP' section (seen from NE).

Contours are log_{10} of particle volume fraction. Please note that the color scale is different in the maps from the sections to highlight the weaker variations in the spatial distribution of pyroclasts.

Figure 16 Maps of particle velocity vectors at 90s for simulations A-3D (a) and B-3D (b).

Values are sampled at 10 m above ground level (the basal cell). Points p1-p4 indicates the probe positions for the sampling of Fig. 20 and correspond to central (p1,p3) and peripheral (p2,p4) locations.

Figure 17. Dynamic pressure, mixture density and mixture velocity at 10m above the ground surface at selected locations marked by the dots in Fig. 18. Left) A-3D, Right) B-3D. The value of the maximum dynamic pressure (corresponding to the passage of the PDC head) drastically decreases in moving away from the source, and also from the flow axial region to the flow periphery.

Figure 18. Comparison between the *maximum* dynamic pressure of simulation A-3D (left plots) and B-3D (right plots). a-d) Map view at 10 m above ground surface in the basal cell at 90 s (dome positioned at [X=80690m;Y=46550m;Z=710m]). Solid lines mark longitudinal and transverse sections; b-e) Longitudinal section topography (green) and corresponding simulated maximum dynamic pressure (blue). Please notice that the longitudinal section does NOT correspond to the flow direction or to the steepest slope (see the map). The maximum value of the dynamic pressure drastically decreases with the distance from the source; c-f) Transverse section topography (green) and corresponding simulated maximum dynamic pressure (blue). Peaks in maximum dynamic pressure correspond to deep valleys where particles tend to concentrate, providing evidence that lateral peaks in maximum dynamic pressure are controlled by flow density, rather than flow velocity. The maximum value of the flow dynamic pressure in B-3D is almost double with respect to A-3D due to the increase of the erupting mass.

Figure 19. Mach number distributions for 2D simulations of volcanic blast at Soufrière Hills volcano; Isocontours are traced every 0.2. Maximum values are saturated in red above $M=2.0$, so that the green color corresponds to $M\sim 1$ (sonic velocity, white isoline). a-b-c) Simulation B-2D ($V_{DRE} = 10 \times 10^6 \text{ m}^3$, $K=10^{-12} \text{ m}^2$). The collapse phase ($t=10\text{s}$) is characterized by relatively high Mach number ($M>2$) in a proximal region ($R = 500\text{-}800 \text{ m}$). High values of the Mach number at 30s correspond to regions at high particle concentration, rather than high velocity. The region affected by locally supersonic flow is limited to $R<2.5 \text{ km}$ and $t = 50\text{s}$. d-e-f) Simulation C-2D ($V_{DRE} = 5 \times 10^6 \text{ m}^3$, $K=10^{-14} \text{ m}^2$). Collapse phase shown at 10 s, with transformation to PDC phase nearly complete by 20 s (not shown). Further movement shows thickening and distortion of PDC front edge by air drag. By 30 s, the region for $M>1$ is limited to a

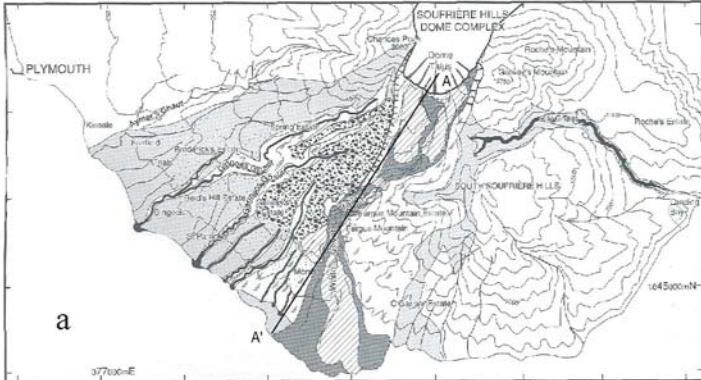
thin basal patch ~ 1.5 km from source. By 50 s, with the plume front at the site of destroyed houses (3.4 km), the basal zone of the PDC displays $M < 0.8$, but with high dynamic pressure.

Figure 20. a) Map of the distribution of mixture Mach number at 50s, and at 10m above the ground level, for simulation B-3D ($V_{DRE} = 11 \times 10^6 \text{ m}^3$, $K = 10^{-12} \text{ m}^2$). b) Longitudinal section LL' and c) transversal section PP' of the Mach number distribution. Isocontours are shown for every 0.2 change. Maximum value observed is about $M \sim 1.0$, comparable with that observed in 2D (Fig. 19).

Figure A1. Influence of the mesh size and stretching on the large-scale PDC dynamics at 90s (left plots) and 180s (right plots). Isolines represent the \log_{10} of the total particle volumetric fraction from -8 to -1. a,e) Reference simulation A-2D: dx varies from 20 to 100m, vertical minimum size is $dz=10\text{m}$ (total number of cells $N_t = 8 \times 10^4$). b,f) Uniform horizontal resolution of 20m, vertical minimum size is $dz=10\text{m}$ ($N_t = 2 \times 10^5$). c,g) Uniform horizontal resolution of 20m, vertical minimum size is $dz=6\text{m}$ ($N_t = 3 \times 10^5$). d,h) Uniform horizontal resolution of 20m, vertical minimum size is $dz=20\text{m}$ ($N_t = 1.5 \times 10^5$).

Figure A2. Influence of the vertical mesh size on the PDC density (a,d), velocity (b,e) and dynamic pressure (c,f) profiles. a, b, and c is at 90 s and 3 km from source; d, e and f is at 90s and 4 km from source. The vertical resolution plotted are 6 m (solid line), 10 m (dashed line), and 20 m (dotted line), with a uniform horizontal resolution of 20 m. The ordinates report the height above the topography in meters (the ground elevation is 161 m at 3 km and 0 m at 4 km).





Extent of the Deposits

Valley-confined Facies:

Block-poor deposits
(Surge-derived pyroclastic flow)

Block-rich deposits

Unconfined Facies:

Unit I
 Layers 1 & 2
(1st pulse)

Unit II
 Layers 1 & 2
(2nd pulse)
(dots represent presence of layer 1 only)

LEGEND

Debris avalanche deposits

0 1km



Topographic Features:

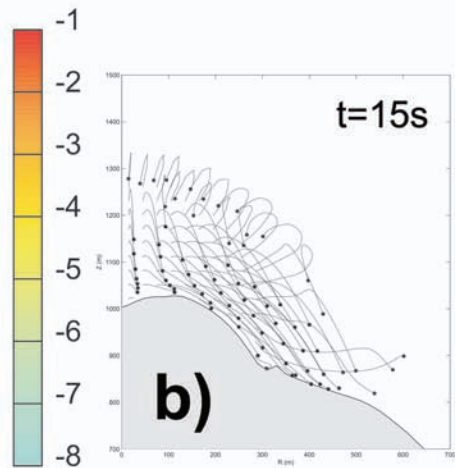
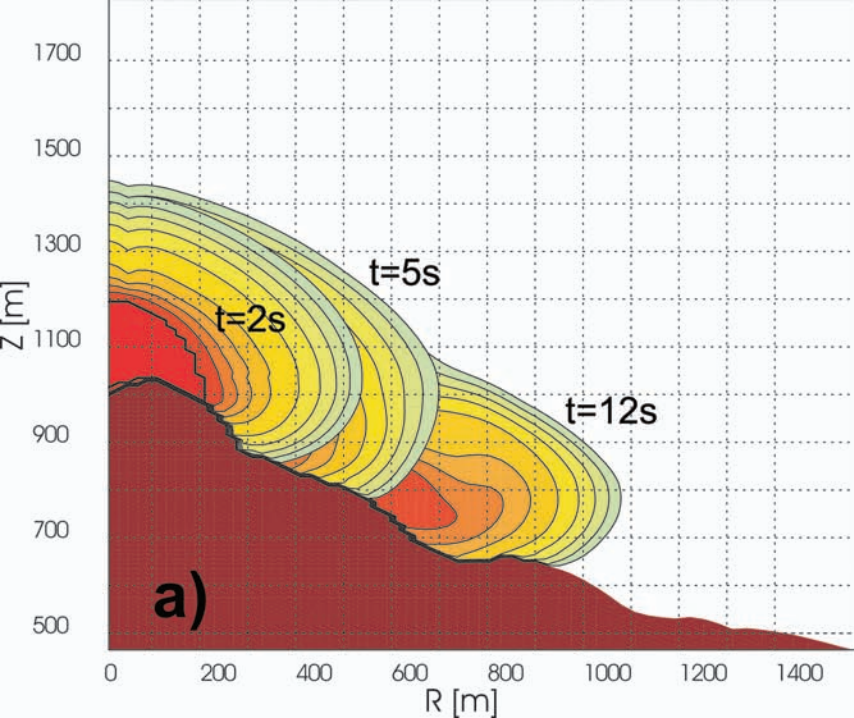
Steep valley sides

