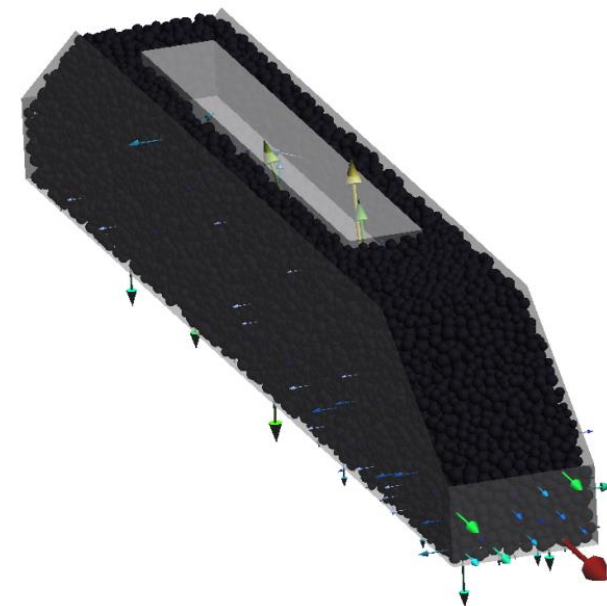
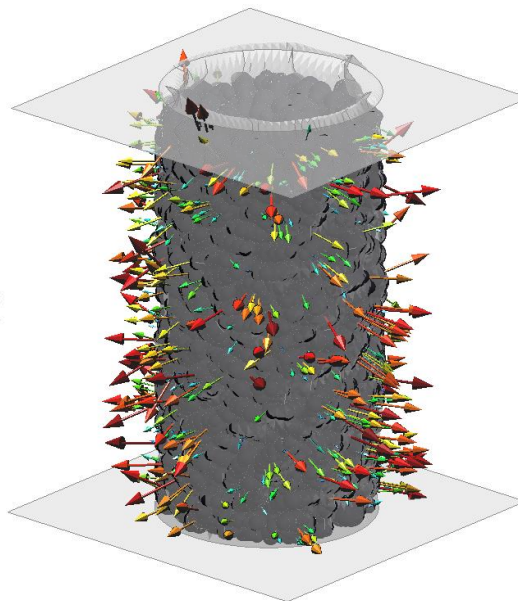
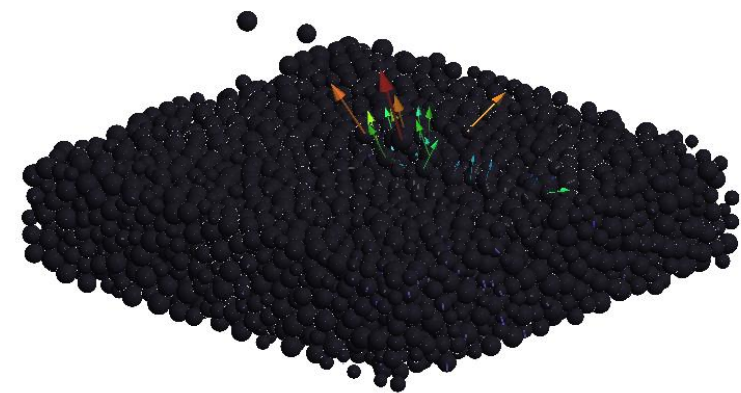


# Numerical modelling of railway ballast behaviour using the Discrete Element Method (DEM) and spherical particles



# OUTLINE

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- **Motivation and objectives**
- **Railway Ballast**
- **Discrete Element Method (DEM)**
- **Software**
- **Ballast representation with spheric particles**
- **Laboratory tests**
- **Different particles shape**
- **Conclusions**

# MOTIVATION AND OBJECTIVES

## Motivation:

- Increasing interest all over the world in high-speed trains

## Objectives:

- Study railway ballast properties
- Develop a numerical tool to reproduce quantitatively the macro-mechanical behaviour of railway ballast using the DEM
- Validate the code

