S$^4$CAST v2.0: sea surface temperature based statistical seasonal forecast model

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Abstract. Sea surface temperature is the key variable when tackling seasonal to decadal climate forecasts. Dynamical models are unable to properly reproduce tropical climate variability, introducing biases that prevent a skillful predictability. Statistical methodologies emerge as an alternative to improve the predictability and reduce these biases. In addition, recent studies have put forward the non-stationary behavior of the teleconnections between tropical oceans, showing how the same tropical mode has different impacts depending on the considered sequence of decades. To improve the predictability and investigate possible teleconnections, the sea surface temperature based statistical seasonal foreCAST model ($S^4$CAST) introduces the novelty of considering the non-stationary links between the predictor and predictand fields. This paper describes the development of the $S^4$CAST model whose operation is focused on studying the impacts of sea surface temperature on any climate-related variable. Two applications focused on analyzing the predictability of different climatic events have been implemented as benchmark examples.

1 Introduction

Global oceans have the capacity to store and release heat as energy that is transferred to the atmosphere altering global atmospheric circulation. Therefore, fluctuations in monthly sea surface temperature (SST) may be considered as an important source of energy affecting seasonal predictability and improving the ability to forecast climate-related variables. Much research has been conducted to study the impacts of worldwide sea surface temperature anomalies (SSTA) by means of dynamical models, observational studies and statistical methods. In this way, tropical oceans receive greater relevance (Rasmusson and Carpenter, 1982; Harrison and Larkin, 1998; Klein et al., 1999; Saravanan and Chang, 2000; Trenberth et al., 2002; Chang et al., 2006; Ding et al., 2012; Wang et al., 2012; Ham, 2013a, b; Keenlyside et al., 2013). Because of the persistence shown by SSTA, alterations that occur in the oceans are slower than changes occurring in the atmosphere. Once the thermal equilibrium between the ocean and the atmosphere is broken, oceans are able to release their energy, changing the atmospheric circulation for some time before dissipating, leading in turn to an influence on other variables. This fact explains why the SSTA can be used as potential predictor of the anomalous associated impacts.

The $S^4$CAST model presented in this work is focused on the study of the predictability and teleconnections of climate-related variables based on the remote influence of the SSTA. It has been shown that such variables can be SST (Rasmusson and Carpenter, 1982; Latif and Barnett, 1995; Harrison and Larkin, 1998; Klein et al., 1999; Trenberth et al., 2002), rainfall (Janicot et al., 2001; Drosdowsky and Chambers, 2001; Giannini et al., 2001, 2003; Rowell, 2001, 2003; Chung and Ramathan, 2006; Haylock et al., 2006; Polo et al., 2008; Joly and Voldoire, 2009; Lu, 2009; Gaetani et al., 2010; Shin et al., 2010; Fontaine et al., 2011; Nnamchi and Li, 2011; Bulić and Kucharski, 2012; López-Parages and Rodríguez-Fonseca, 2012) and other climate-related variables. In this way, there are studies that have focused on the role of the
tropical Pacific on vegetation, crop yields and the economic consequences resulting from these impacts (Hansen et al., 1998, 2001; Adams et al., 1999; Legler et al., 1999; Li and Kafatos, 2000; Naylor et al., 2001; Tao et al., 2004; Deng et al., 2010; Phillips et al., 1998; Verdin et al., 1999; Podestá et al., 1999; Travasso et al., 2009). Regarding human health, tropical SST patterns have been widely linked to the development and propagation of diseases (Linthicum et al., 2010), where El Niño–Southern Oscillation (ENSO)-related variability plays a crucial role mainly affecting tropical and subtropical regions around the world (Kovats, 2000; Patz, 2002; Kovats et al., 2003; Patz et al., 2005; McMichael et al., 2006).

The study of the impacts of tropical global SST on climate has become increasingly important during the last decades. Thus, there are dynamical and statistical prediction models that attempt to define and predict seasonal averages from interannual to multidecadal timescales. In this way, general circulation models (GCMs) emerged from the need to reproduce the ocean–atmosphere interactions, responsible for much of climate variability whose major component is attributed to ENSO phenomenon (Bjerknes, 1969; Gill, 1980). Numerous research centers have done a hard work to create their own prediction systems in which coupled ocean–atmosphere GCMs are used in conjunction with statistical methods to achieve reliable ENSO variability predictions and analyze the skill of these models (Cane et al., 1986; Barnett and Preisendorfer, 1987; Zebiak and Cane, 1987; Barnston and Ropelewski, 1992; Barnett et al., 1993; Barnston et al., 1994, 1999; Ji et al., 1994a, 1994b; Van den Dool, 1994; Mason et al., 1999). Predictability of rainfall has become a scope for these models, finding research that has focused on this issue by means of dynamical and statistical models (Gar- ric et al., 2002; Coelho et al., 2006). However, the difficulty of GCMs to adequately reproduce the tropical climate variability remains a real problem, so that in recent years the number of studies focusing on specific aspects of the biases of these models has increased exponentially (Biasutti et al., 2006; Richter and Xie, 2008; Wahl et al., 2011; Doi et al., 2012; Li and Xie, 2012; Richter et al., 2012; Bellenger et al., 2013; Brown et al., 2013; Tonizzio and Woolnough, 2013; Vannière et al., 2013; Xue et al., 2013; Li and Xie, 2014).

Statistical models have been widely used as an alternative way of climate forecasting, including several techniques described below. Model output statistics (MOS) determine a statistical relationship between the predictand and the variables obtained from dynamic models (Glahn and Lowry, 1972; Klein and Glahn, 1974; Vislocky and Fritsch, 1995). Stochastic climate models were defined in the 1970s to be first applied to predict SSTAs and thermocline variability (Hasselmann, 1976; Frankignoul and Hasselmann, 1977) and later addressing non-linearity problems (Majda et al., 1999). Moreover, linear inverse modeling (Penland and Sardeshmukh, 1995) has been used in predicting variables such as tropical Atlantic SSTAs (Penland and Matrosova, 1998) and the study of Atlantic meridional mode (Vimont, 2012). Statistical modeling with neural networks is also applied in climate prediction (Gardner and Dorling, 1998; Hsieh and Tang, 1998; Tang et al., 2000; Hsieh, 2001; Knutti et al., 2003; Baboo and Shereef, 2010; Shukla et al., 2011) with the potential to be a nonlinear method capable of addressing the problems in atmospheric processes that are overlooked in other statistical methodologies (Tang et al., 2000; Hsieh, 2001).

A special mention goes to two linear statistical methods: maximum covariance analysis (MCA) used in the SCAST model and canonical correlation analysis (CCA). These methods have been widely used in seasonal climate forecasting, either to complement dynamical models or to be applied independently. In this way, Climate Predictability Tool (CPT) developed at International Research Institute for Climate and Society (IRI) allows the user to apply multivariate linear regression techniques (e.g., CCA) to get their own predictions (Korecha and Barnston, 2007; Recalde-Coronel et al., 2014; Barnston and Tippett, 2014). In essence, these techniques serve to isolate co-variability coupled patterns between two variables that act as predictor and predictand, respectively (Bretherton et al., 1992). Based on the ability of the SSTAs as predictor field, these methods were originally applied to analyze the predictability of phenomenon like ENSO (Barnston and Ropelewski, 1992), 500 mb height anomalies (Wallace et al., 1992) or global surface temperature and rainfall (Barnston and Smith, 1996). Nevertheless, there is research discussing the use of these methods, focusing on the differences between the two techniques (Cherry, 1996, 1997) and on the limitations in their applications (Newman and Sardeshmukh, 1995).

