# Modified LCM'S Approximation Algorithm for Solving Transportation Problems 

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#### Abstract

In this paper, Modified LCM's Approximation Algorithm for Solving Transportation Problems has been developed in order to gain foremost fundamental capable solution of transportation issues where entity cut down the transportation expensive. The proposed algorithm is correlate with popular presenting methods corralling NWCM, LCM and improved algorithm and purposed algorithm found that yield to better results. Algorithm is quickest and effective. Few examples are tested by using modified algorithm is correlate with open literature.


Key Words: Transportation problem, Initial Basic Feasible Solution, Optimal Solution
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## 1. Introduction

Transportation problem is extremely important of linear programming issues in the area of applied mathematics and also in operation research of linear programming and also compulsory mathematical tool that cope with the use of limited resources. The type of linear programming problems which may be resolved by applying a classified version of the easier procedure which can be called as transportation issues.

Balanced Transportation in which demand and supply are equal where as demand and supply are different in unbalance transportation problem. The main purpose of transportation problem is to minimize the transportation cost. To reach the feasible and the optimal solution of transportation problems.

The transportation was introduced in 1941 by Hitchcock in order to distribute of production of several numerous localities. In 1947, T.C. Koopmans presented a study called 'Optimum Utilization of the Transportation System'. These two contributions are the fundamentals for the progress of transportation problem. These methods such as LCM, NWCM, IM, VAM and ILCM.

The basic initial solution Methods to solve transportation problems are;
-Northwest Corner Method (NWCM)


to supply or demand by this procedure, continues till we can minimize obtain cost.

## -Least Cost Method (LCM)

In this method we can count low cost in table of transportation by crossing out columns with nothing to supply and demand, we continue this procedure till we can obtain minimize cost.

## - Improved Algorithm (IM)

To sum up $1^{\text {st }}$ about penalty by taking difference between lower to next lower cost. Taking difference between the largest and smallest in column and in row. This procedure is continued till get optimal result

Let $X_{n k} \geq 0$ be the quantity shipped from the inception " $n$ " to the emplacement " $K$ ". The mathematical formulation of the problem is given below.

Minimize $\quad Z-\sum_{n=1}^{0} \sum_{k=1}^{0} m_{n k} x_{n k}$ (Total Transportation cost)
Subject to $\sum_{k=1}^{0} x_{n k}=q n$ (Supply from inception)

$$
\begin{gathered}
\sum_{n=1}^{0} x_{n k}=\operatorname{sk} \text { (Demand from implocement) } \\
X_{n k}>0, \text { for all. } n \text { and } k
\end{gathered}
$$

Where Z: Total transportation cost to be reduced
$\mathrm{C}_{\mathrm{nk}}$ : Unit transportation cost of the commodity from each inception n to emplacement k
$\mathrm{X}_{\mathrm{nk}}$ : Number of units of commodity sent from each inception n to emplacement k .
$\mathrm{Q}_{\mathrm{n}}$ : level of supply at each inception n .
$\mathrm{S}_{\mathrm{k}}$ : level of demand at each emplacement k .
Note: Transportation model is balanced if supply $\left(\sum_{n=1}^{0} q n\right)=\operatorname{Demand}\left(\sum_{n=1}^{o} \mathrm{Sk}\right)$
Otherwise unbalanced if supply $\left(\sum_{n=1}^{0} q n\right) \neq \operatorname{Demand}\left(\sum_{n=1}^{\circ} \mathrm{Sk}\right)$.

