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# CENTRE FOR HEALTH PROGRAM EVALUATION

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## **Competing Methods for Efficiency Measurement**

### **A Systematic Review of Direct DEA vs SFA/DFA Comparisons**

**Mr Duncan Mortimer**

Research Associate, School of Medicine,  
Health Policy & Practice, University of East Anglia

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## Abstract

Various authors have advised a wait and see approach in evaluating the relative precision of alternative techniques, such as data envelopment analysis (DEA) and stochastic frontier analysis (SFA), in estimating industry-average and firm-specific inefficiency. Chirikos and Sear (2000), for example, contend that “policy-makers may be well advised to wait until additional research clarifies reasons why DEA and stochastic frontier models yield divergent results” (p. 1389).

The main objective of this paper is to highlight the likely trade-offs between competing methods based on direct empirical comparisons using simulated data and to demonstrate the wealth of evidence bearing on a range of real-world applications. Whilst this systematic review indicates that a good deal of evidence is already available, evidence of a different sort may be required to identify a ‘correct’ approach in addressing specific policy problems. In particular, the now routine practice of cross checking should be taken one step further to include realistic simulation studies along-side real-world DEA vs SFA comparisons.



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# Competing Methods for Efficiency Measurement

## A systematic Review of Direct DEA vs SFA/DFA Comparisons

### Introduction

Data envelopment analysis (DEA) and stochastic frontier analysis (SFA) employ quite distinct methodologies for frontier estimation and efficiency measurement, each with associated strengths and weaknesses, such that a trade-off exists in selecting the 'correct' approach:

“...non-statistical approaches such as DEA have the disadvantage of assuming no statistical noise, but have the advantage of being non-parametric and requiring few assumptions about the underlying technology. SFA models on the other hand have the attraction of allowing for statistical noise, but have the disadvantage of requiring strong assumptions as to the form of the frontier” (Jacobs, 2000 p. 3).

Previous studies have attempted to clarify this trade-off, so that the choice of a 'correct' method is rather more clear cut in particular applications. Banker, Gahd and Gorr (1993), for example, report findings from a Monte Carlo experiment to the effect that the relative precision of DEA and SFA is context specific. DEA is favoured where measurement error is unlikely to pose much of a threat and where the assumptions of neoclassical production theory are in question. Conversely, SFA should have the advantage in coping with severe measurement error and where simple functional forms provide a close match to the properties of the underlying production technology. Gong and Sickles (1993) report findings along similar lines so that “...as mis-specification of functional form becomes more serious, DEA's appeal (vis-à-vis SFA) becomes more compelling” (Gong & Sickles, 1993 p. 259).

The purpose of this article is to highlight the likely trade-offs between competing methods for frontier estimation based on a systematic literature review of direct empirical comparisons. Clearly, the set of pair-wise comparisons is steadily growing as new methods for frontier estimation and efficiency measurement arise to address the shortcomings of more traditional methods. In recognition of this fact, the review is restricted to comparisons between data envelopment analysis (DEA) and the two most commonly employed parametric alternatives: deterministic frontier analysis (DFA) and stochastic frontier analysis (SFA).

### Frontier Estimation

To provide some necessary background, a brief review of the methods is provided - focusing on the general approach employed in estimating the minimum cost frontier (rather than technical details). In each case, the choice between methods impacts upon the shape, location and interpretation of the resulting frontier.

Data envelopment analysis (DEA) utilises linear programming to fit a boundary function to observational data for a sample of relatively homogeneous firms. The method is distribution free and allows the data to 'speak for themselves' (Bates, Baines & Whynes, 1996). More specifically, the DEA frontier is floated beneath observed cost-output combinations so that the functional form of the cost frontier is determined by the best extremal fit given convexity constraints and assuming free disposal of both inputs and outputs (Seiford & Thrall, 1990).



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Whereas DEA allows the data to 'speak for themselves', parametric methods such as DFA and SFA assume a structure and then fit curve. Several options are available in estimating best-practice frontiers via the parametric approach. The simplest option is to 'correct' the location of the least-squares regression line so as to reflect the behavioural ideal of best-practice rather than an industry-average. An alternative fact, under the parametric approach, is to employ maximum likelihood (ML) methods to estimate the best-practice frontier. ML estimation allows efficient firms to have a greater say in the shape of the frontier, so as to capture any "structural dissimilarity between OLS and frontier technology" (Lovell, 1993 p. 22).

### Efficiency Measurement

The preceding discussion implies that DEA, DFA and SFA frontiers deliver quite different benchmarks describing best-practice. Note, however, that estimating a frontier or benchmark completes only half the job. The next step requires a comparison between actual and frontier production costs to provide a measure of relative efficiency.

Deterministic methods, such as DEA and DFA, characterise deviations from best-practice as entirely due to technical or allocative inefficiency. Inefficient firms are assumed to be capable of producing on the best-practice frontier simply by adopting efficient production methods and all variation in observed cost-output combinations is assumed to be within the control of the firm. More formally, the economic efficiency of a the  $j^{\text{th}}$  firm ( $e_j$ ) is equal to the ratio of actual ( $C_j$ ) to frontier ( $C^*$ ) production cost:  $e_j = C^* / C_j$  where  $e_j \in (0, 1)$  and  $C_j = C^* + e_j$ . In short, measurement error and random variation are simply assumed away and deviations from the frontier are attributed solely to inefficiency.

The value of the stochastic methods such as SFA lies in the assumption that the actual performance of each evaluated firm reflects a range of factors that relate to good fortune as well as to good practice. "Observed hospital costs may deviate from an efficient cost frontier due to events that are both within and outside of the hospital's control" (Zuckerman, Hadley and Iezzoni, 1994 p. 274). More formally, the stochastic frontier approach treats deviations ( $e_j$ ) from best-practice as 'composed residuals' comprising two components: a one-sided inefficiency term ( $u_j$ ) reflecting managerial competence; and a symmetric random error ( $v_j$ ) reflecting omitted variables, measurement error and stochastic elements beyond managerial control. Comparisons between the stochastic frontier ( $C^* + v_j$ ), actual production cost ( $C_j$ ), and the deterministic frontier ( $C^*$ ), reflect the share of excess production cost attributable to random error and inefficiency. More precisely, the economic efficiency of the  $j^{\text{th}}$  firm is given as:  $u_j = (C^* + v_j) / C_j$  where  $u_j \in (0, 1)$ ,  $C_j = C^* + e_j$ , and  $e_j = v_j + u_j$ .