The co-variability patterns between SSTAs themselves might fluctuate from one given study period to another, determining non-stationary behavior along time. In this way, teleconnections associated with El Niño or with the tropical Atlantic are effective in some periods but not in others. In this way, Rodríguez-Fonseca et al. (2009) suggested how the interannual variability in the equatorial Atlantic could be used as predictor of Pacific ENSO after the 1970s, a theory that has been subsequently reinforced by further analysis (Martin-Rey et al., 2012, 2014, 2015; Polo et al., 2015). The non-stationarity in terms of predictability of rainfall has also been found for West African rainfall (Janicot et al., 1996; Fontaine et al., 1998; Mohino et al., 2011; Losada et al., 2012; Rodriguez-Fonseca et al., 2011, 2015), and Europe (López-Parages and Rodriguez-Fonseca, 2012; López-Parages et al., 2014). Thus, the existence of non-stationarities is a key factor in the development of the statistical model.

The present paper describes a statistical model based on the predictive nature of SSTAs treating the stationarity in the relationships between the predictor and predictand fields. Section 2 describes the theoretical framework including the statistical methodology and the significance of the statistical analysis. Section 3 is dedicated to SCAST model description including the determination of stationary periods,
hindcast and forecast calculations and validation. Section 4 describes two case studies concerning the predictability of Sahelian rainfall and tropical Pacific SSTA.

2 Theoretical framework

2.1 Statistical methodology

Maximum covariance analysis is a broadly used statistical discriminant analysis methodology based on calculating principal directions of maximum covariance between two variables. This statistical analysis considers two fields, \( Y \) (predictor) and \( Z \) (predictand) (Bretherton et al., 1992; Cherry, 1997; Widmann, 2005) for applying the singular value decomposition (SVD) to the cross-covariance matrix \( C \) in order to be maximized. SVD is an algebraical technique that diagonalizes non-squared matrices, as it can be the case of the matrices of the two fields to be maximized.

In the meteorological context, \( C \) is dimensioned in time \( (n_t) \) and space domains \( (n_Y \) and \( n_Z \) for \( Y \) and \( Z \), respectively), although the spatial domain can be more complex depending on the user requirements. SVD calculates linear combinations of the time series of \( Y \) and \( Z \), named as expansion coefficients (hereinafter \( U \) and \( V \) for \( Y \) and \( Z \), respectively) that maximize \( C \). The expansion coefficients are computed by diagonalization of \( C \). Since \( C \) is non-squared, diagonalization is first done to \( A = CC^T \) and then to \( B = C^T C \). The singular vectors \( R \) and \( Q \) are the resultant eigenvectors from each diagonalization, which are the spatial configurations of the co-variability modes. The associated loadings on time domain are the expansion coefficients \( U \) and \( V \). The eigenvalues are a measure of the percentage of variance explained by each mode.

Mathematically, the time anomalies of both, \( Z \) and \( Y \) fields are calculated by removing the climatological seasonal cycle to the seasonal means.

\[
Z' = Z - \overline{Z} \quad (1)
\]

\[
Y' = Y - \overline{Y} \quad (2)
\]

Then, the cross-covariance matrix is calculated as

\[
C_{Y'Z'} = \frac{Y'Z'^T}{(n_t - 1)}. \quad (3)
\]

MCA diagonalizes Eq. (3) by SVD methodology, obtaining the singular vectors \( R \) and \( Q \) from which the expansion coefficients are obtained according to the following expression:

\[
U = R^T Y. \quad (4)
\]

\[
V = Q^T Z. \quad (5)
\]

Using the eigenvectors, the percentage of explained covariance is calculated as

\[
s_c f_k = \frac{\lambda_k}{\sum \lambda_i} \quad (6)
\]

where \( \lambda_k \) is the eigenvalue for each \( k \) mode and \( r \) represents the number of modes taken into account for the analysis.

The expression from which an estimation of the predictand is obtained is a linear model as

\[
\hat{Z} = \Phi Y, \quad (7)
\]

where \( \Phi \) is the so-called regression coefficient and \( \hat{Z} \) denotes an estimation of the data to be predicted (hindcast).

Taking into account that \( S \) is the regression map of the field \( Z \) onto the direction of \( U \)

\[
S = UZ^T, \quad (8)
\]

assuming good prediction \( \hat{Z} \), it follows that

\[
S = U\hat{Z}^T \quad (9)
\]

Introducing the equality \((UU^T)(UU^T)^{-1} = I\) and multiplying in Eq. (9) the following expression is obtained:

\[
(UU^T)(UU^T)^{-1} S = U\hat{Z}^T. \quad (10)
\]

Removing \( U \) from both terms

\[
\hat{Z} = U^T (UU^T)^{-1} S^T. \quad (11)
\]

Considering now the expression \( U = Y^T R \) it follows that

\[
\hat{Z} = Y R (UU^T)^{-1} S. \quad (12)
\]

Comparing this expression with Eq. (7) and introducing Eq. (8) it can be concluded that

\[
\Phi = R (UU^T)^{-1} UZ^T. \quad (13)
\]

Which is the regression coefficient to be calculated when defining the linear model from which the predictions and hindcasts will be obtained.

2.2 Statistical field significance

There are many statistical tests to assess the robustness of a result. The \( S^4 \)CAST uses a non-parametric test because, a priori, the model does not know the distribution of the predictand field. Thus, applying Monte Carlo testing assesses the robustness of the results and is used to validate the \( S^4 \)CAST model skill. This method involves performing a large number \((N > 500)\) of permutations from the original time series.
Each permuted time series is used to repeat the calculation and compare the obtained results with the real values. Once this is done, the values obtained with the N permutations are taken to create a random distribution to finally determine the position of the real value within the distribution, which will indicate the statistical significance of the obtained value. This method has been described and used in previous research (Livezey and Chen, 1983; Barnett, 1995; Maia et al., 2007). The user inputs the level of statistical significance at which the test is applied, being the most used 90 % (0.10), 95 % (0.05) and 99 % (0.01).

3 S\(^4\) CAST model

S\(^4\)CAST v2.0 model is conceived as a statistical tool to study the predictability and teleconnections of variables that strongly co-vary with SSTA variability in remote and nearby locations to a particular region of study. The code has been developed as a MATLAB\(^\text{®}\) toolbox. The software requirements are variable and depend on user needs. The spatial resolution and size of data files used as inputs are directly proportional to memory requirements. The software generates an “out of memory” message whenever it requests a segment of memory from the operating system that is larger than what is currently available. The model software consists of three main modules (Fig. 1), each composed of a set of sub-modules whose operation is described below.

