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The surface of the Arctic Ocean in summer is a mix of sea ice and water in both leads and melt ponds. Here we use data collected at multiple sites during the year-long experiment to study the Surface Heat Budget of the Arctic Ocean (SHEBA) to develop a bulk turbulent flux algorithm for predicting the surface fluxes of momentum and sensible and latent heat over the Arctic Ocean during summer from readily measured or modelled quantities. The distinctive aerodynamic feature of summer sea ice is that the leads and melt ponds create vertical ice faces that the wind can push against; momentum transfer to the surface is thus enhanced through form drag. In effect, summer sea ice behaves aerodynamically like the marginal ice zone, which is another surface that consists of sea ice and water. In our bulk flux algorithm, we therefore combine our SHEBA measurements of the neutral-stability drag coefficient at a reference height of 10 m, $C_{DN10}$, with similar measurements from marginal ice zones that have been reported in the literature to create a unified parametrization for $C_{DN10}$ for summer sea ice and for any marginal ice zone. This parametrization predicts $C_{DN10}$ from a second-order polynomial in ice concentration. Our bulk flux algorithm also includes expressions for the roughness lengths for temperature and humidity, introduces new profile stratification corrections for stable stratification, and effectively eliminates the singularities that often occur in iterative flux algorithms for very light winds. In summary, this new algorithm seems capable of estimating the friction velocity $u_*$ (a surrogate for the momentum flux) over summer sea ice with an absolute accuracy of 0.02–0.03 m s$^{-1}$; the sensible heat flux, with an accuracy of about 6 W m$^{-2}$; and the latent heat flux, with an accuracy of 3.5 W m$^{-2}$. Copyright © 2010 Royal Meteorological Society

Key Words: Arctic Ocean; bulk turbulent flux algorithm; drag coefficient; fictitious correlation; Monin-Obukhov similarity; roughness lengths; SHEBA; turbulence measurements

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1. Introduction

In the height of summer, the surface of the Arctic Ocean comprises sea ice and open water in leads and melt ponds. In effect, the leads and melt ponds create vertical sea-ice faces that the wind can push against (Figure 1). As a result, turbulent momentum transfer at the surface is enhanced because it now arises through a combination of skin friction at the horizontal surfaces and form drag associated with the (nearly) vertical surfaces.

During SHEBA, the year-long experiment in 1997 and 1998 to study the Surface Heat Budget of the Arctic Ocean (Uttal et al., 2002), our Atmospheric Surface Flux Group (ASFG) evaluated the neutral-stability drag coefficient at a 10 m reference height, \( C_{DN10} \), hourly at multiple sites over sea ice for nearly a year. Figure 2 shows the time series of these \( C_{DN10} \) values and the fractional surface coverage of water in leads and melt ponds.

On the basis of this plot, we divided the SHEBA year into just two aerodynamic seasons: winter and summer. In winter, the sea ice was compact, visually uniform, and snow covered; and the snow was dry enough and deep enough to drift and blow under wind forcing. In summer, in contrast, the snow was too wet and sticky to drift and eventually melted and disappeared. Furthermore, leads opened and melt ponds formed; at the height of summer, the surface around the SHEBA camp was about 60% bare ice and about 40% water. During SHEBA, aerodynamic summer ran from 15 May to 14 September 1998. Winter constituted the first half and the last couple of weeks of our SHEBA deployment.

An interesting feature of the \( C_{DN10} \) series in Figure 2 is that, during winter (especially the left half of the series), the \( C_{DN10} \) values are somewhat scattered although the sea ice surface appeared visually homogeneous. In summer (May–September in Figure 2), in contrast, although the surface appeared quite heterogeneous, the \( C_{DN10} \) values collapse to a common trend that mirrors the evolution of the water fraction. We infer that the form drag fostered by the vertical ice faces enhanced the turbulent mixing and, therefore, tended to homogenise the atmospheric surface layer in summer.

One of the goals of our participation in SHEBA was to develop a bulk flux algorithm (cf. Fairall et al., 1996, 2003) to accurately predict the turbulent surface fluxes of momentum and sensible and latent heat. Here we describe our bulk flux algorithm for summer sea ice. Andreas et al. (2003, 2005b) report our preliminary work on this algorithm. Andreas et al. (2010) describe our companion bulk flux algorithm for winter sea ice. Brunke et al. (2006) give alternative flux algorithms for both summer and winter based on this same SHEBA dataset; but our approach differs significantly from theirs. First, we acknowledge the contributions of form drag on the parametrization for momentum transfer in summer; and second, our analysis minimises the effects of fictitious correlation that, we believe (Andreas et al., 2010), influenced the analyses by Brunke et al.

We base our bulk flux algorithm on Monin–Obukhov similarity theory. Using data from our main 20 m SHEBA tower, Grachev et al. (2007a, 2007b) developed new wind speed and scalar profile similarity functions to specifically treat the very stable stratification that we encountered during SHEBA. We include those new functions in our flux algorithm.

Another essential feature of a bulk flux algorithm is a module that predicts the roughness length for wind speed (\( z_0 \)) or, equivalently, \( C_{DN10} \). Morphologically, the...
marginal ice zone is like summer sea ice: The surface consists of significant areas of both ice and water (e.g. Guest and Davidson, 1987, 1991), and form drag is presumed to crucially influence surface momentum exchange (e.g. Andreas et al., 1984; Birnbaum and Lüpkes, 2002). We noticed that measurements of \( C_{DN10} \) in marginal ice zones link nicely with our measurements of \( C_{DN10} \) over summer sea ice and, therefore, develop a unified parametrization of \( C_{DN10} \) for both summer sea ice and marginal ice zones that is a function of just ice concentration.

Yet another module in a bulk flux algorithm must predict the roughness lengths for temperature \((z_T)\) and humidity \((z_Q)\). Our data show that the ratios \( z_T/z_0 \) and \( z_Q/z_0 \) as functions of the roughness Reynolds number, \( R_s = u_*\, z_0/\nu \), where \( u_* \) is the friction velocity and \( \nu \) is the kinematic viscosity of air, follow Andreas’s (1987) theoretical model. Plots of these quantities, however, are prone to fictitious correlation if measured values are used throughout to test Andreas’s model (Andreas, 2002; Andreas et al., 2010). We circumvent this problem by using data to compute \( z_T/z_0 \) and \( z_Q/z_0 \) but using our bulk flux algorithm to compute \( R_s \).

## 2. Bulk flux algorithm

Energy budget studies or atmospheric models with sea ice as the lower boundary almost always estimate the surface fluxes of momentum \((\tau)\) and sensible \((H_s)\) and latent \((H_L)\) heat from a bulk flux algorithm (e.g. Maykut, 1978; Ebert and Curry, 1993; Jordan et al., 1999; Briegleb et al., 2004; Huwald et al., 2005). In our algorithm, the relevant flux equations take the form

\[
\tau = -\rho \, \overline{w' \nu'} \equiv \rho \, u_*^2 = \rho \, C_D \, \beta_T, \tag{2.1a}
\]

\[
H_s = \rho \, c_p \, \overline{w' \theta'} = \rho \, c_p \, C_H \, \beta_T \, T_s \left( \Theta_s - \Theta_T \right), \tag{2.1b}
\]

\[
H_L = \rho \, L \, \overline{w' \psi'} = \rho \, L \, C_E \, \beta_T \, Q_s \left( \Theta_s - \Theta_T \right). \tag{2.1c}
\]

In these, \( u, w, \theta, \) and \( q \) are turbulent fluctuations in longitudinal wind speed, vertical wind speed, temperature, and specific humidity; the overbar indicates a time average. Also, \( \rho \) is the air density; \( c_p \) the specific heat of air at constant pressure; \( L \), the latent heat of sublimation; \( S_s \), the effective wind speed at reference height \( r \); \( \Theta_s \) and \( \Theta_T \), the potential temperature and specific humidity at \( r \); and \( \Theta_s \) and \( Q_s \), the temperature and specific humidity at the surface. We evaluate \( Q_s \) as the saturation value at \( \Theta_s \). See Andreas (2005) for the functions we use for calculating quantities like \( \rho, c_p, L, \) and \( Q_s \). Equation (2.1a) also defines the friction velocity, \( u_* \), which we use henceforth as a surrogate for the momentum flux.

