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Nonlinear Dimming and Correlated Color Temperture Control of Bi-Color White LED Systems

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Abstract—This paper proposes a nonlinear approach of controlling the luminous intensity and correlated color temperature (CCT) of white light-emitting diode (LED) systems with dual color temperatures. This LED system is made up of a warm color LED source (2700 K) and a cool color LED source (5000 K). The luminous intensity of each of these LED sources is individually controlled by pulsewidth modulation. The overall intensity of the LED system is due to the combined emitted flux of both LED sources. Its overall CCT is the mixed average CCT of both LED sources. This proposed method is based on the nonlinear empirical luminous and CCT models of the LEDs, which take into consideration the thermal effect of LEDs on its luminance and CCT properties. With reasonable approximation, the theoretical models are simplified into practical solutions, which are translatable into real-life applications. It is experimentally validated that the proposed approach is considerably more accurate than existing linear approaches that do not consider color variations of LED sources. The idea is applicable to LED systems with multiple color temperatures and is not limited to white LEDs.

Index Terms—Lighting system, PWM driving, correlated color control (CCT), light-emitting diodes (LED), white LED

I. INTRODUCTION

The high-power light-emitting diode (LED) is considered an attractive candidate for replacing incandescent and fluorescent lightings for general energy-efficient illumination purpose. There are, however, various aspects that require attention when it comes to applying LEDs for general lighting. One such aspect is related to the LED's junction temperature, which critically affects its operating lifetime,

efficiency, and color properties, and must be properly considered when it comes to designing good-quality light sources [1], [2]. On the other hand, there is also primary concerns of having compatibly efficient and reliable LED ballasts. For this reason, most research works related to LED ballasts so far, have been focused on achieving high energy efficiency [3]–[8], good dimming properties [1], [2], [9]–[14], and high reliability through the avoidance of using electrolytic capacitors [15]–[21]. Recently, it has been pointed out that LEDs with flickering light might be detrimental to human health [22], [23]. Subsequently, a series of work related to achieving good ballast reliability without introducing visible and invisible low-frequency flickering have been reported [24]–[28].

Color perception of the LED light is also an important subject for research in LED systems. In terms of indoor applications, it is important to take into account the correlated color temperature (CCT) of the illumination. Warm-white light sources (i.e., lower CCT) are preferred in public areas to promote relaxation and cool-white light sources (i.e., higher CCT) are used to enhance concentration in offices [29], [30]. For more sophisticated applications as in museums, hotels, boutique shops, etc., a high level of CCT consistency between different lamps is an expectation. Unfortunately, CCT control and dimming is a difficult task in LED technology since binning, age, driving techniques, and temperature drift affect the CCT of the actual emitted light [2], [31]. Therefore, when designing LED ballasts for such applications, factors like the color property and its dimming control should be considered in addition to the basic requirements of achieving high efficiency and reliability. A resulting objective as such would be to achieve LED lamps that can maintain a constant CCT during brightness control and conversely that can maintain constant brightness during CCT adjustment.

Dimmable lamps that have adjustable CCT of wide ranges are currently in good demand [32]. Lamps with such a feature typically allows the continuous change of the CCT from a low value (warm white) to a high value (cool white). In particular, variable CCT LED lamps based on bi-color LED sources are a popular configuration [33], [34], and has been adopted in various products by the lighting industry. In this configuration, the lamp must comprise light sources with at least two distinct CCT values. In the case of LED lamps, an array of LEDs with low CCT (e.g. 2700 K) and an array of LEDs with high CCT (e.g. 5000 K) may be adopted in the product. If light of 2700 K is required, only LEDs with CCT of 2700 K are turned on. If light of 5000 K is required, only LEDs with CCT of 5000 K are

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turned on. Subsequently, for light of CCT between 2700 K and 5000 K, both arrays of LEDs are turned on and driven such that the overall combined light emitted from the lamp is of the required CCT value and brightness.

To perform smooth and continuous brightness control of the lamp, the luminous flux emitted by the individual LED array has to be adjusted. This adjustment can be achieved either by changing the amplitude level or the duty-cycle pulse, or by concurrently changing both the amplitude level and the duty-cycle pulse of the currents flowing through the LEDs [33], [34]. However, the CCT of an LED is dependent on both its junction temperature as well as the amplitude of its drive current [35], [36]. With the two LED sources within the lamp sharing the same heatsink and driven together, but individually controlled, there will be thermal influence of one LED source on the CCT property of the other. In other words, there is mutual thermal interdependence on the CCT of each LED source and such an effect should be carefully treated. For example, if the current of the warm-white LED source is reduced, its junction temperature will be reduced, thereby the heatsink will be cooler. This may indirectly reduce the junction temperature of its companion cool LED source and thereby changing the CCT of the cool-white source. The effect is vice versa for the warm LED source. Hence, the overall CCT control is affected.

Such factors should not be ignored in the design of the bi-color variable CCT white LED lamps. Otherwise, there will always be an undesired change of the CCT in the process of adjusting brightness regardless of the control approach adopted. It must be mentioned that a ± 200 K deviation within the desired CCT value is often cited as an acceptable error in electric lamps and is considered non eye-perceivable. Nevertheless, it is found that existing approaches do not take into consideration the abovementioned factors and possess huge perceivable CCT deviation within their CCT control [33], [34], as will be illustrated in the experimental works in the later section.

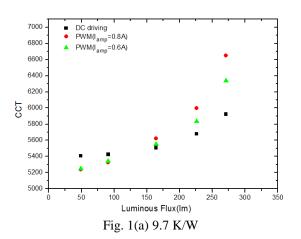
In view of this, the work in this paper is primarily targeted at achieving accurate dimming and CCT control of bi-color variable CCT LED lamps, through the use of a nonlinear empirical LED model that accounts the thermal interdependency effect of the two color sources and the actual imperfections of LEDs. The system described is based on a white LED lamp configured with LEDs of two different color temperatures, namely the 2700 K and 5000 K types of LEDs. Nevertheless, the idea is also applicable to LED systems with multiple color temperatures and is not limited to white LEDs. However, it must be emphasized that this proposed method [37] does not take into consideration the aging effect of LEDs, which can be mitigated through feedback sensor, and is beyond the scope of this discussion. Section II gives an overview of the existing issue of wide CCT variation of common phosphor-converted white LED during brightness control, and discusses why the linear approaches of controlling bi-color white LED lamps are still incapable of achieving satisfactory CCT control performance. Section III gives a description of the proposed nonlinear control approach. Section IV provides the experimental results and discussion. Finally, Section V gives the conclusion of the paper...

