

1 **Examining Biases in Diurnally-Integrated Shortwave Irradiances due to Two-**
2 **and Four-Stream Approximations in Cloudy Atmosphere**

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Abstract

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Shortwave irradiance biases due to two- and four-stream approximations have been studied for the last couple of decades, but biases in estimating Earth’s radiation budget have not been examined in earlier studies. In order to quantify biases in diurnally-averaged irradiances, we integrate the two- and four-stream biases using realistic diurnal variations of cloud properties from Clouds and the Earth’s Radiant Energy System (CERES) synoptic (SYN) hourly product. Three approximations are examined in this study, delta-two-stream-Eddington (D2strEdd), delta-two-stream-quadrature (D2strQuad), and delta-four-stream-quadrature (D4strQuad). Irradiances computed by the Discrete Ordinates Radiative Transfer (DISORT) and Monte Carlo (MC) methods are used as references. The MC noises are further examined by comparing with DISORT results. When the biases are integrated with a one-day of solar zenith angle variation, regional biases of D2strEdd and D2strQuad reach up to 8 W m^{-2} , while biases of D4strQuad reach up to 2 W m^{-2} . When the biases are further averaged monthly or annually, regional biases of D2strEdd and D2strQuad can reach -1.5 W m^{-2} in SW top-of-atmosphere (TOA) upward irradiances and $+3 \text{ W m}^{-2}$ in surface downward irradiances. In contrast, regional biases of D4strQuad are within $+0.9$ for TOA irradiances and -1.2 W m^{-2} for surface irradiances. Except for polar regions, monthly and annual global mean biases are similar, suggesting that the biases are nearly independent to season. Biases in SW heating rate profiles are up to -0.008 Kd^{-1} for D2strEdd and -0.016 K d^{-1} for D2strQuad, while the biases of the D4strQuad method are negligible.

48 **1. Introduction**

49 The integro-differential radiative transfer equation cannot be analytically solved unless a
50 simplifying assumption is made because the radiance leaving to a certain direction is contributed
51 by the multiple scattering components from all directions. To obtain a solution, scattered
52 radiances in the source function are approximated at a limited number of discretized angular
53 directions. The number of angular points is often called the number of streams in the radiation
54 scheme. Even though a higher number of streams gives a better accuracy, the simplified radiation
55 codes such as two- or four-stream approximations (Liou 1974; Joseph et al. 1976; Meador and
56 Weaver 1980; Liou et al. 1988; Chou et al. 1998) have been widely used for reanalysis and
57 general circulation models (GCMs), as well as in the production of radiation budget data,
58 because of efficient computing time (Räisänen 2002; Zhu and Arking 2006; Li et al. 2013).

59 For the last couple of decades, many studies have investigated the accuracy of two- and four-
60 stream approximations in shortwave (SW) irradiance computations (e.g., Meador and Weaver
61 1980; King and Harshvardhan 1986; Shibata and Uchiyama 1992; Barker et al. 2003; Halthore et
62 al. 2005; Lu et al. 2009; Hou et al. 2010; Zhang and Li 2013). They performed sensitivity studies
63 with assumed cloud optical depths and solar zenith angles for examining two- and four-stream
64 biases.

65 The aforementioned findings are valuable, but it is not clear how the two- and four-stream
66 biases influence the estimation of Earth's radiation budget, and if so, how large the magnitude of
67 biases would be. A few studies tried to answer this question. Zhu and Arking (1994) estimated
68 diurnally-integrated biases of the delta-two-stream and four-stream approximations, as functions
69 of latitude and cloud optical depth. However, it is not straightforward to infer the two- and four-
70 stream biases with the realistic variations of the cloud optical depths from their results. In

71 addition, Barker et al. (2015) examined two-stream biases in SW broadband irradiances with
72 clouds derived from A-train space-borne radar and lidar measurements. However, they did not
73 consider diurnal variations of solar zenith angles because A-train satellites only observe a fixed
74 location twice a day. It is expected that the two- and four-stream biases are partly canceled out
75 over the course of a day because the sign of two- and four-stream biases usually changes at a
76 certain solar zenith angle. Even though a smaller magnitude is expected, estimating diurnally-
77 integrated biases is needed to understand the impact of two- and four-stream biases on radiation
78 budget.

79 Therefore, in this study, we use cloud fields from hourly satellite products to estimate two-
80 and four-stream biases in diurnally-integrated SW irradiances. We expect that the magnitudes
81 and signs of two- and four-stream biases are affected by cloud types, generating variations of
82 biases depending on the region. Therefore, our objective is to provide the global distribution of
83 two- and four-stream biases with realistic cloud fields. As a reference, we consider Discrete
84 Ordinates Radiative Transfer (DISORT) and Monte Carlo (MC) methods. Based upon the
85 references, two- and four-stream biases are estimated for each hourly 1° grid box, and then they
86 are averaged monthly or annually. We obtain absolute biases of SW irradiances (W m^{-2}) instead
87 of relative biases (%) to make it easier to assess the impact on Earth's radiation budget.

88

89 **2. Methodology**

90 **2.1. Radiative transfer models**

91 To compute SW irradiances with two- and four-stream approximations, we use the modified
92 version of the Fu-Liou model (Fu and Liou 1993; Fu et al. 1997) by National Aeronautics and
93 Space Administration (NASA) Langley Research Center; i.e. a flux model of Clouds and the

94 Earth's Radiant Energy System (CERES) with k-distribution and correlated-k for Radiation
95 (FLCKKR) (Kratz and Rose 1999; Kato et al. 1999, 2005; Rose et al. 2006). We run the Fu-Liou
96 model in three modes; i) delta-two-stream-Eddington (D2strEdd) (Irvine 1968; Kawata and
97 Irvine 1970; Shettle and Weinman 1970), ii) delta-two-stream-quadrature (D2strQuad) (Liou
98 1992), and iii) delta-four-stream-quadrature (D4strQuad) (Liou et al. 1988; Fu 1991) methods.
99 These three approximations are widely used in the current climate and numerical models, and
100 comprehensive descriptions are provided in earlier studies (e.g., Liou 1974, 1992; Meador and
101 Weaver 1980; Toon et al. 1989). The D2strEdd method assumes $I(\mu, \tau) = I_0(\tau) + \mu I_1(\tau)$, stating that
102 the radiance is expressed by a polynomial of μ along with the zeroth (I_0) and first (I_1) Legendre
103 polynomial moments of the radiance. In the D2strQuad method, the angular integral of the
104 radiance is expressed using the two-point Gaussian quadrature, while the four-point Gaussian
105 quadrature is used for the D4strQuad method. In all D2strEdd, D2strQuad, and D4strQuad
106 methods, a strong forward peak of the phase function is approximated by Dirac delta function (δ
107 function), based on the delta-M scaling method (Wiscombe 1977). Earlier results indicate that
108 the D4strQuad method generally performs better than most two-stream approximation methods
109 (e.g., Zhu and Arking 1994).

110 As a reference to estimate biases of the D2strEdd, D2strQuad, and D4strQuad
111 approximations, we consider the Discrete Ordinates Radiative Transfer (DISORT) model
112 (Stamnes et al. 1988). The DISORT method uses the discrete ordinate approximation to express
113 the integral term of the source function with Gaussian quadrature, which is similar to the
114 D2strQuad and D4strQuad method. However, the DISORT model is designed for a higher
115 number of streams than these methods. For the higher number of streams, the scattering phase
116 function is expanded with Legendre polynomials and the radiance is expanded with a Fourier

117 cosine series. Then the matrix form is used to solve the radiative transfer equation. The accuracy
118 of the DISORT model increases with the number of streams, but the results converge once the
119 number of streams is ≥ 16 (Appendix A). Therefore, we use DISORT model results with 40
120 streams to compare with two- and four-stream simulation results.

121 As another reference, we also use the Intercomparison of 3-D Radiation Code (I3RC)
122 (Cahalan et al. 2005) community Monte Carlo model (Pincus and Evans 2009) with the
123 independent column approximation (ICA) assumption. The principle of the MC method is
124 described in earlier studies (e.g., Barker and Davis 1992, Davis et al 1997) and the short
125 description of the method is following. At the beginning of the model run, photons are injected at
126 top of the domain. When photons reach extinction media such as cloud or gas, photons are either
127 absorbed or scattered based on the specified probability of single scattering albedo. When
128 photons are scattered, the direction of the photons is statistically determined using the cumulative
129 distribution function of the scattering phase function. Photons are tracked until completely
130 absorbed or escape from the domain. By counting the number of photons escaping from the top
131 and bottom boundaries of the domain, reflection and transmittance are determined. The number
132 of absorbed photons in atmospheric layers is used to compute heating rate profiles. To run the
133 I3RC model with all cases at one time, we generate many columns in the domain. With the
134 independent column approximation, only the vertical location of photons is tracked, i.e. the
135 information of horizontal location is lost and thus there is no interaction among columns.
136 Therefore, it is equivalent to having many plane-parallel atmospheres in a domain. Note that the
137 number of photons is distributed proportionally to the cosine of solar zenith angle (μ_0), which is
138 also proportional to the solar incoming irradiance. For example, if we consider ten columns with
139 ten different μ_0 as 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, and 1.0 in the domain, the column with

140 $\mu_0 = 1$ gets 10 times larger number of photons compared to the column with $\mu_0 = 0.1$. If we input
141 1000 photons in the domain, the columns mentioned above get 18, 36, 55, 73, 91, 109, 127, 145,
142 164, and 182 photons, respectively, and their average is 100 photons per column. In other words,
143 the columns with $\mu_0 = 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9,$ and 1.0 get 0.18, 0.36, 0.55 0.73,
144 0.91, 1.09, 1.27, 1.45, 1.64, and 1.82 times the average photons per column, respectively.
145 Throughout this study, when we refer to the number of photons for the MC simulation, we use
146 the average number of photons per column in the domain but a smaller weighting is given to the
147 column with a small μ_0 , and vice versa.

148 Note that the MC takes into account the exact scattering phase functions within the resolution
149 of equal probability bins, and thus the method is equivalent to the results with the infinite
150 number of streams in the model simulation (Barker et al. 2015). This means that as long as
151 enough number of streams is used for the DISORT method and enough number of photons is
152 used for the MC method, the two methods should produce almost identical results. We verify this
153 in Appendix A. For generating the look-up table (LUT) using the MC model in Section 2.2,
154 however, we need to limit the number of photons less than 10^6 due to the long computation time.
155 The expected MC noises with 10^6 photons are up to 1 W m^{-2} (Fig. A1). Because the MC noises
156 are randomly distributed, we will examine if the Monte Carlo noises are canceled out in monthly
157 and annual means by comparing with DISORT results in Section 3.2.

158

159 **2.2. Model inputs**

160 We use common inputs in all radiative transfer methods; D2strEdd, D2strQuad, D4strQuad,
161 MC, and DISORT. Specifically, we consider 18 narrow bands (Rose et al. 2006) for computing
162 gaseous absorption, molecular scattering, cloud scattering, and surface albedo of SW broadband

163 radiation from 0.1754 to 4.0 μm . Aerosol is ignored in this study, and our main focus remains for
164 cloudy atmosphere. The correlated-k distribution method (Kratz and Rose 1999; Kato et al. 1999,
165 2005) is used to compute the gas absorption optical depth, and the molecular scattering optical
166 depth is computed using a pressure profile (Fu and Liou 1993). In this study, midlatitude summer
167 (MLS), and midlatitude winter (MLW) profiles (McClatchey et al. 1972) are considered,
168 depending on the total precipitable water (PW), as explained in Section 2.3.

169 Cloud scattering properties such as single scattering albedo, scattering phase function (or
170 asymmetry factor for two- or four-stream approximations), and extinction efficiency are
171 considered for the 18 bands. The scattering parameters for water particles were computed using
172 Mie theory. In addition, ice particles are assumed to be two habit mixtures (THM) and their
173 optical properties are from Liu et al. (2014).

174 The surface type is assumed to be either ocean, cropland, or snow. The spectral surface
175 albedo for the ocean surface is computed based on Jin et al. (2004), who parameterized the ocean
176 albedo as a function of ocean chlorophyll concentration, near-surface wind speed, atmospheric
177 transmittance, and solar zenith angle. For this study, the wind speed and chlorophyll
178 concentration are fixed at 5 m s^{-1} and 0 mg m^{-3} , respectively. The surface albedo for cropland is
179 fixed at 0.10 for the clear sky, and 0.12 for the cloudy sky. The surface spectral albedo for snow
180 surface is based on Jin et al. (2008) and is a function of snow grain size. The snow grain size =
181 $100 \mu\text{m}$ is assumed.

182 Because of the long computation time of the DISORT and MC models (Table 3), it is
183 practically difficult to run the models with a 1-hour temporal resolution and a 1° spatial
184 resolution for computing monthly and annual means. To improve the computational efficiency of
185 the model simulations in this study, a look-up table (LUT) is made for various combinations of

186 surface, atmospheric, and cloud conditions. These include 3 surface type albedos (ocean, land,
187 and snow), 2 atmospheric profiles (MLS and MLW), and 10 values of the cosine of the solar
188 zenith angle from 0.1 to 1.0 with a 0.1 interval. In addition, for clouds, 9 values of cloud optical
189 depth (0.3, 1, 2, 5, 10, 20, 30, 40, and 50), two cloud phases (ice and liquid), 16 values of the
190 cloud top height from 1 to 16 km with a 1-km interval, and 16 values of the cloud base height
191 from 0 to 15 km with a 1-km interval are included, as listed in Table 1. For ice-phase clouds, an
192 effective diameter (d_e) of 65 μm is used, while a 10 μm of effective radius (r_e) is used for
193 liquid-phase clouds. The pre-computed LUT is used for calculating SW irradiances for surface,
194 atmosphere, and cloud conditions obtained from the CERES synoptic (SYN) product (Section
195 2.3).

196 Because the consistent spectral bands, surface albedos, atmospheric profiles, and cloud
197 properties are used for the D2strEdd, D2strQuad, D4strQuad, MC, and DISORT methods,
198 differences of two- or four-stream irradiances from the MC/DISORT irradiances are regarded as
199 modeling biases solely due to the two-stream or four-stream approximations. Note that the three-
200 dimensional (3D) radiative effects related to horizontal photon transports or sub-pixel scale
201 variabilities do not contribute to the differences discussed in this study because the independent
202 column and plane-parallel approximations are used for all radiative transfer calculations. Ham et
203 al. (2014) showed that the 3D effects decrease with spatial scales and are negligible for scales
204 greater than 20 km. In addition, SW modeling biases due to partly cloudy pixels are quantified in
205 Ham et al. (2019).

206

207 **2.3. Computation of SW irradiances using surface, atmosphere, and cloud properties from** 208 **the CERES SYN product**

209 For obtaining realistic surface, atmospheric, and cloud properties, we use CERES Edition 4A
210 SYN irradiance and clouds hourly product (ASDC 2017, Doelling et al. 2013, Rutan et al. 2015).
211 The CERES SYN product was produced by merging geostationary and polar-orbit satellite
212 measurements. The geostationary satellites include series of Geostationary Operational
213 Environmental Satellite (GOES), Meteosat, and Multi-Functional Transport Satellite (MTSAT),
214 while the polar-orbit satellites include MODIS on Terra and Aqua (Doelling et al. 2013). All
215 geostationary visible and infrared channels are calibrated based on Terra Moderate Resolution
216 Imaging Spectroradiometer (MODIS) radiances (Doelling et al. 2013; Rutan et al. 2015). Cloud
217 properties are derived from MODIS narrow bands using CERES single satellite footprint (SSF)
218 algorithm (Minnis et al. 2011a, b), four times a day, combining two MODIS sensors aboard
219 Terra and Aqua. For the time between Terra and Aqua observations, cloud properties are derived
220 from geostationary satellites (Minnis et al. 1995). The SYN product provides hourly 1°-gridded
221 cloud properties, including cloud top/base heights, cloud phase, and cloud optical depth for four
222 cloud types, where the cloud type is defined by the cloud top pressure; low (> 700 hPa), mid-low
223 ($500\text{--}700$ hPa), mid-high ($300\text{--}500$ hPa), and high (< 300 hPa) clouds. Note that the ice cloud
224 optical depths in Ed4 SYN product were retrieved using the roughened hexagonal scattering
225 database (Yang et al 2008a, b), while all models in this study use more recent two-habit mixture
226 (THM) scattering database (Liu et al. 2014), which will be used for future CERES processing
227 (Edition 5). To avoid modeling errors due to the inconsistent ice scattering databases (Loeb et al.
228 2018), the ice cloud optical depths derived under the roughened hexagonal scattering database
229 are converted into values under THM scattering database by satisfying $(1 - g_{\text{hex}})\tau_{\text{hex}} = (1 -$
230 $g_{\text{THM}})\tau_{\text{THM}}$, where g_{hex} and τ_{hex} are asymmetry parameter and cloud optical depth retrieved with
231 roughened hexagonal scattering database, respectively, and g_{THM} and τ_{THM} are asymmetry

232 parameter and cloud optical depth retrieved with THM scattering database, respectively. This is
233 based on Similarity theory (van de Hulst 1974).

234 For each cloud type of 1° grid box, we derive SW irradiances from the LUT with taking into
235 account sub-grid variations of cloud optical depths. In doing so, a gamma distribution is
236 constructed using the linear and logarithmically mean cloud optical depths for each type (Thom
237 1958; Kato et al. 2005), which are provided in SYN product. Then the integration of irradiances
238 for the gamma distribution is performed using the 9-point Gaussian quadrature, while a similar
239 approach was used in earlier studies (Barker et al. 1996; Ham and Sohn 2010, Ham et al. 2019).
240 Then the gamma-weighted irradiance for each cloud type is weighted by the respective cloud
241 fraction to obtain the irradiance of the hourly grid box:

$$242 \quad F_{grid} = f_{low}F_{low} + f_{mid-low}F_{mid-low} + f_{mid-high}F_{mid-high} + f_{high}F_{high} \\ 243 \quad + (1 - f_{low} - f_{mid-low} - f_{mid-high} - f_{high})F_{clr} . \quad (1)$$

244 Consecutively, the hourly grid-box irradiances are temporarily averaged to obtain monthly or
245 annual means.

246 In the above processes, the SW irradiance is derived by interpolating the LUT for the given
247 cloud optical depth and cosine of the solar zenith angle (μ_0). We determine whether the LUT is
248 interpolated logarithmically or linearly depending on the range of the cloud optical depth and μ_0 ,
249 in order to minimize interpolation errors (Appendix B). As a result, the interpolation errors are
250 expected to be $< 1 \text{ W m}^{-2}$. Note that the interpolation errors affect results from all radiation
251 methods, and therefore, they do not influence the estimation of two- and four-stream biases.

252 While the interpolation of the LUT is performed for the cloud optical depth and μ_0 , cloud
253 altitudes and atmospheric profiles are truncated and the closest values in the LUT are chosen. For
254 example, cloud top and base heights are truncated with a 1 km interval for choosing irradiances

255 in the LUT. In addition, the MLS atmosphere is used for the precipitable water (PW) > 1 cm,
256 while the MLW is used for PW ≤ 1 cm. Surface types are separated into three types, land, ocean
257 and snow/ice covered surfaces. The surface type of the grid box is determined by ocean (f_{ocn}) and
258 snow/ice coverages (f_{snow}) in the SYN product. The rest of ocean and snow/ice coverages is
259 considered as a land coverage ($f_{ind} = 1 - f_{ocn} - f_{snow}$). If the grid box consists of more than one
260 surface type, the irradiances are computed for each surface type, and these are weighted by the
261 coverages:

$$262 \quad F_{grid} = f_{ocn}F_{ocn} + f_{land}F_{land} + f_{snow}F_{snow} \quad (2)$$

263 where F_{ocn} , F_{land} , and F_{snow} are the computed SW irradiances for ocean, land, and snow surface
264 types, respectively.