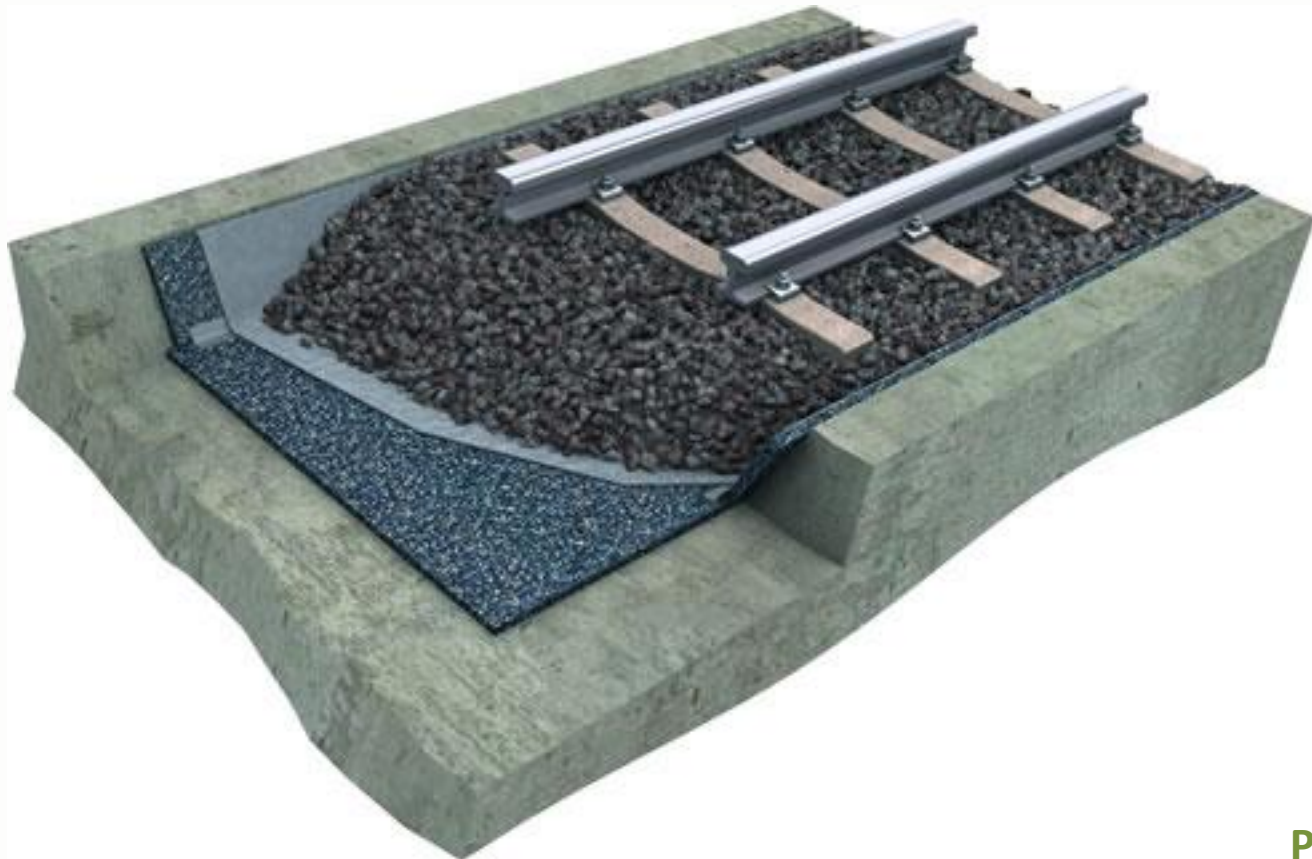
**BALAMED**

January 2013 – December 2015



# RAILWAY BALLAST

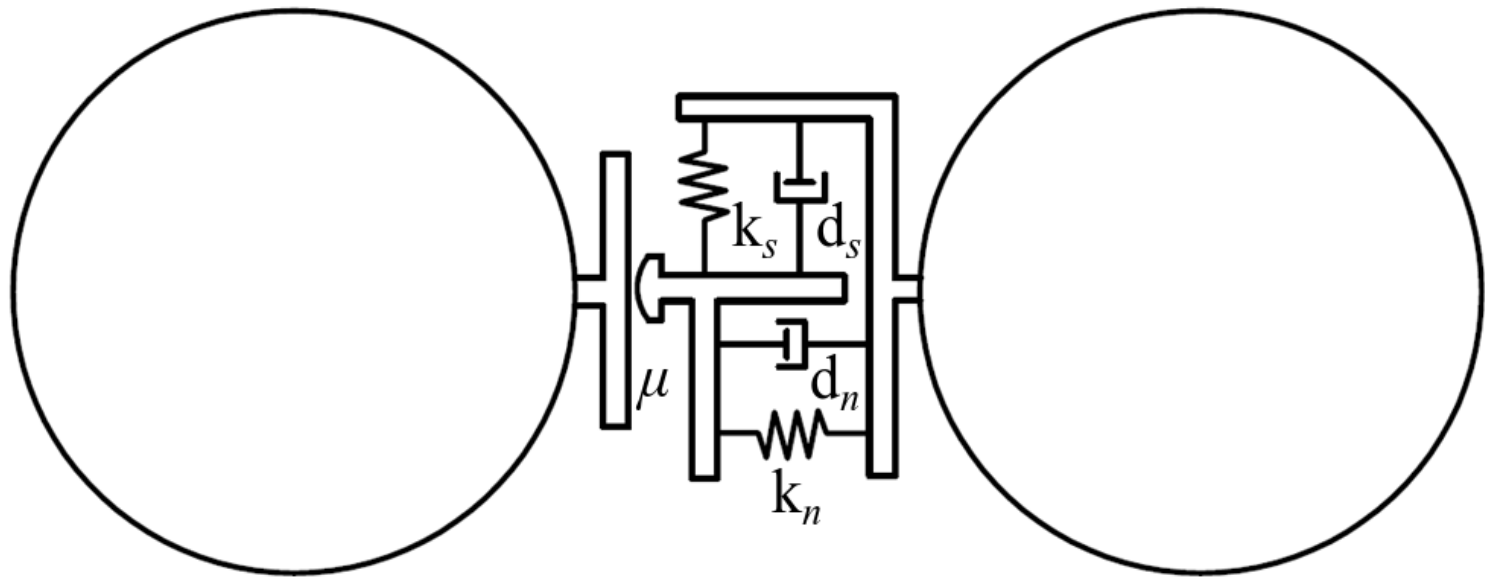
Layer of granular material placed under the sleepers whose roles are: resisting to vertical and horizontal loads and facing climate action