II. ISSUES OF PHOSPHOR-CONVERTED WHITE LED SYSTEMS

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A. Wide CCT Variation of Phosphor-Converted White LED Systems

Currently, the two most popular techniques of driving LEDs are DC drive and pulsewidth modulation (PWM) drive. In DC drive (also known as amplitude mode drive), the current driving the LED is a DC constant current, of which the luminous intensity of the LED is changed by varying the amplitude of current. In PWM drive, the current driving the LED is a current pulsating between constant amplitude and zero current. Brightness control of the LED is typically changed by varying the duty-cycle ratio of the pulsating current [22]. Due to the nonlinear I-V characteristic of the LED, PWM drive results in better linear control of the light intensity as compared to DC drive. However, driving LEDs using PWM techniques introduce additional efficacy loss that is otherwise not present with DC driving methods [9], [22]. This loss is converted into additional heat which further aggravates the undesired chromaticity-shifting trait of LEDs [2], [37]. The effect of dimming and heat on chromaticity shift of LEDs has been reported in [2], [37], [38]. In particular, with DC drive, the peak wavelength of LEDs shows a blue shift with increased light intensity (i.e., increased current level), which is attributed to the band filling and quantum confined stark effects [39]. With PWM drive, LEDs exhibit a red shift with increased light intensity (i.e., increased duty cycle), which is dominantly cause by the increase in junction heat [40]. Despite the various reports on the dimming effects of DC and PWM drives on the chromaticity property of LEDs in terms of peak-wavelength and CIE coordinates, as far as we know, no literature has been published comparing the effect of dimming on the CCT shift of phosphor-converted (PC) white LED for DC and PWM drives, under the same luminous flux output and with consideration to the use of different heatsinks sizes. Additionally, in order to further clarify the misconception that color consistency during dimming is better with PWM drive than DC drive, experimental results of a PC white LED in terms of the CCT versus the luminous flux for PWM drive and DC drive for different heatsinks, are given in Fig. 1.



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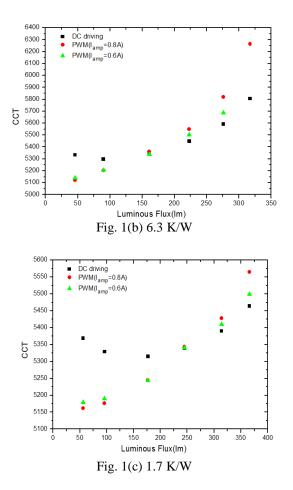


Fig. 1. Experimental results of CCT variation of PC white LEDs versus its luminous flux under DC drive with variable current amplitude and PWM driving methods with amplitude currents of 0.6 A and 0.8 A, under thermal resistance of (a) 9.7 K/W, (b) 6.3 K/W, and (c) 1.7 K/W.

In the experiments, both the DC and PWM drives are applied to the same LED (a Sharp 4.4 W, GW5BNC15L02) for fairness of comparison. Three sets of experiments, each with the LED mounted on a different heatsink, with thermal resistance of respectively 9.7 K/W (see Fig. 1(a)), 6.3 K/W (see Fig. 1(b)), and 1.7 K/W (see Fig. 1(c)) are performed. The ambient temperature is kept constant at 25 °C and the heatsink operates under free convection with no active temperature control¹. For each set of experiment, the DC drive and the PWM drive using amplitude currents of 0.6 A and 0.8 A are employed. The dimmable luminous-flux range of the LED with heatsink's thermal resistance of 9.7 K/W, 6.3 K/W, and 1.7 K/W are respectively from 50 lm to 270 lm, from 50 lm to 320 lm, and from 50 lm to 366 lm.

Table. 1. Experimental results of CCT variation of PC white LEDs versus its luminous flux under DC drive with variable current amplitude and PWM driving methods

¹ All experiments hereon are conducted at ambient temperature of 25 °C under free convection without active temperature control.

	Current amplitude(A)	Heatsink's thermal resistance(K/ W)	Dimmable luminous-fl ux range (lm)	CCT variatio n (K)
	0.6	9.7	50-270	1088
PW	0.8	9.7	50-270	1413
Pw M	0.6	6.3	50-320	548
drive	0.8	6.3	50-320	697
unve	0.6	1.7	50-366	325
	0.8	1.7	50-366	403
DC	-	9.7	50-270	514
drive	-	6.3	50-320	245
anve	-	1.7	50-366	149

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As shown in Fig. 1(a) and Table. 1, the experimental results are 149 K (DC drive), 403 K (PWM, 0.8 A amplitude), and 325 K (PWM, 0.6 A amplitude). Experimental results showed that the CCT variation under PWM drive is much larger than that under DC drive. Also, in all cases of PWM drive, the CCT variation is eye-perceivable when the LED is fully dimmed since the variations are all greater than 200 K. For DC drive, CCT variation is non-perceivable when the heatsink is very large with a thermal resistance of 1.7 K/W. Otherwise, CCT variation of LEDs under DC drive is still perceivable during full range dimming when mounted on more regular sized heatsinks. Note that the analyses above are true for cool-white PC LED, of which the CCT is high and widely varied. In the case of warm-white PC LED of which the CCT is low, the CCT variation is typically small and non-perceivable during dimming. Nevertheless, in applications requiring cool color of a constant CCT during dimming, the single-colored cool-white PC LED array, regardless of the driving method, will be inapplicable. In such circumstances, the bi-color white LED system with automatic CCT control may be adopted. In addition, a bi-color white LED system also allows wide CCT adjustment and light intensity control, which is unachievable with the single-colored type of PC LED systems.

B. Existing Linear Control Approaches for Bi-Color Variable CCT White LED Systems

In general, the bi-color variable CCT white LED systems comprise two LED sources, with each emitting light of a different CCT [33], [34]. The system includes a controller which allows the adjustment of the overall light intensity and CCT of the lamp. This is dictated through the individual adjustment of the light intensity of each LED array. Currently, approaches adopted in performing the CCT mixing in such lamps with bi-color LED sources are generally based on simple linear CCT averaging of the two LED sources. For example, in the method proposed in [33], lights of the two LED sources are mixed to give a desired CCT by controlling the proportion of the emitted light of each respective source. In the method proposed in [34], the two LED sources are placed in anti-parallel manner such the anode of one LED source is connected to the cathode of the other LED source and vice versa. Current flowing in one direction turns on the first LED

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source and current flowing in the opposite direction turns on the second LED source. A controller manages the control of the CCT by adjusting the duty ratio of an alternating current flowing through the two LEDs to control the CCT and/or the brightness of the lighting apparatus.

In both these approaches, the control of the CCT and flux of the LED lamp is based on the mathematical expression

$$\begin{cases} CCT_{_{M}} = CCT_{_{W}}D + CCT_{_{C}}(1-D) = CCT_{_{W}}\frac{\phi_{_{W}}}{\phi_{_{W}} + \phi_{_{C}}} + CCT_{_{C}}\frac{\phi_{_{C}}}{\phi_{_{W}} + \phi_{_{C}}} \\ \phi_{_{M}} = \phi_{_{W}} + \phi_{_{C}} \end{cases}$$
(1)

where $CCT_{\rm M}$ and $\phi_{\rm M}$ are respectively the CCT value and overall flux of the total light mixture from the lamp, $\phi_{\rm W}$ and $CCT_{\rm W}$ are respectively the averaged luminous flux and CCT value of the warm-white LED source, $\phi_{\rm C}$ and $CCT_{\rm C}$ are respectively the luminous flux and CCT value of the cool-white LED source, and *D* is the ratio of the averaged emitted warm color light flux $\phi_{\rm W}$ over the total light flux of the lamp (i.e., $\phi_{\rm W} + \phi_{\rm C}$). Here, $CCT_{\rm W}$ and $CCT_{\rm C}$ are assumed to be constant, which is untrue in practice. Due to this assumption, $CCT_{\rm M}$ is a simple linear combination of $CCT_{\rm W}$ and $CCT_{\rm C}$ with regards to the change of *D*, and for this reason, approaches of this nature are all fundamentally linear approaches.