### Competing Paradigms?

It should be obvious from the above discussion that DFA provides an unhappy compromise between DEA and SFA (at least at a conceptual level). Whereas DFA and SFA adopt a similar approach to frontier estimation; DEA and DFA have much in common when it comes to efficiency measurement. In short, DFA "combines the bad features of the econometric and programming approaches to frontier construction: it is deterministic *and* parametric" (Lovell, 1993 p. 21). Note, however, that pairwise comparisons involving DFA should isolate the differences along one of two relevant dimensions: **deterministic vs stochastic efficiency measurement** or **non-parametric vs parametric frontier estimation**. In contrast, DEA and SFA efficiency scores are expected to differ due to both dimensions.

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Recall that previous studies have attempted to clarify the trade-off between competing paradigms so that the choice of a 'correct' method is rather more clear-cut in certain applications. DEA is favoured where measurement error is unlikely to pose much of a threat and where the assumptions of neoclassical production theory are in question. Conversely, SFA should have the advantage in coping with measurement error and where simple functional forms provide a close match to the properties of the underlying production technology. Unfortunately, neither DEA nor SFA is ideally suited across all applications. In estimating hospital efficiency, for example, both measurement error and functional form are likely to cause problems. In short, the analysis of hospital efficiency really requires a hybrid approach that copes well with random variation and measurement error; but that is also flexible in modelling both the underlying production technology and the objectives and conduct of individual hospitals. Some progress has been made towards making DEA stochastic (see Sengupta, 1987; 1998) and SFA more flexible (see Lovell, 1993). In the meantime, the relative precision and policy value of alternative measures of hospital efficiency remains an empirical question and it is not possible to install a 'gold standard' based solely on *a priori* deliberation.

### **Search Strategy**

The review of empirical comparison that follows is based on literature identified from an initial search of citation databases, together with supplementary searches of the authors own citation databases, review article bibliographies, and web-based resources. The initial search included:

#### ***ISI Web of Science***

- Science Citation Index (SCI-X) Expanded, 1981- April 2002: 25 records
- Social Sciences Citation Index (SSCI), 1981- April 2002: 51 records

#### ***OVID***

- Pre-MEDLINE & MEDLINE, 1966- April 2002: 2 records
- Journals@Ovid Full Text, April 2002 edition: 1 record

Searches were conducted using the following search terms: (“*STOCHASTIC FRONTIER*” OR “*FRONTIER ESTIMATION*” OR “*DETERMINISTIC FRONTIER*”) AND (“*DATA ENVELOPMENT ANALYSIS*”), yielding just over 100 articles after removal of duplicates. Articles published in a language other than English were excluded from the review. Abstracts (and, if necessary, articles) were then scanned to identify 51 articles and unpublished papers reporting at least one pair-wise empirical comparison between DFA, DEA and SFA.

### **Empirical Evidence**

Both DEA and SFA have the potential to deliver biased estimates of inefficiency due to specification errors of one sort or another. Biases in opposite directions raise the possibility of fairly substantial divergence between DEA-, DFA- and SFA-based estimates. In such circumstances, correspondence between real-world DEA, DFA and SFA efficiency scores provides some reassurance that competing methods are accessing similar latent variables. Note, however, that correspondence alone provides no guarantee that competing methods are accessing the 'target' construct and might simply reflect biases in the same direction. Fortunately, the use of simulated data delivers a criterion against which to quantify potential errors and biases under a wide range of different conditions. The simulation studies reviewed below include all

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possible pair-wise comparisons<sup>1</sup> across the two relevant dimensions: non-parametric vs parametric frontier estimation and deterministic vs stochastic efficiency measurement.

## Accuracy: Simulation Studies

For the most part, well-established variants of alternative frontier estimation techniques provide a fairly accurate picture of the relative efficiency of individual production units. Banker, Chang & Cooper (1996), for example, reported mean absolute deviations between DEA-/DFA-based estimates of output-oriented technical efficiency and ‘actual’ efficiency scores that ranged from 0.006 to 0.054 efficiency points (depending on sample size and returns to scale). Banker, Charnes, Cooper & Maindiratta (1987) found a similar correspondence (mean absolute deviations of between 0.003 and 0.049) between DEA-/DFA-based estimates and actual efficiency scores. Note, however, that mean absolute deviations between DEA- and DFA-based estimates (rather than between estimates and actual scores) might be somewhat larger if competing methods diverge in opposite directions. Moreover, the above findings are based on simulated data in which deviations between the efficient frontier and observed production points really are *entirely* due to inefficiency.

In real-world applications, measurement error is the rule rather than the exception. Inclusion of measurement error to simulate ‘noisy’ data would therefore seem an obvious step in making simulated production environments more realistic. Findings from Banker, Gadh & Gorr (1993) suggest that choice of the ‘correct’ or ‘best’ estimation method is likely to be much more important in the presence of measurement error. At low levels of measurement error, mean absolute deviations between DEA-/SFA-based estimates and ‘actual’ efficiency scores varied between 0.03 and 0.11 efficiency points (depending on sample size, technology, and the distributions of inefficiency and measurement error). At higher levels of measurement error, the gap between estimates and ‘actual’ efficiency scores widened, with mean absolute deviations of between 0.08 and 0.40. In short, “neither method performed satisfactorily for high measurement errors” (Banker, Gadh & Gorr, 1993 p. 332).

In contrast, Yu (1998) estimated DEA-/SFA-based efficiency scores against a background of fairly high levels of measurement error and, for lower values of exogenous variables, found mean absolute deviations between estimated and actual scores no higher than 0.161 and correlations ranging from 0.62 to 0.89. Similarly, Resti (2000) estimated DEA-/SFA-based scores for overall economic efficiency in the presence of ‘low’, ‘medium’ and ‘high’ levels of noise. Resti reported mean absolute deviations from actual scores ranging from 0.004 to 0.063, and correlations between estimated and actual scores of between 0.63 and 1.00. In short, “all the ‘classic’ techniques performed rather satisfactorily in measuring the amount of inefficiency, although their performance can worsen in some specific situations” (Resti, 2000 p. 568).