The crux of any bulk flux algorithm is evaluating the transfer coefficients for momentum, sensible heat, and latent heat appropriate for height \( r \) respectively, \( C_{Dr}, C_{HR}, \) and \( C_{Er} \) in (2.1). These generally derive from Monin–Obukhov similarity theory and formally are (e.g. Garratt, 1992, p 52 ff; Andreas, 1998)

\[
C_{Dr} = \frac{k^2}{[\ln(r/z_0) - \psi_m(r/L)]^2}, \tag{2.2a}
\]

\[
C_{HR} = \frac{k^2}{[\ln(r/z_0) - \psi_m(r/L)]\ln(r/z_T) - \psi_H(r/L)}, \tag{2.2b}
\]

\[
C_{Er} = \frac{k^2}{[\ln(r/z_0) - \psi_m(r/L)][\ln(r/z_Q) - \psi_h(r/L)]}. \tag{2.2c}
\]

In these, \( k \) (= 0.40) is the von Kármán constant, and \( \psi_m \) and \( \psi_h \) are empirical functions of the Obukhov length,

\[
L = -\frac{\overline{\Theta_s}}{\overline{w' \theta'}} \left[ \frac{u_*^3}{\overline{w' \theta'}} \right] = -\frac{\overline{\Theta_s}}{\overline{w' \theta'}} \left[ \frac{u_*^3}{\overline{w' \theta'}} + \frac{0.61 \nu}{1 + 0.61 \nu \overline{w' \theta'}} \right]. \tag{2.3}
\]

Here, \( g \) is the acceleration of gravity; \( \overline{\Theta_s}, \overline{w' \theta'}, \) and \( \overline{Q} \) are surface-layer averages of the air temperature, virtual temperature, and specific humidity; and \( \overline{w' \theta'} \) is the flux of virtual temperature.

For the stratification corrections \( \psi_m \) and \( \psi_h \) in (2.2), we use Paulson’s functions (1970) in unstable stratification and the functions from Grachev et al. (2007a) in stable stratification. These latter functions are based on our SHEBA tower data and include proper treatment of a heretofore unrecognized scaling regime in very stable stratification. The \( z_0, z_T, \) and \( z_Q \) in (2.2) are the roughness lengths for wind speed, temperature, and humidity, respectively.

Finally, \( S_r \) in (2.1) is an effective wind speed. For compatibility with the Coupled Ocean–Atmosphere Response Experiment (COARE) algorithm (Fairall et al., 1996, 2003) and other recent flux algorithms (e.g. Andreas et al., 2008), we acknowledge that in unstable stratification gustiness enhances turbulent exchange and therefore model

\[
S_r = \left( U_r^2 + \beta_g^2 \, w_s^2 \right)^{1/2}. \tag{2.4}
\]

Here, \( U_r \) is the actual measured or modelled mean magnitude of the vector wind at reference height \( r \); \( \beta_g \) is 1.25 (Fairall et al., 1996), and \( w_s \) is Deardoff’s (1970) convective velocity scale (Godfrey and Beljaars, 1991):

\[
w_s = u_* \left( -\frac{z_i}{k \, L} \right)^{1/3}, \tag{2.5}
\]

where \( z_i \) is the depth of the convective boundary layer. We take \( z_i \) as a constant, 600 m (Kahl, 1990; Serreze et al., 1992; Bradley et al., 1993; Tjernström and Graversen, 2009), because variability in it does not have much effect on our calculations.

We adopt the suggestion by Jordan et al. (1999) that a similar ‘windless’ coefficient is necessary for stable stratification but express it as

\[
S_r = U_r + 0.5 \text{sech}(U_r). \tag{2.6}
\]

Here, both \( U_s \) and \( S_r \) are in m s\(^{-1}\). Equation (2.6) is similar to Mahrt’s (2008) parametrization that includes a term to quantify mesoscale meandering flow where we have the sech term.

In effect, both (2.4) and (2.6) prevent a singularity in the bulk flux algorithm by making the transfer coefficients well behaved in light winds (cf. Godfrey and Beljaars, 1991; Fairall et al., 1996; Zeng et al., 1998; Andreas et al., 2008). If we use \( U_{\tau} \) instead of \( S_r \), the transfer coefficients must approach infinity to maintain finite fluxes as \( U_t \) approaches zero. But as \( U_t \) increases from zero, the \( S_r \) values calculated with either (2.4) or (2.6) quickly approach \( U_t \) for Arctic
conditions. For instance, when $U_r$ reaches 2.2 m s$^{-1}$, $S_r$ is already within 5% of $U_r$.

Because (2.1) and (2.2) are coupled through the Obukhov length (2.3), they must be solved iteratively using the mean measured or modelled conditions: namely, $U_r$, $\Theta$, $Q_r$, and $\Theta_r$. Moreover, (2.4) and our algorithms for $z_T$ and $z_Q$ also include $u_*$, as we will show. These equations must also be part of the iteration. That iteration usually converges in 3 to 5 steps.

In the analyses reported here, we found it more direct to estimate $C_{DN10}$ than $z_0$ over summer sea ice (cf. Andreas et al., 2010). These two parameters of momentum transfer are related through (2.2a), which in neutral stratification for a standard reference height of 10 m is

$$C_{DN10} = \left[ \frac{k}{\ln(10/z_0)} \right]^2,$$  \hspace{1cm} (2.7)

where $z_0$ must be in metres. The $C_{DN10}$ values computed from (2.7) (once we first found $z_0$, as described later) are what we plotted in Figure 2.

Alternatively, the parametrization that we describe later predicts $C_{DN10}$. We obtain $z_0$ for use in (2.2) from this value by inverting (2.7).

3. The SHEBA data

The SHEBA ice camp drifted approximately 2700 km in the Beaufort Gyre between 2 October 1997 and 11 October 1998 (Uttal et al., 2002). It started in the Beaufort Sea, drifted westward into the Chukchi Sea, then turned north into the Arctic Ocean near the date line.

During our SHEBA deployment, we had one central site in the SHEBA ice camp and, usually, four remote sites that ranged in distance from 0.25 to 30 km from the main camp. We serviced these remote sites about once a week either on foot, by snowmobile, or by helicopter, depending on ice conditions. Andreas et al. (1999, 2002, 2006, 2010), Persson et al. (2002), and Grachev et al. (2005, 2007a) describe the instruments that our Atmospheric Surface Flux Group (ASFG) deployed during SHEBA and review our data processing. Persson et al., in particular, show pictures of the instruments at our main site.

The centrepiece of our site in the SHEBA camp was a 20 m tower instrumented at five levels with identical sonic anemometer/thermometers (K-type sonics from Applied Technologies, Inc.: ATTI) and Vaisala HMP235 temperature and humidity sensors. The tower also held one Ophir fast-responding hygrometer that was mounted at 8 m, near the sonic at that level.

Through eddy-covariance measurements using standard turbulence processing, as described in Persson et al. (2002), Grachev et al. (2005, 2007a), and Andreas et al. (2006), we measured the momentum flux $\tau$ and the sensible heat flux $H_s$ for each of the five tower levels and the latent heat flux $H_l$ at one level (see (2.1)). This latter was the only direct, long-term measurement of latent heat flux from SHEBA.

The sonics also provided the mean wind speed in (2.1), $U_r$, at each level. The Vaisala HMP235s provided the mean temperature and specific humidity, $\Theta$, and $Q_s$, needed in (2.1).

Near this ASFG tower was a full suite of radiometers for measuring incoming and outgoing long-wave and short-wave radiation and several additional sensors for measuring surface temperature, $\Theta_s$ (e.g. Claffey et al., 1999; Persson et al., 2002). Here and for the remote sites, we processed the Eppeley pyrgeometer data to obtain the long-wave radiative fluxes using the method that Fairall et al. (1998) recommend. That is, we measured both dome and case temperatures and corrected the fluxes with these.

Generically, for $\Theta_s$ we used the value implied by the emitted $(Q_{r\uparrow})$ and incoming $(Q_{r\downarrow})$ long-wave radiation measured by our pyrgeometers:

$$\Theta_s = (\sigma \varepsilon)^{-1/4} \left( Q_{r\uparrow} - (1 - \varepsilon)Q_{r\downarrow} \right)^{1/4}. \hspace{1cm} (3.1)$$

Here, $\varepsilon$ (= 0.99; Dozier and Warren, 1982; Warren, 1982; Jordan et al., 1999) is the surface emissivity, and $\sigma$ (= 5.67051 $\times 10^{-8}$ W m$^{-2}$K$^{-4}$) is the Stefan–Boltzmann constant. See the SHEBA data archive at http://www.eol.ucar.edu/projects/sheba for tabulations and descriptions of these surface temperature data and the other datasets that we use in this study.