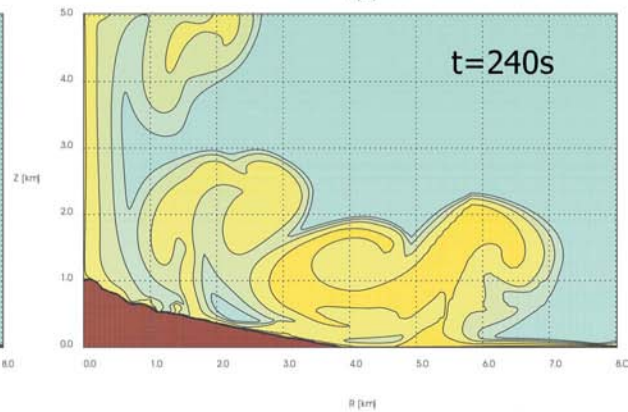
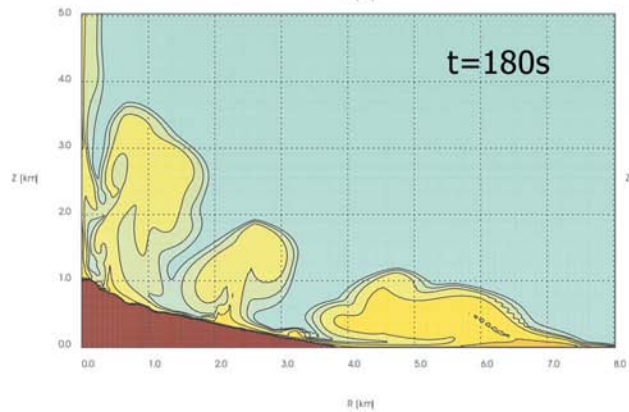
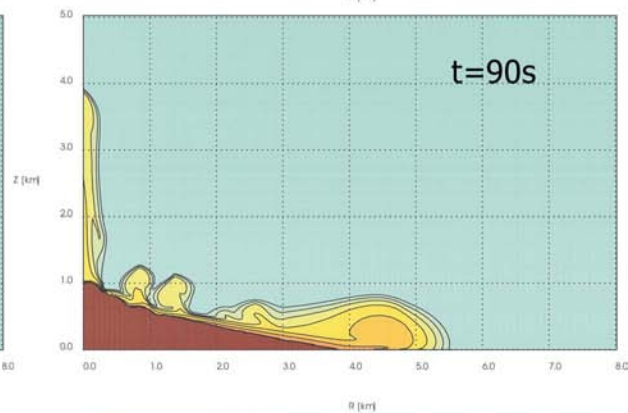
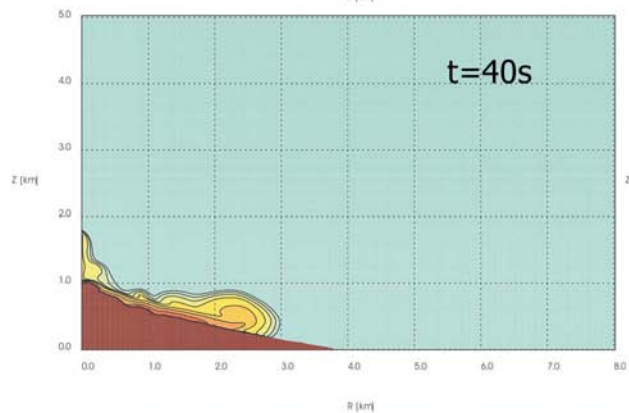
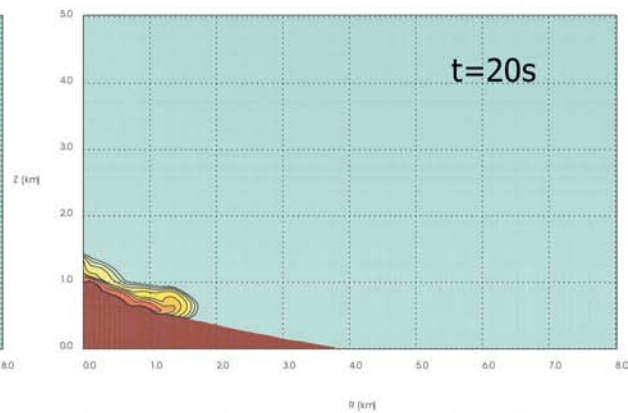
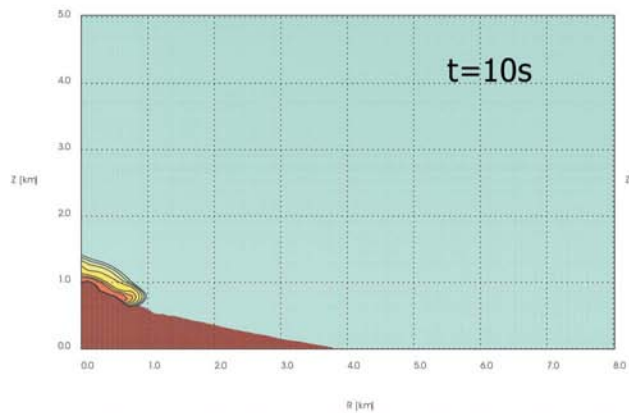
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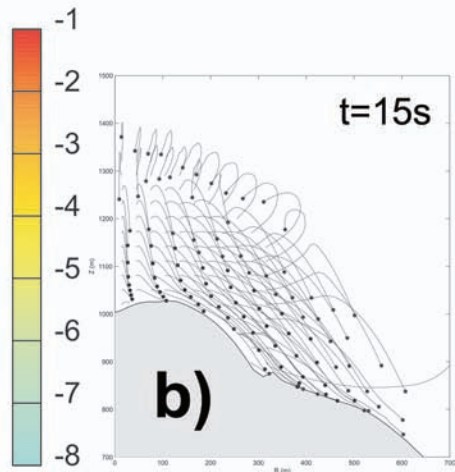
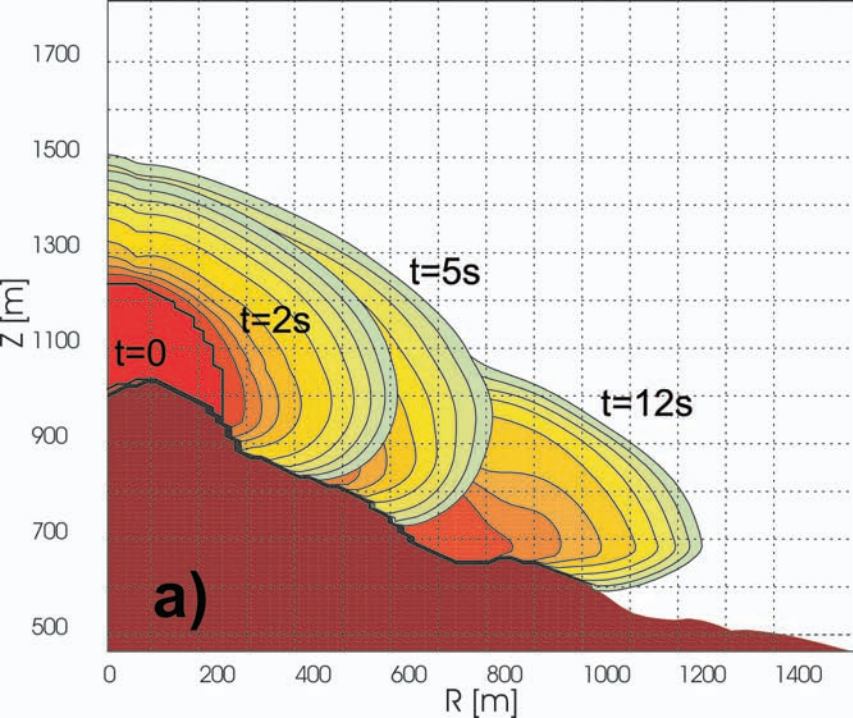
Come talus slope

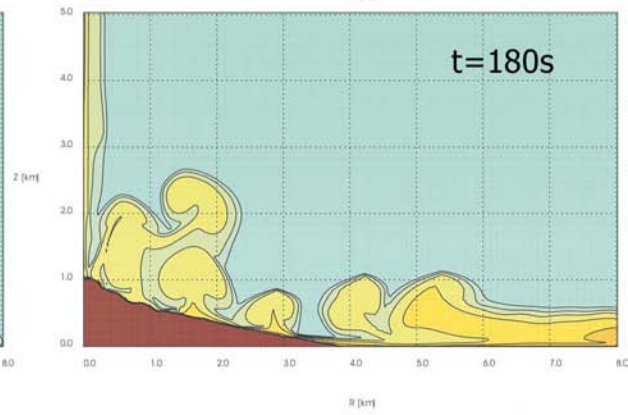
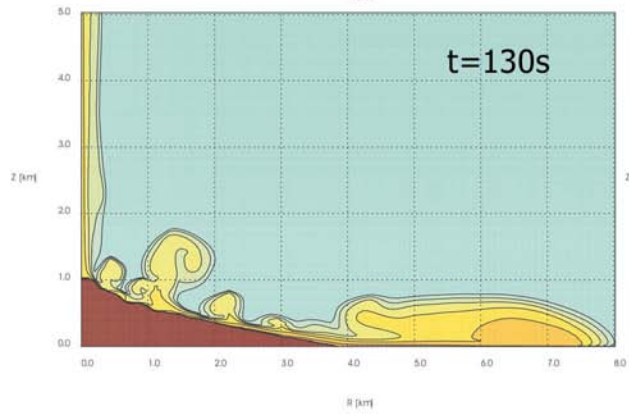
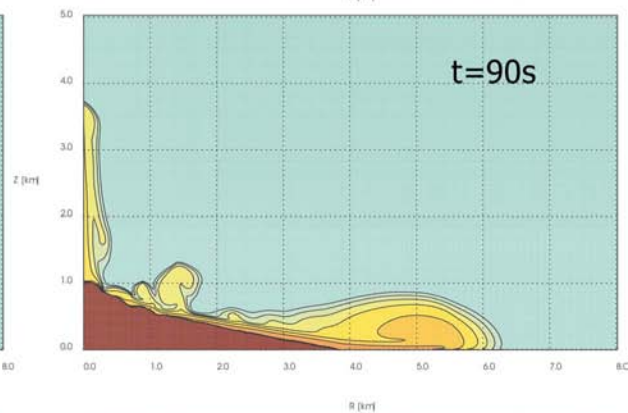
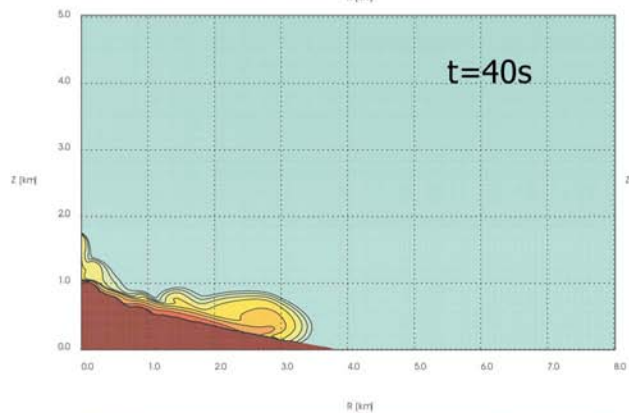
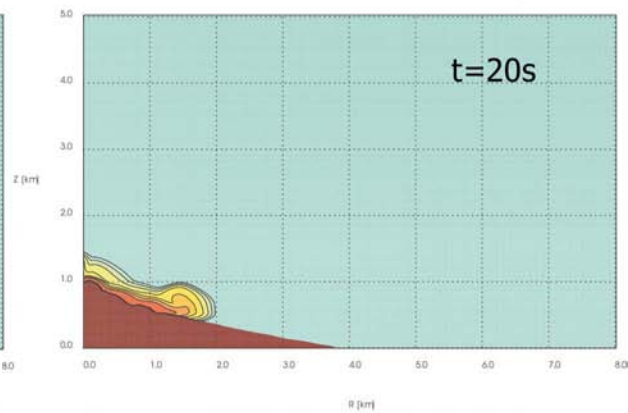
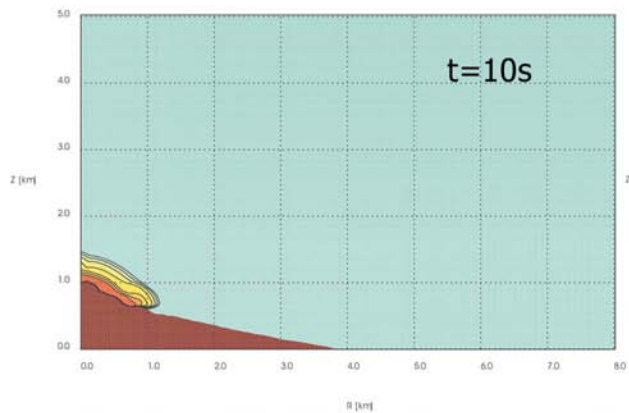
Contours and heights in feet
(0.3048 m)

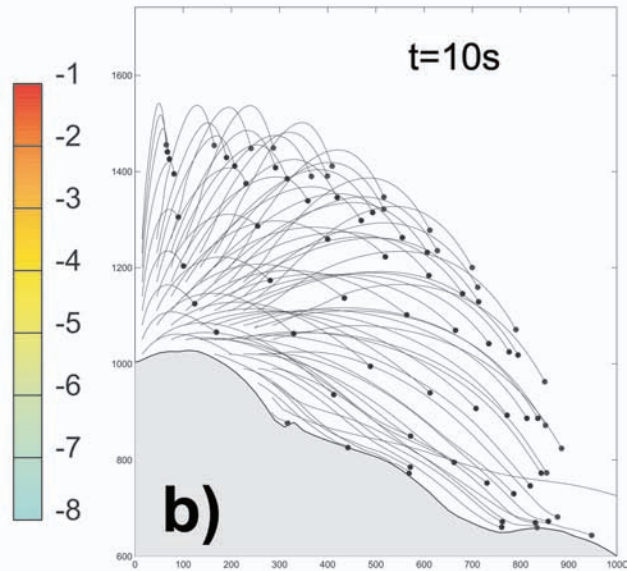
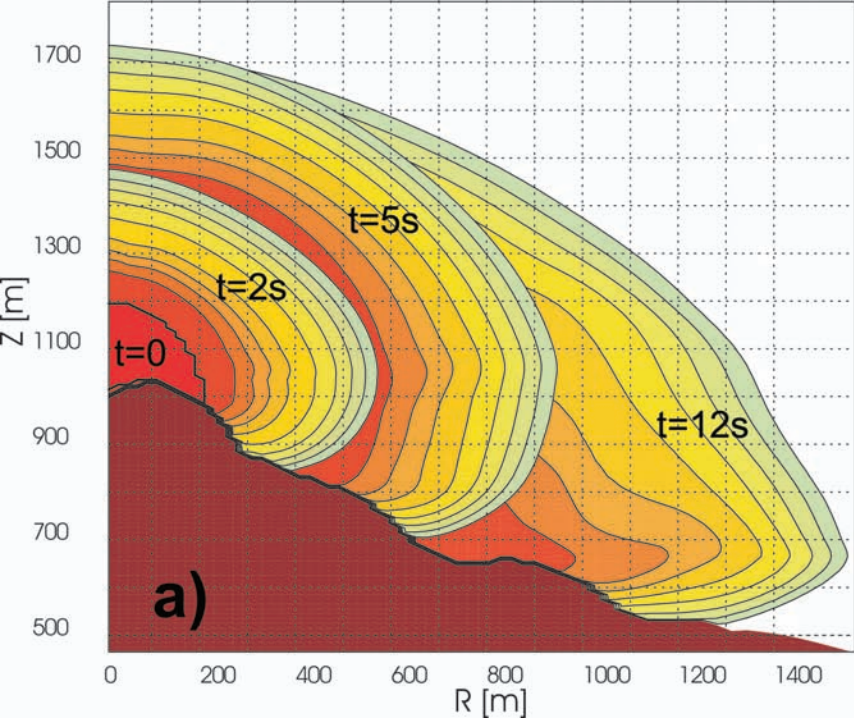
River

