Constructive and Destructive Interplay between Piezoelectricity and Flexoelectricity in Flexural Sensors and Actuators

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Flexoelectricity is an electromechanical effect coupling polarization to strain gradients. It fundamentally differs from piezoelectricity because of its size-dependence and symmetry. Flexoelectricity is generally perceived as a small effect noticeable only at the nanoscale. Since ferroelectric ceramics have a particularly high flexoelectric coefficient, however, it may play a significant role as piezoelectric transducers shrink to the sub-micrometer scale. We examine this issue with a continuum model self-consistently treating piezo- and flexoelectricity. We show that in piezoelectric device configurations that induce strain gradients and at small but technologically relevant scales, the electromechanical coupling may be dominated by flexoelectricity. More importantly, depending on the device design flexoelectricity may enhance or reduce the effective piezoelectric effect. Focusing on bimorph configurations, we show that configurations that are equivalent at large scales exhibit dramatically different behavior for thicknesses below 100 nm for typical piezoelectric materials. Our results suggest flexoelectric-aware designs for small-scale piezoelectric bimorph transducers.

1 Introduction

Electromechanical coupling mechanisms in materials allow us to sense, actuate, and generally transform mechanical energy into electrical energy and vice versa. Piezoelectricity is one such mechanism, by which electric charges accumulate in response to strain. Another related mechanism is flexoelectricity, which refers to a two-way coupling between electric polarization and *strain gradients*, rather than strain as in piezoelectricity, or between polarization gradients and strain [1–3]. Because piezoelectricity is scale invariant but flexoelectricity is not, the ratio between flexo- and piezoelectric coefficients defines a length-scale of strain gradient relaxation, below which flexoelectricity is a stronger effect [4, 5]. This lengthscale ranges between 10s of nanometers to a micron for common piezoelectrics. As a result, flexoelectricity may be a more efficient mechanism for sensing [6, 7] or energy harvesting [8–10] at small scales. Being in principle a universal property for all dielectric materials, flexoelectricity may broaden the class of materials for electromechanical transduction [11, 12], including soft materials [13, 14]. Flexoelectricity may enable electromechanical transduction at high temperatures, where ferroelectric perovskites are in the paraelectric phase but exhibit large flexoelectric coefficients [3, 15]. Furthermore, flexoelectric transduction is devoid of aging due to depoling.

Flexoelectricity is commonly neglected in designing or analyzing electromechanical transducers. Yet, piezoelectric thin-film devices are reaching thicknesses of 10s to 100s nm, using either PZT and AlN ceramics [16, 17] or PVDF polymers [18], which suggests that flexoelectric effects may become significant. Furthermore, since piezo- and flexoelectricity are fundamentally different in terms of symmetry, it is not clear under which circumstances these two effects can cancel each other or act in concert. Here, we examine the interplay between piezo- and flexoelectricity and the resulting electromechanical performance in flexural piezoelectric transducers using numerical computations based on a selfconsistent continuum theory accounting for these two effects [4,5]. We focus on bimorph cantilever beams, which are among the most common configurations for piezoelectric transduction [19, 20]. Applications of bimorphs include ultrasonic motors, laser beam deflectors, fans for heat management in microelectronics, numeric displays, filters, accelerometers, optical choppers, legs of microrobots, and energy harvesting, to mention a few [19, 21, 22]. We consider four common designs of bimorphs, and examine their performance as actuators and sensors as a function of structural size.

2 Computational Model

We model the electromechanical response of bimorphs using a linear theory of piezoelectricity with poling [23], augmented with flexoelectricity [24]. We summarize next the theory of this model previously presented in Refs. [4,5]. The electrical enthalpy density of a linear dielectric solid possessing piezoelectricity and flexoelectricity can be written as

$$\mathcal{H}(\mathbf{\varepsilon}_{ij}, E_i, \mathbf{\varepsilon}_{jk,l}) = \frac{1}{2} \mathbf{C}_{ijkl} \mathbf{\varepsilon}_{ij} \mathbf{\varepsilon}_{kl} - e_{ikl} E_i \mathbf{\varepsilon}_{kl}$$
(1)
$$-\mu_{ijkl} E_i \mathbf{\varepsilon}_{jk,l} - \frac{1}{2} k_{ij} E_i E_j,$$

