Modeling and control of doubly fed induction generator with a disturbance 1 observer: A stator voltage oriented approach 2 E.Emre ÖZSOY⁽¹⁾, Edin GOLUBOVIC⁽²⁾, Asıf ŞÂBANOVIC⁽³⁾, 3 Seta BOGOSYAN⁽⁴⁾, Metin GÖKASAN⁽⁵⁾, 4 ^(1,4,5) Istanbul Technical University, Istanbul, Turkey 5 ^(1,4){eozsoy,gokasan}@itu.edu.tr,⁽³⁾ sbogosyan@alaska.edu 6 ^(2,3)Sabanci University, Istanbul, Turkey, 7 {edin,asif}@sabanciuniv.edu 8 Abstract—The popularity of renewable energy conversion systems, especially wind 9 energy has been increasing in recent years. Doubly fed induction generator (DFIG) 10 based wind energy systems are intensively used due to their wide range of active and 11 reactive power controllability. Conventional DFIG control structures consist of 12 13 decoupled PI rotor current controllers with stator flux orientation and machine parameter dependent compensating terms. The accuracy of stator flux calculation is 14 15 dependent on how accurately the stator resistance is known. Integration problems also 16 exist and additional low pass filters are implemented to accurately calculate the stator flux. In this study, machine dependent compensating terms are estimated with a first 17 order low pass filter disturbance observer. Therefore, a single proportional (P) controller 18 is sufficient to control decoupled rotor currents. The proposed controller structure is 19 implemented on a Matlab/Simulink platform with the parameters of 500KW DFIG used 20 in MILRES (Turkish National Wind Energy) project. The proposed controller is also 21 experimentally validated in an experimental setup. 22 23 **Keywords;** Doubly fed induction generator, disturbance observer, wind energy

24 Symbol Nomenclature

25	i_{sa} , i_{sb} , i_{sc}	: Stator a, b and c phase currents	<i>i_{sd}, i_{sq}</i> :	Stator d and q axis currents
26	i _{ra} , i _{rb} , i _{rc}	: Rotor a, b and c phase currents	i _{rd} , i _{rq} :	Rotor d and q axis currents

1	V _{sa} , V _{sb} ,	v_{sc} : Stator a, b and c phase voltages	V_{sa} , V_{s}	$_{s\beta}$: α and β axis stator voltage
2	V _{ra} , V _{rb} ,	v_{rc} : Rotor a, b and c phase voltages	v _{sd} , v	<i>v_{sq}</i> : Stator d and q axis voltages
3	V _{rd} , V _{rq}	: Rotor d and q axis voltages	R_s , R_s	<i>r</i> : Stator and rotor resistances
4	<i>P</i> _{<i>s</i>} ,	: Stator Active Power	Q_s	: Stator reactive Power
5	L_s , L_r	: Stator and rotor inductances	L_m	: Mutual inductance
6	L_{rb}	: Base value of rotor inductance	ΔL_r	: Disturbance of L_r
7	р	: Number of pole pairs	ω_s	: Stator electrical speed
8	ω_m	: Rotor mechanical speed	T_m	: Mechanical Torque
9	T _e	: Electrical Torque	b	: Viscous friction constant
10	$ heta_s$: Stator electrical angle	$ heta_r$: Rotor electrical angle
11	T_s	: Sample Time	S	: Laplace operator
12	k _p , k _q	: Proportional gain of controller		

13 **1. Introduction**

14 Research on renewable energy conversion systems is of great importance due to the rapid consumption of fuel resources and environmental issues. Wind energy 15 conversion systems appear to be the fastest growing technology and most of the 16 electrical energy generated by renewable sources is from wind energy conversion 17 systems [1]. DFIG based wind turbines have important advantages compared to other 18 19 wind energy conversion systems. For example, 30% of rated stator power is sufficient for 20 the rotor side inverter circuit to achieve 4-quadrant stator active and reactive power flow 21 with a speed variation around $\pm 25\%$. This reduces the cost and complexity of the overall 22 system.