3.1 Model Inputs

S\(^4\)CAST v2.0 has a direct execution mode. By simply typing “\texttt{S4cast}” in the command window, the user is prompted to enter a series of input parameters in a simple and intuitive way.

3.1.1 Loading databases

The model is ready to work with Network Common Data Form (NetCDF) data files. There are different conventions to set the attributes of the variables contained in NetCDF files. In this way, the data structure must conform as far as possible to the Cooperative Ocean/Atmosphere Research Service (COARDS) convention. Execution errors that may occur due to the selection of data files are easily corrected by minor modifications of data assimilation scripts. Data files can be easily introduced at the request of the user. Once downloaded from the website of a determined center of climate and environmental research, the user inserts data files into the directory set by default ($\texttt{S4CAST\_v2.0/data\_files}$).

3.1.2 Input parameters

In order to correctly introduce the input parameters, it is convenient to present some terms commonly used in seasonal forecasting. In this way, the forecast period corresponds to the $n$-month seasonal period concerning the predictand for which the forecast and hindcasts are performed. Moreover, the lead time refers to time expressed in months between the last month comprising the predictor monthly period and the first month comprising the forecast period. Thus, a medium-range forecast refers to a lead-time set to zero, while a long-range forecast refers to a lead-time equal or larger than 1 month. Strictly, we cannot speak about lead-time when the predictor monthly period partially or totally overlaps the forecast period. In this case we refer to lag-time expressed in months between the last month comprising the forecast period and the last month for predictor period. The relationship between lead-time and lag-time depends on the number of months comprising the forecast period. Finally, the forecast time is commonly used to describe the time gap expressed in months between the predictor and predictand monthly periods, assuming the same concept represented by the lead time.

In the first step, predictand and predictor data files are selected. In this way, the predictand field can be precipitation, SST, or any variable susceptible to be predicted from SSTA. The predictor is restricted to SST.

Once predictor and predictand fields are selected, the available common time period between them is analyzed and displayed so that the user is prompted to select the whole common period for analysis or other within it. The same temporal dimension in both fields is required in the statistical analysis to construct the cross-covariance matrix (see Sect. 2.1).

The next step is for selecting the $n$-month forecast period in which the predictand is considered. The model allows for a selection from 1 ($n = 1$) to 4 ($n = 4$) months. From the forecast period, the user determines a specific lead time, relative to the predictor, from which medium range (lead time 0) or long range (lead time > 0) forecast can be performed. In order to study and evaluate possible teleconnections, the
temporal overlapping between the forecast period and the predictor is also available by defining the monthly lags between both fields from monthly lag 0 (synchronous) referred to the case in which the predictor and the predictand fields are taken at the same $n$-month period, through partial overlapping to eliminate the overlapping (medium-range forecast). Note that synchronous and partially overlapping seasons between predictor and predictand fields are not useful when referring to predictability, although this option is available in order to perform simulations focused on the study of physical mechanisms (teleconnections) between the predictor and predictand fields. Thus, it is worth noting that the model may be focused in the study of the predictability but it can be also used to detect teleconnections between SST (predictor) and a predictand field.

Monthly lags indicating forecast times (lead times) are user selectable. To illustrate the above, taking a hypothetical case in which the forecast period corresponds to the months of February–March–April (FMA) whatever the region, the synchronous option will consider the predictor in FMA, while partially overlapping occurs when the predictor is taken for January–February–March (JFM) and December–January–February (DJF). Avoiding overlapping, lead time 0 will be NDJ (November–December–January), lead time 1 will be OND (October–November–December), lead time 2 will be SON (September–October–November), etc., without overlapping the FMA season of the previous year. Thus, the user can select any 3-month isolated period from FMA (synchronous) to MJJ (May–June–July).

Next, the spatial domains of both predictor and predictand fields are easily selected from its latitudinal and longitudinal values. Considering the above options, the user can select a sequence of successive monthly lags or only one so that the predictor is taken for the total amount of selected information (e.g., NDJ + OND + SON).

Later, there is the possibility of applying a filter to the time series of predictor and predictand fields. The current version uses a Butterworth filter, either as high-pass or low-pass filter frequently used in climate-related studies (e.g., Roe and Steig, 2004; Enfield and Cid-Serrano, 2006; Mokhov and Smirnov, 2006; Ault and George, 2012; Schurer et al., 2013), although the selection of low-pass filter is not suitable for seasonal forecast and subsequently is not useful in the current version. Anyway, the possibility of selecting a low-pass filter is maintained in order to include decadal predictability in a future version of the model. The application of a filter allows the user to isolate the frequencies at which the variability operates, which can have different sources of predictability. In this way, the user selects the cutoff frequency, following the expression $2\pi f / T$, being $\pi$ the sampling interval and $T$ the period to be filtered both in the same units of time. If no filter is applied, the raw data are used. There are plenty of filters that could be applied and future versions of the model will include different possibilities.

In the case of multiple time selection for predictor, the statistical methodology is first applied considering the largest lead time and successively adding information for other lead times up to the present. Therefore, continuing with the example above in which the forecast period corresponds to FMA if selected lead times are from 0 to 3, the first predictor selection is made considering the 3-months lead-time period (SON). After, the 2-months lead-time period is added (ASO + SON), next up to the period of 1-month delayed (ASO + SON + OND) and finally the case up to the period with a lead time equal to zero (ASO + SON + OND + NDJ). Previous example is illustrated in Fig. 2.

Once the matrices are determined for each predictor time selection, the statistical methodology is applied. Up to now, the model applies the MCA discriminant analysis technique, although other statistical methodologies will be included in future releases, including CCA or nonlinear methods as neural network and Bayesian methodologies. As indicated in the previous section, MCA determines a new vector base in which the relations between the variables are maximized. Thus, it is important to choose a number of modes (principal directions) to be considered in the computations, selecting either a single mode or a set of them, always consecutive. The analysis of stationarity is performed for a single mode selection. For multi-mode selection, the whole time series will be considered.

The statistical field significance level is set for the first time to assess the analysis of stationarity. Thus, the model
runs for the entire period and for those periods for which the relationships are considered stationary within it. This is internally established by applying the method explained later in the Sect. 3.2.1.

3.1.3 Data preprocessing

From selected data files and input parameters previously defined, preprocessing of data is performed so that the data are prepared for implementing statistical methodology.

3.2 Statistical tools

At this point the statistical procedure described in the methodology is applied considering different periods based on the previously described stationary analysis.