265 Even though the geostationary visible and infrared channels are calibrated against MODIS
266 (Doelling et al. 2013; Rutan et al. 2015), discontinuities at the geostationary satellite boundaries
267 in the CERES SYN product are apparent (ASDC 2017). These discontinuities are smoothed by
268 the constraining algorithm in the downstream CERES Energy Balanced And Filled (EBAF)
269 process (Rose et al. 2013, Kato et al. 2013, 2018a), in which atmosphere and cloud conditions
270 are adjusted to give better consistency in LW and SW top-of-atmosphere (TOA) irradiances to
271 actual TOA observations. However, the adjusted cloud properties are not available in the CERES
272 SYN product, and we use initial cloud properties obtained from multiple satellites in this study.
273 This means that the discontinuities across the geostationary satellites will appear in computed
274 SW irradiances in this study (Fig. 9). However, the impact of discontinuities on the model-to-
275 model differences is negligible, as shown in the next section (Figs. 10, 11).

276

277 **3. Results**

278 3.1. Biases of the two- and four-stream approximation for the simplified cloud cases

279 In this section, we estimate biases by the D2strEdd, D2strQuad, and D4strQuad methods for
280 selected cloud cases. Figure 1 shows biases for water clouds located at 2–3 km altitudes over
281 ocean as a function of the cosine of the solar zenith angle ($\mu_0 = \cos \theta_s$) and cloud optical depth
282 (τ_c) for the MLS atmosphere. Biases by the D2strEdd, D2strQuad, and D4strQuad methods for
283 the MLW atmosphere (not shown) are very similar to those shown in the MLS atmosphere, and
284 we only show the results for the MLS atmosphere in this section. Biases of the D2strEdd (Fig.
285 1a–c) and D2strQuad (Fig. 1e–g) methods are quite similar. The sign of D2strEdd and
286 D2strQuad methods in TOA upward SW irradiances are mostly negative. The sign of biases in
287 surface downward SW irradiances is opposite to the sign of TOA biases, consistent with results
288 in earlier studies (e.g., Meador and Weaver 1980; Zhu and Arking 1994; Lu et al. 2009; Zhang et
289 al. 2012; Barker et al. 2015). In contrast, the D4strQuad method produces positive biases in TOA
290 upward irradiances and negative biases in surface downward irradiances (Fig. 1i–k), with a
291 smaller magnitude compared to the D2strEdd or D2strQuad method (Zhu and Arking 1994).

292 Figure 1 also shows that, for a given cloud optical depth (τ_c), the sign of the irradiance bias
293 often changes when the cosine of the solar zenith angle (μ_0) changes. This means that the biases
294 are partly canceled when we integrate the biases over the course of the day. To examine this
295 feature, we use three examples of the diurnal cycle of μ_0 in Fig. 2. These are chosen at three
296 latitude regions (0.5°N, 30.5°N, and 60.5°N) on 15th October 2010. With these three diurnal
297 cycles, the SW bias is integrated by,

$$298 \quad \Delta F(\tau_c) = \frac{1}{24} \int_0^{24} \Delta F(\mu_0(h), \tau_c) dh \quad (3)$$

299 where $\Delta F(\mu_0, \tau_c)$ is the bias as a function of μ_0 and τ_c obtained in three left columns in Fig. 1, and
300 $\mu_0(h)$ is the cosine of solar zenith angle for the given hour (h) in Fig. 2. The diurnally-integrated

301 biases are shown in the fourth column of Fig. 1. As expected, the diurnally-integrated bias
302 $[\Delta F(\tau_c)]$ is generally smaller than the instantaneous bias $[\Delta F(\mu_0, \tau_c)]$. For example, $\Delta F(\tau_c)$ of the
303 D2stEdd bias in TOA SW upward irradiances is up to -5 W m^{-2} (blue lines, Fig. 1d), while
304 $\Delta F(\mu_0, \tau_c)$ is up to -8 W m^{-2} (Fig. 1a). Note that the overall shape of $\Delta F(\tau_c)$ remains very similar
305 for the three different diurnal cycles of μ_0 [$\mu_0(h)$] – shown by solid, dashed, and dotted lines in
306 Fig. 1d. In the examples of the diurnal integration in Fig. 1, it is assumed that the cloud optical
307 depth remains the same over the course of the day, but in Section 3.2, diurnal variations of both
308 μ_0 and τ_c will be considered using the CERES SYN product for the integration.

309 The diurnally-integrated biases for the D2stQuad method $[\Delta F(\tau_c)]$ have different signs
310 depending on τ_c (Fig. 1h), while the biases of D2strEdd (Fig. 1d) and D4strQuad (Fig. 1l) have
311 the same sign for all ranges of τ_c . This suggests that there will be larger cancellations of the
312 D2stQuad biases compared to the D2strEdd or D4strQuad method when averaging the biases
313 monthly or annually.

314 In Figs. 1m–t, MC simulation results with 10^6 and 10^8 photons, hereafter referred to as
315 MC1M and MC100M, respectively, are compared to DISORT simulation results. The
316 differences between MC1M and DISORT (Figs. 1m–p) or MC100M and DISORT (Figs. 1q–t)
317 are much smaller than the biases of the D2strEdd, D2strQuad, or D4strQuad methods (Figs. 1a–
318 l), demonstrating the robustness of both MC and DISORT methods. However, MC1M results
319 show larger random noises, compared to the MC100M results (Appendix A).

320 The signs of D2strEdd, D2strQuad, D4strQuad biases for ice clouds are similar to those
321 found in water clouds (Fig. 1), but there are also subtle differences mostly due to different
322 scattering phase functions. For example, the D2strEdd method produces positive biases in

323 atmosphere-absorbed irradiance for $\mu_0 > 0.8$ for water clouds (Fig. 1b), but the biases are positive
324 for $\mu_0 > 0.6$ for ice clouds (Fig. 3b).

325 While the biases of the D2strEdd, D2strQuad, D4strQuad methods over ocean and land (not
326 shown) are similar, the biases over snow are quite different. In Fig. 4, both D2strEdd and
327 D2strQuad methods produce much larger magnitudes of biases in surface downward irradiances
328 over snow (Figs. 4c, g) compared to the biases for the ocean surface type (Figs. 1c, g). This
329 suggests that the two-stream biases are significant during summer in polar regions and the use of
330 higher-stream models is desirable.

331 The computed SW heating rates from the D2strEdd, D2strQuad, and D4strQuad methods are
332 compared with those from the MC method in Figs. 5 and 6, for water and ice clouds,
333 respectively. For clear skies, SW heating rate biases are very small (0.02 K d^{-1}) for all altitudes
334 and are not provided here. In the comparison shown in Fig. 5, we use a water cloud layer with
335 cloud optical depth = 10, particle effective radius = $10 \mu\text{m}$, cloud base height = 2 km, and cloud
336 top height = 3 km. Large biases of the D2strEdd, D2strQuad, and D4strQuad occur at the altitude
337 where the cloud layer is present (2–3 km, gray areas in Fig. 5). The SW heating rate bias is
338 negative for D2strEdd and D2strQuad methods at 2–3 km altitude, while the D2strQuad bias is
339 larger negative than the D2strEdd bias. This is consistent with those found in earlier studies (e.g.,
340 Lu et al. 2009). In contrast, the SW heating rate bias by the D4strQuad method is generally
341 positive and the magnitude is smaller compared to D2strEdd and D2strQuad biases. Below 2 km,
342 the D2strEdd and D2strQuad SW heating rate biases are positive, while the magnitude of the
343 positive D2strEdd bias is larger than the D2strQuad bias. The results suggest that both D2strEdd
344 and D2strQuad methods underestimate the cloud absorption and overestimate the cloud
345 transmission, consistent with the results shown in Fig. 1. The MC method with 10^6 and 10^8

346 photons (MC1M and MC100M) produces non-systematic differences from the DISORT results,
347 while MC1M generates larger random noises than MC100M.

348 In Fig. 6, we use ice clouds with cloud optical depth = 10, particle effective diameter = 65
349 μm , cloud base height = 10 km, and cloud top height = 12 km. Similar to the comparison of
350 water cloud heating rates (Fig. 5), large differences in SW heating rates occur at the altitude of
351 ice cloud layers (10–12 km, gray areas in Fig. 6). Both D2strEdd and D2strQuad methods
352 underestimate SW heating rates at 10–12 km and overestimate SW heating rates below 10 km.
353 Compared to water clouds (Fig. 5), the magnitude of SW heating rate biases for ice clouds (Fig.
354 6) is larger, because the SW heating rate is inversely proportional to air density ($\propto 1/\rho_{\text{air}} \times$
355 $\Delta F/\Delta z$) and the air density decreases with altitude.

356 From the sensitivity tests in Figs. 1–6, except over snow surfaces, it is expected that the
357 D2strEdd and D2strQuad methods are likely to cause negative biases in TOA SW upward
358 irradiances, and positive biases in surface SW downward irradiances. In contrast, the D4strQuad
359 method tends to introduce positive biases in TOA SW upward irradiances and negative biases in
360 surface downward irradiances with a smaller magnitude. The specific signs and magnitudes
361 depend on cloud optical depth, cloud phase, cloud altitude, solar zenith angle, and surface type.
362 In the following two sections, we integrate the biases of the three approximated methods using
363 the CERES SYN hourly product.

364

365 **3.2. Diurnally-integrated biases of the delta-two-stream-Eddington (D2strEdd), delta-two-** 366 **stream-quadrature (D2strQuad), and delta-four-stream-quadrature (D4strQuad) methods**

367 In this section, we estimate diurnally-integrated monthly and annual biases in SW irradiances
368 using surface, atmosphere, and cloud properties from the one-year (2010) of the CERES

369 SYN1deg-hour product. Figure 7 shows monthly mean total cloud amount, cloud optical depth,
370 snow coverage, and total precipitation water for January and July 2010. The cloud properties are
371 averaged for four cloud types – high, mid-high, mid-low, and low clouds – weighted by
372 respective cloud fractions. Both months show large cloud amounts over the southern and
373 northern hemisphere storm-track regions (Figs. 7a, 7b), whereas locations of deep convective
374 clouds over the Warm Pool slightly change depending on the two seasons. The large cloud
375 optical depths occur over the Warm Pool and storm-track regions (Fig. 7c, 7d). The snow cover
376 over Antarctica is 100% for both seasons, while the snow cover over the Arctic is close to 100%
377 for winter time, and 60–80% for summer time (Figs. 7e, 7f). In addition, the precipitable water is
378 large over regions where deep convections occur (Figs. 7g, 7h).

379 To examine vertical distributions of cloud layers, we compute volume cloud coverage
380 profiles (%) using cloud top and base heights from the CERES SYN product in the following
381 process. First, for the given cloud base and top heights of each cloud type of each 1° grid box,
382 we compute the volume cloud coverage profile for 126 vertical bins defined from 0 to 20 km
383 with a 0.16 km interval. Second, we average the volume cloud coverage profiles for four cloud
384 types for each 1° grid box based on cloud amounts of the four cloud types. Third, we average the
385 profiles temporally and zonally to get monthly means, as shown in Figs. 8a and 8b. In these
386 figures, abundant high clouds over the tropics and low clouds in high-latitude regions are
387 captured in both seasons. Because we register cloud top and base heights to the nearest boundary
388 of 1-km interval in applying to the look-up-table (LUT) (Section 2.3), we apply the same process
389 to produce cloud coverage profiles shown in Figs. 8c and 8d. This process does not change cloud
390 profiles significantly so that most features in the original vertical resolution remain.

391 Because SW irradiances are computed with the LUT generated by the simplified surface,
392 atmosphere, and cloud properties, resulting irradiances are different from those computed with
393 original properties. To examine the feasibility of our approach, TOA SW irradiances computed
394 with the simplified properties are compared with CERES SYN observed SW irradiances in Fig.
395 9. The large differences between simulations and observations are shown over the desert, deep
396 convective clouds, and polar regions (Figs. 9e, 9f). The large biases over the desert and polar
397 regions are likely due to the simplifying assumption of the surface albedo. The positive modeling
398 biases over deep convective clouds in Figs. 9e, 9f might be related to constructing a gamma
399 distribution for large cloud optical depth values. This is because there is a larger deviation from
400 the gamma function for a larger standard deviation. Except for those regions, the simulated and
401 observed irradiances agree to within 4 W m^{-2} .

402 Note that the simulated results from DISORT and D4strQuad (Figs. 9e and 9f versus Figs. 9g
403 and 9h) show very similar biases compared to the observations. This suggests that the biases
404 shown in Figs. 9e–h are not due to the radiation method but from other parameters such as land
405 surface albedos, cloud optical depths, and gamma functions mentioned above. Note that our
406 simulated irradiances from the LUT (Figs. 9e–h) quite resemble the computed irradiances from
407 CERES SYN product (Figs. 9i, j) except land regions, demonstrating feasibility of the LUT
408 approach. In Figs. 9e–h, discontinuities are shown along the longitudes around 120°E and 60°W ,
409 due to cloud discontinuities at the boundaries of geostationary satellites (Section 2.3). A similar
410 pattern is shown for the differences between SYN computed irradiances and observed irradiances
411 (not shown).

412 From the comparison between simulated and observed SW irradiances, we conclude that our
413 modeling approach has larger uncertainties over land regions compared to ocean regions due to

414 the surface albedo assumption. However, even though the impact of the surface albedo on the
415 SW irradiance is significant, the impact of the surface albedo on the two- and four-stream biases
416 is much smaller, as discussed in Appendix C.

417 Figure 10 shows the biases due to two- and four-stream assumptions in monthly and annual
418 means. In this figure, DISORT simulation results are used as references to quantify biases of the
419 D2strEdd, D2strQuad, and D4strQuad methods. As discussed in Section 3.1, the D2strEdd and
420 D2strQuad methods produce negative biases in TOA irradiances over cloudy regions, up to -1.5
421 W m^{-2} , while the magnitude of the biases of the D2strEdd method is larger than that of the
422 D2strQuad method. This is because the D2strQuad method produces negative biases for optically
423 thin clouds ($\tau < 10$) and positive biases for optically thick clouds ($\tau > 20$) (Figs. 1g, 1h, 3g, and
424 3h), causing partial cancellations in monthly and annual means, as discussed in Section 3.1. Over
425 polar regions, the D2strQuad method shows large positive differences in Figs. 10d–f, as also
426 shown in Figs. 4e and 4h.

427 Compared to the D2strEdd and D2strQuad methods, the D4strQuad method shows smaller
428 regional biases in TOA SW irradiances up to $+0.9 \text{ W m}^{-2}$ (Figs. 10g–i). Global annual means of
429 SW TOA upward irradiance biases (the third column of Fig. 10) are -0.57 , -0.15 , and $+0.32 \text{ W}$
430 m^{-2} for the D2strEdd, D2strQuad, and D4strQuad methods, respectively. Global mean biases by
431 the D2strQuad method are smaller than global mean biases by the D4strQuad method due to the
432 cancellation of positive biases over polar regions and negative biases over cloudy regions. The
433 MC1M method shows quite good agreements with DISORT results, and the regional differences
434 are $< 0.3 \text{ W m}^{-2}$, and the global mean difference is $+0.04 \text{ W m}^{-2}$. This suggests that most of MC
435 noises are smoothed out in monthly and annual means. In all methods, monthly and annual mean
436 biases are quite similar, except for polar regions.

437 When the TOA SW biases are separated by ocean and land regions (Table 2), larger biases
438 occur over ocean. This is because the occurrence of cloudy skies is higher over ocean, and the
439 biases due to two-stream or four-stream approximations are larger in cloudy skies, compared to
440 clear skies.

441 Biases in surface downward irradiances shown in Fig. 11 are larger than biases in TOA
442 upward irradiances. The sign of the biases is positive in the D2strEdd and D2strQuad methods
443 and negative in the D4strQuad method, which is consistent with the results discussed in Section
444 3.1. The biases in the D2strEdd and D2strQuad methods are up to 3 W m^{-2} regionally, and global
445 annual mean biases are $+0.98$ and 1.90 W m^{-2} , respectively. In contrast, D4strQuad biases are
446 regionally up to -1.2 W m^{-2} and the global annual mean is -0.56 W m^{-2} . Except for polar regions,
447 monthly and annual global mean surface irradiance biases are very similar to each other, which is
448 also found in TOA upward irradiances. Compared to land regions, larger biases in surface
449 irradiances occur over ocean (Table 2) due to a similar reason in TOA upward irradiances.

450 Figure 12 shows the biases of SW heating rates computed by the three methods. The
451 D2strEdd (Figs. 12d–f) and D2strQuad (Figs. 12g–i) methods produce negative biases in SW
452 heating rates at 8–12 km over the tropics and 0–8 km in midlatitude to high-latitude regions. The
453 magnitude of the D2strQuad method is larger (up to -0.016 K d^{-1}) than that of the D2strEdd
454 method (up to -0.008 K d^{-1}), as also shown in Figs. 5 and 6. In addition, the D2strEdd method
455 (Figs. 12d–f) produces positive SW biases below 1 km, which is consistent with Figs. 5 and 6.
456 Compared to the D2strEdd and D2strQuad methods, the D4strQuad method (Figs. 12j–l)
457 produces very small biases in SW heating rates, less than 0.004 K d^{-1} . MC results also agree well
458 with DISORT results to within 0.004 K d^{-1} (Figs. 12m–o), suggesting that MC noises are mostly
459 canceled in monthly and annual means.

460

461 **4. Discussions**

462 In this study, due to the long computation time of MC and DISORT models, we minimized
463 the size of look-up-table (LUT). During the process, we simplified the cloud particle size,
464 atmospheric profiles, and land surface albedo. The impact of assumptions of the cloud particle
465 size, atmospheric profile, and land surface albedo on the two- and four-stream biases is examined
466 in Appendix C. It is shown that the impact of the particle size, water vapor profile, and land
467 surface albedo on the diurnally-integrated biases is within 0.17 W m^{-2} , 0.24 W m^{-2} , and 0.61 W
468 m^{-2} , respectively. The impact of these parameters is one-order smaller than the impact of cloud
469 optical depth, considering the biases change easily up to $2\text{--}8 \text{ W m}^{-2}$ depending on the cloud
470 optical depth (fourth columns of Figs. 1, 3, 4, C2, C3, and C4). This justifies our approach that
471 the two- and four-stream biases are estimated for specific cloud optical depths and solar zenith
472 angles, while the crude assumption is made for the cloud particle size, land surface albedo, and
473 water vapor profile. If we implement a more accurate cloud particle size, land surface albedo,
474 and water vapor profile, the overall magnitude of the biases can be slightly shifted, and this is
475 left for future examinations.

476 In this study, irradiances computed by DISORT and MC are used for the reference. While
477 these models produce accurate irradiances, the accuracy comes with a computational cost. In
478 Table 3, the computing time from various radiation methods is estimated for the same set of
479 input cases. D2strEdd and D2strQuad are the fastest methods among them. The computing time
480 of the D4strQuad method is 1.7 times longer than that of D2strEdd, but it is still much faster than
481 the DISORT or MC method. In contrast, the MC method with 10^8 photons is most
482 computationally expensive. In Appendix A, it is shown that DISORT results converge once the

483 number of streams ≥ 16 , while MC results are not completely converged with 10^8 photons.
484 Therefore, it seems that the DISORT method is generally more efficient than the MC method.
485 However, messaging passing interface (MPI) parallel programming is not used for running MC
486 model in this study. If the MPI is implemented, the computing time for the MC method can be
487 significantly improved.