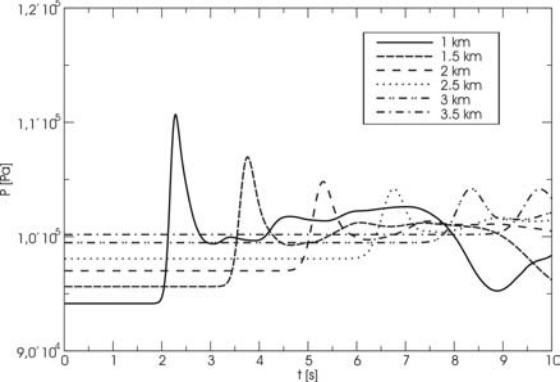


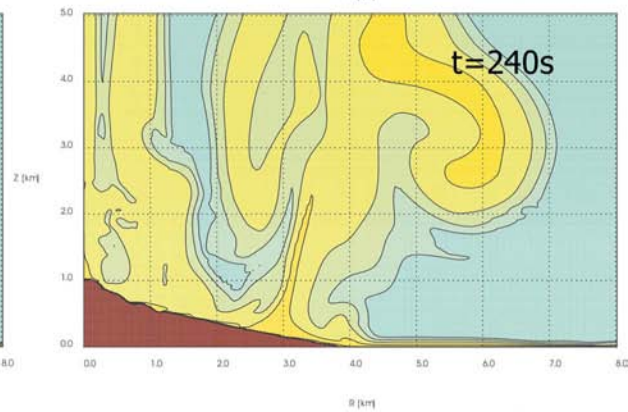
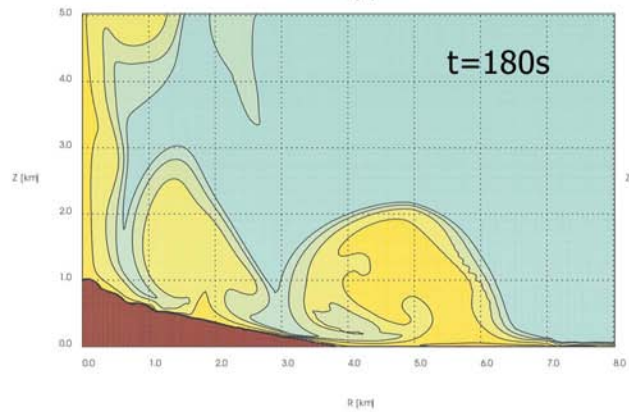
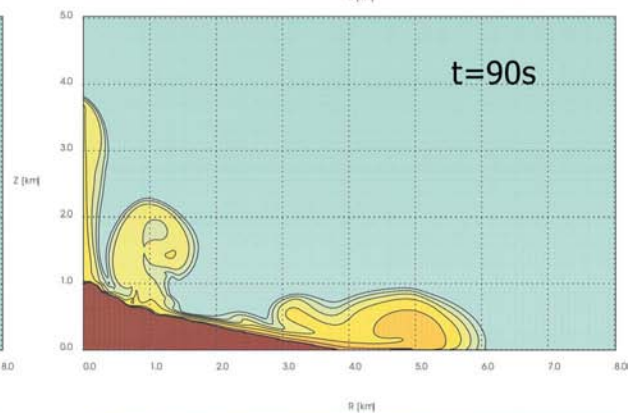
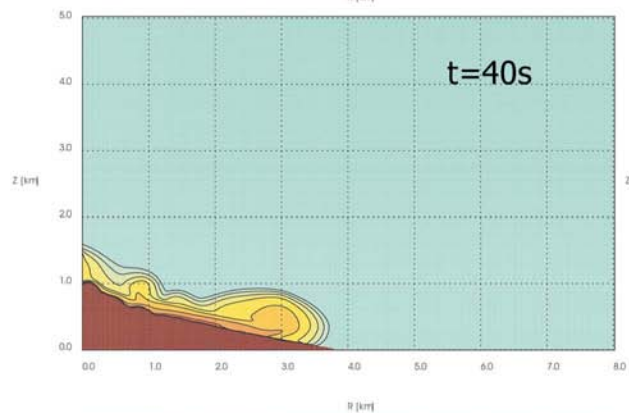
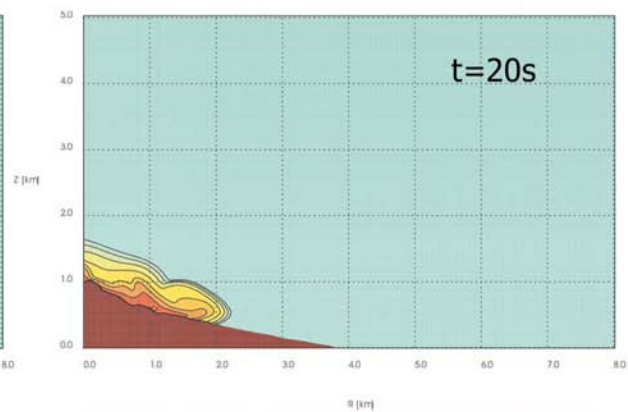
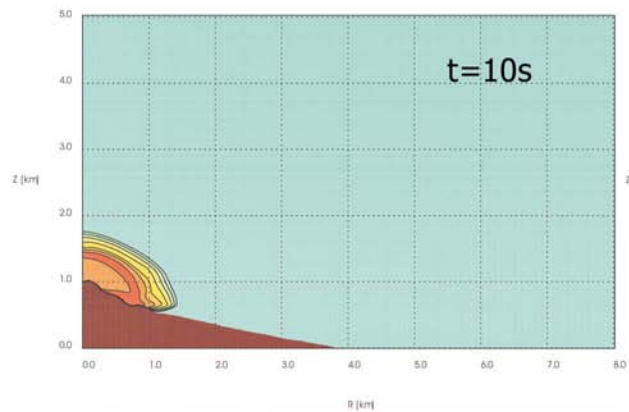


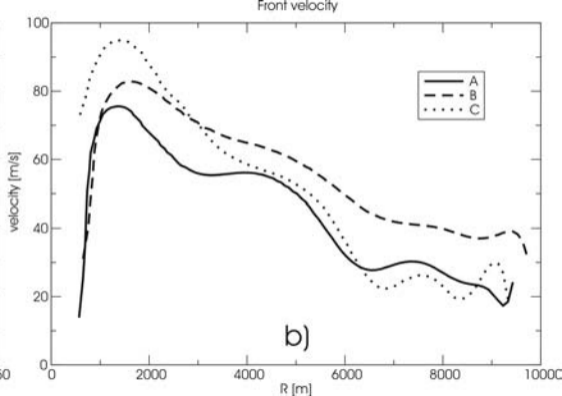
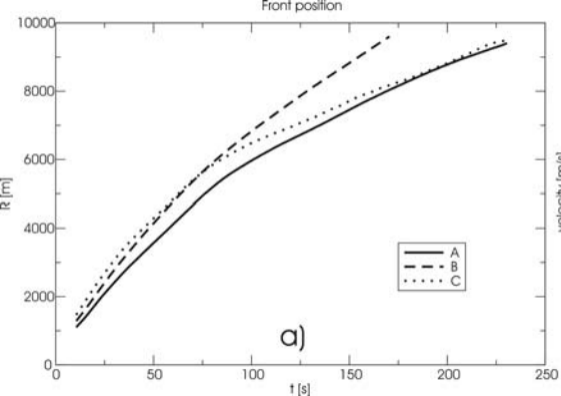


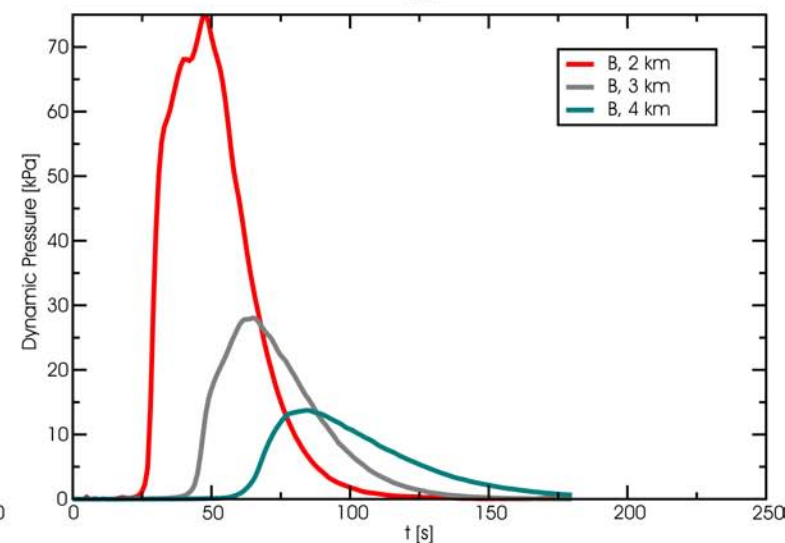
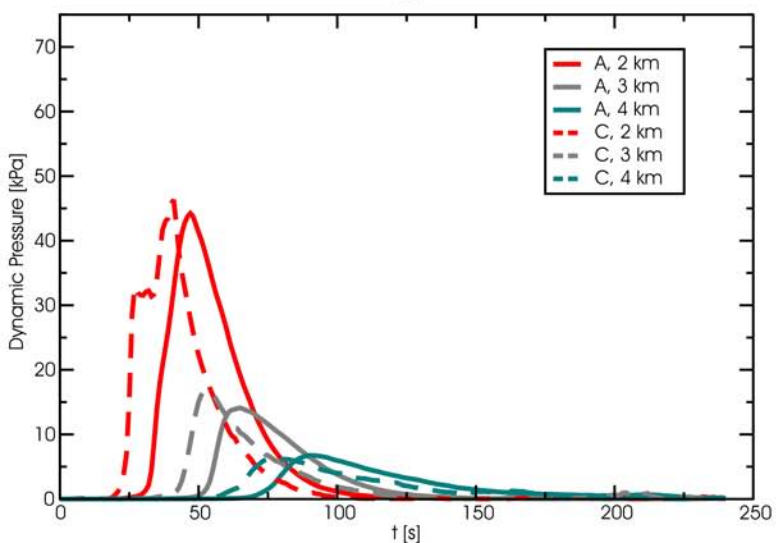
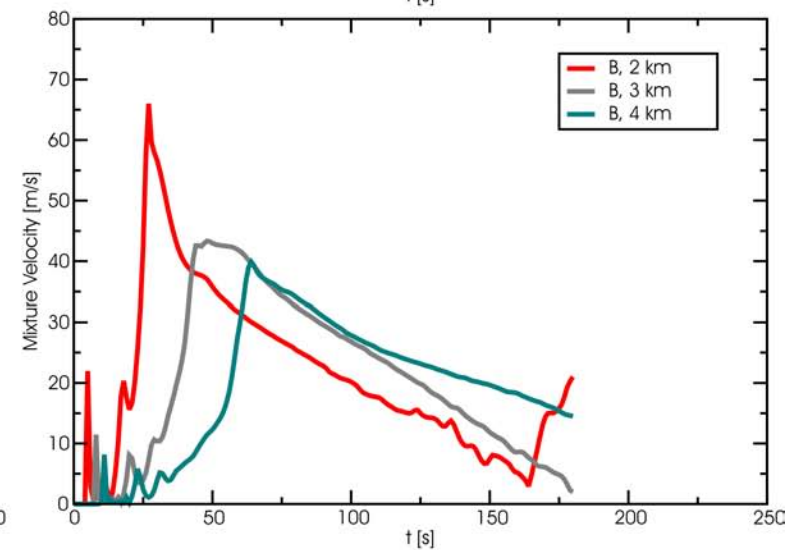
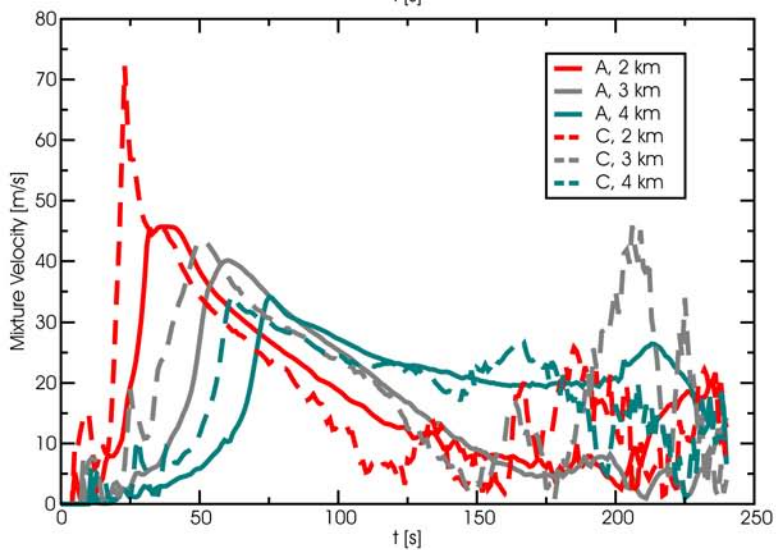
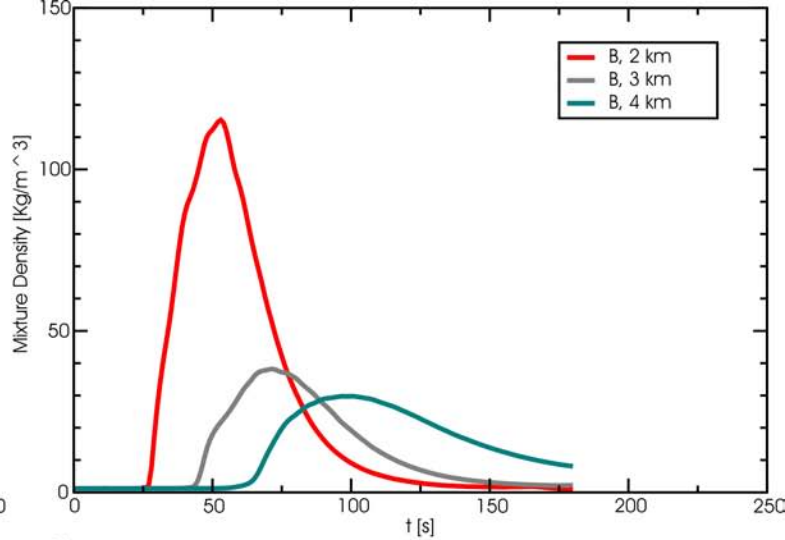
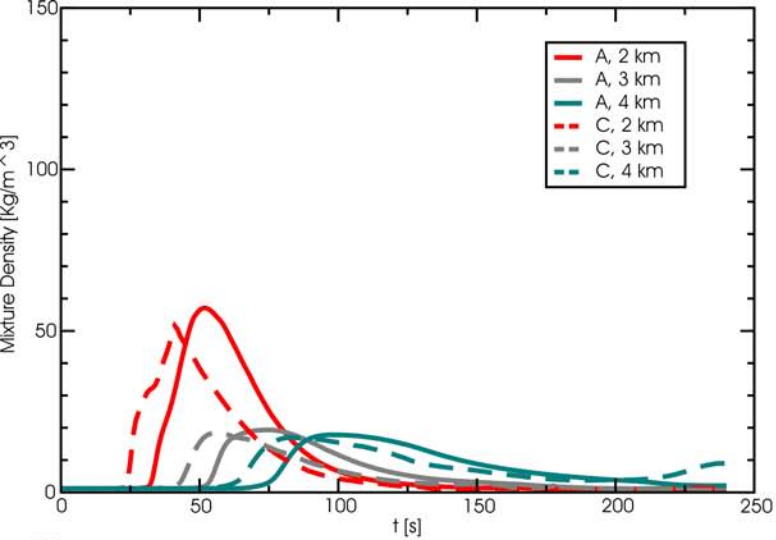