# DISCRETE ELEMENT METHOD

## Contact constitutive model:

Rigid bodies, deformation concentrated in contact points



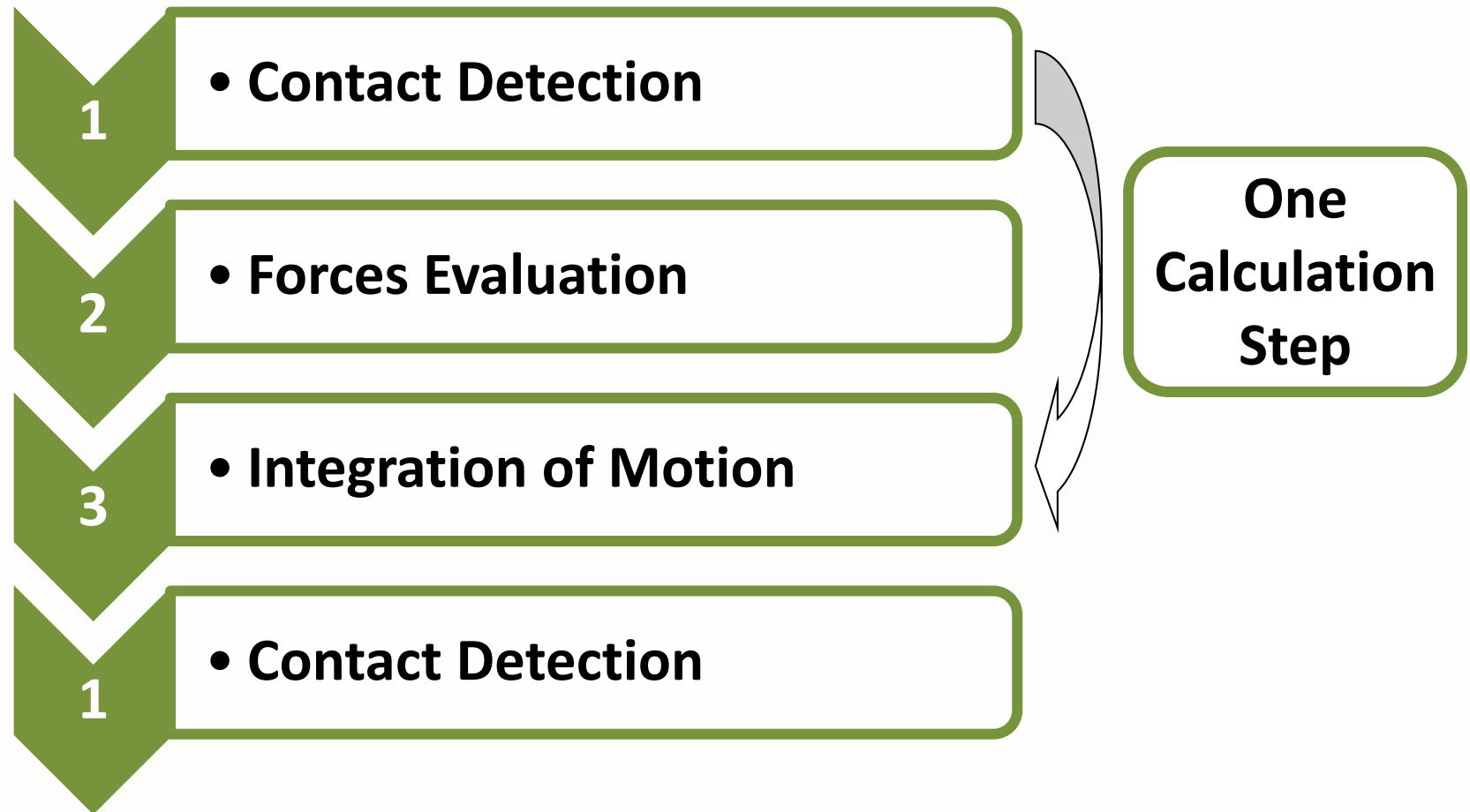
$$\begin{cases} m \cdot \ddot{u} = F \\ I \cdot \dot{\omega} = M \end{cases}$$

