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Dark-state adiabatic passage with spin-one particles

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Adiabatic transport of information is a widely invoked resource in connection with quantum information processing and distribution. The study of adiabatic transport via spin-half chains or clusters is standard in the literature, while in practice the true realization of a completely isolated two-level quantum system is not achievable. We explore here, theoretically, the extension of spin-half chain models to higher spins. Considering arrangements of three spin-one particles, we show that adiabatic transport, specifically a generalization of the dark-state adiabatic passage procedure, is applicable to spin-one systems. We thus demonstrate a qutrit state transfer protocol. We discuss possible ways to physically implement this protocol, considering quantum dot and nitrogen-vacancy implementations.

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I. INTRODUCTION

The communication of information around small quantum networks is becoming increasingly important as the control and design of such quantum systems becomes more advanced. There are now many different approaches to such transport [1] and the choice of the "best" protocol for a given task depends on the size of the quantum system and the level of control that can be applied to it.

One class of transport protocols that is of interest is the set of protocols inspired by adiabatic passage. Generically, adiabatic passage is the controlled evolution of a quantum system from an initial to a final state, so as to maintain the system in an instantaneous eigenstate throughout, by means of control of both tunnel matrix elements and on-site energies. The canonical example of adiabatic passage is perhaps stimulated Raman adiabatic passage (STIRAP) [2] (see Refs. [3,4] for a good discussion of this, and related adiabatic techniques). Here, an excitation (typically an electron) is moved between energy levels in a three-or-more-level atomic system. The only control is via coherent electromagnetic fields (e.g., lasers) and the so-called counterintuitive pulse sequence (defined below) is employed.

Although many extensions of STIRAP are possible, in general the natural restrictions of using atomic systems can limit what is possible or practical. However, combining STIRAP techniques with spatially engineered systems mitigates this restriction somewhat, as seen in original work applying STI-RAP techniques to double quantum dot systems [5,6]. Later, full spatial variants of STIRAP were explored, including the coherent tunneling adiabatic passage (CTAP) approach, which has been studied in the context of atoms in triple well potentials [7], superconductors [8], electrons bound to quantum dots and to donors [9], Bose-Einstein condensates [10,11], photons in waveguides [12,13], and Bose-Hubbard systems [14]. Again, the main strength of CTAP derives from the ability to engineer

the Hilbert space for certain functions, and in this context there exist applications for quantum information transport [9,15], adiabatic splitting and operator measurements [16,17], quantum gates [18], interferometry [19,20], and branching structures for interaction-free measurement [21] and multiport splitting [22]. Most generally, adiabatic passage techniques can be understood as implementing generalized Morris-Shore transformations [23,24].

Another scheme related to STIRAP that also takes advantage of Hilbert-space engineering is dark-state adiabatic passage (DSAP) [25,26]. The dark state in a three-level Λ system is an eigenstate, which has no overlap with the excited state, and is the eigenstate that is utilized by the STIRAP process. DSAP is named for the multispin generalization of this state, although, technically, the term dark state is not meaningful in DSAP as there is no requirement for an optically active excited state to be present in the system. In DSAP, a spin chain is considered with adiabatically controlled spin-spin couplings. Formally, if the chain is a one-dimensional array of spin-1/2 particles, then it is easy to see how to translate the particle hopping approach of CTAP to the spin propagation via spin-spin coupling in DSAP. More generally, spin chains offer the possibility of creating quantum wires for solid-state quantum computers [1].

Here we consider DSAP in a system of three spin-one particles or, equivalently, qutrits depicted schematically in Fig. 1(a). We show that this system can exhibit DSAP in a fashion equivalent to that seen in spin-1/2 systems, but it also introduces richer evolution, which is more akin to alternating adiabatic passage protocols with five states [27–29], and that observed in the Bose-Hubbard treatment [14]. We discuss two methods of implementation, with the first based on complete control of the three-spin Hamiltonian, such as might be expected in triple dot structures, and the second using magic-angle control, such as would be appropriate for dipolar coupled particles.

