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Infrared based measurements of velocity, turbulent kinetic energy, and dissipation at the water surface in a tidal river

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Abstract— Thermal infrared (IR) based particle image velocimetry (PIV) is used to measure the evolution of velocity, turbulent kinetic energy (TKE), and the TKE dissipation rate at the water surface in the tidally influenced Snohomish River. Patterns of temperature variability in the IR imagery arise from disruption of the cool skin layer and are used to estimate the 2D velocity field. Comparisons of IR based PIV mean velocity made against a collocated acoustic velocimeter demonstrate high correlation ($r^2 > 0.9$). Over a tidal period, surface TKE computed from the IR velocity varies from $10^4$ J·kg$^{-1}$ to $3 \times 10^3$ J·kg$^{-1}$, with an average difference from the in situ measurements of 8%. IR-derived TKE dissipation rates vary from approximately $3 \times 10^{-4}$ W·kg$^{-1}$ to $2 \times 10^{-3}$ W·kg$^{-1}$ at peak ebb, agreeing on average to within 7% of the in situ velocimeter results. Infrared-based PIV provides detailed measurements of previously inaccessible surface flow and turbulence statistics.

Index Terms— image motion analysis, velocity field, flow, turbulence, infrared, rivers

I. INTRODUCTION

Turbulence in rivers and estuaries affects water quality, ecosystem processes, and channel morphology by redistributing and mixing momentum, nutrients, pollutants, heat, and salinity. On a large scale, the production of turbulent kinetic energy (TKE) and its dissipation control the evolution of tides and the density structure of estuaries [1], [2]. At the water surface (air-water interface), the dissipation of TKE in the water controls the exchange of gas between water and air [3], and hence determines the re-aeration of oxygen-depleted waters and the exchange of carbon dioxide.

Despite the importance of mixing and transport in rivers and estuaries, in situ measurements of turbulence using current meters, scalar tracers and other techniques are challenging to make accurately, often distort the flow field, and typically lack the spatial resolution needed to assess complex flow patterns. Here we present novel remote measurements of flow and turbulence using two-dimensional thermal infrared (IR) imaging of the water surface. The technique is predicated on the observation that turbulence and coherent structures (e.g., boils and vortices) generate multi-scale temperature variability on the water surface through the disruption of a $O(1)$ mm thick cool-skin layer that is formed by net heat loss to the atmosphere at the water surface [4], a common condition in the absence of strong solar heating. The surface temperature variability is then advected and distorted by surface currents (see supplemental video). We exploit these shifting surface temperature patterns to measure flow velocity, TKE, and TKE dissipation rate ($\varepsilon$) using particle image velocimetry (PIV), a technique used extensively in laboratory experiments, e.g. [5], because it is non-invasive and provides greater spatial resolution than in situ current meters.

We investigate the dynamics of turbulence right at the water surface, a region that is difficult to measure in the field and yet is critical to air-water heat and gas fluxes. PIV techniques have been applied using thermal imagery in laboratory experiments [6], [7] and in the open ocean [8]. To our knowledge, this is the first study to validate the thermal PIV results with in situ measurements. Unlike these studies, which describe wave-breaking processes in the laboratory or ocean, we focus on the surface expression of open channel flow and turbulence characteristics generated from below. Hence, we demonstrate the surprising result that surface flow can be considered isotropic at scales below $O(1)$ m, which permits the use of the inertial cascade method in estimating the TKE dissipation rate.

II. MEASUREMENTS

Centimeter-resolution IR measurements of the river surface temperature field and collocated sub-surface velocity were recorded during a two-week experiment on the Snohomish River in Washington State during September 2009. The study site, which is 15 km upstream of the river mouth at Puget Sound, has a tidal range of 3 m and a maximum tidal velocity of 0.8 m s$^{-1}$. Salinity intrusion was only occasionally detected during spring tides and was not present during the set of measurements considered here. Measurements were made from the R/V Henderson, a 65 ft twin-hulled powered research vessel.
barge held stationary in the river flow by two retractable pilings (or spuds). During a tidal cycle, the barge floated freely up and down the spuds, with no flow induced swinging or rocking of the barge motion except during large boat wakes. An array of Acoustic Doppler Velocimeters (ADVs) was positioned at the end of an 8 m instrument frame on the upstream end of the vessel (Fig. 1a). An Indigo Phoenix 640x512 QWIP array camera (8-9.2 μm spectral response, 25 mK NETD) was affixed in a down-looking position (13.9° incidence) atop a 6 m tower on the end of the frame, such that the field of view included the surface locations of the ADV measurements.