3.2.1 Analysis of stationarity

Stationarity refers to changes along time in the co-variability pattern between two variables. Thus, we speak about stationarity when such a pattern of co-variability keeps invariant within a time period and therefore will be non-stationary when showing changes. To evaluate how much the predictor (Y) and the predictand (Z) fields are related to each other, the model calculates running mean correlations between the expansion coefficients indicated in Eqs. (4) and (5) for the selected kth mode along the record. This technique has been widely used to determine the stationarity of the relationships between the time series of climate indices (e.g., Camberlin et al., 2001; Rimbu et al., 2003; Van Oldenborgh and Burgers, 2005). Next, the significance level of correlation coefficients is calculated according to the method explained in Sect. 2.2. In this way, stationary relationships between the predictor (Y) and the predictand (Z) fields are established by applying a 21-year moving correlation window analysis between the leading expansion coefficients of both fields obtained from the discriminant analysis method (Sect. 2.1) using the whole record in accordance with the evolution of the correlation coefficient. To do this, three types of 21-year moving correlation windows are user selectable: “delayed” to correlate 1 year and the 20 previous years; “centered” to correlate 1 year, the 10 previous years and the 10 next years; or “advanced” to correlate 1 year and the 20 next years. Note that delayed correlation coefficients are the most suitable in a forecast context when referring to future prediction. Nevertheless, centered and advanced correlation coefficients are also available for application no matter the aim of the user.

From previous analysis, three different periods are analyzed depending on the stationarity of the predictability: use the significant correlation period (hereinafter SC) for which the expansion coefficients are significantly correlated, use no significant correlation period (hereinafter EP) and work with the entire period (hereinafter EP). The model performs all calculations for each period separately and, from them, the simulated maps (hindcasts) of the predictand for each year are calculated by applying cross-validation.

3.2.2 Model validation

Cross-validation is used in climate forecasting as part of statistical models when assessing forecast skill (Michaelsen, 1987; Barnston and Van den Dool, 1993; Elsner and Schmertmann, 1994). This method is intended as a model validation technique in which the data for the predictor and the predictand for a given time step is removed from the analysis to make an estimate of it with the rest of data, comparing the simulated value with the removed one. In this way, a cross-validated hindcast is obtained. In the S4CAST model, the leave-one-out method is applied as described by Dayan et al. (2014). From the comparison between the predicted value and the original one, the skill of the model can be inferred using different skill scores. S4CAST considers the Pearson correlation coefficients and the root mean square error (RMSE) although other scores will be introduced in future versions.

3.3 Model outputs

Modes of co-variability are related to spatial patterns of different variables that co-vary over time, and thus are linked to each other. In the case of MCA, the covariance matrix is computed and the SVD method is applied to provide a new basis of eigenvectors for the predictor and predictand fields which covariance is maximized. The obtained singular vectors describe spatial patterns of anomalies in each of the variables that tend to be related to each other. Regression and correlation maps and corresponding expansion coefficients determine each mode of co-variability for the predictor and predictand fields. The expansion coefficients indicate the weight of these patterns in each of the time steps. Thus, regression and correlation co-variability maps can be represented. This is done with the original anomalous matrix, highlighting those grid points whose time series are highly correlated with the obtained expansion coefficients, showing large co-variability and determining the key regions of prediction. To represent it, regression and correlation maps are calculated to analyze the coupling between variables and to understand the physical mechanisms involved in the link.

On the other hand, the time series of the expansion coefficients determine the scores of the regression and correlation maps at each time along the study period. The model represents the expansion coefficients used to calculate the regression coefficients. Thus, those years in which the expansion coefficients for the predictor and the predictand are highly correlated will coincide with years in which we can expect a better estimation.

In the current version of the model, the RMSE and the Pearson correlation coefficients skill scores have been included. These techniques are applied to compare the observed and simulated maps (hindcasts) of the predictand field.
obtaining correlation and RMSE maps and time series. On the one hand, maps are obtained calculating for each grid point the skill scores between the hindcast and the observed maps. On the other hand, time series are obtained for each time by applying correlation and RMSE between the area average of the observed and estimated maps. Some comments on these techniques are addressed by Barnston (1992). The S4CAST model generates the hindcast within the EP, SC and NSC periods separately from applying the one-leave-out method (Dayan et al., 2014) and then the statistical methodology.

4 Application of the model: case studies

Two different case studies have been simulated as benchmark examples. Both cases are focused on the predictive ability of the tropical Atlantic SSTA. In a first simulation, the predictand field corresponds to Sahelian rainfall. In a second simulation, winter tropical Pacific SSTA have been used as predictand field. The links between tropical Atlantic Ocean and the two variables selected as predictand fields have been widely studied exhibiting non-stationary relationships. The results obtained by applying the model have been contrasted in the following sections. Tables 1 and 2 list the entries for both case studies to be easily reproduced by the user.

4.1 Tropical Atlantic – Sahelian rainfall

In this first case study the model has been applied to validate its use in the study of seasonal rainfall predictability in the Sahel taking tropical Atlantic as predictor field. The West African Monsoon (WAM) is characterized by a strong seasonal rainfall regime that occurs from July to September related to the semi-annual shift of the Intertropical Convergence Zone (ITCZ) together with the presence of a strong thermal gradient between the Sahara and the ocean in the Gulf of Guinea. The interannual fluctuations in seasonal rainfall are due to various causes; the changes in global SST are the main driver of WAM variability (Folland, 1986; Palmer, 1986; Fontaine et al., 1998; Rodríguez-Fonseca et al., 2015). Particularly, several observational studies suggest the influence of tropical Atlantic SSTA on the WAM at interannual timescales (Giannini et al., 2003; Polo et al., 2008; Joly and Voldoire, 2009; Nnamchi and Li, 2011).

Regarding the input parameters (Table 1), the predictand field corresponds to precipitation from GPCC Full Data Reanalysis monthly means of precipitation appended with GPCC monitoring data set from 2011 onwards with a resolution of 1.0° × 1.0° covering the period from January 1901 to March 2015 (Rudolf et al., 2010; Becker et al., 2013; Schneider et al., 2014; http://gpcc.dwd.de). The forecast period consists of July–August–September (JAS), computing seasonal anomalous rainfall in the Sahelian domain (18° W–10° E; 12–18° N). No frequency filter is applied for predictand. The predictor field corresponds to NOAA Extended Reconstructed SST (ERSST) V3b monthly means of SST with a resolution of 2.0° × 2.0° spanning the period from January 1854 to May 2015 (Smith and Reynolds, 2003, 2004; Smith et al., 2008; http://www.esrl.noaa.gov/psd/data/gridded/data.noaa.ersst.html). The spatial domain corresponds to southern subtropical and equatorial Atlantic band (60° W–20° E; 20° S–4° N). A high-pass filter with cutoff frequency set to 7 years has been applied to the predictor time series in order to analyze the influence of SST interannual variability, which includes leading oceanic interannual variability modes such as the Atlantic equatorial mode (AEM) (Polo et al., 2008) or the South Atlantic Ocean dipole (SAOD) (Nnamchi et al., 2011). Medium-range forecast has been taken into account setting the lead time to zero (equivalent to monthly lag 3). In this way, April–May–June (AMJ) is the selected season for predictor.

For applying the methodology, the leading mode of co-variability (k = 1) has been selected. The correlation curve (Fig. 3) reflects the stationary periods (SC and NSC) within EP period as stated in Sect. 3.2.1. The SC period is almost restricted to years from 1932 to 1971 with some exceptions. The remaining years are taken to analyze the predictability for the NSC period.

