

Near-Capacity Wireless System Design Principles

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Abstract—In this tutorial, the design procedure of near-capacity channel code design invoking non-binary EXtrinsic Information Transfer (EXIT) charts is illustrated by using design examples of Irregular Concatenated Coding Arrangements (IC-CAs) relying on Irregular Convolutional Codes (IrCCs). More specifically, in order to benchmark the near-capacity design examples, both the capacity and the Outage Probability (OP) of the Continuous-input Continuous-output Memoryless Channel (CCMC), of the Discrete-input Continuous-output Memoryless Channel (DCMC) as well as of the Differential Discrete-input Continuous-output Memoryless Channel (D-DCMC) are characterised. Furthermore, the EXIT-chart aided near-capacity design principles are illustrated by detailing the design process of three characteristic prototype schemes, which represent the family of coherent and non-coherent detection based systems as well as Multi-Input Multi-Output (MIMO) systems, respectively. Moreover, the beneficial application of the EXIT-chart based design principle is also demonstrated in the context of cooperative systems using a specific distributed MIMO prototype scheme.

I. INTRODUCTION

The ultimate aim of designing a wireless communication system is to provide reliable high data rate links. Shannon's pioneering work published in 1948 [1] predicted that arbitrarily reliable communications are achievable with the aid of channel coding, provided that the required amount of redundant information is imposed on the transmitted messages. A breakthrough in channel coding history was the invention of turbo codes [2] in 1993, which may be employed for facilitating near-capacity operation. The original turbo code [3] design was based on a 'composite codec' constituted by two parallel concatenated codecs. Originally, the concatenated coding philosophy was proposed by Forney in 1966 [4], but until the 1990s it was only employed in demanding applications, such as deep-space communications owing to its high complexity. However, following the revolution turbo concept, since the 1990s it has found favour in numerous concatenated coding schemes [5]–[8].

Advances in channel coding made it feasible to gradually approach Shannon's capacity limit in Single Input Single Out (SISO) systems equipped with a single antenna [9]. However, these capacity limits can be further extended with the aid of multiple antennas in Multiple Input Multiple Output (MIMO) systems, which are capable of providing a linearly increasing capacity as a function of the transmit power, provided that the extra power is assigned to additional antennas [10]. Space

Time Trellis Codes (STTCs) [11] and Space Time Block Codes (STBCs) [12] constitute a family of joint coding and transmit-receive diversity aided MIMO systems designed for communicating over fading channels [13]. However, it is impractical to allocate multiple antennas to a shirt-pocket-sized mobile unit. In order to circumvent this space-limitation, the concepts of cooperative communication have recently attracted substantial research efforts [14]–[18], since they are capable of creating a Virtual MIMO (VMIMO) system from several single-antenna aided relays, which cooperatively share their antennas. The important milestones of specific advances related to the subject of this tutorial are listed in Tab. I.

EXtrinsic Information Transfer (EXIT) chart introduced by Stephan ten Brink [32] is a very useful tool used for characterising an iterative process of information transfer between two decoders of turbo codes, which is not easy to analyse and to describe. Based on specific technique of iterative information exchange among the component codes, a concatenated coding scheme can be categorised into three major types [33] as seen in Fig. 1, namely:

- Parallel Concatenated Convolutional (PCC) codes comprise two or more parallel component codes iteratively exchanging mutual information (MI) with the aid of an interleaver. The component codes may be Recursive Systematic Convolutional (RSC) codes [3], Unity Rate Codes (URC) [34] or Trellis Coded Modulation (TCM) codes [35].
- Self-concatenated Convolutional (ScC) codes rely on a single component encoder combined with a turbo interleaver at the transmitter side. The decoder relies on using a single decoder twice [33], [36].
- Serial Concatenated Convolutional (SCC) codes are typically constructed by concatenating M component codes in order to constitute a more powerful amalgamated code, where M component encoders are separated by $M - 1$ interleavers [8], [37].

As classic Turbo Codes (TCs) [2] consist of two or more parallel constituent codes representing PCC codes, while a tutorial of ScC codes has been presented in [33], let us pay attention on the SCC codes. The SCC codes have recently provoked a number of research work focusing on near-capacity EXIT chart aided coding designs [38]–[55], which may be categorised into several sub-areas, as seen in Fig. 1, namely SISO schemes based on coherent detection [40], [41], [43], Non-coherent detection based SISO schemes [50], [51], MIMO schemes [39], [44], [46]–[48], [53], [54], VMIMO schemes

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Year	Author	Milestone
1948	Shannon [1]	Introduced Shannon's capacity theorem.
1955	Elias [19]	Introduced convolutional codes.
1966	Forney [4]	Introduced concatenated codes.
1971	van der Meulen [20]	Introduced a simple relay channel constituted by a source, a destination and a relay.
1972	Bahl <i>et al.</i> [21]	Invented the Maximum A-Posteriori (MAP) algorithm.
1974	Bahl <i>et al.</i> [22]	Proposed the symbol based MAP algorithm.
1979	Cover and El Gamal [23]	Presented capacity analysis of the full duplex relay channel.
1993	Berrou <i>et al.</i> [2]	Discovered turbo codes.
1995	Douillard <i>et al.</i> [24]	Proposed turbo equalisation
1997	Tarokh <i>et al.</i> [25]	Introduced Space Time Trellis Coding (STTC).
	Benedetto <i>et al.</i> [26]	Investigated iterative decoding of an outer convolutional decoder and an inner Trellis-Coded Modulation (TCM) decoder.
1998	Alamouti <i>et al.</i> [27]	Proposed Space Time Block Coding (STBC).
	Benedetto <i>et al.</i> [8], [28]	Derived design guidelines for serially concatenated codes with the aid of the union-bound technique [8], and also extended the turbo principle to multiple serially concatenated codes [28]
1999	ten Brink [29]	Proposed EXIT charts for analysing the convergence behaviour of iterative decoding and demapping.
2002	Tücher and Hagenauer [30]	Proposed irregular convolutional codes as well as a simplified method for computing mutual information in EXIT chart analysis
2004	Ashikhmin <i>et al.</i> [31]	Presented a universal model for conducting EXIT chart analysis as well as various properties of EXIT functions, which form the theoretical foundation of EXIT-curve matching techniques

TABLE I
MILESTONES IN CHANNEL CODING OF INTERESTS FROM SINGLE INPUT SINGLE OUTPUT (SISO) TO MIMO.

[42], [45], [49], [51] and joint source-channel coding schemes [38], [55]. As a result, the authors of [56] have published a tutorial focusing on merely in coherent SISO schemes, while in another tutorial [57] the authors have covered the specific subject-area of joint source-channel coding. Hence, as explicitly portrayed in Fig. 1, this treatise aims for providing a broad tutorial on the application of EXIT charts for near-capacity IrCC aided designs. Specifically, we illustrate the associated principles with the aid of design examples in the general context of taking into account both coherent and non-coherent detection, MIMO scenarios as well as cooperative communications.

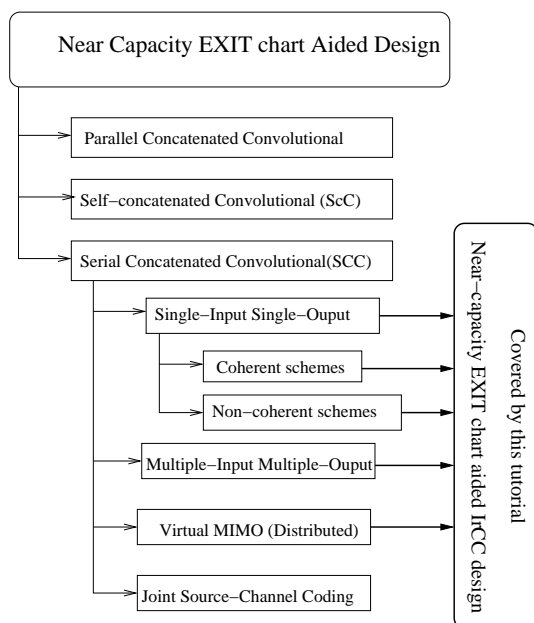


Fig. 1. Taxonomy of near-capacity EXIT aided designs in the literature.

More specifically, in this tutorial we will summarise the techniques of near-capacity code-design with the assistance of

four prototype systems designed upon using the EXIT chart base tool. Accordingly, we will illustrate the basic design principles with the aid of three stage concatenated coding schemes employing an irregular outer code, for example IrCCs. The intermediate code employed for constructing the three-stage concatenated coding schemes is constituted by URC [58]. It was shown in [59], [60] that a recursive URC should be employed as an intermediate code in order to improve the attainable decoding convergence. More specifically, we will show that a URC can be used as a precoder for creating an inner code component having an Infinite Impulse Response (IIR) in order to reach the (1,1) point of perfect decoding convergence in the EXIT chart and hence to achieve an infinitesimally low Bit Error Ratio (BER) [61]. The inner most stage can be a coherent/noncoherent base detector itself for the coherent/noncoherent schemes or STTCs for the MIMO and VMIMO schemes.

To elaborate a little further, in order to benchmark the near-capacity designs considered, we will detail the specifics of calculating both the capacity and the outage capacity, which may be determined by employing EXIT charts. These capacities represent the best possible performance of corresponding coding schemes in both small-scale and large-scale fading environments. The best possible performance may be achieved, when an ideal/perfect capacity-achieving coding scheme is employed. Accordingly, the EXIT chart based design principle will be exemplified for both coherent and non-coherent detection based SCC schemes. Additional discussions on the effect of realistic channel estimation errors will also be presented in order to highlight both the pros and cons of the coherent and non-coherent modulation based schemes. Our discussions are continued by highlighted points on the benefit of employing sub-frame based transmissions in slow-fading environments, where the outage capacity should be used for benchmarking the near-capacity coding schemes considered. Moreover, the paper continues by describing the application of the design principles in the context of coop-

erative communications, where distributed SCC schemes are employed, as seen in Fig. 1.

The rest of the paper is characterised by the stylised illustration of Fig. 2, where all the major subjects presented in the papers are visualised along with the relationships between them. More specifically, our paper is focused on the subject of near-capacity EXIT-chart aided system design. Explicitly, we present the basic design principles in Section V-A, which are then exemplified in Section V-B, Section V-C and Section VI with the aid of prototype designs. The design process is relied on the employment of the EXIT chart design tool, which is briefly characterised in Section II-A and Section V-A. Finally, we provide our generalised design guidelines in Section VII-B.

Observing Fig. 2 from a different perspective, the near-capacity design of wireless systems considered in the context of the tutorial is characterised by three groups of parameters, namely by the coding components, transmission schemes and the associated conflicting metrics. Accordingly, we provide the relevant background on the coding components used, namely on IrCCs in Section II-B and on STTCs in Section II-C, while the transmission regimes covering both the class of coherent and non-coherent systems are detailed in Section V-B and Section V-C, where the related issues of the channel estimation are also covered in Section V-E. Moreover, additional discussions are also extended to different channel fading types, namely to both fast fading and slow fading, in order to highlight the benefit of employing sub-frame based transmission regimes in Section V-D. As regards to the transmission schemes, the tutorial covers the concepts of SISO schemes in Section V-B and Section V-C, MIMO schemes in Section VI-C, whilst those of VMIMO schemes in Section VI-B and Section VI-D. The metrics used for those schemes, namely the outage probability and outage capacity of the schemes, are presented in Section III and Section IV, respectively.

II. PRELIMINARIES

In this section, we will provide background pertaining to the EXIT charts, IrCC, STTC and non-coherent detection, in order to facilitate the presentation of our formal tutorial paper on near-capacity EXIT chart aided IrCC design in the general context taking into account of coherent/non-coherent detection, MIMO scenarios and cooperative communications.

A. Extrinsic Information Transfer Charts

As more and more complicated concatenated codes are constructed for the sake of pursuing a near-capacity performance, one of the major design challenge is to predict and compare their E_b/N_0 convergence thresholds in order to choose the most appropriate channel coding and modulation parameters. Motivated by this problem, researchers have focused their attention on characterizing the convergence behavior of turbo codes [32], [62]–[66], which rely on the ‘turbo principle’. In its basic form, the turbo principle is employed in the context of two concatenated coding components, namely an inner and an outer components, albeit there are also powerful three-component or multiple-component [34], [67] schemes. The salient benefit of the turbo principle is that the inner and outer

components exchange soft values. Accordingly, the extrinsic part of the soft-output of one decoder can be passed to the other decoder to act as its *a priori* input. This decoding process constitutes an iterative information transfer between the two turbo decoders, which can be visualised with the aid of EXIT charts [68].

Several measures have been proposed for characterising the iterative process of turbo codes, which were listed and compared in [69], amongst which, the soft bit transfer (SOBIT) chart and the EXIT chart appealingly visualise the behaviour of the iterative decoding process [69]. Moreover, according to the comparisons in [68], the EXIT chart was considered to be physically more meaningful than the SOBIT chart due to its compelling information theoretical interpretation relying on fractions of a bit.

Generally, an EXIT chart of a serially concatenated scheme visualises the exchange of four MI terms, namely the average *a priori* MI of the inner component I_A^{in} , the average *a priori* MI of the outer component I_A^{out} , the average extrinsic MI of the inner component I_E^{in} and the average extrinsic MI of the outer component I_E^{out} . More specifically, the I_A^{in} and I_E^{in} constitute the EXIT curve of the inner component, while their outer-component based counterpart is formed by I_A^{out} and I_E^{out} . For convenience, the MI transfer characteristics of both the inner and outer components are plotted in a single graph, where the x and y axes of the outer decoder are swapped for each new information exchange step. The resultant EXIT chart quantifies the improvement in mutual information as the iterations proceed, which results in a stair-case-shaped decoding trajectory.

In the rest of this section, we provide insights into the state-of-the-art EXIT chart [32], [65], [66], which can be used for effectively analysing the flow of extrinsic information between turbo coding components so that decoding convergence may be accurately predicted. Accordingly, both the rudimentary theoretical principles as well as the practical applications of EXIT charts will be elaborated on.

1) *Mutual Information and Transfer Characteristics*: Assume that a data bit $b \in \{1, 0\}$ at the transmitter is equiprobable. In order to investigate the flow of MI at a component block at the receiver, the transfer characteristics of the component may be formulated as [32], [70]:

$$I_E = T(I_A), \quad (1)$$

where the *a priori* information I_A and the extrinsic information I_E at the input and at the output of the transfer function T are given by $I_A = I(b; \Lambda_a)$ and $I_E = I(b; \Lambda_e)$, while Λ_a and Λ_e are random variables modelled for L_a and L_e , respectively. Note that the notation $I(X; Y)$ represents the MI between random variables X and Y [71], while L_a and L_e are the corresponding Loglikelihood Ratio (LLR) representing a soft-value input and a soft-value output of the component, respectively. For more details about LLR relating to turbo principle, please allow us to refer readers to the tutorial presented in [68].