The main problem with linear approaches are that they are rather simplistic considering that non-ideal characteristics such as the effect of temperature change on CCT and luminance, and the thermal interdependency effect between the two LED sources, are all neglected. Without proper consideration to the actual dynamics of luminous flux, CCT, current, temperature, and duty cycle change, the achievable CCT control will be highly inaccurate. Such errors are significant especially if wide-range dimming and CCT control are required since the temperature variation in such operations are large. Figs. 2 and 3 give the experimental proofs of the stated problem.

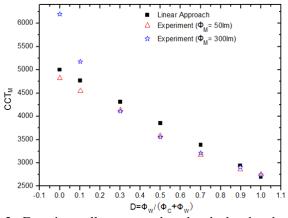


Fig. 2. Experimentally measured and calculated values of CCT_M of bi-color white LED system at different *D* for $\phi_M = 50$ lm and $\phi_M = 300$ lm.

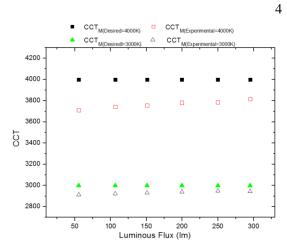


Fig. 3. Experimentally measured values of CCT_M for different luminous flux ϕ_M for two preset CCT references of $CCT_{M(Desired)} = 3000$ K and 4000 K under the linear approach.

In the experiments, a cool-white PC LED (Sharp GW5BNC15L02) and a warm-white PC LED (Sharp GW5BTF27K00) making up the bi-color white LED lamp are mounted on a heatsink with thermal resistance of 6.3 K/W and driven by DC currents. According to the datasheets provided, the typical CCT of GW5BNC15L02 is 5000 K and that of GW5BTF27K00 is 2700 K. For linear approaches, these will be the values adopted for the CCT of the respective sources, that is, $CCT_{\rm C} = 5000$ K and $CCT_{\rm W} = 2700$ K.

Fig. 2 shows the results of the experiment conducted to measure the CCT value of the lamp, i.e., CCT_M , for different *D* and at two different luminance levels of $\phi_M = 50 \text{ Im and } \phi_M = 300 \text{ Im}$. The results plotted as "Linear Approach" is that calculated using equation (1). Predictably, with linear approaches, the value of CCT_M reduces linearly with an increasing *D*, irrespective of the luminance level of the lamp. However, the measured CCT value of the lamp shows otherwise. Not only does CCT_M differ at different luminance levels, they do not change linearly with *D*. Moreover, at high level of CCT and high luminance level, the CCT deviation is higher. A maximum CCT error of 1400 K is found at D = 0 and $\phi_M = 300 \text{ Im}$.

Table. 2. Experimental and desired CCT for different luminous flux

Bi-colo r white LED lamp	CCT _{M(Desired}) (K)	D	Luminou s Flux (lm)	CCT _{M(Experimental}) (K)
$CCT_{\rm C} =$	3000	0.86	50 and	2913 and 2946
5000 K,		9	300	
$CCT_{\rm W} =$	4000	0.43	50 and	3710 and 3814
2700 K		4	300	

Fig. 3 and Table 2 show the results of how the CCT value of the lamp changes with the change in luminance level.. By using these values in the adjustment of the luminance level of the individual LED sources and then measuring the value of CCT_M , it is evident from the data that there is some deviation between the desired CCT and the actual experimental CCT of

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the lamp. In the following section, a nonlinear dimming and CCT approach is proposed to reduce these errors in the control of the lamp.

III. PROPOSED NONLINEAR DIMMING AND CCT CONTROL APPROACH

The essence of the proposed nonlinear dimming and CCT control approach is that by taking into consideration CCT_W , CCT_C , ϕ_C , and ϕ_W are all nonlinear functions of current level, duty ratio, junction temperature, heatsink's thermal resistance, and the thermal interdependency effect of the two LED sources, a more precise dimming and CCT control performance is achievable.

A. Nonlinear CCT function of Bi-Color Variable CCT White LED Systems

According to colorimetry, the relationship between the tristimulus values (X, Y, Z) and chromaticity (x, y, z) of a light source can be written as

$$\begin{cases} x = \frac{X}{X + Y + Z} \\ y = \frac{Y}{X + Y + Z} \\ z = \frac{Z}{X + Y + Z} \end{cases}$$
(2)

Equation (2) can be rewritten as

$$\frac{X}{x} = \frac{Y}{y} = \frac{Z}{z} = X + Y + Z \tag{3}$$

or

$$\begin{cases} X = \frac{x}{y}Y\\ Z = \frac{z}{y}Y = \frac{1 - x - y}{y}Y \end{cases}$$
(4)

If the tristimulus values for the warm-white LED source is (X_W, Y_W, Z_W) and for the cool-white LED source is (X_C, Y_C, Z_C) , the overall tristimulus values of the light emitted from the bi-color LED lamp, which is the sum of the respective sources, is

$$\begin{cases} X_M = X_W + X_C \\ Y_M = Y_W + Y_C \\ Z_M = Z_W + Z_C \end{cases}$$
(5)

Therefore, the overall chromaticity coordinates of the bi-color LED system are given by

$$\begin{aligned} x_{M} &= \frac{X_{M}}{X_{M} + Y_{M} + Z_{M}} = \frac{X_{W} + X_{C}}{X_{W} + X_{C} + Y_{W} + Y_{C} + Z_{W} + Z_{C}} \\ &= \frac{X_{W} + X_{C}}{X_{W} + X_{C} + \frac{y_{w}}{x_{w}}} X_{W} + \frac{y_{C}}{x_{C}} X_{C} + \frac{1 - x_{w} - y_{w}}{x_{w}} X_{W} + \frac{1 - x_{c} - y_{c}}{x_{c}} X_{C} \\ &= \frac{X_{W} + X_{C}}{\frac{X_{W}}{x_{w}} + \frac{X_{C}}{x_{c}}} \end{aligned}$$
(6.1)

$$y_{M} = \frac{Y_{M}}{X_{M} + Y_{M} + Z_{M}} = \frac{Y_{W} + Y_{C}}{X_{W} + X_{C} + Y_{W} + Y_{C} + Z_{W} + Z_{C}}$$

$$= \frac{Y_{W} + Y_{C}}{\frac{x_{w}}{y_{w}}Y_{W} + \frac{x_{c}}{y_{c}}Y_{C} + Y_{W} + Y_{C} + \frac{1 - x_{w} - y_{w}}{y_{w}}Y_{W} + \frac{1 - x_{c} - y_{c}}{y_{c}}Y_{C}}$$

$$= \frac{Y_{W} + Y_{C}}{\frac{Y_{W} + Y_{C}}{y_{w}} + \frac{Y_{C}}{y_{c}}}$$
(6.2)

Since the tristimulus value Y represents luminance, which is a proportional to the luminous flux Φ_{ν} , and chromaticity y can be approximated as being proportional to CCT, as shown in Fig 4, therefore, equation (6.2) can be rewritten as

$$CCT_{M} = \frac{\phi_{W} + \phi_{C}}{\frac{\phi_{W}}{CCT_{W}} + \frac{\phi_{C}}{CCT_{C}}}$$
(7)

Equation (7) represents a nonlinear function of the mixed CCT_M linking luminous flux and CCT of individual LED sources together with that of the mixed light, for a general bi-color white LED system. Unlike in linear approaches based on equation (1) of which CCT_W and CCT_C are assumed constant, here CCT_W and CCT_C are functions of its operating conditions, i.e., current, junction temperature, and ratio D. This is important since in practice, the CCT of an LED source is highly dependent on its junction temperature and current amplitude.