There has been relatively little work on quantum transport in spin-one chains, compared with that of spin-half chains, and certainly we are not aware of adiabatic passage techniques in these systems. Understanding of the transport in spin-one

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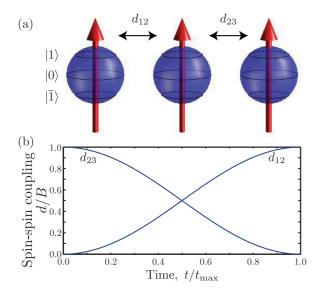


FIG. 1. (Color online) (a) Schematic representation of the three-spin system. Individual spin states are labeled according to their z projection and spin-spin coupling is nearest neighbor only. (b) Dark-state adiabatic passage is effected by varying the couplings according to the counterintuitive pulse sequence, in this case illustrated using sinusoidal modulation of d_{12} and d_{23} .

chains ultimately seems to derive from the Haldane [30] and Affleck *et al.* (AKLT) studies for a spin-one Heisenberg chain [31], and typically focuses on the properties of the elementary excitations with the chains (e.g., Refs. [32–35]) or in some cases teleportation-based transport [36–38] or entanglement swapping [39].

II. DARK-STATE ADIABATIC PASSAGE WITH SPIN-ONE PARTICLES

Our treatment of the adiabatic passage protocol is applicable to many systems. All that is required is three effective spin-one systems with controllable nearest-neighbor coupling. The generic, nearest-neighbor Hamiltonian can be expressed as a function of time t (with $\hbar=1$) as

$$\mathcal{H} = B \sum_{i=1}^{3} J_{z,i} + [d_{12}(t)J_{1}^{+}J_{2}^{-} + d_{23}(t)J_{2}^{+}J_{3}^{-} + \text{H.c.}],$$
(1)

where B is the (possibly time-varying) Zeeman energy associated with the magnetic field, $J_{z,i}$ is the spin projection operator along the z axis for particle i, J_i^+ (J_i^-) is the spin raising (lowering) operator for particle i, and $d_{ij}(t)$ is the time-varying (gated) coupling energy between (nearest-neighbor) particles i and j. We label the states of the particles according to their z projection as $|1\rangle$, $|0\rangle$, and $|\bar{1}\rangle$. For a given state ψ , we define the population in a given basis state as $P_{\alpha,\beta,\gamma}=|\langle\alpha,\beta,\gamma|\psi\rangle|^2$ for $\alpha,\beta,\gamma=\bar{1},0,1$. The passage involves "moving" the state of a given spin, for example a 0, from particle 1 to particle 3 during the interval from t=0 to $t=t_{\rm max}$, such that at t=0 the system is in the state $|0,\alpha,\alpha\rangle$ and at $t=t_{\rm max}$ the system is in the state $|\alpha,\alpha,0\rangle$ for particular spin projections α . The restrictions on the allowed α for DSAP are discussed below.

Adiabatic passage implementation involves the counterintuitive pulse ordering such that $d_{12}(0) \rightarrow 0$, $d_{23}(0) \gg d_{12}(0)$ and $d_{23}(t_{\text{max}}) \rightarrow 0$, $d_{12}(t_{\text{max}}) \gg d_{23}(t_{\text{max}})$, with the $d_{jk}(t)$ smoothly varied throughout the protocol (although even this restriction is not absolute; see, for example, piecewise adiabatic passage [40] and digital adiabatic passage [41]). The counterintuitive pulse sequence is named for the fact that the state to be transferred is initially uncoupled, while the non-transferred states are initially strongly coupled. This sequence admits an infinite amount of possible implementations and, for simplicity and definiteness, we choose

$$d_{12}(t) = d \sin^2(\pi t / 2t_{\text{max}}),$$

$$d_{23}(t) = d \cos^2(\pi t / 2t_{\text{max}}),$$
(2)

where d is the maximum coupling, and the total time t_{max} is assumed long enough to ensure adiabatic evolution. This particular sequence is shown in Fig. 1(b).

We first assume that the interspin coupling can be directly and independently controlled. This method is best suited to quantum dot implementations where gates can be used to independently control the exchange interaction between neighboring spins.

To gain insight into the dynamics of the three-spin system under the counterintuitive pulse sequence, we present the time-dependent eigenspectra in Fig. 2. We have arbitrarily set d/B=0.2 in the figure to separate the manifolds with different numbers of excitations. The full solution is relatively complicated, with several degeneracies appearing; however, it is easier to obtain insight into the dynamics if we focus our attention on each manifold of states centered around a given energy. The manifolds and evolution for $E=\pm 3B$ are trivial. These correspond to the system in $|111\rangle$ or $|\bar{1}\bar{1}\bar{1}\rangle$ states, respectively, which do not respond to the coupling interaction variations and are therefore ignored in what follows.