The first step of obtaining I_E with given I_A is to generate a group of *a priori* LLRs L_a from values of I_A . Then, $I_E = I(b; \Lambda_e)$ may be evaluated accordingly, where the extrinsic

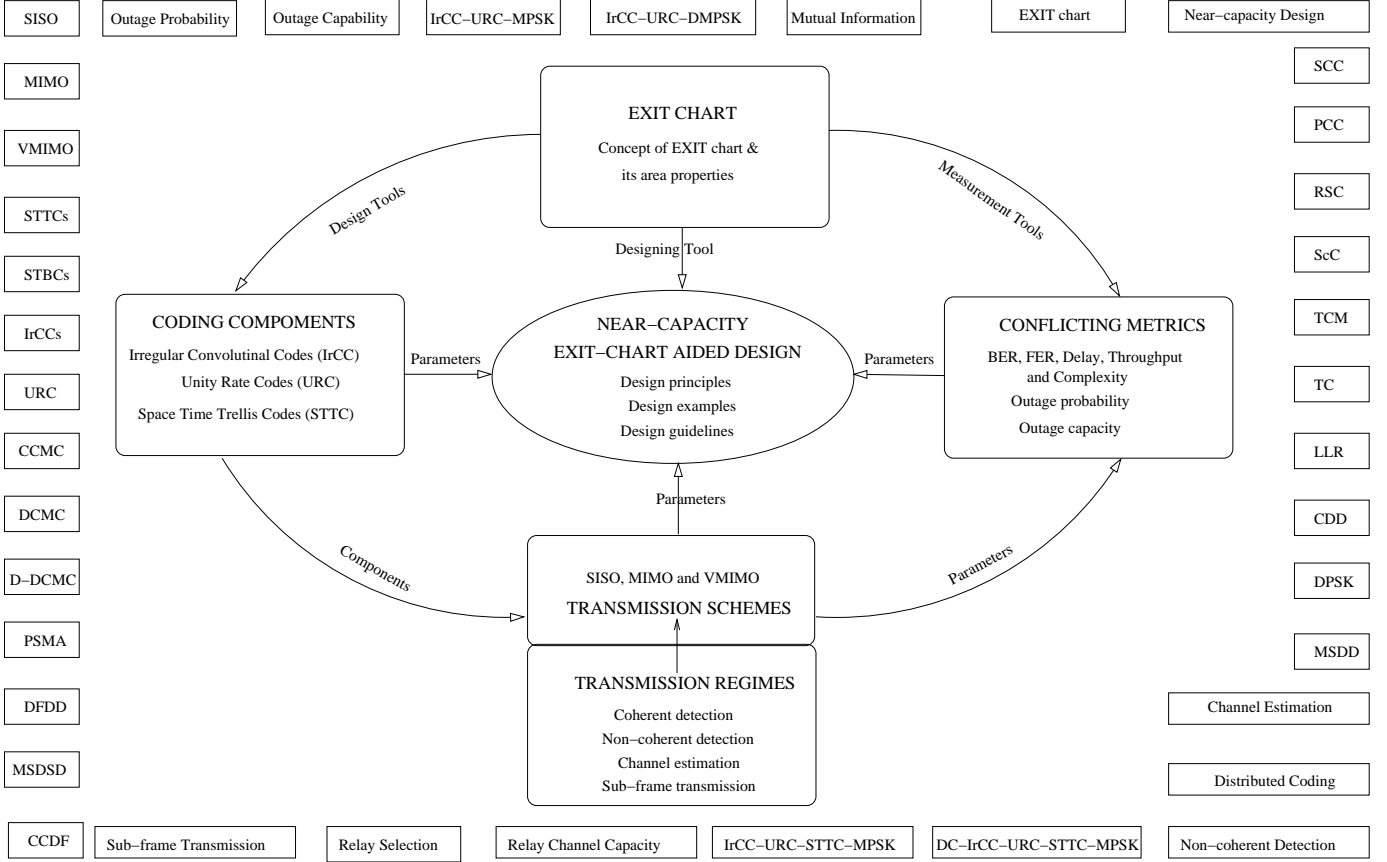


Fig. 2. Outline and rationale of the paper.

LLRs L_e are obtained by feeding L_a to the component under study.

Assume that long interleavers are employed between concatenated components so that the LLRs exchanged by them are uncorrelated and Gaussian-distributed. Therefore, the Gaussian-distributed LLRs of L_a may be generated [32]. Accordingly, the formula of I_A may be simplified by an input-output relationship characterised as a function $J(\cdot)$ as:

$$I_A = J(\sigma_A), \quad (2)$$

where σ_A^2 obeying $\sigma_A \geq 0$ is a variance of a Gaussian random variable constituting the value of L_a , while $0 \leq I_A \leq 1$ is satisfied. Furthermore, function $J(\cdot)$ of Eq. (2) has the following properties:

$$\lim_{\sigma_A \rightarrow 0} J(\sigma_A) = 0, \quad \lim_{\sigma_A \rightarrow \infty} J(\sigma_A) = 1. \quad (3)$$

It is observed that the output I_A of function $J(\cdot)$ increases monotonically with respect to input σ_A . Although the function $J(\cdot)$ and its inverse function $J^{-1}(\cdot)$ cannot be expressed in closed form [32], we refer to [72] for the approximate form of the functions $J(\cdot)$ and $J^{-1}(\cdot)$.

As a result, we can summarise the procedures of evaluating the transfer characteristics of Eq. (1) as:

- (1) For given a specific *a priori* mutual information I_A , a group of *a priori* LLRs L_a may be generated [32], where the standard deviation σ_A of the Gaussian distribution is

given by the inverse function of $J(\cdot)$ [72], i.e. we have $\sigma_A = J^{-1}(I_A)$.

- (2) Feed the generated soft-value inputs L_a to the tested component in the concatenated code, and then a group of extrinsic LLR outputs L_e may be obtained.
- (3) Finally, the extrinsic MI output of Eq. (1) may be computed upon evaluating the histograms of L_e [73] with respect to the source data bit being $b = 1$ and $b = 0$.

2) *Area Property*: EXIT charts have been introduced as an effective tool conceived for analysing the convergence properties of iterative decoding aided concatenated coding schemes [74]. By exploiting two basic properties:

- *EXIT charts may be used for visually characterising the flow of soft-information between component codes of concatenated coding schemes.* Given the EXIT chart of a concatenated coding scheme, the Signal to Noise Ratio (*SNR*), at which an infinitesimally low BER of the scheme is achieved, may be predicted by exploiting that once the Monte-Carlo simulation based bit-by-bit decoding trajectory reaches the (1,1) point of the EXIT chart, perfect decoding convergence has been attained. Hence, no further decoding iterations are required. In other words, the turbo-cliff SNR of the concatenated coding scheme may be found by merely looking at the EXIT chart. Moreover, upon counting the number of stair-case-shaped steps in the decoding trajectory curves,

the appropriate number of iterations between two coding components may be determined.

- *The area under the EXIT curve of an inner decoder component is approximately equal to the attainable channel capacity, provided that the channel's input symbols are equiprobable [31], [75].* This property [31], [75] may be exploited for determining the achievable rates of Forward Error Control (FEC) schemes relying on iterative multi-stage coding. Then, the achievable capacity may be used for selecting a specific coding scheme from the available set and may also be used for optimising coding arrangements relying on numerous parameters by using the achievable capacity as a criterion for comparing all legitimate sets of parameters used for specifying the coding arrangement. As an advantage, a near-capacity code design can be found by employing EXIT charts without performing time-consuming Monte-Carlo simulations. EXIT charts can also be used for finding powerful codes exhibiting guaranteed convergence for a given channel [76]. Specifically, near-capacity codes have been successfully designed by applying an EXIT-chart-based technique, for example in [30], [61], [77].

B. Irregular Convolutional Codes

The irregular design of channel codes has received significant scientific attention from a wide range of researchers for the sake of characterising the irregularity of low density parity check codes (LDPC) [63], [78]–[80], of accumulate codes [80]–[84], of variable length codes [38], [40] as well as of convolutional codes [39], [44], [45], [51]. In the framework of this tutorial, we focus our attention on the family of irregular convolutional codes, which constitute the juxtapositioned counterpart of classic PCCs, ScSs and SCCs seen Fig. 1. Since the literature of PCC and ScC structures has been covered in [33], [56], the goal of this tutorial is to present the suit of irregular convolutional codes in the context of both coherent/non-coherent detection, MIMO scenarios and cooperative communication. By contrast, the subject of joint source-channel coding has been presented in [57], as indicated in Fig. 1.

In the framework of this paper, let us commence by considering a classic two-stage SCC, where the two component codes may be deemed as inner code and outer code. A variety of near-capacity systems [32], [46], [85]–[87] aim to match the EXIT curves of inner and outer codes, so that an open tunnel may be encountered at the lowest possible E_b/N_0 . For the extreme situation of having an infinitesimally small open tunnel, we have a perfect match of the inner and outer codes, where the maximum achievable rate is achieved. Therefore, a near-capacity system's design may aim for achieving an infinitesimally low BER at an SNR , so that no transmit power should be wasted.

In order to achieve this goal, on one hand, numerous researchers have focused their attentions on how to design optimised modulation schemes so that their EXIT curves may fit closer to the outer channel code's EXIT curve. This topic is widely known as mapping optimization for Bit-Interleaved

Coded Modulation with Iterative Decoding (BICM-ID) [86], [88]–[92]. On the other hand, as the family of modulation schemes keeps growing especially for MIMO applications, it becomes more feasible to adjust channel coding's transfer characteristics as illustrated in [46], [87], [93], where IrCCs is a popular application of the aforementioned near capacity design.

Tüchler and Hagenauer [30], [87] proposed the employment of IrCCs for the design of near-capacity serial concatenated schemes, which are constituted by a family of convolutional codes having different rates. These IrCCs were specifically designed with the aid of EXIT charts for improving the convergence behaviour of iteratively decoded systems. Briefly, these schemes were then further developed for a broad class of turbo-transceivers in [85]. Each subcode ϕ encodes an appropriately selected fraction α_ϕ of the input bit stream, where $\phi = [1, 2, \dots, \Phi]$. More explicitly, the appropriate fractions may be selected with the aid of EXIT-chart analysis in order to shape the inverted EXIT curve of the composite IrCC for ensuring that it matches the EXIT curve of the so-called inner decoder constituted by the demodulator/detector. In this manner, an open EXIT-chart tunnel can be created at low SNR values, which implies approaching the channel's capacity bound, as detailed in [31]. In our example, we choose either $\Phi = 17$ or $\Phi = 36$ for illustrating our design principles. Accordingly, if the ϕ^{th} subcode having a code rate β_ϕ encodes the fraction α_ϕ of the input bit stream, where the values of β_ϕ are listed in Tab. II, the values of the weighting coefficient α_ϕ and subcode rate β_ϕ always have to satisfy the constraint of:

$$R_c = \sum_{\phi=1}^{\Phi} \alpha_\phi \beta_\phi, \quad (4)$$

where R_c is the coding rate (aggregate coding rate) of the IrCC. As a result, the EXIT curve of each IrCC subcode

Subcode	Code Rate β_ϕ	Subcode	Code Rate β_ϕ
1	$\beta_1=0.10$	18	$\beta_{18}=0.10$
2	$\beta_2=0.15$	19	$\beta_{19}=0.15$
3	$\beta_3=0.20$	20	$\beta_{20}=0.20$
4	$\beta_4=0.25$	21	$\beta_{21}=0.25$
5	$\beta_5=0.30$	22	$\beta_{22}=0.30$
6	$\beta_6=0.35$	23	$\beta_{23}=0.35$
7	$\beta_7=0.40$	24	$\beta_{24}=0.40$
8	$\beta_8=0.45$	25	$\beta_{25}=0.45$
9	$\beta_9=0.50$	26	$\beta_{26}=0.50$
10	$\beta_{10}=0.55$	27	$\beta_{27}=0.45$
11	$\beta_{11}=0.60$	28	$\beta_{28}=0.50$
12	$\beta_{12}=0.65$	29	$\beta_{29}=0.55$
13	$\beta_{13}=0.70$	30	$\beta_{30}=0.60$
14	$\beta_{14}=0.75$	31	$\beta_{31}=0.65$
15	$\beta_{15}=0.80$	32	$\beta_{32}=0.70$
16	$\beta_{16}=0.85$	33	$\beta_{33}=0.75$
17	$\beta_{17}=0.90$	34	$\beta_{34}=0.80$
		35	$\beta_{35}=0.85$
		36	$\beta_{36}=0.90$

TABLE II
LIST OF THE SUBCODE RATES FOR THE IRCC CODE HAVING $\Phi = 17$ OR
 $\Phi = 36$ SUBCODES.

is provided Fig. 3, where superposition of EXIT curves of

the subcodes selected from Φ available subcodes are plotted. It should be noted that each EXIT curve is generated by employing the algorithm detailed in Section II-A1 and that the IrCC is equivalent to the subcode of interest if the corresponding fraction of the subcode is set to one.

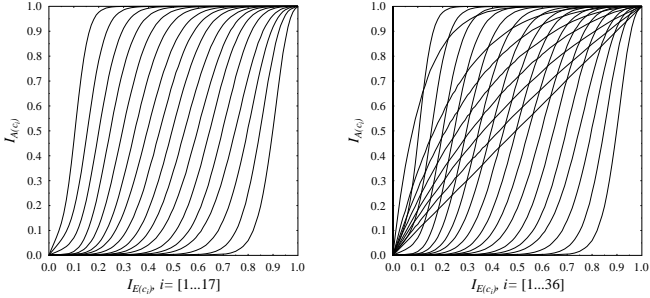


Fig. 3. EXIT curves of Φ IrCC subcodes, where $\Phi = 17$ or $\Phi = 36$.

C. Space Time Trellis Code

As mentioned in Section I, STTCs [11] and STBCs [12] constitute a family of joint coding and transmit-receive diversity aided MIMO systems designed for communicating over fading channels [13]. We note, however that in contrast to STBCs, STTCs are also capable of attaining a coding gain in addition to their spatial diversity gain, while again, the STBCs of [76] can only achieve a spatial diversity gain [85] but no coding gain. As a result, we opted for using the STTCs in our subsequent prototype design examples for demonstrating the EXIT chart based design principles detailed in Section V-A.

STTCs [11], [13], [94], [95] were proposed by Tarokh *et al.*, which incorporate jointly designed channel coding, modulation, transmit diversity and optional receiver diversity. The performance criteria for designing STTCs were listed in [11] with the assumption that the channel is fading slowly and that the fading is non-dispersive. It was illustrated in [11] that the systems performance is determined by matrices constructed from pairs of distinct code sequences. The diversity gain and coding gain of the codes are determined by the minimum rank and the minimum determinant [11], respectively. The results were then also extended to fast-fading channels [96]. The STTCs proposed in [11] strike the best trade-off among the data rate, diversity gain and trellis complexity. The effect of multiple propagation paths on the performance of STTCs were investigated in [13] for transmission over slowly varying Rayleigh fading channels. It was shown in [13] that the presence of multiple paths does not decrease the diversity order guaranteed by the design criteria used for constructing the STTCs. The results provided in [13] were then also extended to rapidly-fading dispersive and non-dispersive channels.

Having presented a rudimentary introduction to STTCs, we refer the motivated readers to [11] for the details of encoding and decoding processes of the STTCs. A specific example employed for our subsequent illustrations is that of the 4-state, 4-level Phase Shift Keying (4PSK) STTC using $N_t = 2$ transmit antennas. More sophisticated STTCs were designed for 4PSK and 8PSK [11] by increasing the number S of trellis states to $S = \{8, 32\}$.

D. Non-coherent detection

The early development of Differential Phase Shift Keying (DPSK) may be found in [97], [98], where the data carrying symbol x_{n-1} is mapped on to the change of the consecutive transmitted symbols as $s_n = x_{n-1}s_{n-1}$. As a result, in AWGN channels where both a Gaussian noise v_n and a constant frequency offset phase $\exp(j\theta)$ contaminate the received signal as $y_n = s_n \exp(j\theta) + v_n$, the simple non-coherent detection operation of $z_{n-1} = y_n y_{n-1}^*$ may eliminate the need for estimating the unknown phase for recovering x_{n-1} . This low-complexity non-coherent detection, which detects a single symbol based on two observations may be termed as Conventional Differential Detection (CDD). However, the CDD aided DPSK suffers from a 3 dB performance penalty compared to its idealistic coherent PSK counterpart assuming perfect estimation of the phase offset [99]. Moreover, an irreducible error floor occurs for DPSK [100], when the CDD is employed in rapidly fluctuating high-Doppler fading channels.

The pragmatic approach of Multiple Symbol Differential Detection (MSDD) conceived for improving non-coherent detection was proposed in [101], [102] for DPSK reception in AWGN channels. In the approach, the symbols in an adjustable detection window relying on N_w received samples are jointly detected. The MSDD designed for DPSK was then further extended for DPSK operating in fading channels [103], [104]. In the extension, upon increasing the detection window length N_w , MSDD is not only capable of mitigating the 3 dB performance gap between non-coherent detection and coherent detection in AWGN channels, but it is also capable of reducing the error floor by exploiting the correlation of the fading envelope. However, the MSDD complexity may increase exponentially with the window length N_w .

In order to reduce the MSDD complexity, an efficient algorithm was conceived for MSDD in AWGN channels [105], where a low detection complexity order of $O(\log N_w)$ was imposed by detecting a single symbol upon observing the phase changes over the N_w samples. This method may also be applied for improving the performance of the CDD aided DPSK in block fading channels. It is due to the fact that accurate channel estimation may be implemented at a low cost in slowly fluctuating fading channels. For example, Pilot Symbol Assisted Modulation (PSAM) was proposed in [106], where the known pilot samples may be transmitted periodically. Accordingly, the receiver may recover the complex-valued fading factors by estimating the channel with the aid of pilot samples. However, when the fading fluctuates rapidly, the PSAM aided coherent scheme has to dedicate more transmission power to the pilot symbols instead of the data-carrying symbols. Despite of this, the accuracy of channel estimation also degrades in comparison to the case of block fading. Therefore, the implementation of the MSDD at an affordable complexity is desirable in the context of rapidly fading channels.