Figure 4 show regression maps associated with the leading mode for the periods SC, EP and NSC explaining 50, 32 and 41% of co-variability, respectively. For the SC period (Fig. 4, top panels), the co-variability pattern exhibits a quasi-isolated cooling in the tropical Atlantic associated with a rainfall dipole over West Africa with negative anomalies in the region of the Gulf of Guinea and opposite in the Sahel. The opposite co-variability pattern takes place under negative scores of the expansion coefficient. These results are in agreement with those found in the last decades of the 20th century by several authors who have discussed the role of
Table 1. Input parameters used to reproduce the first case study. Left column represents the statements reproduced by the model with the same format as in the simulation. Right column represents the input parameters entered by the user.

<table>
<thead>
<tr>
<th>Statements reproduced by the model</th>
<th>Input parameters entered by the user</th>
</tr>
</thead>
<tbody>
<tr>
<td>Enter the NetCDF file containing the predictand data in the path /S4CAST_v2.0/data_files/predictand/ Press enter to continue</td>
<td>“y”</td>
</tr>
<tr>
<td>PREDICTAND data available from Jan 1901 to Mar 2015</td>
<td></td>
</tr>
<tr>
<td>Enter the NetCDF file containing the predictor data in the path /S4CAST_v2.0/data_files/predictor/ Press enter to continue</td>
<td></td>
</tr>
<tr>
<td>PREDICTOR data available from Jan 1854 to May 2015</td>
<td></td>
</tr>
<tr>
<td>Select a common analysis period</td>
<td></td>
</tr>
<tr>
<td>The common longest analysis period extends from Jan 1902 to Mar 2015</td>
<td></td>
</tr>
<tr>
<td>Do you want to select this period? y/n</td>
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</tr>
<tr>
<td>The selected analysis period extends from Jan 1902 to Mar 2015</td>
<td></td>
</tr>
<tr>
<td>Select the forecast period</td>
<td></td>
</tr>
<tr>
<td>Type 1 to select a set of months</td>
<td></td>
</tr>
<tr>
<td>Type 2 to select 1 month</td>
<td></td>
</tr>
<tr>
<td>Enter the forecast period using the initials of the months</td>
<td>“JAS”</td>
</tr>
<tr>
<td>2015 forecast available from lead time 1 (monthly lag 4) to lead time 6 (monthly lag 9)</td>
<td></td>
</tr>
<tr>
<td>Enter PREDICTAND spatial domain</td>
<td></td>
</tr>
<tr>
<td>West longitude from −179.5 to 179.5</td>
<td>−18</td>
</tr>
<tr>
<td>East longitude from −179.5 to 179.5</td>
<td>10</td>
</tr>
<tr>
<td>South latitude from −89.5 to 89.5</td>
<td>12</td>
</tr>
<tr>
<td>North latitude from −89.5 to 89.5</td>
<td>18</td>
</tr>
<tr>
<td>Do you want to standardize the predictand? y/n</td>
<td>“y”</td>
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<tr>
<td>Do you want to apply a Butterworth filter to the predictand? y/n</td>
<td>“n”</td>
</tr>
<tr>
<td>Enter PREDICTOR spatial domain</td>
<td></td>
</tr>
<tr>
<td>West longitude from −180 to 178</td>
<td>−60</td>
</tr>
<tr>
<td>East longitude from −180 to 178</td>
<td>20</td>
</tr>
<tr>
<td>South latitude from −88 to 88</td>
<td>−20</td>
</tr>
<tr>
<td>North latitude from −88 to 88</td>
<td>5</td>
</tr>
<tr>
<td>Do you want to standardize the predictor? y/n</td>
<td>“n”</td>
</tr>
<tr>
<td>Do you want to apply a Butterworth filter to the predictor? y/n</td>
<td>“y”</td>
</tr>
<tr>
<td>Type 1 to apply a high-pass filter</td>
<td>1</td>
</tr>
<tr>
<td>Type 2 to apply a low-pass filter</td>
<td></td>
</tr>
<tr>
<td>Introduce the cutoff frequency</td>
<td>7</td>
</tr>
<tr>
<td>Select the predictor monthly periods</td>
<td></td>
</tr>
<tr>
<td>Type 1 to select a set of chronological monthly periods</td>
<td>2</td>
</tr>
<tr>
<td>Type 2 to select one monthly period</td>
<td></td>
</tr>
<tr>
<td>Enter the monthly lag regarding the predictand</td>
<td>3</td>
</tr>
<tr>
<td>Select the number of modes for MCA analysis</td>
<td></td>
</tr>
<tr>
<td>Do you want to select a set of modes? y/n</td>
<td>“n”</td>
</tr>
<tr>
<td>Enter the mode number</td>
<td>1</td>
</tr>
<tr>
<td>To assess the stationarity the model will analyze 21 years moving correlation windows between the expansion coefficients of the PREDICTOR and PREDICTAND fields obtained from MCA method Indicate delayed, centered or advanced moving correlation windows</td>
<td>“delayed”</td>
</tr>
<tr>
<td>To assess the significant stationary periods, indicate the degree of statistical significance from 0 to 100</td>
<td>90</td>
</tr>
<tr>
<td>To validate the model skill, indicate the degree of statistical significance from 0 to 100</td>
<td>90</td>
</tr>
</tbody>
</table>
Figure 4. Regression maps obtained for the leading mode by applying MCA between SSTA in the tropical Atlantic (predictor) and western Sahel rainfall (predictand). Left column represents the homogeneous regression map done by projecting the expansion coefficient $U$ onto global SSTA ($^\circ$C). Right column represents the heterogeneous regression map done by projecting expansion coefficient $U$ onto the anomalous Sahelian rainfall (mm day$^{-1}$). Period SC (top panels), EP (middle panels) and NSC (bottom panels). Rectangles show the selected regions for predictor and predictand fields considered in the MCA analysis. Values are plotted in regions where statistical significance under a Monte Carlo test is higher than 90%.

the tropical Atlantic SST as a dominant factor in the WAM variability at interannual and seasonal timescales (Janowiak, 1988; Janicot, 1992; Fontaine and Janicot, 1996). Losada et al. (2010b) found how the response to an isolated positive equatorial Atlantic Niño event is a dipolar rainfall pattern in which the decrease of rainfall in Sahel is related to the increase of rainfall in Guinea (as in Fig. 4) due to changes in the sea–land pressure gradient between Gulf of Guinea SSTs and the Sahel. Mohino et al. (2011) and Rodríguez-Fonseca et al. (2011) have found in the observations how this dipolar behavior takes place for some particular decades coinciding with the SC periods, confirming in this way the correct determination of the leading co-variability mode by the model. When considering the EP period (Fig. 4, middle panels), a co-variability pattern similar to that observed for the SC period is appreciated with small differences. Regarding the predictand field, the anomalous rainfall signal is less intense when compared to SC. For the predictor, the cooling in the tropical Atlantic is accompanied by opposite weak anomalies in the north subtropical and tropical Pacific. Regarding the NSC period (Fig. 4, bottom panels), as for the previous periods (SC, EP) a cooling in the tropical Atlantic is observed concerning the predictor associated with negative rainfall anomalies in the Gulf of Guinea and a weak positive signal in the eastern Sahel, virtually disappearing the rainfall dipole. The global SSTA regression map shows a significant warming in the tropical Pacific. The opposite pattern should be considered under negative scores of the expansion coefficient.