Fig. 1. (a) Photograph of the IR camera and ADV array on the barge instrument frame prior to deployment (the upper and lower white circles highlight the aerial IR camera and near surface ADV, respectively). (b) Multibeam bathymetry of the Snohomish River and location of the barge sampling location analyzed here (+). River flow during ebb tide is from east to west (right to left in the plot).

Here, we analyze an ebb tide during the night of 24 September 2009, when atmospheric conditions were calm and clear and there was no density stratification. The river bottom at the study site was characterized by large dunes with an average wavelength of 10 m and height of 0.5 m (Fig. 1b) in water depth that decreased from 5.5 m to 2.5 m over the course of the ebb tide. The barge was positioned with the instrument frame upstream of the hull and measurements were made during the night to maximize the temperature contrast between water and the atmosphere and to avoid waves that occur due to daytime winds and boat traffic.

A. Infrared based surface velocimetry

Particle image velocimetry analysis was performed on IR image data collected at a frequency of 5 Hz (sub-sampled from 20 Hz data) with a 4.5 m by 3.5 m field of view. The average pixel resolution over the imaged field is 7.5 mm, providing resolution of fine-scale temperature features. The camera was periodically corrected for image non-uniformity and spatial noise via a two-point blackbody calibration.

The PIV technique measures horizontal velocity by tracking shifts in coherent temperature patterns across sequences of infrared images. Typical PIV uses normalized cross-correlation between image pairs [5], but the technique used here is based on phase correlation to better define image feature motion in the presence of large-scale background variation [9]. The basic algorithm assumes some small uniform shift \((x_0, y_0)\) in pairs of images \(I_1\) and \(I_2\),

\[
I_2(x, y) = I_1(x - x_0, y - y_0)
\]

The cross-stream and along-stream direction are \(x\) and \(y\), respectively. The corresponding phase correlation map between \(I_1\) and \(I_2\) is estimated as

\[
P(x, y) = \mathcal{F}^{-1} \left( \frac{\hat{I}_1 \hat{I}_2^*}{|\hat{I}_1|^2} \right) G
\]

where \(\mathcal{F}^{-1}\) is the inverse 2D Fourier transform operator, \((\cdot)^*\) indicates the Fourier transformed image, \((\cdot)\) is the complex conjugate, and \(G\) is a Gaussian shaped window with unit peak amplitude centered at the origin and a width (equivalent to twice the standard deviation) of 2/3 of the analysis window size. For a set of continuous and infinite length images, the raw phase map is analytically represented as a delta (impulse) function centered at \((x_0, y_0)\) [10], and the feature shift is found by locating this peak. The multiplication of \(G\) in the frequency domain results in a Gaussian shaped phase correlation peak in the spatial domain using the convolution theorem. However, fidelity of the velocity estimation is limited to unit pixel shifts if the discrete phase correlation maximum is used. Therefore, we obtain sub-pixel refinement by using the calculated peak location of a two-dimensional Gaussian hump fit to the phase correlation map within a 3-point radius of the discreet peak, e.g. [11]. The full PIV algorithm uses a multi-pass implementation of the above basic method with decreasing interrogation window sizes, so that subsequent PIV velocity estimates are refinements of prior estimates, thus enabling better estimation in regions of high velocity gradients. In this processing we have used interrogation windows with 50% overlap starting with 450x450 pixels, continuing with 128x128 and 32x32 pixels, and culminating with a 16x16 pixel window for a final velocity field with 6 cm spatial resolution (Fig. 2). The PIV algorithm was applied to
sequential images to produce 5 Hz time series of the 2D velocity field (see the supplementary video).

![Image](25-Sep-2009 06:15:31)

**Fig. 2.** An example of the convergence between two river boils in an IR image and the associated vector field of the turbulent (mean removed) velocity derived from PIV. Brighter regions in the underlying IR image are warmer, and the displayed temperature range (white to black) is less than 0.7°C. The maximum velocity magnitude (arrow length) shown is 11 cm s\(^{-1}\), and the circle indicates the location of the near surface ADV and PIV analysis location used for comparison. Time is in U.T.C.