| Table of the general transportation Problem |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Destinations $\quad$ Origins | $l_{1}$ | $l_{2}$ | ... | $l_{k}$ | ... | $l n$ | Supply:qn |
| $P_{1}$ | $m_{11}$ | $m_{12}$ | ... | $m_{1 k}$ | ... | $m_{1 r}$ | $q_{1}$ |
| $P_{2}$ | $m_{21}$ | $m_{22}$ | ... | $m_{2 k}$ | $\cdots$ | $m_{2 r}$ | $q_{2}$ |
| ! | ! | : | : | : | : | : | : |
| $P_{n}$ | $m_{n 1}$ | $m_{n 2}$ | ... | $m_{n k}$ | ... | $m_{n r}$ | $q_{n}$ |
| : | : | : | : | : | $\vdots$ | : | : |
| $P_{o}$ | $m_{61}$ | $m_{02}$ | $\cdots$ | $m_{o k}$ | $\cdots$ | $m_{o r}$ | 90 |
| Demand: $p_{k}$ | $p_{1}$ | $p_{2}$ | $\cdots$ | $p_{k}$ | $\cdots$ | $p_{r}$ | $\sum_{n=1}^{0} q_{n}=\sum_{k=1}^{0} S_{k}$ |

The total number of variables is O.R. The total number of constraints is $(\mathrm{o}+\mathrm{r})$ while the total number of locations ( $\mathrm{o}+\mathrm{r}-1$ ) should be in feasible solution. Here the letter indicates the number of rows and indicate the number of columns.
2. Methodology

| $\mathrm{c}_{11}$ | $\mathrm{c}_{12}$ | $\mathrm{c}_{13}$ | $\ldots$ | $\mathrm{c}_{1 \mathrm{n}}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{c}_{21}$ | $\mathrm{c}_{22}$ | $\mathrm{c}_{23}$ | $\ldots$ | $\mathrm{c}_{2 \mathrm{n}}$ |
| $\mathrm{c}_{31}$ | $\mathrm{c}_{32}$ | $\mathrm{c}_{33}$ | $\ldots$ | $\mathrm{c}_{3 \mathrm{n}}$ |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| $\mathrm{c}_{\mathrm{m} 1}$ | $\mathrm{c}_{\mathrm{m} 2}$ | $\mathrm{c}_{\mathrm{m} 3}$ | $\ldots$ | $\mathrm{c}_{\mathrm{mn}}$ |
|  |  |  |  |  |

$C_{i j}$ are the cost cells where $i=1,2,3 \ldots, n$ and $j=1,2,3, m$. they are following steps

1) Transportation problem ought to be $\sum_{n=1}^{0} q n-\sum_{n=1}^{o} S_{k}$, In case it is not $\sum_{i n=1}^{0} q n+\sum_{n=1}^{o} S_{k}$ a dummy variable needs to be added in order to balance it.
2) Select large number from each columns of each cells and subtract that number from each entry of that cell Suppose $c_{31}$ is large number in $\mathrm{C}_{11}\left|c_{31}-c_{21}\right|,\left|c_{31}-c_{11}\right| \ldots$
3) Allocate largest absolute number of each column corresponding column with respect to supply and demand.
4) If there are similar in column $\left(m_{1}=m_{2}=m_{n}\right)$ then the minimum cell has to selected from the ginen cells finally there to be applied $S_{k}$ and $q_{n}$.
5) If $S_{k}$ and $q n$ of the current row are completed we shall move towards the next row repeat step 1-4 till all quantities are exhausted.

## 3. NUMERICAL ILLUSTRATION

In this paper, esteem four dissimilar size cost minimizing transportation problems, chosen form literature. We also describe these examples to perform a comparative study of proposed algorithm with north and west corner and least cost methods. We solve example 1 step-by-step continuous.

## Example No: 1

| Destination source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | Supply |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{S}_{1}$ | 6 | 4 | 1 | 50 |
| $\mathrm{~S}_{2}$ | 3 | 8 | 7 | 40 |
| $\mathrm{~S}_{3}$ | 4 | 4 | 2 | 60 |
| Demand | 20 | 95 | 35 | $\sum 150$ |

Step 1: Count on the different column by receiving large number from each columns of each cells and subtract from each entry of that cell of each columns Table 2.1.

| Destination source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | D 3 | Supply |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{S}_{1}$ | 6 | 4 | 1 | $50-35=15$ |
| $\mathrm{~S}_{2}$ | 3 | 8 | 7 | 40 |
| $\mathrm{~S}_{3}$ | 4 | 4 | 2 | 60 |
| Demand | 20 | 95 | $35-35=0$ | $\sum 115$ |