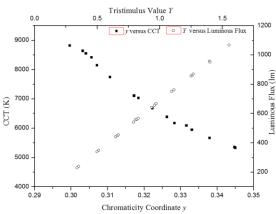


Fig. 4. Measured tristimulus value *Y* versus luminous flux and measured chromaticity coordinate *y* versus CCT.

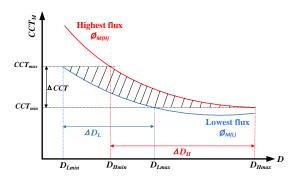


Fig. 5. Typical nonlinear CCT behavior of the bi-color white LED system for different *D* at high and low luminous flux.

Fig. 5 depicts the typical nonlinear CCT behavior of a bi-color white LED system for different values of $D = \phi_w/(\phi_w + \phi_c)$ with its highest and lowest total luminous flux, i.e., $\phi_{M(H)}$ and $\phi_{M(L)}$, respectively. As illustrated in the diagram, full range dimming (from $\phi_{M(H)}$ to $\phi_{M(L)}$) and CCT control of the lamp is achievable only for the range ΔCCT (from CCT_{min} to CCT_{max}) through the ratio range of ΔD_L (from D_{Lmin} to D_{Lmax}) in the case of the lowest flux and ΔD_H (from D_{Hmin} to D_{Hmax}) in the case of the highest flux. This is represented by the shaded area in the figure. No dimming actions can be performed at CCT below CCT_{min} and that above CCT_{max} , and that the CCT range is restricted within these values. These boundaries represent the operational dimming and CCT limits of a dimmable bi-color variable CCT white LED lamp.

B. Empirical Luminous Model of the LEDs in the Bi-Color White LED Lamp

It is known that the junction temperature of an LED affects its luminous efficacy and CCT. Typically, the junction temperature of an LED is affected by its current level, driving technique, heatsink size, and ambient temperature. In the case of the bi-color white LED lamp, the junction temperature of the cool-white LED source will be affected by the operating state of the warm-white LED source since heat of the latter will affect the temperature of the heatsink, which in turns affect the junction temperature of the former, and this is conversely true. Such a thermal interdependency effect will be accounted in the proposed empirical luminous and CCT models.

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(i). Experimental Measurement: The luminous models are built upon results obtained from the LED sources through the following experimental steps. Firstly, with both the cool-white and warm-white LED sources mounted on the same heatsink, the current amplitude of both sources are set at 0.5 A. For both sources, PWM drive is adopted. Then, the warm-white LED is covered using a black rubber which prevents its luminous flux from being emitted into space. What this means is that when the warm-white LED is driven, it only contributes thermal energy into the heatsink. Since the minimum and maximum thermal energy that the warm-white LED can contribute to the LED lamp are generated when it is fully turned off at $D_W = 0$ and when it is fully turned on at $D_W = 1$, respectively, the measurement of the luminous characteristic of the cool-white LED with regards to the operating condition of the warm-white LED will be performed for both these boundary conditions. Fig. 6(a) shows the luminous flux versus duty ratio D_C of the cool-white LED in both conditions of $D_W = 0$ and $D_W = 1$. Clearly, the maximum and minimum luminous flux emission from the cool-white occurs at respectively $D_W = 0$ and $D_W = 1$ as heat energy contribution by the warm-white LED is respectively at its lowest and highest. The operating range of the cool-white LED at different operating condition of the warm-white LED (i.e., $0 < D_W < 1$) should occur between maximum and minimum curves. By swopping the placement of the black rubber onto the cool-white LED, the same measurement process is repeated on the warm-white LED. Fig. 6(b) shows the luminous flux versus duty ratio D_W of the warm-white LED in both conditions of $D_C = 0$ (cool-white turned off) and $D_C = 1$ (cool-white fully turned on).

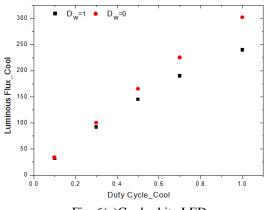


Fig. 6(a)Cool-white LED

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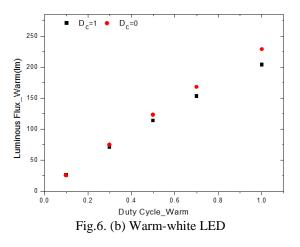


Fig. 6. Experimental values of luminous flux of the (a) cool-white LED when the warm-white LED is fully off at $D_W = 0$ and fully on at $D_W = 1$ and (b) warm-white LED when the cool-white LED is fully off at $D_C = 0$ and fully on at $D_C = 1$.

(*ii*) *Exponential Function Curve Fitting:* Careful observation of the results shows that the luminous flux characteristics of the cool-white LED with consideration to the thermal contribution from the warm-white LED (as given in Fig. 6(a)) can be modeled using an exponential function of the following form

$$\phi_C = \phi_{C0} - \alpha_C e^{\beta_C D_C} \tag{8a}$$

where ϕ_c is luminous flux of cool-white LED, ϕ_{c0} and α_c are constant parameters derivable from measurement, and β_c is a variable related to the duty cycle of warm-white LED, i.e., D_W . Likewise, the characteristics of the warm-white LED can be expressed as

$$\phi_W = \phi_{W0} - \alpha_W e^{\beta_W D_W} \tag{8b}$$

Both equations (8a) and (8b) can be rewritten as

$$\ln[\phi_{C0} - \phi_C] = \beta_C D_C + \ln \alpha_C \tag{9a}$$

$$\ln[\phi_{W0} - \phi_W] = \beta_W D_W + \ln \alpha_W \tag{9b}$$

Clearly, for any fixed β_c , the luminous flux variation of $\ln[\phi_{C0} - \phi_c]$ is a linear function of $D_c \cdot \beta_c$ is a negative parameter that describes the rate of reduction in $\ln[\phi_{C0} - \phi_c]$ with respect to an increasing D_c . For this cool-white LED sample, ϕ_{c0} is around 500 lm. The rule of thumb for choosing ϕ_{c0} is to set it at $3 \times \phi_c$ when $D_c = 0.5$. As illustrated in Fig. 7, the experimental values of $\ln[\phi_{c0} - \phi_c]$ against the change of D_c is basically linear for both cases of $D_W = 0$ and $D_W = 1$. Similarly, by setting $\phi_{W0} = 370 \text{ Im} (3 \times \phi_W (D_W = 0.5))$, the experimental values of $\ln[\phi_{W0} - \phi_W]$ against the change of D_W can be calculated for both cases of $D_c = 0$ and $D_c = 1$, and are plotted as shown in Fig. 8. The linear relationship of $\ln[\phi_{W0} - \phi_W]$ against D_W is observed.