Accordingly, the Decision-Feedback Differential Detection (DFDD) was proposed for DPSK operating in AWGN channels [107], [108] and was further detailed in [109]. The DFDD

makes a decision regarding a single symbol based on $(N_w - 1)$ previous decisions. As a result, the DFDD has a low detection complexity order of $O(M)$, when detecting a single symbol. The DFDD designed for DPSK was then further extended to fading channels [110], [111] in the context of coded DPSK. The DFDD is considered to be equivalent to the MSDD associated with decision feedback, but the DFDD fails to approach the optimum MSDD detection capability. In order to mitigate this problem, Multiple Symbol Differential Sphere Detection (MSDSD) was proposed in [112] for uncoded DPSK and in [113] for coded DPSK, where a sphere decoder was invoked for implementing MSDD. The MSDSD complexity is lower bounded by $O(M)$, but the algorithm exhibits its highest complexity in the low SNR region [114], [115].

III. OUTAGE PROBABILITY AND CHANNEL CAPACITY

The outage probability (OP) can be used for characterising the Quality of Service (QoS) of diverse systems. For example, the OP of the idealised transmission link operating exactly at the CCMC channel's capacity may be used as a benchmarker relying on Gaussian distributed signals, as detailed in Section III-A. By contrast, the OP of a specific digital modulation scheme corresponding to the DCMC of Section III-B and to the D-DCMC of Section III-C may be used as tighter and more realistic bounds.

Let us commence by considering the model of a single transmission link associated with the transmitted and received signals of x and y , respectively. The received signal can be represented as

$$y = hx + n, \quad (5)$$

where $h = h_s h_f$ is the complex-valued fading coefficient that comprises two components, namely a block fading coefficient (slow fading, large-scale shadow fading or quasi-static fading) h_s , which is constant for all symbols within a frame and a fast fading (small-scale fading) coefficient h_f , which fluctuates on a symbol-by-symbol basis. Finally, n is the AWGN process having a variance of $N_0/2$ per dimension.

We refer to C as the maximum achievable transmission rate of reliable communication supported by the channel characterised by (5). Let us assume that the transmitter encodes data at a rate of R bits/s/Hz. If the channel realisation h has a capacity of $C|h| < R$, which is lower than required, the system is declared to be in outage, where the OP is given by:

$$P_e(R) = Pr \{C|h| < R\}, \quad (6)$$

with $C|h|$ being the capacity, i.e. the maximum achievable rate of the channel, when h is known.

A. Continuous-Input Continuous-Output Memoryless Channel

We may be able to calculate the OP of the CCMC channel by applying the principle represented by Eq. (6) for the CCMC model. Accordingly, the OP of the interleaved channel associated with a transmission frame length of N symbols spanning from $N \rightarrow \infty$ can be formulated as [116], [117]

$$P_e^{CCMC}(R) = Pr \left\{ |h_s|^2 E[|h_f|^2] < \frac{2^R - 1}{SNR} \right\}, \quad (7)$$

where it was exploited that the block fading coefficient h_s remains constant for all N symbols of a transmitted frame and faded independently for the next transmit frame. This can be directly inferred from Eq. (7) for the OP corresponding to the scenario in which the signals experience small-scale fading as well as for the case of signals that do suffer from block fading, but no small-scale fading. Note that in the block fading scenario, the OP is equivalent to the Frame Error Ratio (FER) of the corresponding transmission link.

B. Discrete-Input Continuous-Output Memoryless Channel

For a specific modulation order, for example Binary Phase-Shift Keying (BPSK), Quadrature Phase-Shift Keying (QPSK), it is more practical to employ the DCMC capacity and the associated OP for benchmarking an associated near-capacity channel coded modulation scheme. Thus, in this section we first review the capacity calculation of a DCMC channel, before detailing the steps to be followed for determining the corresponding outage capacity.

More specifically, the reference of [118] details formulae for calculating the corresponding channel capacity of a transmission link operating over the DCMC channel, over which a specific modulation scheme is advocated. The modulation scheme is characterised by $L = 2^\eta$ known as the number of modulation levels, while η is the number of modulated bits. For example, Fig. 4 presents capacity curves of the DCMC channel influenced by uncorrelated Rayleigh (small-scale) fading, when employing BPSK, QPSK, 8 level Phase Shift Keying (8PSK) and 16 level Phase Shift Keying (16PSK) schemes. These channel capacities of Fig. 4 are evaluated by employing the classic Monte Carlo simulation method for averaging the expectation terms, which can be modified for covering the scenario of MIMO systems, as detailed in [118].

In order to define the OP for the DCMC scenario, let us denote the receiver's faded signal to noise power ratio as $SNR_r = E[|h|^2 SNR]$. At a given throughput R , one can readily identify the corresponding signal to noise power ratio $SNR_r|_R$ that is defined as the SNR value associated with the capacity $C_{(\eta)}^{DCMC} = R$ on the $C_{(\eta)}^{DCMC}$ -versus- SNR capacity curve plotted in Fig. 4. Then, similar to the philosophy applied for the CCMC scenario reflected by Eq. (7), the OP of the interleaved DCMC model is equivalent to the probability of the event that we have $|h|^2 SNR < SNR_r|_R$, which is expressed as

$$P_e^{DCMC}(R, \eta) = Pr \left\{ |h_s|^2 E[|h_f|^2] < \frac{SNR_r|_R}{SNR} \right\}. \quad (8)$$

From Eq. (8), it is also straightforward to infer the OP corresponding to the scenario, in which the received signals experience only fast fading but no block fading or only block fading but no fast fading.

For the sake of providing a fair comparison between different modulation schemes, for example BPSK and QPSK, we should use the normalized throughput of

$$R_n = \frac{R}{\eta}. \quad (9)$$

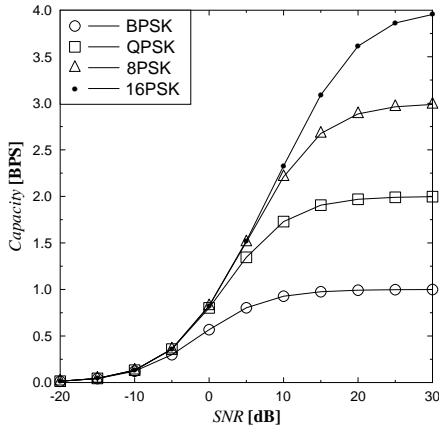


Fig. 4. Capacity curves [118] of the DCMC channel calculated for uncorrelated Rayleigh (small-scale) fading channel, when employing Binary Phase-Shift Keying (BPSK), Quadrature Phase-Shift Keying (QPSK), 8 level Phase Shift Keying (8PSK) and 16 level Phase Shift Keying (16PSK) schemes.

Normalised throughput $R_n = R/\eta$	$SNR_r _{R_n}$ [dB]	
	BPSK ($\eta = 1$)	QPSK ($\eta = 2$)
0.01	-21.45	-18.55
0.20	-7.38	-4.40
0.40	-3.01	-0.01
0.50	-1.20	1.78
0.60	0.59	3.60
0.80	4.92	7.95
0.99	28.37	31.75

TABLE III

$SNR_r|_R$ VALUES OF EQ. (8) FOR DCMC SCHEMES CORRESPONDING TO CONSIDERING DIFFERENT NORMALISED THROUGHPUTS, NAMELY $R_n = \{0.01, 0.2, 0.4, 0.5, 0.6, 0.8, 0.99\}$, WHEN COMMUNICATING OVER UNCORRELATED RAYLEIGH FADING CHANNELS.

Accordingly, the $SNR_r|_R$ values corresponding to different values of the normalised throughput R_n considered in the DCMC scheme can be calculated and listed in Tab. III. Accordingly, we have Fig. 5 characterising the relationship between the OP versus the normalised throughput R_n , when employing the BPSK and QPSK modulation schemes for transmission over slow Rayleigh fading channel.

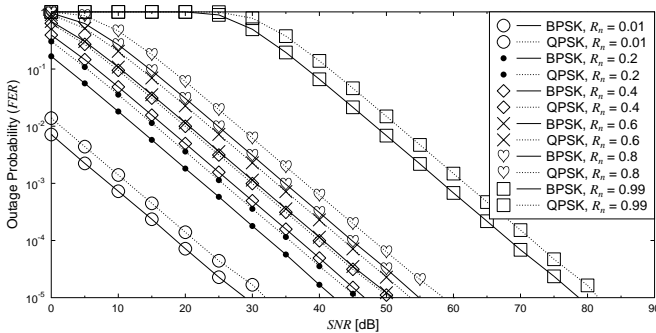


Fig. 5. Outage probability (FER) of the DCMC calculated by Eq. (8) for BPSK and QPSK modulation scheme for transmission over the large-scale(slow) Rayleigh fading channel.

Additionally, the DCMC capacity can also be calculated by employing the EXIT chart method, which is illustrated in the next section for determining the capacity of the D-DCMC.

C. Differential Discrete-Input Continuous-Output Memoryless Channel

EXIT charts may be invoked for calculating the D-DCMC capacity supported by the non-coherent detection scheme of Section II-D. More specifically, it can be inferred from the second property of the EXIT chart detailed in Section II-A2 that the area under the EXIT curve of a Differential Quadrature Phase Shift Keying (DQPSK) modem for example quantifies its attainable capacity. Accordingly, in order to obtain the capacity curves seen in Fig. 6, the following steps have to be carried out:

- **Generate** the EXIT curves of various differential modulation schemes, for example those of Differential Binary Phase Shift Keying (DBPSK) and DQPSK, for different SNR_r values.
- **Determine** a single point on the capacity curves by computing the area under an EXIT curve and its corresponding SNR_r . As a result, the capacity curves are plotted in Fig. 6 for an uncorrelated Rayleigh fading channel, when for example employing DBPSK and DQPSK modulation schemes.

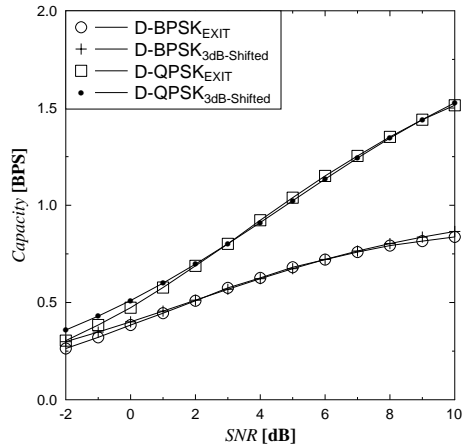


Fig. 6. Capacity curves of the D-DCMC determined by the EXIT-chart based method or by shifting the DCMC capacity curves of Fig. 4 to the right a distance of 3 dB, when employing BPSK and QPSK modulation schemes over uncorrelated Rayleigh (fast) fading channel.

As an alternative method, the D-DCMC capacity curves can be obtained by shifting the corresponding DCMC capacity curves plotted in Fig. 4 to the right by 3dB. As a result, the D-DCMC curves determined by the shifting method are also plotted in Fig. 6.

Having obtained the D-DCMC capacity curves, at a given throughput of R , the $SNR_r^{EXIT}|_R$ required for maintaining this specific throughput can now be specified, again as seen in Fig. 6. Note that the normalised throughput R_n should be used for the sake of a fair comparison. Accordingly, the $SNR_r^{EXIT}|_R$ values are determined and listed in Tab. IV for different values of the normalised throughput R_n .

Then, similar to the OP of the DCMC channel formulated in Eq. (8) the term of $SNR_r|_R$ in Eq. (8) should be replaced by that of $SNR_r^{EXIT}|_R$, in order to construct an expression for the OP corresponding to the D-DCMC model. Accordingly, the OP of the scenario pertaining to the uncorrelated Rayleigh

Normalised throughput $R_n = R/\eta$	$SNR_{r _{R_n}}^{EXIT}$ [dB]	
	DBPSK ($\eta = 1$)	DQPSK ($\eta = 2$)
0.01	-12.03	-10.31
0.20	-3.13	-0.78
0.40	0.26	2.98
0.60	3.44	6.45
0.80	7.89	11.32
0.99	28.00	32.00

TABLE IV

$SNR_{r|_{R_n}}^{EXIT}$ VALUES CALCULATED WITH THE AID OF THE EXIT CHARTS TO BE INTRODUCED AT A LATER STAGE IN SECTION V FOR A D-DCMC SCHEME, WHEN VARIOUS NORMALISED THROUGHPUT R_n , NAMELY 0.01, 0.2, 0.4, 0.6, 0.8 AND 0.99, ARE CONSIDERED.

(fast) and the block Rayleigh (slow) fading channels can be quantified. For example, Fig. 7 visualises the resultant OP associated with diverse values of the normalised throughput R_n for the block Rayleigh fading channel, when for example DBPSK and DQPSK modulation schemes are employed.

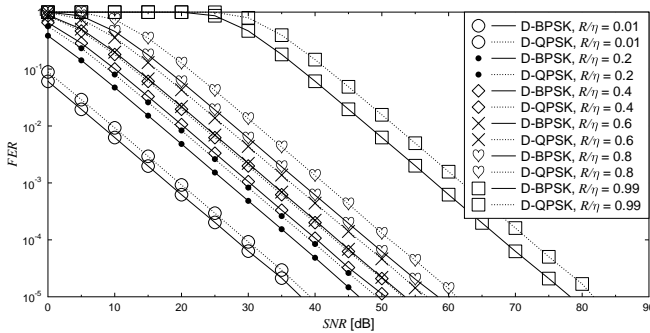


Fig. 7. Outage probability (FER) of the D-DCMC system operating over block Rayleigh fading channels, when DBPSK and DQPSK modulation schemes are used. The OP is plotted across different values of the normalised throughput R/η , namely 0.01, 0.2, 0.4, 0.6, 0.8, 0.99.

It should be noted that the EXIT chart based method applied for the D-DCMC based system can also be used for the DCMC based system and can provide similar results to those obtained by the formula provided in [118], as detailed in Section III-B. Thus, EXIT charts can be considered to be a generic tool for evaluating the OP and the outage capacity of an arbitrary coded modulation scheme. We will further clarify this aspect in the subsequent sections.

IV. OUTAGE CAPACITY

The concept of the outage capacity [116], [119]–[121] was shown to be useful for representing the best possible performance of a system, namely the SNR-versus-FER performance, where a given degree of QoS quantified in terms of the FER is required. This upper bound of the system's performance is useful for designing a specific system.

Let us consider a scenario, where the channel coding is unable to significantly improve the achievable error probability in block fading channels, as elaborated on in [116]. More specifically, in the presence of the small-scale fading, where the channel coefficients change for every symbol, the transmitter can send data at the rate of $R < C|h$, while maintaining an arbitrarily low error probability. However, it may not be possible to maintain a vanishingly low BER for a large-scale

fading channel, where the channel coefficients remain constant over a frame duration. Thus, the capacity of large-scale fading channels may become zero in the strict sense.

Hence, the outage capacity $C(\varepsilon)$ introduced in [116], [119] was defined as the highest possible value of transmission rate R , which was still capable of ensuring that the OP or FER becomes less than ε . It should be noted that the capacity of the quasi-static fading channels is dependent on the OP ε characterising the desired quality of transmission. Thus, the outage capacity is different from the channel capacity detailed in Section III-B and Section III-C.

Similar to the formulaic relationship established for the CCMC case in [116], it can be inferred from (8) that the outage capacity of the DCMC channel may be formulated as:

$$SNR(\varepsilon, \eta) = F^{-1}(1 - \varepsilon), \quad (10)$$

where $F(SNR_r|R)$ is the Complementary Cumulative Distribution Function (CCDF) of the combined fast-and slow-fading (small-and large scale-fading) envelope of $|h|^2 = |h_s|^2|h_f|^2$, which is defined as

$$F(SNR_r|R) = Pr \left\{ |h_s|^2 > \frac{SNR_r|R}{SNR} \right\}. \quad (11)$$

Note that $F(SNR_r|R)$ depends on the transmission rate R , while the corresponding SNR_r may be calculated by the method illustrated in Section III-B and Section III-C, where the EXIT chart tool is considered as a generic tool. In order to provide a fair comparison of the different-throughput modulation schemes, the CCDF $F(SNR_r|R_n)$ of the SNR_r is used at the same value of the normalised transmission rate R_n . Accordingly, the transmission rate of Eq. (11) should be replaced by the normalised transmission rate R_n .

A. Coherent schemes

For the outage capacity of the DCMC system, let us first recall the DCMC capacity presented in Section III-B. Again, at a given normalised throughput of R_n , we can readily identify the receive signal to noise power ratio $SNR_r|R_n$ required for maintaining R_n from the DCMC capacity curves, namely those plotted in Fig. 4. As a result, the $SNR_r|R_n$ values corresponding to the normalized throughput R_n are obtained and summarised in Tab. III. The $SNR_r|R_n$ values of Tab. III are employed for computing the CCDF of $F(SNR_r|R_n)$ defined by Eq. (11).

