

## Holographic optics based two-channel interferometer

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The paper describes a simple and cost effective method for making a two-channel interferometer based on holographic optics, which is suitable for performing optical test studies on two different phase objects simultaneously and independently. The optical arrangement in the proposed method involves a simple alignment procedure and inexpensive recording material is used in the formation of holographic optical elements. Recording schemes for the formation of holographic optical elements and the related techniques for the realization of the proposed interferometer along with the effect of misalignment of holographic optical elements and typical experimental results are presented.

**Keywords:** Optical interferometry, Two-channel interferometer, Holography, Optical testing instruments, Phase visualization

**IPC Code:** G03H

### 1 Introduction

Different types of optical interferometers are in use for the study of phase objects<sup>1,2</sup> as the interferograms provide accurate representation of the phase objects. The conventional optical interferometers generally use expensive and precise custom-made bulky optics and also involve rather tedious and time-consuming alignment procedures, which make them impractical in some applications. The use of holographic optical elements instead of the conventional optics can drastically reduce the bulkiness and high cost factors. Because of the several attractive features offered by holographic optical elements, such as light weight; compactness; ease of fabrication; containing multiple optical functions in a single element, their use provide the advantage in the construction of compact optical systems and their high functionality compared with conventional bulky optics. In recent years, there has been an increasing interest of using holographic optics based interferometers<sup>3-6</sup> for the study of phase objects in real time. These interferometers are generally suitable for performing optical test studies on a single phase object. A multi-channel optical interferometer<sup>7,8</sup> for the study of many phase objects simultaneously has been reported recently. This Young type interferometer, based on waveguide structures, is however suitable only for testing microstructure phase

objects and not for the macro-structure objects. In this paper, we present a simple and cost effective method for making a compact and versatile two-channel interferometer based on holographic optics, which is suitable for performing optical test studies of two different macro size phase (transparent) objects simultaneously and independently. The proposed interferometer set-up has utility for comparative testing studies between two different phase objects in real time and may be useful in the studies of refractive index, wavefront measurements, thermal profiling, combustion, plasma diagnostics, atmospheric turbulence and flow visualization etc. The effect of misalignment of holographic optical elements on the interferograms has also been analyzed.

### 2 Principle of the Method

The method reported in this paper for making a two-channel interferometer is based on the formation of multiple holographic optical elements on two different recording plates in two recording steps. The first recording step involves the formation of two spatially separated holographic optical elements ( $H_{11}$  and  $H_{12}$ ) on same recording plate  $H_1$ . The  $H_{11}$  and  $H_{12}$  are formed by using two different sets of collimated beams,  $O_1$  with  $O_2$  and  $O_3$  with  $O_4$  respectively, in conjunction with a common collimated beam  $R$  (Fig. 1). The plate  $H_1$ , containing these two permanently recorded HOEs, upon illumination with a single collimated beam  $R$  provides four in-built

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collimating beams  $O'_1, O'_2, O'_3$  and  $O'_4$  for subsequent recording. In the second recording step, the in-built collimated beam pairs  $O'_1$  with  $O'_3$  and  $O'_2$  with  $O'_4$  (generated from  $H_1$ ) are used for the formation of two spatially separated holographic optical elements  $H_{21}$  and  $H_{22}$  on the second recording plate  $H_2$  (Fig. 2). After processing,  $H_2$  is repositioned at the same location at which it was recorded. These holographic plates  $H_1$  and  $H_2$  when placed in this configuration and illuminated with a single collimated beam  $R$  serves as a versatile two-channel interferometer (Fig. 3). Here  $H_1$  upon illumination with  $R$  provides four illuminating beams,  $O'_1$  and  $O'_2$  from  $H_{11}$  and  $O'_3$  and  $O'_4$  from  $H_{12}$  for  $H_2$ . In this case, the so-generated beams  $O'_1$  and  $O'_3$  illuminate  $H_{21}$  and similarly  $O'_2$  and  $O'_4$  illuminate  $H_{22}$ . The illuminating beams  $O'_1$  and  $O'_3$