Our remote sites were instrumented with Flux-PAM (portable automated mesonet) stations from the National Center for Atmospheric Research instrument pool (Militzer et al., 1995; Horst et al., 1997). Our first four sites, which we deployed in October 1997, were named Atlanta, Baltimore, Cleveland, and Florida. The Cleveland station, however, was damaged by a pressure ridge in early February 1998 and removed from service for repairs.

The original Florida site was on smooth ice within 400 m of our main tower. Because of ice deformation, however, we extracted this PAM station and placed it and the refurbished Cleveland station next to our main tower for intercomparison during 1–20 April 1998. We then re-established the Florida site on a pressure ridge 250 m from our main tower, where it remained for the rest of the deployment.

In mid-April, we redeployed the refurbished Cleveland station at a new site called Seattle. Seattle, however, became untenable because of ice motions; and this PAM station was again redeployed in mid-June 1998 to a site named Maui. That Maui site lasted until late September 1998, as did the Atlanta, Baltimore, and Florida sites.

We have found the turbulence measurements from Seattle to be disturbed by a pressure ridge just upwind of the station and, thus, do not include data from that site in our analysis. We do use data from the other five PAM sites, however.

Each Flux-PAM station measured at one height the same quantities that we measured at the ASFG tower: wind speed and direction, temperature, relative humidity, and the turbulent fluxes of momentum and sensible heat. The website http://www.eol.ucar.edu/isl/projects/SHEBA contains instrument details, a history of each of the PAM sites deployed during SHEBA, and information on data processing.

Briefly, the PAM stations provided hourly averaged data, as did the main tower site. Each PAM station used a sonic anemometer/thermometer mounted at a height between 2.5 and 3.5 m, depending on instrument type, to measure the turbulent fluxes of momentum and sensible heat by eddy-covariance techniques (i.e. $\tau$ and $H_s$ in (2.1)). We used sonics from both Gill (Solent R2) and Applied Technologies, Inc. (K-type), for the turbulence measurements at these sites.

Sonic anemometer/thermometers do not measure the instantaneous air temperature, $\tilde{\theta}$ (=$\Theta + \tilde{\theta}$). Rather, the measured instantaneous ‘sonic’ temperature, $\tilde{\theta}_s$, is a
combination of $\bar{\theta}$ and the instantaneous specific humidity, $\bar{q}$ (Schotanus et al., 1983; Kaimal and Gaynor, 1991; Larsen et al., 1993):

$$\bar{\theta}_s = \bar{\theta}(1 + 0.51\bar{q}).$$  \hspace{1cm} (3.2)

This $\bar{\theta}_s$ is very close to the instantaneous virtual temperature,

$$\bar{\theta}_v = \bar{\theta}(1 + 0.61\bar{q}).$$  \hspace{1cm} (3.3)

Consequently, the covariance between fluctuations in sonic temperature ($\theta_s$) and in the vertical velocity ($w$) is

$$\bar{w}\theta_s = \bar{w}(1 + 0.51Q) + 0.51\bar{w}\bar{q}.$$  \hspace{1cm} (3.4)

That is, this covariance is almost identical to the flux of virtual temperature required in the Obukhov length, (2.3), and can be used there with negligible error (e.g. Kaimal and Finnigan, 1994, p 224).

In some cases, though, obtaining the true sensible heat flux, $\rho \bar{c}_w \bar{w}\theta$, from a sonic anemometer requires corrections based on (3.4) and an estimate of $\bar{w}\bar{q}$. For the five sonics on our main tower, we made these corrections using either the measured $\bar{w}\bar{q}$ or a bulk flux estimate of $\bar{w}\bar{q}$ (Persson et al., 2002; Grachev et al., 2005). The Flux-PAM stations, however, made no measurement of $\bar{w}\bar{q}$; we consequently used $\bar{w}\theta_s$ directly to estimate $\bar{w}\theta$ for these. Because of the low humidity and small Bowen ratio over sea ice, $\bar{w}\theta$ and $\bar{w}\theta_s$ are typically within 5% of each other and are essentially interchangeable in our dataset (cf. Andreas et al., 2005a; Grachev et al., 2005).

To measure mean temperature and relative humidity at the Flux-PAM sites, we used Vaisala HMD50Y sensors in mechanically aspirated radiation shields (Andreas et al., 2002). Each PAM station also measured barometric pressure with a Vaisala PTB 220B digital barometer. Because our main ASFG tower had no measurement of barometric pressure, we used the pressure data from the Florida PAM site at the tower site also, because only a few hundred metres separated the two sites.

Each PAM station included sets of up-looking and down-looking radiometers to measure short-wave (Kipp and Zonen model CM21) and long-wave (Eppley model PIR) radiation. We obtained surface temperature at the PAM sites exclusively from these long-wave radiometers through (3.1).

We saw early in our SHEBA deployment that sensor riming was a problem at the PAM sites. Rime ice occasionally coated the domes of the radiometers (especially the up-looking ones) and, thereby, ruined the radiation measurements and our estimates of surface temperature. Rime also collected on the sonics; and when it coated the transducers, we lost wind information. In early March 1998, we installed effective heaters and blowers on all four radiometers at each site. This heating minimised the effects of dome icing for the rest of the experiment.

To mitigate riming on the PAM sonics, in mid-January 1998 we fixed heating tape around each transducer and at several locations along the support arms. The computer-controlled data acquisition system that monitored the PAM stations turned this heating on, however, only when it noticed that data returns from a sonic were deteriorating; and this heating remained on until the data returns again reached 100%. We flagged these heating periods and did not use any flux data that were collected when the heaters were on.

The sonics and radiometers at our main site did not suffer as much from riming as the PAM instruments. First, someone was always attending the instruments at our main site and cleaning them as necessary. Second, the radiometers at our main site had effective blowers and heaters from the beginning of the experiment. Third, our 20 m tower was fitted exclusively with ATI sonics, which seemed to resist riming much better than the Gill sonics that were originally mounted on each PAM station. (We later replaced the Gill sonics with ATI sonics at the three most remote PAM sites.)

From the turbulent fluxes and mean meteorological quantities measured at multiple levels on our main tower and at the Flux-PAM sites, we could compute the turbulent transfer coefficients $C_{D_{h1}}$, $C_{h1}$, and $C_{D_0}$ from (2.1). These, in turn, give us estimates of the roughness lengths from (2.2):

$$z_0 = r \exp[-k_1 C_{D_{h1}}^{-1} + \psi_m(r/L)],$$

$$z_T = r \exp[-k_1 C_{D_{h1}}^{-1} + \psi_h(r/L)],$$

$$z_Q = r \exp[-k_1 C_{D_{h1}}^{-1} + \psi_h(r/L)].$$  \hspace{1cm} (3.5a)

(3.5b)

(3.5c)

Here, the roughness lengths are in metres if $r$ is in metres.

4. Uncertainty analysis and quality controls

Turbulence data generally have a lot of random scatter. Roughness lengths evaluated from these data, in turn, are commonly quite scattered because they derive from (3.5) and (2.1) and thus rely on several mean and turbulence variables. The only way to overcome this scatter is to collect a lot of high-quality data.

Table I summarises typical uncertainties in the quantities that we measured at the ASFG tower and at the PAM sites during SHEBA and in the variables that we calculate from these data. We base these estimates on previous similar summaries by Fairall et al. (1996) and Persson et al. (2002), on data analyses by Andreas et al. (2002), on similar uncertainty analyses by Andreas et al. (2005a, 2006), and on studies done for this paper. The main messages in Table I are that evaluations of $z_0$ are uncertain by a factor of 3, evaluations of $z_T$ and $z_Q$ are uncertain by a factor of 200, and $CD_{DN10}$ has an uncertainty of ±119%.