The results presented above support the existence of a non-stationary behavior of the teleconnections between SSTA variability and rainfall associated with WAM. Several authors have addressed the dipolar anomalous rainfall pattern as a response of an isolated tropical Atlantic warming (cooling) (Rodríguez-Fonseca et al., 2011; Losada et al., 2010a, b; Mohino et al., 2011) restricted to the period 1957–1978 in the observations. The uniform rainfall signal over the whole of West Africa, with negative anomalies related to a cooling over the tropical Atlantic and an opposite sign pattern over the tropical Pacific, is only observed for the period from 1979 in advance. These results agree with Losada et al. (2012), who focused on non-stationary influences of tropical global SST in WAM variability, explaining how the disappearance of the dipole was due to the counteracting effect of the anomalous responses of the Pacific and Atlantic on the Sahel. Recently, Diatta and Fink (2014) have documented similar non-stationary relationships.

The associated skill of the model to reproduce the rainfall is shown in Fig. 5 in terms of correlation maps and time series for SC and EP periods. A qualitative improvement is ob-
observed when considering the SC periods instead of the whole period (EP). This result points to a better spatial distribution of the significant values for particular decades in which the signal extends to a larger spatial domain. In order to analyze the performance of the simulation for each particular year, the correlation between observed and predicted maps at each time step is calculated and shown in Fig. 5. There is no skill when NSC period is considered (Fig. 6). Since it has only been considered the leading mode of co-variability, the time series of validation between observed and simulated rainfall should evolve following the absolute values of the expansion coefficients. Thus, when the expansion coefficient ($U$) of the predictor (SST) shows high scores in the leading mode, good hindcasts are obtained.

4.2 Tropical Atlantic – tropical Pacific

A non-stationary behavior in the association between tropical Atlantic and tropical Pacific SSTA has been recently documented in some research suggesting that the tropical Atlantic SSTA during the boreal summer could be a potential predictor of winter tropical Pacific SSTA variability after the 1970s (Rodríguez-Fonseca et al., 2009; Ding et al., 2012). In this section, the S$^4$CAST model has been applied to corroborate the non-stationarity in the teleconnection between tropical Atlantic considered as predictor field and tropical Pacific variability, a feature that has been also demonstrated in Martin del Rey et al. (2015).

The input parameters are listed in Table 2. Both predictor and predictand fields correspond to NOAA ERSST introduced in the previous section (Sect. 4.1), covering the period from January 1854 to May 2015. The forecast period consists of December–January–February–March (DJFM). The selected region for predictand corresponds to SSTA in the tropical Pacific domain ($120^\circ$E–$60^\circ$W; $30^\circ$S–$20^\circ$N), while the predictor corresponds to tropical Atlantic SSTA ($60^\circ$W–$20^\circ$E; $20^\circ$S–$4^\circ$N) and has been considered for the period July–August–September–October (JASO), which means long-range forecast sets the lead time to 1 month. A high-pass filter with cutoff frequency set to 7 years has been applied to both predictor and predictand time series in order to analyze the predictability considering interannual variability. For applying the methodology and assess the stationary periods (SC and NSC) within EP, the leading mode of co-variability ($k = 1$) has been selected.
Table 2. Input parameters used to reproduce the second case study. Left column represents the statements reproduced by the model. Right column represents the input parameters.

<table>
<thead>
<tr>
<th>Statements reproduced by the model</th>
<th>Input parameters entered by the user</th>
</tr>
</thead>
<tbody>
<tr>
<td>Enter the NetCDF file containing the predictand data in the path /S4CAST_v2.0/data_files/predictand/</td>
<td>Press enter to continue</td>
</tr>
<tr>
<td>Enter the NetCDF file containing the predictor data in the path /S4CAST_v2.0/data_files/predictor/</td>
<td>Press enter to continue</td>
</tr>
<tr>
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</tr>
<tr>
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<td>Do you want to select this period? y/n</td>
</tr>
<tr>
<td>Type 1 to select a set of months</td>
<td>1</td>
</tr>
<tr>
<td>Type 2 to select 1 month</td>
<td></td>
</tr>
<tr>
<td>Enter the forecast period using the initials of the months</td>
<td>“JAS”</td>
</tr>
<tr>
<td>2016 forecast not available</td>
<td></td>
</tr>
<tr>
<td>Enter PREDICTAND spatial domain</td>
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</tr>
<tr>
<td>West longitude from −179.5 to 179.5</td>
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</tr>
<tr>
<td>East longitude from −179.5 to 179.5</td>
<td>−60</td>
</tr>
<tr>
<td>South latitude from −89.5 to 89.5</td>
<td>−30</td>
</tr>
<tr>
<td>North latitude from −89.5 to 89.5</td>
<td>20</td>
</tr>
<tr>
<td>Do you want to standardize the predictand? y/n</td>
<td>“n”</td>
</tr>
<tr>
<td>Do you want to apply a Butterworth filter to the predictand? y/n</td>
<td>“y”</td>
</tr>
<tr>
<td>Type 1 to apply a high-pass filter</td>
<td>1</td>
</tr>
<tr>
<td>Type 2 to apply a low-pass filter</td>
<td></td>
</tr>
<tr>
<td>Enter the cutoff frequency</td>
<td>7</td>
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<tr>
<td>Enter PREDICTOR spatial domain</td>
<td></td>
</tr>
<tr>
<td>West longitude from −180 to 178</td>
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<td>East longitude from −180 to 178</td>
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<td>South latitude from −88 to 88</td>
<td>−20</td>
</tr>
<tr>
<td>North latitude from −88 to 88</td>
<td>5</td>
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<tr>
<td>Do you want to standardize the predictor? y/n</td>
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<tr>
<td>Do you want to apply a Butterworth filter to the predictor? y/n</td>
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<td>Type 2 to apply a low-pass filter</td>
<td></td>
</tr>
<tr>
<td>Introduce the cutoff frequency</td>
<td>7</td>
</tr>
<tr>
<td>Select the predictor monthly periods</td>
<td></td>
</tr>
<tr>
<td>Type 1 to select a set of chronological monthly periods</td>
<td>2</td>
</tr>
<tr>
<td>Type 2 to select one monthly period</td>
<td></td>
</tr>
<tr>
<td>Enter the monthly lag regarding the predictand</td>
<td>5</td>
</tr>
<tr>
<td>Select the number of modes for MCA analysis</td>
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</tr>
<tr>
<td>Do you want to select a set of modes? y/n</td>
<td>“n”</td>
</tr>
<tr>
<td>Enter the mode number</td>
<td>1</td>
</tr>
<tr>
<td>To assess the stationarity the model will analyze 21 years moving correlation windows between the expansion coefficients of the PREDICTOR and PREDICTAND fields obtained from MCA method</td>
<td>“delayed”</td>
</tr>
<tr>
<td>Indicate delayed, centered or advanced moving correlation windows</td>
<td></td>
</tr>
<tr>
<td>To assess the significant stationary periods, indicate the degree of statistical significance from 0 to 100</td>
<td>90</td>
</tr>
<tr>
<td>To validate the model skill, indicate the degree of statistical significance from 0 to 100</td>
<td>90</td>
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</table>
The correlation curve (Fig. 7) presents the SC period clearly divided into two intervals: from 1889 to 1939 and from 1958 up to the present (2015). Consequently, the NSC period corresponds to the remaining years within the study period (1854–2015).