Under relatively benign conditions, frontier methods also manage to get reasonably close to the mark in characterising the properties of the underlying production technology. Banker, Chang & Cooper (1996) correctly identified returns to scale properties in up to 87.9% of observations for some DEA-based estimates (but the proportion misclassified reached 38.33% for some DFA-based estimates). Banker, Charnes, Cooper & Maindiratta (1987) reported mean absolute

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<sup>1</sup> In particular: SFA vs SDEA (Resti, 2000), DFA vs DEA (Banker, Chang & Cooper, 1996; Banker, Charnes, Cooper & Maindiratta, 1987), SFA vs DEA (Banker, Gadh & Gorr, 1993; Bojanic, Caudill & Ford, 1998; Gong & Sickles, 1992; Resti, 2000; Yu, 1998), and SFA vs DFA (Ruggiero, 1999).

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deviations between DEA-based estimates and actual rates of technical substitution as low as 0.085 (but as high as 0.24 for some DFA-based estimates). Similarly, the proportion of observations misclassified with respect to scale effects was as low as 6.4% for some DEA-based estimates (but as high as 40.4% for some DFA-based estimates).

## Pair-wise Comparisons: Simulation Studies

Recall that comparisons between DEA and DFA isolate differences due to parametric vs non-parametric frontier estimation. Banker, Charnes & Cooper (1996) conclude that 'DEA generally shows superior performance' (p. 233) with variable returns to scale (VRTS) DEA models dominating DFA-based alternatives under all conditions. Note, however, that DFA was often 'closer to the mark' than constant returns to scale (CRTS) DEA models and it is not possible to specify a 'best' model for all conditions. Under a more restricted set of conditions Banker, Charnes, Cooper & Maindiratta (1988) found DEA-based estimates of output-oriented technical efficiency to be more accurate and more stable than their DFA-based counterparts. In short, comparisons between DEA and deterministic variants of the parametric approach simply confirm what was already suspected: the move from DEA to DFA comes at the cost of reduced flexibility in modelling the production environment and offers nothing by way of compensation.

In assuming an environment characterised by measurement errors and stochastic variation, SFA appears (at least at the conceptual level) less of a straw man. Even so, results drawn from Banker, Gahd & Gorr's (1993) DEA vs SFA comparison "show DEA to produce more accurate efficiency estimates ...even with remarkably high measurement errors present" (p. 341). SFA only gains the upper hand when measurement errors reach a threshold of between  $\pm 17\%$  to 45% of observed output values (depending on sample size, technology, and the distribution of inefficiency). Results also suggest that SFA is more accurate whenever sample size reaches a threshold of 50 units and distributional *assumptions* mirror 'actual' distributions of noise and inefficiency<sup>2</sup>. In other words, the expected trade-off applies with relatively few caveats: SFA has the advantage in coping with *severe* measurement error or when the distributional assumptions required in separating measurement error from inefficiency accurately reflect the properties of the underlying production environment.

More recent studies have sought to generalise decision-rules to more realistic production environments. Yu (1998), for example, simulated the impact of exogenous factors (beyond managerial control) with varying degrees of influence over output. One-step, two-step and first-stage SFA-based estimates of technical efficiency were generally more accurate than any of the DEA-based alternatives. Within the SFA camp, the one-step procedure strictly dominates two-step and first-stage options in accounting for the impact of exogenous variables. Within the DEA camp, first-stage and two-step options are preferred whenever the impact of exogenous factors is relatively minor. As the influence of exogenous factors on observed performance increases, the Banker and Morey (1986) one-step procedure edges in front of the DEA-based competition. In every case, the one-step SFA procedure yields lower mean absolute deviations and higher rank correlations between estimated and actual scores than the next best option.

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<sup>2</sup> Results also suggest that, for small sample sizes and small measurement errors, DEA and SFA are biased in *opposite* directions. As such, "...a combination frontier may be more accurate than either estimate by themselves" (Banker, Gahd & Gorr, p. 341).

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In a similar vein, Resti (2000) generated simulated production units that mimicked the scale and scope of production, concentration of market power, and various other features of a real-world banking sector. Results suggest that SFA-based estimates of overall economic efficiency are always more accurate for the large sample size of 500 units and, as expected, the relative advantage of the stochastic frontier approach increases with the amount of noise in the data. Even for Resti's small sample size of 50 units, SFA occasionally edges out the DEA-based competition (depending on the form of the frontier, the magnitude of between-unit differences in actual efficiency scores and the amount of noise in the composed residuals). For the small sample size, DEA is most accurate and most likely to outstrip SFA when RTS assumptions mirror RTS properties of the simulated production technology (Resti, 2000).

## Impact of Specification Error: Simulation Studies

Specification error is expected to have two effects: firstly, it should weaken the correspondence between estimates and true values and secondly, certain sorts of errors should favour one or other of the competing approaches. More specifically:

- DEA is usually thought to be less accurate and more erratic at 'corner points' where few, if any, observations are available to provide a reliable standard of comparison in estimating the best-practice frontier. This is largely because measurement error is more likely to influence the location and shape of the frontier around corner points, but also because VRTS models tend to confuse technical efficiency with scale effects when regions on the feasible set remain 'hidden'. Competing parametric methods encounter a similar problem because it is difficult to fit a well-specified curve over sparsely populated regions of the feasible set (Read and Thanassoulis, 1996).

In line with expectations, Resti (2000) and Yu (1998) found that VRTS DEA models tended to overestimate the efficiency of atypical and outlying production units. Similarly, Read and Thanassoulis (1996) reported higher mean absolute deviations around atypical and outlying observations for SFA-/DEA-based estimates of technical efficiency. Banker, Chang and Cooper (1996) reported an increase in mean absolute deviations for both DEA- and DFA-based estimates in the vicinity of corner points. Moreover, efficiency scores drawn from Banker, Chang and Cooper's (1996) VRTS DEA models were most erratic when faced with sparse comparison sets around corner points.