In light of these uncertainties, we screened the data that we used in our analyses of $z_0$, $z_T$, $z_Q$, and $CD_{DN10}$ to ensure a reasonable signal-to-noise ratio. If any hour of data from a PAM station or from any level on the ASFG tower met the following criteria, we excluded the data as inadequate for determining $z_0$, $z_T$, $z_Q$, and $CD_{DN10}$:

$$\tau \leq 0 \text{ N m}^{-2},$$

$$|H_u/\rho c_p| \leq 0.005 \text{ C m s}^{-1},$$

$$|H_L/\rho L_v| \leq 2.5 \times 10^{-2} \text{ (kg kg}^{-1}) \text{ (m s}^{-1}),$$

$$|\Theta_s - \Theta_i| \leq 0.5 \text{ C},$$

$$|Q_s - Q_i| \leq 1.0 \times 10^{-5} \text{ kg kg}^{-1}.$$
Table I. Typical uncertainties in our hourly SHEBA measurements and in the variables that we calculate from these measurements

<table>
<thead>
<tr>
<th>Variable</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Measured Variables</strong></td>
<td></td>
</tr>
<tr>
<td>Measurement height, ( r )</td>
<td>±0.3 m</td>
</tr>
<tr>
<td>Wind speed, ( U_r )</td>
<td>±0.03 m s(^{-1})</td>
</tr>
<tr>
<td>Air temperature, ( \Theta_r )</td>
<td>±0.2°C</td>
</tr>
<tr>
<td>Relative humidity, ( \text{RH} )</td>
<td>±3%</td>
</tr>
<tr>
<td>Specific humidity, ( \text{Q}_r )</td>
<td>±5%</td>
</tr>
<tr>
<td>Surface temperature, ( \Theta_s )</td>
<td>±0.5°C</td>
</tr>
<tr>
<td>Surface specific humidity, ( \text{Q}_s )</td>
<td>±5%</td>
</tr>
<tr>
<td>Friction velocity, ( u_* )</td>
<td>±0.02 m s(^{-1})</td>
</tr>
<tr>
<td>Sensible heat flux, ( H_s )</td>
<td>±20%</td>
</tr>
<tr>
<td>Latent heat flux, ( H_L )</td>
<td>±20%</td>
</tr>
<tr>
<td><strong>Calculated Variables</strong></td>
<td></td>
</tr>
<tr>
<td>Neutral-stability, 10 m drag coefficient, ( C_{DN10} )</td>
<td>±11%</td>
</tr>
<tr>
<td>Roughness length for wind speed, ( z_0 )</td>
<td>( \frac{1}{3} ) – 3 times computed ( z_0 )</td>
</tr>
<tr>
<td>Roughness length for temperature, ( z_T )</td>
<td>( \frac{1}{200} ) – 200 times computed ( z_T )</td>
</tr>
<tr>
<td>Roughness length for humidity, ( z_Q )</td>
<td>( \frac{1}{200} ) – 200 times computed ( z_Q )</td>
</tr>
</tbody>
</table>

Only data that fail (4.1a) or (4.1b) prevent our computing \( z_0 \) and \( C_{DN10} \). (Remember, we need \( H_s \) – actually \( \rho \, \text{cp} \, \Theta_1 / \nu \) – to compute the Obukhov length.) Data that fail (4.1a), (4.1b) or (4.1d) prevent our computing \( z_T \). A failure to pass any of (4.1a), (4.1b), (4.1c) or (4.1e) prevent our computing \( z_Q \).

As additional screening, if any calculated roughness lengths met the following criteria, we assumed the result was unrealistic and ignored it for our analyses of \( z_0 \), \( z_T \), and \( z_Q \):

\[
0, z_T \text{ or } z_Q \geq 0.1 \text{ m}, \quad (4.2a)
\]
\[
z_T \text{ or } z_Q \leq 7 \times 10^{-8} \text{ m}. \quad (4.2b)
\]

We instituted (4.2a) because roughness lengths simply cannot be this large over sea ice (e.g. Banke et al., 1980; Overland, 1985; Guest and Davidson, 1991; Andreas, 1995). The limit on \( z_0 \) in (4.2a) also implies that we did not let \( C_{DN10} \) be larger than \( 7.54 \times 10^{-3} \). The second limit, (4.2b), is the approximate mean free path of air molecules at sea level. We presume that the surface exchange of heat and moisture cannot occur at scales smaller than this (cf. Andreas and Emanuel, 2001; Andreas et al., 2008).

In effect, the screening criteria (4.1) and (4.2) excluded from our analysis situations in which Monin–Obukhov similarity theory breaks down. In stable boundary layers, a host of phenomena occur that violate similarity theory; for example, the boundary layer may be so thin that a constant-flux layer does not exist, the turbulence may be only intermittent, gravity waves can confound the turbulence series, or a low-level jet rather than the surface may be the source of the turbulence (e.g. Mahrt, 1998, 1999; Grachev et al., 2005). Tests (4.1) and (4.2) tended to keep us out of these regimes.

Because the five ASFG tower levels each had a sonic anemometer/thermometer and a temperature and humidity sensor, any hour of data could yield from none to five independent estimates of \( z_0 \) and \( z_T \) from this site. (We did use the same \( \Theta_r \) for all estimates, though.) We do not report all of these values. Rather, we took the median value for all results that passed our screening for that hour. The median is the ‘most common robust and resistant measure of central tendency’ (Wilks, 2006, p 26).

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Figure 3. The 10-day averages of summer \( C_{DN10} \) values in Figure 2 from the ASFG tower and from the Flux-PAM sites called Atlanta, Baltimore, Florida, and Maui are plotted against ice concentration, \( C_i \). The figure also shows \( C_{DN10} \) values obtained in the Antarctic marginal ice zone (MIZ; Andreas et al., 1984) and the Arctic MIZ (Guest and Davidson, 1987; Anderson, 1987; Birnbaum and Lüpkes, 2002). The solid curve is (5.2); the dashed curve is Lüpkes and Birnbaum’s (2005) Equation (22).

5. Drag coefficient over summer sea ice and in the marginal ice zone

For the \( C_{DN10} \) data depicted in Figure 2, we assigned an ice concentration (defined as the fractional surface area of ice) appropriate for the middle of the averaging period. (Remember, the \( C_{DN10} \) markers represent 8, 10, or 11 days of averaged hourly data.) Figure 3 shows a plot of these averaged \( C_{DN10} \) values against ice concentration, \( C_i \). We found \( C_i \) from the constant:

\[
1 = C_i + C_L + C_p, \quad (5.1)
\]
where $C_L$ and $C_P$ are, respectively, the area fractions of leads and melt ponds shown in Figure 2.

The SHEBA summer data, which are on the right side of Figure 3, for ice concentrations between 0.6 and 1.0, reiterate what we observed in Figure 2. As the ice concentration decreases or as the total water fraction ($C_W = 1 - C_I$) increases, $C_{DN10}$ increases. An increasing water fraction means more vertical ice faces for the wind to push against and thereby to transfer momentum by form drag – that is, through pressure forces.

Classic studies in wind tunnels of momentum transfer over arrays of solid roughness elements (e.g. Marshall, 1971; Raupach et al., 1980) and ensuing analyses (e.g. Wooding et al., 1973; Arya, 1975; Raupach, 1992; MacDonald et al., 1998; Shao and Yang, 2005) typically relate the effective roughness height or the drag coefficient over the array to the areal coverage of the obstacles. The data and analyses repeatedly show that, as the obstacle packing increases from sparse coverage to nearly complete coverage, the roughness length or the drag coefficient increases from a minimum, reaches a maximum for intermediate packing density, then decreases as the obstacles become more tightly packed.

The theoretical interpretation for these observations is as follows. With loose packing, all obstacles have high pressure on the upwind face and low pressure on the downwind face caused by flow separation. Thus, momentum transfer by pressure forces increases as the areal coverage of obstacles increases because of the increasing frontal area of the obstacles. As the obstacles become more tightly packed, however, the flow separation bubble downwind of an obstacle encroaches on the next obstacle. That obstacle is, thus, somewhat ‘sheltered’ by the upwind obstacle and does not feel the full force of the wind. As a result, momentum transfer becomes less efficient. Eventually, the packing becomes so tight that all vertical faces are sheltered, and transfer by pressure forces is ineffective. In short, $z_0$ and $C_{DN10}$ are low for a surface with no obstacles, increase to maxima for intermediate packing density, then decrease to local minima for tightly packed obstacles.