488 The cloud properties used in this study were obtained from passive sensors from
489 geostationary and polar-orbiting satellites, while active sensors such as CALIPO or CloudSat in
490 A-train mission can give more accurate cloud height information particularly for multiple cloud
491 layers (Kato et al. 2018b). However, active sensors on A-train satellite observations are limited
492 to twice a day, which do not provide diurnal variations of clouds. From the comparison between
493 passive-derived only and active-passive combined cloud properties for the consistent temporal
494 sampling (Kato et al. 2018b), it was shown that cloud top heights of deep convective clouds over
495 the tropics are too low, and cloud top heights of southern hemisphere storm-track clouds are too
496 high in passive sensor measurements. Therefore, this suggests that the negative SW heating rate
497 biases by the D2strEdd and D2strQuad methods, shown at 8–12 km over the tropics (Fig. 12),
498 might be shifted upward if we implement more accurate cloud height derived from active
499 sensors. In addition, the negative biases shown in the southern storm-track clouds will be shifted
500 towards the surface. However, the SW TOA and surface irradiances are less sensitive to cloud
501 vertical distributions in comparison to heating rate profiles, and thus the two- and four-stream
502 biases in the TOA and surface irradiances shown in this study should not be affected by cloud
503 height errors.

504 In this study, we considered up to four cloud types in 1° grid box without taking into account
505 overlapping clouds. This is different from the operational CERES SYN algorithm, where a

506 random overlap assumption is used (Kato et al. 2019). The primary reason why we did not use
507 the overlap assumption is the long computing time for MC and DISORT methods because we
508 need to include all combinations of overlapping cloud scenarios for up to four layers in the LUT.
509 If we consider the overlapping clouds, it would increase each cloud fractions. However, the
510 column-integrated cloud optical depth would remain the same, as identified by passive-sensor
511 retrieved values. This means that the estimated two- and four-stream biases at TOA and surface
512 irradiances are less impacted by the overlapping assumption, in a similar context to the previous
513 paragraph.

514

515 **5. Conclusions**

516 We estimated the biases in diurnally integrated TOA and surface SW irradiances caused by
517 delta-two-stream-Eddington (D2strEdd), delta-two-stream-quadrature (D2strQuad), and delta-
518 four-stream-quadrature (D4strQuad) approximations using satellite measurements of the surface,
519 atmosphere, and cloud properties. We generated a look-up-table (LUT) with the pre-defined
520 surface, atmosphere, and cloud conditions and integrate the biases using the CERES Edition 4A
521 SYN data product.

522 The instantaneous and diurnally-integrated biases of the D2strEdd and D2strQuad methods
523 are 2–4 times larger than those found in the D4strQuad method (Fig. 1, 3, and 4). However, the
524 D2strQuad method produces different signs in the biases depending on the cloud optical depth,
525 and as a result, the biases are largely canceled in monthly and annual means (Figs. 10 and 11).
526 Nevertheless, the D4strQuad method generally produces a smaller bias than the biases produced
527 by D2strEdd and D2strQuad methods. In addition, the bias of the D4strQuad method shows a
528 smaller spatial variability compared to the D2strEdd and D2strQuad methods. Compared to

529 ocean or land regions, the D2strEdd and D2strQuad methods produce particularly large biases in
530 surface downward irradiances over snow, and as a result, the monthly regional bias can be as
531 large as 4 W m^{-2} during summer time over polar regions. The results of this study underscore the
532 advantage of the four-stream approximation compared to two-stream approximations in
533 computing daily, monthly, and annual mean irradiances for radiation budget estimates.

534

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537 downloaded from the NASA Langley Research Center CERES ordering tool at
538 <http://ceres.larc.nasa.gov/>.

539

540 **Appendix A: Monte Carlo (MC) noises**

541 The Monte Carlo (MC) method does not approximate the scattering phase function, and thus
542 it is generally considered as truth to assess other approximated radiative transfer methods.
543 However, the MC method uses a statistical approach to determine 1) whether the photon is
544 absorbed or scattered by the media (e.g., clouds) based on the single scattering albedo 2) the
545 direction of the scattered photon based on the cumulative function of the scattering phase
546 function. The magnitude of random noises of the MC method is determined by the number of
547 photons used for computations. The Monte Carlo noise is inversely proportional to the square
548 root of the number of photons ($\propto 1/\sqrt{N_p}$) (Evans and Marshak 2005; Barker et al. 2015) because
549 the variance of the sampling distribution equals the variance of the population divided by the
550 sampling size.

551 As an alternative way, the I3RC MC model provides a standard deviation of radiative
552 quantities from grouped batches of photons, which can be used as uncertainties of the MC
553 method. The standard deviation of the SW irradiances is obtained as:

$$554 \quad \sigma_{Batch} = \sqrt{\frac{1}{N_B-1} \sum_{i=1}^{i=N_B} (F_i - F)^2} \quad (A1)$$

555 where N_B is the number of batches, F_i is the mean of the SW irradiance for the i th batch, and F is
556 the mean of irradiances including all batches, i.e.:

$$557 \quad F = \frac{1}{N_B} \sum_{i=1}^{i=N_B} F_i . \quad (A2)$$

558 The smaller σ_{Batch} means a small deviation of irradiance outputs among batches, indicating a
559 smaller uncertainty of the MC results. We consider 100 batches (each batch contains $N_p/100$
560 photons where N_p is the total number of photons) and obtain σ_{Batch} in Fig. A1a–d. Compared to
561 the simulation results with 10^6 photons (MC1M) in Figs. A1a and b, the results with 10^8 photons

562 (MC100M) in Figs. A1c and d show a one-order magnitude smaller σ_{Batch} . In both simulation
563 results, σ_{Batch} generally increases with a cosine of solar zenith angle (μ_0) simply because an
564 incoming solar irradiance increases with μ_0 . For fixed μ_0 , the largest σ_{Batch} appears when the
565 cloud optical depth is around 10. This is because the SW irradiances become less sensitive to the
566 cloud optical depth for the cloud optical depth > 10 . In Figs. A1e and A1f, values of F from 10^6
567 and 10^8 photons are compared. For all solar zenith angles and cloud optical depths, the
568 differences in F are randomly distributed and the magnitudes of them are $< 1.0 \text{ W m}^{-2}$ for TOA
569 upward and surface downward irradiances.

570 Since the largest σ_{Batch} is shown for $\mu_0 = 1$ and cloud optical depth around 10 in Figs. A1a–d,
571 σ_{Batch} is estimated with various numbers of photons for the fixed $\mu_0 (=1)$ and cloud optical depth
572 $\tau_c (= 10)$ in Figs. A2a–b. The standard deviation of SW irradiances (σ_{Batch}) rapidly decreases
573 with the number of photons, particularly from 10^4 to 10^6 photons. In Fig. A2c–d, the mean
574 irradiances (F) are provided for various photon numbers with black symbols. In this figure, F
575 with 10^4 photons is deviated from F with 10^8 photons by 9 W m^{-2} for TOA upward SW
576 irradiances (Fig. A2c) and by 15 W m^{-2} for surface downward SW irradiances (Fig. A2d). The
577 SW irradiance differences between 10^6 and 10^8 photons are within 1 W m^{-2} , consistent with Figs.
578 A1e–f. In Figs. A2c–d, the DISORT simulation results with various numbers of streams (red
579 symbols) are also compared with the MC results (black symbols). DISORT produces almost
580 constant values of irradiances with increasing number of streams. For the number of streams \geq
581 16, the irradiances are within $< 0.01 \text{ W m}^{-2}$ among different numbers of streams. This indicates
582 that high accuracy can be achieved if the number of streams ≥ 16 is used in the DISORT model.
583 In comparison to the DISORT results, MC results with 10^8 photons are still off by 0.5 W m^{-2} for
584 TOA SW irradiances and 1 W m^{-2} for surface downward irradiances due to MC noises. From

585 these comparison results, the DISORT method with 40 streams is used as a reference to obtain
586 modeling biases of D2strEdd, D4strQuad, and D4strQuad methods.

587

588 **Appendix B: Interpolation of the look-up-table (LUT) for the given cosine of solar zenith**
589 **angle (μ_0) and cloud optical depth (τ_c)**

590 In this study, the interpolation of the LUT is performed to obtain SW irradiances for the
591 given cosine of solar zenith angle (μ_0) and cloud optical depth (τ_c). If the SW irradiance perfectly
592 follows a linear or logarithmic function with μ_0 or τ_c , the interpolation would not introduce
593 errors. However, the SW irradiance does not follow a linear or logarithmic function perfectly.

594 In Fig. B1, the interpolation errors are estimated for TOA SW irradiances when a linear-scale
595 (the first row) or logarithmic-scale (the second row) interpolation is performed over μ_0 (left
596 column) or over the cloud optical depth τ_c (right column). The linear interpolation generally
597 works better than the logarithmic interpolation over μ_0 (Fig. B1a versus B1c) except for $\mu_0 \geq 0.5$.
598 Therefore, we apply the linear interpolation for $\mu_0 < 0.5$ and the logarithmic interpolation for μ_0
599 ≥ 0.5 , and the corresponding interpolation errors are computed in Fig. B1e. The errors in Fig.
600 B1e is only for $\tau_c = 10$, and interpolation errors for all ranges of cloud optical depths are
601 $0.09 \pm 0.66 \text{ W m}^{-2}$ with a 68% confidence level.

602 When the interpolation is performed over the cloud optical depth (τ_c), the linear interpolation
603 causes negative errors in TOA SW irradiances for $\tau_c > 2$ (Fig. B1b). In contrast, the logarithmic
604 interpolation introduces positive errors for $\tau_c < 10$ (Fig. B1d). To minimize the interpolation
605 errors, we combine the linear and logarithmic interpolations depending on the range of τ_c as
606 follows and the corresponding errors are given in Fig. B1f.

607
$$F = F_{\text{lin}} \qquad \text{for } \tau_c < 2 \qquad \text{(B1)}$$

608
$$F = 0.7 F_{\text{lin}} + 0.3 F_{\text{log}} \quad \text{for } 2 \leq \tau_c < 5 \quad (\text{B2})$$

609
$$F = 0.4 F_{\text{lin}} + 0.6 F_{\text{log}} \quad \text{for } 5 \leq \tau_c < 10 \quad (\text{B3})$$

610
$$F = F_{\text{log}} \quad \text{for } \tau_c \geq 10 \quad (\text{B4})$$

611 Where F_{lin} is the irradiance obtained from the linear interpolation and F_{log} is the irradiance
 612 obtained from logarithmic interpolation for the given τ_c . The errors in Fig. B1f is only for $\mu_0 = 1$,
 613 and when including all ranges of solar zenith angles, the interpolation errors are $-0.52 \pm 0.60 \text{ W}$
 614 m^{-2} with a 68% confidence level. Note that the interpolation errors shown in this section are
 615 included in all simulation results of the D2strEdd, D2strQuad, D4strQuad, MC1M, MC100M,
 616 and DISORT methods, and thus the model-to-model differences are not affected by the
 617 interpolation errors.

618

619 **Appendix C: Impacts of the assumptions made for cloud particle size, water vapor profile,**
 620 **and land surface albedo on the estimation of two- and four-stream biases**

621 In this study, the cloud particle size is fixed at $10 \mu\text{m}$ for water clouds and $65 \mu\text{m}$ for ice
 622 clouds. Since the SW absorption increases with increasing cloud particle size, a different particle
 623 size may alter estimated two- and four- stream SW biases. However, if all radiation models show
 624 similar behaviors of SW irradiance to the change of the cloud particle size, the two- and four-
 625 stream biases would not be much affected by the assumption of the particle size. To examine the
 626 impact of water particle size on the biases, in Fig. C1, the biases are estimated for various ice
 627 particle effective diameters (d_e) and cosine of solar zenith angles (μ_0) with the fixed cloud optical
 628 depth = 10 (first to third columns in Fig. C1). It is shown that the biases change with μ_0 (along
 629 the horizontal axes of Fig. C1), but the biases remain almost the same with d_e (along the vertical
 630 axes of Fig. C1), suggesting that the SW biases are not sensitive to d_e . As a result, when the

631 biases are diurnally integrated using the three examples of diurnal variations of μ_0 in Fig. 2 with
632 Eq. (3), the diurnally-integrated SW biases are almost constant with d_e (fourth column, Fig. C1).

633 In Fig. C2, using the three examples of diurnal variations of μ_0 in Fig. 2, the diurnally-
634 integrated SW biases are computed as a function of the cloud optical depth for three different ice
635 particle sizes as $d_e = 40, 65, \text{ and } 80 \mu\text{m}$. The values of $40 \mu\text{m}$ and $80 \mu\text{m}$ are considered as
636 minimum and maximum of observed ice effective diameters based on the annual statistics from
637 Ed4 SYN hourly product in 2010; the mean and standard deviation of d_e are $60.6 \mu\text{m}$ and 18.8
638 μm , respectively. As the ice particle size (d_e) changes, the diurnally-integrated biases at TOA
639 upward, atmosphere-absorbed, and surface downward irradiances change by up to 0.17 W m^{-2} , as
640 summarized in Table C1. The bias changes due to the water particle size (r_e) are slightly larger
641 than those with d_e , but different signs occur depending on the range of r_e (Table C1).

642 In Fig. C3, we obtain similar plots to Fig. C2 but with changing water vapor profiles in order
643 to examine the impact of the water vapor profile on the estimation of the two- and four-stream
644 biases. In this examination, we scale MLS water vapor profile by 0.1, 1, and 2, which
645 corresponds to the PW values of 0.3, 2.97, and 5.87 cm, respectively, and the results are given in
646 three columns in Fig. C3. Note that the PW of 0.3 cm and 5.87 cm are considered as minimum
647 and maximum of PW, considering total precipitable waters (PWs) for standard tropical (TRO),
648 MLS, MLW, subarctic summer (SAS), and subarctic winter (SAW) are 4.19, 2.97, 0.86, 2.11,
649 and 0.42 cm, respectively. In addition, according to the one-year of Ed4 SYN hourly product in
650 2010, the mean and standard deviation of PW are 1.90 cm and 1.66 cm, respectively. In Fig. C3,
651 as the water vapor profile changes, the diurnally-integrated biases in atmosphere-absorbed
652 slightly increase, and the biases of surface downward slightly decrease. Note that we use MLW
653 profiles for dry conditions with $\text{PW} \leq 1 \text{ cm}$ and MLS profiles for humid conditions with $\text{PW} > 1$

654 cm when estimating two and four-stream biases (Section 2.1). Therefore, we obtain the bias
655 changes when the PW is changing from 0.3 cm to 0.86 cm (MLW), or the PW is changing 2.97
656 cm (MLS) to 5.87 cm in Table C1. The overall changes of the biases due to the PW changes are
657 smaller than 0.24 W m^{-2} .

658 Lastly, the impact of land surface albedo (α_s) is examined in Fig. C4, by comparing the
659 diurnally-integrated biases for three land surface albedos as 0.1, 0.2, and 0.36. Note that the land
660 surface albedos of 0.1 and 0.12 are used in estimating two- and four-stream biases for clear and
661 cloudy skies, respectively. Considering the brightest land albedo occurs over desert and a typical
662 albedo of desert is around 0.36 (Coakley 2003), $\alpha_s = 0.36$ is used as a maximum value for the
663 sensitivity test. When the land surface albedo changes from 0.1 to 0.36, the biases in diurnally-
664 integrated irradiances change up to 0.61 W m^{-2} (Table C1).

665 It should be noted that the two- and four-stream biases for clear skies are much smaller than
666 those for cloudy skies. For example, in Fig. C4, the clear-sky biases remain near-zero values
667 with changing land surface albedo (see converged lines for $\tau_c = 0$). Considering that cloud
668 amounts over land are smaller than 40%, we expect that the actual impact of land surface albedo
669 would be smaller than the numbers found in Table C1, which was computed for all range of
670 cloud optical depths. However, further study is desired with a more sophisticated land surface
671 bidirectional model with taking into account spectral dependency.

672 This section only examines albedo changes over land regions except for snow regions. For the
673 particularly bright snow surface, the biases can be significantly different from those estimated
674 over land, also shown in Fig. 4. We used the snow albedo model of Jin et al. (2008) for this
675 study, with a fixed snow grain size at $100 \mu\text{m}$. The snow grain size should be affected by

676 meteorological conditions and seasons, and therefore it is also desired to adopt the season-
677 dependent snow albedo model in the future.

678

References

- 679
680 ASDC, 2017: CERES SYN 1deg Ed4A Data Quality Summary. NASA Langley Research
681 Center, 36pp, [Available at
682 https://ceres.larc.nasa.gov/documents/DQ_summaries/CERES_SYN1deg_Ed4A_DQS.pdf].
- 683 Barker, H. W. and J. A. Davis, 1992: Cumulus cloud radiative properties and the characteristics
684 of satellite radiance wavenumber spectra. *Remote Sens. Environ.*, **42**(1), 51–64,
685 [https://doi.org/10.1016/0034-4257\(92\)90067-T](https://doi.org/10.1016/0034-4257(92)90067-T).
- 686 ———, 1996: Parameterization for computing grid-averaged solar fluxes for inhomogeneous
687 marine boundary layer clouds. Part I: Methodology and homogeneous biases. *J. Atmos. Sci.*,
688 **53**, 2289–2303.
- 689 ———, and Coauthors, 2003: Assessing 1D atmospheric solar radiative transfer models:
690 Interpretation and handling of unresolved clouds. *J. Climate*, **16**, 2676–2699.
- 691 ———, J. N. S. Cole, J. Li, B. Yi, and P. Yang, 2015: Estimation of errors in two-stream
692 approximations of the solar radiative transfer equation for cloudy-sky conditions. *J. Atmos.*
693 *Sci.*, **72**, 4053–4074, <https://doi.org/10.1175/JAS-D-15-0033.1>.
- 694 Cahalan, R. F., and Coauthors, 2005: THE I3RC: Bringing together the most advanced radiative
695 transfer tools for cloudy atmospheres. *Bull. Amer. Meteor. Soc.*, **86**, 1275–1293.
- 696 Chou, M.-D., M. J. Suarez, C.-H. Ho, M. M.-H. Yan, and K. T. Lee, 1998: Parameterizations for
697 cloud overlapping and shortwave single-scattering properties for use in general circulation
698 and cloud ensemble models. *J. Climate*, **11**, 202–214, [https://doi.org/10.1175/1520-0442\(1998\)011<0202:PFCOAS>2.0.CO;2](https://doi.org/10.1175/1520-0442(1998)011<0202:PFCOAS>2.0.CO;2).
- 700 Coakley J., 2003: Reflectance and albedo, surface. *Encyclopedia of the Atmosphere*. Academic
701 Press, Cambridge, MA, USA, pp. 1914–1923.

702 Davis, A., A. Marshak, R. F. Cahalan, and W. J. Wiscombe, 1997: The Landsat scale break in
703 stratocumulus as a three-dimensional radiative transfer effect: Implications for cloud remote
704 sensing. *J. Atmos. Sci.*, **54**, 241–260.

705 Doelling, D. R., and Coauthors, 2013: Geostationary enhanced temporal interpolation for
706 CERES flux products. *J. Atmos. Oceanic Technol.*, **30**, 1072–1090,
707 <https://doi.org/10.1175/JTECH-D-12-00136.1>.