where **E** is the electric field, defined as $\mathbf{E} = -\nabla \phi$, ϕ being the electric potential. The first term is the elastic potential, where C is the fourth-order tensor of elastic moduli. The piezoelectric coupling between strain and electric field is through the second term with the third-order tensor of piezoelectricity e. The last term is the electrostatic potential, where k is the second-order dielectric tensor. The flexoelectric coupling between the gradient of strain $\nabla \varepsilon$ and the electric field is through the third term, where the flexoelectric tensor μ represents the combination of direct and converse flexoelectric effects [12]. In this formulation, the remanent state of the piezoelectric material has been taken as the reference configuration, and the poling of the piezoelectric material is implicitly encoded in the constitutive equations through the piezoelectric tensor e [23]. In the absence of surface charges, the total electromechanical enthalpy is

$$H = \int_{\Omega} \mathcal{H} d\Omega - \int_{\Gamma_t} \bar{t}_i u_i \, dS, \qquad (2)$$

where $\mathbf{\bar{t}}$ are the mechanical tractions applied on the boundary. By making this enthalpy stationary with respect to the displacement and electric potential fields, the self-consistent governing equations in weak form are obtained for the electro-mechanical boundary value problem [4]. Numerically, we deal with the fourth-order nature of the partial differential equations by approximating displacements and electric potential using a meshfree method with smooth basis functions [25]. Unlike our 3D study of flexoelectric effects in pyramids [5], here we restrict out attention to 2D plane strain conditions for conceptual clarity. The strain gradient elasticity (SGE) term, which guarantees the thermodynamic stability of the system at small scales [26], is not included in our calculations because its effect is very small for flexoelectric multilayer structures of technologically relevant scales [27]. However, while the SGE term has been shown to be insignificant in some situations, it is possible that this term is important in other cases. We checked that its effect was negligible in the simulations reported below. We also note that, while we focus here on bulk flexoelectricity, it has been argued that its phenomenology can be the result of surface piezoelectricity. In this interpretation, surface relaxation induces a local symmetry loss, creating an effectively piezoelectric superficial layer. Its size-dependent effect is



Fig. 1. Piezoelectric bimorph cantilever beams consist of two identical piezoelectric layers (a) series arrangement and (b) parallel arrangement. The beams are mechanically fixed at the left-end and the mechanical point load F is applied at the right-end. In the series bimorph, the electric potential is fixed to zero at the top face while it is fixed to zero at the top and bottom faces of the parallel bimorph. An active electrode is placed at the bottom of the series bimorph and at the layers interface in the parallel bimorph. This active electrode may either fix the electric potential to a constant value (V in series and V/2 in parallel) or undergo a difference of electric potential as a result of mechanical deformation. The blue and red arrows indicate the directions of polarization (P) and electric field (E), respectively. The polarized layers in the series bimorph can be either head-tohead (HH) or tail-to-tail (TT) while they can be polarized downward (negative, P-) or upward (positive, P+) in the parallel bimorph.

negligible at macroscopic scales, but can be as significant as bulk flexoelectricity at small scales and has the same symmetry [28, 29]. Thus, from a practical viewpoint, surface piezoelectricity and flexoelectricity play the same role.

Piezoelectric bimorphs consist of two identical and perfectly bonded piezoelectric layers, with an electrode configuration such that when an electric field is applied, one layer elongates and the other contracts. This results in a bending deformation of the composite structure. Figure 1 shows the geometry and typical bimorph configurations. Two arrangements are commonly considered. The first type of bimorph shown in Fig. 1(a) is often called series bimorph or antiparallel bimorph. In this arrangement, piezoelectric layers are poled in opposite direction, either head-to-head (HH) or tail-to-tail (TT). The electric potential is applied between the bottom and top faces, generating the same nominal electric field in both layers. The displacement and the electric field are continuous across the interface between the layers in the series device. The second arrangement is known as parallel piezoelectric bimorph and has an intermediate electrode at the interface between the two piezoelectric layers, as depicted in Fig. 1(b). In this case, both layers are poled in the same direction. The polarization can be either downward (negative) or upward (positive). However, the arrangement



Fig. 2. Normalized vertical displacement as a function of the normalized beam thickness for the series bimorph arrangements: tail-to-tail (TT) and head-to-head (HH) polarized layers. The results are obtained for the piezoelectric bimorphs with and without flexoelectricity. The insets show the distribution of electric field in both arrangements for different beam thicknesses.

of electrodes results in opposite electric fields in the layers. Therefore, the electric field is discontinuous across the interface in the parallel device.