Andreas et al. (1984) based their interpretation of $C_{DN10}$ values measured in the Antarctic marginal ice zone (MIZ) on form drag arguments like these. Because marginal ice zones are mixes of ice and water, as is summer sea ice, we have added four sets of observations from marginal ice zones to Figure 3. The data from Andreas et al. (1984) are single-point observations for which $C_{DN10}$ was based on radiosonde ascents. Guest and Davidson (1987) and Anderson (1987) obtained their data from inertial-dissipation measurements on ships in the East Greenland Sea. Generally, their data points represent multiple measurements for the given ice concentration. The data from Birnbaum and Lüpkes (2002) are a synthesis of multiple aircraft turbulence measurements collected during flights over the Fram Strait and reported by Hartmann et al. (1994) and Mai et al. (1996).

In Figure 3, all four sets of MIZ $C_{DN10}$ values start at the open-ocean value, typically $1.5 \times 10^{-3}$, and increase from there with increasing ice concentration. Three of the MIZ sets include relatively large values for $C_{DN10}$ for $C_I$ on the order of 0.8, but the larger dataset from Birnbaum and Lüpkes (2002) reaches a maximum near $C_I = 0.6$ then falls right along the cluster of SHEBA values to the local minimum for compact sea ice.

Birnbaum and Lüpkes (2002) and Lüpkes and Birnbaum (2005) developed physically based parametrizations to describe the behaviour of the drag coefficient in the marginal ice zone. These models require knowing or parametrizing such physical quantities as the freeboard of the ice floes, the height of the ridge that generally borders floes in the MIZ, the width of typical floes, and the open water distance between floes. Through sensitivity studies, these models provide good insights into the processes and parameters that control momentum exchange in a sea ice environment that consists of both ice and water; but the models are much too complex for use in global climate models and even in sea ice models – they require too many unmeasured and unmodelled variables.

Lüpkes and Birnbaum (2005) realised the impracticality of their full model for large-scale computing and therefore simplified it to predict $C_{DN10}$ as a function of just ice concentration. Following Andreas et al. (1984), we fitted by eye a second-order polynomial in ice concentration to the combined MIZ and SHEBA data in Figure 3 before we had seen the Lüpkes and Birnbaum paper. That fit is

$$10^3 C_{DN10} = 1.500 + 2.233 C_I - 3.333 C_I^2,$$

where $C_I$ is still the fractional ice concentration ($0 \leq C_I \leq 1.0$). As do Lüpkes and Birnbaum, in fitting (5.2), we discounted the few large $C_{DN10}$ values at large $C_I$ from marginal ice zones: The 10,000 hours of SHEBA summer data at these concentrations overwhelm these outliers.

Figure 3 also shows the fit that Lüpkes and Birnbaum (2005) made to just their own MIZ data. This result is their Equation (22), which uses ice concentration as the only independent variable but requires specifying $C_{DN10}$ over open water and over compact sea ice. We used $1.5 \times 10^{-3}$ and $1.4 \times 10^{-3}$, respectively, for these values to obtain the Lüpkes and Birnbaum curve in Figure 3.

The Lüpkes and Birnbaum (2005) curve in Figure 3 is higher than third order in $C_I$ and, therefore, more complex than our (5.2); but the two equations differ little in how well they represent the data shown in Figure 3. Because of its relative simplicity, we retain (5.2) in our bulk flux algorithm as the prediction for $C_{DN10}$ (and, thus, $z_0$) for summer sea ice and in any marginal ice zone.

## 6. Estimating the turbulent heat fluxes

### 6.1. Mosaic method

In summer, when the Arctic surface is a patchwork of sea ice, melt ponds, and leads, estimating the sensible and latent heat fluxes, $H_s$ and $H_L$, from a bulk flux algorithm might require weighted averages of the fluxes from the individual surfaces. With sensible heat flux as an example, this hypothesis is (cf. Andreas and Makshtas, 1985)

$$H_s = C_{i 3} H_{s,i} + C_{i 4} H_{s,4} + C_P H_{s,P}.$$

Here, $H_{s,i}$, $H_{s,4}$, and $H_{s,P}$ are the fluxes that we would compute using (2.1b) over ice, leads, and melt ponds; and $H_s$ is the area average. This approach is usually termed the mosaic method (e.g. Vihma, 1995).

On substituting (2.1b) for the various fluxes in (6.1), we obtain

$$H_s = \rho_s c_p, i H_{s,i} C_{Hr,i} S_{r,i} (\Theta_{s,i} - \Theta_{r,i})$$

$$+ \rho_s c_p, 4 H_{s,4} C_{Hr,4} S_{r,4} (\Theta_{s,4} - \Theta_{r,4})$$

$$+ \rho_p c_p, P H_{s,P} C_{Hr,P} S_{r,P} (\Theta_{s,P} - \Theta_{r,P}).$$

Here, subscripts i, L, and P denote individual values appropriate over ice, leads, and melt ponds. Because the leads and ponds were fairly small, we can assume that the air at reference height \( r \) was well mixed. Thus, we can approximate \( S_{r,i} = S_{r,L} = S_{r,P} = S \) and \( \Theta_{r,i} = \Theta_{r,L} = \Theta_{r,P} = \Theta_r \). Likewise, since the temperatures of the air and the various surfaces were all within a few degrees of 0°C in our SHEBA summer data (Andreas et al., 2002; Persson et al., 2002), we can further approximate \( \rho_i = \rho_L = \rho_P = \rho \) and \( c_{p,i} = c_{p,L} = c_{p,P} = c_p \). These conditions on wind speed and temperature further suggest that \( C_{Hr,i}, C_{Hr,L}, \) and \( C_{Hr,P} \) are all approximately equal. Call the common value \( C_{Hr} \).

With these approximations, (6.2) simplifies to

\[
H_s = \rho_c c_p C_{Hr} S_r (\Theta_{s,Ave} - \Theta_r),
\]

where the areally averaged surface temperature is

\[
\Theta_{s,Ave} = C_l \Theta_{s,L} + C_p \Theta_{s,P}.
\]

That is, over summer sea ice, when surface heterogeneities are small and air and surface are close to isothermal, we can approximate the areally averaged sensible heat flux with (2.1b) and a mosaic-based estimate of surface temperature. Incidentally, Overland et al. (2000) used equations comparable to (6.3) and (6.4) to estimate the regional sensible heat flux over winter Arctic sea ice.

Nearly the same sequence of equations and approximations that leads to (6.3) and (6.4) produces a similar conclusion for estimating the latent heat flux over summer sea ice. The only change is that we must account for the difference between the latent heat of sublimation over ice, \( L_i \), and the latent heat of vaporization, \( L_o \), over the leads and ponds, where \( L_i \) is the latent heat of fusion. As a result, the equation analogous to (6.3) for the areally averaged latent heat flux has an extra term:

\[
H_l = \rho_l L_i C_{E_l} S_i (Q_{s,Ave} - Q_s) - \rho L_o C_{E_l} S_i (Q_{s,Ave} - Q_s) \frac{(Q_s - Q_{s,i})}{(Q_{s,i} - Q_{s})}.
\]

Here, \( Q_{s,Ave} \) is obtained as \( \Theta_{s,Ave} \) in (6.4) from specific humidities at the surfaces of the ice, and ponds: \( \Theta_{s,L} \), \( \Theta_{s,P} \), and \( \Theta_{s,P} \) respectively. Moreover, in light of the scatter we find in \( H_l \), we can ignore the second term on the right of (6.5) because it is at least eight times smaller than the first term (i.e. \( L_o/L_i \approx 28.3/3.3 \)) and approaches zero as \( C_i \) approaches one.

With the conclusion above that \( C_{Hr} \) is uniform over summer sea ice, (3.5b) implies that the roughness length \( z_T \) is also uniform. In effect, both are now interpreted as area averages. We have hypothesised, though, that \( C_{Hr} \) for use in (3.5b) to find \( z_T \) must be obtained from (6.3) and our measured value of \( H_s \).

During the SHEBA summer, T. C. Grenfell (2003, personal communication) made sporadic measurements of the surface temperatures of leads and melt ponds in the vicinity of the SHEBA camp. From these data, from the values of \( C_l \), \( C_p \), and \( c_p \) that we used to make Figures 2 and 3, and from our own measurements of \( \Theta_{s,i} \) near the ASFG tower, we created a rudimentary time series of \( \Theta_{s,Ave} \) for summer. We say ‘rudimentary’ here because we had only occasional values of \( \Theta_{s,L}, \Theta_{s,P}, C_l \), and \( c_p \) (once a week, on average). We interpolated those to be compatible with our hourly measurements of \( \Theta_{s,i} \).