- Banker, Charnes, Cooper & Maindiratta (1988) encountered problems due to the non-parametric equivalent of incorrect functional form. More specifically, "DEA performs poorly for observations that fall in the region where the 'true' production possibility set is non-convex, violating the convexity axiom in DEA" (p. 50). In a similar vein, Gong and Sickles (1992) reported that failure to correctly specify the form of *parametric* frontiers, relying instead on overly flexible functional forms such as the translog, leads to imprecise estimates of technical efficiency. Banker, Charnes and Cooper (1996), Ruggiero (1999) and Resti (2000) encountered much the same problem when relying on flexible functional forms in smaller samples. Resti (2000) attributed this loss of precision to multicollinearity between cross products and higher-order terms in the unrestricted translog.
- A number of studies (eg. Banker, Gahd & Gorr, 1993; Read & Thanassoulis, 1996; Ruggiero, 1999; Resti, 2000; Ondrich & Ruggiero, 2001) have reported a loss of precision for DEA, DFA and/or SFA in the presence of higher levels of measurement error. Recall



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that deterministic methods, such as DEA and DFA, are usually regarded as particularly susceptible to measurement error because deviations from the frontier are attributed *solely* to inefficiency. Results from Resti (2000) confirm the superior performance of SFA in the presence of higher levels of measurement error. Read and Thanassoulis (1996) encountered problems (mean absolute deviations as high as 0.284) in obtaining accurate DEA-based estimates of technical efficiency from noisy data. In contrast, SFA-based estimates from the same study remained reasonably close to the mark even at 'high' levels of noise (Read & Thanassoulis, 1996).

Note, however, that a number of findings call into question SFA's comparative advantage in handling noisy data. Banker, Gahd and Gorr (1993), for example, "show DEA to produce more accurate efficiency estimates... even with remarkably high measurement errors present" (p. 341). In particular, COLS-based SFA models frequently characterised deviations from the frontier as entirely due to inefficiency, "leading to overall poor performance relative to DEA" (Banker, Gahd & Gorr, 1993 p. 337). Ruggiero (1999) and Ondrich and Ruggiero (2001) report similar results in comparing DFA- and SFA-based models. Even in the presence of 'high' levels of measurement error, the deterministic approach sometimes out-performs the SFA-based competition (Ruggiero, 1999; Ondrich and Ruggiero, 2001). In each case, SFA failed to accurately separate noise and inefficiency: calling into question one of the chief selling points of the stochastic frontier approach - the ability to cope with noisy data. In other words, these results suggest that the 'poor-cousin' status of DFA might not stand up to scrutiny.

- Bojanic, Caudill & Ford (1998) allowed the extent of measurement error to increase as output increased (ie. heteroskedastic measurement error). Both DEA and SFA systematically overestimated the inefficiency parameter in the presence of severe and heteroskedastic measurement errors<sup>3</sup>. Whilst neither method delivered satisfactory estimates for technology and efficiency parameters, SFA-based estimates consistently outperformed their DEA-based counterparts<sup>4</sup>.
- Banker, Charnes and Cooper (1996) simulated the impact of common specification errors via the inclusion of an irrelevant variable and the omission of a relevant variable. Inclusion of an irrelevant variable frequently increased mean absolute deviations but left the relative standing of DEA- and DFA-based models largely intact. In contrast, omitting a relevant variable *always* increased mean absolute deviations and dramatically eroded the relative standing of estimates drawn from CRTS DEA models (relative to the DEA- and DFA-based competition) with respect to both accuracy and consistency (Banker, Charnes & Cooper, 1996). Ruggiero (1999) reported similar problems due to omitted variables when

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<sup>3</sup> DEA-based estimates were, however, much more inflated than their SFA-based counterparts. For the case of moderate inefficiency and moderate heteroskedasticity, SFA overestimated the inefficiency parameter by about five times and DEA by about ten times. For the case of low inefficiency and high heteroskedasticity, SFA overestimated the inefficiency parameter by about 25 times and DEA by about 50 times (Bojanic, Caudill & Ford, 1998).

<sup>4</sup> Note that the relative standing of DEA and SFA was (at least partly) a result of 'rigging' the simulation in favour of SFA. Specifically, the relatively poor performance of DEA is less than surprising given the presence of fairly severe levels of measurement error. In addition, the functional form of the true frontier and the distributions of both error and inefficiency were known in advance; eliminating two sources of specification error that are specific to the stochastic frontier approach.

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estimating SFA production frontiers. Because any loss of precision can be attributed to an increase in noise (that would otherwise be explained by the omitted variable), and because the performance of all methods declines as noise increases; Ruggiero (1999) argues that the adverse impact of omitting a relevant variable is common to all competing methods.

## Real-world Comparisons

Simulated studies have the advantage of providing a *criterion* against which to compare the performance of competing methods for frontier estimation and efficiency measurement. In particular, the true values of technology and inefficiency parameters are known and available for comparison against estimated values. Note, however, that simulation studies tend to assume away the sort of complications that arise for real-world applications. In attempting to provide a neutral setting and a fair comparison, simulated production units, technologies, and production environments might not be all that realistic in capturing the multi-plant, multi-product organisation of many real-world firms<sup>5</sup> and might not provide a true test of the techniques (Resti, 2000). The stability of, and correspondence between, competing methods *in real-world applications* therefore make an important contribution to the weight of empirical evidence.

The majority of direct DEA vs SFA/DFA comparisons reported in the literature have found moderate to strong correspondence when ranking financial institutions (eg. Drake & Weyman, 1996; Resti, 1997), railways (Coelli & Perelman, 1999), social security offices (Bjurek, Hjalmarsson & Forsund, 1990), cement plants (Hjalmarsson, Kumbhakar & Heshmati, 1996), pig farms (Sharma, Leung & Zaleski, 1997), school districts (Ruggiero & Vitaliano, 1999), local governments (de Borger & Kerstens, 1996), and acute care hospitals (eg. Linna, 1998; Webster, Kennedy & Johnson, 1998). A smaller number of studies found only mediocre to poor correspondence in ranking acute care hospitals (eg. Chirikos & Sear, 2000), financial institutions (eg. Ferrier & Lovell, 1990), and electrical utilities (eg. Ray & Mukherjee, 1995). A summary review of the 41 real-world DEA vs SFA/DFA comparisons identified in the literature is provided in table 1 below.