$$F = \sum_{c=1}^{N_c} F^c + F^{ext} + F^{damp}$$

$$M = \sum_{c=1}^{N_c} (r^c \times F^c + q^c) + M^{ext} + M^{damp}$$

# DISCRETE ELEMENT METHOD

## Algorithm:



# SOFTWARE



**KRATOS**  
MULTI-PHYSICS



<http://www.cimne.com/dempack/>

<http://www.cimne.com/kratos/>

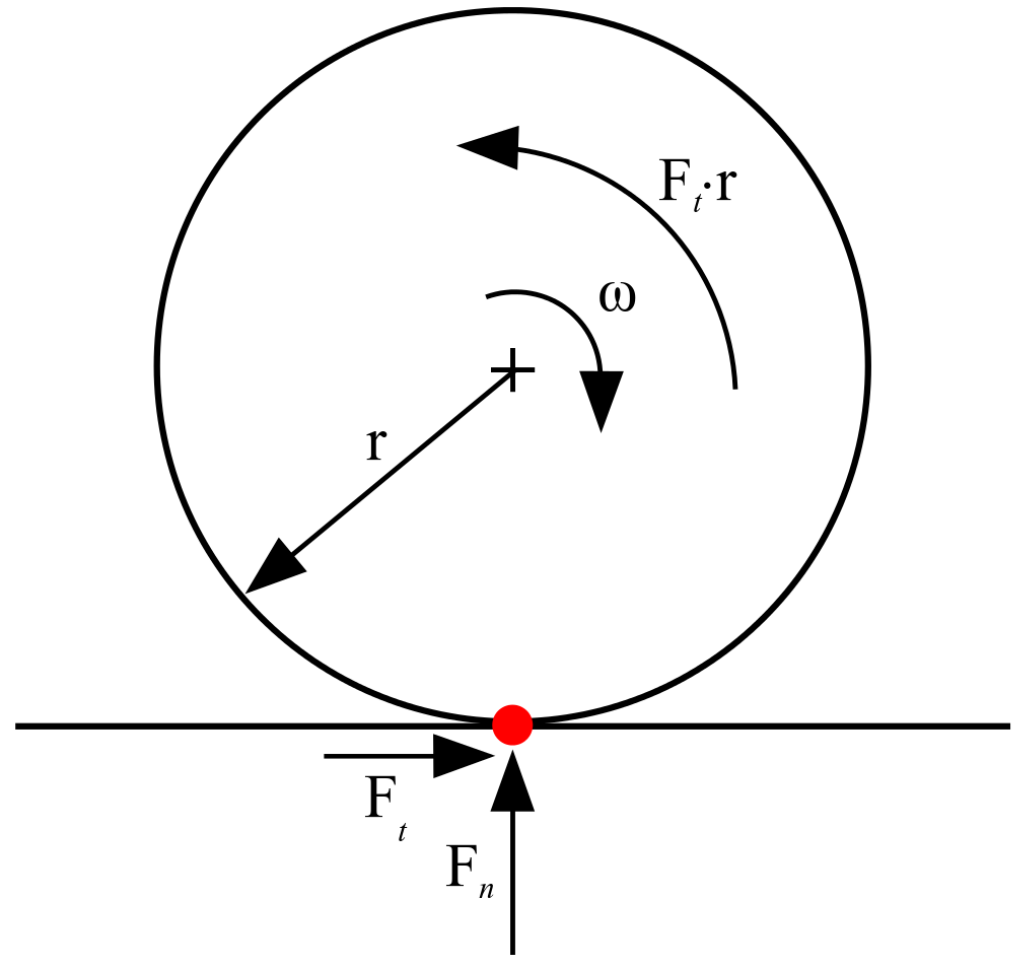
<http://gid.cimne.upc.es/>

# BALLAST REPRESENTATION WITH SPHERES

## Rolling friction:

Geometrical “property”  
that consists in  
imposing a virtual  
moment opposite to  
particle rotation and  
dependent on its size

C. M. Wensrich and A. Katterfeld.  
Rolling friction as a technique for  
modelling particle shape in DEM.  
Powder Technology, 217:409–417,  
February 2012