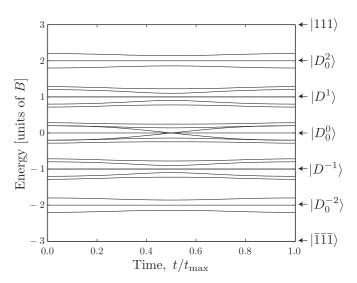


FIG. 2. Eigenspectra over the counterintuitive pulse sequence with B=1, d=0.2. The states separate into various manifolds, which are discussed in the text. Highlighted are some of the kets with constant energy throughout the DSAP protocol.

The energy levels around $E=\pm 2B$ are relatively straightforward. There are three states involved in each manifold. In the E=2B manifold, the basis states involved are $|011\rangle$, $|101\rangle$, and $|110\rangle$. These show the possibility for a DSAP-like pathway where the spin state on particle one, $|0\rangle$, is transferred

to particle three. This can equivalently be thought of as adiabatic passage of a hole along the chain, as discussed by Benseny *et al.* in the context of atomtronics [42].

For our particular pulse sequence, the eigenstates around E = 2B are

$$\left|D_0^{(2)}\right\rangle = \frac{\cos^2\left(\frac{\pi t}{2t_{\text{max}}}\right)|011\rangle - \sin^2\left(\frac{\pi t}{2t_{\text{max}}}\right)|110\rangle}{\sqrt{\cos^4\left(\frac{\pi t}{2t_{\text{max}}}\right) + \sin^4\left(\frac{\pi t}{2t_{\text{max}}}\right)}},\tag{3}$$

$$|D_{\pm}^{(2)}\rangle = \frac{\sin^2\left(\frac{\pi t}{2t_{\text{max}}}\right)|011\rangle \pm \sqrt{\frac{3+\cos\left(\frac{2\pi t}{t_{\text{max}}}\right)}{2}}|101\rangle - \cos^2\left(\frac{\pi t}{2t_{\text{max}}}\right)|110\rangle}{\sqrt{3+\cos\left(\frac{2\pi t}{t_{\text{max}}}\right)}},\tag{4}$$

with energies

$$E_0^{(2)} = 2B, \quad E_{\pm}^{(2)} = 2B \pm \frac{d}{2}\sqrt{3 + \cos\left(\frac{2\pi t}{t_{\text{max}}}\right)}.$$
 (5)

We interpret these results in the usual fashion for CTAP, namely, that when t=0, $d_{23}\gg d_{12}$, the system is initialized in the state $|D_0^{(2)}\rangle=|011\rangle$, and adiabatically following the counterintuitive pulse sequence transfers the spin 0 state from site 1 to site 3 without modifying the spin state at site 2. The calculated time evolution of the populations in this case is shown in Fig. 3. We note that the evolution presented here and all subsequent figures is calculated from a full solution of the time-varying Hamiltonian. When compared with the analytical results provided, full agreement is obtained. The evolution at E=-2B follows from exactly the same reasoning, except

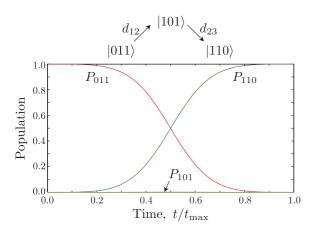


FIG. 3. (Color online) Populations in the E=2B manifold throughout the protocol determined using density matrix analysis as a function of time, confirming the DSAP evolution. The red line is P_{011} and the green line is P_{110} . Note that the system is initialized in the state $|011\rangle$ ($P_{011}=1$) and evolves to the state $|110\rangle$, staying in the state $|D_0^2\rangle$ as expected, with $P_{101}=0$ throughout the protocol. Population in the E=-2B manifold follows similarly. For this simulation, $t_{\rm max}=100B^{-1}$. The path of the adiabatic passage is schematically shown at the top, where only the lower states are populated. This representation also makes clear the connection between the DSAP pathway under consideration and STIRAP in the Λ configuration.

that in this case, the states involved are $|0\bar{1}\bar{1}\rangle$, $|\bar{1}0\bar{1}\rangle$, and $|\bar{1}\bar{1}0\rangle$. In this case, we can picture the transport as a particle moving along a chain in a CTAP process. It should be self-evident that in these one-particle and one-hole cases, *all* of the standard CTAP-like results can be obtained. In particular, extension to many-site (i.e., more than 3-site) straddling [9] and alternating geometries [28,29] will follow trivially. Also straightforward is the extension to the fractional protocol discussed in the context of STIRAP in Refs. [43] and [44], or adiabatic splitting in a five-site configuration [45]. In the DSAP case, these splittings will produce entangled states, rather than the superpositions generated in STIRAP or CTAP; however, we will not discuss these possibilities here.