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<sup>5</sup> For example, hospitals are typically multi-product firms that might operate on several campuses and employ a broad range of heterogeneous inputs in the production of teaching, research, hotel services, and patient care. Moreover, episodes of care are likely to differ with respect to *case-mix factors* such as diagnosis, treatment, *severity*, age, complications and co-morbidity.

**Table 1 - Direct DEA vs SFA/DFA Comparisons**

Author / Date	Country	Units / Period	DEA Model		SFA/DFA Model		Findings		
			Orientation	RTS	Form	Frontier	DEA	SFA/DFA	Comparison
Banker, Chang & Cooper (1996)	N/A	simulation study: 50 - 200 units	output-increasing	CRTS	Cobb-Douglas	deterministic prod. frontier	"Both DEA and COLS generally give good results at all sample sizes. In evaluating efficiency, DEA generally shows superior performance" (p. 233).		
				VRTS	translog				
Banker, Charnes, Cooper & Maindiratta (1987)	N/A	simulation study: 100 & 500 units	output-increasing	VRTS	translog	deterministic prod. frontier	"DEA outperforms the parametric approach ...the piecewise linear production function is more flexible in approximating the true frontier... simulation results reported in this study bear this out" (pp. 42 & 50).		
Banker, Conrad & Strauss (1986)	US	114 acute care hospitals 1978/79	input-reducing	CRTS	CRTS translog	deterministic TC frontier	45 units $TE_x = 1$ 37 units $0.9 \leq TE_x \leq 1$ 32 units $TE_x < 0.9$	45 units $EE_x = 1$ 37 units $0.9 \leq EE_x \leq 1$ 32 units $EE_x < 0.9$	$(\chi^2 = 11.79, df = 4, p < 0.05)$ ie. 'broad agreement'
Banker, Gahd & Gorr (1993)	N/A	simulation study: 25 - 200 units	output-increasing	VRTS	translog	stochastic prod. frontier	In most cases, "DEA produces more accurate efficiency estimates than COLS, even with remarkably high measurement errors" (p. 341).		
Bates (1997)	England	96 local education authorities, 1980s	output-increasing	CRTS	Cobb-Douglas	stochastic prod. frontier	23 units $TE_y > 0.95$ 55 units $0.95 \leq TE_y \leq 0.9$ 18 units $TE_y < 0.9$	16 units $TE_y > 0.95$ 71 units $0.95 \leq TE_y \leq 0.9$ 9 units $TE_y < 0.9$	"...much agreement between DEA and SF results" (p. 92).
Bauer, Berger, Ferrier & Humphrey (1998)	US	683 banks, 1977 - 1988	cost-reducing	VRTS	translog	stochastic TC frontier	$EE_x$ means: 0.21-0.385	$EE_x$ means: 0.875-0.88	Spearman's rho: 0.10-0.17
Bjurek, Hjalmarsson & Forsund (1990)	Sweden	400 social security offices 1974 - 1984	input-reducing	CRTS	Cobb-Douglas	deterministic input-req. frontier	potential input-saving: 0.17-0.31	potential input-saving: 0.18-0.26	Spearman's rho > 0.83
				DRTS NITRS	quadratic		potential input-saving: 0.16-0.25	potential input-saving: 0.12-0.20	Spearman's rho > 0.87
Bojanic, Caudill & Ford (1998)	N/A	simulation study: 25 - 200 units	cost-reducing	CRTS	Cobb-Douglas	stochastic TC frontier	"...heteroskedasticity in the two-sided error term introduces substantial biases into ML, COLS and DEA estimators. Although none perform well, both ML and COLS are found to be superior to DEA" (p. 140).		
Brümmer (2001)	Slovenia	147 private farms, 1995 & 1996	revenue-increasing	VRTS	translog	stochastic prod. frontier	$TE_y$ means: 0.43-0.45	$TE_y$ means: 0.74-0.75	Spearman's rho: 0.69



**Table 1 (cont.) - Direct DEA vs SFA/DFA Comparisons**

Author / Date	Country	Units / Period	DEA Model		SFA/DFA Model		Findings		
			Orientation	RTS	Form	Frontier	DEA	SFA/DFA	Compare
Chirikos & Sear (2000)	US	186 acute care hospitals, 1982 - 1993	cost-reducing	CRTS	translog	stochastic TC frontier	EE <sub>x</sub> mean: 0.80	EE <sub>x</sub> mean: 0.85	Pearson's r: 0.33
					CRTS translog			EE <sub>x</sub> mean: 0.75	Pearson's r: 0.13
					hybrid			EE <sub>x</sub> mean: 0.82	Pearson's r: 0.26
Coelli & Perelman (1999)	Europe	17 railway firms, 1988-1993	input-reducing	CRTS	CRTS translog	deterministic input dist <sub>f</sub>	TE <sub>x</sub> = TE <sub>y</sub> means: 0.81-0.88	TE <sub>x</sub> = TE <sub>y</sub> mean: 0.78	Pearson's r: 0.56-0.71
			output-increasing			deterministic output dist <sub>f</sub>			
			input-reducing	VRTS	translog	deterministic input dist <sub>f</sub>	TE <sub>x</sub> means: 0.86-0.93	TE <sub>x</sub> mean: 0.90	Pearson's r: 0.29-0.43
			output-increasing			deterministic output dist <sub>f</sub>	TE <sub>y</sub> means: 0.88-0.93	TE <sub>y</sub> mean: 0.89	Pearson's r: 0.26-0.43
Cooper, Kumbhakar, Thrall & Yu (1995)	China	3 industries (textiles, chemicals, metals), 1966 - 1988	output-increasing	CRTS	Cobb-Douglas	stochastic prod. frontier	"Although there are discrepancies, results from DEA and SFA generally tend toward confirmation. ...this consistency increases confidence that behaviour is 'in the observations' and not simply a reflection of our models" (p. 101).		
Cummins & Zi (1998)	US	445 life insurers, 1988-1992	cost-reducing	VRTS	translog	stochastic TC frontier	EE <sub>x</sub> means: 0.42-0.50	EE <sub>x</sub> means: 0.44-0.86	Spearman's rho: 0.56-0.60
De Borger & Kerstens (1996)	Belgium	589 local govts, 1985	cost-reducing	VRTS	translog	deterministic TC frontier	EE <sub>x</sub> mean: 0.727	EE <sub>x</sub> mean: 0.570	Pearson's r: 0.81 Spearman's rho: 0.81
						stochastic TC frontier		EE <sub>x</sub> means: 0.78-0.81	Pearson's r: 0.82-0.83 Spearman's rho: 0.82
Dismuke & Sena (1999)	Portugal	2 DRGs in 52 central & general hospitals, 1992-1994	input-reducing	CRTS	linear	stochastic input-req. frontier	"...technical efficiency change and technological change computed using DEA... results are generally consistent with those obtained from parametric methods" (pp. 112-113).		
Drake & Weyman-Jones (1996)	UK	46 building societies, 1988	cost-reducing	VRTS	translog	stochastic TC frontier	EE <sub>x</sub> mean: 0.876	EE <sub>x</sub> mean: not reported	Spearman's rho: 0.97
Eisenbeis, Ferrier & Kwan (1999)	US	254 banks, 1986 - 1991	cost-reducing	VRTS	restricted translog	stochastic TC frontier	EE <sub>x</sub> means: 0.60-0.72	EE <sub>x</sub> means: 0.81-0.92	Spearman's rho: 0.444-0.589