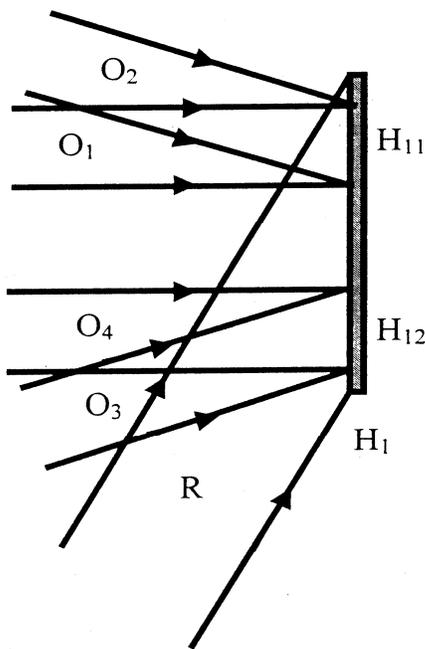


Fig. 1 — Schematic of forming holographic optical elements on  $H_1$

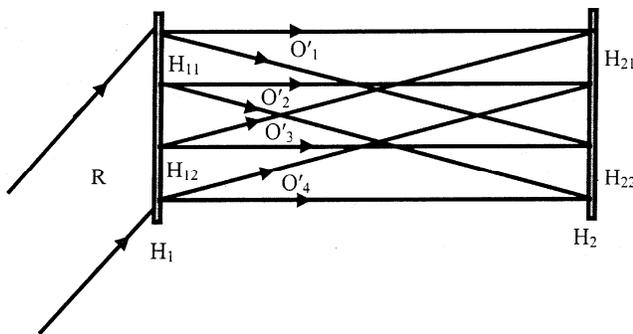


Fig. 2 — Schematic of forming holographic optical elements on  $H_2$

on  $H_{21}$  further provide undiffracted-order beam  $O'_1$  and diffracted-order beam  $O''_1$  (due to  $O'_3$ ) overlapping each other and also undiffracted-order beam  $O'_3$  and diffracted-order beam  $O''_3$  (due to beam  $O'_1$ ) overlapping each other at two separate locations. Similarly at  $H_{22}$ , the illuminating beams  $O'_2$  and  $O'_4$  further provide undiffracted-order beam  $O'_2$  and diffracted-order beam  $O''_2$  (due to beam  $O'_4$ ) which are overlapping each other and also undiffracted-order beam  $O'_4$  and diffracted-order beam  $O''_4$  (due to beam  $O'_2$ ) overlapping each other at two separate locations. This results in the generation of four different interferograms at separate locations in the observation plane  $OP$ , which can be viewed on a screen or with a video camera.

Here  $O_1, O_2, O_3, O_4, O'_1, O'_2, O'_3, O'_4, O''_1, O''_2, O''_3, O''_4$  and  $R$  are the complex amplitude distribution of the respective wavefronts. For simplicity, it is assumed that the holographic plates are developed in the linear region of the transmittance versus exposure curve. The amplitude transmittance of the processed  $H_1$  is given<sup>9</sup> by:

$$t_1 \sim k [ |O_1 + O_2 + R|^2 + |O_3 + O_4 + R|^2 ] \quad \dots(1)$$

where  $k$  is a parameter dependent on the recording material used, exposure and the processing conditions. For forming two spatially separated  $H_{21}$  and  $H_{22}$  on another recording plate  $H_2$ , the  $H_1$  is illuminated only with a single collimated beam  $R$  (as was used in the first recording step). The complex amplitude of the transmitted field from  $H_1$  is:

$$U_1 = R t_1 \approx k [ R \{ |O_1|^2 + |O_2|^2 + |R|^2 + O_1^* O_2 + O_1^* R + O_2^* O_1 + R O_2^* + O_1 R^* + O_2 R^* + |O_3|^2 + |O_4|^2 + |R|^2 + O_4 O_3^* + R O_3^* + O_3 O_4^* + R O_4^* + O_3 R^* + O_4 R^* \} ] \quad \dots(2)$$

It may be noted that the  $H_{11}$  and  $H_{12}$  are spatially separated and are recorded on a holographic recording plate  $H_1$  in the form of holographic gratings. In the right hand side of Eq. 2 the first three terms [i.e.,  $kR (|O_1|^2 + |O_2|^2 + |R|^2)$ ] represent the undiffracted beam and the 4<sup>th</sup> to 9<sup>th</sup> terms represent the diffracted beams from  $H_{11}$ . In a similar manner, 10<sup>th</sup> to 12<sup>th</sup> terms (i.e.  $kR(|O_3|^2 + |O_4|^2 + |R|^2)$ ) represent the undiffracted beam and 13<sup>th</sup> to 18<sup>th</sup> terms represent the diffracted beams from  $H_{12}$ . All these beams are spatially separated from each other. We can consider  $|R|^2$  to be constant across the plate  $H_1$ , as a plane beam  $R$  is used

