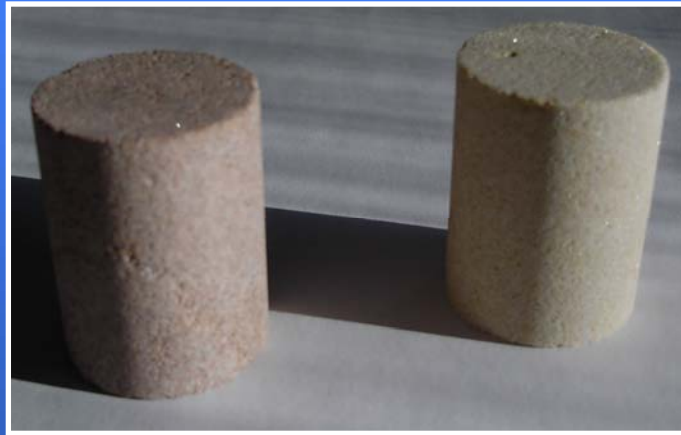


Interpretation of permeability change due to effective stress with special focus on pore space geometry

Coupling of hydro-mechanical properties of
porous media

Guido Blöcher, Harald Milsch & Günter Zimmermann

Two different sandstones (Flechtinger and Bentheimer) were investigated:



- Determine the effective pressure ($p_{\text{eff}} = p_c - p_p$) dependency of Skempton coefficient B and the permeability k
- Analysing the pore space geometry
- Derive linkages between pore space geometry and transport properties

Sample dimension:

length: 10cm
diameter: 5cm

Experiment conditions:

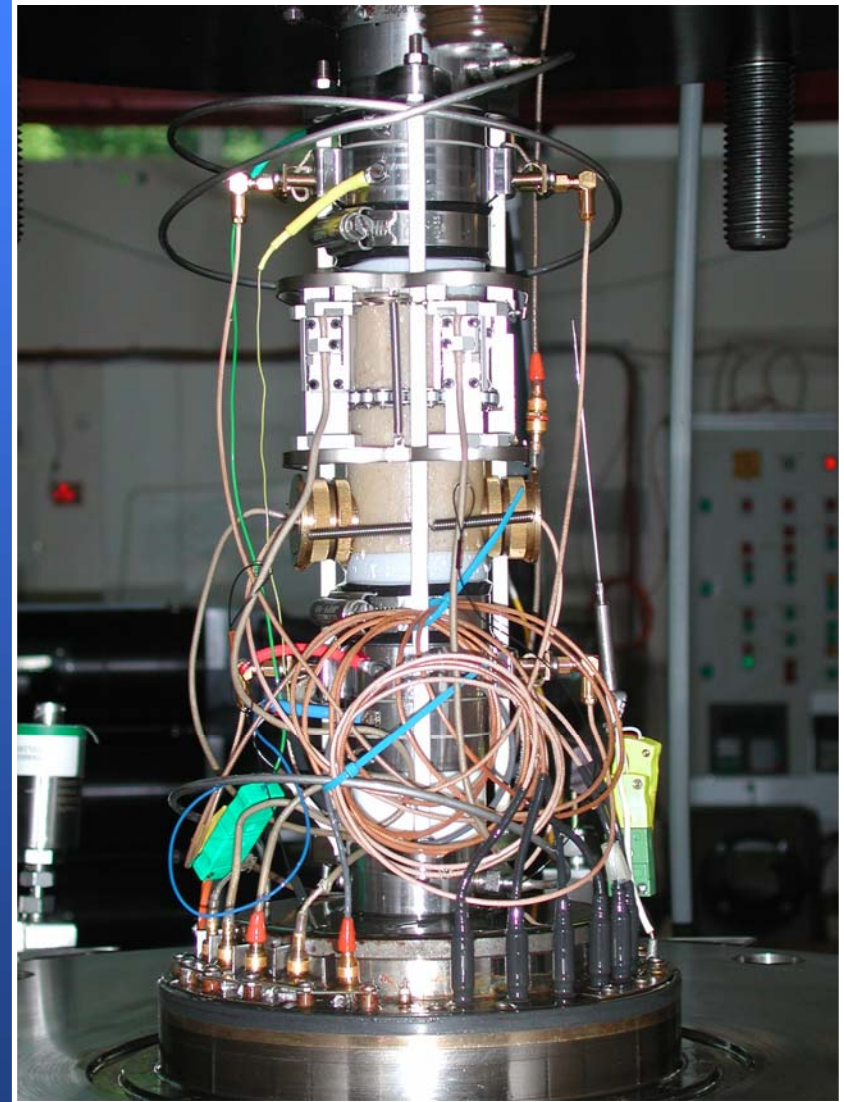
fully undrained
pre-conditioned
confining pressure range $p_c = 5$ to 60MPa

Measurement:

pore pressure p_p

Result:

Skempton coefficient $B = \frac{dp_p}{dp_c}$



Sample dimension:

length: 4cm

diameter: 3cm

cross sectional area $A=7.07\text{cm}^2$

Experiment conditions:

drained

$T=40^\circ\text{C}$

0.1 molar NaCl- brine

confining pressure range $p_c = 5$ to 47MPa

pore pressure range $p_p = 2.5$ to 42MPa

flow rate range $Q = 0.05$ to 30 ml/min

Measurement:

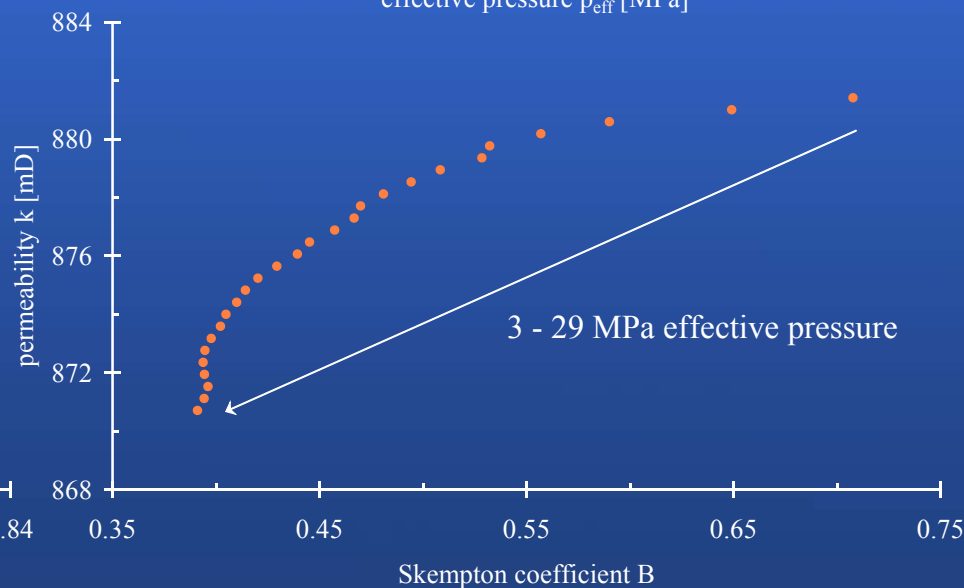
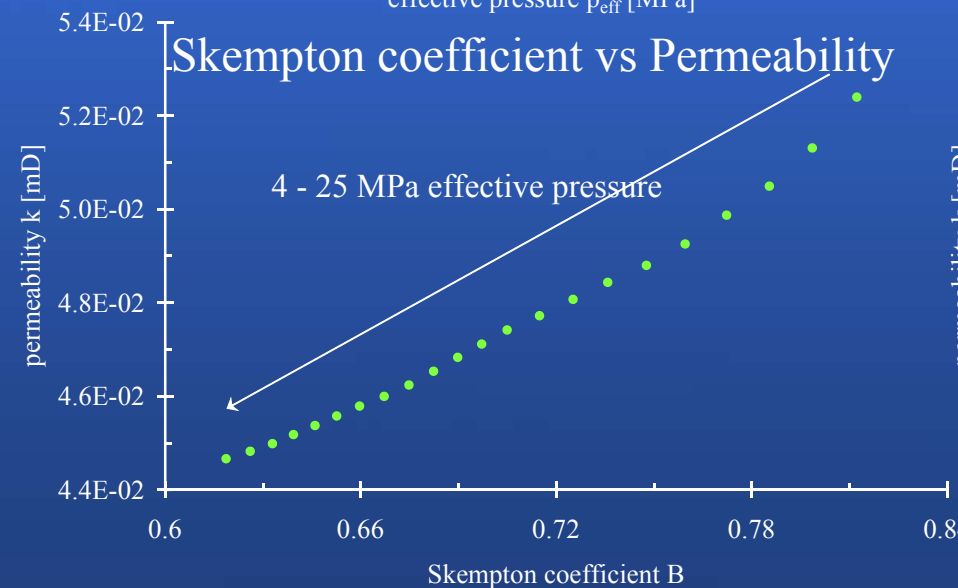
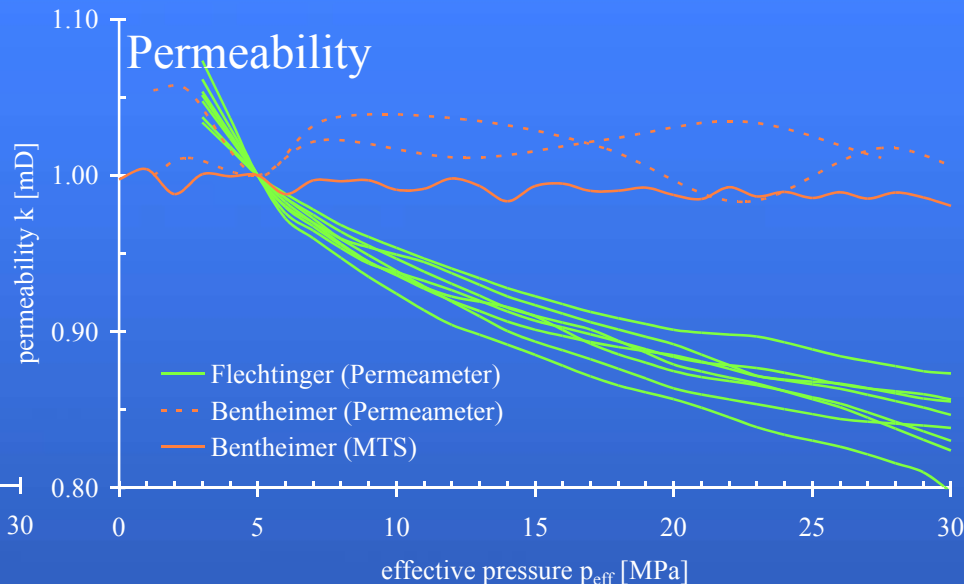
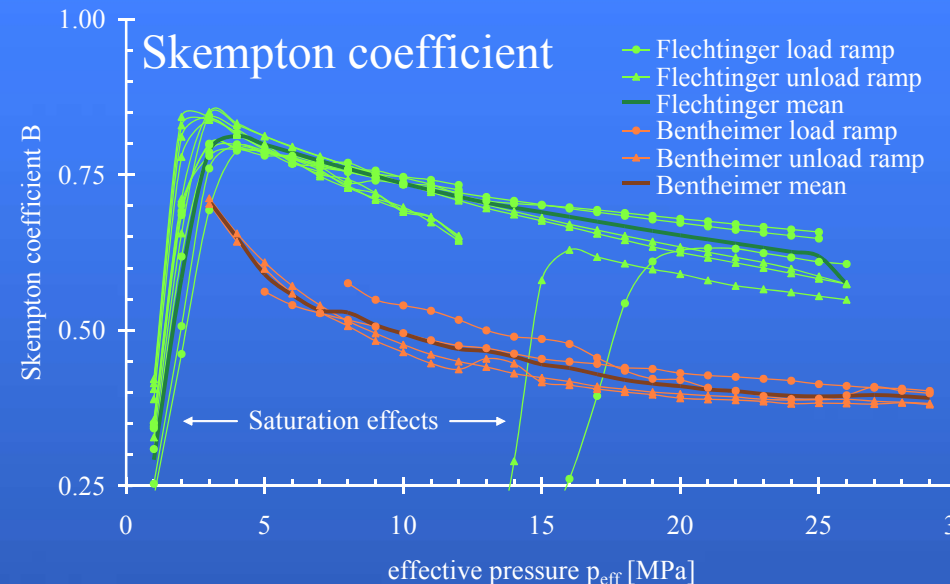
pore pressure gradient $\text{grad}(p_p)$