Having computed the CCDF of $F(SNR_r|R_n)$, it is now ready to calculate the minimum value of the SNR required for achieving a given OP of ε by applying Eq. (10). For the sake of comparing different modulation schemes, the notation $C_n(\varepsilon)$ is defined as the normalised outage capacity, which is given by

$$C_n(\varepsilon) = \frac{C(\varepsilon)}{\eta}, \quad (12)$$

where $C(\varepsilon)$ is the outage capacity determined by the relationship of Eq. (10), while η is the number of modulated bits used for representing a symbol in the modulation scheme of consideration.

As a result, the normalised outage capacity $C_n(\varepsilon)$ of Eq. (12) can be calculated, when the OP of ε is known. For example, the curves representing the outage capacity are plotted in Fig. 8 for a range of OP values ε , namely for $\varepsilon = 10^{-1}, 10^{-2}, 10^{-3}$, when the BPSK and the QPSK modulation schemes are employed in the block Rayleigh fading channel.

Let us now exemplify the above-mentioned steps by considering a specific system employing the parameters summarised in Tab. V.

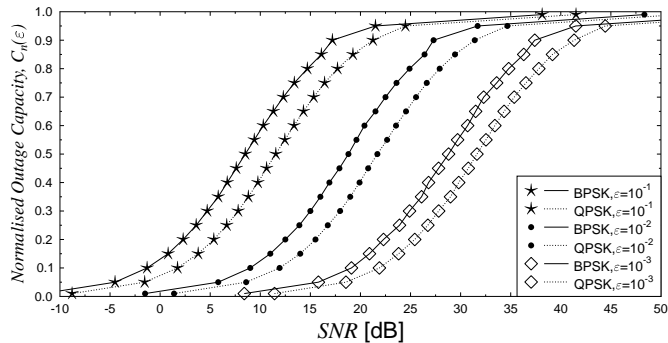


Fig. 8. Outage capacity of the DCMC calculated by Eq. (10) upon the CCDF of $F(SNR_r|R)$ defined by Eq. (11), for the range of the OP η , namely $10^{-1}, 10^{-2}$ and 10^{-3} , when the BPSK and the QPSK modulation schemes are employed for communicating over the block Rayleigh fading channel.

Parameters	Values
Transmission rate	$R = 1$ [Bit Per Symbol (BPS)]
Modulation scheme	QPSK
Modulation lever	$L = 4$
Number of bit per symbol	$\eta = 2$ bits
Equivalent channel coding rate	$R_c = 0.5$
Required OP	$\varepsilon = 10^{-3}$

TABLE V

THE RELATING PARAMETERS OF THE ILLUSTRATIVE SYSTEM EMPLOYING QPSK MODULATION (NUMBER OF MODULATION LEVELS $L = 4$ AND NUMBER OF MODULATED BITS PER SYMBOL $\eta = 2$) AND A CHANNEL CODING SCHEME HAVING A CODING RATE $R_c = 0.5$, WHICH RESULTS IN THE INFORMATION RATE $R = 1.0$. THE OUTAGE CAPACITY CORRESPONDING TO THE OP $\varepsilon = 10^{-3}$ IS CALCULATED UPON THE LISTED PARAMETERS.

Since a QPSK modulation scheme is employed in the example considered, we can have $\eta = 2$ and $L = 2^2 = 4$ either as inputs for the channel capacity formulae of DCMC capacity detailed in [118] or as parameters for estimating the corresponding channel capacity using the EXIT chart based method advocated. The resultant capacity curve is shown in Fig. 9. Accordingly, given the transmission rate of $R = R_c\eta = 0.5 \times 2.0 = 1.0$, the associated signal-to-noise ratio of $SNR_r|R = 1.793$ dB can be determined in Fig. 9. Having computed the CCDF of $F(SNR_r|R = 1.793)$ plotted in Fig. 10, we can then compute the minimum SNR required for maintaining a given OP of $\varepsilon = 10^{-3}$ by substituting $\eta = 2$ and $\varepsilon = 10^{-3}$ into Eq. (10). As a result, the $SNR = 31.63$ dB shown in Fig. 10 corresponds to an OP of $\varepsilon = 10^{-3}$. Naturally, the point having $R = 1.0$ BPS and $SNR = 31.63$ dB constitutes a single point on the outage capacity curve plotted in Fig. 11. Repeatedly, other SNR values associated with different values of R are calculated in order to form the outage capacity curve plotted in Fig. 11, provided that the same OP of $\varepsilon = 10^{-3}$ is considered.

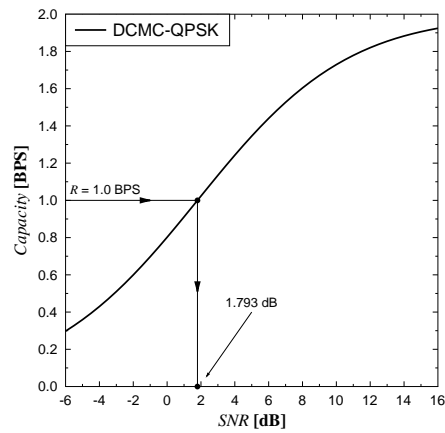


Fig. 9. The DCMC capacity curve for small-scale Rayleigh fading channel, when the QPSK modulation is employed. The value of $SNR_r|R$ corresponding to $R = R_c\eta = 0.5 \times 2.0 = 1.0$ is specified on the DCMC capacity curve.

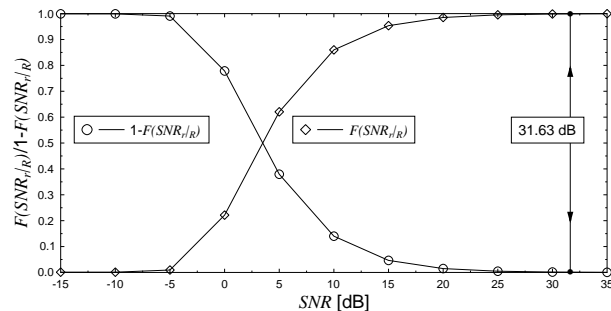


Fig. 10. The CCDF of $F(SNR_r|R)$ given in Eq. (11) and its offset function of $(1 - F(SNR_r|R))$ are calculated across different values of SNR for the value of $SNR_r|R = 1.793$, which is associated with the specific system having the relevant parameters listed in Tab. V.

In brief, the specific point at $R = 1.0$ BPS and $SNR = 31.63$ dB for $\varepsilon = 10^{-3}$ recorded in Fig. 11 may be interpreted as follows. If the SNR_r value is equal to or lower than 31.63 dB, the maximum outage capacity is equal to 1.0 BPS, provided that the OP of $\varepsilon = 10^{-3}$ is guaranteed. Viewed from a different perspective, if we have $SNR_r \leq 31.63$ dB at the receiver and the transmission rate is $R = 1$ BPS, the best possible quality of transmission is achieved at an OP of $\varepsilon = 10^{-3}$.

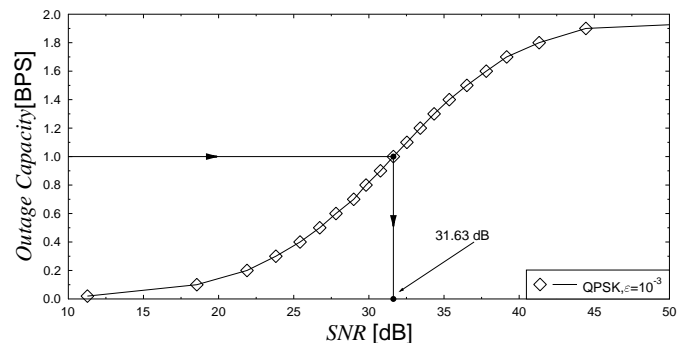


Fig. 11. The outage capacity of Eq. (11) corresponding to the OP value of $\varepsilon = 10^{-3}$ for the DCMC system characterised by Tab. V.

B. Non-coherent schemes

It should be noted that the general outage capacity formula of Eq. (10) can also be used for the D-DCMC case, where the CCDF $F(SNR_r|_R)$ of the achievable rate R is replaced by $F(SNR_r^{EXIT}|_R)$, which can be obtained by substituting the value of $SNR_r|_R$ in Eq. (11) by that of $SNR_r^{EXIT}|_R$.

Note that the CCDF $F(SNR_r^{EXIT}|_R)$ depends both on the transmission rate R and on the modulation scheme employed. The two parameters are used for specifying the $SNR_r^{EXIT}|_R$ value on the corresponding capacity curve calculated by the EXIT-chart based method, as detailed in Section III-C, where the capacity curves of DBPSK and DQPSK are plotted in Fig. 6. Similarly to the DCMC case, the normalised transmission rate R_n should be employed for the sake of appropriately characterising different modulation schemes, such as DBPSK and DQPSK. Hence, the term $SNR_r^{EXIT}|_R$ is substituted by the term $SNR_r^{EXIT}|_{R_n}$.

Accordingly, having calculated $SNR_r^{EXIT}|_{R_n}$ values listed in Tab. IV, the CCDF $F(SNR_r^{EXIT}|_{R_n})$ similarly presented by Eq. (11) is obtained. Then, the CCDF $F(SNR_r^{EXIT}|_{R_n})$ can be used in conjunction with Eq. (10) for calculating the outage capacity of a perfect D-DCMC capacity-achieving system. For the sake of comparison between different modulation schemes, namely DBPSK and DQPSK, the normalised outage capacity $C_n(\varepsilon)$ defined by Eq. (12) is utilised for characterising the outage capacity of a perfect D-DCMC capacity-achieving system. As a result, we have Fig. 12 showing the normalised outage capacity pertaining to a range of OP values ε , namely to $\varepsilon = 10^{-1}, 10^{-2}$ and 10^{-3} , when the DBPSK and DQPSK modulation schemes are used for communicating over the block Rayleigh fading channel.

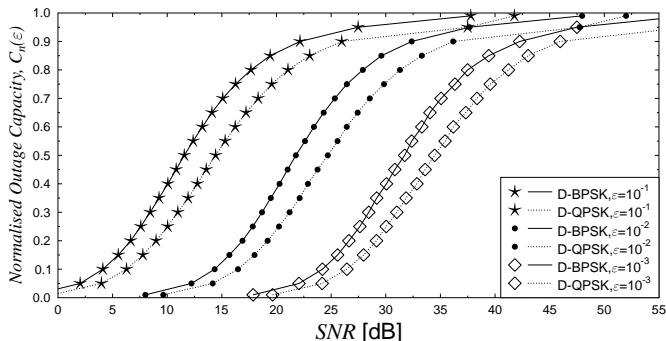


Fig. 12. The normalised outage capacity $C_n(\varepsilon)$ of the D-DCMC associated with the range of OP values ε , namely with $\varepsilon = 10^{-1}, 10^{-2}$ and 10^{-3} , is calculated by for the cases of employing the DBPSK and the DQPSK modulation schemes, when communicating over the block Rayleigh fading channel.

V. NEAR-CAPACITY CHANNEL CODE DESIGN

As portrayed in Fig. 2 about the architecture of our tutorial, after having detailed both OP and outage capacity, which can be served as benchmarks for the EXIT-chart based near-capacity design, we are now at a convenient position to present the design principles with the aid of illustrative examples.

A. EXIT-chart based code design principles

The design principles that we present here are based on exploiting the basic properties of EXIT charts, which are

detailed in Section II-A. According to the first property, EXIT charts can be used for visually observing the flow of soft-information exchanges. Hence, the benefits of iterations between the components of the composite coding schemes may be comprehensively visualised by diagrams. As a result, both 3D-EXIT [39], [122]–[124] and 2D-EXIT [44], [125], [126] charts have been shown to be helpful in investigating complex composite coding schemes.

The second property of EXIT charts [31], [77], [85] is that the area under the EXIT curve of an inner decoder component reflects the corresponding channel capacity. Accordingly, the designer is able to measure and compare the different channel capacities in order to facilitate the design of composite coding schemes as well as to determine the SNR-distance from the capacity of a specific coding scheme.

In the context of irregular code designs [44], [45], [125], [126], the irregular outer code employed is capable of adjusting the shape of its EXIT curve to match that of the corresponding inner amalgamated code. In such irregular codes, the IrCC may be used as a typical example of the outermost coding stage of a serially concatenated scheme. Based on a number of designs using irregular codes [44], [45], [125], [126], we summarise the associated design guidelines in the form of the following two-step procedure:

- **Step1:** Create the EXIT curve of the amalgamated inner decoder. The amalgamated inner decoder can be constituted by multi-component schemes, for example by the above-mentioned URC having a beneficial IIR with the inner-most detector constituted by the demodulator. An appropriate number of iterations between the components, for example the number of decoding iterations between the URC decoder and the inner-most detector, is decided based on exploiting the second properties of the EXIT charts. More specifically, the area under the EXIT curve of this amalgamated inner decoder represents the respective achievable DCMC capacity [31]. Naturally, a high number of iterations would incur a high complexity, the design objective is to opt for the minimum number of iterations, which only result in a marginal capacity loss.
- **Step2:** Carefully choose the overall coding rate of the outer IrCC encoder in order to match it to the shape of the amalgamated inner decoder. The EXIT curve matching algorithm of [30] may then be employed for searching for the most appropriate configuration of the outer code. The matching algorithm aims for finding a set of codes facilitating decoding convergence to a vanishingly low BER at the lowest possible SNR_r , where a narrow but marginally open EXIT chart tunnel would appear in the EXIT chart.

In what follow, the general principle of the two-step procedure briefly above-described will be demonstrated with the aid of specific design examples detailed in Section V-B, Section V-C and Section VI-C. As visualised in the architecture of the manuscript portrayed in Fig. 2, the specific design examples of Irregular Convolutional Coded Unity Rate Coded M-ary Phase Shift Keying (IrCC-URC-MPSK), Irregular Convolutional Coded Unity Rate Coded Differential M-

ary Phase Shift Keying (IrCC-URC-DMPSK) and Irregular Convolutional Coded Unity Rate Coded Space Time Trellis Coded M-ary Phase Shift Keying (IrCC-URC-STTC-MPSK) coding arrangements will be respectively presented.

B. IrCC-URC-MPSK coding scheme

In this section, the design principles summarised in Section V-A are illustrated by a specific design example, namely those of a coherent-detection based scheme constituted by the near-capacity IrCC-URC-MPSK scheme, which may be used in a transmission system portrayed in Fig. 13.

At the transmitter side seen in Fig. 13, an information frame of N bits is encoded by the IrCC encoder having a coding rate of R_c , in order to produce an output frame having a frame length of N/R_c bits. The frame is then interleaved by the interleaver π before being encoded again by the URC encoder for providing a URC-encoder frame of the same length, which is of N/R_c bits. The frame from output of the URC encoder is modulated by a modulation scheme employing η bits for representing a symbol, before transmitting to the receiver side, as seen in Fig. 13.

At the receiver side pictured in Fig. 13, the signals received during a single frame duration are demodulated then decoded by the URC decoder before entering the iteratively decoding process of J iterations occurring between the inner decoder and the outer IrCC decoder, where the interleaver π and deinterleaver π^{-1} are employed in each iteration. The inner decoder component is an amalgamated arrangement comprising the demodulation block and the URC decoder, as seen in Fig. 13.

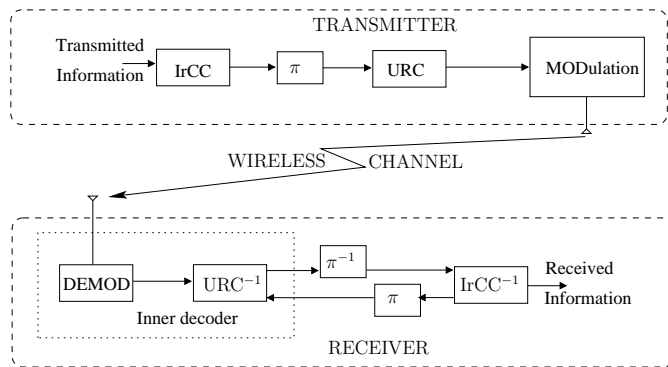


Fig. 13. Architecture of a transmission system employing IrCC-URC-MPSK scheme.