**B. In situ flow measurements**

An array of acoustic Doppler velocimeters (ADVs) was mounted on the barge, with sampling depths 1.5 m, 0.7 m, 0.4 m, and 0.02 m below the surface (Fig. 1a). To avoid influence from the boat hull and to be collocated within the IR field of view, these instruments were mounted on a rigid aluminum frame attached to a cantilevered A-frame, both of which were further stiffened with multiple cable stays. The instruments were aligned with the axis of the barge, and the alignment was verified after the experiment with surveys using an optical total station. Visual assessment of the in situ velocities confirms that surface waves (which can contaminate turbulence estimates) were negligible during the experiment.

To provide the best comparison with surface PIV flow estimates, we focus on measurements with an upward facing ADV whose sample volume was located 2 cm below the water surface (Fig. 1a). The ADV sampled continuously at 25 Hz and was sub-sampled to 5 Hz for comparison with the PIV sampling rate. We corrected for a rotational offset of 13 degrees between the PIV and ADV measurements. The ADV measurement is located within 3 cm of the nearest PIV velocity estimate used for comparison (Fig. 2).

**III. RESULTS**

Infrared image data reveals a rich pattern of temperature contrast on the river surface. Boils at the surface produce areas of warmer (brighter) upwelled water contrasted against regions in which the cool skin layer remains undisturbed (Fig. 2; supplemental video). These features advect downstream with the mean flow and evolve, as documented by the pattern of mean-removed (turbulent) velocity. The observed turbulent velocity field in Fig. 2 consists of divergent, upwelling flow in the center of an active boil (x = 0.2 m and y = 2.2 m). This flow converges with the upstream edge of a second boil located downstream (lower right corner), in which fluid is slower than the mean and hence appears to be directed upstream. The large center convergence (downwelling) area appears as a cooler temperature.

![Image](u_9m_1.png)

**Fig. 3.** Example of a 5 minute ADV and IR based PIV time series of the (a) lateral, \(u\), and (b) alongstream component of flow, \(v\), (negative is downstream flow). ADV and PIV velocities were sampled at 25 Hz and 5 Hz, respectively. (c) Spectra from the measured \(u\), \(v\), and \(w\) (vertical velocity) components using ADV and IR PIV, with a 95% confidence limit and an \(f^{-5/3}\) slope indicated. The spectra show good agreement over the majority of the frequency range and both methods show a noise floor at \(f > 1.5\) Hz in the horizontal components. ADV-measured \(w\) contains less energy at low frequencies compared with \(u\) and \(v\), consistent with confinement due to the free surface.

The 2D velocity fields (Fig. 2) are validated by comparing the sub-surface, ADV velocity with the nearest velocity estimate on the PIV grid. The three-minute mean along-stream flow and cross-stream flow (\(v^\prime\) and \(u^\prime\)) and its temporal perturbation (\(v^\prime\) and \(u^\prime\)) estimated with the PIV technique agree well with the in situ velocimeter measurements (Fig. 3a and 3b). Similarly, power spectra (Fig. 3c) of cross-stream and along-stream velocity derived from PIV and from the in situ velocimeter are in agreement, particularly for larger scale motions with a frequency (\(f\)) of less than 1 Hz. For \(f > 2\) Hz, the horizontal spectra begin leveling out, indicating that a noise floor is approached. The spectra from both instruments exhibit an \(f^{-5/3}\) decay, which is consistent with a turbulent...
cascade transferring energy from large to small scales [12]. We use this observation later to estimate turbulent energy dissipation, as also done for example by [13] for surface measurements in a laboratory. Over a tidal period, three-minute averaged along-stream velocities \(\langle u^\prime \rangle\) are highly correlated with ADV measurements \(r^2 = 0.99; \text{Fig. 4a}\). Cross-stream mean velocities \(\langle v^\prime \rangle\) are similarly correlated \(r^2 = 0.94\). The combined PIV velocity components (magnitudes) are approximately 2% larger than ADV estimates.

\[
\phi(k) = \alpha \varepsilon^{5/3} k^{-5/3} \quad (3)
\]

over the range \(0.25 < k < 3.3\), where the constant \(\alpha\) is taken as 0.5 [12]. We eliminate \(\varepsilon\) estimates when the fit to \(\phi(k)\) results in log-log wavenumber slopes in the inertial subrange of less than -2 or greater than -3/4.