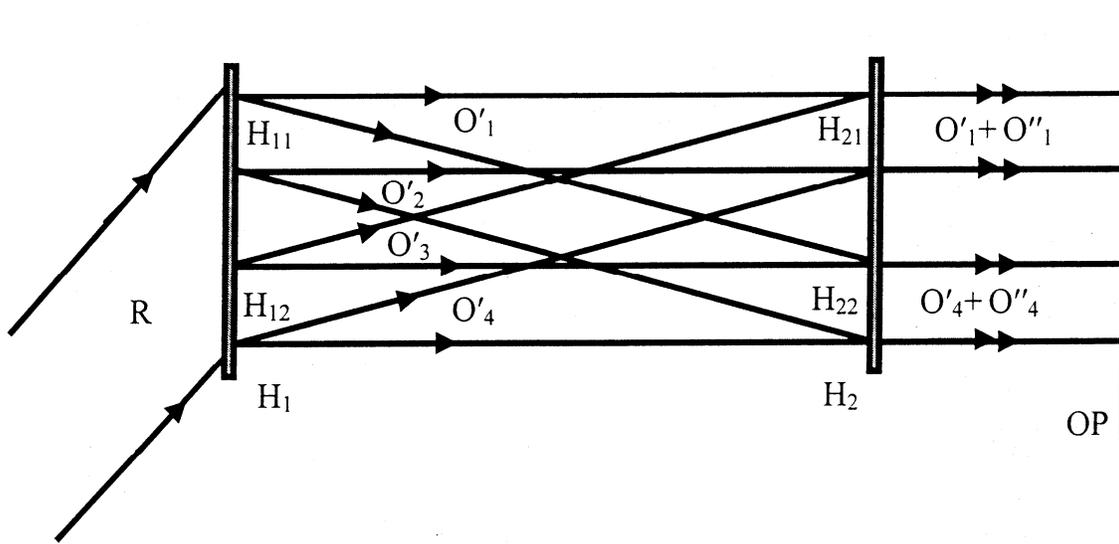


Fig. 3 — Schematic of a two-channel interferometer based on holographic optical elements

for the illumination of  $H_1$ . Thus, only the 8<sup>th</sup>, 9<sup>th</sup>, 17<sup>th</sup> and 18<sup>th</sup> terms on the right hand side of Eq. (2) are of interest to us as they represent the diffracted-order beams  $O'_1$  and  $O'_2$  generated from  $H_{11}$ ;  $O'_3$  and  $O'_4$  generated from  $H_{12}$ , respectively. Here  $O'_1, O'_2, O'_3$  and  $O'_4$  are identical to the original respective beams  $O_1, O_2, O_3$  and  $O_4$  as they possess all the properties of these and can be considered to be as replica of the original beams and can be represented as:

$$kO_1|R|^2 + kO_2|R|^2 + kO_3|R|^2 + kO_4|R|^2 \approx O'_1 + O'_2 + O'_3 + O'_4 \quad \dots(3)$$

The so-generated beams  $O'_1, O'_2, O'_3$  and  $O'_4$  are further used for forming two spatially separated HOEs on another recording plate  $H_2$  in the second recording step (Fig. 2). After processing,  $H_2$  is repositioned at the same location at which it was recorded. By using a similar analysis as followed for  $H_1$ , the amplitude transmittance of the processed  $H_2$  is:

$$t_2 \approx k [ |O'_1 + O'_3|^2 + |O'_2 + O'_4|^2 ] \quad \dots(4)$$

In this configuration, when  $H_1$  is illuminated with a collimated beam  $R$ , it provides four illuminating beams  $O'_1, O'_2, O'_3$  and  $O'_4$  for  $H_2$  such that  $O'_1$  and  $O'_3$  illuminate  $H_{21}$  and  $O'_2$  and  $O'_4$  illuminate  $H_{22}$  respectively. The complex amplitude of the transmitted field from  $H_2$  is given by:

$$U_2 = (O'_1 + O'_3) [ k ( |O'_1 + O'_3|^2 ) ] + (O'_2 + O'_4) [ k ( |O'_2 + O'_4|^2 ) ] \approx k [ O'_1 [ |O'_1|^2 + |O'_3|^2 ] +$$

$$O'_3 [ |O'_1|^2 + O'_1{}^2 O'_3{}^* + O'_3 [ |O'_1|^2 + |O'_3|^2 ] + O'_3{}^2 O'_1{}^* + O'_1 |O'_3|^2 + O'_2 [ |O'_2|^2 + |O'_4|^2 ] + O'_4 |O'_2|^2 + O'_2{}^2 O'_4{}^* + O'_4 [ |O'_2|^2 + |O'_4|^2 ] + O'_4{}^2 O'_2{}^* + O'_2 |O'_4|^2 ] \quad \dots(5)$$