**Table 1 (cont.) - Direct DEA vs SFA/DFA Comparisons**

Author / Date	Country	Units / Period	DEA Model		SFA/DFA Model		Findings		
			Orientation	RTS	Form	Frontier	DEA	SFA/DFA	Compare
Ferrier & Lovell (1990)	US	575 financial institutions, 1984	cost-reducing	VRTS	translog	stochastic TC frontier	TE <sub>x</sub> mean: 0.84 AE <sub>x</sub> mean: 0.95 EE <sub>x</sub> mean: 0.79	TE <sub>x</sub> mean: 0.91 AE <sub>x</sub> mean: 0.83 EE <sub>x</sub> mean: 0.74	Spearman's rho: 0.014-0.017
Gong & Sickles (1992)	N/A	simulation study: 50 units over 10 to 50 periods	input-reducing	VRTS	translog, CES translog & generalised Leontief stochastic prod. frontiers		“...if the employed form is close to the underlying technology, stochastic frontier models outperform DEA. As specification error becomes more serious, DEA's appeal becomes more compelling” (p. 259).		
Guiffrida & Gravelle (1998)	England	90 FHSAs, 1993/94 - 1994/5	cost-reducing	CRTS	hybrid	deterministic TC frontier	EE <sub>x</sub> means: 0.89-0.97	EE <sub>x</sub> means: 0.86-0.91	Spearman's rho: 0.26-0.70
						stochastic TC frontier		EE <sub>x</sub> means: 0.89-0.99	Spearman's rho: 0.22-0.71
Hjalmarsson, Kumbhakar & Heshmati (1996)	Colombia	15 cement plants, 1968 - 1988	output-increasing	CRTS	Zellner-Revankar	deterministic prod. frontier	TE <sub>y</sub> means: 0.72-0.89	TE <sub>y</sub> means: 0.68-0.78	Spearman's rho: 0.52-0.80
				VRTS					TE <sub>y</sub> means: 0.75-0.97
				CRTS	translog	stochastic prod. frontier	TE <sub>y</sub> means: 0.72-0.89	TE <sub>y</sub> means: 0.71-0.97	Spearman's rho: -0.08-0.75
				VRTS					TE <sub>y</sub> means: 0.75-0.97
Jacobs (2001)	UK	232 NHS hospitals, 1995/96	cost-reducing	VRTS	linear	stochastic TC frontier	EE <sub>x</sub> means: 0.65-0.94	EE <sub>x</sub> means: 0.83-0.88	Pearson's r: 0.43-0.63
Johnes (1998)	UK	50 universities, 1989/90	cost-reducing	CRTS	quadratic	stochastic TC frontier	“...comparison of efficiency measures obtained by SFA and DEA confirms that these are broadly in accord with one another. ...the magnitude of the rank correlation coefficient, at 0.133, is rather low, however” (p. 206).		
			VRTS						
Linna (1998)	Finland	43 acute care hospitals, 1988 - 1994	cost-reducing	CRTS	Box-Cox transform	stochastic TC frontier	EE <sub>x</sub> means: 0.70-0.93	EE <sub>x</sub> means: 0.84-0.93	Spearman's rho: 0.57-0.75
				VRTS					EE <sub>x</sub> means: 0.79-0.96
Linna & Häkkinen (1999)	Finland	95 acute care hospital units, 1994	cost-reducing	CRTS	Box-Cox transform	stochastic TC frontier	EE <sub>x</sub> means: 0.90-0.92	EE <sub>x</sub> mean: 0.86	Spearman's rho: 0.41-0.58
				VRTS					EE <sub>x</sub> means: 0.85-0.87