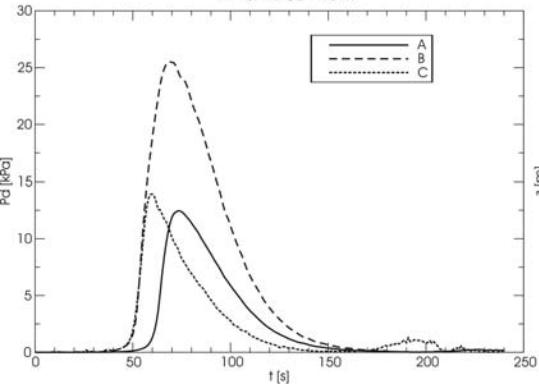






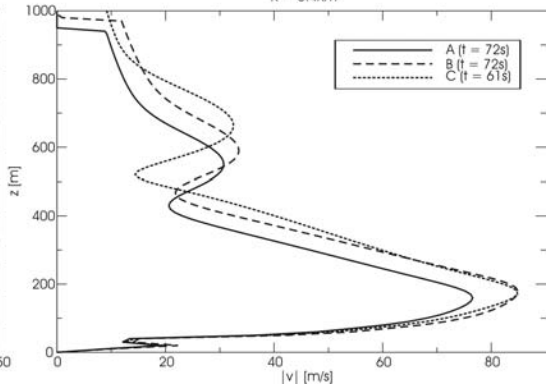
Dynamic Pressure @ St. Patrick

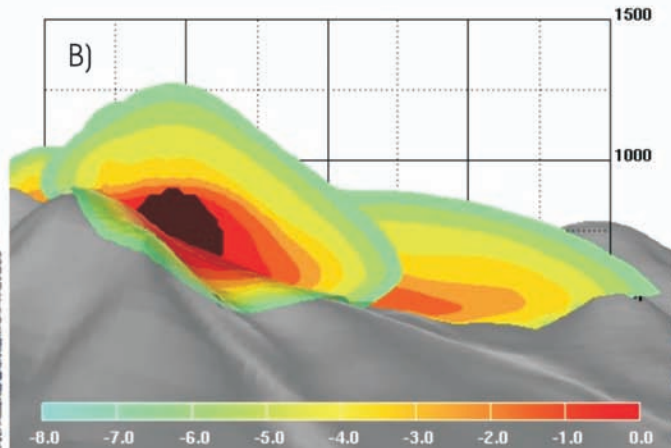
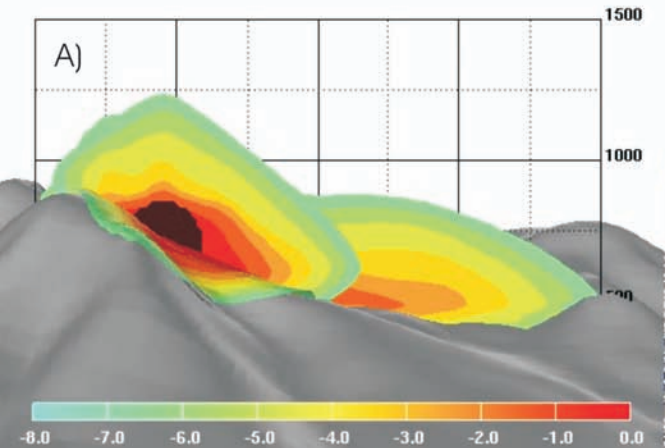
$R = 3.4 \text{ Km}$, $z = 10 \text{ m}$



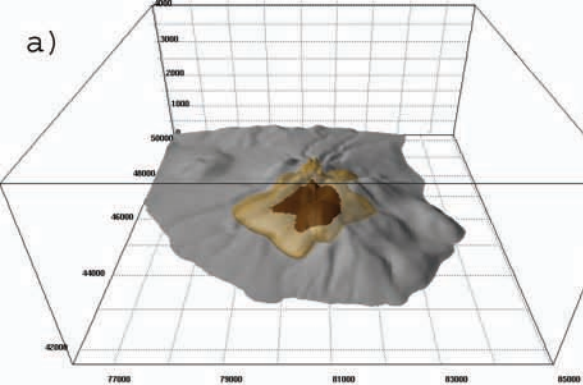
Mixture velocity modulus @ St. Patrick

$R = 3.4 \text{ Km}$

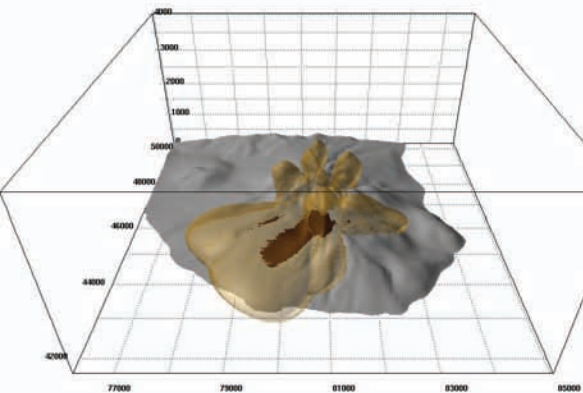
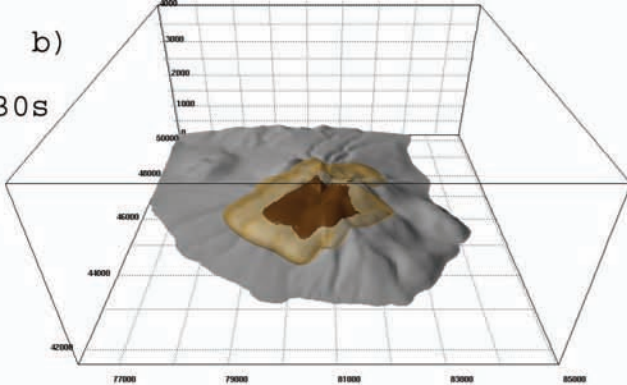
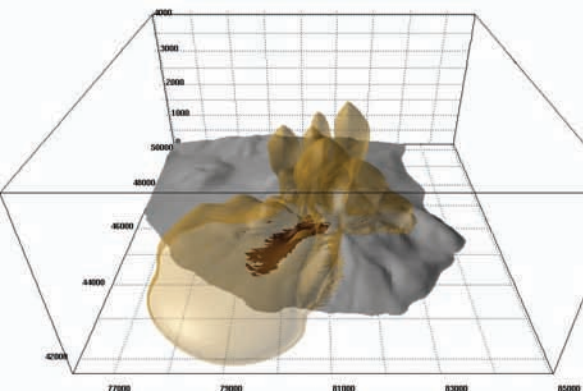
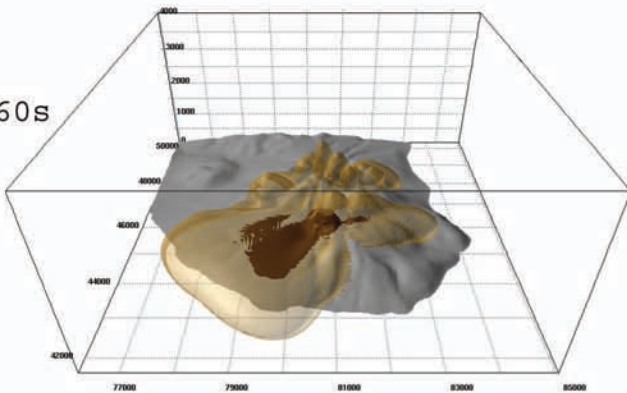
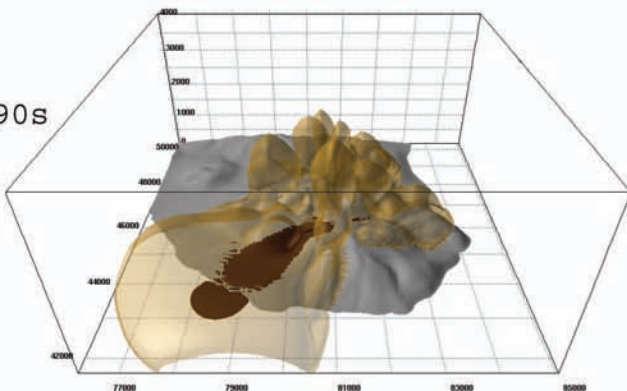