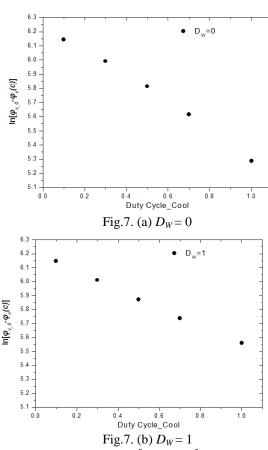


Fig. 7. Experimental values of $\ln[\phi_{C0} - \phi_C]$ against duty cycle for the cool-white LED at (a) $D_W = 0$ and (b) $D_W = 1$.

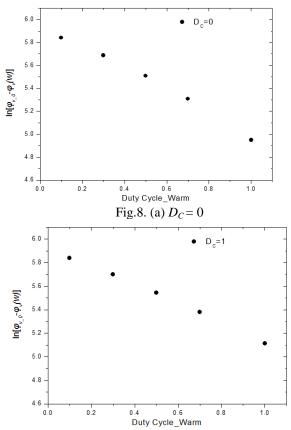


Fig. 8. (b) $D_C = 1$ Fig. 8. Experimental values of $\ln[\phi_{W0} - \phi_W]$ against duty cycle for the warm-white LED at (a) $D_C = 0$ and (b) $D_C = 1$.

The results given in Figs. 7 and 8 can be fitted into straight lines and assume the expressions given in (9a) and (9b), respectively. Both the fitted lines in Figs. 7(a) and 7(b) cross the y axis at the same constant point $\ln \alpha_{c}$ (cool-white LED) and that of Figs. 8(a) and 8(b) at $\ln \alpha_W$ (warm-white LED). The values of α_C and α_W can be derived from these results. The gradient of each of these lines represents the value of β_x , of which in the case of the cool-white LED source, an operating range of $D_{W,min} \leq D_W \leq D_{W,max}$ for its companion warm-white LED source will generate a range of gradient values of $\beta_{C,min} \leq \beta_C \leq \beta_{C,max}$. Likewise, for the warm-white LED source, an operating range of $D_{C,min} \leq D_C \leq D_{C,max}$ for its companion cool-white LED source will generate a range of gradient values of $\beta_{W,min} \leq \beta_W \leq \beta_{W,max}$. Through the linear association of D_W with β_C and D_C with β_W , the luminous flux expression of the cool-white and warm-white LED sources with respect to D_C and D_W can be respectively expressed as

$$\phi_{c}(D_{C}, D_{W}) = \phi_{C0} - \alpha_{C} \exp\left\{ \begin{bmatrix} \left(\beta_{C,\max} - \beta_{C,\min}\right) \\ \left(D_{W,\max} - D_{W,\min}\right) \right) \\ \left(D_{W} - D_{W,\min}\right) + \beta_{C,\min} \end{bmatrix} D_{C} \right\}$$
(10a)
$$\phi_{W}(D_{C}, D_{W}) = \phi_{W0} - \alpha_{W} \exp\left\{ \begin{bmatrix} \left(\beta_{W,\max} - \beta_{W,\min}\right) \\ \left(D_{C,\max} - D_{C,\min}\right) \right) \\ \left(D_{C} - D_{C,\min}\right) + \beta_{W,\min} \end{bmatrix} D_{W} \right\}$$
(10b)

Equation (10a) gives the luminous flux of the cool-white LED at any D_C and D_W value, of which D_W contributes to the thermal energy affecting the junction temperature of the cool-white LED. Here, the gradient β_C for any D_W is obtained through the linear interpolation of $\beta_{C,max}$ and $\beta_{C,min}$. Equation (10b) is the counterpart equation for the warm-white LED.

(iii) Model Validation: From the experimental results given in Fig. 7, the parameters derived are $\phi_{C0} = 500$, $\alpha_C = 503$, $\beta_{C,max} = -0.657$, $\beta_{C,min} = -0.954$, $D_{W,max} = 1$, $D_{W,min} = 0$. Fitting these values into equation (10a), the luminous flux for the cool-white LED can be predicted for any D_C and D_W . Fig. 9 gives a comparison of the experimentally measured flux and that calculated using equation (10a). The maximum discrepancy between the two is around 13.2% and it occurs at $D_C = 0.3$ and $D_W = 1$. The minimum discrepancy is around 0.14% and it occurs at $D_C = 0.7$ and $D_W = 0$. The averaged discrepancy between the measured and calculated results is around 5.2%. Therefore, it is concluded that the proposed mathematical model is in good agreement with the actual luminous characteristic of the cool-white LED source in the bi-color lamp.

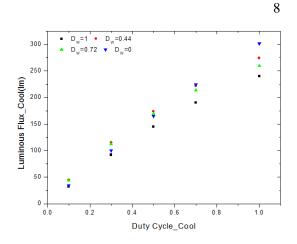


Fig.9. (a) Measured

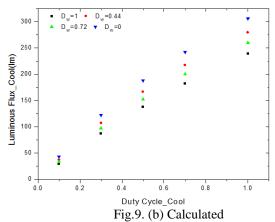


Fig. 9. (a) Measured luminous flux and (b) calculated luminous flux of cool-white LED at different D_C and D_W .

From the experimental results given in Fig. 8, the parameters derived are $\phi_{W0} = 370$, $\alpha_W = 376$, $\beta_{W,max} = -0.810$, $\beta_{W,min} = -0.992$, $D_{C,max} = 1$, $D_{C,min} = 0$. Fitting these values into equation (10b), the luminous flux for the warm-white LED can be predicted for any D_C and D_W . Fig. 10 gives a comparison of the experimentally measured flux and that calculated using equation (10b). The maximum discrepancy between the two is around 14.7% and it occurs at $D_C = 0$ and $D_W = 0.1$. The minimum discrepancy is around 0.6% and it occurs at $D_C = 1$ and $D_W = 1$. The averaged discrepancy between the measured and calculated results is around 4.5%. Therefore, it is concluded that the proposed mathematical model is in good agreement with the actual luminous characteristic of the warm-white LED source in the bi-color lamp.

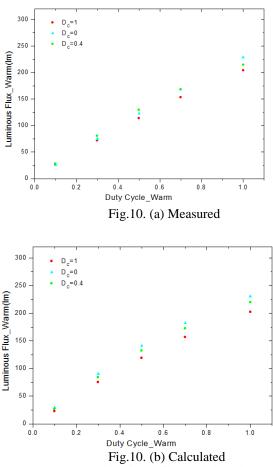


Fig. 10. (a) Measured luminous flux and (b) calculated luminous flux of warm-white LED at different D_C and D_W .

C. Empirical Correlated Color Temperature (CCT) Model of the LEDs in the Bi-Color White LED Lamp

Similar to the luminous model, the thermal interdependency effect of each LED source on the other will be accounted in the proposed empirical CCT model.