Table 2.1
Step 2: Using table 2.1 Taking largest absolute number in columns
$X_{11}=\max (6,3,4)=0, X_{12}=\max (4,8,4)=4, X_{13}=\max (1,7,2)=6$ Here 6 is largest absolute number and allocated largest absolute number of each row corresponding with respect to supply and demand then remove $D_{3}$ column due to its zero demand

| Destination source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | Supply |
| :--- | :--- | :--- | :--- |
| $\mathrm{S}_{1}$ | 6 | 4 | $15-15=0$ |
| $\mathrm{~S}_{2}$ | 3 | 8 | 40 |
| $\mathrm{~S}_{3}$ | 4 | 4 | 60 |
| Demand | 20 | $95-15=80$ | $\sum 100$ |

Table 2.2
Step3: Using table 2.2 Taking largest absolute number in columns
$\mathrm{X}_{11}=\max (6,3,4)=0, \mathrm{X}_{12}=\max (4,8,4)=4$
4 is largest absolute number in column $S_{1}$ is 4 allocated supply and demand $S_{1}$ is detected because its supply is zero.

| Destination source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | Supply |
| :--- | :--- | :--- | :--- |
| $\mathrm{S}_{2}$ | 3 | 8 | $40-20=20$ |
| $\mathrm{~S}_{3}$ | 4 | 4 | 60 |
| Demand | $20-20=0$ | 80 | $\sum 80$ |

Table 2.3
Step 4: Using table 2.3 Taking largest absolute number in columns
$\mathrm{X}_{21}=\max (3,4)=1, \mathrm{X}_{22}=\max (8,4)=0$
1 is largest absolute number then detect
$D_{1}$ column because its supply is zero

| Destination source | $\mathrm{D}_{2}$ | Supply |
| :--- | :--- | :--- |
| $\mathrm{S}_{2}$ | 8 | $20-20=0$ |
| $\mathrm{~S}_{3}$ | 4 | 60 |
| Demand | $80-20=60$ | $\sum 60$ |

Table 2.4

Step 5: Using table 2.4 Taking largest absolute number in column $X_{22}=\max \{8,4\}=8$ so here 8 is largest absolute number in row $\mathrm{S}_{3}$ is detected because supply is zero

| Destination source | $\mathrm{D}_{2}$ | Supply |
| :--- | :--- | :--- |
| $\mathrm{S}_{3}$ | 4 | $60-60$ |
| Demand | $60-60$ | $\sum 0$ |

Table 2.5
In last, we have allocated demand and supply and then detect the exclusive matrix due to nothing to supply and demand.

Steps 6: applying table 1 all allocates hints for gaining minimized cost.

| Destination source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | Supply |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{S}_{1}$ | 6 | 4 | 1 | 50 |
| $\mathrm{~S}_{2}$ | 3 | 8 | 7 | 40 |
| $\mathrm{~S}_{3}$ | 4 | 4 | 2 | 60 |
| Demand | 20 | 95 | 35 | $\sum 150$ |

$$
Z=1 \times 35+4 \times 15+3 \times 20+4 \times 60=35+60+60+160+240=555
$$

## 4. Optimality Test of Example 1

Taking initial basic feasible solution due to proposed method, we now proceed for optimality using modified Distribution methods here calculate $u_{i}$ and $v_{j}$ for occupied basic cell using $u_{i}+v_{j}=c_{i j}$

Initial we take $u_{1}=0$
$\mathrm{C}_{12}=41+\mathrm{v}_{2}=4=>\mathrm{V}_{2}=4$
$C_{13}=41+v_{3}=1 \Rightarrow 0+v_{3}=1=>v_{3}=1$
$\mathrm{C}_{21}=\mathrm{u}_{2}+\mathrm{v}_{1}=3=>4+\mathrm{v}_{1}=3 \Rightarrow \mathrm{v}_{1}=-1$
$\mathrm{C}_{22}=\mathrm{u}_{2}+\mathrm{v}_{2}=8 \Rightarrow \mathrm{u}_{2}+4=8 \Rightarrow \mathrm{u}_{2}=4$
$C_{32}=u_{3}+v_{2}=4=>u_{3}+4=>u_{3}=0$