708 Evans, K. F. and A. Marshak, 2005: *Numerical methods. Three-Dimensional Cloud Structure*
709 *and Radiative Transfer*. A. Marshak and A. Davis, Eds., Springer-Verlag, 243–281.

710 Fu, Q., 1991: *Parameterization of radiative processes in vertically inhomogeneous multiple*
711 *scattering atmospheres*. Ph.D. dissertation, University of Utah, 259 pp.

712 —, and K.-N. Liou, 1993: Parameterization of the radiative properties of cirrus clouds. *J.*
713 *Atmos. Sci.*, **50**, 2008–2025, [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0469(1993)050<2008:POTRPO>2.0.CO;2)
714 [0469\(1993\)050<2008:POTRPO>2.0.CO;2](https://doi.org/10.1175/1520-0469(1993)050<2008:POTRPO>2.0.CO;2).

715 —, K. Liou, M. Cribb, T. Charlock, and A. Grossman, 1997: On multiple scattering in thermal
716 infrared radiative transfer. *J. Atmos. Sci.*, **54**, 2799–2812, [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0469(1997)054<2799:MSPITI>2.0.CO;2)
717 [0469\(1997\)054<2799:MSPITI>2.0.CO;2](https://doi.org/10.1175/1520-0469(1997)054<2799:MSPITI>2.0.CO;2).

718 Halthore, R. N., and Coauthors, 2005: Intercomparison of shortwave radiative transfer codes and
719 measurements. *J. Geophys. Res.*, **110**, D11206, <https://doi.org/10.1029/2004JD005293>.

720 Ham, S.-H. and B. J. Sohn, 2010: Assessment of the calibration performance of satellite visible
721 channels using cloud targets: application to Meteosat-8/9 and MTSAT-1R. *Atmos. Chem.*
722 *Phys.*, **10**, <https://doi.org/10.5194/acp-10-11131-2010>.

723 ———, S. Kato, F. G. Rose, 2019: Impacts of Partly Cloudy Pixels on Shortwave Broadband
724 Irradiance Computations. *J. Atmos. Ocean. Technol.* **36**, 369–386,
725 <https://doi.org/10.1175/JTECH-D-18-0153.1>.

726 Hou, W., Q. Yin, H. Xu, L. Li, Z. Chen, 2010: A comparison of two stream approximation for
727 the discrete ordinate method and the SOS method, IGARSS, 2010,
728 <https://doi.org/10.1109/IGARSS.2010.5652681>.

729 Irvine, W. M., 1968: Multiple-scattering by large particles. II. Optically thick layers. *Astrophys.*
730 *J.*, **152**, 823–834.

731 Jin, Z., T. P. Charlock, W. L. Smith Jr., and K. Rutledge, 2004: A parameterization of ocean
732 surface albedo. *Geophys. Res. Lett.*, **31**, L22301, <https://doi.org/10.1029/2004GL021180>.

733 Jin, Z., T. P. Charlock, P. Yang, Y. Xie, and W. Miller, 2008: Snow optical properties for
734 different particle shapes with application to snow grain size retrieval and MODIS/CERES
735 radiance comparison over Antarctica. *Rem. Sens. Environ.*, **112(9)**, 3563–3581.

736 Joseph, J. H., W. J. Wiscombe, and J. A. Weinman, 1976: The Delta-Eddington Approximation
737 for radiative flux transfer. *J. Atmos. Sci.*, **33**, 2452–2459.

738 Kato, S., T. P. Ackerman, J. H. Mather, and E. E. Clothiaux, 1999: The k-distribution method
739 and correlated-k approximation for a shortwave radiative transfer model. *J. Quant. Spec.*
740 *Radia. Trans.*, **62**, 109–121, [https://doi.org/10.1016/S0022-4073\(98\)00075-2](https://doi.org/10.1016/S0022-4073(98)00075-2).

741 ———, F. G. Rose, and T. P. Charlock, 2005: Computation of domain-averaged irradiance using
742 satellite derived cloud properties. *J. Atmos. Ocean. Technol.*, **22**, 146–164,
743 <https://doi.org/10.1175/JTECH-1694.1>.

744 ———, N. G. Loeb, F. G. Rose, D. R. Doelling, D. A. Rutan, T. E. Caldwell, L. Yu, and R. A.
745 Weller, 2013: Surface irradiances consistent with CERES-derived Top-of-atmosphere

746 shortwave and longwave irradiances, 26, 2719–2740, [https://doi.org/ 10.1175/JCLI-D-12-](https://doi.org/10.1175/JCLI-D-12-)
747 00436.1

748 ———, F. G. Rose, D. A. Rutan, T. J. Thorsen, N. G. Loeb, D. R. Doelling, X. Huang, W. L.
749 Smith, W. Su, and S.-H. Ham, 2018a: Surface irradiances of Edition 4.0 Clouds and the
750 Earth’s Radiant Energy System (CERES) Energy Balanced and Filled (EBAF) data product.
751 *J. Climate*, **31**, 4501–4527, <https://doi.org/10.1175/JCLI-D-17-0523.1>.

752 ———, F. G. Rose, S.-H. Ham, D. A. Rutan, A. Redkevich, T. E. Caldwell, S. Sun-Mack, W. F.
753 Miller, and Y. Chen, 2018b: Radiative heating rates computed with clouds derived from
754 satellite-based passive and active sensors and their effects on generation of available
755 potential energy. *J. Geophys. Res.*, *Submitted*.

756 Kawata, Y. and W. M. Irvine, 1970: The Eddington approximation for planetary atmospheres.
757 *Astrophys. J.*, **160**, 787–790.

758 King, M. D. and Harshvardhan, 1986: Comparative accuracy of selected multiple scattering
759 approximations. *J. Atmos. Sci.*, **43**, 784–801.

760 Kratz, D. P., and F. G. Rose, 1999: Accounting for molecular absorption within the spectral
761 range of the CERES window channel. *J. Quant. Spec. Radia. Trans.*, **61**, 83–95,
762 [https://doi.org/10.1016/S0022-4073\(97\)00203-3](https://doi.org/10.1016/S0022-4073(97)00203-3).

763 Li, J.-L. F., D. E. Waliser, G. Stephens, S. Lee, T. L’Ecuyer, S. Kato, N. Loeb, H.-Y. Ma, 2013:
764 Characterizing and understanding radiation budget biases in CMIP3/CMIP5 GCMs,
765 contemporary GCM, and reanalysis. *J. Geophys. Res.*, **118(15)**, 8166–8184,
766 <https://doi.org/10.1002/jgrd.50378>.

767 Liou, K.-N., 1974: Analytic two-stream and Four-stream Solutions for Radiative Transfer. *J.*
768 *Atmos. Sci.*, **32**, 1473–1475.

769 ———, Q. Fu, and T. P. Ackerman, 1988: A simple formulation of the delta-four-stream
770 approximation for radiative transfer parameterizations. *J. Atmos. Sci.*, **45**, 1940–1948.

771 ———, 1992: *Radiation and Cloud Processes in the Atmosphere: Theory, Observation, and*
772 *Modeling*. Oxford University Press, 487 pp.

773 Liu, C., P. Yang, P. Minnis, N. Loeb, S. Kato, A. Heymsfield, and C. Schmitt, 2014: A two-habit
774 model for the microphysical and optical properties of ice clouds. *Atmos. Chem. Phys.*, **14**,
775 13719–13737, <https://doi.org/10.5194/acp-14-13719-2014>.

776 Loeb, N. G., and Coauthors, 2018: Impact of ice cloud microphysics on satellite cloud retrievals
777 and broadband flux radiative transfer model calculations. *J. Clim.*, **31**, 1851–1864, [https://](https://doi.org/10.1175/JCLI-D-17-0426.1)
778 doi.org/10.1175/JCLI-D-17-0426.1.

779 Lu, P., H. Zhang, J. Li, 2009: A comparison of two-stream DISORT and Eddington radiative
780 transfer schemes in a real atmospheric profile. *J. Quant. Spec. Radia. Trans.*, **110**, 129–138,
781 <https://doi.org/10.1016/j.jqsrt.2008.09.009>.

782 McClatchey, R. A., R. W. Fenn, J. E. A. Selby, F. E. Volz, and J. S. Garing, 1972: *Optical*
783 *Properties of the Atmosphere*. Air Force Cambridge Research Laboratory Environmental
784 Research Paper 411, 3rd ed., pp. 110, Air Force Cambridge Research Laboratories, Bedford,
785 MA.

786 Meador, W. E. and W. R. Weaver, 1980: Two-Stream Approximations to Radiative Transfer in
787 Planetary Atmospheres: A Unified Description of Existing Methods and a New
788 Improvement. *J. Atmos. Sci.*, **37**, 630–642.

789 Minnis, P., W. L. Smith Jr., D. P. Garber, J. K. Ayers, and D. R. Doelling, 1995: *Cloud*
790 *properties derived from GOES-7 for spring 1994 ARM intensive observing period using*
791 *version 1.0.0 of ARM satellite data analysis program*. NASA Reference Publ. 1366, 59 pp.

792 ———, and Coauthors, 2011a: CERES Edition-2 cloud property retrievals using TRMM VIRS and
793 Terra and Aqua MODIS data—Part I: Algorithms. *IEEE Trans. Geosci. Remote Sens.*, **49**,
794 4374–4400, <https://doi.org/10.1109/TGRS.2011.2144601>.

795 ———, and Coauthors, 2011b: CERES Edition-2 cloud property retrievals using TRMM VIRS and
796 Terra and Aqua MODIS data—Part II: Examples of average results and comparisons with
797 other data. *IEEE Trans. Geosci. Remote Sens.*, **49**, 4401–4430,
798 <https://doi.org/10.1109/TGRS.2011.2144602>.

799 Pincus, R., and K. F. Evans, 2009: Computational cost and accuracy in calculating three-
800 dimensional radiative transfer: Results for new implementations of Monte Carlo and
801 SHDOM. *J. Atmos. Sci.*, **66**, 3131–3146, <https://doi.org/10.1175/2009JAS3137.1>.

802 Räisänen, P., 2002: Two-stream approximations revisited: A new improvement and tests with
803 GCM data. *Quart. J. Roy. Meteor. Soc.*, **128**, 2397–2416.

804 Rose, F. G., T. Charlock, Q. Fu, S. Kato, D. Rutan, and Z. Jin, 2006: CERES proto-edition 3
805 radiative transfer: Tests and radiative closure over surface validation sites. *12th Conference*
806 *on Atmospheric Radiation*, American Meteorological Society, Madison, Wisconsin, 10–14
807 July 2006 [Available at <http://snowdog.larc.nasa.gov/cave/>].

808 ———, D. A. Rutan, T. Charlock, G. L. Smith, and S. Kato, 2013: An algorithm for the
809 constraining of radiative transfer calculations to CERES-observed broadband top-of-
810 atmosphere irradiance. *J. Atmos. Ocean. Tech.*, **30**, 1091–1106,
811 <https://doi.org/10.1175/JTECH-D-12-00058.1>.

812 Rutan, D. A., S. Kato, D. R. Doelling, F. G. Rose, L. T. Nguyen, T. E. Caldwell, and N. G. Loeb,
813 2015: CERES synoptic product: Methodology and validation of surface radiant flux. *J.*
814 *Atmos. Oceanic Technol.*, **32**, 1121–1143, <https://doi.org/10.1175/JTECH-D-14-00165.1>.

815 Shettle, E. P. and J. A. Weinman, 1970: The transfer of solar irradiance through inhomogeneous
816 turbid atmospheres evaluated by Eddington's approximation. *J. Atmos. Sci.*, **27**, 1048–1055.

817 Shibata, K., and A. Uchiyama, 1992: Accuracy of the delta-four-stream approximation in
818 inhomogeneous scattering atmospheres. *J. Meteor. Soc. Japan*, **70(6)**, 1097–1109.

819 Stamnes, K., S.-C. Tsay, W. Wiscombe and K. Jayaweera, 1988: Numerically stable algorithm
820 for discrete-ordinate-method radiative transfer in multiple scattering and emitting layered
821 media. *Appl. Opt.* **27**, 2502-2509.

822 Thom, H. C. S., 1958: A note on the gamma distribution. *Mon. Wea. Rev.*, **86**, 117–122.

823 Toon, O. B., C. P. McKay, and T. P. Ackerman, 1989: Rapid calculation of radiative heating
824 rates and photodissociation rates in inhomogeneous multiple scattering atmospheres. *J.*
825 *Geophys. Res.*, **94(D13)**, 16 287–16 301.

826 van de Hulst, 1974: The spherical albedo of a planet covered with a homogeneous cloud layer,
827 *Astron. Astrophys.*, **35**, 209–214.

828 Wiscombe, W. J., 1977: The delta-M method: Rapid yet accurate radiative flux calculations for
829 strongly asymmetric phase functions. *J. Atmos. Sci.*, **34**, 1408–1422.

830 Yang, P., G. W. Kattawar, G. Hong, P. Minnis, and Y. Hu, 2008a: Uncertainties associated with
831 the surface texture of ice particles in satellite-based retrieval of cirrus clouds—Part I: Single
832 scattering properties of ice crystals with surface roughness. *IEEE Trans. Geosci. Remote*
833 *Sens.*, **46**, 1940–1947, <https://doi.org/10.1109/TGRS.2008.916471>.

834 ———, G. Hong, G. W. Kattawar, P. Minnis, and Y. Hu, 2008b: Uncertainties associated with the
835 surface texture of ice particles in satellite-based retrieval of cirrus clouds: Part II— Effect of
836 particle surface roughness on retrieved cloud optical thickness and effective particle size.

837 *IEEE Trans. Geosci. Remote Sens.*, **46**, 1948–1957,
838 <https://doi.org/10.1109/TGRS.2008.916472>.

839 Zhang, F., Z. Shen, J. Li, X. Zhou, and L. Ma, 2012: Analytic Delta-Four-Stream Doubling-
840 adding method for radiative transfer parameterizations. *J. Atmos. Sci.*, **70**, 794–808,
841 <https://doi.org/10.1175/JAS-D-12-0122.1>.

842 ———, and J. Li, 2013: Doubling–Adding method for delta-four-stream spherical harmonic
843 expansion approximation in radiative transfer parameterization. *J. Atmos. Sci.*, **70**, 3084–
844 3101.

845 Zhu, X. and A. Arking, 1994: Comparison of daily averaged reflection, transmission, and
846 absorption for selected radiative flux transfer approximations. *J. Atmos. Sci.*, **51**,
847 3580–3592.

848 Table 1: Values of surface, atmospheric, cloud properties used for generating look-up-table
 849 (LUT) of SW irradiances and heating rates. The LUT is interpolated for the given cosine of solar
 850 zenith angle (μ_0) and cloud optical depth (τ_c) based on the method in Appendix B.

851

Input Variable	Value
Cosine of solar zenith angle (μ_0)	0.1 to 1.0 with a 0.1 interval
Surface types	Ocean, land, and snow
Atmospheric profiles	Midlatitude summer (MLS) and Midlatitude winter (MLW)
Cloud phases	Water ($r_e = 10 \mu\text{m}$) and ice ($d_e = 65 \mu\text{m}$) phases
Cloud optical depths (τ_c)	0.3, 1, 2, 5, 10, 20, 30, 40, and 50
Cloud top heights (CTHs)	1 km to 16 km with an 1 km interval
Cloud base heights (CBHs)	0 km to 15 km with an 1 km interval

860

861 Table 2: Annual means SW irradiances for various domains (global, ocean, land, Antarctic, and
862 Arctic) computed by various radiative transfer methods (DISORT, D2strEdd, D2strQuad, and
863 D4strQuad, and MC1M) with surface, cloud, and atmosphere properties derived for 2010. The
864 numbers in parentheses are differences of the D2strEdd, D2strQuad, D4strQuad, and MC1M
865 methods to the DISORT method.

Domain					
Method	Global 90°S–90°N	Ocean 60°S–60°N	Land 60°S–60°N	Antarctic 90°S–60°S	Arctic 60°N–90°N
TOA upward Irradiances ($W\ m^{-2}$)					
DISORT	99.63	97.51	100.03	99.39	118.59
D2strEdd	99.06	96.82	99.72	98.85	118.28
	(−0.57)	(−0.69)	(−0.31)	(−0.54)	(−0.31)
D2strQuad	99.48	97.17	100.09	99.57	119.14
	(−0.15)	(−0.34)	(+0.06)	(+0.18)	(+0.56)
D4strQuad	99.96	97.87	100.25	99.74	118.88
	(+0.32)	(+0.36)	(+0.22)	(+0.34)	(+0.29)
MC1M	99.67	97.58	100.04	99.30	118.50
	(+0.04)	(+0.07)	(+0.01)	(−0.09)	(−0.09)
Surface Downward Irradiances ($W\ m^{-2}$)					
DISORT	186.54	195.80	210.91	99.45	103.71
D2strEdd	187.52	196.93	211.32	100.92	104.81
	(+0.98)	(+1.13)	(+0.41)	(+1.46)	(+1.09)
D2strQuad	188.44	197.61	212.31	102.40	107.12
	(+1.90)	(+1.81)	(+1.39)	(+2.95)	(+3.40)
D4strQuad	185.98	195.13	210.45	99.20	103.50
	(−0.56)	(−0.67)	(−0.46)	(−0.25)	(−0.21)
MC1M	186.41	195.73	210.64	99.31	103.59
	(−0.13)	(−0.08)	(−0.27)	(−0.15)	(−0.12)

890 Table 3: Computing time of the D2strEdd, D2strQuad, D4strEdd, MC1M, MC100M, and
891 DISORT methods for the same set of cases (10 solar zenith angles \times 3 surface types \times 19 cloud
892 cases \times 2 atmospheric profiles, where the 19 cloud cases consist of 1 clear case + 9 cloud optical
893 depths \times 2 cloud phases). Note that computing time for Monte Carlo method depends on how
894 many parallel modules are used. In this study, 70 parallel modules are used for independent
895 computation of 70 gas absorption k bands. Since the computing time is also affected by the speed
896 of the workstation, a normalized computing time by that of the D2strEdd method is provided in
897 the second column.

898 Method	899 Computing time (sec)	Normalized time by D2strEdd
900 D2strEdd	11	1
901 D2strQuad	10	0.9
902 D4strQuad	19	1.7
903 MC10K	80	7.3
904 MC100K	792	72.0
905 MC1M	7847	713.3
906 MC10M	79515	7228.6
907 MC100M	946923	86083.9
908 DISORT 4str	7260	660.0
909 DISORT 8str	7282	662.0
910 DISORT 16str	7921	720.1
911 DISORT 24str	10205	927.7
912 DISORT 40str	36643	3331.2
913 DISORT 60str	42570	3870.0
914 DISORT 80str	52662	4787.5

915

916

917 Table C1: Changes of diurnally integrated biases of the D2strEdd, D2strQuad, and D4strQuad
918 methods due to deviations of r_e , d_e , PW, and α_s . For diurnally-integrated biases, the three
919 examples of solar zenith angles in Fig. 2 are used. When deviating r_e , d_e , and α_s , the fixed water
920 vapor profile from MLS atmosphere (= 2.97 cm) is used. When deviating PW and α_s , ice clouds
921 with $d_e = 65 \mu\text{m}$ are used. When deviating r_e , d_e , and PW, the ocean surface type is used.