Figure 4 explains this null result. It shows the difference between \( \Theta_{s,Ave} \) and \( \Theta_{s,i} \) for summer. This difference is biased slightly positive: Its average from Figure 4, 0.05°C, is statistically different from zero but not practically different from zero. And rarely is the absolute value of this difference larger than 0.5°C. Remember (4.1d): We do not have much confidence in estimates of \( C_{Hr} \) when the surface–air temperature difference has an absolute value of 0.5°C or less. Similarly, we cannot expect much signal-to-noise ratio in estimates of \( C_{Hr} \) (and \( z_T \)) when we apply the mosaic method but the areally averaged surface temperature \( \Theta_{s,Ave} \) is within 0.5°C of the temperature of the main surface component – the sea ice (\( \Theta_{s,i} \)).

The long-wave radiation budget may be the physical explanation for this seeming uniformity in surface temperature. During SHEBA summer, the average cloud fraction was above 80% (Intrieri et al., 2002). As a result, the net flux of long-wave radiation was, on average, slightly upward but within 20 W m\(^{-2}\) of zero (Intrieri et al., 2002). That is, the clouds and the sea ice were near radiative equilibrium – a condition that would tend to homogenise surface temperatures.

In conclusion, although the mosaic method is formally more accurate way to evaluate heat fluxes over heterogeneous surfaces, summer sea ice does not seem to be thermally heterogeneous enough to make the method practically important. Henceforth, the values of \( z_T \) and \( z_0 \) that we report were obtained with \( \Theta_{s,i} \) as the surface temperature in (2.1b) and with \( Q_s \) in (2.1c) evaluated as the saturation specific humidity at \( \Theta_{s,i} \).

On the other hand, for marginal ice zones, especially in seasons other than summer, when ice and ocean will have much different surface temperatures, using the mosaic technique will likely be essential for estimating areally averaged sensible and latent heat fluxes (e.g. Andreas and Makhtas, 1985).
6.2. Finding the scalar roughness lengths

The scalar roughness length $z_0$, where $z_0$ is either $z_T$ or $z_Q$ (see (2.2)), is usually expressed as the ratio $z_T/z_0$. Many sources corroborate that $z_T/z_0$ should depend on the roughness Reynolds number, $R_u = u_z/z_0/\nu$, where $\nu$ is the kinematic viscosity of air (e.g. Garratt and Hicks, 1973; Liu et al., 1979; Brutsaert, 1982, p 89 ff.).

Andreas’s (1987) theoretical model:

$$\ln(z_T/z_0) = b_0 + b_1 \ln R_u + b_2(\ln R_u)^2. \quad (6.6)$$

Andreas (1987, 2002) tabulates the polynomial coefficients $b_0$, $b_1$, and $b_2$, which are different sets for $z_T$ and $z_Q$. Briefly, according to this model, $z_T$ is 13–40% larger than $z_T$ – primarily because the molecular diffusivity of water vapour in air is larger than the molecular diffusivity of heat in air.

For the five SHEBA summer flux sites, we used (3.5b) and (3.5c) to obtain estimates of $z_T$ and $z_Q$ for all the hourly data that passed the quality controls described in section 4. Figure 5 shows $z_T/z_0$ as a function of roughness Reynolds number for all the surviving summer data. Table II shows that this figure summarises over 1177 hours of data.

Figure 6 shows a comparable plot of $z_Q/z_0$ versus the roughness Reynolds number. Because our only measurements of the latent heat flux were at one level on the Atmospheric Surface Flux Group tower, Figure 6 shows fewer points than in Figure 5 (see Table II).

One hazard in plotting $z_T/z_0$ and $z_Q/z_0$ versus $R_u$ to test (6.6), however, is fictitious correlation. $R_u = u_z/z_0/\nu$, $z_T/z_0$, and $z_Q/z_0$ all obviously include $z_0$; and $u_z$ appears in the evaluations of $z_0$, $z_T$, and $z_Q$. Andreas (2002) demonstrated that, as a result of these shared variables, plots of $z_T/z_0$ and $z_Q/z_0$ versus $R_u$, where all quantities are measured, suffer from fictitious correlation such that the plotted data tend to follow the slope of (6.6) predicts.

If we use our bulk flux algorithm to compute $R_u$, however, the same measured $u_z$ and $z_0$ do not appear in both dependent and independent variables, and the fictitious correlation is mitigated. Andreas et al. (2006) first suggested using a bulk estimate of $R_u$ to parametrize another set of turbulence measurements (see also Andreas et al. (2010)). We denote this bulk estimate as $R_{u,B} = u_{z,B}/z_{0,B}/\nu$, where $u_{z,B}$ and $z_{0,B}$ come from our bulk flux algorithm.

Moreover, the objective of a bulk flux algorithm is to predict accurate values of $z_T/z_0$ and $z_Q/z_0$ from the algorithm’s estimate of $R_u$. Consequently, comparing measured values of $z_T/z_0$ and $z_Q/z_0$ with the bulk estimate of $R_{u,B}$, as we do in Figures 5 and 6, is the proper way to test or develop a parametrization for the scalar roughness length.

The clouds of hourly data in Figures 5 and 6 are scattered, but this spread is not surprising in light of the uncertainties in $z_0$, $z_T$, and $z_Q$ that we summarised in Table I. A lot of high-quality data are therefore required to obtain meaningful estimates of the average behaviours of $z_T/z_0$ and $z_Q/z_0$. The black circles in Figures 5 and 6 are therefore bin averages of the hourly data such that there are four evenly spaced $R_{u,B}$ bins per decade.

These bin averages are computed as geometric means rather than arithmetic means. Measured roughness lengths have distributions that are approximately log-normal (Vickers and Mahrt, 2006). The geometric mean, which is based on the average of the logarithms of the values within a bin, is a better indicator of the central tendency of the distribution than is the arithmetic mean, which is biased high by the largest values in the bin. The error bars on these bin averages are likewise computed as two standard deviations in the bin mean, where the standard deviation is also calculated from the logarithms of the hourly values in the bin.

These bin averages in Figures 5 and 6 corroborate Andreas’s (1987) model. In each figure, four of the five averages in the highest $R_{u,B}$ bins are within two standard deviations of the model. That is, these averages validate the model’s predictions for the magnitudes of $z_T/z_0$ and $z_Q/z_0$ and its prediction that both $z_T/z_0$ and $z_Q/z_0$ decrease with increasing roughness Reynolds number.
At small $R_{a,b}$, two averages in each plot are above the model curve; but these bins contain fewer hourly values as evidenced by the generally larger error bars. In fact, the left-most black circle in Figure 5 has no error bars because that bin ‘average’ consist of only one hourly value.

Although the model (6.6) has seen relatively wide use in studies of turbulent exchange over ice and snow (e.g. Launiainen and Vihma, 1990; Jordan et al., 1999; Andreas et al., 2004; Reijmer et al., 2004), it has not been fully validated over sea ice. Andreas (2002) tested (6.6) with data from the literature, but these data were collected over snow-covered ground and glaciers. Likewise, Smeets et al. (1998) and Denby and Snellen (2002) tested the $z_T$ prediction from (6.6) with data collected over Austrian and Icelandic glaciers, respectively, and found good agreement. In another glacier study using data from Greenland and Iceland, Smeets and Van den Broeke (2008) found (6.6) to represent their $z_T$ and $z_Q$ data well for $5 < R_a < 60$ but not as well for larger roughness Reynolds numbers.

Evidently, only Andreas et al. (2005a, 2010) and Brunke et al. (2006) have tested (6.6) with flux data collected over sea ice. Andreas et al. (2005a) used winter data from Ice Station Weddell, and Brunke et al. used these same SHEBA data. Andreas et al. (2010) reanalysed the SHEBA winter data; our work here is the complementary summer analysis and the first to focus exclusively on summer sea ice. We felt it was necessary to repeat some of the work in Brunke et al., for two reasons: They did not study the behaviour of $z_Q$; and we have introduced new techniques to mitigate the effects of fictitious correlation.