In right hand side of Eq. (5), the first term represents the undiffracted-order beam  $O'_1$  and the sixth term represents the diffracted-order beam  $O''_1 = O'_1 k |O'_3|^2 \approx O'_1$  (due to beam  $O'_3$ ) and superimposes the above undiffracted-order beam  $O'_1$ . The second term represents the diffracted-order beam  $O''_3 = O'_3 k |O'_1|^2 \approx O'_3$  (due to beam  $O'_1$ ) and the fourth term represents the undiffracted-order beam  $O'_3$  and superimposes with the above diffracted-order beam  $O''_3$ . These spatially separated superimposed beam pairs generated from  $H_{21}$  thus provide two different interferograms at two separate locations in the observation plane  $OP$ . Similarly, the 7<sup>th</sup> term represents the undiffracted-order beam  $O'_2$  and the 12<sup>th</sup> term represents the diffracted-order beam  $O''_2 = O'_2 k |O'_4|^2 \approx O'_2$  (due to beam  $O'_4$ ) and superimposes the above undiffracted-order beam  $O'_2$ . The 8<sup>th</sup> term represents the diffracted-order beam  $O''_4 = O'_4 k |O'_2|^2 \approx O'_4$  (due to beam  $O'_2$ ) and the tenth term represents the undiffracted beam  $O'_4$  and superimposes the above diffracted beam  $O''_4$ . These spatially separated superimposed beam pairs generated from  $H_{22}$ , thus, also provide two different interferograms at separate locations in the observation plane  $OP$ . These four

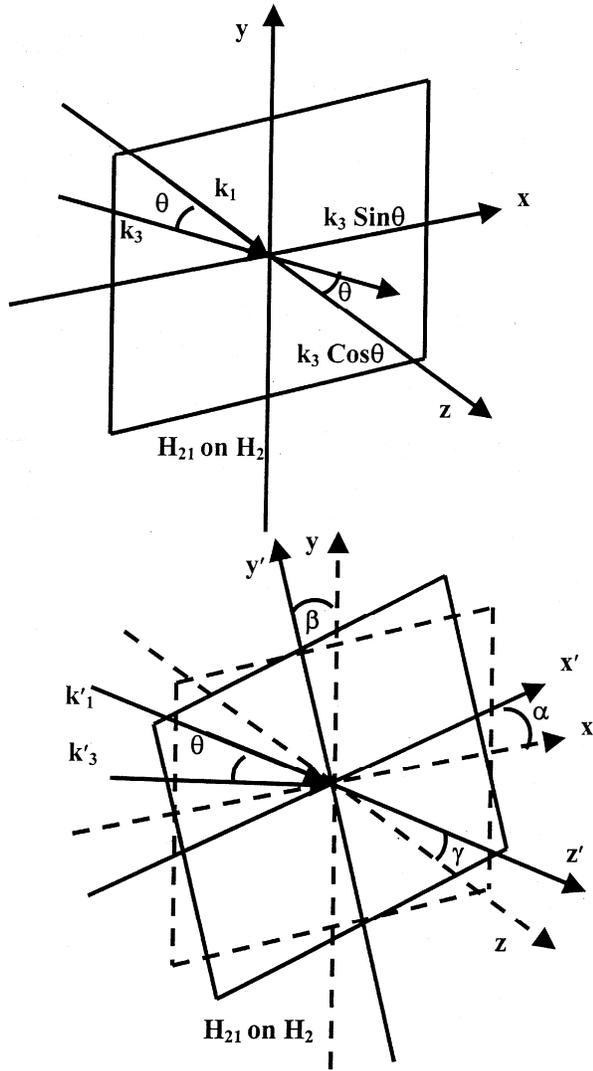


Fig. 4 — Schematic view of (a) initial orientation of H<sub>21</sub> on plate H<sub>2</sub> and the related recording beams (b) reorientation of H<sub>21</sub> on plate H<sub>2</sub> to eliminate fringes due to misalignment

interferograms generated in the observation plane OP are spatially separated from each other. By applying a simple alignment procedure in repositioning of H<sub>2</sub> results in infinite-fringe (i.e. zero fringe) interferograms (Fig. 4) in the observation plane. In this configuration, the portion of beams O<sub>1</sub> and O<sub>4</sub> generated between H<sub>1</sub> and H<sub>2</sub> can be used as two separate test arms for performing optical test studies on two different phase objects simultaneously. Typically, if a phase object S = exp [iφ<sub>1</sub>] is introduced in the first test arm O<sub>1</sub> and a second phase object P = exp [iφ<sub>2</sub>] is introduced in the second test arm O<sub>4</sub>, then the complex amplitude of the transmitted field from H<sub>2</sub> is given by:

$$U_3 = (O'_1 S + O'_3) k [|O'_1 + O'_3|^2] + (O'_2 + O'_4 P) k [|O'_2 + O'_4|^2] \approx k [O'_1 S [|O'_1|^2 + |O'_3|^2] + O'_3 S |O'_1|^2 + O'_1^2 S O_3^* + O'_3 [|O'_1|^2 + |O'_3|^2] + O'_3^2 O_1^* + O'_1 |O'_3|^2 + O'_2 [|O'_2|^2 + |O'_4|^2] + O'_4 |O'_2|^2 + O'_4^* O_2^2 + O'_4 P [|O'_2|^2 + |O'_4|^2] + P O_4^2 O_2^* + O_2 P |O_4|^2] \dots(6)$$