922

923 Changes of biases in SW TOA upward irradiances (W m^{-2})

924 Parameter	925 Change of			
x	x	D2strEdd	D2strQuad	D4strQuad
926 Water r_e	8 → 10 μm	+0.51±0.42	+0.50±0.39	+0.55±0.42
927 Water r_e	10 → 17 μm	-0.45±0.24	-0.47±0.32	-0.38±0.22
928 Ice d_e	40 → 65 μm	+0.17±0.08	+0.16±0.08	+0.10±0.08
929 Ice d_e	65 → 80 μm	+0.02±0.04	+0.01±0.04	-0.02±0.03
930 PW	0.3 → 0.86 cm	+0.06±0.07	+0.18±0.03	+0.05±0.04
931 PW	2.97 → 5.87 cm	-0.08±0.10	+0.02±0.01	+0.04±0.03
932 α_s	0.1 → 0.36	+0.61±0.59	+0.23±0.58	-0.13±0.20

933 Changes of biases in SW atmosphere-absorbed irradiances (W m^{-2})

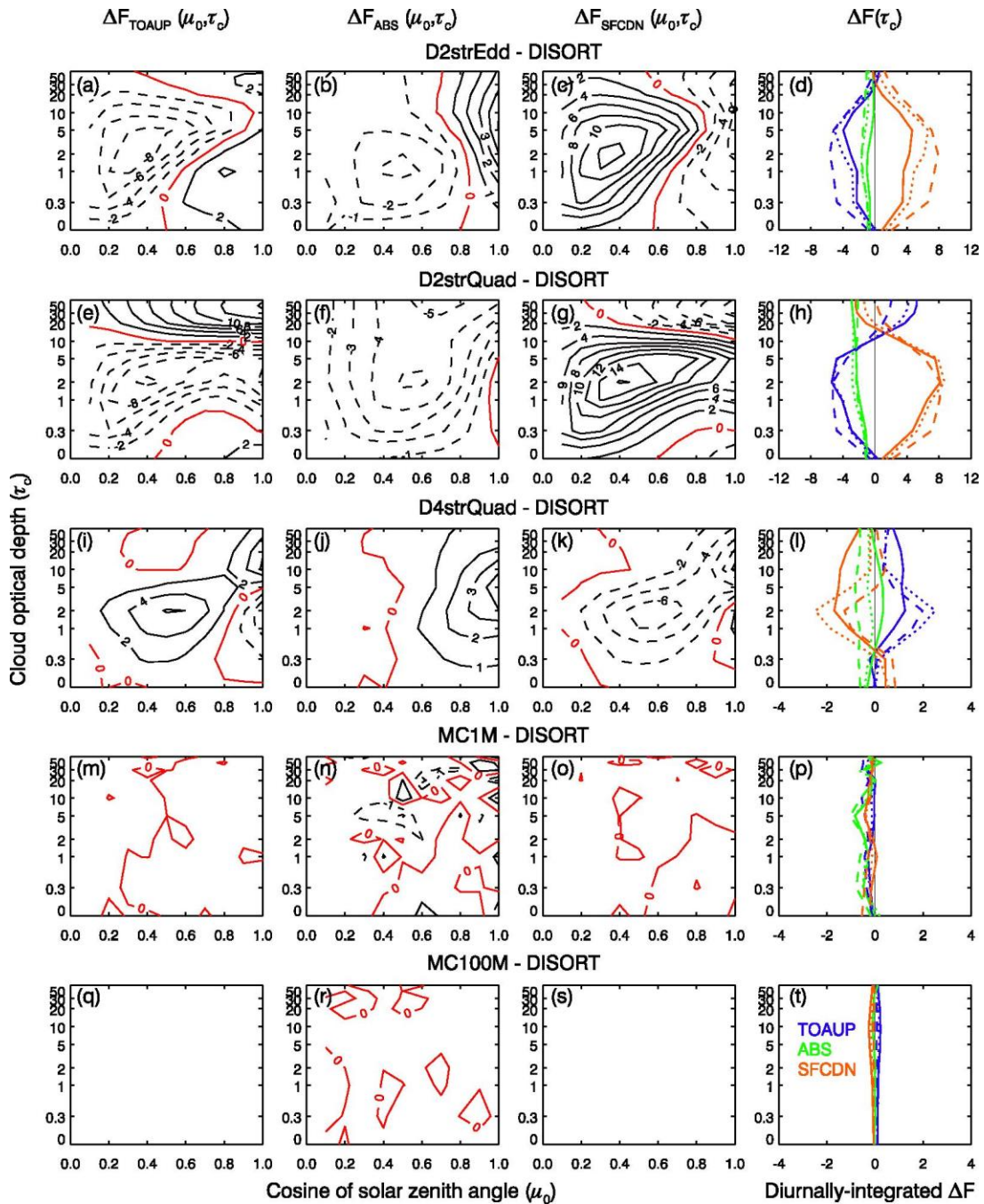
934 Parameter	935 Change of			
x	x	D2strEdd	D2strQuad	D4strQuad
935 Water r_e	8 → 10 μm	-0.09±0.08	+0.10±0.09	-0.09±0.06
936 Water r_e	10 → 17 μm	+0.02±0.10	-0.01±0.10	+0.02±0.03
937 Ice d_e	40 → 65 μm	-0.16±0.08	-0.16±0.08	-0.11±0.05
938 Ice d_e	65 → 80 μm	-0.01±0.02	-0.01±0.02	+0.01±0.02
939 PW	0.3 → 0.86 cm	+0.05±0.13	-0.14±0.05	-0.05±0.06
940 PW	2.97 → 5.87 cm	+0.24±0.19	+0.09±0.12	0.00±0.08
941 α_s	0.1 → 0.36	+0.15±0.16	-0.08±0.06	+0.04±0.04

942 Changes of biases in SW surface downward irradiances (W m^{-2})

943 Parameter	944 Change of			
x	x	D2strEdd	D2strQuad	D4strQuad
944 Water r_e	8 → 10 μm	-0.45±0.37	-0.42±0.34	-0.49±0.41
945 Water r_e	10 → 17 μm	+0.46±0.31	+0.51±0.42	+0.39±0.22
946 Ice d_e	40 → 65 μm	-0.01±0.04	+0.01±0.06	+0.01±0.02
947 Ice d_e	65 → 80 μm	-0.01±0.03	0.00±0.04	+0.01±0.01
948 PW	0.3 → 0.86 cm	-0.12±0.09	-0.05±0.08	0.00±0.04
949 PW	2.97 → 5.87 cm	-0.17±0.11	-0.12±0.13	-0.05±0.06
950 α_s	0.1 → 0.36	-0.39±0.76	+0.45±0.64	+0.10±0.16

951

952

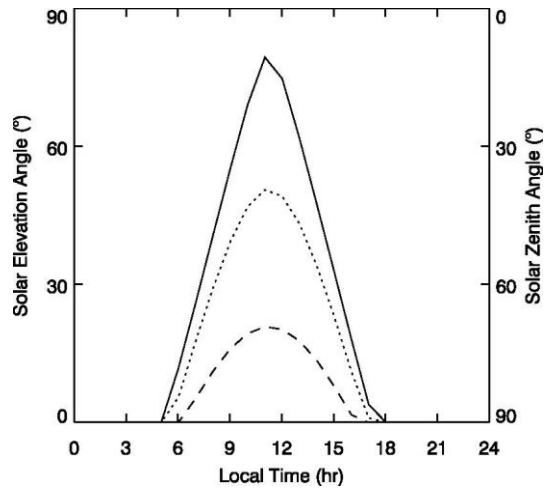


954

955 Figure 1: Biases of delta-two-stream-Eddington (D2strEdd) (the first row), delta-two-stream-
 956 Quadrature (D2strQuad) (the second row), delta-four-stream-quadrature (D4strQuad) (the third
 957 row), MC with 10^6 photons (MC1M) (the fourth row), and MC with 10^8 photons (MC100M) (the
 958 fifth row) to the DISORT simulation results with 40 streams. Instantaneous biases as a function

959 of cosine of solar zenith angle (μ_0) and cloud optical depth (τ_c) are given for TOA upward (the
960 first column), atmosphere-absorbed (the second column), and surface downward (the third
961 column) SW irradiances. In the first to third columns, solid contour lines are positive values, and
962 dashed lines are negative values. Zero lines are given as red lines. The intervals of contours for
963 TOA upward (the first column), atmosphere-absorbed (the second column), and surface
964 downward (the third column) irradiances are 2, 1, and 2 W m^{-2} , respectively. Using the three
965 examples of diurnal variations of μ_0 in Fig. 2 (solid, dashed, and dotted lines), the instantaneous
966 biases are integrated for TOA upward (blue), atmosphere-absorbed (green), and surface
967 downward (orange) irradiance (the four column). The simulation is performed for water clouds
968 over ocean with the mid-latitude summer (MLS) profile. Cloud top and base heights of the water
969 cloud layer are, respectively, 2 and 3 km. Water particle effective radius of 10 μm is used.

970

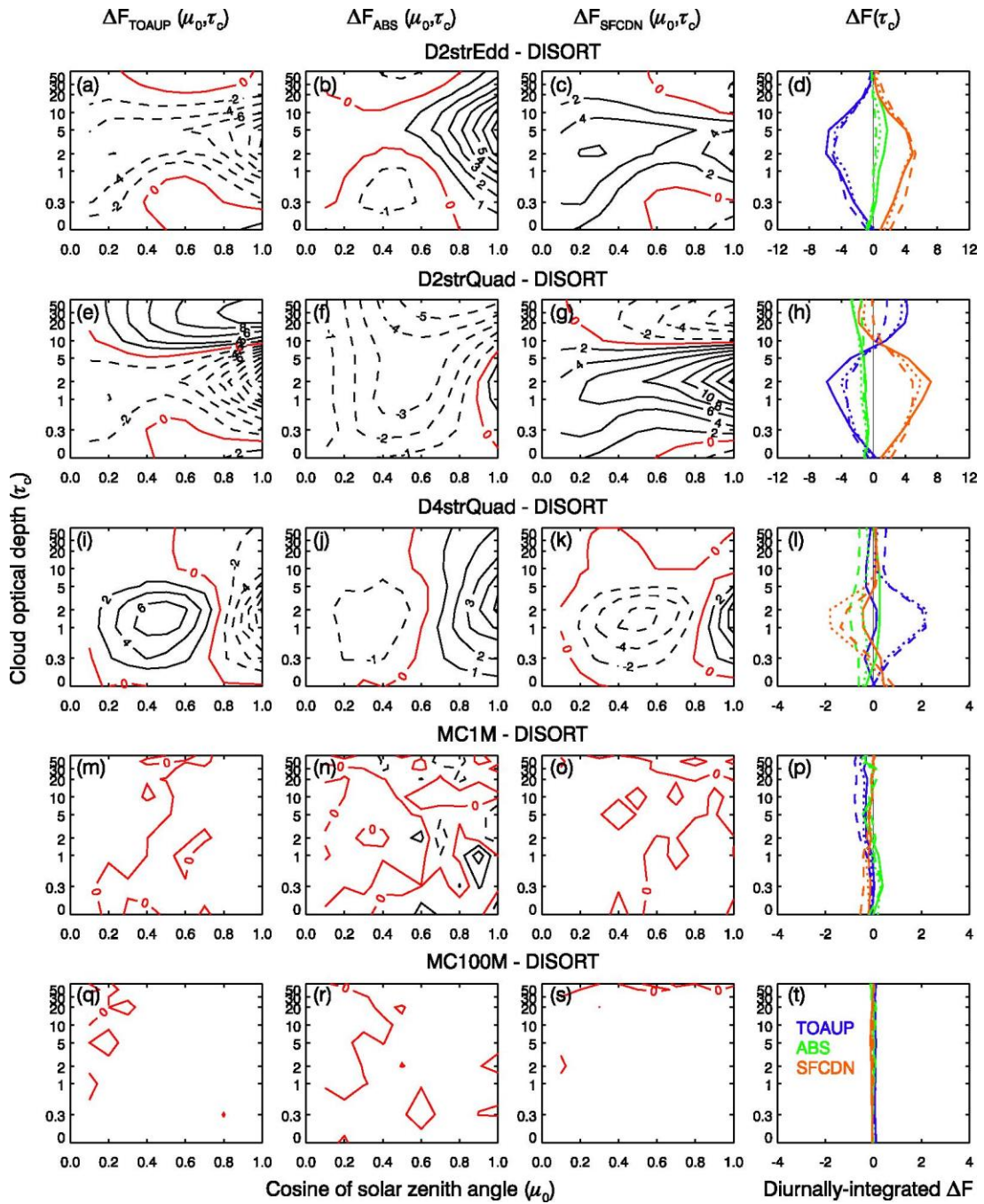


971

972

973 Figure 2: Examples of diurnal variations of the solar zenith angle on 15th October 2010. Three
 974 locations are selected; 1) 0.5°E, 0.5°N (solid line), 2) 0.5°E, 30.5°N (dotted line), and 3) 0.5°E,
 975 60.5°N (dashed line). SYN Ed4A hourly product is used to obtain the solar zenith angles.

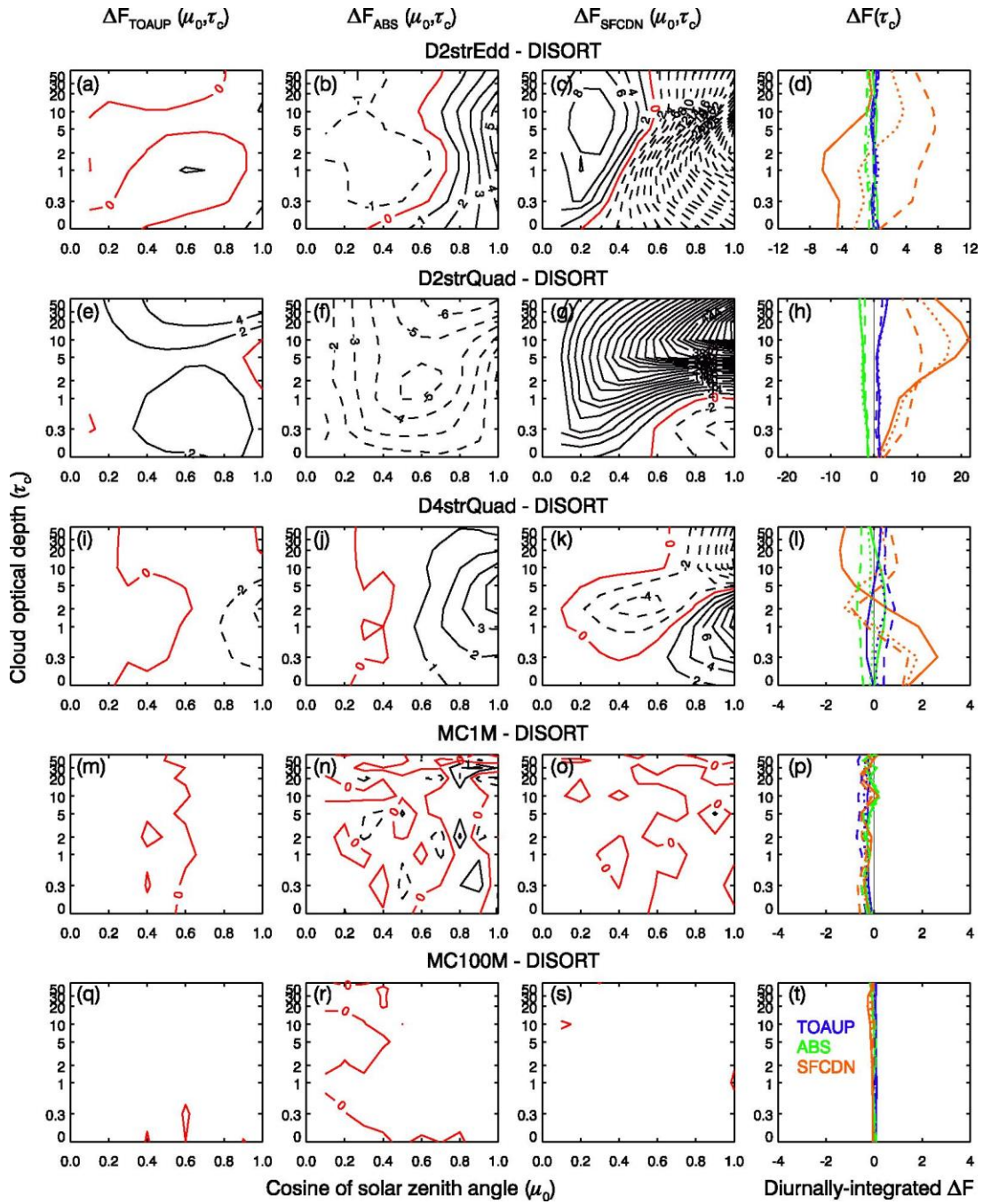
976



978

979 Figure 3: Same as Fig. 1 but for ice clouds. Cloud top and base heights of the ice cloud layer are,
 980 respectively, 10 and 12 km. The ice particle effective diameter of 65 μm is used.