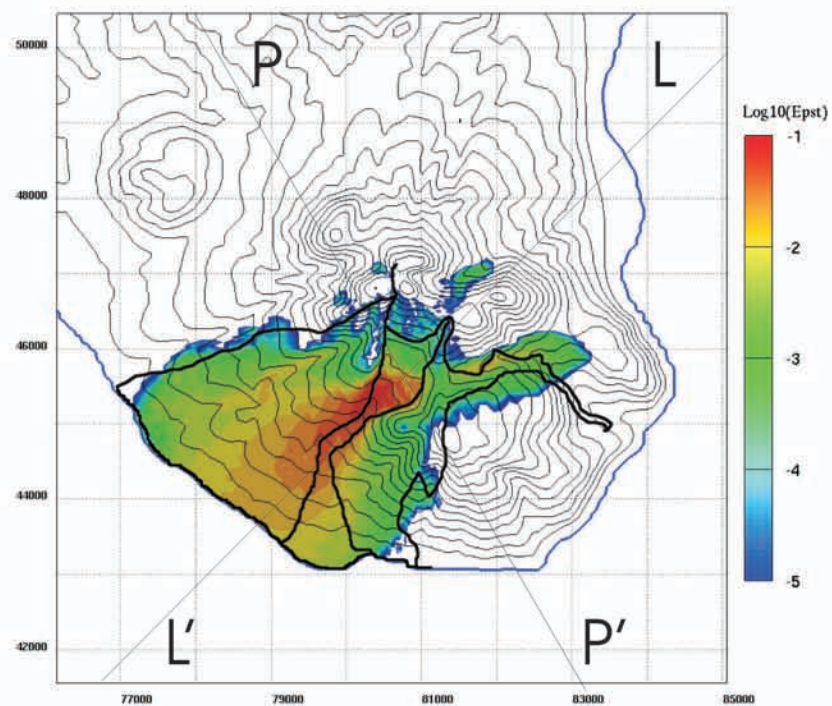


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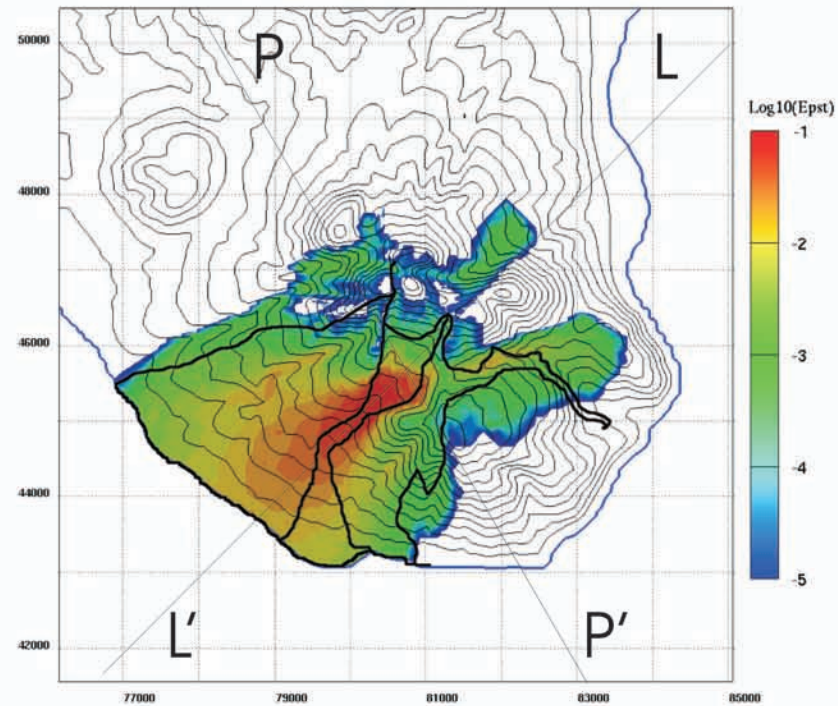
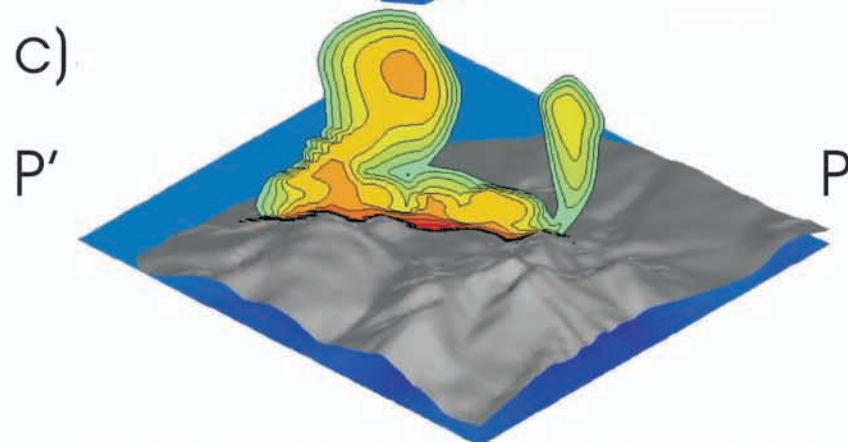
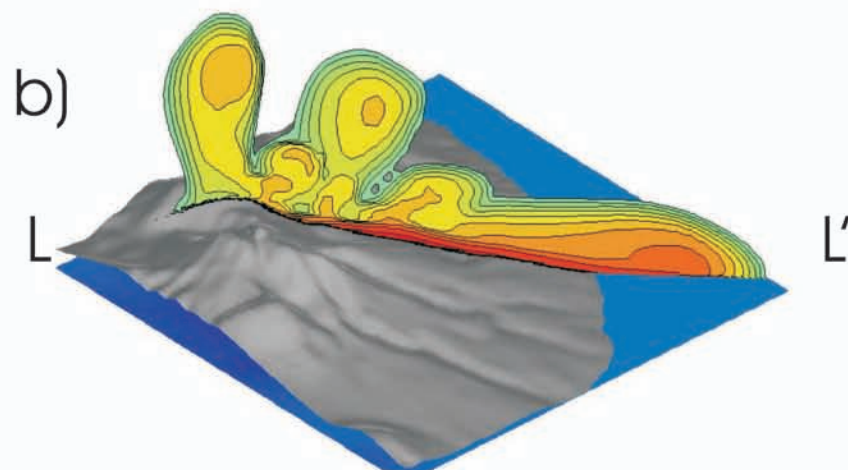


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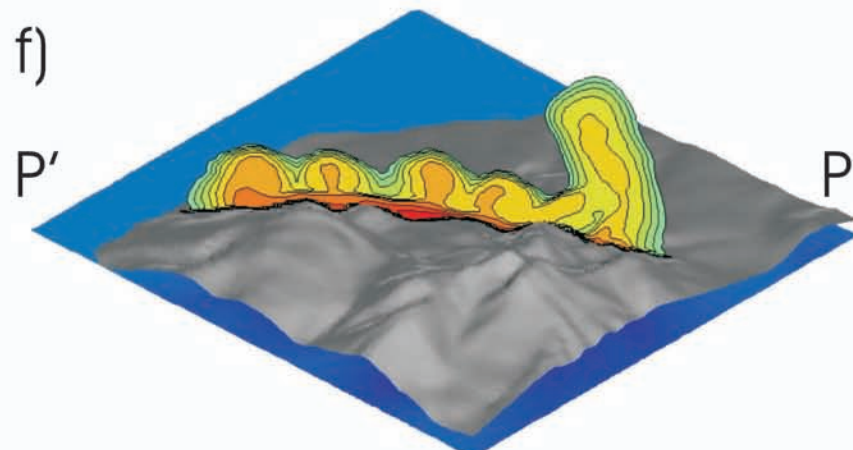
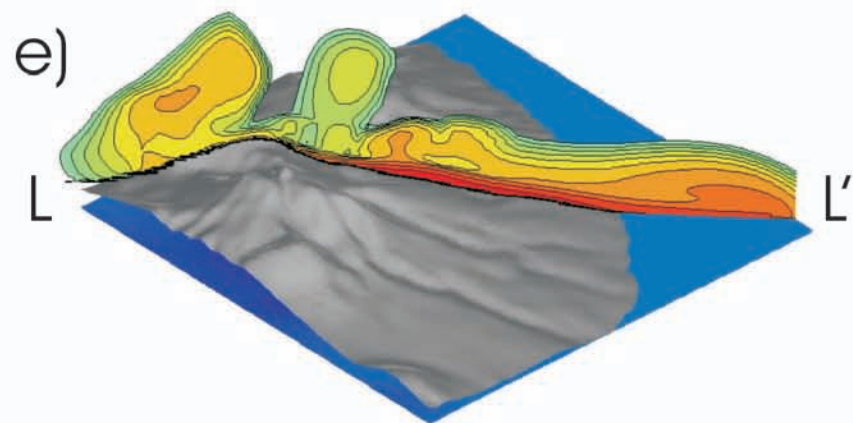
 $t=30s$  $t=60s$  $t=90s$ 

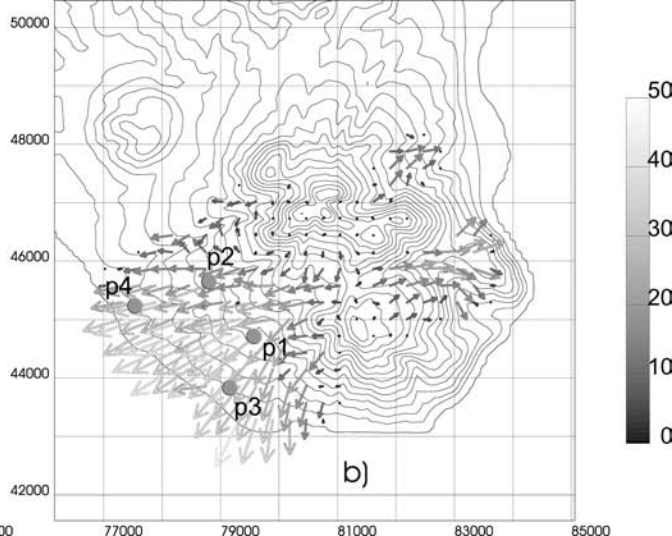
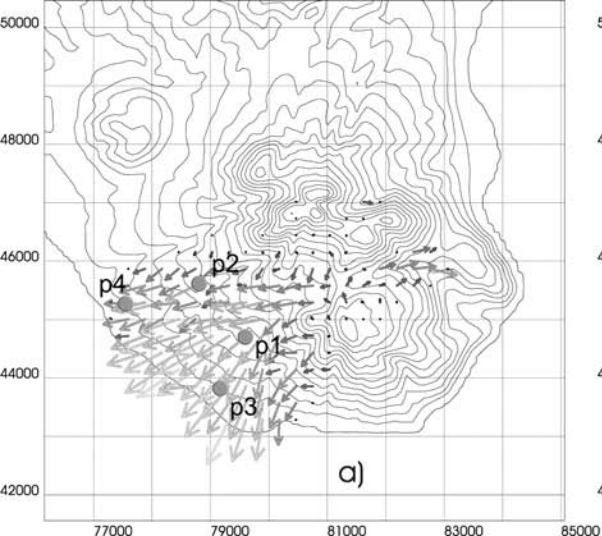