In the right hand side of Eq. (6), the 1<sup>st</sup> term represents the undiffracted-order beam O<sub>1</sub> (containing information about phase object S) and the 6<sup>th</sup> term represents the diffracted beam O<sub>1</sub>' (generated due to O<sub>3</sub> illuminating beam). Similarly, the 10<sup>th</sup> term represents the undiffracted beam O<sub>4</sub> (containing information about phase object P) and the 8<sup>th</sup> term represents the diffracted beam O<sub>4</sub>' (generated due to O<sub>2</sub> illuminating beam). Here, the beams O<sub>1</sub> and O<sub>1</sub>' generated from H<sub>21</sub> superimpose each other and similarly the beams O<sub>4</sub> and O<sub>4</sub>' generated from H<sub>22</sub> also superimpose each other and generate two different interferograms at separate locations in the observation plane. It may be noted that by following a similar procedure, two more spatially separated interferograms [due to O<sub>3</sub> and O<sub>3</sub>' overlapping beams generated from H<sub>21</sub> and also due to O<sub>2</sub> and O<sub>2</sub>' overlapping beams generated from H<sub>22</sub>] will be formed in the observation plane. For the sake of simplicity, we are considering only the upper two interferograms so as to explain the working phenomena. Thus, due to above, the complex amplitude distribution for the H<sub>2</sub> is:

$$U_4 \approx k [O'_1 S [|O'_1|^2 + |O'_3|^2] + O'_1 |O'_3|^2] + k [O'_4 P [|O'_2|^2 + |O'_4|^2] + O'_4 |O'_2|^2] \dots(7)$$

The intensity distribution, due to these interference patterns, in the observation plane is:

$$I_r = I_1 + I_2 \approx \{k^2 |O'_1 S|^2 [|O'_1|^2 + |O'_3|^2]^2 + k^2 |O'_1|^2 |O'_3|^4 + k^2 |O'_1|^2 |O'_3|^2 [|O'_1|^2 + |O'_3|^2] (S + S^*)\} + \{k^2 |O'_4 P|^2 [|O'_2|^2 + |O'_4|^2]^2 + k^2 |O'_4|^2 |O'_2|^4 + k^2 |O'_4|^2 |O'_2|^2 [|O'_4|^2 + |O'_2|^2] (P + P^*)\}$$

$$I_r \approx A + B \cos \phi_1 + C + D \cos \phi_2 \dots(8)$$

where A, B, C and D are constants. It is thus seen that the intensity distribution of the interference patterns,

recorded in the observation plane, depends only on the phase variation introduced by the phase objects S and P into the respective test beams  $O'_1$  and  $O'_4$  between  $H_1$  and  $H_2$ . In order to realize the proposed interferometric set-up, the processed HOEs are required to be repositioned at the same location at which these are formed. A slight misalignment in either  $H_1$  or  $H_2$  results in finite fringe interferograms in the observation plane. The effect of misalignment<sup>10</sup> in either of the HOEs, which results in finite fringe interferograms in the observation plane, is analyzed.

### 3 Alignment Sensitivity

For simplicity, the effects of misalignment in the plates  $H_1$  and  $H_2$  on one of the holographic optical elements say  $H_{21}$  on  $H_2$  are considered. In this case, the interferogram gets formed due to superposition of undiffracted-order beam  $O'_1$  and diffracted-order beam  $O''_1 \approx O'_1$  (generated due to beam  $O'_3$ ) can be represented as:

$$U \sim A^2 \psi O'_1$$

where, A is the amplitude of the beams  $O'_1$  and  $O'_3$ ;  $\psi$  is the distorting phase term<sup>11</sup> and is given by:

$$\psi \sim \exp i(\mathbf{k}'_1 \mathbf{r}' - \mathbf{k}_1 \mathbf{r}) + \exp i(\mathbf{k}'_3 \mathbf{r}' - \mathbf{k}_3 \mathbf{r}) \quad \dots(9)$$

where,  $\mathbf{k}_1$ ,  $\mathbf{k}_3$  and  $\mathbf{r}$  represent the wavevectors of the illuminating beams and the position of the  $H_{21}$  in the recording condition, and  $\mathbf{k}'_1$ ,  $\mathbf{k}'_3$  and  $\mathbf{r}'$  are the corresponding values for the reconstruction condition. The effect of misalignment in either  $H_1$  or  $H_2$  is separately analyzed.