(*i*) *Cool-White LED*: With the warm-white LED covered by a black rubber, the maximum and minimum CCT values of the cool-white LED (i.e, $CCT_{C,max}$ and $CCT_{C,min}$) are measured as a function of the total duty ratio D_T , where $0 \le D_T = D_C + D_W \le 2$. For any value of D_T , there are two combinations of D_C and D_W that will each result in a maximum and a minimum CCT value. To obtain the plot of maximum CCT against D_T , the following equation is considered.

$$(D_C, D_W)_{CCT_{C,\text{max}}} = \begin{cases} D_C = D_T, D_W = 0; & \text{if } D_T \le 1\\ D_C = 1, D_W = D_T - 1; & \text{if } D_T > 1 \end{cases}$$
(11a)

To measure the minimum CCT plot against D_T , the following equation is considered.

$$(D_C, D_W)_{CCT_{C,\min}} = \begin{cases} D_C = 0.1, D_W = D_T - 0.1; & \text{if } D_T \le 1 \\ D_C = D_T - 1, D_W = 1; & \text{if } D_T > 1 \end{cases}$$

9

....

(11b) nd minimum CCT, the

With the measured maximum and minimum CCT, the averaged CCT of the cool-white LED at any D_T can be calculated using

$$CCT_{C,\text{ave(measured)}}(D_T) = \frac{CCT_{C,\max(D_T)} + CCT_{C,\min(D_T)}}{2} \quad (12)$$

Fig. 11 shows a plot of the averaged CCT that is calculated from the measured maximum and minimum CCT using equation (12). Clearly, the graph can be modeled using piecewise linear equations and for this case, the plot is fitted using three straight lines.

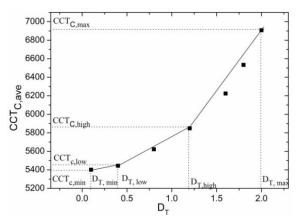


Fig. 11. Plot of the averaged CCT against D_T of the cool-white LED fitted by three straight lines.

For the modeling of the averaged CCT using piecewise linear solution as that given in Fig. 11, the following expression can be adopted.

$$CCT_{C,ave(calculated)} \left(D_T \right) = \begin{cases} \frac{CCT_{C,Jow} - CCT_{C,\min}}{D_{T,Jow} - D_{T,\min}} \left(D_T - D_{T,\min} \right) + CCT_{c,\min} & \text{if } D_{T,\min} \le D_T < D_{T,Jow} \\ \frac{CCT_{C,high} - CCT_{C,low}}{D_{T,high} - D_{T,low}} \left(D_T - D_{T,low} \right) + CCT_{c,low} & \text{if } D_{T,low} \le D_T < D_{T,high} \\ \vdots \\ \frac{CCT_{C,\max} - CCT_{C,high}}{D_{T,\max} - D_{T,high}} \left(D_T - D_{T,high} \right) + CCT_{c,high} & \text{if } D_{T,high} \le D_T \le D_{T,\max} \end{cases}$$

$$(13)$$

On the other hand, if a more accurate CCT model of the LED is desired, polynomial curve fitting may be used, which will lead to a mathematical expression of this general form

$$CCT_{C,\text{ave}(calculated)}(D_T) = \alpha D_T^2 + \beta D_T + \gamma$$
(14)

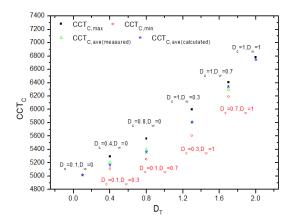


Fig. 12. Measured and calculated CCT of the cool-white LED against D_T .

Fig. 12 shows the graphs of the measured $CCT_{C,max}(D_T)$ and $CCT_{C,min}(D_T)$ of the cool-white LED, and their averaged values $CCT_{C,ave(measured)}(D_T)$ (obtained from equation (12)) and $CCT_{C,ave(calculated)}(D_T)$ (obtained from equation (13)). The maximum and minimum difference between $CCT_{C,ave(measured)}(D_T)$ and $CCT_{C,max}(D_T)$ is about 143 K (at $D_T = 1.3$) and 36 K (at $D_T = 0.4$), respectively. Their averaged difference is about 62 K. Since the variations are considerably small (within the perceivable range of 200 K), the averaged CCT data, i.e., $CCT_{C,ave(measured)}(D_T)$ can be used as a simplified representation of the actual CCT characteristics of the cool-white LED. This eases the actual implementation of the control with negligible effect on the quality of its performance. With this as the basis, the parameters can be extracted from the graph of $CCT_{C,ave(measured)}(D_T)$, as shown in Table 3, and then formulate the correlated mathematical expression representing the CCT characteristic of the cool-white LED. A plot of the CCT value based on equation (13) 12 given in Fig. and is represented by is $CCT_{C,ave(calculated)}(D_T)$ It is clear that both . $CCT_{C,ave(measured)}(D_T)$ and $CCT_{C,ave(calculated)}(D_T)$ are in good agreement with negligible discrepancy. Hence, equation (13) can be used for the CCT control of the cool-white LED.

Table. 3. The required parameters in (13) for cool-white LED

$D_{T,}$ min	D _{T,} low	D _{T,} high	D _{T,} max	CCT _{C,min} (K)	CCT _{C,low} (K)	CCT _{C,high}	CCT _{C,max}
0.1	0.4	1.1	2	5017	5114	5543	6747

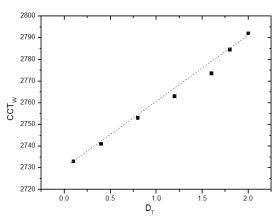
(*ii*) *Warm-White LED*: Likewise, with the cool-white LED covered by the black rubber, the maximum and minimum CCT values of the warm-white LED (i.e, $CCT_{W,max}$ and $CCT_{W,min}$) are measured as a function of the total duty ratio D_T , where $0 \le D_T = D_C + D_W \le 2$. To obtain the plots of maximum and minimum CCT against D_T , the following equations for setting the duty ratios of the cool-white and warm-white LEDs are considered.

$$(D_C, D_W)_{CCT_{W,max}} = \begin{cases} D_W = D_T, D_C = 0; & \text{if } D_T \le 1\\ D_W = 1, D_C = D_T - 1; & \text{if } D_T > 1 \end{cases}$$
(15a)

$$(D_C, D_W)_{CCT_{W,\min}} = \begin{cases} D_W = 0.1, D_C = D_T - 0.1; & \text{if } D_T \le 1 \\ D_W = D_T - 1, D_C = 1; & \text{if } D_T > 1 \end{cases}$$
(15b)

Then, the averaged CCT of the warm-white LED can be calculated from

$$CCT_{W,\text{ave}(\text{measured})}(D_T) = \frac{CCT_{W,\max(D_T)} + CCT_{W,\min(D_T)}}{2} \quad (16)$$



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Fig. 13. Plot of the averaged CCT against D_T of the warm-white LED fitted by a single straight line.

Fig. 13 shows a graph of the averaged CCT of the warm-white LED that is calculated from the measured maximum and minimum CCT using equation (16). As shown in the figure, the variation of the graph is relatively small and it can be modeled using a straight line with the following expression

$$CCT_{W,\text{ave}(calculated})(D_T) = \frac{CCT_{W,\text{max}} - CCT_{W,\text{min}}}{D_{T,\text{max}} - D_{T,\text{min}}} (D_T - D_{T,\text{min}}) + CCT_{W,\text{min}}$$
(17)

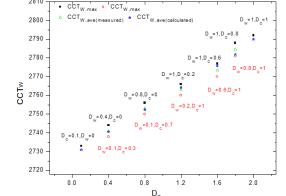


Fig. 14. Measured and calculated CCT of the cool-white LED against D_T .