| Destination Source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | Supply | Ui |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{S}_{1}$ | 6 | $4_{15}$ | 135 | 50 | $4_{1}=0$ |
| $\mathrm{S}_{2}$ | 320 | 820 | 7 | 40 | $4_{2}=4$ |
| $\mathrm{S}_{3}$ | 4 | 4 | 2 | 60 | $4{ }_{3}=0$ |
| Demand | 20 | 95 | 35 | $\sum 150$ |  |
| $\mathrm{V}_{\mathrm{j}}$ | $\mathrm{V}_{\mathrm{i}}=1$ | $\mathrm{V}_{2}=4$ | $\mathrm{V}_{3}=1$ |  |  |

$\mathrm{D}_{11}=\mathrm{c}_{11}-\left(\mathrm{U}_{1}+\mathrm{U}_{2}\right)=6-(0+1)=6-1=5$
$D_{23}=C_{23}-\left(U_{2}+V_{3}\right)=7-(4+1)=7-5=2$
$\mathrm{D}_{31}=\mathrm{C}_{31}-\left(\mathrm{u}_{3}+\mathrm{v}_{1}\right)=4-(0+1)=4-1=3$
$\mathrm{D}_{11}=\mathrm{C}_{33}-\left(\mathrm{u}_{3}+\mathrm{V}_{3}\right)=2-(0+1)=2-1=1$
$\mathrm{D}_{11}=5, \mathrm{D}_{23}=2, \mathrm{D}_{31}=3, \mathrm{D}_{33}=1$
Check the all unoccupied cell single

| Destination Source | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | Supply |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{S}_{1}$ | 65 | 415 | 135 | 50 | $4_{1}=0$ |
| $\mathrm{S}_{2}$ | 320 | 820 | 72 | 40 | $4_{2}=4$ |
| $\mathrm{S}_{3}$ | 43 | 460 | 21 | 60 | $4_{3}=0$ |
| Demand | 20 | 95 | 35 | $\sum 150$ |  |
| $\mathrm{V}_{\mathrm{j}}$ | $\mathrm{V}_{1}=1$ | $\mathrm{V}_{2}=4$ | $\mathrm{V}_{3}=1$ |  |  |

All unoccupied Single are $\mathrm{D} \geq 0$ then optimal Solution is
$\mathrm{Z}=4 * 5+1 * 35+3 * 20+8 * 20+4 * 60=555$ Answer.

The same process is adopted on various examples given below.

| Example-2 | Destination Source | D1 | D2 |  | D3 | Supply | Optimal Solution |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | S1 | 6 | 8 |  | 4 | 14 |  |
|  | S2 | 4 | 9 |  | 8 | 12 | 143 |
|  | S3 | 1 | 2 |  | 6 | 5 |  |
|  | Demand | 5 | 10 |  | 15 | $\Sigma^{31}$ |  |
| Example-3 | Destination Source | D1 | D2 | D3 | D4 | D5 Supply | Optimal Solution |
|  | S1 | 4 | 1 | 2 | 4 | $4 \quad 60$ | 273 |
|  | S2 | 2 | 3 | 2 | 2 | 235 |  |
|  | S3 | 3 | 5 | 2 | 4 | 440 |  |
|  | Demand | 22 | 45 | 20 | 18 | $30 \quad \Sigma^{135}$ |  |
| Example 4 | Destination Source | D1 | D2 | D3 | D4 | Supply | Optimal Solution |
|  | S1 | 7 | 5 | 9 | 11 | 30 | 430 |
|  | S2 | 4 | 3 | 8 | 6 | 25 |  |
|  | S3 | $3$ | 8 | 10 | $5$ | $20$ |  |
|  | S4 | $2$ | $6$ | 7 | $3$ | $15$ |  |
|  | Demand | 30 | 30 | 20 | 10 | $\Sigma^{90}$ |  |
| $\underset{5}{\text { Example }} \text { - }$ | Destination Source | D1 | D2 | D3 | D4 | Supply | Optimal Solution |
|  | S1 | 3 | 1 | 7 | 4 | 300 | 2850 |
|  | S2 | 2 | 6 | 5 | 9 | 400 |  |
|  | S3 | 8 | 3 | 3 | 2 | 500 |  |
|  | Demand | 250 | 350 | 400 | 200 | $\Sigma^{1200}$ |  |