The aspect ratio of the piezoelectric layers is fixed to L/h = 10 unless otherwise stated, where L and h are the length and height of the layers. The bimorphs are mechanically constrained at the left-end, and a point force F is applied at the right-end. For the series bimorph in Fig. 1(a), the top electrode is connected to ground and the bottom electrode is active. For the parallel bimorph in Fig. 1(b), the top and bottom electrodes are connected to ground and the intermediate electrode is active. The active electrode can either prescribe a voltage difference (V in series and V/2 in parallel), or experience a change of electric potential as a result of deformation. In the latter case, we constrain the electric potential to be constant at the active surface, and find its value as a result of the numerical calculation using Lagrange multipliers. The material parameters are chosen to fit the behavior of PZT-5H [30], a common piezoelectric material for bimorphs. We consider both the longitudinal and transversal flexoelectric coefficients μ_{11} and μ_{12} . The magnitude of these coefficients is chosen as $\mu = \chi f$, where f is the flexocoupling coefficient and χ is the dielectric susceptibility of PZT. The value of f has been estimated to be of the order of 1 - 10Vfor simple ionic solids [3]. Here, we choose f = 10V.

3 Bimorph Actuator

The bimorph structures shown in Fig. 1 exhibit bending deformation upon application of a voltage difference at the electrodes. Using our computational model, we evaluate the actuation vertical displacement of the cantilever tip for different bimorph arrangements. To apply the electrical load in the simulations, we set V = -12.8h (MV/m), where *h* is the thickness of a single piezoelectric layer. Figure 2 shows the normalized vertical displacement u_2/L as a function of the normalized beam thickness h/h_0 for the series bimorph arrangement. The normalization parameter h_0 is given by $h_0 = \mu/e_{33}$, representing a length-scale emanating from the balance between piezo- and flexoelectricity.

For reference, we show the results of a model accounting for piezoelectricity but not for flexoelectricity. As expected, the response is independent of the size of the beam, and the sign of the displacement changes with polarization reversal (e.g. from head-to-head to tail-to-tail). By accounting for flexoelectricity, however, the actuation response of the beam becomes size-dependent and sensitive to the polarization arrangement of the device. The actuation is considerably enhanced in the head-to-head design, converging to the purely flexoelectric response at the small-scale limit. To investigate the source of this actuation, the distribution of the electric field is shown as insets in Fig. 2 for different beam thicknesses. This distribution is nearly uniform across the thickness for large systems, where the response is dominated by piezoelectricity, see Fig. 2(a). However, by decreasing the bimorph size, the electric field becomes non-uniform across the thickness with considerable gradients near the top and bottom electrodes, c.f. Fig. 2(b) and (c). These gradients, with opposing sign in each of the layers, generate high stresses and an actuation mechanical moment because of converse flexoelectricity, as discussed in detail in Ref. [4]. The flexoelectrically-induced moment always contracts the positive electrode, irrespective of the polarization orientation. In contrast, the mechanical moment induced by piezo-



Fig. 3. Normalized vertical displacement as a function of the normalized beam thickness for the parallel bimorph arrangements: negatively (P-) and positively (P+) polarized layers. The results are obtained for the piezoelectric bimorphs with and without flexoelectricity. The insets show the distribution of electric field in both arrangements for different beam thicknesses.

electricity changes sign with polarization reversal. In the head-to-head design, the piezo- and flexoelectric moments are in the same direction, i.e. the interplay between piezoand flexoelectricity is constructive, leading to an enhancement in the actuation response. In contrast, in the tail-to-tail design the piezoelectric moment counteracts the flexoelectric moment (Fig. 2(d)), diminishing the actuation response. For intermediate sizes where piezo- and flexoelectricity are comparable effects, the actuation response vanishes due to the destructive interplay between these two effects. This point is marked with the green dashed line in Fig. 2, and corresponds to about 50 nm for PZT. By further decreasing the beam size, the flexoelectric response becomes dominant, converging to the purely enhanced flexoelectric response at the small-scale limit.

Turning to the parallel bimorph arrangement, Fig. 3 shows a relatively small effect of flexoelectricity on the actuation response. Since the arrangement of electrodes in this configuration results in opposite electric fields (see Fig. 1b), opposite flexoelectric moments are induced in the top and bottom layers. Although these moments increase in magnitude by decreasing the beam thickness, they cancel each other. The small deviation from the purely piezoelectric response at small scales is due to the non-uniformity of the electric field induced by flexoelectricity, see the insets in Fig. 3.