Fig. 14 shows the graphs of the measured $CCT_{W,max}(D_T)$ and $CCT_{W,min}(D_T)$ of the warm-white LED, and their averaged values $CCT_{W,ave(measured)}(D_T)$ (obtained from equation (16)) and $CCT_{W,ave(calculated)}(D_T)$ (obtained from equation (17)). The maximum difference between $CCT_{W,ave(measured)}(D_T)$ and $CCT_{W,max}(D_T)$ is about 6 K (at $D_T = 0.8$). Therefore, the averaged CCT data, i.e., $CCT_{W,ave(measured)}(D_T)$ can be used as to represent the actual CCT characteristics of the warm-white LED. The required parameters in (17), can be extracted from the graph of $CCT_{W,ave(measured)}(D_T)$, as shown in Table 4, then formulate the correlated mathematical expression representing the CCT characteristic of the warm-white LED. A plot of the CCT value based on equation (17) is given in Fig. 14 and is represented by $CCT_{W,ave(calculated)}(D_T)$. It is clear that both $CCT_{W.ave(measured)}(D_T)$ and $CCT_{W,ave(calculated)}(D_T)$ are in

good agreement with negligible discrepancy. Hence, equation (17) can be used for the CCT control of the warm-white LED.

Table. 4. The required parameters in (17) for warm-white

LED				
$D_{T,min}$	$D_{T,max}$	$CCT_{C,min}(K)$	$CCT_{C,max}(K)$	
0.1	2	2733	2792	

D. Complete Luminous and CCT Model of the Bi-Color White LED Source Lamp

The total luminous flux $\phi_M(D_c, D_w)$ of the bi-color LED system is the combined luminous flux of both the warm-white and the cool-white LED and by considering (10a) and (10b), the equation can be expressed as $\phi_M(D_v, D_v) = \phi_M(D_v, D_v) + \phi_M(D_v, D_v)$

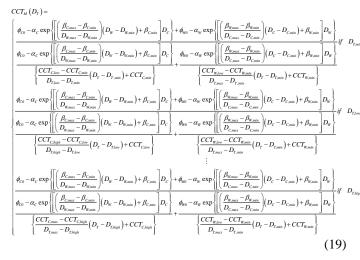
$$\phi_{M} \left(D_{C}, D_{W} \right) = \phi_{C} \left(D_{C}, D_{W} \right) + \phi_{W} \left(D_{C}, D_{W} \right)$$

$$= \phi_{C0} - \alpha_{C} \exp \left\{ \left[\frac{\left(\beta_{C, \max} - \beta_{C, \min} \right)}{\left(D_{W, \max} - D_{W, \min} \right)} \left(D_{W} - D_{W, \min} \right) + \beta_{C, \min} \right] D_{C} \right\}$$

$$+ \phi_{W0} - \alpha_{W} \exp \left\{ \left[\frac{\left(\beta_{W, \max} - \beta_{W, \min} \right)}{\left(D_{C, \max} - D_{C, \min} \right)} \left(D_{C} - D_{C, \min} \right) + \beta_{W, \min} \right] D_{W} \right\}$$

$$(18)$$

Considering that the CCT of the cool-white LED and the warm-white LED are represented by linear regions as shown in (13) and (17), the mixed CCT_M of the bi-color LED system given in (7) can be expressed as



IV RESULTS AND DISCUSSIONS

In this section, the results on the application of the nonlinear dimming and CCT control based on the developed empirical CCT and luminous models versus that of the conventional linear approach is reported.

A. Experimental Setup

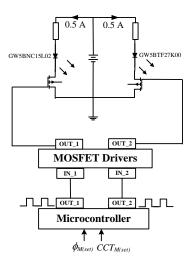


Fig. 15. Basic diagram of the experimental circuit.

Fig. 15 shows the basic diagram of the experimental circuit. With the desired flux $\phi_{M(set)}$ and correlated color temperature $CCT_{M(set)}$ being input into the circuit, the microcontroller (STC 11F60XE-35I-PLCC44) which includes a software numerical solver, will generate two individual PWM signals feeding the MOSFET switches through the MOSFET drivers (MC33512), for dimming the cool-white LED (GW5BNC15L02) and the warm-white LED (GW5BTF27K00) to perform the necessary control. The current amplitude of the cool-white and warm-white LEDs are set precisely at 0.5 A and 0.5 A. Both the LEDs are mounted on the same heatsink which has a thermal resistance of 6.3 K/W. The combined light of both LED sources if ferms of the overall ϕ_M and CCT_M are measured using a PMS-50 Spectro-Photocolorimeter.

B. Numerical Solver <u>B.</u> <u>1</u> For Sharp LED samples

The purpose of the software numerical solver is to generate the required duty ratio D_c and D_W for the bi-color lamp to produce the required CCT and flux according to the input values of $\phi_{M(set)}$ and $CCT_{M(set)}$.

The substitution of the parameters $\phi_{C0} = 500, \phi_{W0} = 370, \alpha_C = 503, \alpha_W = 376, \beta_{C,max} = -0.657, \beta_{C,min} = -0.954, D_{W,max} = 1, D_{W,min} = 0, \beta_{W,max} = -0.81, \beta_{W,min} = -0.992, D_{C,max} = 1, D_{C,min} = 0, D_{T,min} = 0.1, D_{T,low} = 0.4, D_{T,high} = 1.1, D_{T,max} = 2, CCT_{C,min} = 5017, CCT_{C,low} = 5114, CCT_{C,high} = 5543, CCT_{C,max} = 6747, CCT_{W,min} = 2733$, and $CCT_{C,max} = 2792$, which are obtained in the previous sections into equations (18) and (19) give respectively

$$\phi_{M}(D_{C}, D_{W}) = 870 - 503 \exp[(0.297D_{W} - 0.954)D_{C}]$$
(20)
-376 exp[(0.182D_{C} - 0.992)D_{W}]

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$$\begin{aligned} & \left[\frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]+370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{323D_{r}+4984} if \quad D_{T,min} \leq D_{T} \leq D_{T,lo} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{323D_{r}+4984} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,low} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{613D_{r}+4868} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,low} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{613D_{r}+4868} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,low} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right] + 370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.182D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{370-376\exp\left[(0.18D_{C}-0.992)D_{W}\right]}{53.6D_{r}+2728} if \quad D_{T,low} \leq D_{T} \leq D_{T,m} \right] \\ & \frac{500-503\exp\left[(0.297D_{W}-0.954)D_{C}\right]}{1337D_{r}+4071} + \frac{500$$

Then, D_C and D_W can be solved numerically from (20) and (21). Since there are two equations solving for two unknown variables, the solution is unique. Figs. 16 and 17 depict the complete profile of the luminous flux and CCT values of the bi-color LED system for the full operating range that are calculated using (20) and (21), respectively. For the experiments performed using the nonlinear approach, the microcontroller generates the respective D_C and D_W by solving equation (20) and (21) based on the input values of $\phi_{M(set)}$ and $CCT_{M(set)}$. For the experiments performed on the linear approach, the respective D_C and D_W are generated by solving (20) and (22), which is given as

$$CCT_M = 2700D_W + 5000D_C \tag{22}$$

Equation (22) is obtained from equation (1) by setting $CCT_W = 2700$ and $CCT_c = 5000$.