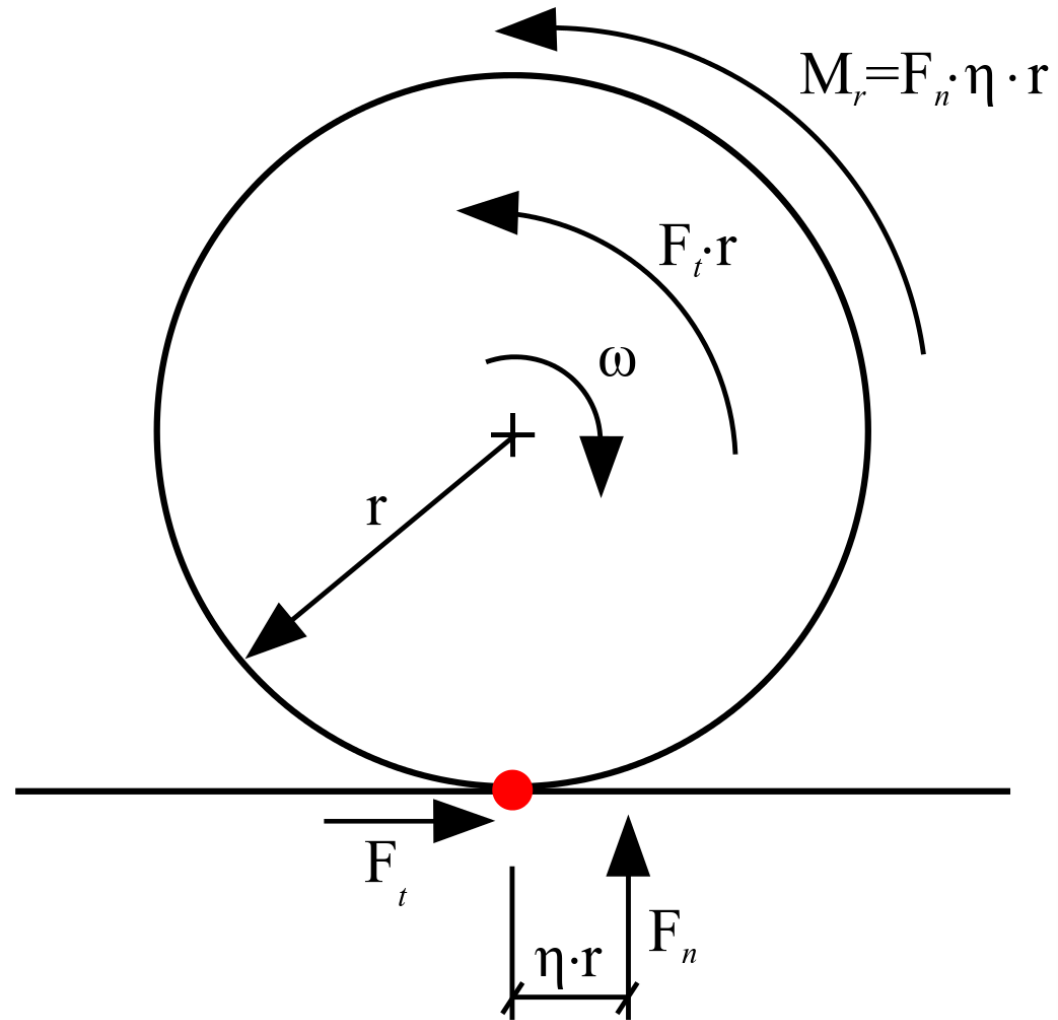


# BALLAST REPRESENTATION WITH SPHERES

## Rolling friction:

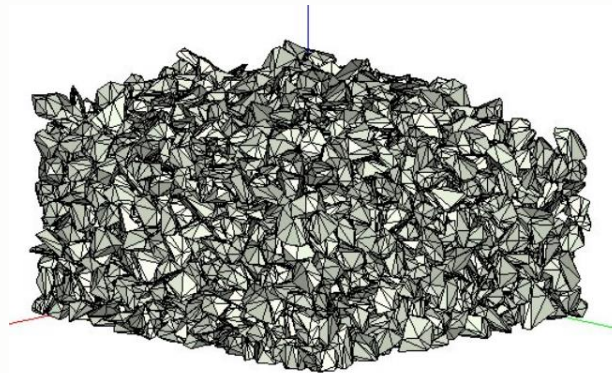
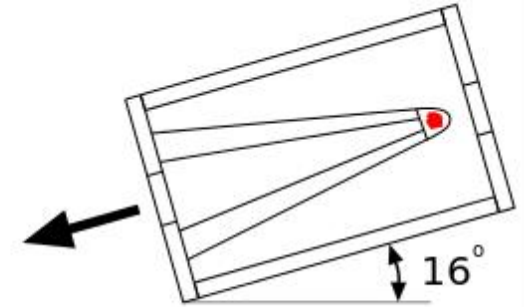
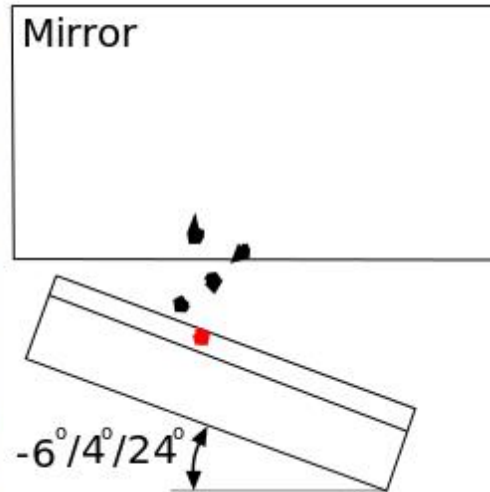
Geometrical “property”  