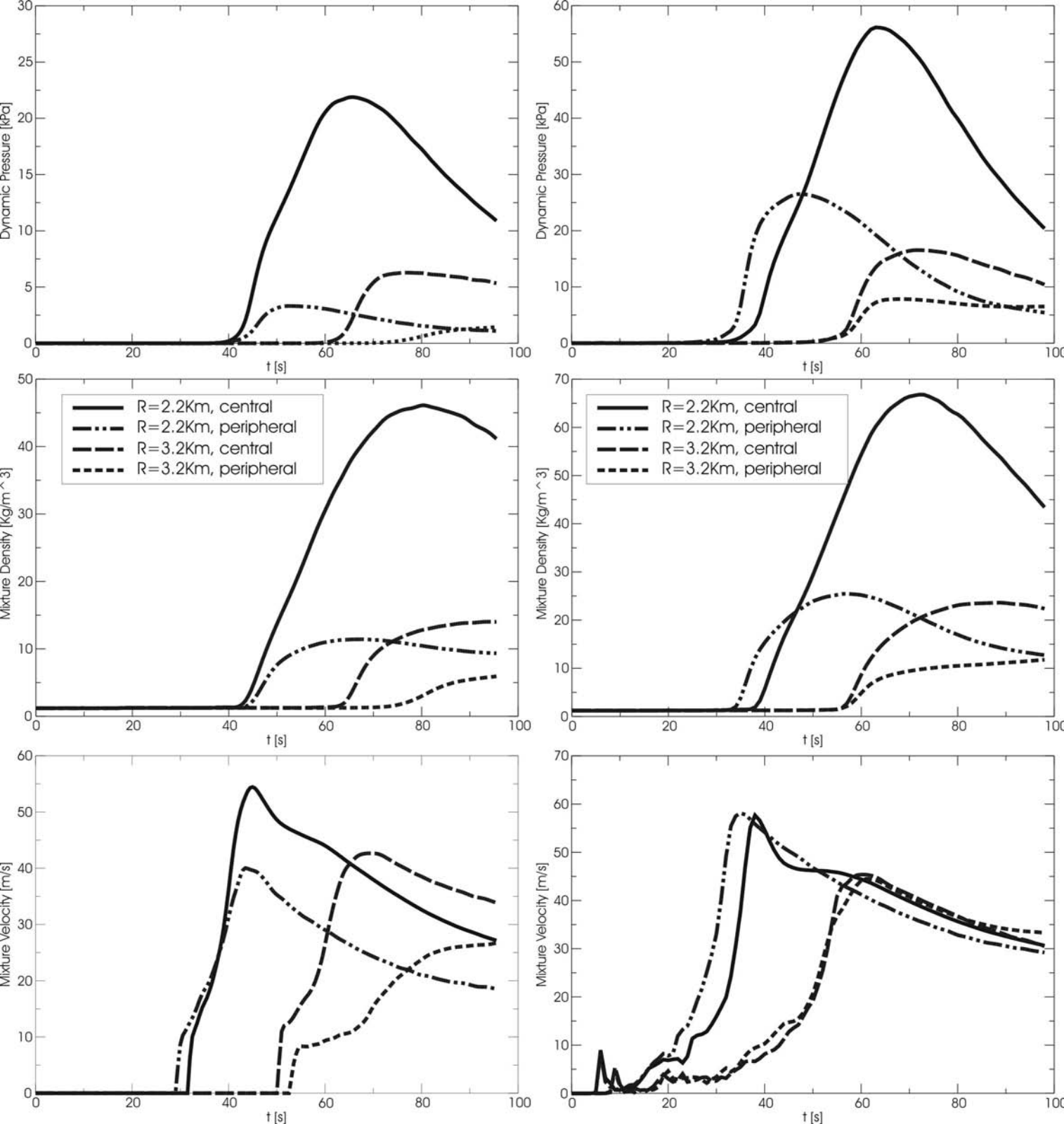
a) $t = 90 \text{ s}$

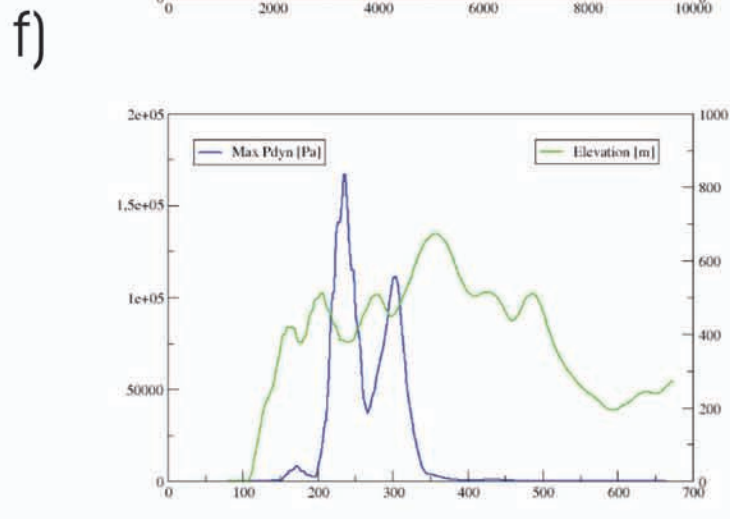
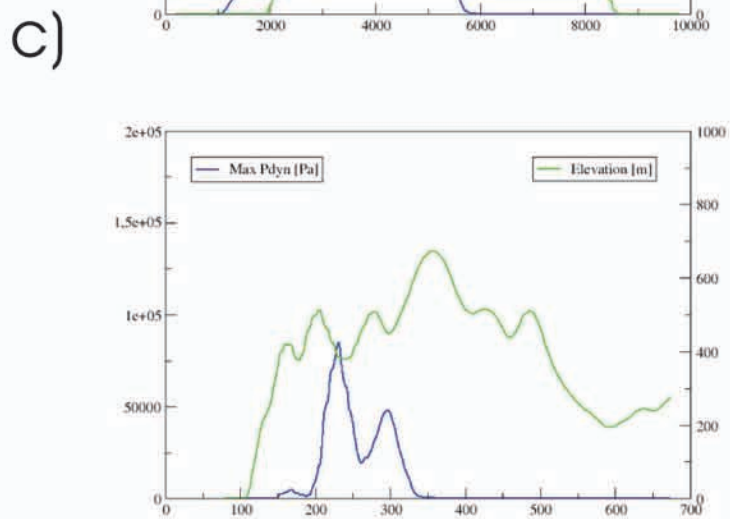
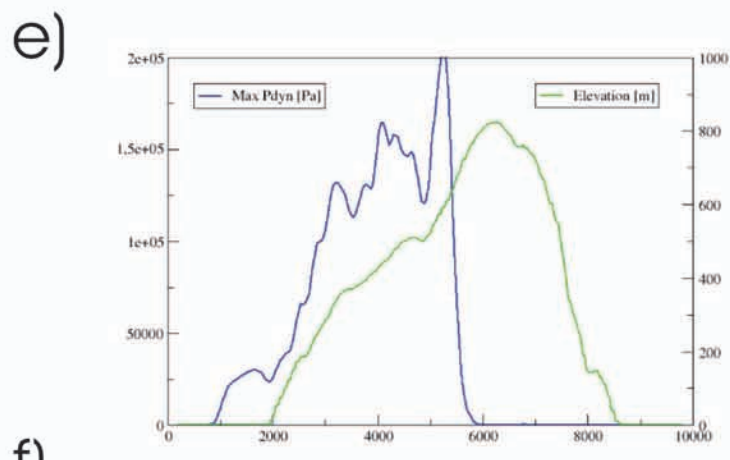
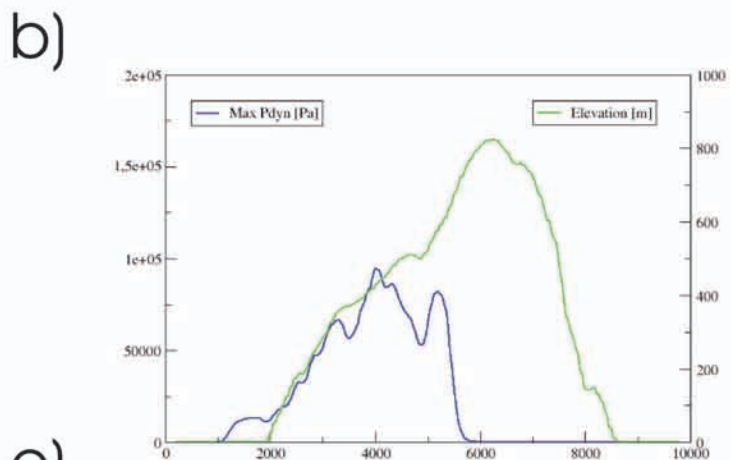
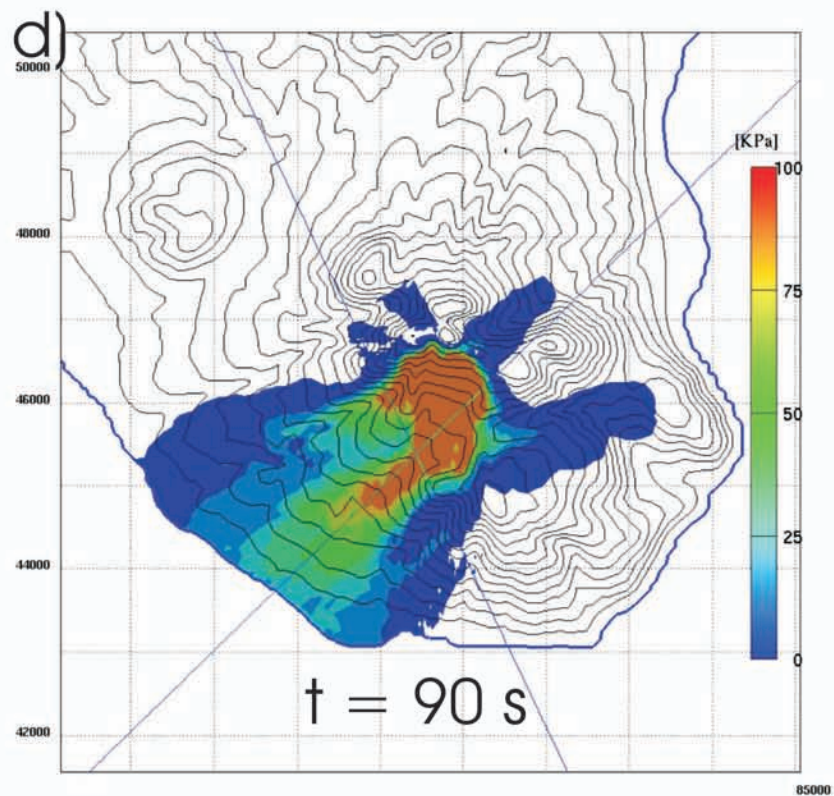
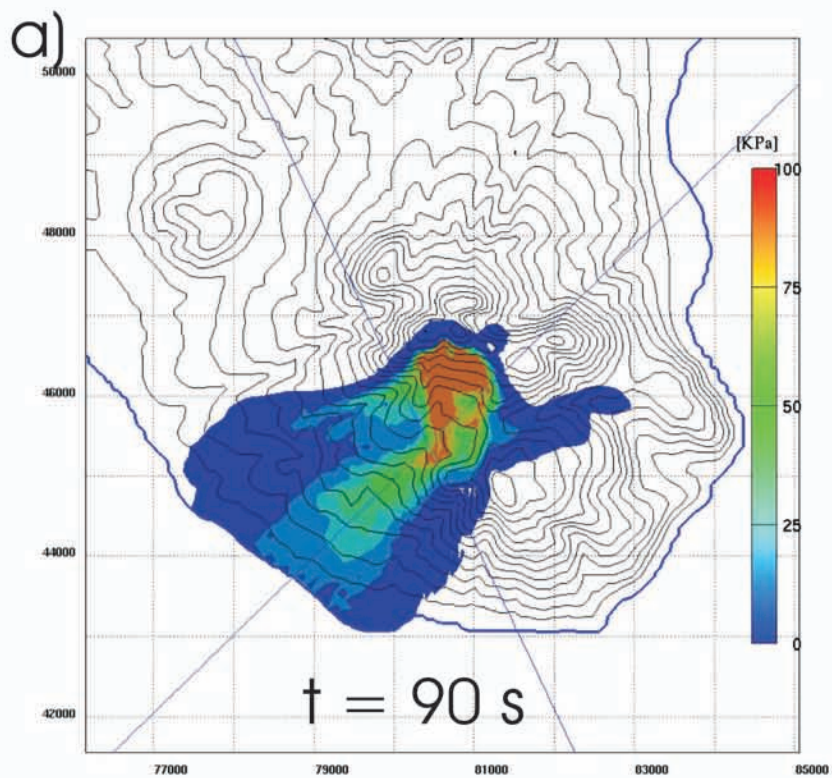


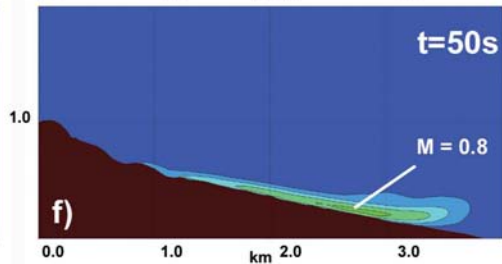
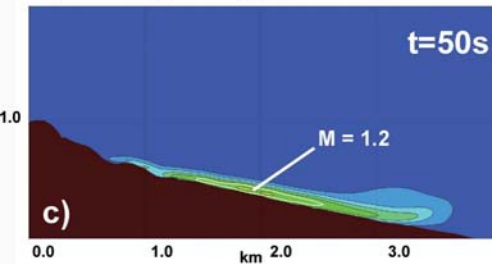
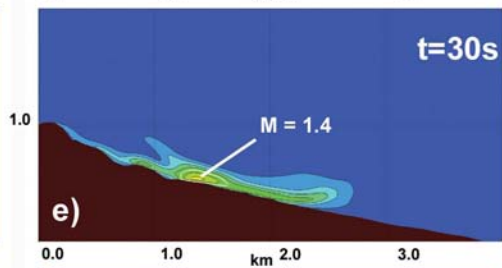
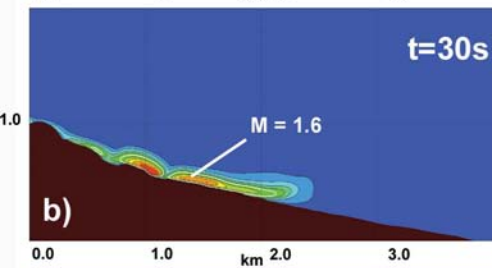
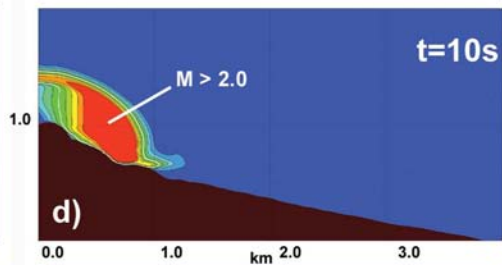
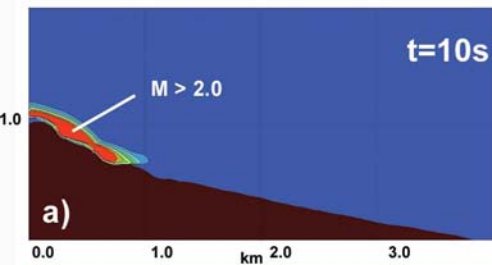
d) $t = 90 \text{ s}$