981



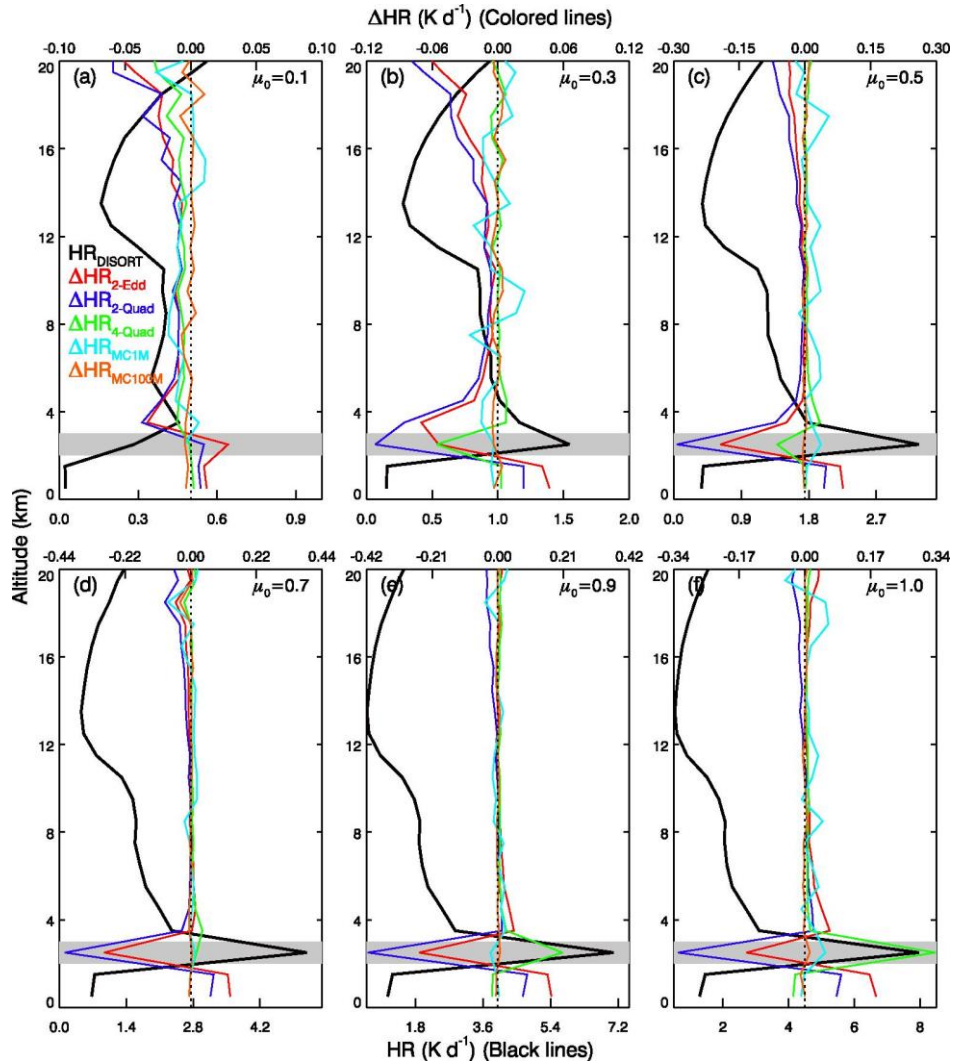
982

983

984 Figure 4: Same as Fig. 1 but for water clouds over the snow surface type.

985

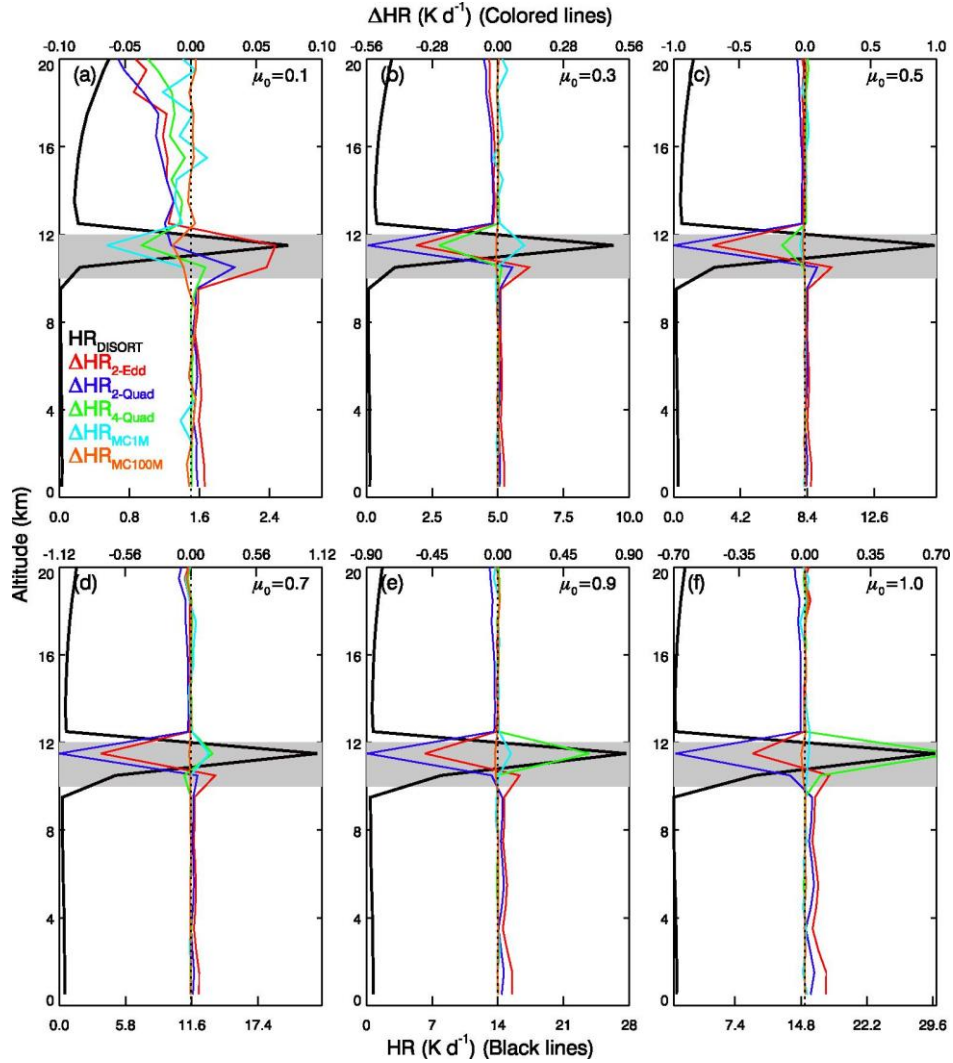
986



987

988 Figure 5: Computed SW heating rate profiles (black lines) by the 40-stream DISORT method
 989 with a cosine of solar zenith angle (μ_0) of (a) 0.1 (b) 0.3 (c) 0.5 (d) 0.7 (e) 0.9 (f) 1.0 for water
 990 clouds over ocean. Cloud top and base heights of the water cloud layer are, respectively, 2 and 3
 991 km (gray box area). The water particle effective radius of 10 μm and cloud optical depth of 10
 992 are used. Mid-latitude atmospheric (MLS) profiles are used for temperature and humidity
 993 profiles. The biases in SW heating rates by the D2strEdd (red lines), D2strQuad (blue lines),
 994 D4strQuad (green lines), MC1M (cyan lines), and MC100M (orange lines) methods are given
 995 with the top horizontal axes where DISORT results are used as references. Note that the
 996 magnitude of biases is one order smaller than the absolute magnitude of the MC heating rates.

997



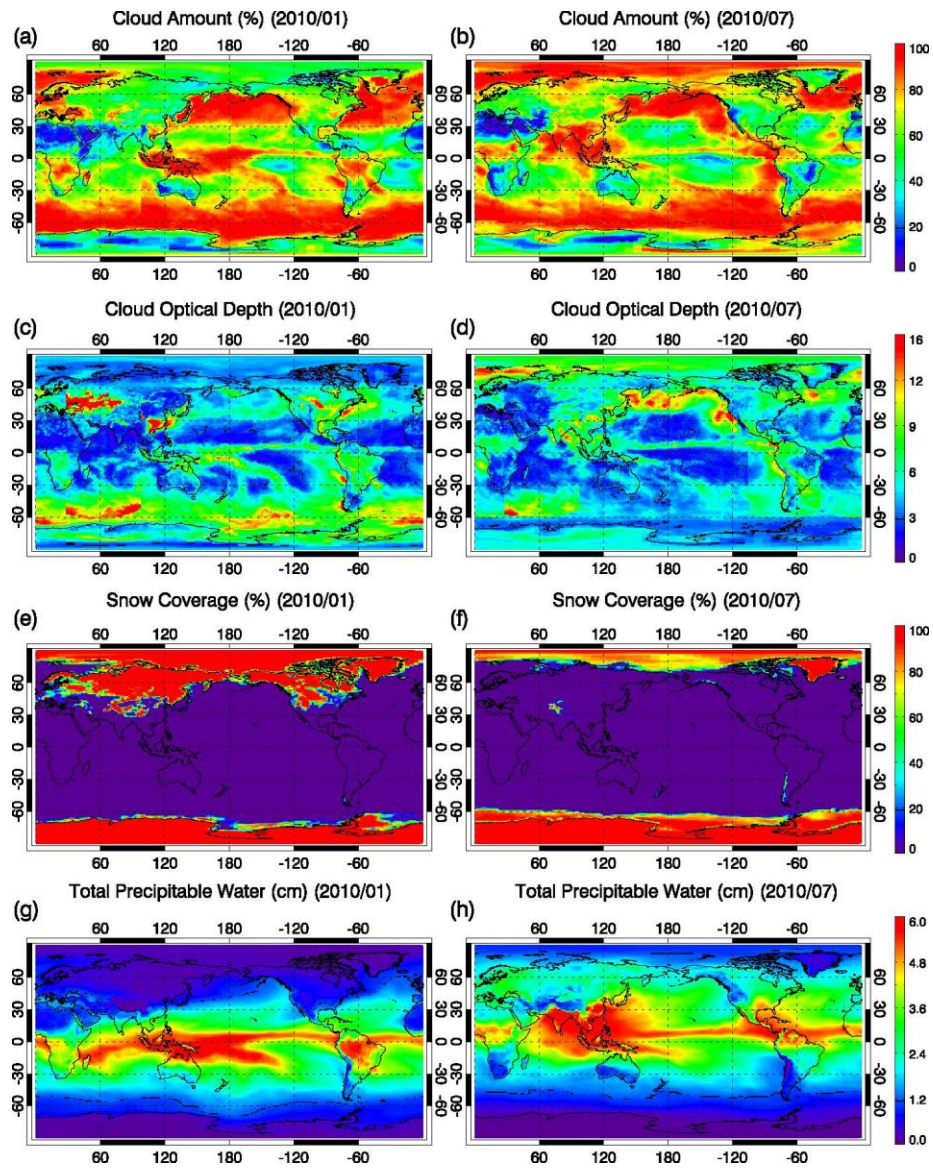
999

1000 Figure 6: Same as Fig. 5 but for ice clouds with a cloud optical depth of 10, ice effective

1001 diameter = 65 μm , cloud base height = 10 km, and cloud top height = 12 km.

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1005

1006 Figure 7: Monthly mean cloud amounts (%) for (a) January 2010 and (b) July 2010. (c) and (d)

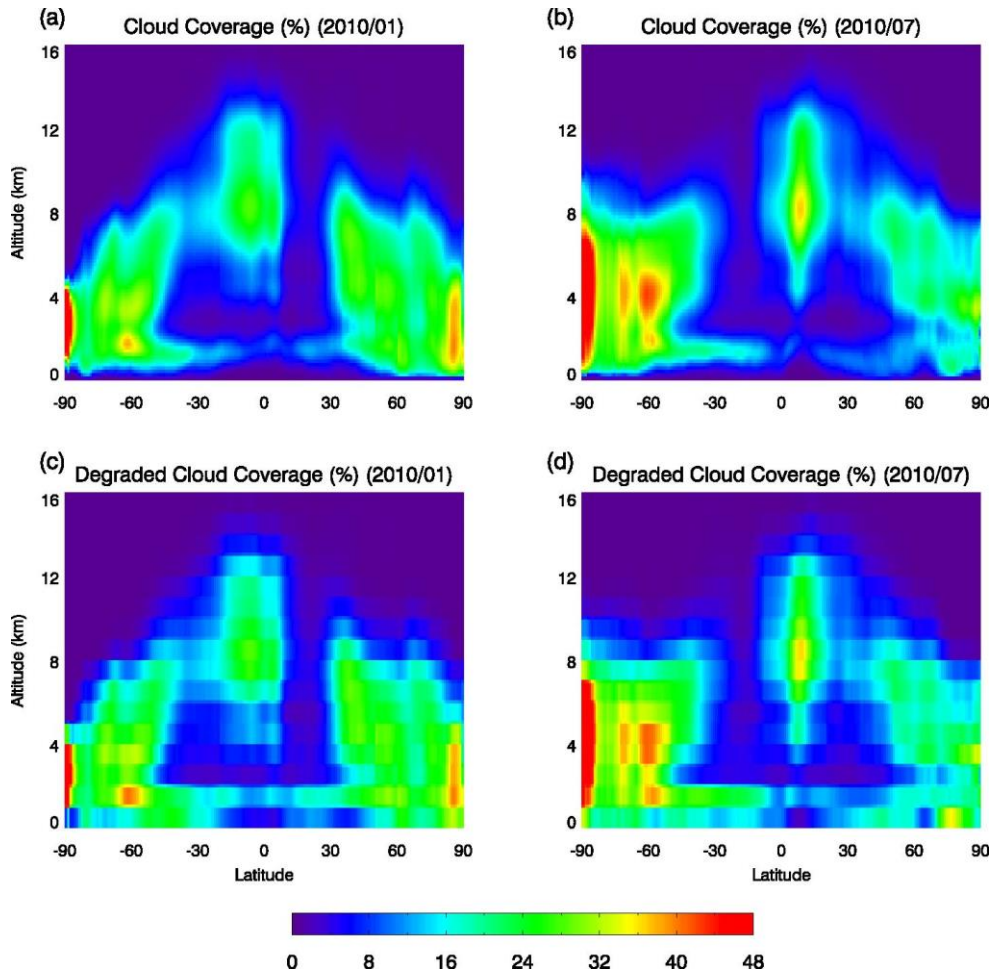
1007 are the same as (a) and (b) but for cloud optical depths. (e) and (f) are the same as (a) and (b) but

1008 for snow/ice coverage (%). (g) and (h) are the same as (a) and (b) but for total precipitable water

1009 (cm).

1010

1011

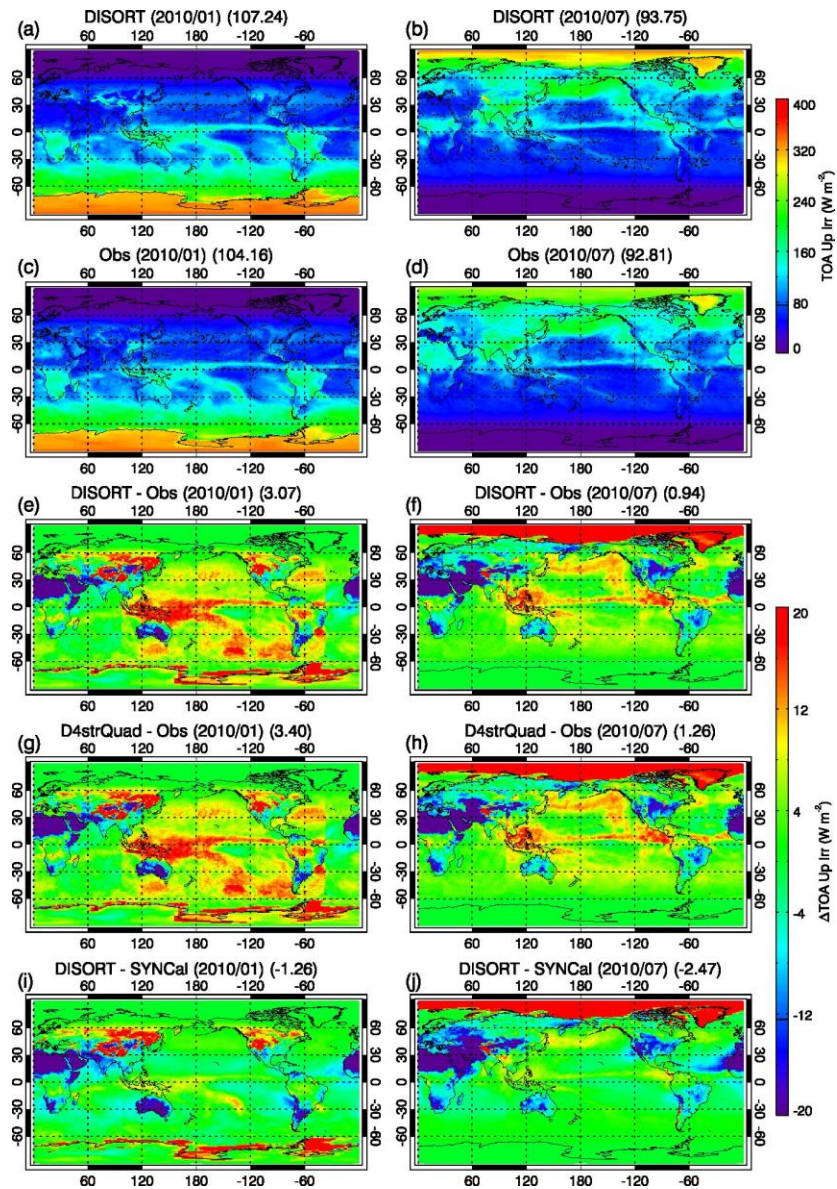


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1013

1014 Figure 8: Monthly mean volume cloud coverage (%) profiles from 0 to 20 km computed with a
1015 0.16 km vertical grid bin interval for (a) January 2010 (b) July 2010. In each 1° grid box, cloud
1016 base and top heights of four cloud types (high, mid-high, mid-low, and low) are used to assign
1017 the cloud coverage profile. Then the cloud coverage profiles are temporally and zonally averaged
1018 to plot this figure. Since the discretized cloud top and base heights are used in applying the look-
1019 up table (LUT), the cloud coverages with the discretized cloud heights are also provided in (c)
1020 January 2010 (d) July 2010.

1021

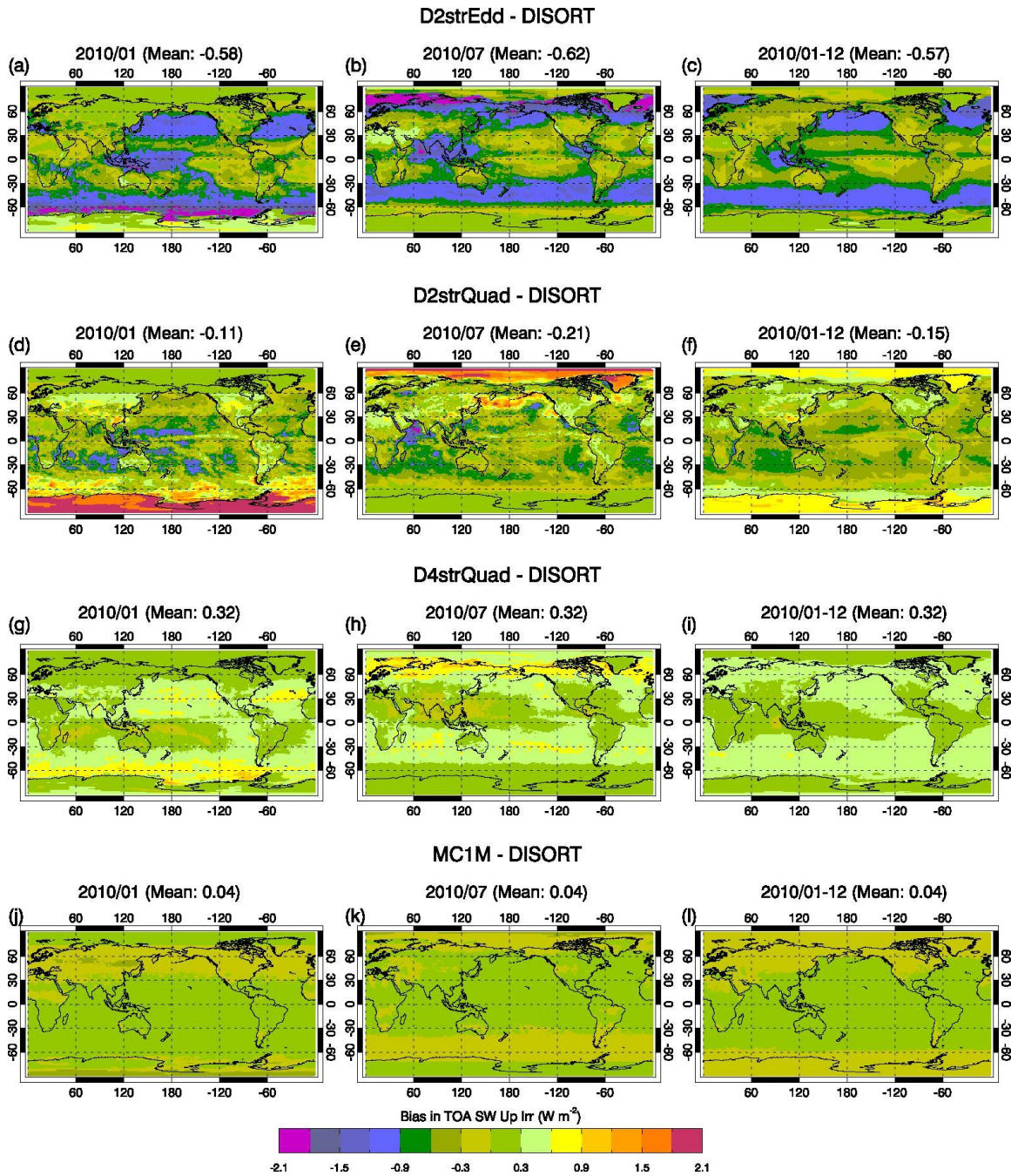


1022

1023 Figure 9: Monthly mean TOA SW irradiances computed with the DISORT method using
 1024 simplified surface, atmosphere, and cloud properties for (a) January 2010 (b) July 2010. (c) and
 1025 (d) are the same as in (a) and (b) but for observed TOA SW irradiances from CERES SYN
 1026 product. The differences between DISORT-computed and observed irradiances are provided for
 1027 (e) January 2010 (b) July 2010. (g) and (h) are same as in (e) and (f) but for differences between
 1028 D4strQuad-computed and observed irradiances. Differences between DISORT-computed

1029 irradiances (from our study) and SYN calculated irradiances (from CERES SYN product) are
1030 obtained for (a) January 2010 and (b) July 2010.