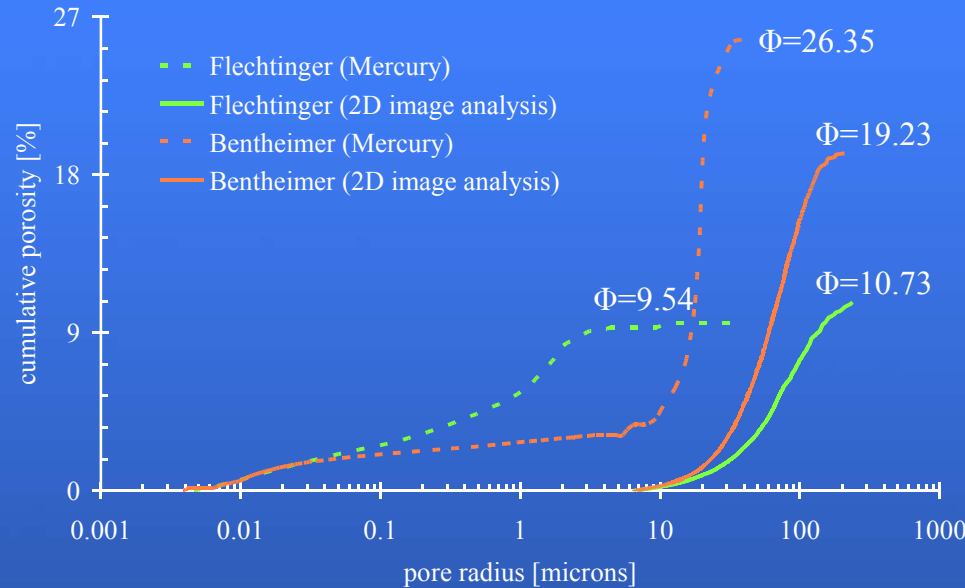
Result:

permeability

$$k = - \frac{Q^* \eta}{A^* \text{grad}(p_p)}$$







Bentheimer:

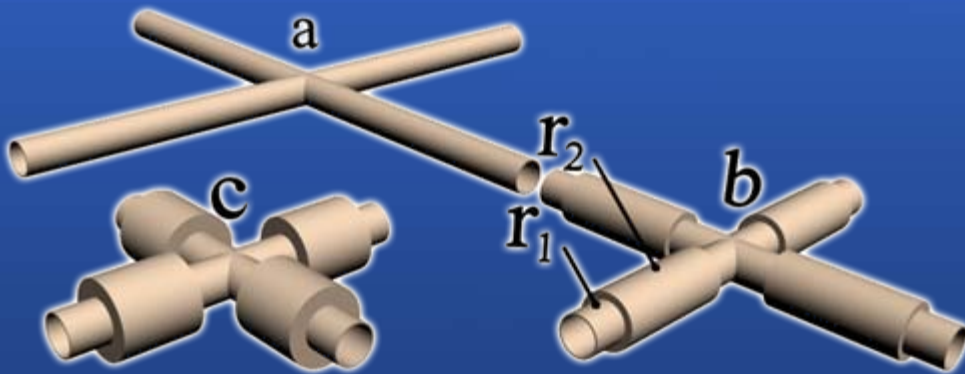
total porosity: 19.23-26.35
pore radii: 40-110 microns
pore cavity to throat ratio: small

Flechtinger:

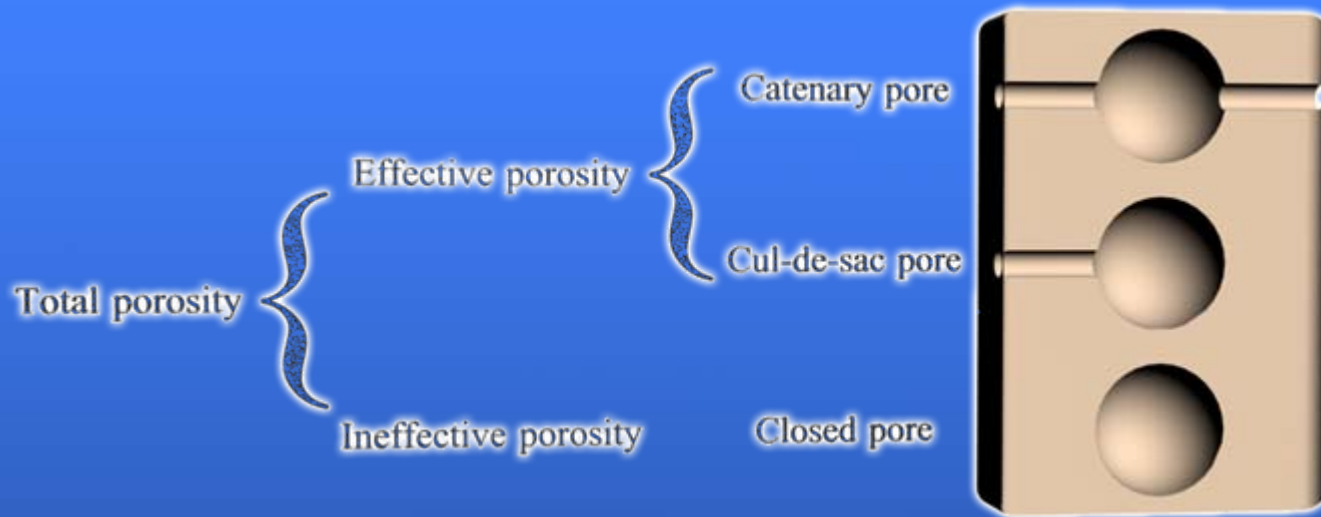
total porosity: 9.54-10.73
pore radii: 6.5-200 microns
pore cavity to throat ratio: high

Pore cavity-throat-ratio

- mercury injection assumes cylindrically shaped pores \rightarrow determined radius is close to pore throat radius
- 2D image analysis directly determines the pore radii



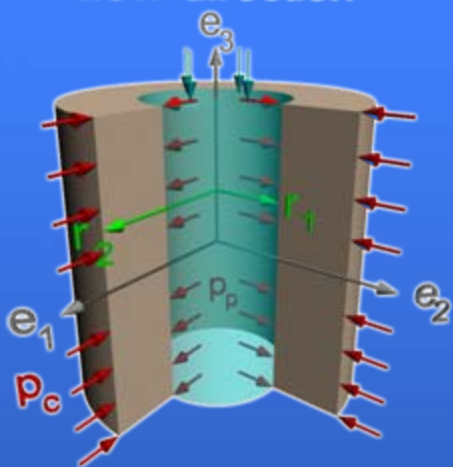
\rightarrow Gap between Mercury injection and 2D image analysis indicates the pore cavity to throat ratio