1) *EXIT-charts matching and optimisation*: By invoking the EXIT chart-aided design principles presented in Section V-A, the specific design for IrCC-URC-QPSK scheme can be summarised as follows:

Step1: Create the EXIT curve of the inner decoder constituted by the Unity-Rate Code and Quadrature Phase-Shift Keying (URC-QPSK) scheme for different SNR_r values for respective outer codes, namely $SNR_r = 3.6, 3.4, 3.2, 3.0$ and 2.8 dB for the 17-subcode IrCC in Fig. 14, as well as namely $SNR_r = 2.7, 2.6, 2.5, 2.4$ and 2.3 dB for the 36-subcode IrCC in Fig. 15. The two outer codes of both the 17-subcode

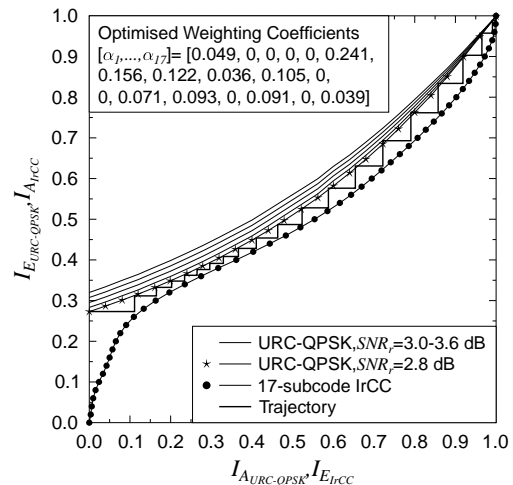


Fig. 14. The EXIT curves of the inner decoder URC-QPSK and the outer decoder 17-subcode IrCC for a single transmission link along with the Monte-Carlo simulation based decoding trajectory, provided that $R_c = 0.5$.

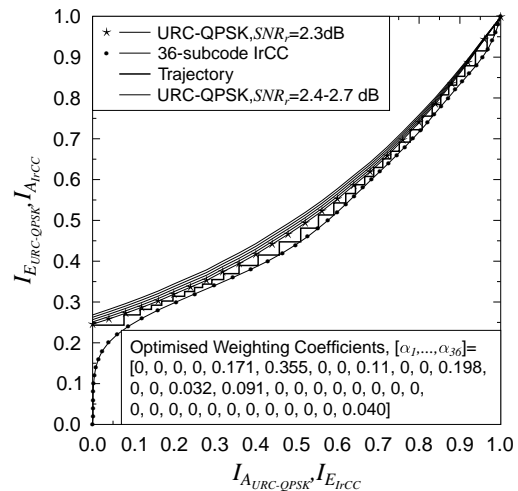


Fig. 15. The EXIT curves of the inner decoder URC-QPSK and the outer decoder 36-subcode IrCC having the coding rate $R_c = 0.5$ for a single transmission link along with the Monte-Carlo simulation based decoding trajectory.

IrCC and of the 36-subcode IrCC are presented in parallel in Tab. VI for highlighting how a near-capacity performance can be achieved by adjusting the configuration of the outer code, namely by adjusting the number and weight of the subcodes.

It shown by Fig. 16 that there is no iterations within the inner decoder component, since no improvement in the capacity is seen when performing iterative decoding at the inner decoder of URC-QPSK. More specifically, it is seen in Fig. 16 that the capacity of the URC-QPSK scheme almost coincides with the DCMC-QPSK curve, which confirms that no iterations between URC and QPSK demodulator are required. Hence, a narrow tunnel is created between the EXIT curve of the outer IrCC decoder and the inner URC-QPSK decoder is sufficient to ensure that a near-capacity coding scheme is conceived.

Step2: The system throughput is set, for example to $R = 1$. Then, given the IrCC code rate of for example $R_c = 0.5$,

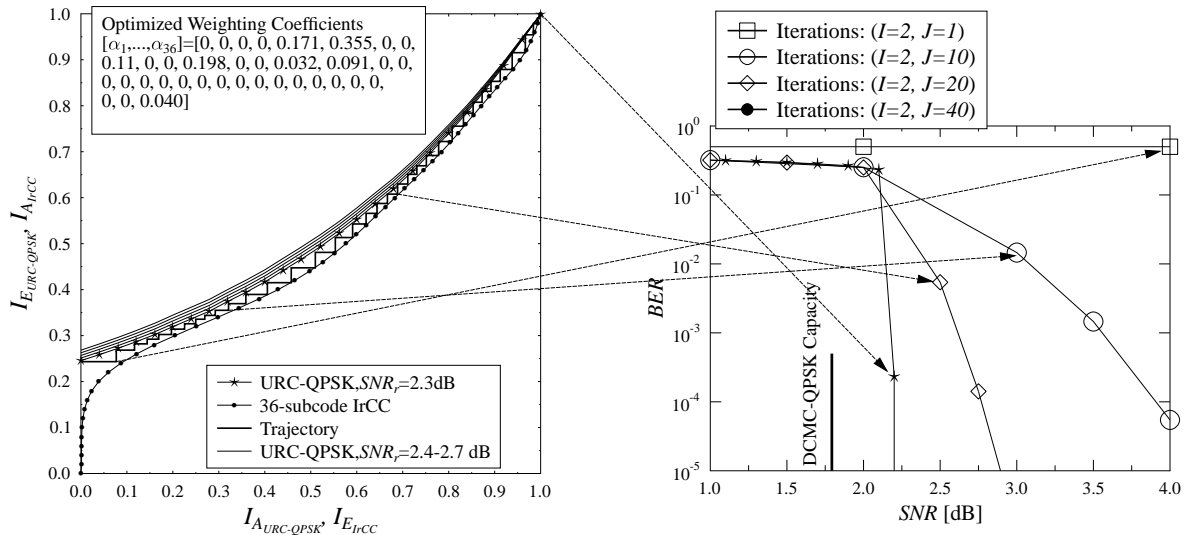


Fig. 17. Performance of the IrCC36-URC-QPSK scheme under Rayleigh small-scale fading conditions, when different numbers of iterations are applied.

C. IrCC-URC-DMPSK coding scheme

For the non-coherent based schemes, the EXIT-chart based design principle given in Section V-A can be invoked for facilitating the near-capacity coding design, for example of the IrCC-URC-Multiple-Symbol Detection aided Differential M-ary Phase-Shift Keying (IrCC-URC-MSDD-aided-DMPSK) scheme. The scheme may be employed in the system portrayed in Fig. 18.

In the system described by Fig. 18, the transmitted frame of N bits at the transmitter side is first encoded by the IrCC encoder having the coding rate R_c , in order to produce an egress frame of N/R_c bits. The egress frame is mixed by the first interleaver π_1 before being encoded by the URC in order to introduce the resultant frame of the same size. The frame at the output of the URC encoder is again blended by the second interleaver π_2 before being modulated by the differential modulation for transmitting over wireless channel, as seen in Fig. 18.

At the receiver side of the system portrayed in Fig. 18, the signals received from an antenna during a frame duration are first processed in I inner iterations by iteratively performing two steps, namely conducting demodulation using the MSDD method and decoding at the URC decoder. Once having performed the I inner iterations, the resultant frame is fed into J so-called outer iterations. It should be noted that each of J outer iterations contains I inner iterations. As a result, the receiver featured in Fig. 18 has to perform totally $I \times J$ inner iterations, in order to retrieve the transmitted frame.

The primary goal for designing the IrCC-URC-MSDD-aided-DMPSK scheme is to determine important parameters stipulating the near-capacity of the systems, namely the optimal values of I inner iterations, J outer iterations as well as configurations of the irregular outer code characterised by weighting coefficients of IrCC. In particular, the EXIT-chart tool is employed for predicting the number of inner and outer iterations, for formatting the IrCC encoder as well as for determining the D-DCMC capacity of the non-coherent

inner most component of the coding scheme, namely the DMPSK and the Unity Rate Coded DMPSK (URC-DMPSK). Moreover, the EXIT chart tool may be used for appraising the design by evaluating the channel capacities associated with different design steps.

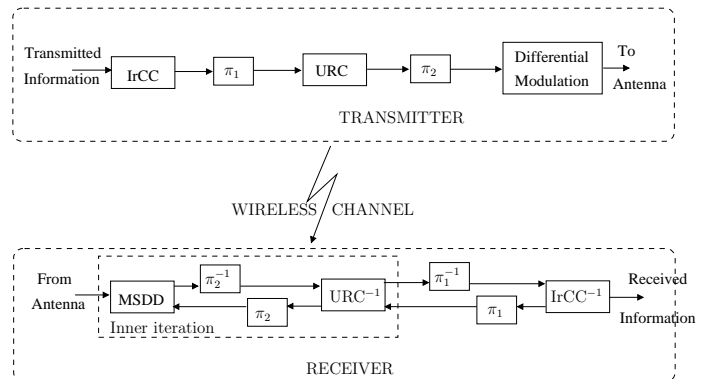


Fig. 18. Architecture of the IrCC-URC-MSDD-aided-DMPSK scheme.

1) *EXIT-chart design for IrCC-URC-MSDD-aided-DMPSK*: Similar to the manner used for presenting the design example of the coherent scheme in Section V-B, for the sake of clarity, the generic EXIT-chart based design principle presented in Section V-A is demonstrated by applying for a specific example. More specifically, the IrCC-URC-Differential Quadrature Phase Shift Keying (IrCC-URC-DQPSK) associated with MSDD $N_w = 4$ is designed by using the generically applicable EXIT-chart aided method, which is summarised as follows:

Step1: In order to optimise the number I of inner iterations between URC and MSDD-aided DEModulation (MSDD-aided-DEM), the area property of EXIT-charts detailed in Section II-A2 can be exploited for determining the achievable capacities of the URC-MSDD-aided-DQPSK and IrCC-URC-MSDD-aided-DQPSK systems, which are quantified

in Fig. 20. In brief, It is shown by Fig. 20 that the capacity curve of the outer scheme (URC-MSDD-aided-DQPSK scheme) approaches that of the inner scheme (the MSDD-aided-DQPSK arrangement), when $I > 1$ inner iterations are employed for the composite outer decoder of the URC-MSDD-aided-DQPSK decoder. It is also demonstrated in Fig. 20 that the attainable capacity improvement becomes negligible for $I > 2$. Therefore, the number of inner iterations should be fixed to its optimal value of $I = 2$ thereafter;

Step2: Similar to the design procedure presented in Section V-B1. The EXIT curve matching algorithm of [46] can be employed for generating the optimised weighting coefficients $\alpha_i, i = 1, \dots, 36$, of the 36 different-rate subcode IrCC codes. As a result, the weighting coefficients of the IrCC associated with SNR_r value are obtained, as noted in the upper left side of Fig. 19. Then, these parameters are sufficient to generate the respective trajectory, which exhibits the number J of the outer iterations between IrCC and the amalgamated arrangement URC-MSDD-aided-DQPSK, as seen in the left side of Fig. 19.

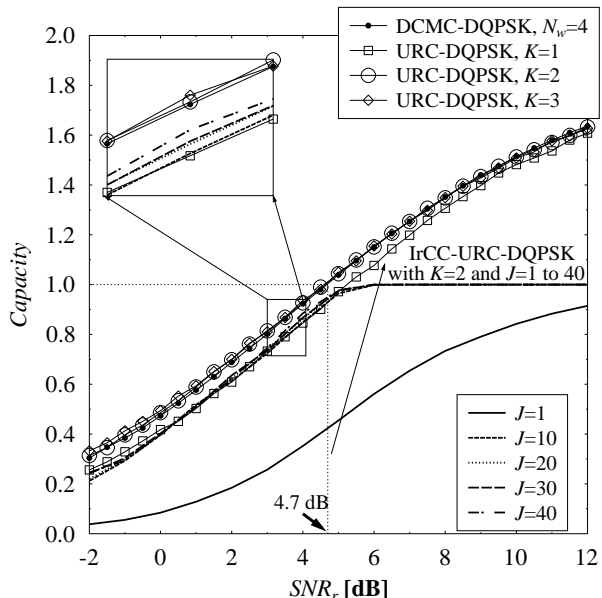


Fig. 20. Channel capacity comparison for the MSDD-aided-DQPSK, URC-MSDD-aided-DQPSK and IrCC-URC-MSDD-aided-DQPSK based systems when having the normalised Doppler frequency of $f_d = 0.03$.

2) *Performance of IrCC-URC-DMPSK coding scheme:* The numerical results of Fig. 20 also show that for a sufficiently high number of say $J \geq 30$ outer iterations, the distance between the capacity curve of the IrCC-URC-MSDD-aided-DQPSK scheme and that of the DCMC-MSDD-aided-DQPSK arrangement is less than 0.5 dB.

Setting IrCC coding coefficients as seen in Fig. 19, as well as the number of inner iterations to $I = 2$, and the number of outer iterations to $J = 1, 10, 20, 25, 30$, we can see the relationship between the performance of the coding scheme and its complexity, where the complexity is represented by the number J of iterations. This relationship can also be observed on Fig. 20, where again the capacity of the system is seen to vary along with the number J of outer iterations. This suggests that the area property of the EXIT chart can be beneficially

used for determining the most appropriate number of iterations between a pair concatenated coding components.

D. Benefit of sub-frame transmission

The EXIT chart-aided design procedure has been shown to be an effective tool of designing irregular coding schemes that are capable of approaching the fast-fading channel's capacity. More explicitly, the fast-fading channel's capacity may be determined by the versatile tool of EXIT charts, as detailed in Section III-A, Section III-B and Section III-C. When slow fading is encountered, the concept of outage probabilities detailed in Section IV has to be used for providing a benchmarker for the coding schemes under study. In [127]–[132], the sub-frame based transmission mode has been invoked in slow-fading environments for the sake of improving the system's performance, which is hence expected to be as good as that exhibited in fast-fading environments. To conclude our related discussion, Section V-D aims for accentuating the benefit of employing the sub-frame based transmission mode as well as the advantages of using the outage probability as a benchmarker for near-capacity coding schemes.

In the fast (small-scale) fading channel, the transmitter can send data at the rate of $R < C|_h$, while maintaining an arbitrarily small error probability, but this idealised performance cannot be maintained for block fading channel [116]. Let us take one of the near-capacity coding schemes, for example the IrCC-URC-MSDD-aided-DQPSK scheme designed in previous sections to illustrate the scenario. As above-mentioned, in the practical system [127]–[130], each channel-encoded frame tends to be transmitted in an N_{sub} sub-frames, where the average SNR value at the receiver side may be formulated as:

$$SNR_r = \frac{E[|h_s|^2]}{N_0} = \frac{\sum_{i=1}^{N_{sub}} |h_{s,i}|^2 / N_{sub}}{N_0}, \quad (13)$$

with $h_{s,i}$ representing the block shadow fading corresponding to the i^{th} sub-frame of the channel-encoded frame.

It is expected that by partitioning each encoded frame into subframes [131], [132], the diversity order of the transmission link is increased, thereby improving the attainable performance of the transmission link for transmission over the block fading channel. As a result, the detrimental influence of a single deep fade spreads over a larger number of encoded frames. Hence, the propagation effects of a fast fading scenario can be mimicked.

Let us continue by considering the performance of the IrCC-URC-MSDD-aided-DBPSK coding scheme for pointing out the specific benefit of employing of subframes. More specifically, it can be seen in Fig. 21 that while the number N_{sub} of the sub-frames is increasing from $N_{sub} = 1$ to $N_{sub} = 10^4$, the performance of the IrCC-URC-MSDD-aided-DBPSK scheme recorded for transmission over a channel, where both the block shadow fading and the small-scale Rayleigh fading are taken into consideration, approaches that of the IrCC-URC-MSDD-aided-DBPSK scheme communicating over the small-scale Rayleigh fading channel.