As the tidal flow accelerates, the resulting near-surface dissipation rates vary by roughly two orders of magnitude from less than \(3 \times 10^{-6} \text{ W kg}^{-1}\) right after slack water to nearly \(2 \times 10^{-4} \text{ W kg}^{-1}\) during peak ebb (Fig. 4c). The IR-based PIV measurements of \(\varepsilon\) reproduce the tidal trends in the ADV data \(r^2 = 0.59\), with PIV dissipation rates approximately 7% higher than in situ estimates, on average. We attribute the small difference in TKE and \(\varepsilon\) between methods to the larger noise of the PIV estimates compared to ADV measurements, the spatial resolution of the IR, and possible flow bias from the in situ measurement frame.

IV. DISCUSSION AND SUMMARY

The surface velocity measured with the IR PIV technique closely matches the near-surface flow pattern measured in situ, validating our approach and providing a method for new insights into the surface expression of coherent structures and turbulence. The well-resolved turbulent velocity signal allows for calculation of higher order statistics such as TKE and \(\varepsilon\). These statistics match the tidal progression of TKE and \(\varepsilon\) measured by an in situ ADV during all periods observed. We note, however, that the apparent increased noise of IR based PIV will limit estimates of \(\varepsilon\) to times when the TKE is sufficient to overcome measurement noise. Future improvement should focus on refined PIV algorithms and increasing the spatial resolution of the IR imager to decrease noise.

The presence of a -5/3 slope in the velocity spectra at the water surface is a surprising result, since [14] assumes that an inertial cascade requires isotropic conditions. Because vertical velocity fluctuations are suppressed by the surface (kinematic) boundary condition, the surface flow is highly anisotropic and is not expected to have a turbulent cascade. However, other studies have also found a -5/3 slope at the surface, e.g. [15], and used the inertial subrange method to estimate the dissipation rate, noting however that its interpretation is a topic under debate [16].

We investigate this conundrum by examining the near-surface anisotropy at different scales. At large scales (low frequency) the ratio of vertical to horizontal fluctuations measured 2 cm below the water surface is quite small (Fig. 5); hence, large-scale flow variations are anisotropic. However, this ratio approaches near unity at \(f = 1 \text{ Hz}\), or \(k = 1.5 \text{ m}^{-1}\) (at
maximum flow) so that fluctuations with a frequency \( \geq 1 \text{ Hz} \) can be considered to be isotropic. Interestingly, the \(-5/3\) slope occurs between 1 Hz and 12.5 Hz (the Nyquist frequency) in the \( w' \) spectra, but it only occurs between roughly 0.1 Hz and 2 Hz for the \( u' \) and \( v' \) spectra (Fig. 3). The lack of a \(-5/3\) cascade for the horizontal spectra for frequencies above 2 Hz reflects the noise floor of the instruments, and is not physical (the vertical resolution of an ADV is approximately four times the horizontal resolution). This noise causes a spurious decrease in the anisotropy ratio between 2 Hz and 12 Hz.

Although the overlap between the range of scales exhibiting the \(-5/3\) behavior in the horizontal and vertical components is somewhat limited, both clearly lie along the same line (i.e., have the same slope and intercept). Thus, dissipation rates computed using the lower frequency \(-5/3\) range of the spectrum in the horizontal components match the dissipation rates computed from the higher frequency range in the vertical component. It is likely that the observed cascade for the horizontal components is inherited from lower in the water column, and is not restricted by the surface boundary condition. In the vertical direction, the surface boundary more severely restricts the larger scales than the small scales [16], and produces the observed roll-off in the power spectrum. The results in Fig. 4 and 5 suggest a less stringent condition for the inertial cascade; namely, that flow must only be isotropic at small scales. Additionally, dissipation rates can be estimated from the horizontal velocity components at scales larger than those scales that are blocked in the vertical component.

To our knowledge, these are the first natural turbulence measurements using PIV applied to IR imagery to be validated with collocated in situ observations. This result presents an opportunity to remotely sense turbulence exactly at the water surface, through which important fluxes occur. On a fine scale, the intricate pattern of turbulent motions on the surface and their relation to subsurface turbulence profiles and bottom roughness can be explored. An improved understanding of the surface expression of subsurface turbulence may provide new insights into the processes responsible for air-water fluxes of gas and heat in rivers, estuaries and any environment characterized by full water-column mixing due to flow over bathymetry. On a large scale, application of this technique to larger fields of view could be used to measure spatial variation in flow and turbulent statistics due to a river geometry (e.g., bends) or bottom bathymetry with unprecedented resolution.

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