1 Considerable research studies are encountered about DFIG modeling and control 2 in the literature. DFIG dynamic equations are fully written in [1, 2]. A complete 3 simulation and modeling for high power DFIG wind farms are given in [3]. Reduced 4 order DFIG dynamic model was also proposed in this study due to simulation 5 constraints.

6 From orientation frame point of view, basically, stator flux [4] and stator voltage 7 orientation [5] can be encountered in which the position of the stator-flux or voltage 8 space vector is aligned with the d-axis of the d-q frame. Stator flux orientation control techniques are dependent on the accuracy of stator resistance information. Integration 9 problems also exist and additional low pass filters are implemented to accurately 10 calculate stator flux [4]. The effect of stator resistance value can be neglected in flux 11 calculation and stator voltage orientation could be applied by adding 90° phase shift to 12 voltage angle. This may cause additional coupling effect in active and reactive power 13 14 control, which can be compensated by implementing additional controllers in the outer loop as given in [5]. It is claimed in [6] that controller performances of both orientation 15 frames are equivalent. 16

The idea of stator voltage orientation with disturbance observer starts with [7]. The scheme of [7] consists of simulation results of direct stator active and reactive power control with disturbance observer.

20 Synchronization is also another issue to smoothly connect DFIG to the grid. Grid 21 and generated stator voltages must be collinear, which means that equal in phase and 22 amplitude, before DFIG is connected to the grid to prevent high currents. Majority of

the contributions focus on a mode of operation that DFIG is already connected to the grid. Synchronization procedure is comprehensively analyzed in [8] with important citations.

There are also considerable research studies which are looking from different control perspectives. Direct power control strategies which directly control stator power without rotor current control loops are reported in [9, 10]. Sliding mode controller structures [11, 12] are also important contributions which deal with energy maximization and robustness against disturbances. There are also reputable studies which consider robustness against grid voltage problems [13, 14, 15].

10 This study focuses on designing a novel robust stator voltage oriented DFIG controller structure with low pass filter first order disturbance observer. The main 11 contribution of this paper is to achieve a simpler controller compared to basic 12 conventional schemes given in [4, 5]. Machine dependent compensating terms are 13 14 accurately estimated with the first order low pass filter disturbance observer. This prevents the necessity to accurately know the machine parameters which may 15 deteriorate according to physical conditions. Decoupled proportional rotor current 16 controllers are sufficient to separately control stator active and reactive power. The 17 parameters of the actual 500KW DFIG in the MILRES (National Wind Energy 18 Systems) project are used for the Matlab/Simulink based system model. The proposed 19 current controller is also implemented on 1.1KW DFIG experimental test bed. 20

The rest of the paper is organized as follows. The dynamic equations of DFIG are given in chapter 2. Chapter 3 provides a controller structure based on a first order

disturbance observer. Simulation results of the proposed control structure are
 demonstrated in chapter 4. Experimental results are in chapter 5. Finally, 6th chapter
 gives the conclusion and proposes the future work.

4 5

2. DFIG Dynamic Equations

Before writing the dynamic equations L_r value could be written as follows.

$$6 L_r = L_{rb} + \Delta L_r (1)$$

7 L_{rb} is the inductance value at fundamental frequency. ΔL_r is the value which is affected 8 by frequency and other physical disturbances. DFIG dynamic equations in [1, 2] can be 9 rewritten as follows;

10
$$V_{s} = L_{s} \frac{dI_{s}}{dt} + R_{s}I_{s} + L_{m} \frac{dI_{r}}{dt} + M_{s}(I_{s} + M_{r}I_{r})$$
(2)

11
$$V_r = L_{rb} \frac{dI_r}{dt} + \Delta L_r \frac{dI_r}{dt} + R_r I_r + L_m \frac{dI_s}{dt} + N_s (I_r + N_r I_s)$$
(3)

12 The matrices V, I, M and N are defined as follows;

13
$$\mathbf{V} = \begin{bmatrix} \mathbf{V}_{d} & \mathbf{V}_{q} \end{bmatrix}^{\mathrm{T}} I = \begin{bmatrix} i_{d} & i_{q} \end{bmatrix}^{\mathrm{T}}$$
(4)