**Table 1 (cont.) - Direct DEA vs SFA/DFA Comparisons**

Author / Date	Country	Units / Period	DEA Model		SFA/DFA Model		Findings					
			Orientation	RTS	Form	Frontier	DEA	SFA/DFA	Compare			
Linna & Häkkinen (1998)	Finland	95 acute care hospital units, 1994	cost-reducing	CRTS	Cobb-Douglas	stochastic TC frontier	EE <sub>x</sub> mean: 0.84-0.89	EE <sub>x</sub> mean: 0.89-0.93	Spearman's rho: 0.52-0.63			
					translog			EE <sub>x</sub> mean: not reported	Spearman's rho: 0.28			
					Box-Cox transform			EE <sub>x</sub> mean: 0.86-0.89	Spearman's rho: 0.55-0.68			
Meibodi (1998)	developing countries	26 electricity industries, 1987 - 1988	input-reducing	CRTS	Cobb-Douglas	stochastic prod. frontier	TE <sub>x</sub> mean: 0.72	TE <sub>y</sub> mean: 0.77	Pearson's r: 0.48 Spearman's rho: 0.36			
				VRTS			TE <sub>x</sub> mean: 0.79		Pearson's r: 0.71 Spearman's rho: 0.66			
Mortimer (2001)	Australia	38 public hospitals, 1993	cost-reducing	VRTS	Cobb-Douglas	stochastic TC frontier	EE <sub>x</sub> means: 0.83-0.86	EE <sub>x</sub> means: 0.81-0.86	Pearson's r: 0.61-0.65 Spearman's rho: 0.48-0.55			
Odeck (2001)	Norway	170 rock-blasting units, 1993	input-reducing	CRTS	Cobb-Douglas	deterministic prod. frontier	TE <sub>x</sub> = TE <sub>y</sub> mean: 0.36	TE <sub>x</sub> = TE <sub>y</sub> mean: 0.12	Spearman's rho: 0.85			
			output-increasing									
			input-reducing	VRTS						TE <sub>x</sub> mean: 0.47 SE <sub>x</sub> mean: 0.77	TE <sub>x</sub> mean: 0.23 SE <sub>x</sub> mean: 0.60	Spearman's rho: 0.78 Spearman's rho: 0.71
			output-increasing							TE <sub>y</sub> mean: 0.44 SE <sub>y</sub> mean: 0.85	TE <sub>y</sub> mean: 0.19 SE <sub>y</sub> mean: 0.76	Spearman's rho: 0.81 Spearman's rho: 0.66
Ondrich & Ruggiero (2001)	N/A	simulation study: 200 & 1000 units	N/A	N/A	Cobb-Douglas	stochastic vs deterministic prod. frontier	"using the rank correlation criterion, the COLS deterministic model performs as well as the stochastic frontier model regardless of actual measurement error variance and sample size" (p. 441)					
Park & Lesourd (2000)	South Korea	64 power plants, 1990	input-reducing	CRTS	translog	stochastic prod. frontier	TE <sub>x</sub> mean: 0.904	TE <sub>y</sub> mean: 0.761	Pearson's r: 0.636			
				VRTS			TE <sub>x</sub> mean: 0.934		Pearson's r: 0.612			
Ray & Mukherjee (1995)	US	123 electricity utilities, 1970	cost-reducing	VRTS	hybrid	stochastic TC frontier	EE <sub>x</sub> means: 0.82-0.92	EE <sub>x</sub> means: 0.88-0.97	Spearman's rho: 0.21-0.55			
Read & Thanassoulis (1996)	N/A	simulation study: 500 units	output-increasing	CRTS	Cobb-Douglas	stochastic prod. frontier	"...when the SF function does specify the underlying technology closely, SF estimates are... much better than DEA" (p. 28).					

**Table 1 (cont.) - Direct DEA vs SFA/DFA Comparisons**

Author / Date	Country	Units/Period	DEA Model		SFA/DFA Model		Findings		
			Orientation	RTS	Form	Frontier	DEA	SFA/DFA	Compare
Reinhard, Lovell & Thijssen (2000)	Holland	613 dairy farms, 1991- 1994	input-reducing	VRTS	restricted translog	stochastic prod. frontier	TE <sub>x</sub> means: 0.81-0.82	TE <sub>x</sub> means: 0.90	Spearman's rho: 0.70
			output-increasing				EnvE <sub>x</sub> means: 0.51-0.53	EnvE <sub>x</sub> means: 0.79-0.8	Spearman's rho: 0.49
							TE <sub>y</sub> means: 0.78-0.79	TE <sub>y</sub> means: 0.89	Spearman's rho: 0.76
Resti (2000)	N/A	simulation study: 50 & 500 'banks'	cost-reducing	CRTS VRTS	restricted translog	stochastic TC frontier	"...different techniques do not lead to dramatically different results when used in the same methodological framework (as far as selection of variables and of the relevant concept of efficiency are concerned)" (p. 574).		
Resti (1997)	Italy	270 banks, 1988 - 1992	cost-reducing	CRTS	restricted translog	stochastic TC frontier	EE <sub>x</sub> means: 0.66-0.69	EE <sub>x</sub> means: 0.69-0.70	Pearson's r: 0.87
				VRTS			EE <sub>x</sub> means: 0.73-0.76		Spearman's rho: 0.89
									Pearson's r: 0.71
									Spearman's rho: 0.73
Ruggiero (1999)	N/A	simulation study: 25 - 200 units	N/A	N/A	translog & Cobb-Douglas	stochastic vs deterministic prod. frontier	"...the parametric deterministic model outperformed the stochastic frontier model in nearly all of the model situations considered. ...In addition, the deterministic frontier approach was more consistent" (p. 562).		
Ruggiero & Vitaliano (1999)	US	520 school districts, 1990/91	cost-reducing	VRTS	Cobb-Douglas	stochastic TC frontier	EE <sub>x</sub> mean: 0.875	EE <sub>x</sub> mean: 0.860	Spearman's rho: 0.86
Scarsi (1999)	Italy	76 electricity firms, 1994 - 1996	output-increasing	VRTS	translog	stochastic prod. frontier	TE <sub>y</sub> means: 0.60-0.71	TE <sub>y</sub> mean: 0.62	Paired t: -0.65-6.41 p ≤ 0.518
Sharma, Leung & Zaleski (1997)	US	53 pig farms, 1994	output-increasing	CRTS	Cobb-Douglas	stochastic prod. frontier	TE <sub>y</sub> mean: 0.644	TE <sub>y</sub> mean: 0.749	Spearman's rho: 0.883
				VRTS			TE <sub>y</sub> mean: 0.726		Spearman's rho: 0.745
Sickles & Streitwieser (1992)	US	14 natural gas firms, 1977 - 1985	input-reducing	CRTS	translog	stochastic prod. frontier	TE <sub>x</sub> = TE <sub>y</sub> means: 0.78-0.86	TE <sub>y</sub> means: 0.70-0.78	Pearson's r: 0.53-0.54 Spearman's rho: 0.46-0.61
Singh, Coelli & Fleming (2000)	India	23 dairy plants, 1992/93 - 1996/97	cost-reducing	VRTS	Cobb-Douglas	stochastic prod. frontier	TE <sub>x</sub> mean: 0.91 AE <sub>x</sub> mean: 0.68 EE <sub>x</sub> mean: 0.62	TE <sub>x</sub> mean: 0.89 AE <sub>x</sub> mean: 0.91 EE <sub>x</sub> mean: 0.80	"...choice of method can have a significant impact on results" (p.25).
Souza, Alves & Avila (1999)	Brazil & Argentina	34 research units, 1996	output-increasing	CRTS	Cobb-Douglas	stochastic prod. frontier	TE <sub>x</sub> = TE <sub>y</sub> mean: 0.65	TE <sub>y</sub> means: 0.67-0.68	Pearson's r > 0.91 Spearman's rho > 0.90