#### (1) Misalignment in $H_2$

In this case (when  $H_2$  is not properly repositioned after processing), the reconstructing beams are identical with the recording beams, i.e.,

$\mathbf{k}'_1 = \mathbf{k}_1$  and  $\mathbf{k}'_3 = \mathbf{k}_3$ , and the components [Fig. 4(a)] of the two vectors are:

$$\mathbf{k}_1 \sim (0, 0, k_1)$$

$$\mathbf{k}_3 \sim (k_3 \sin\theta, 0, k_3 \cos\theta)$$

Here the  $H_2$  is assumed to be positioned perpendicular to the z-axis. This is not a general case, however, it is sufficiently close to the practical case. A more general treatment is possible but interpretation of results might be obscured by the complicated expressions. Since the illuminating source is coherent, thus  $k_1 = k_3 = k$  and the

misalignment vector associated with the  $H_2$  plate position is:  $\mathbf{r}' - \mathbf{r} = \Delta\mathbf{r}$

#### (a) Lateral position misalignment

In case, the plate co-ordinates are misaligned by a parallel translation i.e.  $\Delta\mathbf{r} = (\Delta x, \Delta y, \Delta z)$  then  $\psi$  can be written as

$$\psi = \exp i k \Delta z + \exp i(k \sin\theta \Delta x + \cos\theta \Delta z)$$

Thus

$$|\psi|^2 = 4 \cos^2 k [\{\sin\theta \Delta x + (\cos\theta - 1) \Delta z\}/2]$$

Here repositioning is critical in the x and z directions as  $k_1$  and  $k_3$  differ in their x and z components. No fringe will occur (in the interferogram) in the observation plane when  $\Delta x = (2n + 1) \pi/k \sin\theta$ , and  $\Delta z = (2n + 1)\pi/k (\cos\theta - 1)$ ; where n is an integer. To minimize the sensitivity with respect to x and z positioning, the components in these directions should be as small as possible.

#### (b) Rotation around x-axis

In case  $H_2$  is rotated by an angle  $\Delta\alpha$  along the x-axis then displacement vector

$$\Delta\mathbf{r} = (0, -z\Delta\alpha, + y\Delta\alpha)$$

Eq. (9) can now be written as:

$$\psi = \exp i k y \Delta\alpha (\cos\theta - 1) + 1$$

$$\text{Thus, } |\psi|^2 = 4 \cos^2 [k y \Delta\alpha (\cos\theta - 1)/2]$$

The sensitivity of  $\psi$  with respect to the rotation around the x-axis is thus of the first order of the rotation angle  $\Delta\alpha$ . Equally spaced fringes will appear parallel to the x-axis with spacing of  $2\pi/k\Delta\alpha(\cos\theta - 1)$ .

#### (c) Rotation around y-axis

When  $H_2$  is rotated by an angle  $\Delta\beta$  along the y-axis then displacement vector

$$\Delta\mathbf{r} = (z\Delta\beta, 0, -x\Delta\beta)$$

Eq. (9) can thus be written as:

$$\psi = \exp (ik \sin\theta z\Delta\beta) \exp [-i k x \Delta\beta (\cos\theta - 1)] + 1$$

Since the z-axis is perpendicular to the  $H_2$  plane, thus only the projection of fringes onto the  $H_2$  plane are observed.

Thus,

$$|\psi|^2 = 4 \cos^2 \{k [\sin\theta x (\Delta\beta)^2] - x \Delta\beta (\cos\theta - 1)\}/2$$

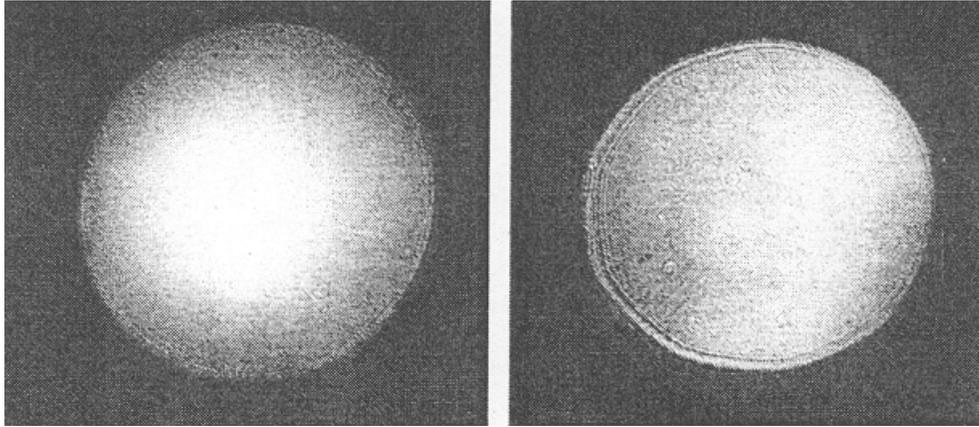


Fig. 5 — Typical infinite-fringe interferograms in the two channels

The sensitivity of  $\psi$  with respect to the rotation around the y-axis is thus of the second and first orders of the rotation angle  $\Delta\beta$ . Equally spaced fringes will appear parallel to the y-axis with a spacing of  $2\pi/[k(\Delta\beta)\{\sin\theta \Delta\beta + (\cos\theta - 1)\}]$ .