4 Bimorph Sensor

Next, we perform simulations of bimorph beams under a mechanical point load F, see Fig. 1, which we set at F = 20h (MN/m). Then, we obtain the induced voltage V as the electrical response to the mechanical load. Figure 4 shows the normalized voltage $200Vh_0/h$ as a function of the normalized beam thickness h/h_0 , considering the series bimorph arrangement. As expected, the electrical response in not sensitive to the beam thickness in the absence of flexo-

electricity and it changes sign by reversing the polarization direction. However, an interesting size-dependent behavior is observed when flexoelectricity is accounted for. Similar to the bimorph actuators, the flexoelectric effect leads to an enhancement of the response in the head-to-head design as structural size progressively diminishes. As shown in Fig. 4(a), bending due to the mechanical load induces tensile and compressive strain fields, which result in a significant strain gradient. In turn, because of the direct flexoelectric effect, the strain gradient induces an electrical charge captured by the active electrode. Therefore, the interplay between piezoelectricity and flexoelectricity is constructive in this sensor arrangement at intermediate scales. However, this moderate enhancement disappears below a critical thickness. The origin of this opposing effect of flexo- and piezoelectricity with regards to sensing at small scales is the converse flexoelectric effect. As discussed earlier, this effect generates a mechanical moment due to the non-uniform distribution of the electric field across the beam thickness. The direction of the flexoelectric moment is clockwise in the head-tohead bimorph sensor, opposing the moment induced by the point load, see Fig. 4(a). This effect makes the beam stiffer against the applied load as the beam thickness decreases [4], progressively reducing the strain gradients and the induced flexoelectric charges. This point is clear in Fig. 4(c), where a significantly smaller strain field is induced at small-scales. Thus, there is a constructive interplay between piezo- and flexoelectricity at intermediate scales, coexisting with a destructive effect of converse flexoelectricity at small scales in the head-to-head sensor configuration.

Similar to its actuation response, the tail-to-tail design shows a destructive interplay between piezo- and flexoelectricity with regards to sensing; the induced voltage magnitude decreases with decreasing beam thickness. The sensing ability of the device is completely lost at a thickness close to 50 nm for PZT. Below this thickness, the flexoelectric effect becomes dominant, changing the sign of the induced volt-



Fig. 4. Normalized voltage as a function of the normalized beam thickness for the series bimorph arrangements: tail-to-tail (TT) and headto-head (HH) polarized layers. The results are obtained for the piezoelectric bimorphs with and without flexoelectricity. The insets show the distribution of axial strain ε_{11} in both arrangements for different beam thicknesses. The circular arrows show the mechanical moments induced by converse flexoelectricity.

age. In the negative voltage range (negative electric field), the moments induced by the point load and the converse flexoelectric effect are in the same direction (anti-clockwise, see Fig. 4(b)), leading to larger strain gradients and a sharper change of the voltage with respect to the head-to-head design. However, turning to the positive voltage range (below 50 nm), the flexoelectric moment acts against the mechanical moment and the response of the device approaches that of the head-to-head design.

Figure 5 shows the behavior of parallel bimorph configurations as a function of size. A destructive interplay between piezo- and flexoelectricity is apparent, leading to vanishing sensing ability at the small-scale limit. The reason for this effect is that flexoelectricity induces electric fields in the same direction (bending direction) in the top and bottom layers, while piezoelectricity generates electric fields of opposite directions in the parallel configuration. Therefore, the flexoelectric field always acts against the piezoelectric field in one of the top or bottom layers of this design.

5 Conclusions

The fundamental distinguishing features of flexoelectricity as compared to piezoelectricity are size-dependence and a different symmetry. We have shown that these features significantly affect the performance of flexural piezoelectric sensors and actuators (bimorphs) when they are shrunk to the sub-micron scale [16–18]. We have considered two series and two parallel bimorph configurations that exhibit essentially the same behavior in the absence of flexoelectricity (at large structural sizes). While parallel bimorphs are



Fig. 5. Normalized voltage as a function of the normalized beam thickness for the parallel bimorph arrangements: negatively (P-) and positively (P+) polarized layers. The results are obtained for the piezoelectric bimorphs with and without flexoelectricity.

quite insensitive to structural size with regards to actuation, their performance as sensors significantly degrades because of flexoelectric effects at the nanoscale. In series bimorphs in head-to-head configuration, piezo- and flexoelectricity act in concert enhancing actuation as structural size decreased. For sensing, however, this enhancement only occurs at intermediate sizes. Tail-to-tail bimorph configurations should be avoided in general because of the destructive interplay between piezo- and flexoelectricity. From a broader perspective, our results suggest that flexoelectric-aware designs can significantly enhance the performance of sub-micron piezoelectric transducers, whereas ignoring flexoelectricity can result in degraded performance. In addition to bimorph beams, our results could be extended to atomically thin sheets which exhibit anomalous piezoelectricity due to flexoelectric effects [31].

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