14
$$M_s = \begin{bmatrix} 0 & L_s \omega_s \\ -L_s \omega_s & 0 \end{bmatrix}, \qquad M_r = \begin{bmatrix} 0 & \frac{L_m}{L_s} \\ -\frac{L_m}{L_s} & 0 \end{bmatrix}$$
 (5)

15
$$N_s = \begin{bmatrix} 0 & L_s \omega_s \\ -L_s \omega_s & 0 \end{bmatrix}$$
, $N_r = \begin{bmatrix} 0 & \frac{L_m}{L_r} \\ -\frac{L_m}{L_r} & 0 \end{bmatrix}$ (6)

All the rotor variables are referred to the stator side. The electromagnetic torque can begiven as;

18
$$T_{em} = \frac{3}{2} p L_m (i_{rd} i_{sq} - i_{rq} i_{sd})$$
 (7)

19 Stator active and reactive Power equations can be written as;

1
$$P_{s} = \frac{3}{2} (v_{sd} i_{sd} + v_{sq} i_{sq})$$
 (8)

2
$$Q_s = \frac{3}{2}(v_{sq}v_{sd} - v_{sd}i_{sq})$$
 (9)

3 The equation of motion can be given as;

$$4 \quad \frac{d\omega_m}{dt} = \frac{1}{J} \left(T_m - T_e + b. \, \omega_m \right) \tag{10}$$

5 **3. Control System**

6 **3.1 Stator Voltage Angle Calculation**

Rotating frames could be differently aligned in the literature. Stator voltage angle is aligned with d axis, with $v_s=v_{sd}$ and $v_{sq}=0$. The voltage vectors and reference frames are in figure 1.

10 The voltage angle could be calculated by using,

11
$$\theta_s = \arctan(\frac{v_{s\beta}}{v_{s\alpha}})$$
 (11)

However, phase lock loop (PLL) techniques which are more robust against 12 13 voltage disturbances are widely used for phase and frequency detection of the voltage 14 signal. Different PLL techniques could be encountered in the literature [16]. A basic PLL algorithm which is given in figure 2 is used in simulations and experiments of this 15 16 study. Grid voltages, transformed into dq coordinate system are the inputs of the algorithm. Q component of the voltage could be forced to be zero with a PI controller. 17 18 Output of the PI controller is the grid frequency. Integration of the grid frequency is the position of the signal. This position is used in the abc-dq calculation. 19

1 **3.2 Design of Current Controllers**

DFIG rotor voltage equation in (3) must be rewritten to simply design proportional rotor current controllers. All currents and voltages could be measured in real applications without any problems. However, machine parameters may deteriorate according to physical conditions. The aim of rewriting the equations is to separate the machine dependent and independent terms. Therefore, a simpler controller structure could be achieved. Rotor dynamics in (3) could be rewritten as follows;

$$8 \qquad \frac{dI_r}{dt} = \frac{V_r}{L_{rb}} + \left(\underbrace{-\frac{R_r}{L_r}V_r - \frac{L_m}{L_r}\frac{dI_s}{dt} + N_s(I_s + N_rI_r) - \Delta L_r\frac{dI_r}{dt}}_{V_r^{dis}}\right) \tag{12}$$

9 The vector V_r^{dis} is defined as $V_r^{dis} = \begin{bmatrix} v_{rd}^{dis} & v_{rq}^{dis} \end{bmatrix}$ that is considered as parameter 10 dependent disturbance terms. Equation (12) could be simplified as follows.