In brief, the employment of the sub-frame based transmission can be interpreted as follows. A near-capacity channel

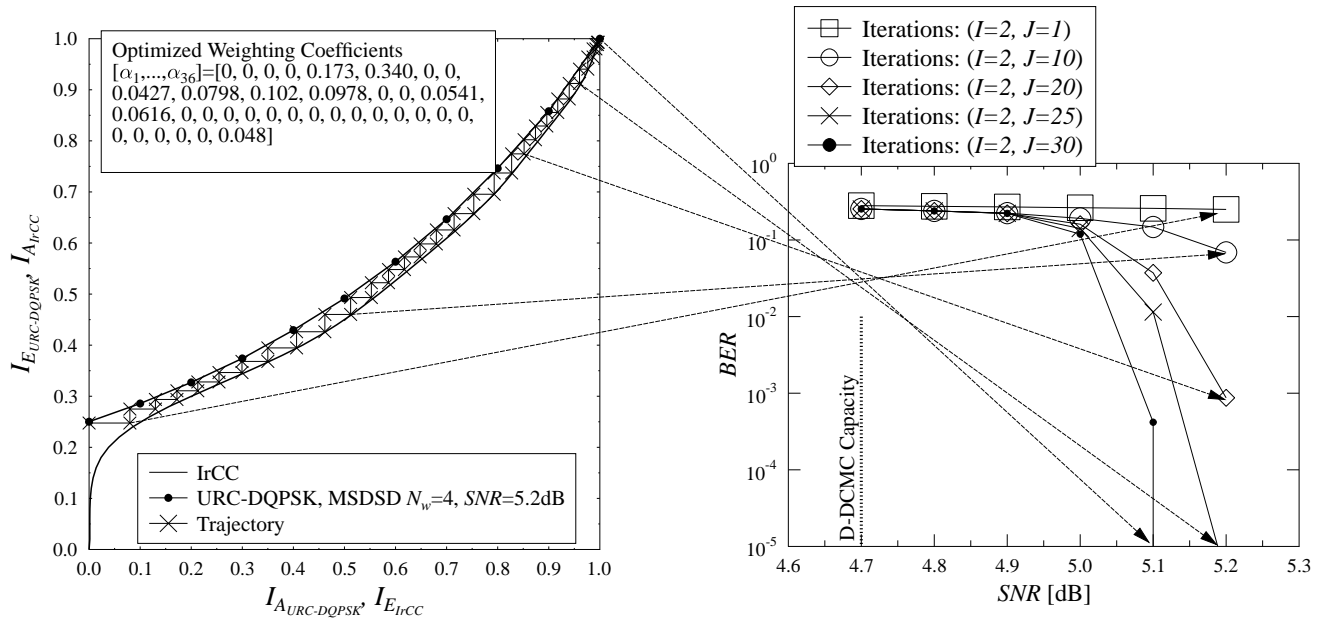


Fig. 19. The EXIT curves and performance of the IrCC-URC-MSDD-aided-DQPSK scheme.

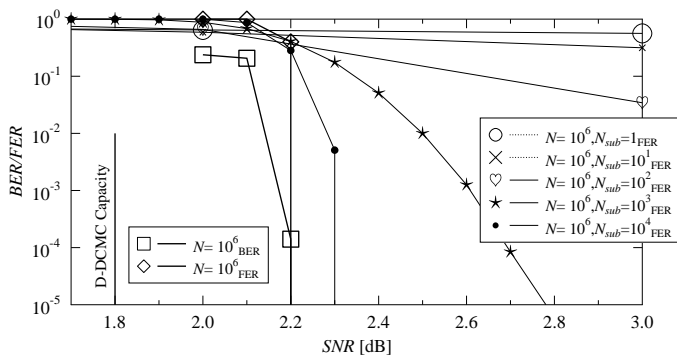


Fig. 21. Performance of the IrCC-URC-MSDD-aided-DBPSK scheme in the small-scale Rayleigh fading channel ($N = 10^6_{BER}$ and $N = 10^6_{FER}$) with the normalised Doppler frequency $f_d = 0.03$ as well as in the block fading channel, the number of sub-frames ranging from $N_{sub} = 1$ to $N_{sub} = 10^4$ for allocating an encoded frame of $N = 10^6$ bits.

coding scheme can be designed for the sake of providing the time diversity within a frame. Hence an arbitrarily low BER may be achieved in a small-scale fading environment, where the channel conditions vary on a symbol-by-symbol basis. For the block fading channel, where the channel conditions within a frame duration are determined by a single channel coefficient, inter-frame diversity provided by the sub-frame based transmission regime may be exploited for attaining a good performance.

E. Non-Coherent versus Coherent Near-Capacity Schemes

Having presented philosophy of the near-capacity designs for both the coherent detection schemes of Section V-B and for the non-coherent detection schemes of Section V-C may pose to a dilemma, namely as to whether the coherent or non-coherent system would be favoured in a given scenario. In order to discuss this dilemma, let us now provide further insights into the effects of channel estimation errors on the

performance of coherent systems. The influence of channel estimation in coherent detection based schemes can be characterised by the term θ defined as the normalised channel estimation accuracy, which may be formulated as:

$$\theta = 100 \times \mathbb{E} \left[1 - \frac{||h| - |\hat{h}||}{|h|} \right], \quad (14)$$

where \hat{h} is the estimated value of the channel coefficient h . It should be noted that if we have $\frac{||h| - |\hat{h}||}{|h|} > 1$, the accuracy is equal to zero, $\theta = 0$. For the sake of readability, the estimated channel coefficient of \hat{h} is deemed to be formed by

$$\hat{h} = h + n_{est}, \quad (15)$$

where n_{est} is likened to the estimated noise springing from the inaccuracy of the channel estimator. The estimated noise of n_{est} can be further considered as an AWGN process having a variance of $N_{0,est}/2$ per dimension at a nominal estimated signal to noise ratio of SNR_{est} . Accordingly, as seen in Fig. 22, the normalised channel estimation accuracy of θ given in (14) varies according to different frame lengths N ranging from $N = 10^1$ bits to $N = 10^6$ bits, as plotted against different values of SNR_{est} listed in Tab. VII.

The benefit of introducing the estimated signal to noise ratio of SNR_{est} is that we can examine the performance's degradation of the coherent system employing a practical channel estimator, compared to the performance of the coherent system assuming that the channel state information is available at the receiver.

It can be inferred from Fig. 22 that the value of SNR_{est} corresponding to a given value of the channel estimation accuracy can be calculated. For example, Table VII lists the values of SNR_{est} associating with different values of normalised channel estimation accuracy, namely from 10% to 100%.

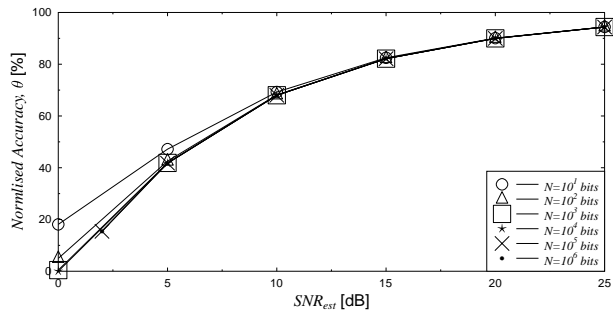


Fig. 22. The normalised channel estimation accuracy of θ , when considering different frame lengths N ranging from $N = 10^1$ bits to $N = 10^6$ bits.

Normalised channel estimation accuracy, θ [%]	SNR_{est} [dB]
10%	1.676
20%	2.518
30%	3.554
40%	4.783
50%	6.276
60%	8.127
70%	10.571
80%	14.027
90%	20.015
100%	100.667

TABLE VII

SNR_{est} VALUES CORRESPONDING TO DIFFERENT VALUES OF THE NORMALISED CHANNEL ESTIMATION ACCURACY θ RANGING FROM $\theta = 10\%$ TO $\theta = 100\%$, WHEN APPLYING THE FRAME LENGTH $N = 10^6$ BITS.

Employing the channel estimation noise conventionally corresponding to SNR_{est} given by Table VII, we can evaluate the performance of the coherent coding schemes, for example IrCC-URC-QPSK scheme, when different levels of the channel estimation accuracy are achieved by the channel estimator. By doing comparison between the performance of the coherent scheme and that of the non-coherent counterpart, the threshold value of the channel estimation accuracy can be determined.

For example, the performance comparison of the IrCC-URC-QPSK scheme in different regimes, namely both in the non-coherent and in the coherent regime was carried out by taking into consideration a realistic channel estimator. As seen in Fig. 23, the performance of the system employing IrCC-URC-DQPSK coding scheme is equivalent to that of IrCC-URC-QPSK, provided that of the channel estimator is capable of achieving an accuracy of $\theta = 60\%$. As a result, the threshold of $\theta = 60\%$ can be used by the system to switch between coherent and non-coherent detection regime.

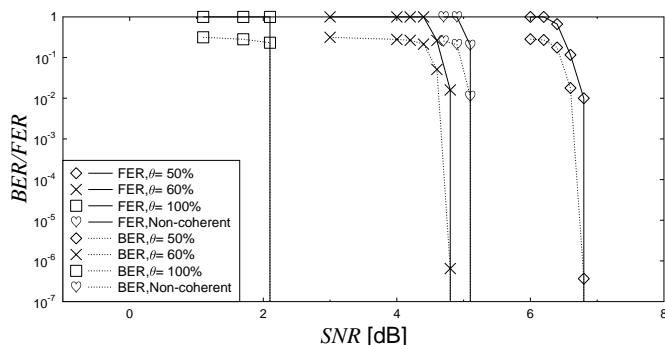


Fig. 23. Comparison of the non-coherent versus coherent: IrCC-URC-QPSK scheme versus IrCC-URC-MSDD-aided-DQPSK, the frame length of $N = 10^5$, when communicating over the small-scale Rayleigh fading channel.

VI. APPLICATION IN COOPERATIVE COMMUNICATION

Classically, relays have been used for extending the range of wireless communication systems [23], [133]–[138]. However, in recent years, numerous exciting new applications of relay aided communications have emerged [139]–[141], including the design of efficient cooperative protocols and of distributed signal processing techniques [142]. By designing sophisticated cooperative medium access protocols for the source and relay nodes [143], [144] in conjunction with appropriate modulation and coding [145], [146], it has been found that the diversity gain of the system can be substantially improved [147]. The cooperative protocols may be categorised depending on the specific operations [117], [148], [149] carried out at the relays, namely as amplify-and-forward (AAF), demodulation and forward (DemAF), decode and forward (DAF) as well as adaptive relaying protocol (AFP).

Distributed signal processing techniques cast in the context of multi-component coding schemes employing relay-aided transmissions focus on the joint signal and coding design at both the source, as well as at the relay and destination nodes. Such a joint coding design is referred to as distributed coding. Naturally, having the distributed nature constitutes the crucial difference between the distributed coding scheme and its conventional counterpart. The distributed nature manifests itself in terms of constructing of encoded codewords at the destination node, which are transmitted via different propagation paths. Having this distributed construction lends a higher degree of freedom to the system, which is achieved at the cost of a more complex design and implementation. The distributed coding schemes may be classified into five categories, namely distributed source-channel coding schemes [150]–[152], distributed network and channel coding [153], [154], distributed low density parity check codes (LDPC) [155], [156], distributed turbo coding schemes [157]–[159] and finally distributed space time coding [45], [160]. In all the above-mentioned distributed schemes [45], [151], [154], [156], [159], EXIT charts were shown to be an effective tool used for designing the distributed schemes for approaching the corresponding channel capacity.

In order to demonstrate the benefits of EXIT charts in designing distributed coding schemes, we will illustrate the code design principles presented in Section V-A with the aid of a typical example, where distributed turbo and space-time coding schemes were designed jointly. Let us commence by describing an example of the typical cooperative systems presented in Fig. 24, in which a source node (S) and a destination node (D) are communicating through $N_R = 2$ relay nodes (R) due to the low quality of the signal transmitted from the S node at the D node. Hence the SD link is often assumed to be unavailable [161]. For the case of considering the availability of the signal transmitted via the SD link, please allow us to refer interested readers to Ref. [45], [159]. Note that the number of relay nodes $N_R = 2$ is chosen for clarity of presentation. A transmission session of the system detailed in Fig. 24 is accomplished in two transmission periods. The first transmission period is for the transmission from the S node to the R nodes, while the other is for the transmission from

the R nodes to the D node.

A. Distributed System Model

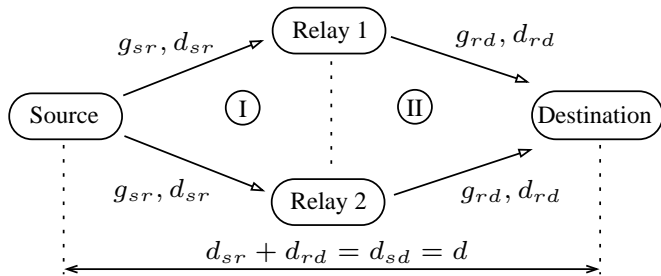


Fig. 24. The model of the distributed coding system in the absence of the source-destination link.

Typically, during the first transmission period, the S node transmits its coded frame to the R nodes. Then, after decoding and re-encoding the signals received from the S node, the two R nodes transmit the resultant coded frame to the D node during the second transmission period. At the destination, the signals received from the two single-antenna aided relays are combined, detected and decoded, in order to recover the information transmitted from the S node. Although the signals are transmitted from two separate R nodes having a single antenna, these signals are treated, as if they came from a single relay having two transmit antennas. Naturally, the two relays are required to collaborate, which is further elaborated on Section VI-B, where the structure of the distributed encoder and decoder is described.

As seen on the system model presented in Fig. 24, owing to the advantageous position, the relays have a benefit of the power-gain (or geometrical pathloss reduction) w.r.t. the source-to-relay and relay-to-destination links, namely g_{sr} and g_{rd} . The magnitude of the power-gain is proportional to the ratio of the two respective distances. Naturally, the power-gain of the source-to-destination link with respect to itself is unity, i.e. $g_{sd} = 1$. For the sake of simplicity, we may stipulate another assumption, namely that the R nodes are located on the straight line from the S node to the D node. For the convenience of presentation, the unconventional SNR_t [14], [45], [162] was defined as the ratio of the power transmitted from the transmitter to the noise power encountered at the receiver¹. Accordingly, we have the ratio of the received power to the noise power at the receiver

$$SNR_r = G + SNR_t, \quad (16)$$

where G (dB) is the power gain of the link.

B. Structure of Distributed Turbo Space-Time Coding

As above-mentioned, cooperative communication has been shown to be an effective technique of allowing single antenna aided users to share their antennas to create a virtual MIMO system, thus providing extra spatial diversity in wireless networks. Distributed turbo and space-time coding schemes [45],

¹This definition is unconventional, because it relates physical quantities measured at different locations. However, it is convenient for illustrating the benefit the geometrical pathloss reduction.

[157]–[160] are inherently capable of supporting VMIMO systems with the goal of facilitating near-capacity operation. An example of the distributed turbo coding scheme used for the system model portrayed in Fig. 24 is presented in Fig. 25. In the DC-IrCC-URC-STTC coding scheme depicted in Fig. 25, a two-stage encoder constituted by an Irregular Convolutional Code and Unity-Rate Code (IrCC-URC) is employed at the S node. By contrast, at both the two R nodes and D node, the three-stage coding scheme constituted by the IrCC-URC-STTC is employed. It should be noted that the collaboration of the two R nodes has to guarantee that at any instant only the signals of a single STTC component of the single-antenna R nodes is transmitted. Thus, the signals received at the D node are a combination of the signals received from the two relays during the second transmission period. Then, the signals received at the D node are treated, as if they arrived from a single relay transmitter equipped with two co-located transmit antennas. In the illustrative example, 8PSK modulation is employed for the two-stage IrCC-URC coding scheme of the S node, while only QPSK modulation is used for the three-stage IrCC-URC-STTC.

In the model of the distributed coding scheme depicted in Fig. 25, the information bit sequence u is encoded by the IrCC encoder at the S node for producing the coded sequence c , before passing c through the interleaver π_1 . The interleaved bit sequence is encoded by the URC encoder and then modulated using 8PSK or QPSK, in order to form the transmitted symbol sequence x . The signals y_{r1} and y_{r2} received at the both relays are iteratively decoded by the IrCC-URC decoders, as seen in Fig. 25, in order to estimate the original information bit sequences, u_1 and u_2 , at R node 1 and 2, respectively. Then the estimated bit sequences of u_1 and u_2 are passed through the IrCC-URC-STTC encoding process relying on the pair of interleavers, π_1 and π_2 , which are located between the IrCC encoder and URC encoder as well as between the URC encoder and the STTC encoder, respectively. These two interleavers facilitate the provision of hitherto in exploited extrinsic information for the iterative decoding process at the destination, where the iterations exchanging extrinsic information between the STTC decoder and the URC decoder are performed I times, before one of J times iteration between the URC decoder and the IrCC decoder is carried out, as detailed in Section VI-C. In other words, once I inner iterations are accomplished, one iteration of J outer iterations is triggered before passing the information back to the inner iterations. This process is repeated, until all the affordable number of J outer iterations are performed, as seen in the destination block of Fig. 25.