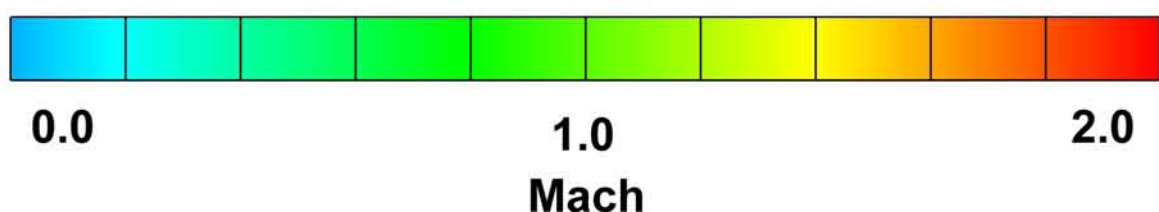
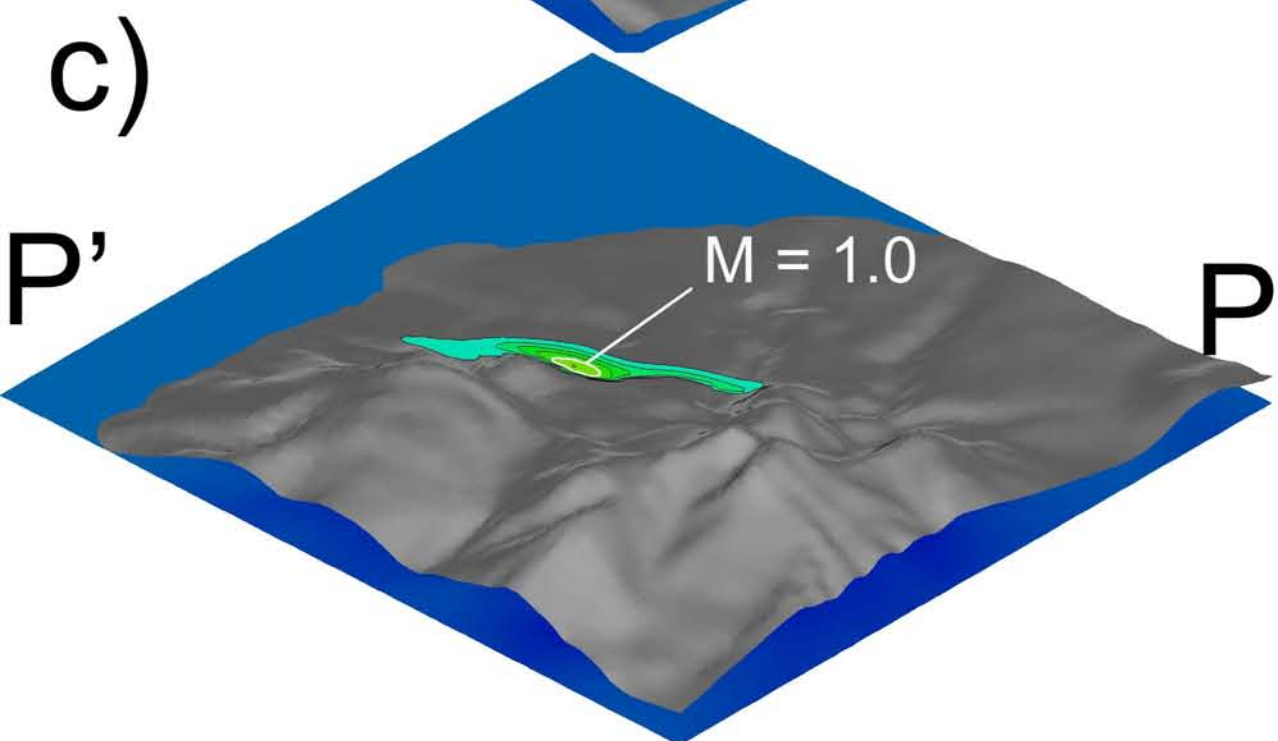
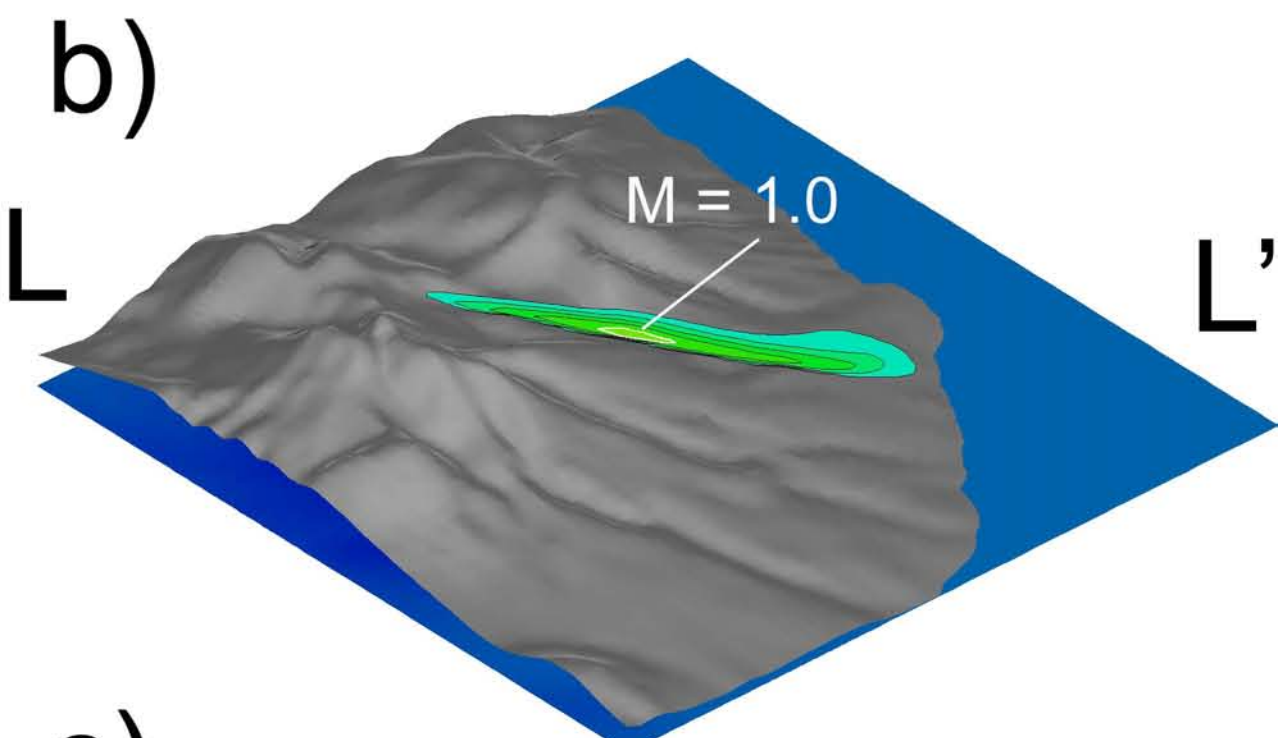
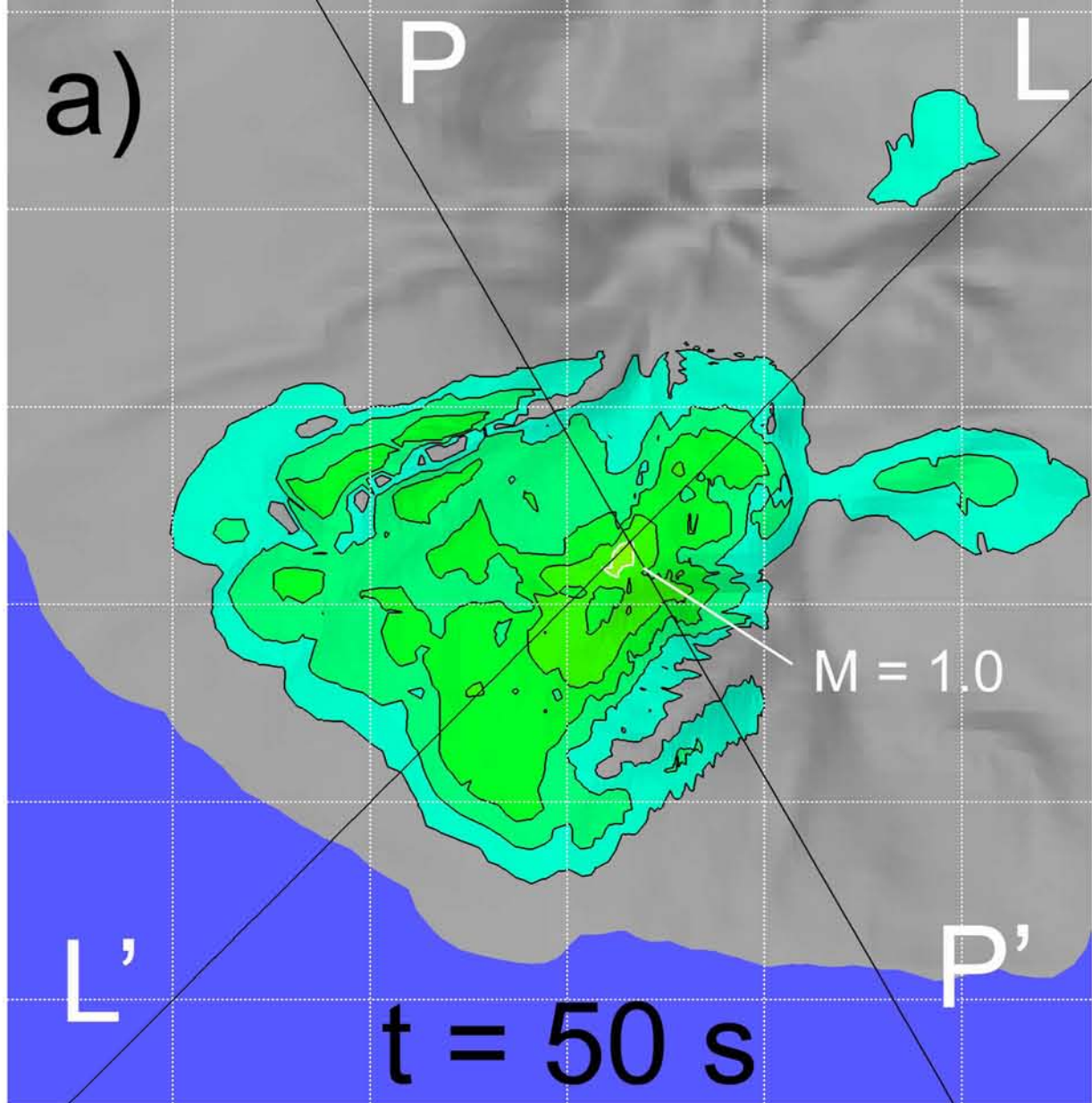