**Table 1 (cont.) - Direct DEA vs SFA/DFA Comparisons**

Author / Date	Country	Units / Period	DEA Model		SFA/DFA Model		Findings		
			Orientation	RTS	Form	Frontier	DEA	SFA/DFA	Compare
Stone (2000)	Spain	21 High Courts, 1991	input-reducing	CRTS	Cobb-Douglas	stochastic TC frontier	TE <sub>x</sub> mean: 0.77	EE <sub>x</sub> means: 0.66-0.84	Pearson's r: 0.85-0.90
			cost-reducing				EE <sub>x</sub> mean: 0.66		Pearson's r: 0.82-0.89
Uri (2001)	US	19 telecom LECs 1988 - 1998	input-reducing	CRTS VRTS	Cobb-Douglas	stochastic prod. frontier	“...based on DEA results there was no identifiable improvement in technical efficiency over the 1988-1998 period ... results from a stochastic frontier approach confirm no change in technical efficiency” (p. 844).		
van den Broek, Førsund, Hjalmarsson & Meeusen (1980)	Sweden	28 dairy plants, 1964 -1973	N/A	N/A	Zellner-Revankar	deterministic prod. frontier stochastic prod. frontier	N/A	TE <sub>y</sub> means: 0.46-0.80 TE <sub>y</sub> means: 0.79-0.90	SFA TE <sub>y</sub> > DFA TE <sub>y</sub>
Wadud & White (2000)	Bangladesh	150 rice farms, 1997	output-increasing	CRTS	translog	stochastic prod. frontier	TE <sub>y</sub> means: 0.789	TE <sub>y</sub> means: 0.791	Spearman's rho: 0.777
				VRTS			TE <sub>y</sub> means: 0.858		Spearman's rho: 0.747
Webster, Kennedy & Johnson (1998)	Australia	301 private hospitals, 1991/92 - 1994/5	input-reducing	VRTS	translog & Cobb-Douglas	stochastic prod. frontier	TE <sub>x</sub> means: 0.39-0.90	TE <sub>y</sub> means: 0.71-0.79	Pearson's r: 0.29-0.79 Spearman's rho: 0.32-0.80
Whiteman (2000)	worldwide	41 electricity, 51 natural gas & 31 telecom firms, 1996 & 1996/97	input-reducing	CRTS	Cobb-Douglas	deterministic dist <sub>f</sub> s & ray prod. frontier stochastic dist <sub>f</sub> s & ray prod. frontier	“...the existence of stochastic error appears to have little impact on estimates of TE. Also there appear to be major problems in estimating multiple output stochastic frontier models which make the parametric deterministic models or DEA our preferred methodologies” (pp. 10 & 11).		
				VRTS					
				CRTS					
				VRTS					
Yin (2000)	worldwide	102 softwood pulp mills, 1996	cost-reducing	VRTS	Cobb-Douglas	stochastic TC frontier	EE <sub>x</sub> means: 0.857	EE <sub>x</sub> means: 0.922 EE <sub>x</sub> range: 0.751-0.976	Spearman's rho: 0.7
					translog		EE <sub>x</sub> range: 0.681-1.00	EE <sub>x</sub> means: 0.951 EE <sub>x</sub> range: 0.801-0.992	Spearman's rho: 0.5
Yu (1998)	N/A	simulation study: 250 units	output-increasing	CRTS VRTS	translog	stochastic prod. frontier	“...the one-step stochastic frontier method has a dominant advantage over other methods in dealing with exogenous variables...as long as exogenous variables are correctly identified and accounted for” (pp. 569 & 579).		

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## Conclusions & Directions for Future Research

This paper reviews empirical results drawn from published simulation studies with the aim of highlighting the pros and cons of competing methods for frontier estimation and efficiency measurement. In summary, the conclusions drawn by Resti (2000) seem appropriate:

“...none of these articles demonstrates that either DEA or econometric models have an absolute advantage over their competitors. Nevertheless, ...they succeed in indicating a range of specific situations (depending for example on the number of units in the sample, or on the amount of inefficiency and noise in the data) where some estimation technique proves superior” (Resti, 2000 p. 560).

In other words, results drawn from the simulation studies reviewed above confirm, clarify and/or contradict expected trade-offs, so that the choice of a 'correct' method is rather more clear cut in certain specific situations. The problem is that these specific situations (defined over key features of the simulated technology and production environment such as dimensionality of input/output space, economies of scale and scope, heterogeneity of production units, the extent of measurement error and random shocks, et cetera) are usually much simplified and occur relatively infrequently in the real world.

Our review of some 41 real-world DEA vs SFA/DFA comparisons suggests that calls for the parallel application of competing methods (to cross check results) have already been heeded. Unfortunately, real-world comparisons aren't much help either unless actual efficiency scores (like those underlying simulated data) are available for comparison purposes. It seems that the best of both worlds (realism *and* a criterion measure) is required in determining the relative precision (and policy value) of DEA, DFA and SFA. Both Yu (1998) and Resti (2000) have already made some progress in this regard by making their simulated data “more realistic and closer to the characteristics of existing industries” (Resti, 2000 p. 560). To provide further clarification as to the relative precision of competing methods, the now routine practice of cross checking should be taken one step further to include realistic simulation studies along-side real-world DEA vs SFA/DFA comparisons.

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