The leading mode (Fig. 8) for the periods SC, NSC and EP explains 52, 28 and 43% of co-variability, respectively. Regarding the SC (Fig. 8; top panels) and NSC (Fig. 8; middle panels) periods, it is observed how a cooling (warming) in the tropical Atlantic is related to a warming (cooling). Thus, the co-variability pattern is defined by opposite sign anomalies between predictor and predictand fields, although the magnitude of the anomalies is greater concerning the SC period. Considering the NSC period (Fig. 8; bottom panels), a signal in tropical Pacific is not observed in response to the tropical Atlantic cooling (warming).

Previous results are in agreement with former studies in which a similar tropical SST pattern with opposite temperature anomalies in the equatorial Atlantic and Pacific in summer has been documented to occur in the decades within the SC period (Rodríguez-Fonseca et al., 2009; Martín-Rey et al., 2012). Thus, Martín-Rey et al. (2014, 2015) point to a non-stationary relationship that seems to take place in the early 20th century and after the 1970s, confirming the correct determination of the leading co-variability mode by the model.

The mechanism, from which the teleconnection takes place, has been explained by Polo et al. (2015), who suggest that a cooling in the equatorial Atlantic results in enhanced equatorial convection, altering the Walker circulation and consequently enhancing subsidence and surface wind divergence over the equatorial Pacific during the period JASO. The anomalous wind piles up water in the western tropical Pacific, triggering a Kelvin wave eastward from autumn to winter, setting up the conditions for a cold event in the equatorial east Pacific during the period DJFM. Considering a cooling in the tropical Atlantic, the opposite sequence takes place.

The skill of the model in reproducing tropical Pacific SSTAs (Fig. 9) is also restricted to stationary conditions. Thus, depending on the considered sequence of decades within the period EP (Fig. 9; middle panels), the model provides better results for period SC (Fig. 9; top panels), while it is not able to produce reliable estimations when period NSC (Fig. 9; bottom panels) is taken into account. These results highlight the need to consider different periods and possible modulations when tackling seasonal predictability of tropical Pacific SSTAs, in agreement with recent results of Martin del Rey et al. (2015).

5 Discussion and conclusions

It is well known how dynamical models need to be to produce very accurate seasonal climate forecast for non-ENSO events, partly due to the presence of strong biases in some regions, such as the tropical Atlantic (Barnston et al., 2015). In contrast, statistical models, despite being a useful and effective supplement, are mostly unable to reproduce the nonlinearity in the ocean–atmosphere system, exceptions include neural networks and Bayesian methods. Attempts to implement new statistical models constitute a fundamental contribution aimed to enhance and complement the dynamical models. Nevertheless, statistical models have evolved linked to dynamical models, either as an alternative or within them as a hybrid model.

Following this reasoning, this paper introduces the $S^4$CAST v2.0 model. The model was created from the first version ($S^4$CAST v1.0) developed as the main part of a cooperation project between the Laboratoire de Physique de l’Atmosphère et de l’Océan Siméon Fongang of the University Cheik Anta Diop (UCAD) in Dakar (Senegal) and the Complutense University of Madrid (UCM) within the VIII UCM Call for Cooperation and Development projects (VR: 101/11) and was named “Creation and Donation of a statistical seasonal forecast model for West African rainfall”.

Thereby, the authors wanted to respect the number of the donation version despite not having a publication. As a brief explanation on the history, the original model was restricted to study the predictability of West African rainfall from tropical global SSTAs using much more limited input parameters that those described in this work for version 2.0. Thus, the reason for developing and improve the model for publication is the motivation arising from colleagues in different institutions along Africa and Europe to expand the model and use it as an alternative tool to look for SST-related predictability due to the strong SST bias that coupled dynamical models exhibit nowadays.

The model is based on the predictive power of the SST. Concerning the association along time between SSTAs and

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**Figure 7.** Shown are 21-year moving correlation windows (green line) between the expansion coefficients $U$ corresponding to tropical Atlantic SSTAs (predictor, blue bars) and $V$ corresponding to tropical Pacific SSTAs (predictand, red line) obtained for the leading mode of co-variability from MCA analysis between predictor and predictand fields. Shaded triangles indicate significant correlation under a Monte Carlo Test at 90%.

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any climate-related variable susceptible of being predicted from it, the concept of stationarity is raised as one of the motivating factors in creating the $S^4$CAST model. The stationarity refers to changes in the co-variability patterns between the predictor and the predictand fields along a given sequence of decades, so that it can be kept invariant (stationary) or changing (non-stationary). This concept has been addressed by different authors (Janicot et al., 1996; Fontaine et al., 1998; Rodríguez-Fonseca et al., 2009, 2011; Mohino et al., 2011; Martín-Rey et al., 2012; Losada et al., 2012) and becomes the main novelty and contribution introduced by $S^4$CAST as a key factor to consider in seasonal forecasting provided by current prediction models, either dynamical or statistical. Thus, $S^4$CAST model is an alternative to enhance and complement the estimates made by dynamical models, which have a number of systematic errors to adequately reproduce the tropical climate variability (Biasutti et al., 2006; Richter and Xie, 2008; Wahl et al., 2011; Doi et al., 2012; Richter et al., 2012; Bellenger et al., 2013; Brown et al., 2013; Li and Xie, 2013; Toniazzo and Woolnough, 2013; Vannière et al., 2013; Xue et al., 2013). For the time being, the $S^4$CAST model cannot be applied for strict operational forecasts, although its application in determining stationary relationships between two fields and their co-variability patterns can be crucial for improving the estimates provided by the operating prediction models currently used.

The model is proposed for use in two areas: the study of seasonal predictability and the study of teleconnections, both based on the influence of SST. On the one hand, we refer to predictability when predictor is considered from a lead time equal to 0 months (medium-range forecast) in advance (long-range forecast). On the other hand, we speak about the study of teleconnections when predictor seasonal selection partially or totally overlaps (synchronous) the forecast period, meaning that one cannot speak about lead time, instead we speak about a monthly lag between the last month in the forecast period and the last month comprising the predictor monthly period.