**(d) Rotation around z-axis**

When  $H_2$  is rotated by an angle  $\Delta\gamma$  along the z-axis then displacement vector:

$$\Delta\mathbf{r} = (y\Delta\gamma, -x\Delta\gamma, 0)$$

In this case, Eq. (9) can be written as:

$$\psi = \exp i (k \sin\theta y\Delta\gamma) + 1$$

$$\text{Thus, } |\psi|^2 = 4 \cos^2 \{k (\sin\theta y\Delta\gamma/2)\}$$

The sensitivity of  $\psi$  with respect to the rotation around the z-axis is thus of the first order of the rotation angle  $\Delta\gamma$ . Equally spaced fringes will appear parallel to x-axis with spacing of  $2\pi/(\sin\theta \Delta\gamma)$ .

**(2) Misalignment in  $H_1$**

In case, when there is any misalignment in  $H_1$  and the  $H_2$  is perfectly repositioned (i.e.,  $\mathbf{r} = \mathbf{r}'$ ), then the two illuminating beams on  $H_2$  gets modified as:

$$\mathbf{k}'_1 - \mathbf{k}_1 = \delta \mathbf{k}_1 \text{ and } \mathbf{k}'_3 - \mathbf{k}_3 = \delta \mathbf{k}_3;$$

Eq. (9) can now be written as:

$$\psi = \exp i (\delta \mathbf{k}_1 \cdot \mathbf{r}) + \exp i (\delta \mathbf{k}_3 \cdot \mathbf{r})$$

Thus,

$$|\psi|^2 = 4 \cos^2 [(\delta \mathbf{k}_1 - \delta \mathbf{k}_3) \cdot \mathbf{r}/2] \quad \dots(10)$$

Eq. (10) depicts the presence of finite fringes (in the interferogram) in the observation plane, which

may be in any direction depending upon the directions of  $\mathbf{k}'_1$  and  $\mathbf{k}'_3$ . By using a simple geometrical analysis, it is observed that by providing a suitable rotation to the  $H_2$  through angles  $\alpha$ ,  $\beta$  and  $\gamma$  with respect to the x, y, and z-axis [Fig. 4(b)]; the new coordinates  $x'$ ,  $y'$ ,  $z'$  can be achieved in such a manner that the relative position of the  $H_2$  with respect to the  $\mathbf{k}'$  vectors is almost identical to the initial position with respect to the  $\mathbf{k}$  vectors. This then facilitates in obtaining infinite fringe interferogram in the observation plane.

**4 Experimental Details**

In our experimental arrangement, a 35 mW He-Ne laser system was used in the first and second recording steps of the method for the formation of two different sets of spatially separated holographic optical elements on two different holographic plates  $H_1$  and  $H_2$ . A large-size collimated beam (R) and four small-size collimated beams ( $O_1$ ,  $O_2$ ,  $O_3$  and  $O_4$ ) were generated by using a 100 mm-diameter and four 30 mm-diameter collimating lenses, respectively. The shear plate interferometric technique was applied to ensure the optical quality of the collimated beams, which were used for forming the holographic optical elements on  $H_1$  and  $H_2$ . Standard Kodak D-19 developer and R-9 bleach bath solutions are used with Slavich PFG-01 plates (having spatial resolution power of more than  $3000 \text{ mm}^{-1}$ ) to give high efficiency and low noise holographic optical elements (grating holograms) on  $H_1$  and  $H_2$ . Holographic optical elements with almost uniform diffraction efficiency were generated using these holographic recording plates with exposure energies of the order of  $100\text{-}120 \mu\text{J}/\text{cm}^2$ . In order to realize the proposed interferometer set-up, the processed  $H_2$  plate is