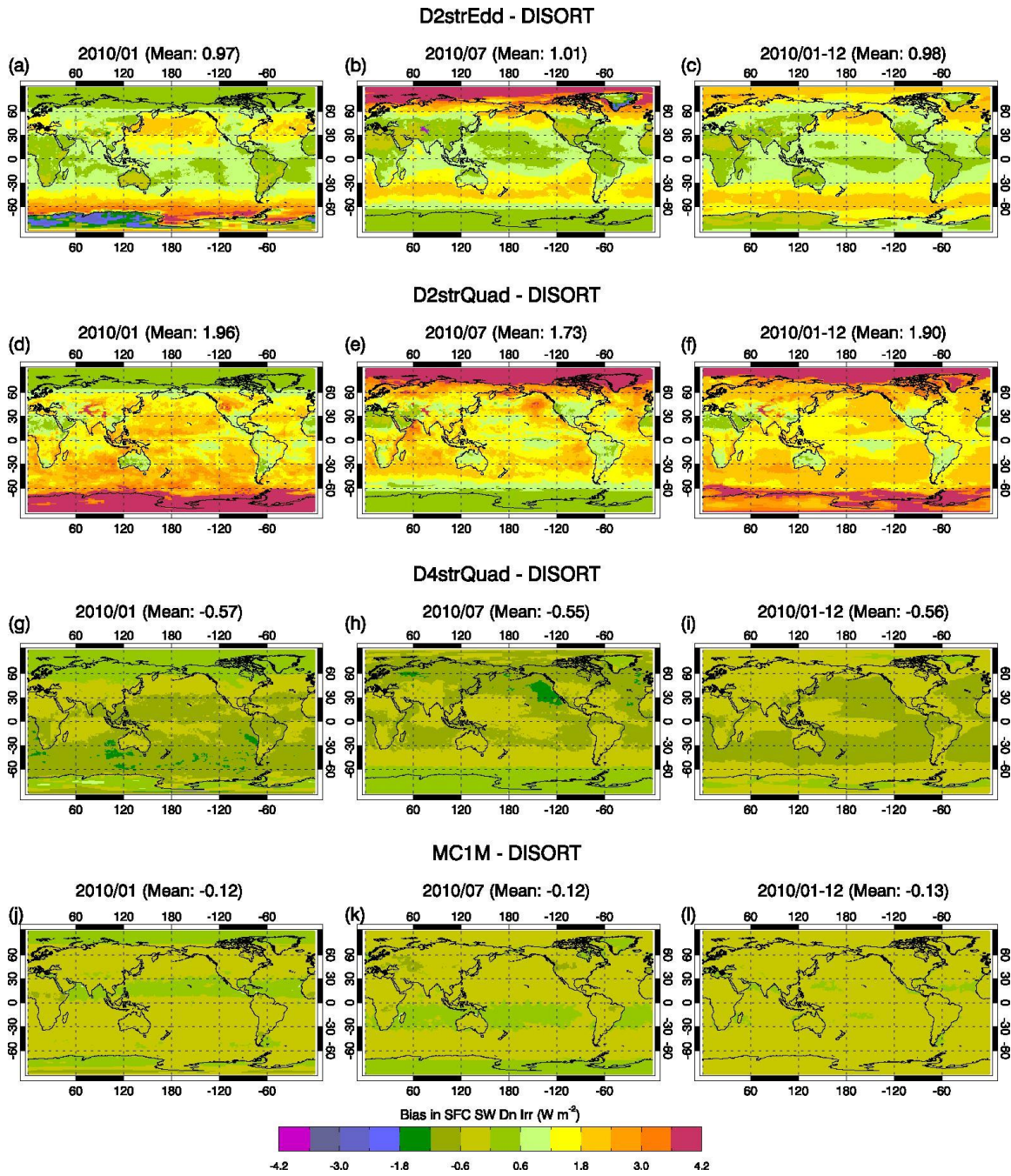
1031



1032

1033 Figure 10: Biases in SW TOA upward irradiances ($W m^{-2}$) by the D2strEdd (the first row)
 1034 D2strQuad (the second row) D4strQuad methods (the third row), and MC1M (the fourth row)
 1035 methods to the 40-stream DISORT method. The biases are obtained for January 2010 (left
 1036 column), July 2010 (middle column), and January–December 2010 (right column). Numbers in
 1037 parentheses are global means.

1038



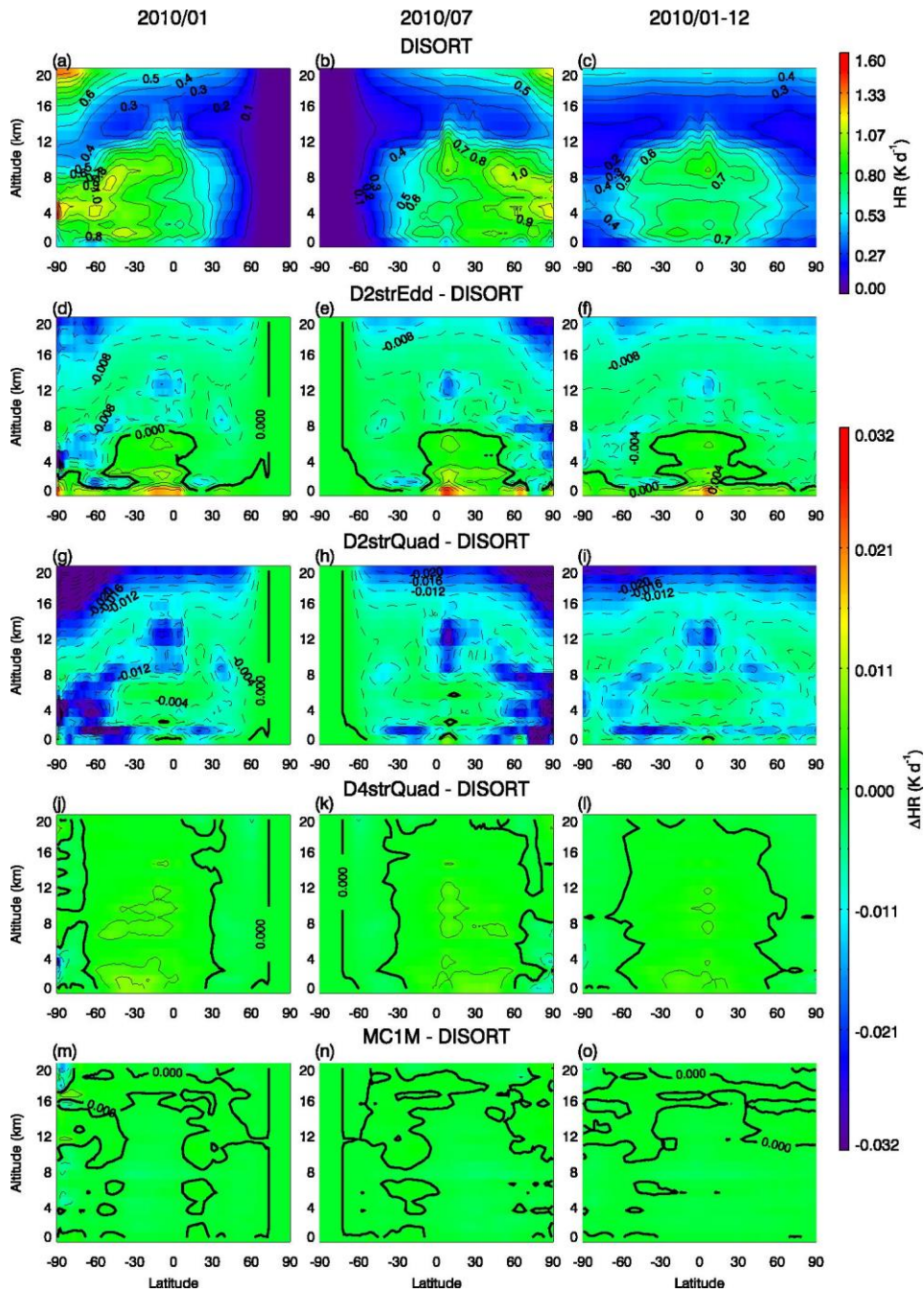
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1040

1041 Figure 11: Same as Fig. 10 but for biases in surface downward irradiances (W m^{-2}).

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1045

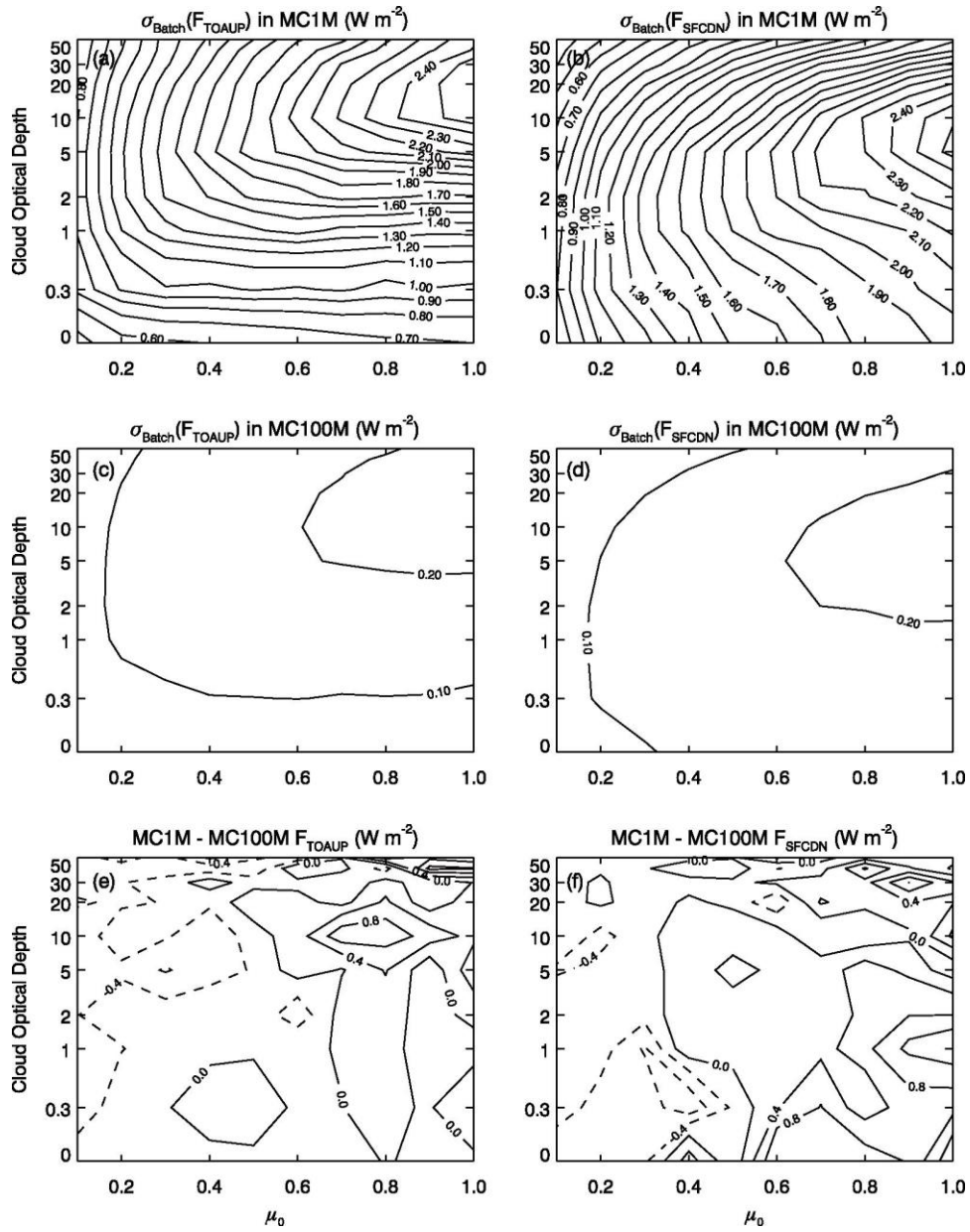
1046 Figure 12: SW heating rates computed by the DISORT method for (a) January 2010 (b) July
 1047 2010 (c) January–December 2010. Biases in SW heating rates by the D2strEdd method in
 1048 comparison to the DISORT method for (d) January 2010 (e) July 2010 (f) January–December
 1049 2010. (g)–(i) are the same as (d)–(f) but for biases by the D2strQuad method. (j)–(l) are the same

1050 as (d)–(f) but for biases by the D4strQuad method. (m)–(o) are the same as (d)–(f) but for biases
1051 by the MC1M method. The contour interval is 0.1 K d^{-1} for (a)–(c) and 0.004 K d^{-1} for (d)–(o).

1052 Thick solid black lines in (d)–(o) are zero lines.

1053

1054



1055

1056

Figure A1: Standard deviations (σ_{Batch}) of (a) TOA upward SW irradiances (b) surface

1057

downward SW irradiances computed by the MC method with 10^6 photons (MC1M). (c) and (d)

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are the same as (a) and (b) except that 10^8 photons are used (MC100M). Differences in (e) TOA

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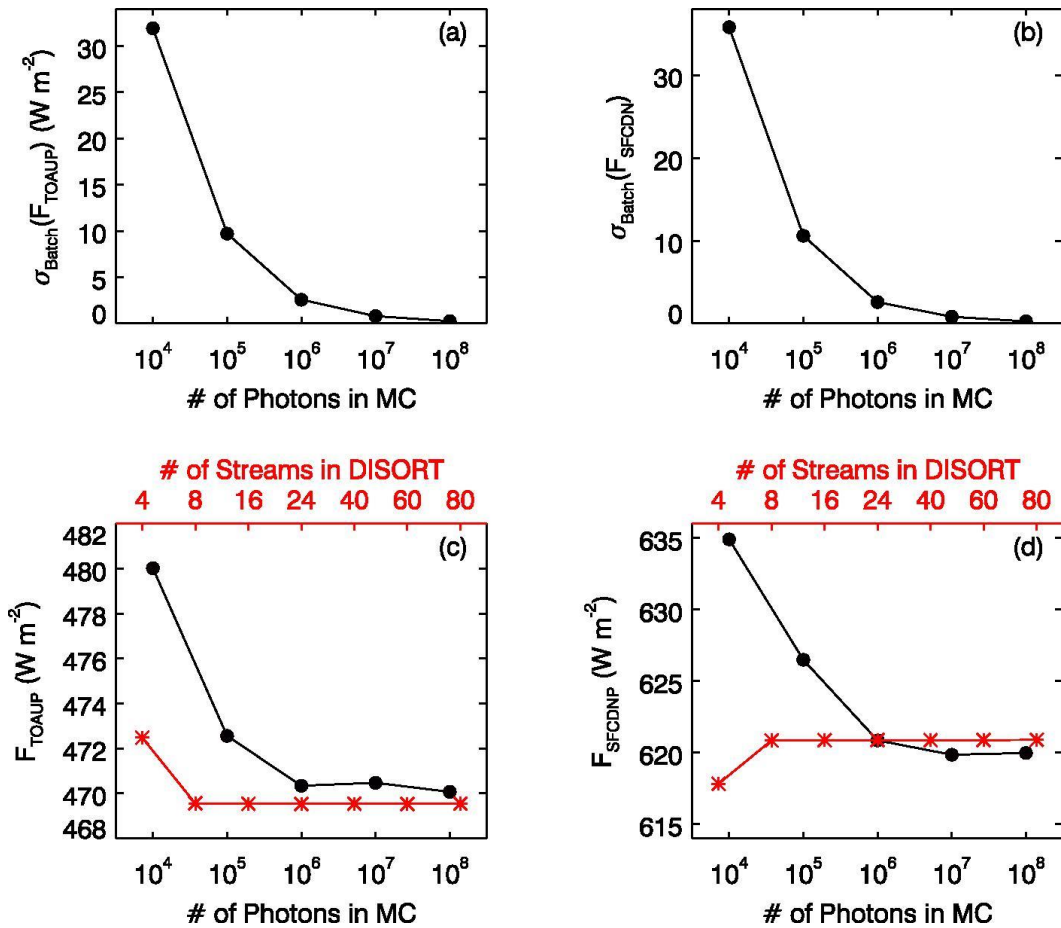
upward SW irradiances (f) surface downward SW irradiances computed from 10^6 and 10^8

1060

photons (MC1M minus MC100M). Water clouds located at 2–3 km over ocean are placed in the

1061 Midlatitude-summer profile (MLS) atmosphere. The interval of contour lines is 0.1 W m^{-2} in (a)–
1062 (d) and 0.4 W m^{-2} in (e)–(f).

1063

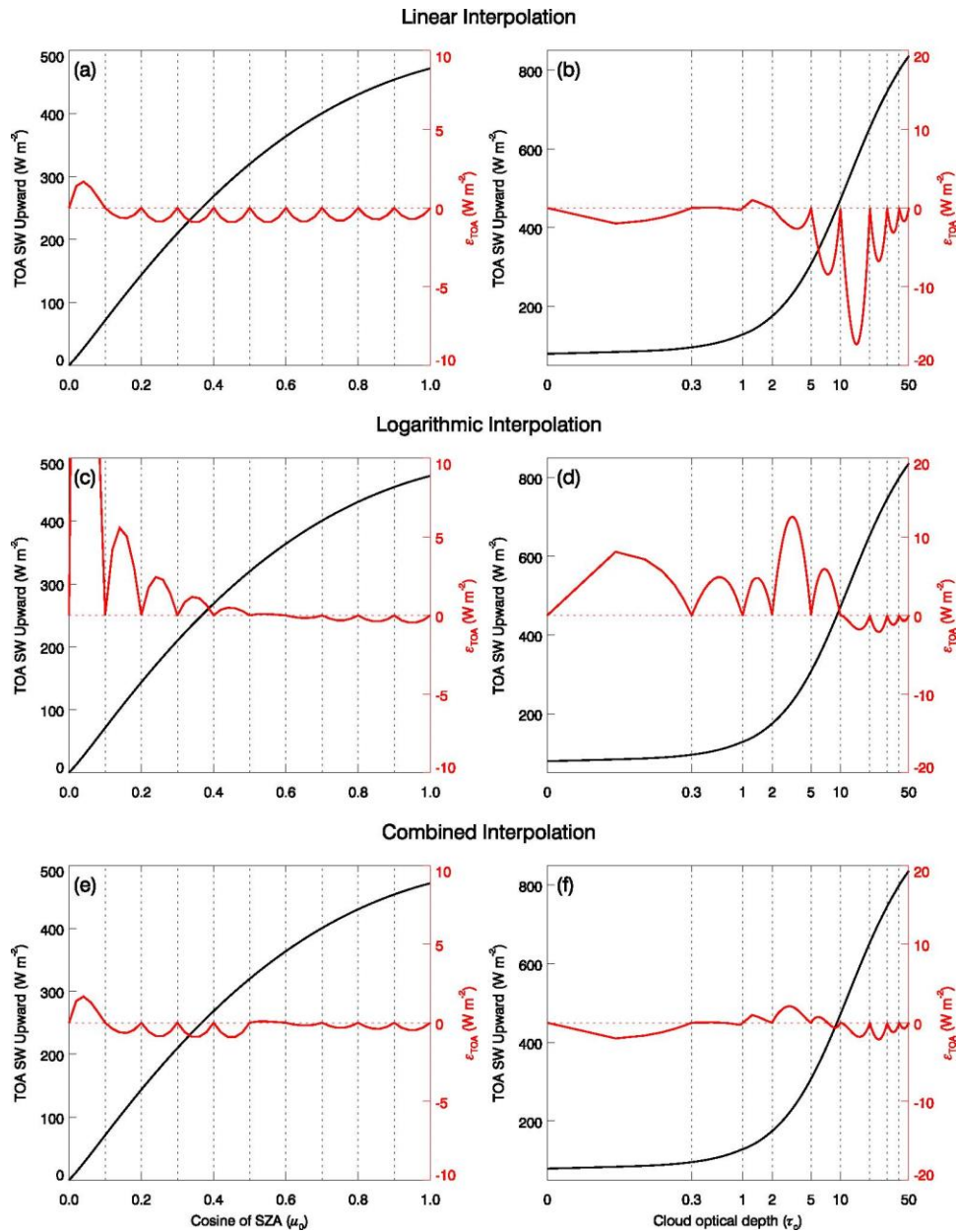


1064

1065

1066 Figure A2: Standard deviations (σ_{Batch}) of (a) TOA upward SW irradiances and (b) surface
 1067 downward SW irradiances for various numbers of photons in the MC method. The results of the
 1068 MC method (black symbols and lines) with various numbers of photons are compared with those
 1069 from the DISORT method (red symbols and lines) with various number of streams for (c) TOA
 1070 upward SW irradiances and (d) surface downward SW irradiances. The cosine of solar zenith
 1071 angle (μ_0) = 1.0 and cloud optical depth = 10 are used for the simulations. Water clouds located
 1072 at 2–3 km over ocean are placed in the Midlatitude-summer profile (MLS) atmosphere.