In addition to previous considerations, the model always provides the predictions in hindcast mode for the different periods of stationarity (SC, NSC and EP), while the forecast mode depends on input parameters and data files used for predictor and predictand fields. For instance, considering from SON as the forecast period concerning the predictand and selecting a lead time of 2 months for the prediction, which means taking the predictor 2 months before September (from AMJ), the prediction for SON 2015 will be performed if the predictand field is available at least until November 2014 and the predictor is available at least until

![Figure 8](https://example.com/figure8.png)

Figure 8. Regression maps obtained for the leading mode by applying MCA between SSTA in the tropical Atlantic (predictor) and SSTA in the tropical Pacific (predictand). Left column represents the homogeneous regression map done by projecting the expansion coefficient $U$ onto global SSTA ($^\circ$C) for predictor seasonal period. Right column represents the heterogeneous regression map done by projecting expansion coefficient $U$ onto global SSTA ($^\circ$C) for predictand seasonal period. Period SC (top panels), EP (middle panels) and NSC (bottom panels). Rectangles show the selected regions for predictor and predictand fields considered in the MCA analysis. Values are plotted in regions where statistical significance under a Monte Carlo test is higher than 90%.
June 2015. Thus, the model constructs the regression coefficient by using the common period until November 2014. Regression coefficients along with predictor data (AMJ 2015) will provide the forecast for SON 2015. In this way, the model first checks data availability related to the input parameters and shows by screen if future forecast is enabled. If enabled, the model performs three types of forecast by computing the regression coefficient for each period (SC, NSC, EP). Finally, the user should determine the better forecast by a study of the modulations of each stationary period and the sequence of hindcasts immediately preceding the present.

In the applications shown in this paper, we have focused in the results from MCA. This statistical methodology, along with canonical correlation analysis (CCA), have been widely used on studies of predictability during the last decades (Barnston and Ropelewski, 1992; Bretherton et al., 1992; Wallace et al., 1992; Barnston and Smith, 1996; Fontaine et al., 1999; Korecha and Barnston, 2007; Barnston and Tippett, 2014; Recalde-Coronel et al., 2014). Integration of the methodology and intuitive use through a user interface are some of the main advantages of the S4CAST model, allowing the selection of a big number of inputs. Future releases of the model will include other methodologies that are currently being introduced and tested.

Originally, the model was created to tackle the study of the predictability of anomalous rainfall associated with WAM, which co-varies in a different way with the tropical band of Atlantic and Pacific ocean basins, being an indicator of non-stationarity (Losada et al., 2012). The transition between SC and NSC periods, around the 1970s, has served as the starting point of many studies focusing on the influence of global SSTA before and after that period (Mohino et al., 2011; Rodríguez-Fonseca et al., 2011, 2015; Losada et al., 2012) while being one of the motivations to create S4CAST.

The choice of the case study related to Sahelian rainfall predictability is motivated by the following reasons: on the one hand, SST in the tropical Atlantic is well known to strongly influence the dynamics of the ITCZ (Fontaine et al., 1998) which in turn determines the subsequent WAM. Nevertheless, dynamical models do not reproduce the influence of SST on the ITCZ (Lin, 2007; Richter and Xie, 2008; Doi et al., 2012; Toniazzo and Woolnough, 2013) becoming the statistical prediction an alternative way to predict WAM variability. The second reason is related to the non-stationary influence of the tropical Atlantic on Sahelian rainfall reported in some studies (Janicot et al., 1996, 1998; Ward, 1998; Rodríguez-Fonseca et al., 2011; Mohino et al., 2011; Losada et al., 2012).

The second case study has served as a benchmark to certify the ability of the S4CAST model in the study of SSTA predictability by the corroboration of the equatorial Atlantic variability as predictor of ENSO. This is a recently discov-
considered relationship (Rodríguez-Fonseca et al., 2009; Ding et al., 2012; Polo et al., 2015) that has been found to be non-stationary (Martín del Rey et al., 2014, 2015).

The application of moving correlation windows between expansion coefficients obtained from MCA analysis results in three periods of stationarity depending on the statistically significant correlation: entire period (EP), significant correlation period (SC) and no-significant correlation period (NSC). For the case in which non-stationarity is considered, we refer to EP period, assuming changes in co-variability patterns. Stationarity is referred to SC and NSC periods. These periods may slightly vary depending on the type of moving correlation windows: advanced, centered or delayed. Stationary analysis to determine the three different work periods (SC, NSC, EP) is limited to the selection of a single mode of co-variability. When selecting a set of modes, the stationarity analysis is not applied so that simulations are only developed for EP period, whereby the whole time series is considered for both the predictor and predictand fields.

Three conditions may enhance the degree of confidence in a given predictor. The first has to do with the selection of moving correlation windows (see Sect. 3.1.2) used to determine the working scenarios (SC, NSC, EP). Delayed moving correlation windows can help in this task. Thus, if correlation coefficients between the expansion coefficients \( U \) and \( V \) exhibit significant values for the present year and the previous 21 study years, greater confidence is assumed for the predictor. The second condition is determined by the value of the expansion coefficient \( U \) for the current year so that the higher its value, the better the forecast. The last condition has to do with the percentage of variance explained by the selected co-variability mode, the higher its value, the better the forecast. Nevertheless, despite previous conditions, the influence of other remote and nearby oceanic predictors must be considered in order to provide a full and reliable predictability study.

So far, the data files used as predictor and predictand fields correspond to observations and reanalysis from several institutions. The use of new data files is simple and can be performed according to user needs. The upgrade of data files from respective websites must be checked periodically to strengthen the results. In addition, it is also advisable to launch the same simulations using different data files in order to compare the results and assess the robustness of the forecast. The results shown in this work for different selections have been verified by following these criteria.

The results obtained by using the S⁴CAST model put forward the consideration of non-stationarity in the co-variability patterns and therefore in climatic teleconnections. Thus, it is important to determine the multidecadal modulator of the interannual variability in order to know which predictor is the one affecting in particular periods and regions (Rodríguez-Fonseca et al., 2015).

Code availability

The model consists of a software package organized in folders containing libraries, functions and scripts developed as a MATLAB® toolbox from version R2010b onwards. Two of the folders, named as mexcdf and netcdf_toolbox, correspond to libraries needed for working with NetCDF files and have been downloaded from www.mexcdf.sourceforge.net and built into the model. The file containing the model core with the executable code is named S⁴core. Once the toolbox has been added to the MATLAB® path and by simply typing “S⁴cast” in the command window, the user is prompted to enter a number of input parameters required to launch a simulation. The software package S⁴plot dedicated to plot figures has been added so that the user can use this software by typing “figures” in the command window. Note that figures presented in this work have been further improved manually. The code is open access and can be downloaded from the Zenodo repository (doi:10.5281/zenodo.15985) in the URL https://zenodo.org/record/15985. To facilitate the execution of the model leading to the results shown in this paper, used data files that have been previously defined in Sect. 4, are included in the directories /S⁴CAST_v2.0/data_files/predictand and /S⁴CAST_v2.0/data_files/predictor. The second case study requires NOAA ERSST as predictor and predictand. The code has been thoroughly analyzed by using several data files and input parameters. However, the emergence of software bugs is not ruled out, being mostly associated with problems to adapt and use NetCDF files. To solve these hypothetical code bugs, please do not hesitate to contact authors.

The Supplement related to this article is available online at doi:10.5194/gmd-8-3639-2015-supplement.

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Edited by: M.-H. Lo
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Recalde-Coronel, G. C., Barnston, A. G., and Muñoz, Á. G.: Predictability of December–April rainfall in Coastal and An-