Then, QPSK modulation is employed at the output of the R node's STTC encoder. Note that the sequences transmitted by each of the relays, namely x_{r1} and x_{r2} , are created by choosing only one predefined output of the two-antenna 4-state STTC encoder of [11]. The sequence received at the D node, namely y_d seen in Fig. 25, is then subjected to the inverse process: y_d is demodulated, and finally the resultant sequence is decoded by two iterative decoders, namely by the URC-STTC decoder and the IrCC-[amalgamated-URC-STTC] decoder of Fig. 25. The decoded information bit sequence u'

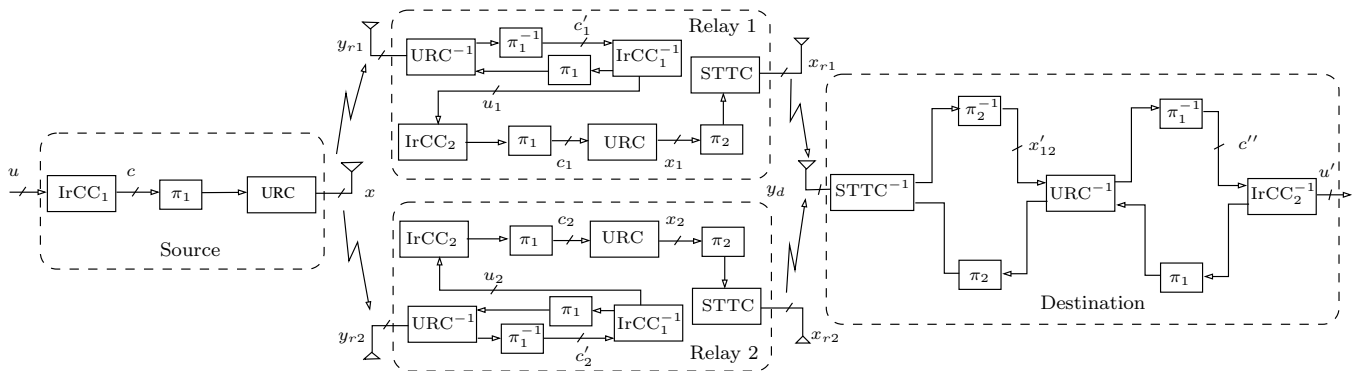


Fig. 25. The block diagram of the Distributed Concatenated Irregular Convolutional Code, Unity-Rate Code and Space-Time Trellis Code scheme for the system model presented in Fig. 24. This scheme relies on the IrCC-URC-STTC-MPSK arrangement detailed in Section VI-C and on the Irregular Convolutional Coded Unity Rate Coded M-ary Phase Shift Keying (IrCC-URC-MPSK) arrangement presented in Section V-B.

seen in Fig. 25 is compared to the original one for evaluating the performance of the system.

The URC, IrCC and STTC component codes have the code rates of R_{URC} , R_{IrCC} and R_{STTC} , respectively, where $R_{STTC} = 1$ in the example.

Accordingly, the system's overall throughput of η representing the relationship between the E_b/N_0 and SNR values of the system can be formulated as:

$$\eta = \frac{N_i}{N_s + N_r} = 0.6 [BPS], \quad (17)$$

where N_i is the number of information bits transmitted within a duration of $(N_s + N_r)$ symbol periods, while N_s and N_r are the number of symbols transmitted by the S node and the R node within a transmission session, respectively. It should be noted that the system's overall throughput η also denotes the average number of bits conveyed by a symbol transmitted in the distributed system. Hence, when comparing the distributed system to the single link transmission system, the system's overall throughput and the number of modulated bits defined in Section III-B are equivalent.

C. Design of distributed IrCC-URC-STTC-MPSK coding scheme

The design of the distributed coding scheme portrayed in Fig. 24 relies on the IrCC-URC-MPSK scheme presented in Section V-B and on the IrCC-URC-STTC regime portrayed in Fig. 26. Going beyond the design procedure presented in Section V-B and Section V-C, the tool of EXIT charts may also be used for optimising the BER performance of the entire distributed coding scheme, so that it becomes capable of approaching the corresponding cooperative channel capacity. In order to design such distributed coding schemes, we can use EXIT charts for finding the most appropriate configurations of the entire coding scheme. Hence the coding scheme becomes capable of attaining the best possible performance, provided that the position of relays and their transmit powers are given. Alternatively, we can pursue an adaptive approach, where a set of the most appropriate system configurations is determined by employing EXIT charts. Then the system will adaptively

adjust its various configuration to adapt to the specific relay positions and transmit powers available.

For the ease of presentation, the time-invariant approach is used here for portraying the design of the IrCC-URC-STTC-MPSK coding arrangement detailed in Fig. 26. According to the structure of the IrCC-URC-STTC scheme featured in Fig. 26, the bit stream at the transmitter side is first encoded by the IrCC encoder before it is fed into the interleaver π_1 , in order to get the interleaved input stream for feeding to the URC encoder. The output of the URC encoder is again scrambled by the interleaver π_2 before being encoded by the STTC detailed in Section II-C. This signal is then transmitted to the receiver side over wireless fading channels, as portrayed in Fig. 26.

At the receiver side, as seen in Fig. 26, the signals provided by the receive antenna are demodulated and decoded by the STTC decoder before being processed by the I inner iterations exchanging extrinsic information between the STTC decoder and the URC decoder. The resultant soft information extracted from the received signals by the inner iterations are then used as the input data for the J outer iterations exchanging extrinsic information between the IrCC encoder and the amalgamated inner component, which is the Unity Rate Coded M-ary Phase Shift Keying (URC-STTC-MPSK) arrangement. Hence, the design goals are to determine the most appropriate number of inner and outer iterations, as well as the weighting coefficients of the IrCC subcodes used in the IrCC codec.

Note that in the distributed coding scheme portrayed in Fig. 25, the IrCC-URC-STTC-MPSK coding scheme is invoked for constructing a virtual Multi-Input Multi-Output (MIMO) scheme constituted by the relay-aided system. In the following, we will show how the EXIT-chart based design principles outlined in Section V-A can be applied for designing the specific IrCC-URC-STTC coding scheme relying on MPSK modulation. Accordingly, we will present design results associated with the IrCC-URC-STTC-QPSK arrangement employing 17-subcode IrCC as a numerical example.

1) *EXIT-chart matching and optimisation of the IrCC-URC-STTC-MPSK scheme*: Firstly, the two-stage inner arrangement URC-STTC-QPSK is designed. Secondly, the design process

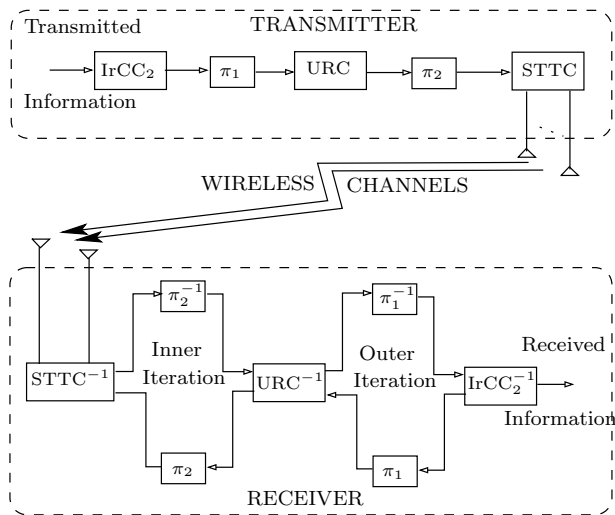


Fig. 26. The structure of the Irregular Convolutional Coded Unity Rate Coded Space Time Trellis Code (IrCC-URC-STTC) coding scheme.

is continued by viewing the three-stage IrCC-URC-STTC-QPSK coding arrangement as the two-stage-concatenated IrCC outer code and the amalgamated URC-STTC-QPSK inner code. Again the design guidelines introduced in Section V-A can be applied for both the two coding arrangements.

For the two-stage inner Unity Rate Coded Space Time Trellis Code Quadrature Shift Keying (URC-STTC-QPSK) arrangement, the design task can be interpreted as that of increasing the achievable channel capacity of the amalgamated URC-STTC-QPSK inner code, in order to approach that of a Space Time Trellis Coded (STTC) and STTC-QPSK aided system. Accordingly, the area property of EXIT charts can be exploited for calculating the DCMC capacity of the two inner-most coding arrangements, namely that of the Space Time Trellis Code Quadrature Shift Keying (STTC-QPSK) and URC-STTC-QPSK schemes. Then, based on the capacity of these two coding arrangements, the most appropriate number of iterations $I = 3$ is determined. As shown Fig. 27 shows that once at least $I = 3$ iterations had been applied, the achievable channel capacities of the STTC-QPSK and URC-STTC-QPSK systems become near-identical.

For the three-stage IrCC-URC-STTC-QPSK coding arrangement, firstly the EXIT chart of the URC-STTC-QPSK scheme is created for different receiver signal to noise ratios SNR_r . Secondly, EXIT-curve the matching algorithm is applied for the IrCC codes having a total rate of $R_c = 0.5$ for example, in order to determine the optimised weighting coefficients $\alpha_j, j = 1, \dots, 17$, of the 17-subcode IrCC codes corresponding to the lowest possible SNR_r . As a result, the EXIT-chart results corresponding to the optimised weighting coefficients reveal the optimal number of iterations between the IrCC and URC-STTC-QPSK block. This optimal number of iterations was found to be $J = 24$ in Fig. 27.

Again, by exploiting the area property of the EXIT-charts detailed in Section II-A2, the achievable DCMC capacities of the MIMO $_{2 \times 1}$ -QPSK, the STTC $_2 \times 1$ -QPSK, URC-STTC $_2 \times 1$ -QPSK and IrCC-URC-STTC $_2 \times 1$ -QPSK aided

systems are quantified for determining the associated capacity curves, as plotted in Fig. 27. It should be noted that the capacity of an inner arrangement sets an upper bound for the capacity of an outer arrangement. Hence, according to the afore-listed order, the capacity associated with the inner most arrangement MIMO $_{2 \times 1}$ -QPSK sets the maximum achievable capacity for all the systems employing the other schemes, namely the STTC $_2 \times 1$ -QPSK, URC-STTC $_2 \times 1$ -QPSK and IrCC-URC-STTC $_2 \times 1$ -QPSK, as seen in Fig. 27.

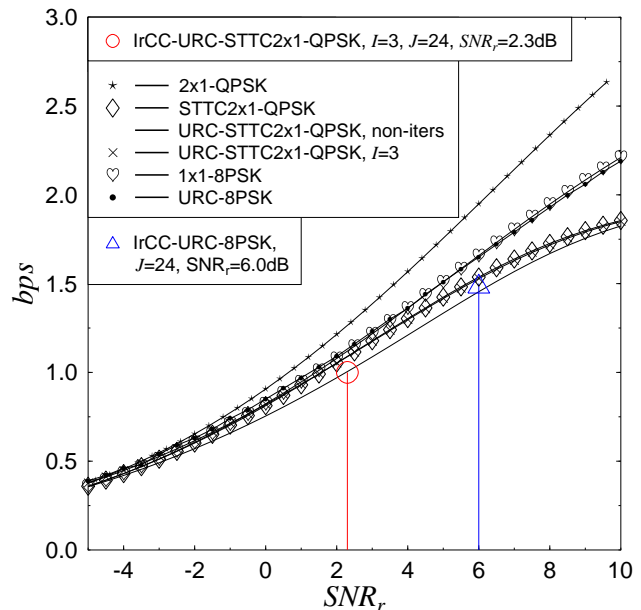


Fig. 27. Channel capacity comparison for the IrCC-URC-STTC $_{2 \times 1}$ -QPSK and IrCC-URC-8PSK systems.

Following the same procedure as illustrated by designing the IrCC-URC-STTC-QPSK, other coding arrangements relying on 8PSK and 16PSK, namely the IrCC-URC-STTC-8PSK and IrCC-URC-STTC-16PSK schemes were also designed. As a result, the corresponding weighting coefficients of the IrCC encoder are listed in Table VIII.

Arrangement (Turbo-cliff SNR_r)	Coefficients: $[\alpha_1, \alpha_2, \dots, \alpha_{17}]$
URC-STTC-QPSK (2.3 dB)	[0.05, 0, 0, 0.169, 0.219, 0.036, 0.023, 0.0166, 0.149, 0.015, 0.089, 0.058, 0, 0.093, 0.033, 0.044]
URC-STTC-8PSK (4.4 dB)	[0.171, 0.093, 0, 0, 0.195, 0, 0, 0.099, 0.05, 0, 0.197, 0, 0, 0.025, 0.165]
URC-STTC-16PSK (7.0 dB)	[0.203, 0, 0.093, 0.102, 0, 0, 0.148, 0, 0, 0.055, 0.149, 0, 0, 0, 0.248]

TABLE VIII
SUBCODE WEIGHTING COEFFICIENTS OF THE IRCC ENCODER ASSOCIATED WITH URC-STTC-QPSK, URC-STTC-8PSK AND URC-STTC-16PSK.

Importantly, the value of the 'turbo-cliff' SNR given in Table VIII indicates that once the SNR value exceeds this value, the BER/FER of the coding scheme is expected to become

infinitesimally low. Indeed, the performance prediction provided by the EXIT-chart curves, which were created by using the procedure briefly summarised in Section V-A, is always satisfied by Monte Carlo simulation results. Accordingly, the BER of the system supported by the coding schemes, such as the IrCC-URC-STTC-QPSK, IrCC-URC-STTC-8PSK and IrCC-URC-STTC-16PSK arrangements, drops to a value below 10^{-6} , when the SNR value exceeds the corresponding turbo-cliff SNR.

D. EXIT chart analysis in relay selection

As mentioned above, EXIT charts can also be employed more widely than that demonstrated in Section V-B and Section V-C. A further application is that of optimising the BER/FER performance of the entire distributed coding scheme upon activating the appropriate relays at a favourable position or upon assigning the most appropriate transmit power to the relays for the sake of approaching the corresponding cooperative channel capacity. In what follow, we will exemplify the further employment of EXIT charts in the context of the distributed coding scheme featured in Fig. 25.

In order to allow the distributed coding scheme detailed in Fig. 25 to attain the best possible performance, a pair of appropriate relays should be utilised. Without any loss of generality, it can be assumed that a sufficiently high number of relays are roaming between the source and destination. For the sake of employing appropriate active relays, one can either choose two relays at an appropriate position or equivalently choose two relays at an arbitrary position, provided that accurately controlled transmit powers are used both at the S node and at the two R nodes. These two strategies have the same influence on the system, since they result in the same received power.

For illustrating the further application of EXIT chart analysis to the relay selection issues, let us consider the first strategy. Accordingly, There might be two approaches for choosing the activated ones from the set of available relays. The first approach of selecting the relays located at the halfway position is straightforward. By contrast, the second approach relies on a more sophisticated idea, namely on ensuring that the appropriately shaped EXIT tunnel of the system remains open:

- 1) On the first approach, the system should activate two arbitrary relays that are about half-way between the S node and the D node. This approach can be generalised by picking two arbitrary relays that are close to each other and they both have a similar distance from both the S node and D node.
- 2) The more sophisticated EXIT-chart based approach appoints the optimal relays, which are those that facilitate the creation of an open EXIT tunnel, as presented in Section VI-C1 and Section V-B1, leading to the (1,1) point at sufficiently high SNR_r values at both the R node and D node, provided that the SNR_t value is also sufficiently high. More specifically, the EXIT charts can be used for determining SNR values corresponding to the BER turbo-cliffs of the two respective coding arrangements, namely those of the IrCC-URC and the

IrCC-URC-STTC arrangements. Upon the difference a of those SNR values, the optimal relay-position conditions are established as follows [42]:

$$d_{sr} = \frac{d}{(1 + \sqrt{a})}, d_{rd} = \frac{d \times \sqrt{a}}{(1 + \sqrt{a})},$$

$$g_{sr} = (1 + \sqrt{a})^2, g_{rd} = \frac{(1 + \sqrt{a})^2}{a}. \quad (18)$$

For example, let us consider the numerical results pertaining to the coding scheme detailed in Fig. 25, where 8PSK is used for the source-relay transmission, while QPSK is employed for the transmission between the R nodes and D node. The URC, IrCC and STTC components have the code rates of $R_{URC} = 1.0$, $R_{IrCC} = 0.5$ and $R_{STTC} = 1.0$, respectively. Accordingly, one can find the value of $A = 10 \log_{10} a = 3.7$ dB by comparing the two SNR values representing the respective open EXIT tunnels, as given in Tab. IX. By substituting the values of A into Eq. (18), the optimal position of the relays given in Tab. X can be determined.

Coding Schemes	Convergent Point, SNR_r [dB]
IrCC-URC-STTC-QPSK	2.3
IrCC-URC-8PSK	6.0

TABLE IX
CONVERGENCE-SNRs EXTRACTED FROM EXIT CHARTS, NAMELY OF THE IrCC-URC-8PSK SCHEME LISTED IN TAB. VI AND OF THE IrCC-URC-STTC-QPSK SCHEME LISTED IN TAB. VIII. THESE EXIT CHARTS WERE OBTAINED IN A RAYLEIGH SMALL-SCALE FADING SCENARIO.