The adiabaticity is a convenient way to quantify whether the system evolves along a continually varying series of connected eigenstates during evolution or is likely to make a discontinuous jump to an unrelated eigenstate [46]. Using the standard approach, we parameterize the adiabaticity for any two instantaneous eigenstates $|\phi_1\rangle$ and $|\phi_2\rangle$ as

$$A = \frac{\langle \phi_1 | \partial_t | \phi_2 \rangle}{|E_{\phi_1} - E_{\phi_2}|}.$$
 (6)

In particular, for the E=2B manifold, we have the adiabaticity between $|D_0^{(2)}\rangle$ and either of $|D_\pm^{(2)}\rangle$,

$$A^{(2)} = \frac{2\sqrt{2}\pi \sin\left(\frac{\pi t}{t_{\text{max}}}\right)}{dt_{\text{max}} \left[3 + \cos\left(\frac{2\pi t}{t_{\text{max}}}\right)\right]^{3/2}}.$$
 (7)

The remaining three manifolds at $E=\pm B$ and E=0 are not as simple due to the increase in the degeneracies. The composition of the E=-B manifold follows obviously by symmetry argument from the E=B manifold, hence we do not treat it separately.

The states comprising the E=B manifold are, in general, complicated and their form is not especially illuminating; however, the states at E=B exactly highlight an interesting adiabatic pathway for population transfer. For the E=B manifold, the degenerate spanning states may be

taken as

$$|D_1^1\rangle = \frac{1}{\sqrt{3}}(|11\bar{1}\rangle - |1\bar{1}1\rangle + |\bar{1}11\rangle),\tag{8}$$

and
$$|D_2^1\rangle = \frac{\left(-d_{12}^2 + d_{23}^2\right)|11\bar{1}\rangle - d_{23}^2|1\bar{1}1\rangle + d_{12}d_{23}|010\rangle}{\sqrt{d_{12}^4 - d_{12}^2d_{23}^2 + 2d_{23}^4}}.$$
(9)

Of course, any superposition of these states is also in the E=B eigenspace. It is convenient here to take a particular superposition,

$$|D^{1}\rangle \propto -|D_{2}^{1}\rangle + \frac{\sqrt{3}d_{23}^{2}}{\sqrt{d_{12}^{4} - d_{12}^{2}d_{23}^{2} + 2d_{23}^{4}}}|D_{1}^{1}\rangle$$

$$= \frac{d_{23}^{2}|\bar{1}11\rangle - d_{12}d_{23}|010\rangle + d_{12}^{2}|11\bar{1}\rangle}{\sqrt{d_{12}^{4} - d_{12}^{2}d_{23}^{2} + d_{23}^{4}}}.$$
 (10)

A complete discussion of adiabatic evolution in degenerate subspaces can be found in the work by Rigolin and Ortiz [47]. The state $|D^1\rangle$ is analogous to the states found with alternating STIRAP [27] and CTAP protocols with five sites (ACTAP₅) [28,29]. In the adiabatic limit with counterintuitive pulse ordering, the passage is from $|\bar{1}11\rangle$ to $|11\bar{1}\rangle$. This can be understood as transport of the $|\bar{1}\rangle$ state from spin 1 to spin 3 via the states $|001\rangle$, $|010\rangle$, and $|100\rangle$, with the populations $P_{001} = P_{100} = 0$, and transient population in state $|010\rangle$. This evolution is shown in Fig. 4.