With Figures 5 and 6, we confirm that (6.6) is a good parametrisation for $z_T$ and $z_Q$ for $R_{a,b}$ values between 1 and 40, the largest roughness Reynolds numbers represented in our summer dataset. We therefore retain (6.6) as the parametrisation for $z_T$ and $z_Q$ in our bulk flux algorithm.

### 7. Flux comparisons

Let us now look at how the bulk flux algorithm that we have described performs in representing the measured turbulent fluxes. We again use the SHEBA summer data for these comparisons, but our approach is not based on circular logic. That is, we are not testing our algorithm with only the same data that we have used to develop it. First, our polynomial parametrisation for $C_{DN10}$, shown in (5.2) and Figure 3, relies on data collected in marginal ice zones as well as on the summer SHEBA data. Furthermore, that fit was made by eye rather than statistically. In other words, the fit was not made by formally minimising statistical errors in the data. Finally, Table II shows that slightly different data were used to obtain the $C_{DN10}$ values in Figure 3 and the $u_*$ values that we show soon in Figure 7.

Similarly, our upcoming plots that compare measured and modelled sensible and latent heat fluxes do not suffer from circular logic either. The key to predicting the fluxes is good predictions for $z_T$ and $z_Q$. Although Figure 5 and 6 confirm that, on average, the SHEBA summer data agree well with Andreas’s (1987) model predictions for $z_T/z_0$ and $z_Q/z_0$, we have not used those data in any way to tune that model. In our bulk flux algorithm, we use (6.6) exactly as it was published in 1987. Secondly, Table II summarises the number of hours of data depicted in Figures 5 and 6 and in our plots of sensible and latent heat fluxes to follow, Figures 8 and 9, respectively. We use many more hours of data in our plots that compare fluxes than in the plots that validate our predictions for $z_T/z_0$ and $z_Q/z_0$. Figures 5 and 6, because we now ignore the screening conditions (4.1) and (4.2) and use all available data.

Figure 7 compares measured and modelled values of the friction velocity for the five SHEBA summer sites. From Table II, we see that these plots represent over 11 000 hours of data.

To evaluate the performance of our flux algorithm, we computed two metrics, following Willmott (1982). Let $M_i$ be a measured flux (i.e. $u_*$, $H_s$, or $H_L$) and let $B_i$ be the corresponding estimate of that flux from our bulk flux algorithm. The mean bias error in the modelled (bulk) values is

$$\text{MBE} = \frac{1}{N} \sum_{i=1}^{N} (B_i - M_i), \quad (7.1)$$

where $N$ is the number of observations (see Table II). The root-mean-square error in the modelled values is

$$\text{RMSE} = \left\{ \frac{1}{N} \sum_{i=1}^{N} (B_i - M_i)^2 \right\}^{1/2}, \quad (7.2)$$

Table III list these metrics for the comparisons shown in Figure 7.

In each panel in Figure 7, the best fitting line through the data is very close to the 1:1 line. The metrics in Table III reiterate how well our bulk flux algorithm does in predicting...
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$u_*$, measured on the Atmospheric Surface Flux Group tower and at the Flux-PAM sites named Atlanta, Baltimore, Florida, and Maui during summer and modelled with our bulk flux algorithm using data from those sites. In each panel, the solid line is 1:1. The dashed line is the best fit through the data, taken as the bisector of $y$-versus-$x$ and $x$-versus-$y$ least-squares fits (e.g. Andreas, 2002). Table II lists the hours of data in each plot; Table III summarises the model metrics.

The absolute value of the bias error in all five examples is well less than 0.01 m s$^{-1}$, and the sign is both positive and negative. The root-mean-square error, which is a measure of the scatter in the data, is typically 0.03 m s$^{-1}$. Under the reasonable assumption that approximately half of the mean-square error is attributable to measurement uncertainty and half to model uncertainty, we can assess the absolute accuracy of our bulk flux algorithm for estimating $u_*$ as RMSE/$\sqrt{2}$, which is 0.02–0.03 m s$^{-1}$.

Figure 8 compares measured and modelled values of the sensible heat flux, $H_s$, for all five of the SHEBA summer sites. These plots likewise represent over 11 000 hours of data (see Table II). As usual, obtaining any modelled flux (in this case, $H_s$) requires iterating on the full set of equations.
that constitute our bulk flux algorithm: (2.1)–(2.7), (5.2) and (6.6). In these and in our later heat flux plots, Figures 9 and 11, a positive flux is upward – from surface to air (see (2.1b) and (2.1c)).

The results in Figure 8 are somewhat mixed. The ASFG tower and Maui panels have the smallest mean bias errors and root-mean-square errors among the five panels (Table III). But while the Maui results trend fairly well toward the 1:1 line, the ASFG tower points deviate from 1:1 because of some measured fluxes with large absolute values.

In general, though, the range of measured and modelled fluxes – typically between $-20$ and $+20$ W m$^{-2}$ – emphasises the difficulties in both measuring and modelling sensible heat flux over summer sea ice. The vertical temperature gradients are small, and the magnitudes of the fluxes are small; errors in either quantity thus severely degrade comparisons between measured and modelled fluxes. Nevertheless, atmospheric models must still estimate the sensible heat flux over summer sea ice. The panels in Figure 8 demonstrate how accurate these model estimates might be.

Table III lists the fitting metrics for all the sites shown in Figure 8. For the five sites, the mean bias error ranges from $-1.4$ to $-5.0$ W m$^{-2}$. That is, the bias error is always negative; at least for the SHEBA dataset, our bulk flux algorithm is biased low in its predictions of sensible heat flux over summer sea ice.
The root-mean-square errors (RMSE) for the five panels in Figure 8 range from 5.5 to 11.3 W m\(^{-2}\). Again, under the assumption that half of the mean-square error is attributable to the measurements and half to the algorithm, we use RMSE/\(\sqrt{2}\), which is typically 6 W m\(^{-2}\), as an estimate of the general precision in our algorithm’s prediction for sensible heat flux in the summer.

Figure 9 shows the only comparison between measured and modelled latent heat flux possible with our SHEBA dataset – values based on data from the Atmospheric Surface Flux Group tower. Again, the range of fluxes in this plot – typically from 0 to 10 W m\(^{-2}\) – implies how difficult measuring and modelling latent heat flux is over sea ice.

The best fit through the data in Figure 9 deviates a bit from the 1:1 line – primarily because of some seemingly unrealistically large modelled fluxes that do not correspond with comparable measured values. The fitting metrics in Table III, however, suggest that our algorithm does better in estimating the latent heat flux than the sensible heat flux. The mean bias error in latent heat flux is only 0.05 W m\(^{-2}\).

The root-mean-square error in the latent heat flux plot, 5.0 W m\(^{-2}\), is also smaller than any of the comparable errors in the sensible heat flux plots for the five SHEBA summer sites.

As above, we assign half of the mean-square error to uncertainty in our flux algorithm. Thus, an estimate of the absolute accuracy of our bulk flux algorithm’s ability to estimate latent heat flux is RMSE/\(\sqrt{2}\), which is 3.5 W m\(^{-2}\).

### 8. An alternative algorithm

As a demonstration of the improved predictions our new algorithm offers, we compare it with the Community Ice Code (CICE; Hunke and Lipscomb, 2008). The CICE module is an integral part of the Community Climate System Model (Briegleb et al., 2004) and, as such, is a crucial tool for climate studies (e.g., Kiehl and Gent, 2004; Collins et al., 2006; Holland et al., 2006). Although CICE is much more than a bulk turbulent flux algorithm, surface flux calculations are essential in it; and it parametrizes these fluxes using the same formalism that our algorithm does. Because CICE differs in detail from our algorithm, however, it is a worthy alternative for testing the efficacy of the presumed improvements in our algorithm.

CICE assumes \(z_0 = z_T = z_Q = 5.0 \times 10^{-4}\) m. Although it uses the Paulson (1970) functions for \(\psi_m\) and \(\psi_h\) in unstable stratification, as does our algorithm, it uses the functions from Holtslag and De Bruin (1988) in stable stratification. Remember, our new algorithm uses the functions from Grachev et al. (2007a). Finally, CICE does not have a gustiness parametrization, like our (2.4), in unstable stratification but does parametrize windless transfer in stable stratification – for the sensible heat flux only – following Jordan et al. (1999) (cf. our (2.6)). In effect, for stable stratification, CICE adds to all computed sensible heat fluxes 1W m\(^{-2}\) K\(^{-1}\) (\(\Theta_s - \Theta_r\)). Consequently, all negative fluxes become more negative.