E. Relay Positioning and its Power Gain

In this section, we discuss the achievable BER versus E_b/N_0 performance in comparison to the associated attainable cooperative channel capacity based on the two different relay-selection approaches, in order to highlight the employment of the EXIT-chart aided design tool.

The cooperative channel capacity can be calculated by applying the general formulae given in [17] in the context of the specific example detailed in this paper. Accordingly, the components of the specific formula need to be estimated by exploiting the area property of the EXIT chart detailed in Section II-A2. Further details elaborating on the calculation of the cooperative channel capacity are presented in [45], [49].

Let us now consider the BER-performance of the distributed coding scheme relying on the IrCC-URC-STTC regime from different perspectives. Although perfect relaying is not required for the success of the coding scheme, benchmark results for the perfect-relaying scenario, where no errors are imposed by the source-relay link, are presented for showing the achievable upper bound performance. Note that the term ‘practical relay’ indicates that the quality of the source-to-relay transmission link reflects the performance of the channel coding scheme used. Accordingly, let us consider the four configurations of the system portrayed in Fig. 25. These configurations listed in Tab. XI are different in terms of the position and type of relays activated as well as in the

Distributed Coding Scheme		A (Convergence SNR Difference)	Optimal Position
Source-Relay	Relay-Destination		
IrCC-URC-QPSK	IrCC-URC-STTC-QPSK	0.5	$d_{sr} = 0.48d, d_{rd} = 0.52d$
IrCC-URC-8PSK	IrCC-URC-STTC-QPSK	3.7	$d_{sr} = 0.39d, d_{rd} = 0.61d$

TABLE X
OPTIMAL POSITIONS OF THE RELAYS.

Configuration	Position of relays	Type of relays	Scheme in use
1	Half way	Perfect	$S \rightarrow R$: IrCC-URC-8PSK $R \rightarrow D$: IrCC-URC-STTC-QPSK
2	Half way	Practical	$S \rightarrow R$: IrCC-URC-8PSK $R \rightarrow D$: IrCC-URC-STTC-QPSK
3	Optimal	Perfect	$S \rightarrow R$: IrCC-URC-8PSK $R \rightarrow D$: IrCC-URC-STTC-QPSK
4	Optimal	Practical	$S \rightarrow R$: IrCC-URC-8PSK $R \rightarrow D$: IrCC-URC-STTC-QPSK

TABLE XI
CONFIGURATIONS OF THE SYSTEM PRESENTED IN FIG. 25, CORRESPONDING TO DIFFERENT MODULATION SCHEMES EMPLOYED FOR TRANSMISSION FROM THE S NODE TO THE R NODES, AS WELL AS THE POSITION AND TYPE OF THE RELAYS IN USE.

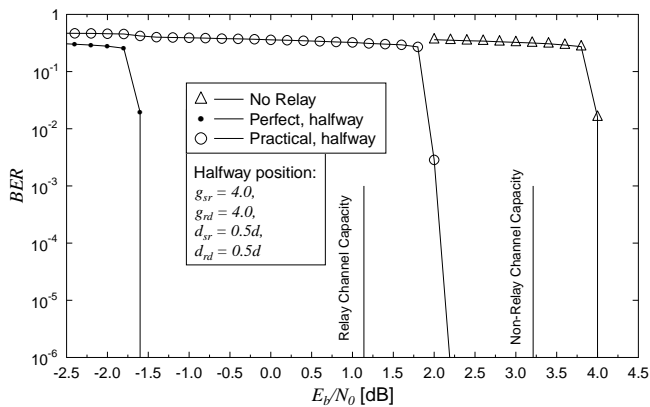


Fig. 28. BER-performance comparison of the distributed coding aided system of Fig. 25, when activating the R nodes located half-way between the S node and the D node, which corresponds to the configuration 1 and 2 listed in Tab. XI, where the 8PSK modulation scheme is employed for the transmission link spanning from the S node to the R nodes. A Rayleigh-distributed small-scale fading scenario is considered for all the transmissions in the system.

modulation scheme used for the source-to-relay transmission links.

The performance of the distributed coding scheme recorded in Fig. 28 and Fig. 29 for all the four configurations clearly confirms the fact that having a distributed structure has system performance benefits. More specifically, as shown in Fig. 28, when having access to relays at the half-way position, an E_b/N_0 improvement of 2.0 dB is achieved at a BER of 10^{-5} . The improvement becomes higher, for example the improvement of 4.0 dB at a BER of 10^{-5} seen in Fig. 29, when selecting the relays in the vicinity of the optimal position determined by the EXIT chart tool.

The performance gain of selecting relays at the optimum location, as opposed to stipulating the idealised simplifying assumption of having relays at the half-way location, will be higher when we have a higher value of A , which quantifies

the difference between the pair of convergence SNR_r values obtained by the EXIT chart analysis. In other words, EXIT chart analysis can be used for determining the proximity of the distributed coding scheme's performance to its optimal performance. The optimal performance can be achieved by adjusting the transmission rate of the coding components, by activating mobile relays that happen to be roaming in the vicinity of the optimal position or by accurately controlling the transmit power of both the source and of the relays nodes.

The performance of a practical relaying scheme, which may impose error-propagation owing to its decision-errors, was shown to be either about 0.2 dB or 3.6 dB from that of the idealised perfect relay scheme, which is due to the effects of error propagation imposed by the R nodes, as seen in Fig. 28. By definition, the optimal relay selection method aims for solving this problem by activating relays exactly at the optimal locations, so that the system may reach the $SNR_{r(relay)}$ and $SNR_{r(dest.)}$ values required for simultaneously achieving a low BER at both the R and D nodes. The optimal relay nodes in the scheme considered are located at normalised positions of $0.39d$ closer to the S node, in order to achieve $g_{sr} = 6.41$, $g_{rd} = 2.73$. The size of the performance gap between the practical and the idealised perfect relaying depends on how close the distributed coding scheme operates to its optimal configuration, which can be ascertained with the aid of EXIT chart tool.

The distributed coding scheme is capable of operating at a similar SNR-distance, for example 1.1 dB, from the relay realistic channel's capacity in case of both 'mid-way' and optimal relay positions. However, the channel capacity of these two scenarios is different due to the fact that the channel's capacity can be optimised by accurately tuning the distributed coding configuration to its optimum. Explicitly, this may be achieved by adjusting the coding rate of its coding components, by carefully activating relays roaming in the vicinity of the optimal position or by accurately controlling the transmit power of both the source and relays nodes.

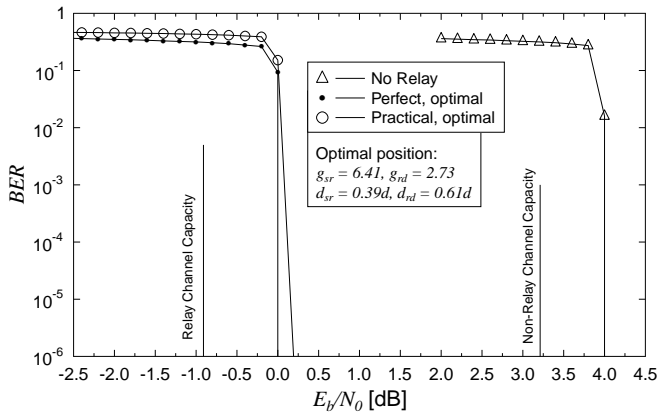


Fig. 29. BER-performance of the distributed coding aided system pictured in Fig. 25, when selecting R nodes nearby the optimal position determined by Eq. (18). The scenarios considered corresponds to the configuration 3 and 4 mentioned in Tab. XI, where the 8PSK modulation scheme is chosen for the transmission link spanning from the S node to the R nodes, provided that all the transmissions in the system are carried out over Rayleigh-distributed small-scale fading channels.

The relay channel's capacity detailed in [17], [42] also suggests that there should be a different optimal position, when the objective function is that of maximising the relay channel's capacity. However, satisfying the optimal condition of Eq. (18), which is found by the EXIT chart analysis, always provides the best possible performance for the coding scheme, which is hence also better than that of the position that was optimally chosen for maximising the relay channel's capacity. Explicitly, depending on the specific choice of the optimisation cost-function (CF), diverse optimum solutions may be found and the system designer has to opt for using that specific CF, which is the most pertinent one for a particular service.

It should be noted that since a near-capacity design is applied for the DC-IrCC-URC-STTC scheme, no further system performance improvement may be achieved upon utilising at the D node the signal transmitted from the S node.

VII. CONCLUSIONS, DESIGN GUIDELINES AND FUTURE RESEARCH

A. Summary and Conclusions

We have summarised the relevant EXIT-chart based design guidelines, which have been illustrated with the aid of various examples for diverse near-capacity wireless transceivers covering both the family of coherent and non-coherent based detection systems, MIMO systems and VMIMO systems. The IrCC-URC-MPSK, IrCC-URC-DMPSK, IrCC-URC-STTC-MPSK and distributed IrCC-URC-STTC-MPSK coding schemes of Section V-B, Section V-C and Section VI have been respectively used as illustrative examples for demonstrating the application of the EXIT chart design tool in facilitating near-capacity performance. In order to benchmark the near-capacity code design advocated, both the outage capacity and the OP of the schemes operating at the CCMC, at the DCMC as well as at the D-DCMC limits were presented. Specifically, the OP of the idealised at the DCMC and D-DCMC can be calculated by employing EXIT charts for determining the associated SNR_r ,

value corresponding to a given transmission rate R of the systems of interest.

Additional discussions on the issue as to whether the coherent or the non-coherent scheme should be employed have been presented by providing a comparison of non-coherent versus coherent systems, where the effects of channel estimation errors were also alluded to. Moreover, for the sake of clarifying the trade-off between the system's latency and performance, the employment of sub-frame based transmissions was discussed, which has indicated the substantial benefit of employing the sub-frame transmission regime of Section V-D, when transmitting over slow fading channels.

The benefits of the EXIT chart-aided design principles in distributed coding schemes have been illustrated with the aid of the DC-IrCC-URC-STTC coding scheme, in the context of a single-user single-antenna based cooperative relaying system. In Section VI-D, we also presented a further application of EXIT charts in forming an optimisation criterion for selecting the relays by maintaining an open EXIT chart tunnel for all the composite coding arrangements of the distributed coding scheme.

B. Design Guidelines

In summary, the design process of the Irregular Concatenated Coding Arrangements (ICCA) may be conducted in the following phases.

Phase 1 represents the specification of the basic design requirements, which includes the choices of the particular FEC scheme, the maximum code rate of the FEC scheme, the available modulation modes and their throughput, the tolerable complexity and latency, etc.

In phase 2, we need to quantify the capacity of the schemes stipulated in Phase 1, which are the outage capacity and the OP of the CCMC, of the DCMC as well as those of the D-DCMC. The OP of the DCMC and D-DCMC may be calculated based on the associated SNR_r value corresponding to a given transmission rate R and modulation scheme. Accordingly, the SNR_r value may be determined by looking up the corresponding value on the capacity curves or by employing EXIT charts. The employment of EXIT charts used for formulating the capacity curve may be described in the following steps:

- EXIT curves pertaining to a given modulation scheme are generated for different SNR_r values.
- A single point on the capacity curves is determined by computing the area under the EXIT curve and its corresponding SNR_r .

Phase 3 is dedicated for conducting the near-capacity design according to the scenario provided by the design requirement. The typical three component concatenated coding arrangement relying on IrCCs may be designed by carrying out the following steps:

- Optimise the inner-most two-stage coding arrangement by finding the most appropriate number of iterations associated with the affordable complexity.
- Create the EXIT curve of the amalgamated optimised inner decoder for different SNR_r values.

- Use the coding rate of the IrCC encoder specified by the design requirement and then employ the EXIT curve matching algorithm for generating the optimised weighting coefficients α_i , where the number of IrCC subcodes is stipulated by the tolerable complexity of the design requirement.

C. Future Research

Future research may consider applying both the design principles as well as the resultant schemes in the context of cooperative communications. More particularly, it was suggested [163]–[165] that equalisers, namely Least Mean Square (LMS) equalisers or trellis based equalisers, can be incorporated into a cooperative communication system to exploit the joint advantages of having both relays and equalisers in dispersive scenarios. Once appropriate equalisers have been found for cooperative communication systems, we can integrate them with our existing coding schemes designed in Section V. Furthermore, we may employ these solutions in next-generation multi-user systems. Additionally, building upon the initial research on combining channel coding and network coding [166]–[168], cognitive radio schemes [169], [170] may be integrated into the system of [168] at the link level, where the knowledge of channel state information may be utilised for introducing adaptive channel coding and modulation into our system.

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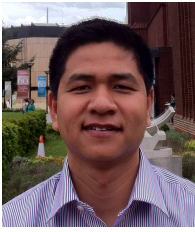
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LIST of ACRONYMS and SYMBOLS	
16PSK	16 level Phase Shift Keying
4PSK	4-level Phase Shift Keying
8PSK	8 level Phase Shift Keying
BICM-ID	Bit-Interleaved Coded Modulation with Iterative Decoding
BPS	Bit Per Symbol
BPSK	Binary Phase-Shift Keying
CCMC	Continuous-input Continuous-output Memoryless Channel
CDD	Conventional Differential Detection
CSI	Channel State Information
DC-IrCC-URC-STTC	Distributed Concatenated Irregular Convolutional Code, Unity-Rate Code and Space-Time Trellis Code
DCMC	Discrete-input Continuous-output Memoryless Channel
D-DCMC	Differential Discrete-input Continuous-output Memoryless Channel
DMPSK	Differential M-ary Phase Shift Keying
EXIT	EXtrinsic Information Transfer
FEC	Forward Error Control
FER	Frame Error Ratio
ICCA	Irregular Concatenated Coding Arrangements
IIR	Infinite Impulse Response
IrCCs	Irregular Convolutional Codes
IrCC-URC-DMPSK	Irregular Convolutional Coded Unity Rate Coded Differential M-ary Phase Shift Keying
IrCC-URC-MPSK	Irregular Convolutional Coded Unity Rate Coded M-ary Phase Shift Keying
IrCC-URC-STTC-MPSK	Irregular Convolutional Coded Unity Rate Coded Space Time Trellis Coded M-ary Phase Shift Keying
LMS	Least Mean Square
LTE	Long Term Evolution
LLR	Loglikelihood Ratio
MAP	Maximum A-Posteriori
MIMO	Multiple Input Multiple Output
ML	Maximum Likelihood
MSDD	Multiple-Symbol Differential Detection
MSDSD	Multiple-Symbol Differential Sphere Detection
OP	Outage Probability
PCC	Parallel Concatenated Convolutional
PDF	Probability Density Function
QPSK	Quadrature Phase-Shift Keying
RSC	Recursive Systematic Convolutional
ScC	Self-concatenated Convolutional
SCC	Serial Concatenated Convolutional
SISO	Single Input Single Output
STBCs	Space Time Block Codes
STTC	Space Time Trellis Coding
STTCs	Space Time Trellis Codes
TCM	Trellis Coded Modulation
TCs	Turbo Codes
URC	Unity Rate Codes
I_A	<i>A priori</i> mutual information
I_A^{in}	I_A at the inner component
I_A^{out}	I_A at the outer component
I_E	Extrinsic mutual information
I_E^{in}	I_E at the inner component
I_E^{out}	I_E at the outer component
L_a	A group of <i>a priori</i> LLRs
L_e	A group of extrinsic LLRs
ϕ	Number of subcodes in IrCC
α_ϕ	Weighting coefficient of subcode ϕ
β_ϕ	Coding rate of subcode ϕ
N_t	Number of transmit antenna
N_w	Window size
h_s	Slow fading coefficient
h_f	Fast fading coefficient
η	Modulated bits per symbol
R	Data transmission rate
R_n	Normalised throughput
$SNR_r _R$	Signal to noise ratio at the receiver, given R
$SNR_r^{EXIT} _R$	$SNR_r _R$ calculated by the EXIT based method
ϵ	Outage probability
I	Number of inner iterations
J	Number of outer iterations
T_u	SNR value corresponding to turbo cliff
D_c	Distance to the respective capacity
N_{sub}	Number of sub-frames
θ	Normalised channel estimation accuracy
d_{sr}	Distance form source to relay
g_{sr}	Power gain of the source-to-relay link
d_{rd}	Distance form relay to destination
g_{rd}	Power gain of the relay-to-destination link

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