The manifold of seven states around E = 0 is also very interesting. At time $t = t_{\text{max}}/2$ (i.e., when $d_{12} = d_{23}$), there is a clear anticrossing arising from the adiabatic passage transfer,

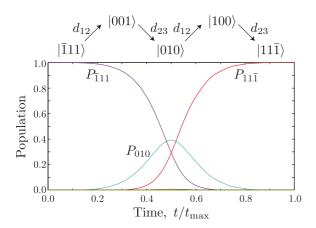


FIG. 4. (Color online) Time evolution of the populations in the E=B manifold when the starting state is $|\bar{1}11\rangle$, corresponding to evolution in the state $|D^1\rangle$. The purple line shows $P_{\bar{1}1\bar{1}}$, the cyan line shows P_{010} , and the orange line shows $P_{11\bar{1}}$. This evolution is completely analogous to the evolution observed in alternating adiabatic passage protocols with five states. The system is initially in the state $|\bar{1}11\rangle$ and evolves to the state $|11\bar{1}\rangle$, with transient population in the state $|010\rangle$.

and also a true three-state crossing. The state

$$|D_0^0\rangle = \frac{d_{23}(|01\bar{1}\rangle - |0\bar{1}1\rangle) - d_{12}(|1\bar{1}0\rangle - |\bar{1}10\rangle)}{\sqrt{2}\sqrt{d_{12}^2 + d_{23}^2}}$$
(11)

remains an eigenstate with E=0 throughout the protocol and demonstrates adiabatic passage of the spin 0 state from site 1 to site 3, with the rest of the chain in a particular entangled state.

III. OUTRIT TRANSPORT PROTOCOL

The DSAP protocols involving $|011\rangle$ and $|\bar{1}11\rangle$ are quite similar, and both can be effected by the same gate control sequence, i.e., the same variation in the $d_{ij}(t)$. Although the control sequence is the same in each case, the properties of the evolution differ quantitatively. The protocol involving $|\bar{1}11\rangle$ is slightly less adiabatic than the $|011\rangle$ protocol, which follows from the form of the null states, as discussed in Ref. [29]. We compare the rate limiting adiabaticities for the two evolutions in the $E=\pm 2B$ and the $E=\pm B$ manifolds for the transitions between the states $|D_0^{(\pm 2)}\rangle$ and $|D_\pm^{(\pm 2)}\rangle$, denoted $A^{(2)}$, with the adiabaticity between the states $|D_0^{(\pm 1)}\rangle$ and $|D_\pm^{(\pm 1)}\rangle$, denoted $A^{(1)}$. One needs to be careful about applying the adiabatic theorem within degenerate subspaces. Adiabaticities involving degenerate subspaces are taken relative to the closest states outside of the degenerate manifold. Under these conditions, we find that

$$A^{(2)}\left(t = \frac{t_{\text{max}}}{2}\right) = \frac{\pi}{t_{\text{max}}d},$$
 (12)

$$A^{(1)}\left(t = \frac{t_{\text{max}}}{2}\right) = \frac{2\pi}{t_{\text{max}}d}\sqrt{\frac{3}{7}(4+\sqrt{2})}.$$
 (13)

The presence of parallel DSAP channels in the same system suggests two interesting corollaries. First, this DSAP protocol would allow the adiabatic transport of a qutrit encoded in one of the spins, i.e., where the initial state of the chain is a superposition $\alpha |111\rangle + \beta |011\rangle + \gamma |\bar{1}11\rangle$. As $A^{(1)} > A^{(2)}$, for high-fidelity qutrit transport, the worst case adiabaticity must be used to ensure adiabatic passage for the qutrit as a whole. Note that this is an advantage of adiabatic passage, as a nonadiabatic scheme would require gate operations of precise durations, such that equal populations were transferred from each of the starting states, which is more restrictive than simply requiring high-fidelity population transfer for the states independently. Second, we can see that an error that only affects the first spin will not be communicated to the rest of the chain. Although this latter point is appealing for the purposes of quantum information transfer, it is clear that the converse is not true, and, in general, errors in the chain do affect the transport protocol.

The configuration described above, where the nondata qutrits are in the state $|11\rangle$, is not the only possible state to allow qutrit transport via DSAP. By examining the null states described above, we observe that complete qutrit transport can be achieved when the two nondata qutrits are in the states $|11\rangle$, $|\bar{1}\bar{1}\rangle$, and $(1/\sqrt{2})(|1\bar{1}\rangle - |\bar{1}1\rangle)$. Also, any superposition of these states of the chain will allow for DSAP transport, including entangled states of the form $\sin \varphi |11\rangle - \cos \varphi |\bar{1}\bar{1}\rangle$

for arbitrary φ , although we note that the state $(1/\sqrt{2})(|1\bar{1}\rangle + |\bar{1}1\rangle)$ does *not* allow qutrit transport.