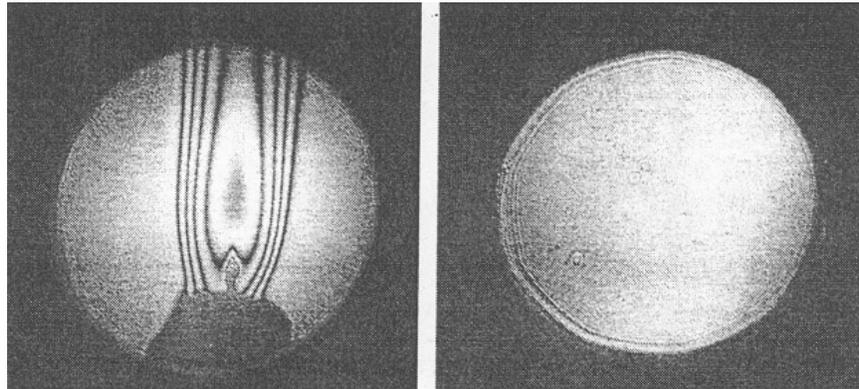


Fig. 6 — Typical interference pattern of heat flow due to a burning candle in one channel while second channel is without any object

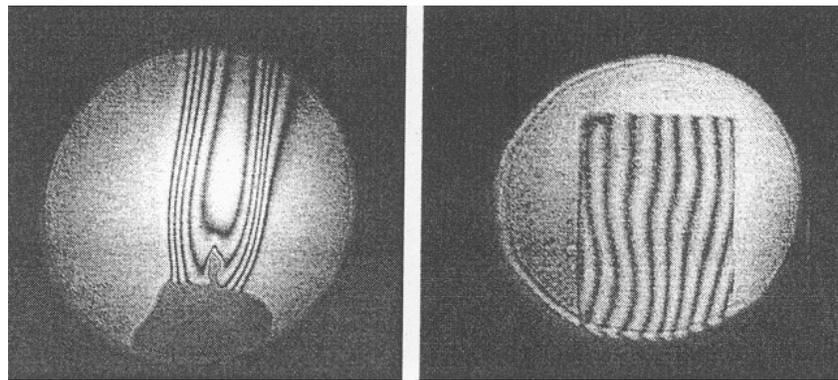


Fig. 7 — Typical interference pattern of heat flow due to a burning candle in one channel and a glass plate in the second channel

required to be repositioned at the same location at which it was formed. However, since in our recording scheme the interfering beams have permanently been frozen on a single element ( $H_1$ ), the repositioning became much simpler. It was achieved by merely mounting the  $H_2$  plate on a holder having the capabilities of providing tilt motion to the plate in horizontal and vertical directions. By using a simple alignment procedure, spatially separated infinite fringe interferograms are easily obtained in the observation plane [Fig. 5]. Optical test studies on two different phase objects were performed simultaneously and independently by inserting them in both the test arms between  $H_1$  and  $H_2$ . In our studies, initially a burning candle was inserted in one of the test arm and no phase object was inserted in the other test arm. Typical interference patterns of heat flow caused by inserting a burning candle in one of the test arm and without inserting any phase object in the other test arm are shown in Fig. 6. It is seen from Fig. 6 that both the interferograms are independent of

each other and any perturbation caused in any one of the test arms does not have any effect on the other test arm. Further studies were performed by inserting two different phase objects simultaneously and independently in both the test arms. Figure 7 shows typical interference patterns, in real time, obtained due to a burning candle in one of the test arm and a glass plate in the other test arm simultaneously and independently.

## 5 Conclusions

This paper presents a simple and cost effective method for making a compact and versatile two channel interferometer based on holographic optics, which is suitable for performing optical test studies of two different phase (transparent) phase objects simultaneously and independently. The advantage of this method lies in the fact that the proposed optical arrangement of the interferometer involves a very simple alignment procedure and portions of any one of the collimated beams  $O'_1$  or  $O'_3$  and  $O'_2$  or  $O'_4$

generated between  $H_1$  and  $H_2$  can be used as test arms for studying the phase objects. The effect of misalignment in  $H_1$  or  $H_2$  has also been studied and the infinite fringe interferograms are easily obtained by mounting the  $H_2$  on a holder having the capabilities of providing tilt motion to the plate in horizontal and vertical directions and by following a simple alignment procedure. Wavefront distortions caused due to emulsion shrinkage/swelling and substrate etc get cancelled as the interfering beams pass through the same portions of the holographic optical elements on plate  $H_2$ . The interferometer is also suitable for performing comparison type studies of different phase objects in real time. It may be seen from Figs 6 and 7 that the proposed interferometric method, in infinite fringe mode set-up, gives high contrast interference patterns on insertion of different phase objects in any one of or both the test arms. Quantitative evaluation of the phase change may be performed by phase shifting interferometry, where it is possible to acquire a series of interferograms by giving a transverse displacement to the plate  $H_2$  with a precision micrometer stage<sup>12</sup>. Further, the vital components of the interferometer could be produced in great numbers using hologram-copying methods<sup>13</sup>.

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