11
$$\frac{\mathrm{dI}_{\mathrm{r}}}{\mathrm{dt}} = \frac{\mathrm{V}_{\mathrm{r}}}{\mathrm{L}_{\mathrm{rb}}} + \mathrm{V}_{\mathrm{r}}^{\mathrm{dis}}$$
(13)

12 Derivative of errors for rotor currents can be written as;

13
$$\frac{d\varepsilon_{\rm r}}{dt} = \frac{dI_{\rm r}^{\rm ref}}{dt} - \frac{dI_{\rm r}}{dt}$$
(14)

- 14 Where $\varepsilon_{rd} = \begin{bmatrix} \varepsilon_{rd} & \varepsilon_{rq} \end{bmatrix}^T$
- 15 (13) and (14) could be written with (14) as follows;

$$16 \qquad \frac{d\varepsilon_r}{dt} = -\frac{V_r}{L_{rb}} - \left(-\frac{dI_r^{ref}}{dt} + V_r^{dis}\right) \tag{15}$$

17 Next, the desired closed loop dynamics can be written as;

$$18 \quad \frac{d\varepsilon_r}{dt} + K\varepsilon_r = 0 \tag{16}$$

- 19 Where $K = \begin{bmatrix} k_d & k_q \end{bmatrix}$ is defined as proportional controller gain.
- 20 If (15) is written to (16) desired closed loop dynamics is rewritten as follows;

$$1 \qquad -\frac{V_r}{L_{rb}} + \left(\frac{dI_r^{ref}}{dt} + V_r^{dis}\right) - K\varepsilon_r = 0 \tag{17}$$

2 Rotor voltage equations could be obtained by rewriting (17)

3
$$V_r^{\text{ref}} = L_{rb} \left(\frac{dI_r^{\text{ref}}}{dt} + V_r^{\text{dis}} + K\varepsilon_r \right)$$
(18)

4 If the effect of $\frac{dI_r^{ref}}{dt}$ is neglected, control effort could be expressed as follows.

5
$$V_r^{\text{ref}} = V_r^{\text{dis}} + L_{rb} K \varepsilon_r$$
 (19)

6 **3.3 Disturbance Observer**

In this section, the derivation of the disturbance observer is presented. The vector V_r^{dis} is the disturbance term which is dependent on physical conditions. Controller structure could be finalized, if the disturbances are correctly estimated.

10
$$V_r^{\rm dis} = V_r - L_{\rm rb} \frac{\mathrm{d}I_r}{\mathrm{d}t}$$
(20)

Writing (22) in s domain and implementing first order low pass filter disturbance
observer concept [17];

13
$$\widehat{V}_{r}^{dis} = (V_{r} - L_{rb} \frac{dI_{r}}{dt}) \frac{g}{s+g}$$
(21)

14 The estimation error can be expressed as;

15
$$V_r^{dis} - \hat{V}_r^{dis} = (V_r - L_{rb} \frac{dI_r}{dt}) - (V_r - L_{rb} \frac{dI_r}{dt}) \frac{g}{s+g} = (1 - \frac{g}{s+g}) V_r^{dis}$$
 (22)

The estimation error converges to zero. The vector $\hat{V}_{rd}^{dis} = [\hat{v}_{rd}^{dis} \ \hat{v}_{rq}^{dis}]$ is parameter dependent estimated disturbance. The term g is the cut-off frequency of the low pass filter in radians. It is obvious from (21) that \hat{v}_{rd}^{dis} and \hat{v}_{rq}^{dis} are independent from machine parameters. As a result, block diagram in figure 3 can be obtained. Decoupled control of active and reactive power could be achieved by controlling i_{rq} and i_{rd} respectively. This control structure can be implemented in speed, torque or power
control of DFIG. Maximum power point tracking (MPPT) algorithms can be followed
according to any wind turbine dynamics.

4

4. Simulation Results

5 More accurate simulation platform is obtained compared to [3] without necessity 6 of reduced order models by using discretized model of DFIG. 100µs sample time in 7 Matlab/Simulink is used in simulations. Inverter dynamics are neglected. 500KW DFIG 8 parameters [18] which will be used in MILRES project is given in Table 1. All the rotor 9 parameters are referred to the stator side. Control system can work in different scenarios. 10 In this study, generator is controlled according to speed control strategy.