IV. DIPOLE COUPLING EFFECTED VIA MAGIC-ANGLE CONTROL

Not all spin systems have obvious mechanisms to allow independent control of the spin-spin coupling via some gate mechanism. Magic-angle coupling can be used for controllable dipole-dipole coupling to effect the desired counterintuitive pulse sequence, a mechanism proposed for controlled coupling in a dipolar phosphorus in silicon quantum computer [48]. The approach here is to vary the magnetic field direction along a trajectory that zeros the coupling between spins 1 and 3, while varying d_{12} and d_{23} according to the counterintuitive pulse sequence.

The dipole-dipole coupling between two spins, j and k, in a magnetic field is $(\hbar = 1)$

$$d_{jk}(\theta_{jk}, r_{jk}) = \frac{\gamma_j \gamma_k}{r_{jk}^3} (3\cos^2 \theta_{jk} - 1), \tag{14}$$

where the γ are the dipole moments, $\omega = \gamma B$, θ_{jk} is the angle between the magnetic field and the line joining the spins, and r_{jk} is the separation between spins. Now when $|\cos\theta_{jk}| = 1/\sqrt{3}$, we must have $d_{jk} = 0$, hence there is no coupling.

To demonstrate the appropriate control of the dipole-dipole coupling, we consider an arrangement of three equally spaced spins in the x-y plane, as shown in Fig. 5(a). To understand an implementation of the counterintuitive pulse sequence for DSAP from spin 1 to spin 3, in Fig. 5(b) we show the rays between the spins and the cones show the magic angles for the magnetic field to null the dipolar coupling. A possible counterintuitive pulse sequence trajectory is highlighted in yellow, where the central cone corresponds to nulling the 1-3

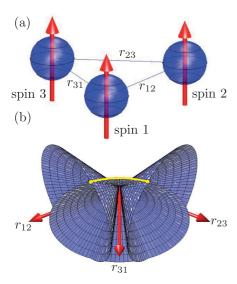


FIG. 5. (Color online) (a) Arrangement of three spins in the x-y plane. (b) Interspin separations with magic angles for each pair of spins marked. Because there are points of intersection of the magic angles, it is possible to define a magnetic field trajectory that effects the counterintuitive pulse sequence, and one such trajectory is shown here in yellow with the start and stop points marked with yellow dots.

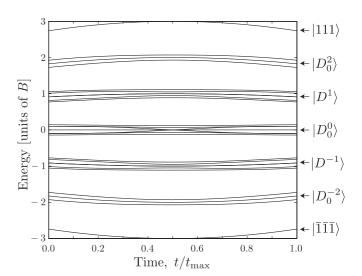


FIG. 6. Eigenspectrum for the magic-angle control protocol, where the angle of the applied field is according to the trajectory outlined in Eq. (15) for the case that the three spins are located at the vertices of an equilateral triangle.

coupling and the end points (yellow dots) correspond to the case where either the 1-2 or 2-3 coupling is also canceled. The magic magnetic trajectory defined by this configuration is

$$\mathbf{B} = B[\cos\varphi(t), \cot\theta_m, \sin\varphi(t)], \tag{15}$$

where θ_m is the magic angle and $\varphi(t)$ specifies the time-varying trajectory of the counterintuitive pulse sequence and

$$\cos[\varphi(0)] = \pi - \frac{\cot \theta_m \sin(2\pi/3)}{\cos(2\pi/3) - 1},$$
 (16)

$$\cos[\varphi(t_{\text{max}})] = \frac{\cot \theta_m \sin(2\pi/3)}{\cos(2\pi/3) - 1}.$$
 (17)

Following a magic-angle trajectory of the form envisaged here perforce changes B_z as well as the d_{jk} , and hence the eigenspectrum, shown in Fig. 6, is slightly more complicated than the simpler case studied in Sec. II. Nevertheless, the overall structure of the manifolds is unchanged from our earlier treatment, with the trajectories appearing to "bend" due to the varying z component of the magnetic field relative to the dipoles. However, the relative ordering of the states and their degeneracy is unaffected by using this control scheme rather than the earlier, more idealized approach where the magnitude of B_z is constant. We note that the form of the dipole coupling ensures square sinusoidal variation in the coupling coefficients as we assumed for the "ideal" version.