1073



1074

1075 Figure B1: Black lines are SW TOA irradiances as a function of cosine of solar zenith angle (μ_0)

1076 with $\tau_c = 10$ (left column) and cloud optical depth (τ_c) with $\mu_0 = 1$ (right column). Red lines are

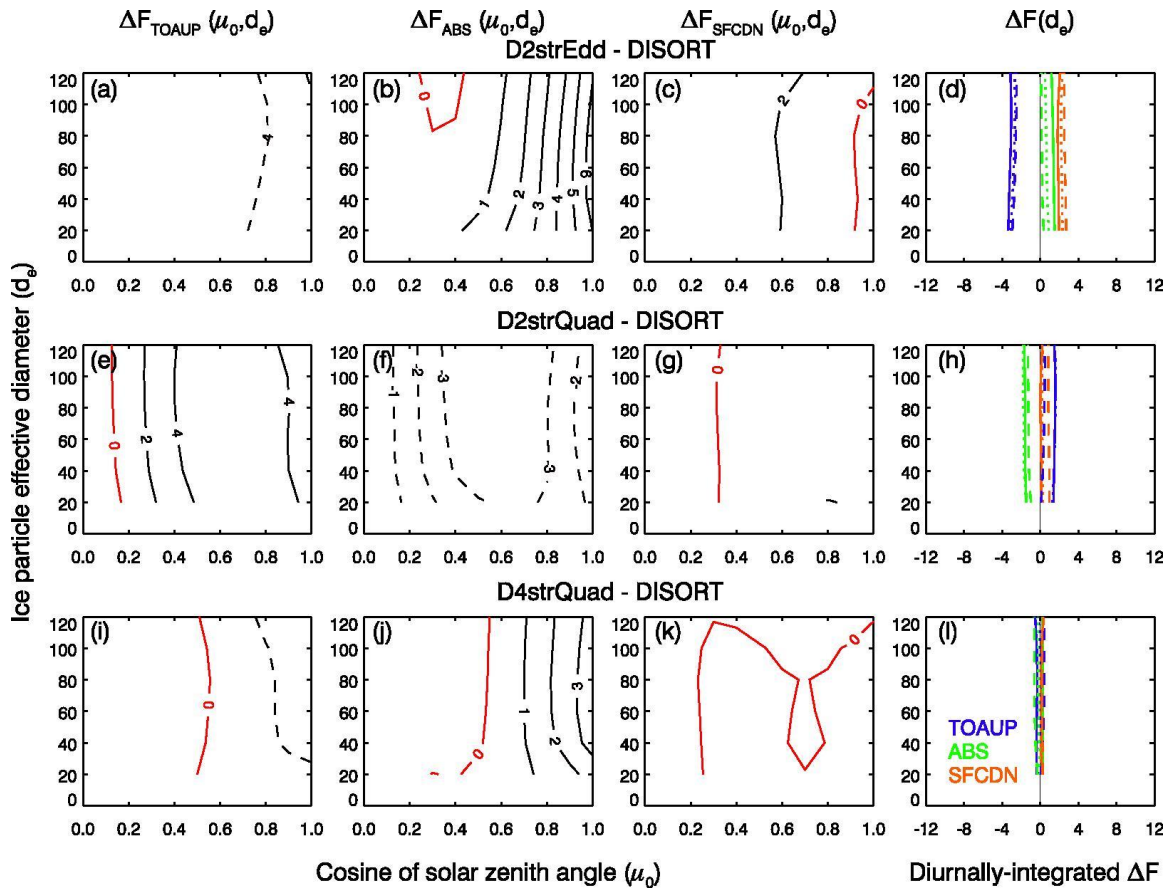
1077 interpolation errors (ϵ_{TOA}) when the linear (the first row), logarithmic (the second row), and

1078 combined interpolation (the third row) are used. The combined method is described in Appendix

1079 B. Vertical dashed lines are cosine of solar zenith angle (left column) or cloud optical depth

1080 (right column) bins used in the look-up-table (LUT).

1081



1083

1084

1085 Figure C1: Same as Fig. 3 but for instantaneous biases as a function of the cosine of solar zenith

1086 angle (μ_0) and ice particle effective diameter (d_e) are given for TOA upward (the first column),

1087 atmosphere-absorbed (the second column), and surface downward (the third column) SW

1088 irradiances. Using the three examples of diurnal variations of μ_0 in Fig. 2 (solid, dashed, and

1089 dotted lines), the instantaneous biases are integrated for TOA upward (blue), atmosphere-

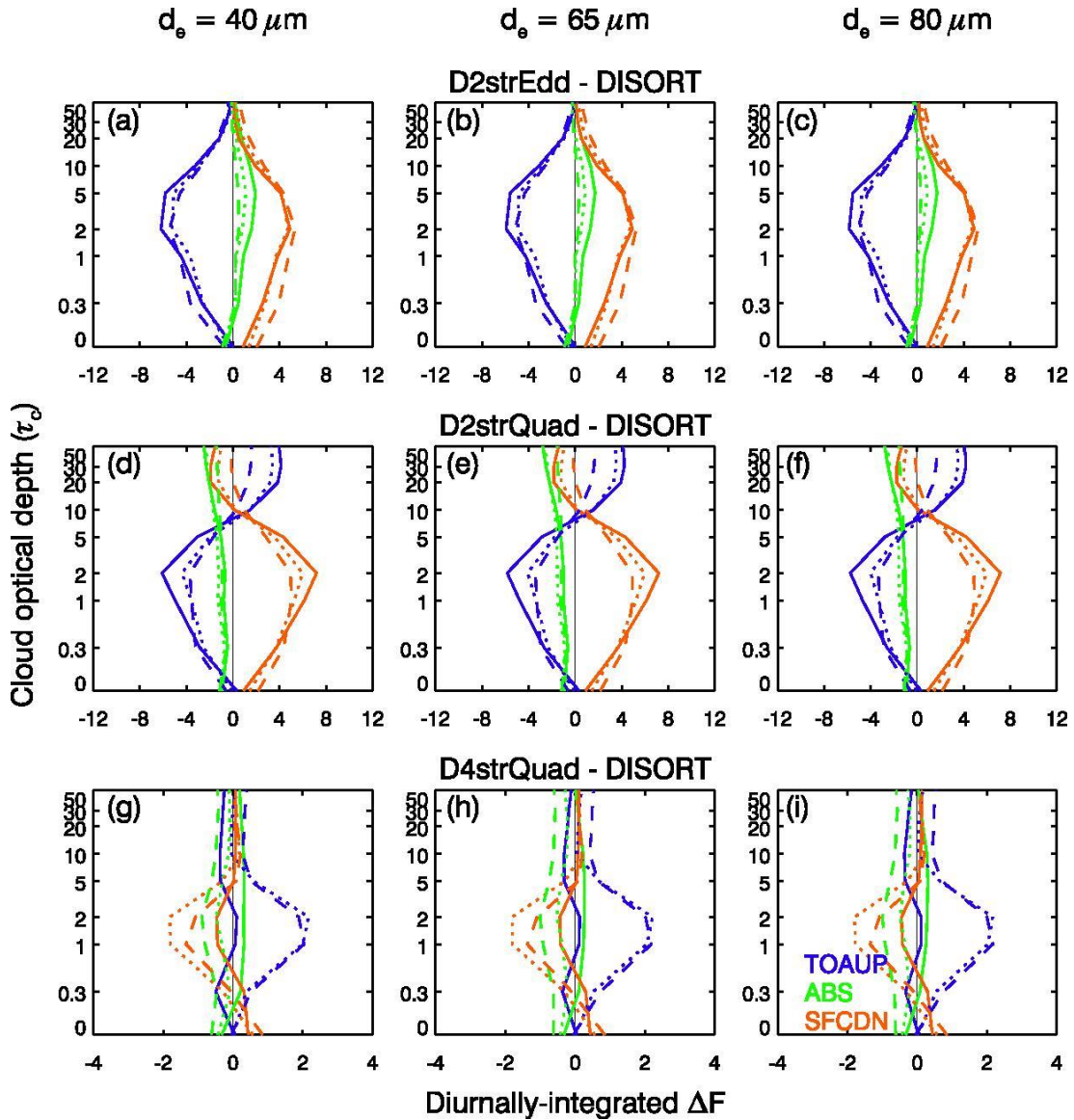
1090 absorbed (green), and surface downward (orange) irradiance in the four column. The simulation

1091 is performed for ice clouds over ocean with the mid-latitude summer (MLS) profile. Cloud top

1092 and base heights of the cloud layer are 10 and 12 km, respectively. The cloud optical depth of 10

1093 is used. The unit of biases is W m^{-2} .

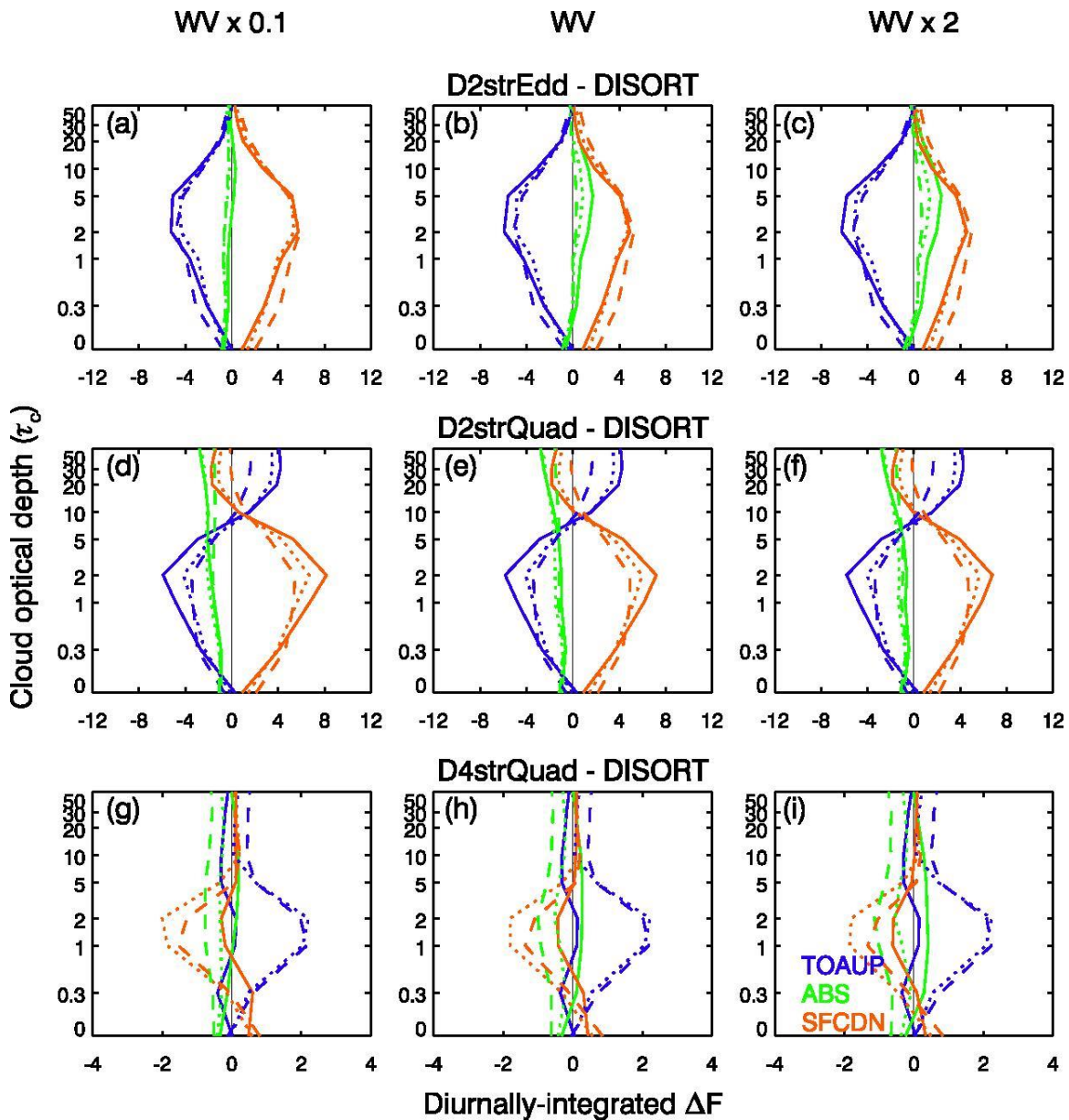
1094



1095

1096 Figure C2: Diurnally-integrated biases in TOA upward (blue lines), atmosphere-absorbed (green
 1097 lines), and surface downward (orange lines) irradiances using the three examples of cosine of
 1098 solar zenith angle (μ_0) variations in Fig. 2. Three ice effective diameter (d_e) values as = 40 μm
 1099 (left column), 65 μm (middle column), and 80 μm (right column) are used over ocean. The
 1100 biases of the D2strEdd, D2strQuad, and D4strQuad methods are given in the first, second, and
 1101 third row, respectively. Ice clouds at 10–12 km in MLS atmosphere are considered. The unit of
 1102 biases (ΔF) is W m^{-2} .

1103

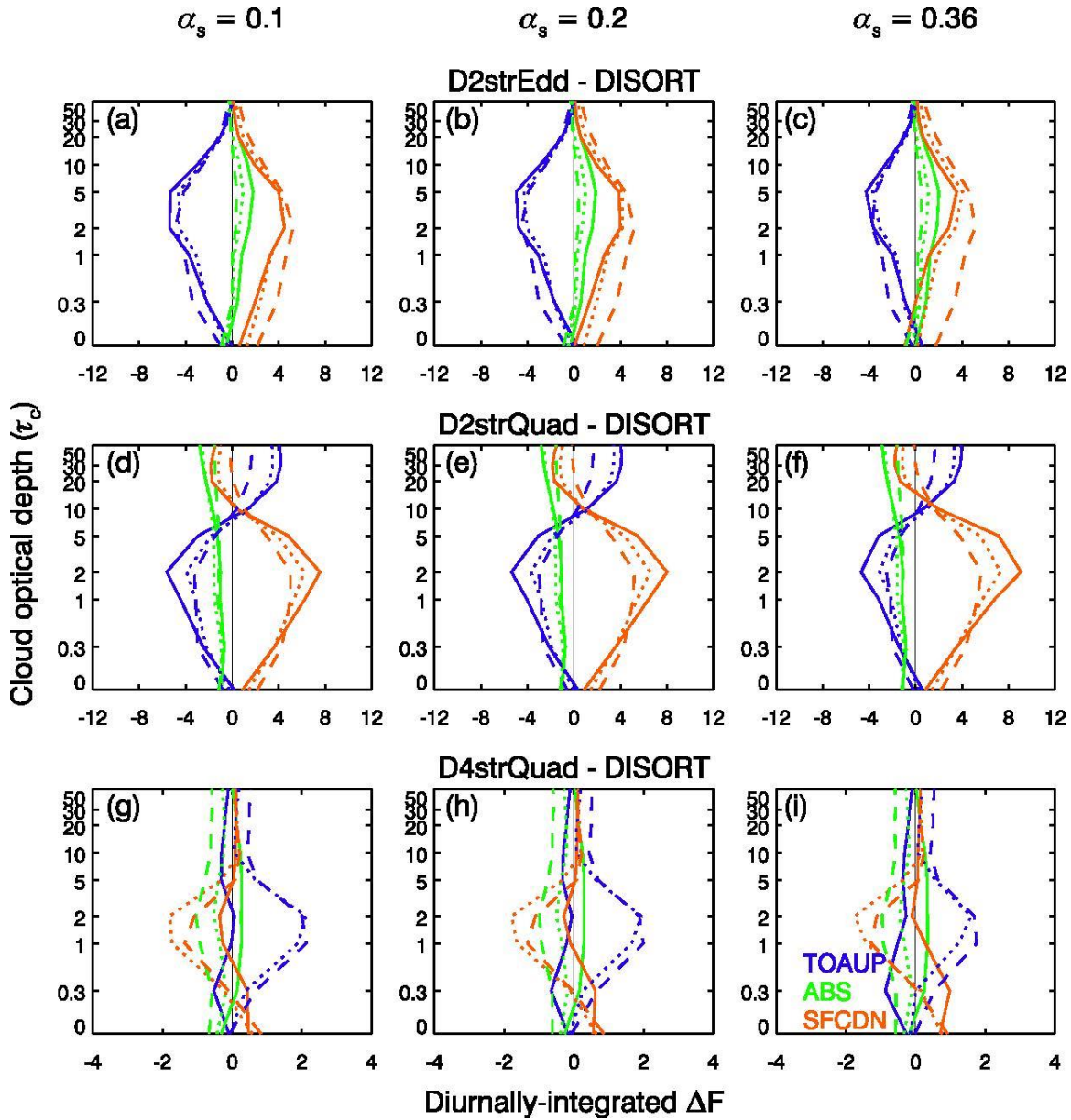


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1105

1106 Figures C3: Same as Fig. C2 but for three different water vapor profiles as MLS water vapor
 1107 profile scaled by 0.1 (left column), MLS water vapor profile (middle column), and MLS water
 1108 vapor profile scaled by 2 (right column). Ice clouds with a particle size of $d_e = 65 \mu\text{m}$ and 10–12
 1109 km altitude are assumed over ocean. The unit of biases (ΔF) is W m^{-2} .

1110



1111

1112 Figure C4: Same as in Fig. C2 but for three different land surface albedos (α_s) as 0.1 (left
 1113 column), 0.2 (middle column), and 0.36 (right column). Ice clouds with a particle size of $d_e = 65$
 1114 μm and 10–12 km altitude are assumed over ocean in MLS atmosphere. The unit of biases (ΔF)
 1115 is W m^{-2} .