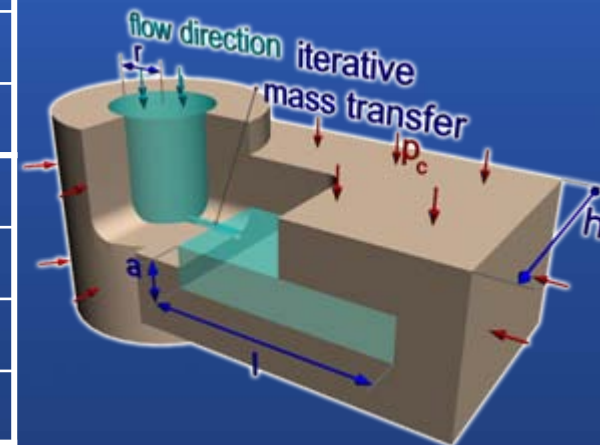
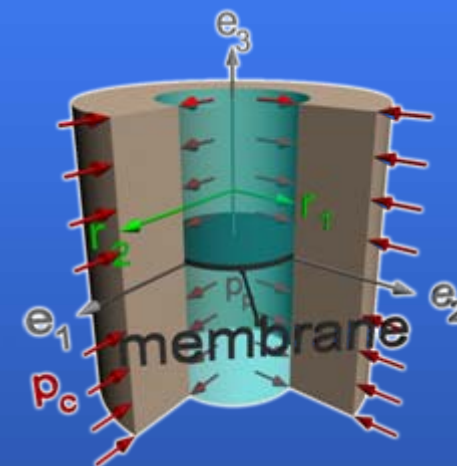
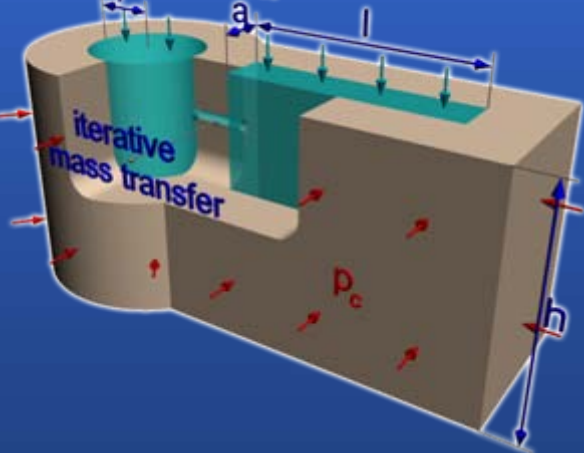
	Measured pore types		
	2D Image Analysis	Skempton Experiment	Permeability Experiment
Catenary pores	X	X	X
Cul-de-sac pores	X	X	
Closed pores	X		

Note: The ratio of Catenary, Cul-de-sac and Closed pores is changing due to effective pressure