Figures 10 and 11 compare \(u_s\) and \(H_s\) values measured at the Flux-PAM sites Atlanta and Baltimore with values modelled with the surface flux algorithm in CICE. Compare these plots with similar plots in Figures 7 and 8 for which the modelled values come from our new algorithm. We chose Atlanta and Baltimore for these comparisons because they have long records of summer data but, unlike the

<table>
<thead>
<tr>
<th>Site</th>
<th>(u_s) (m s(^{-1}))</th>
<th>RMSE</th>
<th>MBE</th>
<th>RMSE</th>
<th>MBE</th>
<th>RMSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>SHEBA Algorithm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ASFG Tower</td>
<td>0.0062</td>
<td>0.0300</td>
<td>-1.4</td>
<td>5.5</td>
<td>-0.05</td>
<td>5.0</td>
</tr>
<tr>
<td>Atlanta</td>
<td>-0.0008</td>
<td>0.0339</td>
<td>-5.0</td>
<td>8.2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baltimore</td>
<td>0.0004</td>
<td>0.0233</td>
<td>-4.8</td>
<td>8.7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Florida</td>
<td>-0.0004</td>
<td>0.0453</td>
<td>-4.5</td>
<td>11.3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Maui</td>
<td>-0.0038</td>
<td>0.0285</td>
<td>-1.6</td>
<td>5.7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>CICE Algorithm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Atlanta</td>
<td>-0.0059</td>
<td>0.0318</td>
<td>-6.6</td>
<td>10.6</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Baltimore</td>
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<td>0.0236</td>
<td>-6.6</td>
<td>12.0</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The mean bias error (MBE) and the root-mean-square error (RMSE) are computed according to (7.1) and (7.2). Table II gives the number of observations used in each set of calculations.

AsFG tower, have only one measurement height. They thus provide a data source similar to what a regional or climate model would be replicating.

In Figure 10, *u*∗ values modelled with the CICE algorithm are biased low for both PAM stations. On the other hand, the Atlanta and Baltimore panels in Figure 7 show virtually no model bias in *u*∗. Table III confirms these visual results; the mean bias errors in the CICE prediction of *u*∗ are significantly more negative than for our new SHEBA algorithm. The scatter in the two panels in Figure 10 – as quantified by the root-mean-square error in Table III – is not very different from the scatter in Figure 7.

We attribute the negative mean bias errors in Figure 10 to the constant value of *z*0, 5.0 × 10⁻⁴ m, in the CICE algorithm. This *z*0 value corresponds to a *C*DN₁₀ value of 1.63 × 10⁻³. Figure 3 shows that, although summer *C*DN₁₀ values can occasionally be smaller than 1.63 × 10⁻³, they are more often considerably larger. The CICE algorithm simply always underestimates *C*DN₁₀ during the height of summer.

Figure 11 presents similar comparisons of *H*s measured at Atlanta and Baltimore and modelled with the CICE algorithm. The agreement between measured and modelled sensible heat flux is noticeably poorer than for the comparable panels in Figure 8, where the modelled *H*s is based on our new algorithm. The values for mean bias error (MBE) and root-mean-square error in Table III reiterate the poorer performance of the CICE algorithm; the MBEs are significantly more negative for both PAM sites in Figure 11, and the RMSE values are both at least 25% larger than for fluxes modelled with our new algorithm.

Furthermore, both panels in Figure 11 show that the CICE algorithm overestimates the magnitude of *H*s (compared to the Atlanta and Baltimore panels in Figure 8) when *H*s is negative. As a result, both fitting lines in Figure 11 are rotated significantly counter-clockwise from the 1:1 line. With (2.6) and the new stratification corrections from Grachev et al. (2007a), we have focused our developmental efforts on improving flux parametrizations in stable stratification. When compared with Figure 8, the results in Figure 11 confirm that these were beneficial improvements.

9. Conclusions

Using the longest set of turbulent flux data ever collected over sea ice – data from SHEBA – we have developed and tested parametrizations for the turbulent fluxes of momentum and...
sensible and latent heat over summer sea ice. Ours is an 
aerodynamic definition of summer as the period when the 
sea surface is a mosaic of sea ice and water in both leads 
and melt ponds. In the SHEBA dataset at the height of 
summer, water covered about 40% of the surface.

The leads and melt ponds of summer produce vertical ice 
faces that the wind can push against; momentum transfer 
to the surface is thereby enhanced by form drag. And this 
enhanced momentum exchange seems to homogenise the 
atmospheric surface layer despite the visual heterogeneity of 
the surface. As an example, Figure 2 shows that, among the 
several SHEBA sites, the neutral-stability drag coefficient at 
a reference height of 10 m, \( C_{DN10} \), behaves more coherently 
in summer than in winter.

Because marginal ice zones are other ocean regions 
where the surface consists of ice and open water, we 
have merged our SHEBA measurements of \( C_{DN10} \) with 
comparable measurements made in marginal ice zones. 
These various datasets yield a consistent picture of how 
\( C_{DN10} \) varies with ice concentration. The drag formulation 
in our bulk flux algorithm, (5.2), therefore simply predicts 
\( C_{DN10} \) over summer sea ice and in any marginal ice zone 
from a second-order polynomial in ice concentration, \( C_0 \). 
Because \( C_0 = 1 - C_w \), where \( C_w \) is the fractional surface 
area of water, to employ our algorithm, sea-ice models must 
include a parametrization for melt pond coverage because 
the area of these is included in \( C_w \).

Other essential components of our bulk turbulent flux 
algorithm are predictions for the roughness lengths for 
temperature (\( z_T \)) and humidity (\( z_Q \)). The sensible heat flux 
data from five SHEBA sites support Andreas’s (1987) model 
for predicting \( z_T/z_0 \). Results from the lone long-term 
latent heat flux measurement site during SHEBA – at one 
level on the Atmospheric Surface Flux Group tower – also 
support Andreas’s predictions for \( z_Q/z_0 \).

Because \( z_T/z_0 \) and \( z_Q/z_0 \) are theoretically related to the 
roughness Reynolds number, \( R_e = u_a z_0/\nu \), plots to study this 
relationship must be made carefully to minimise the 
fictitious correlation that results because of the shared 
variables \( z_0 \) and \( u_a \). When \( z_T/z_0 \), \( z_Q/z_0 \) and \( R_e \) are all 
calculated from measured values, the fictitious correlation 
can be severe and, thus, misleading. We have here introduced 
a method to mitigate the fictitious correlation by forming 
\( z_T/z_{0,20} \) and \( z_{Q,20}/z_{0,20} \) from data but computing \( R_e \) 
from our bulk flux algorithm. In fact, this is the way that parametrizations 
for roughness lengths should be developed and tested: The 
goal of a bulk flux algorithm is to predict accurate values of 
\( z_T \) and \( z_Q \) from the algorithm’s estimate of \( R_e \).

Other components of our bulk flux algorithm are equations (2.1)–(2.7) and expressions for the stability 
corrections in (2.2), \( \psi_W \) and \( \psi_L \). From the SHEBA data, Grachev et al. (2007a) developed new expressions for \( \psi_W \) and \( \psi_L \) in stable stratification that we incorporated into our 
algorithm.

Based on the error analyses associated with our flux 
comparisons in Figures 7–9, we believe that our flux 
algorithm can estimate \( u_a \) over summer sea ice to 
0.02–0.03 m s\(^{-1}\) and with negligible bias for \( u_a \) values 
between 0 and 0.60 m s\(^{-1}\). For sensible heat flux, our 
algorithm has an absolute error of about 6 W m\(^{-2}\) (i.e. 
typically RMSE/\( \sqrt{2} \) from Table III) and seems to be biased 
low by 2–4 W m\(^{-2}\). Finally, for predicting the latent heat 
flux, our algorithm has an absolute error of only 3.5 W m\(^{-2}\) 
and a bias error of only 0.05 W m\(^{-2}\). In closing, we have developed FORTRAN code for the bulk 
flux algorithm that we have described here. It complements 
the related algorithm that Andreas et al. (2010) reported for 
winter sea ice. We are willing to share the code for both 
algorithms with anyone interested in trying it out.

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