Machine parameters dependent compensating terms of control structure is 11 estimated by disturbance observer. Basically, two different step response tests are 12 applied in one simulation at different time instants. Speed reference is changed from 60 13 to 90 rad/s (from sub synchronous to super synchronous speed) at 10th second. Wind 14 torque reference is changed from 3000Nm to 5000Nm at 12th second. It is expected that 15 system must follow the speed (Figure 4) and wind torque (Figure 5), while accurately 16 estimating disturbance terms. There is a huge current torque and current increase at 10th 17 second of simulation. The reason of high current and torque is the speed step which is 18 deliberately applied with a high speed controller gain in order to check the performance 19 of the controller structure. Control system could handle this dramatic step and kept 20 21 stable. i_{rd} reference (Figure 6) is kept zero during the simulations.

It is obviously seen from the simulation results that DFIG dynamic model works properly and compensating terms are accurately estimated by disturbance observer (Fig. 9-10). Rotor power is changing the direction while the speed changes from subsynchronous to supersynchronous speed (Figure 8). Active and reactive stator powers are decoupled (Figure 7). Performance of the speed controller could be modified (Figure 4) according to physical conditions. However, focus of the simulation results is accurately estimating compensating terms.

8

5. Experimental Results

9 Experimental setup in Figure 11 is used in the experiments. A squirrel cage induction machine (SCIM) driven by a commercial inverter which represents the wind. 10 DFIG plate data is given in Table 2. Controller algorithm is generated in dSPACE 11 DS1103 by using Controldesk C language. Sample time of the control structure is 12 100µs. Semikron Semistack (21f b6u e1cif b6ci 12 v12) inverter used in 13 14 experiments and 120VDC constant voltage power is directly applied to DC link. 15 Switching frequency is 10 kHz. Low pass filter cut-off frequency (g) is chosen as 1200. Proportional gains of the controllers (k_p and k_q) are 100. These values are found in trial 16 17 and error method in the experiments without any algebraic calculations.

18

5.1 Experiment 1

The aim of the first experiments is to show that decoupled control of I_{rd} and I_{rq} rotor currents separately changes the stator active and reactive power respectively. DFIG is rotated in constant subsynchronous speed by SCIM. I_{rd} and i_{rg} step response tests are

applied in different experiments, and the change of stator reactive and active power is
 demonstrated respectively.

It is obvious from the experimental results that both rotor current controllers accurately change stator active and reactive power (Figure 13 and 16). Compensating terms also change (Figures 14 and 17)when step responses are applied.

6

Experiment 2

The main objective of DFIG based wind turbines is decoupled control of active and reactive power. Control structure given in figure 3 is implemented by using basic PI power controllers in the outer loop while generator is driven by SCIM at arbitrary speed. Active and reactive power step response tests are applied and decoupled control of active and reactive stator power could be achieved.

12 Conclusion

5.2

Decoupled control of active and reactive power with a first order low pass filter disturbance observer is fully demonstrated with the simulation and experimental results. It is shown that compensating terms are accurately estimated by the disturbance observer in simulations. Experimental results validate the accuracy of the proposed control method by effectively achieving stator active and reactive power flow.

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TABLES

Fable 1.	DFIG	parameters	in	simulati	ion
1 4010 1.		parameters		Sillianat	.011

Stator Power (P _s)	457.6	KW
Rotor Power (P _r)	61.4	KW
Stator Voltage	690	V
Number of Poles (p)	4	
Slip Variation	0.25	
Nominal Torque	6784	Nm
Synchronous Speed	750	rpm
Stator Resistance (R _s)	0,018	ohm
Rotor Resistance (R _r)	0,021	ohm
Mutual Inductance (L _m)	0,011	Η
Stator Inductance (L _s)	0,012	Н
Rotor Inductance (L _r)	0,012	Н
Turn Ratio (n _s /n _r)	4	
Moment of Inertia	22	kgm ²

Power	1,1	KW
Stator Voltage	220/380	V (D/Y)
Stator Current	6,4/3,7	А
Power Factor	0,67	
Speed	1360	rpm
Rotor Voltage	70	V
Rotor Current	12	А