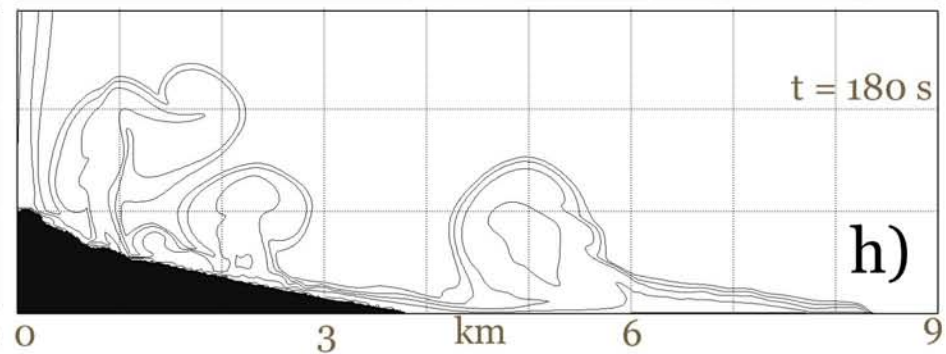
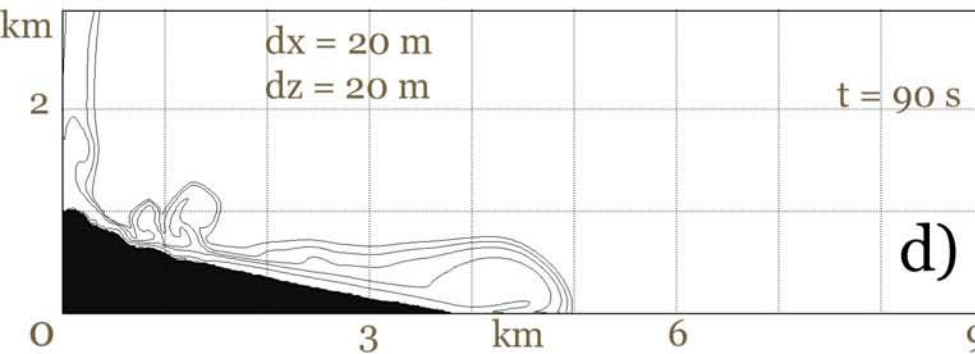
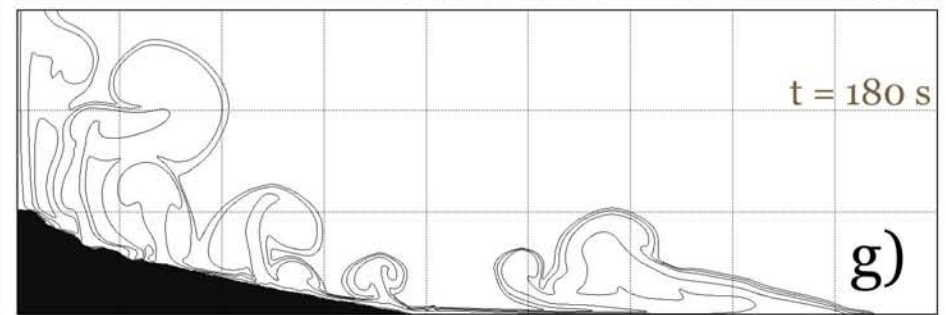
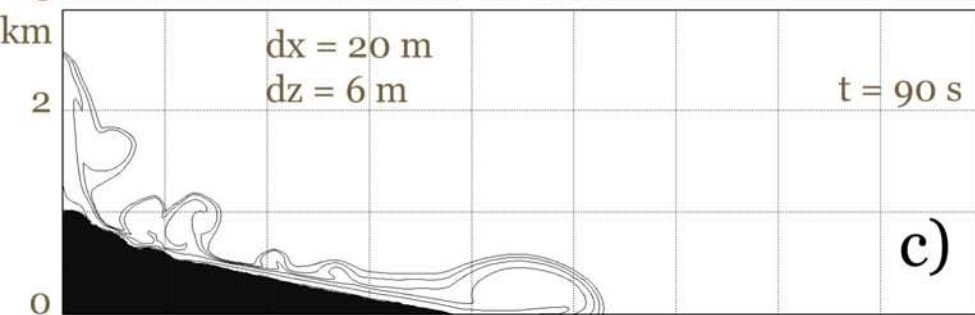
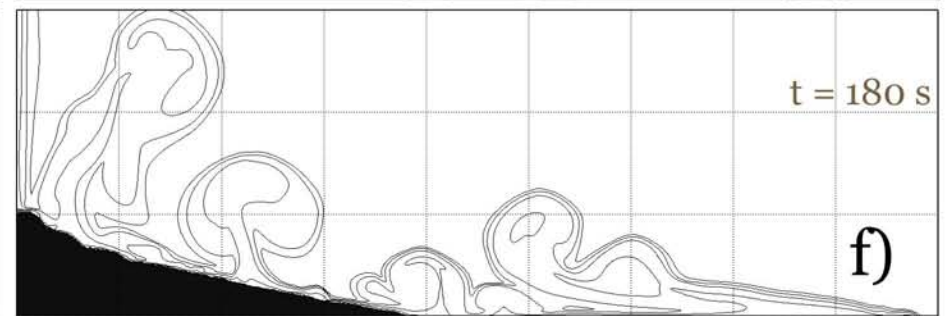
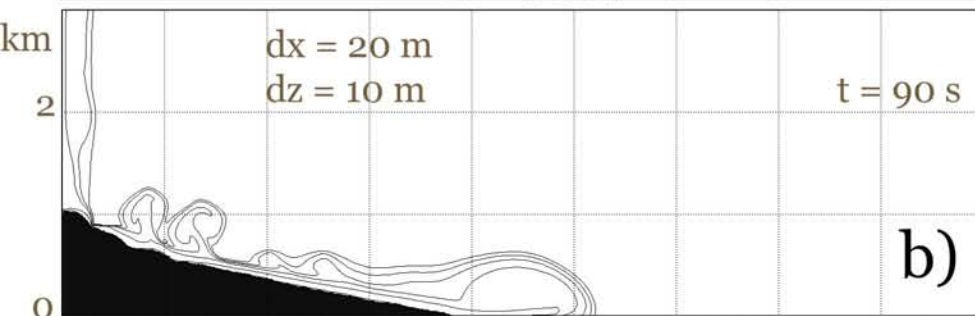
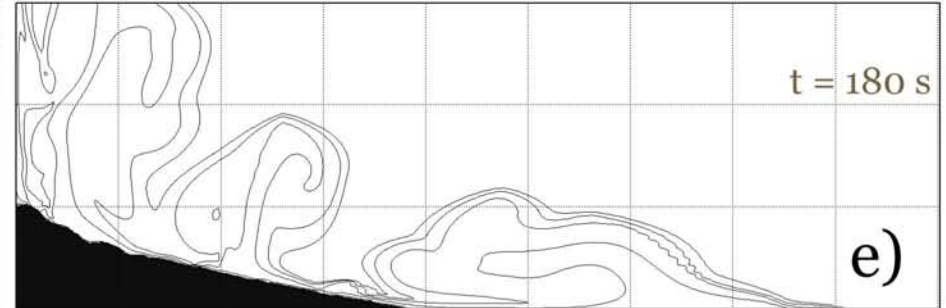
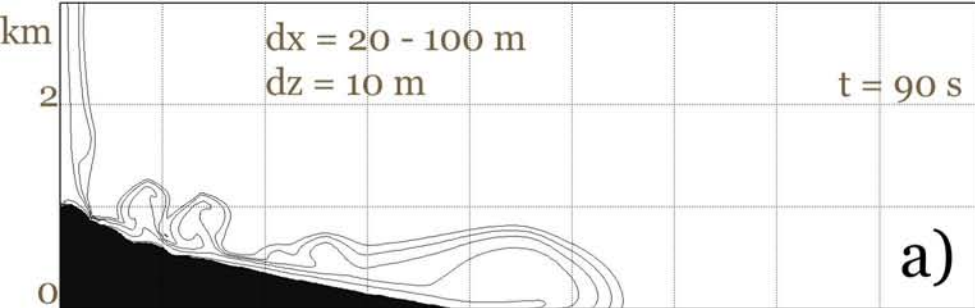


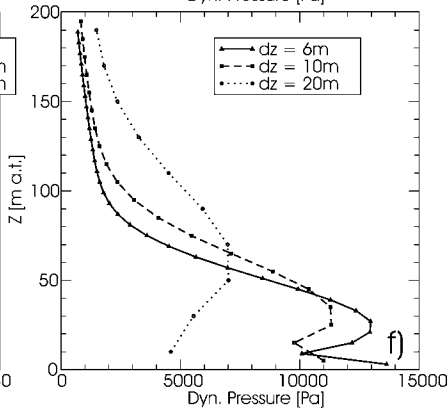
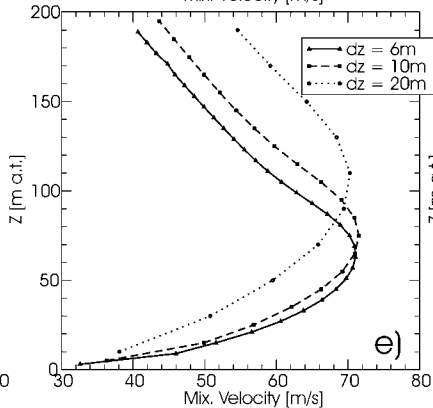
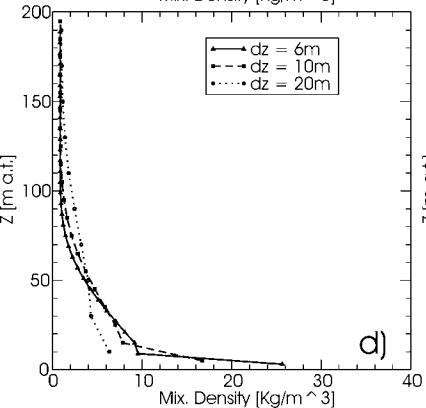
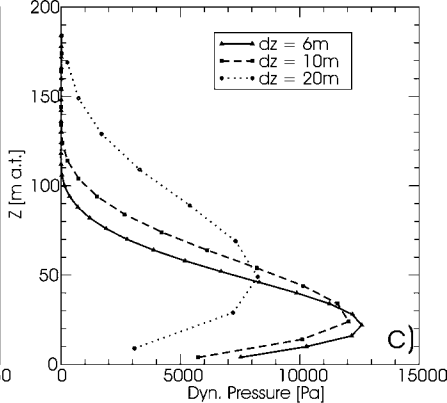
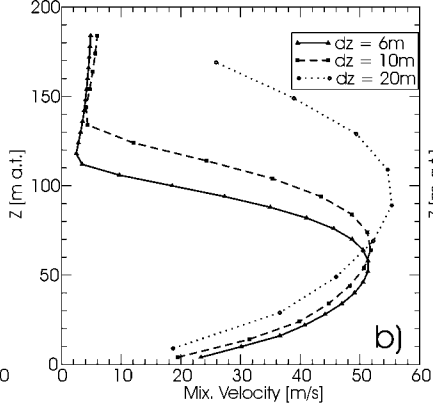
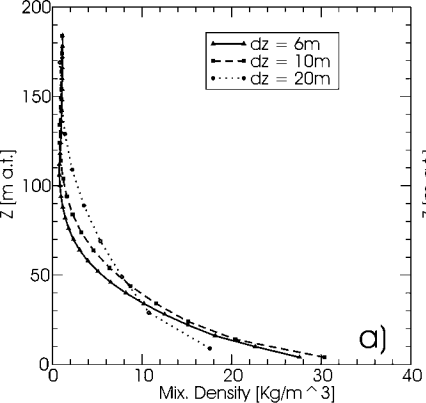












Run	$\kappa(\text{m}^2)$	$V_{\text{DRE}} (\text{m}^3)$	$R_d (\text{m})$	Mass (kg)	α	E [J/kg]
A-2D	10^{-12}	5.0×10^6 $\times(360/70)$	227	60×10^9	0.1	320-490
B-2D	10^{-12}	10.0×10^6 $\times(360/70)$	280	120×10^9	0.1	390-610
C-2D	10^{-14}	5.0×10^6 $\times(360/70)$	227	60×10^9	0.1	1880-3380
A-3D	10^{-12}	5.0×10^6	142	12×10^9	0.1	320-480
B-3D	10^{-12}	10.0×10^6	180	24×10^9	0.1	340-520

Table 1

Run	H _b (m)	U _{b,g} (m s ⁻¹)	U _{b,p} (m s ⁻¹) (5000, 500, 50μm)	U _f (m s ⁻¹)	T _p (s)	E (%) (5000, 500, 50 μm)	Rm _{max} (kg m ⁻³) (at 2,3,4 km)	Um _{max} (m s ⁻¹) (at 2,3,4 km)	Pd _{max} (kPa) (at 2,3,4 km)	Pd _{SP} (kPa)
A-2D	250	160	75,125, 155	70	160	50, 20, ~0	57, 19, 18	46, 40, 34	44, 13, 7	>12.5
B-2D	300	160	75,125, 155	80	>180	0	54, 16, 17	72, 44, 33	46, 16, 6	>26
C-2D	500	175	85,145, 175	90	150	65, 30, <5	118, 38, 30	66, 43, 40	75, 28, 14	>14

Table2