V. POSSIBLE EXPERIMENTAL REALIZATIONS

There are many possible systems in which the spin-one version of DSAP could be implemented. Here we briefly explore two such platforms: spin-based quantum dot arrays and spin-one defects in diamond. We also note other possibilities to be explored for implementation, such as chains of trapped ions [49], NiCl₂-4SC(NH₂)₂ [33,34], and liquid-phase nuclear magnetic resonance (NMR), e.g., via deuterated molecules [50,51].

A. Quantum dots

The design and engineering of controlled electrostatic potential landscapes in two-dimensional electron gasses has led to the production of quantum dots with remarkable and beautiful quantum properties. A single quantum dot can typically be manipulated to hold a preset number of electrons, and the singlet-triplet subspace of a two-electron quantum dot has been identified as a useful qubit encoding [52]. Conversely, the triplet subspace defines a spin-one subspace that may be used for our purposes. Triple dots have been demonstrated several times [53,54], although we are not aware of any that have specifically operated in the particular six-electron configuration necessary to test spin-one DSAP. Entanglement between pairs of double dots operating in the single-triplet basis has also been demonstrated [55]. This latter work shows controlled coupling similar to that required to test DSAP, with two-qubit coupling times of the order of 100 ns.

B. Nitrogen-vacancy center in diamond

The negatively charged nitrogen-vacancy (NV) center in diamond has emerged as an extremely interesting system for room-temperature quantum information processing. This is because the ground-state spin levels, which form a natural spin-one system, are long lived at room temperature and they can be optically initialized and read out at room temperature. However, most of the concepts for scalable quantum computing with NV centers require cryogenic temperatures due to spectral broadening of the main optical transitions [56]. If there were no requirements for coherent coupling from the ground-state manifold to the excited state, then it might be possible to construct a room-temperature quantum computer based on NV, and this is the subject of the proposal by Yao et al. [57].

While a deterministically created array of three NV centers at these separations has not been achieved, pair implantations (i.e., implantation of N_2^+) have been used to create coupled NV-N systems [58], and NV-NV systems [59] have also been formed by implantation through a mask. It should be possible to extend these methods to create small clusters of implanted N, which could be searched to identify a cluster of three NV centers. Reference [59] demonstrated dipole-dipole couplings between the NV centers that were around 10 nm apart. The techniques outlined in Sec. IV should enable a three-NV complex to perform spin-one DSAP. Other fabrication techniques that have the required precision include low-energy nanoimplantation through a nanostencil [61] and ultracold ion source implanters [62].

An alternative to explore electron-spin coupling would be to look at the nuclear spin coupling in the three N system. The ¹⁴N nucleus is also a spin-one particle [60]. In fact, Bermudez *et al.* have already proposed a two-qubit operation between two N nuclear spins in diamond, mediated by the electron spin [63].

VI. CONCLUSIONS

We have shown that the concept of dark-state adiabatic passage (DSAP) [25] can be extended from spin-half particles to arrays of spin-one particles. In particular, we have shown adiabatic pathways for an array of three spin-one particles by either direct control of the qutrit-qutrit coupling or by alignment control of a uniform, external dc magnetic field

In the case of conventional DSAP, the state of a single qubit is transmitted along a chain of qubits using the counterintuitive pulse sequence. The canonical example, where the chain qubits are all either aligned parallel or antiparallel to the quantization axis, is formally equivalent to the case of coherent tunneling adiabatic passage of either particles [7,9] or holes [42]. The spin-one version of DSAP is certainly richer than the spin-half or pseudo-spin-half version. We have shown qutrit transport across three spin-one particles when the other two spins are in one of the states $|11\rangle$, $|\bar{1}\bar{1}\rangle$, or $|1\bar{1}\rangle - |\bar{1}1\rangle$.

While the transport of the qutrit is adiabatically protected, it is important to stress that single qutrit errors on the chain particles (i.e., the nondata qutrits) will, in general, cause errors in the protocol. One may think of the error as producing another effective particle, and then particle-particle interactions will become important and will likely destroy the desired or predicted transport outcome. The sensitivity of the intended spin passage to errors in the nondata qutrits appears to be a property of most bus-type proposals for quantum information transport if a defined propagation direction is not maintained.

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