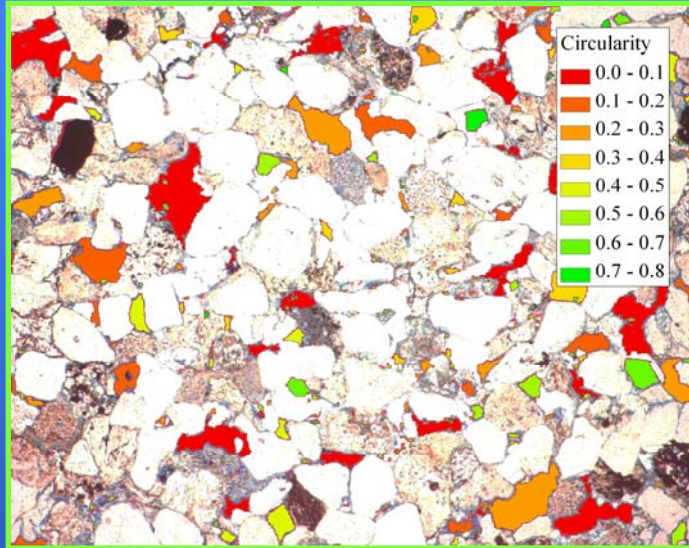
flow direction



flow direction



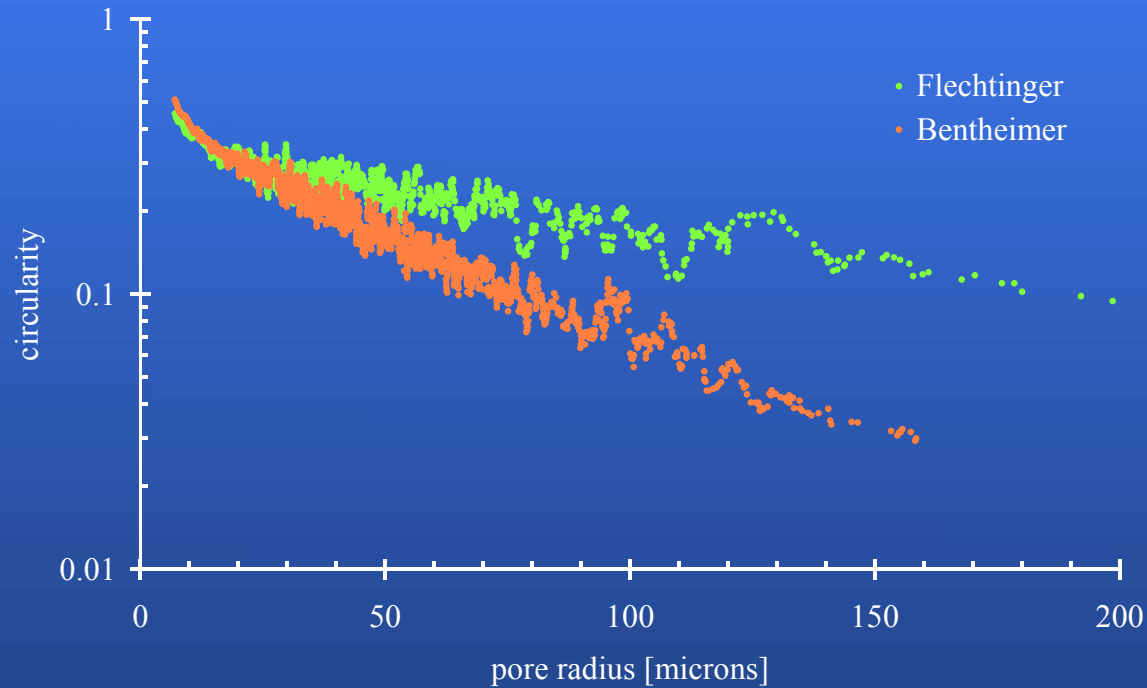
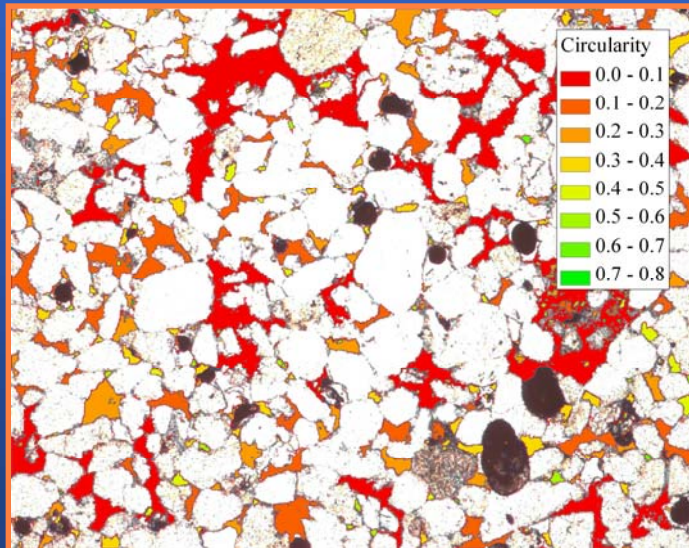
$B(p_{\text{eff}}=0\text{MPa})$	0.1373
$k(p_{\text{eff}}=0\text{MPa}) [\text{m}^2]$	7.81E-09
$dB/dp_{\text{eff}} [1/\text{MPa}]$	-4.5E-06
$dk/dp_{\text{eff}} [\text{m}^2/\text{MPa}]$	-5.7E-13
$B(p_{\text{eff}}=0\text{MPa})$	0.1373
$k(p_{\text{eff}}=0\text{MPa}) [\text{m}^2]$	0
$dB/dp_{\text{eff}} [1/\text{MPa}]$	-4.5E-06
$dk/dp_{\text{eff}} [\text{m}^2/\text{MPa}]$	0
$B(p_{\text{eff}}=0\text{MPa})$	0.4085
$k(p_{\text{eff}}=0\text{MPa}) [\text{m}^2]$	1.10E-08
$dB/dp_{\text{eff}} [1/\text{MPa}]$	-4.5E-05
$dk/dp_{\text{eff}} [\text{m}^2/\text{MPa}]$	-2.3E-12
$B(p_{\text{eff}}=0\text{MPa})$	0.4085
$k(p_{\text{eff}}=0\text{MPa}) [\text{m}^2]$	7.81E-09
$dB/dp_{\text{eff}} [1/\text{MPa}]$	-4.5E-05
$dk/dp_{\text{eff}} [\text{m}^2/\text{MPa}]$	-5.7E-13