## 5. RESULTS AND DISUCSSION

It has been examined that the performance of proposed Algorithm in comparison to LCM, NWCM and Improved Algorithm by examining five examples the result gained using proposed algorithm in examples 1, 2, 3and 5 was same as the optimal outcome., While in example 4 it is close to the optimal solution. It could be clearly seen that the proposed algorithm gave reliable results which was against with the flourishing methods- NWCM, LCM and Improved Algorithm.

| No. of <br> Example | Type of <br> problem | Result of <br> NWCM | Result of <br> LCM | Result of <br> IM | Result of proposed <br> Methods | Optimal <br> Solution |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Example-1 | $3 * 3$ | 730 | 555 | 555 | 555 | 555 |
| Example-2 | $3 * 3$ | 228 | 163 | 144 | 143 | 143 |
| Example-3 | $3 * 5$ | 363 | 278 | 273 | 273 | 273 |
| Example-4 | $4 * 4$ | 540 | 435 | 415 | 430 | 410 |
| Example-5 | $3 * 4$ | 4400 | 2900 | 2850 | 2850 | 2850 |

## 6. CONCLUSION

In this paper, for achieving fundamental capable solution of transportation issues, Modified LCM'S approximation Algorithm has been developed. The proposed algorithm has been looked over for optimality. A comparison of proposed algorithm has been made with Least Cost Method, North West Corner Method and An Improved Algorithm by examining 5 numerical examples. It is examined that the proposed algorithm has succumbed capable of outcome which were opposite to the conventional methods.

## REFERENCES:

[1] M.S.R.Shaikh , S.F.Shah , Z. Memon (2018), An improved algorithm to solve transportation problems for optimal solution , mathematical theory and modelling (IISTE), vol.8(08)PP.01-08
[2] PalanivelM,Suganya M (2018) A new method to solve transportation problem-Harmonic mean approach.Journal of Engineering Technology,Vol.02(03), pp.001-003
[3] Eghbal Hosseini., (2017) "Three New Methods to find Initial Basic Feasible solution of Transportation problems ", Applied Mathematical Science, vol. 11(37), 1803-184
[4] Shraddha Mishra, (2017) "Solving Transportation problem by various methods and their comparison", International Journal of Mathematics trends and technology (IJMT)-VOL. 44 (4), 2231-5373
[5] MdsharifUddin ; ChowdhuryGolam.K, A.R khan, I.Raeva (2016) Improved least cost method to obtain a better IBFS to the transportation problem, Journal of Applied mathematics and Bioinformatics, Vol.6(02), pp.01-20
[6] A.S.Soomro.,Md. Junaid, G.A.Tularam. , (2015) Modified vogel's approximation method for solving transportation problems. Journal of mathematical Theory andmodelling, Vol 05(04), pp.32-43.
[7] M.M. Ahmed., M. Aslam, M. Katun, M.S. Uddin., (2015), "New procedure of Finding an Initial Basic Feasible Solution of the time Minimizing Transportation Problems", Open Journal of Applied Science, 5, 634-640
[8] U. K. Das., M. A. Babu., A.R. Khan., M. A. Helal and M. S. Uddin., (2014). "Logical Development of Vogel's Approximation Methods (LD-VAM): An Approach to find Basic feasible of transportation problem", International Journal of Scientifics And technology Research (IJSTR), 3(2), 42-48
[9] M.A Babu, M.A.Helal, U K das, (2013) A new approach to obtain feasible solution of Transportation model , journal ofScientific and Engineering research, Vol.4(11). pp.1344-1348
[10] Pandian, G.Natarajan (2010) A new approach for solving the transportation problem and with mixed constraints., Journal of Physical sciences, Vol.14, pp.53-61