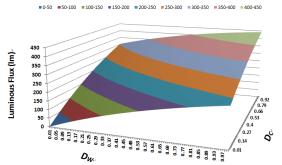


Fig. 16. Profile of the total luminous flux ϕ_M versus D_W and D_C calculated using (20).

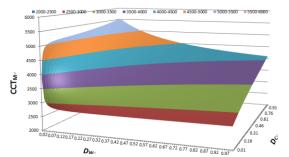


Fig. 17. Profile of CCT_M versus D_W and D_C calculated using (21).

B.2 For CREE LED samples

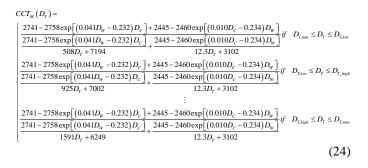
In order to confirm proposed method, eight CREE XPE cool-white LEDs (XPEWHT-L1-0000-00C01) and eight

CREE XPE warm-white LEDs (XPEWHT-L1-0000-00BE4) making up the bi-color white LED lamp are mounted on a heatsink with thermal resistance of 2.1 K/W. According to the datasheets the typical provided, CCT of 7500 ^{ath} XPEWHT-L1-0000-00C01 is Κ and that of GW5BTF27K00 is 3000 K. The current amplitude of the cool-white and warm-white LEDs are set precisely at 0.35 A and 0.35 A.

The substitution of the parameters $\phi_{C0} = 2741$ lm, $\phi_{W0} = 2445$ lm, $\alpha_C = 2758$, $\alpha_W = 2460$, $\beta_{C,max} = -0.191$, $\beta_{C,min} = -0.232$, $D_{W,max} = 1$, $D_{W,min} = 0$, $\beta_{W,max} = -0.225$, $\beta_{W,min} = -0.235$, $D_{C,max} = 1$, $D_{C,min} = 0$, $D_{T,min} = 0.1$, $D_{T,low} = 0.4$, $D_{T,high} = 1.1$, $D_{T,max} = 2$, $CCT_{C,min} = 7249$ K, $CCT_{C,low} = 7401$ K, $CCT_{C,high} = 8048$ K, $CCT_{C,max} = 9481$ K, $CCT_{W,min} = 2101$ K and $CCT_{C,max} = -2126$ K. which are obtained in the

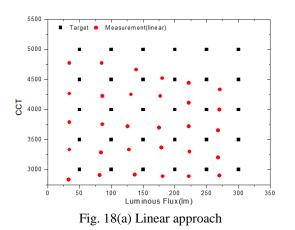
3101 K, and $CCT_{c,max} = 3126$ K, which are obtained in the previous sections into equations (18) and (19) give respectively

$$\phi_{M}(D_{C}, D_{W}) = 5186 - 2758 \exp[(0.041D_{W} - 0.232)D_{C}]$$
(23)
-2460 exp[(0.010D_{C} - 0.235)D_{W}]



C. Experimental Results and Discussion

For the comparison between the proposed nonlinear approach and the linear approach, the following setpoints of luminous flux ($\phi_{M(set)} = 50 \text{ lm}$, 100 lm, 150 lm, 200 lm, 250 lm, and 300 lm) and CCT ($CCT_{M(set)} = 3000 \text{ K}$, 3500 K, 4000 K, 4500 K, and 5000 K) are chosen for the experimental work. Therefore, there are in all 30 possible combinations of target setpoints.



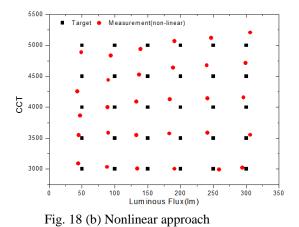


Fig. 18. Targeted and measured values of the luminous flux and CCT of the bi-color Sharp white LED lamp obtained with (a)

the linear approach and (b) the proposed nonlinear approach.

Table 5. Targeted and measured values of the luminous flux and CCT of the bi-color CREE white LED lamp obtained with the linear approach and the proposed nonlinear approach.

Target Value		Non-Linear Approach		Linear Approach	
Flux	CCT	Elux (1m)	CCT	Flux	CCT
(lm)	(K)	Flux (lm)	(K)	(lm)	(K)
100	3300	95	3250	88	2754
100	5400	96	5238	93	4013
100	7500	96	7394	92	6493
300	3300	296	3235	258	2789
300	5400	293	5515	264	4054
300	7500	292	7654	265	6687
550	3300	562	3392	455	2798
550	5400	568	5523	463	4356
550	7500	569	7729	461	6843

Table. 6 Nominal CCT Categories	(extracted from [41])
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Nominal CCT	Target CCT and Tolerance
	(K)
2700 K	2725 ±145
3000 K	3045 ±175
3500 K	3465 ± 245
4000 K	3985 ±275
4500 K	4503 ±243
5000 K	5028 ± 283
5700 K	5665 ± 355
6500 K	6530 ± 510

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Figs. 18(a) and 18(b) depict the experimentally measured values of the luminous flux and CCT of the bi-color Sharp white LED lamp under the 30 target setpoints that are obtained with the linear approach and the proposed nonlinear approach, respectively. As shown in Fig. 18(a), the maximum error between the target setpoints and the experimental results obtained with the linear approach is 22 lm (15%) and 717 K (14%) at the target setpoint (300 lm, 5000 K), as shown in Table 6. Such errors exceed the allowance CCT tolerance according to Table 6, where the non-perceivable CCT variation at target setpoint (5000K) is about 283K. Their averaged error is about 16 lm (10%) and 202 K (5%). With the nonlinear approach (see Fig. 17(b)), the maximum error between the target setpoint and experimental results is about 17 lm (11%) and 215 K (5%) at the target setpoint (50 lm, 4500 K), as shown in Table 6. Such errors fall within the acceptable CCT tolerance according to Table 6, where the non-perceivable CCT variation at target setpoint (4500K) is about 243K. Their averaged errors are about 9 lm (6%) and 93 K (2%), respectively. Table 5 shows the measured values of luminous flux and CCT of the bi-color CREE white LED lamp using by nonlinear method has good agreement with target value, compared to linear method. Therefore, it is clearly shown that the nonlinear approach results in a more accurate flux and CCT control of the bi-color variable LED system. While control errors are still present with the nonlinear approach because of model and measurement inaccuracies, these errors in luminance and color is basically non-perceivable and meets the requirement set in the ANSI Standard C78.377 [41] as given in Table 6.

V. CONCLUSIONS

A nonlinear approach of controlling the luminous intensity and correlated color temperature (CCT) of bi-color variable CCT white light-emitting diode (LED) lamps is proposed in this paper. The control is built upon nonlinear empirical flux and CCT models of the LEDs that are developed from the experimental results obtained in this work. It is demonstrated that these nonlinear models are easily simplified into practical solutions that are appropriate for implementations. Experimental results verified that the proposed approach is considerably more accurate than existing linear approaches in obtaining the desired brightness and CCT control in bi-color LED lamps. This approach is applicable to lamps with LEDs of multiple color temperatures.

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