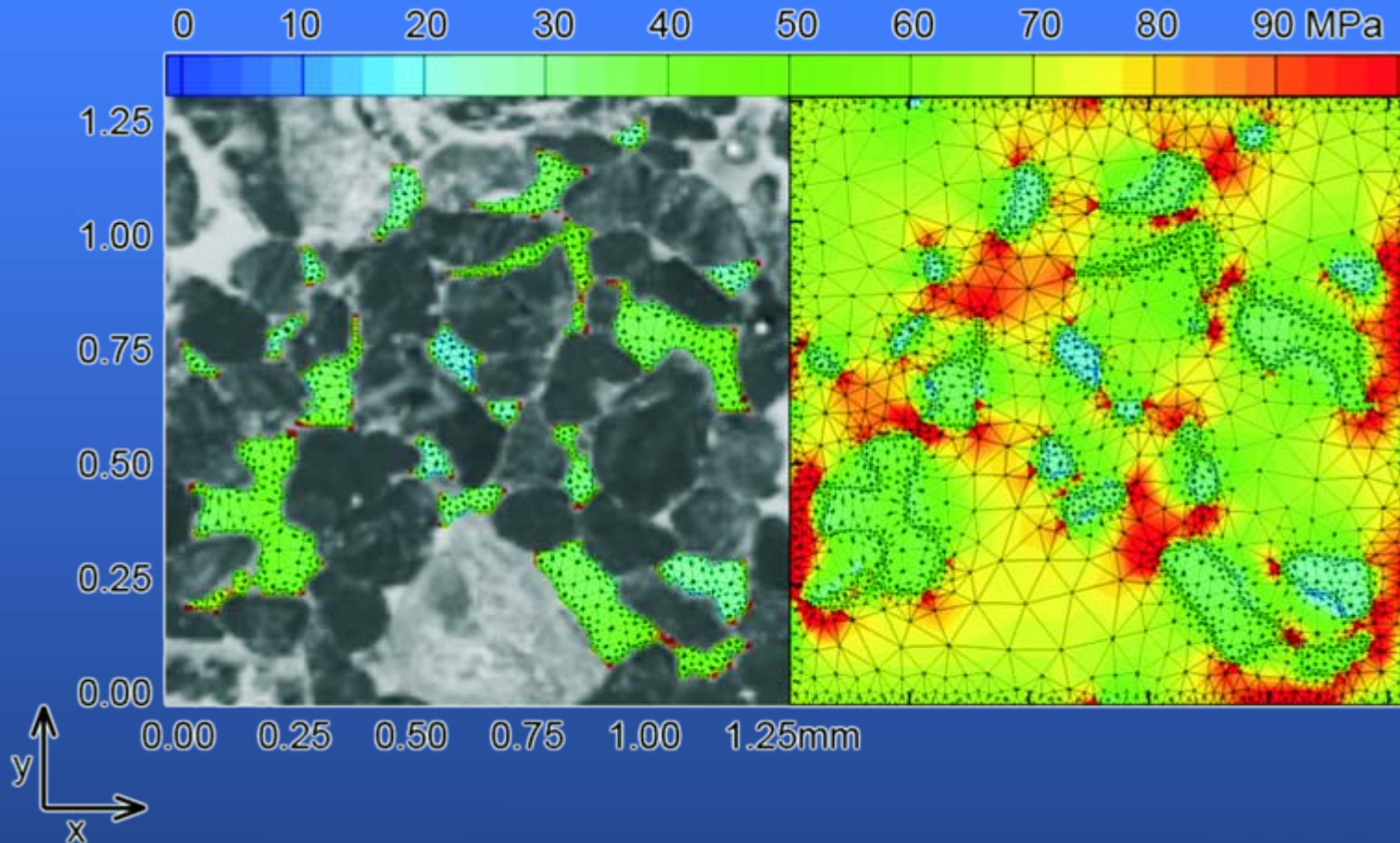


$$C = 4\pi \frac{A_p}{l^2}$$

$A_p \rightarrow$ pore area

$l \rightarrow$ perimeter length





Skempton coefficient varies for each single pore from 0.32 to 0.68 dependent on the pore shape

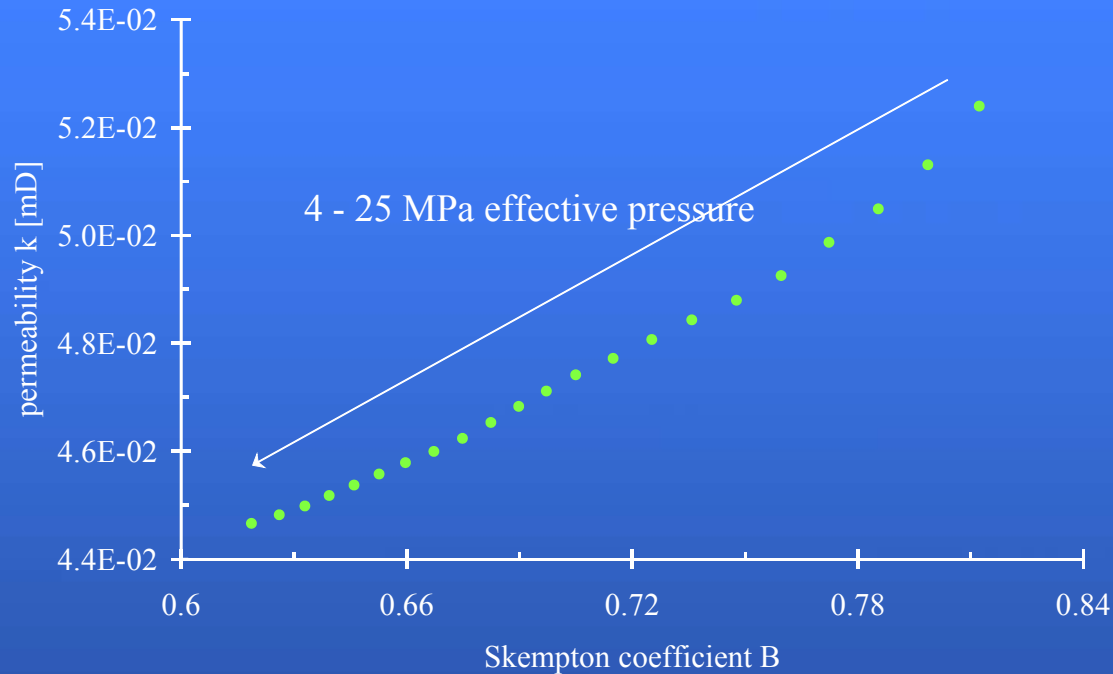
Two mechanisms lead to a change in porosity, Skempton coefficient and permeability with changing effective stress:

1. A pore separation by closing of pore throats

- Catenary pore → Cul-de-sac pore leads to a decrease of permeability
- Cul-de-sac → Closed pore leads to a decrease of Skempton coefficient
- The separation of pores depends on the pore cavity to throat ratio

2. A poro-elastic deformation of the pore space itself

- poro-elastic deformation affects porosity, Skempton coefficient and permeability
 - The change in Skempton coefficient is highest
- Irregularly shaped pores are more susceptible to poro-elastic deformation



Observation:

High circularity

High pore cavity-throat-ratio

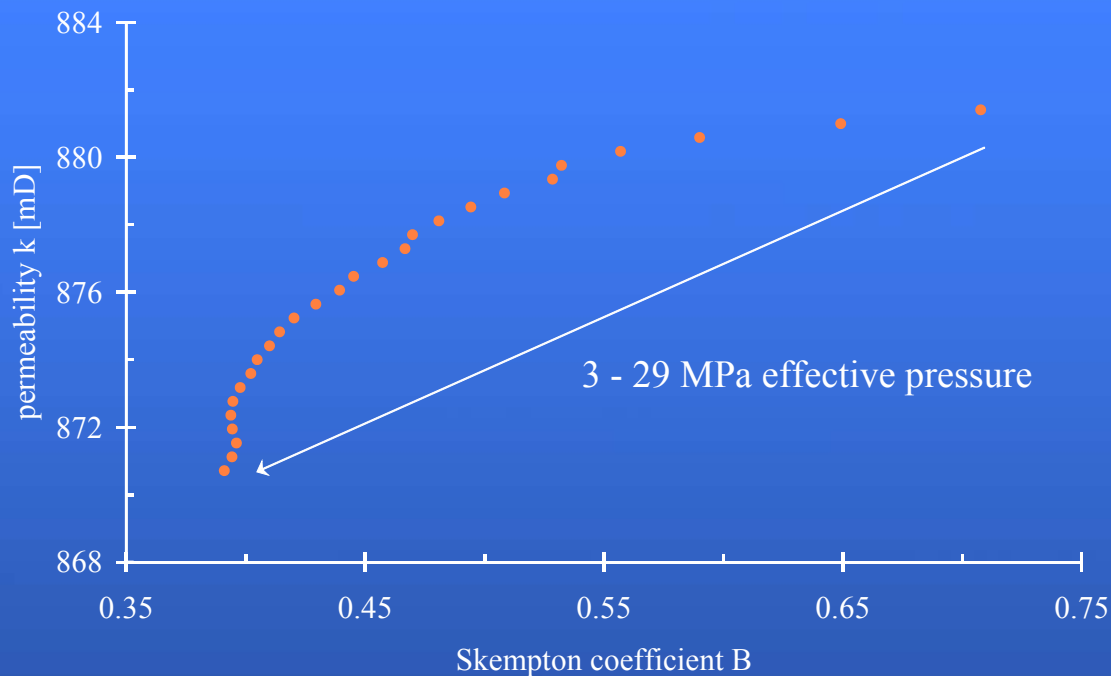
Continuous decrease of permeability and Skempton coefficient with effective pressure increase

Interpretation:

No change of the pore shape

Separation of pores

Cut-off of flow path leads to a change in permeability and Skempton coefficient



Observation:

Low circularity (irregular pore shapes)

Low pore cavity-throat-ratio

High decrease in Skempton coefficient at low effective pressure and no significant change in permeability

Interpretation:

Sensitive for poro-elastic deformation

No separation of pores

High poro-elastic deformation at low effective pressure. After stiffening of the frame work no further change in B and k.

Conclusion

- Two types of sandstone (**Flechtinger** and **Bentheimer**) were investigated
- Both samples show differences in effective pressure dependencies as expressed by their Skempton coefficient and permeability
- By means of a three pore type model in combination with a heterogeneous pore space geometry change a qualitative interpretation is possible

Future Work

- A quantification of the geometry change will be necessary
- A direct method to measure the geometry change due to effective pressure change must be developed
- Further experiments to validate the results of this work