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dependent on its size

C. M. Wensrich and A. Katterfeld.  
Rolling friction as a technique for  
modelling particle shape in DEM.  
*Powder Technology*, 217:409–417,  
February 2012



# TEST RESULTS

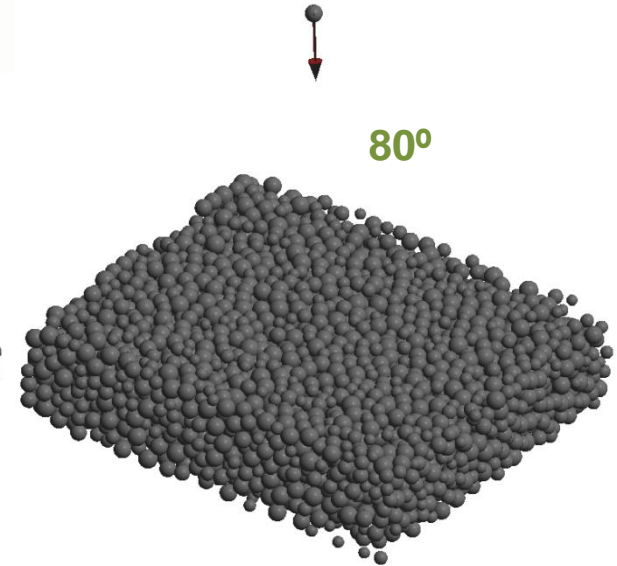
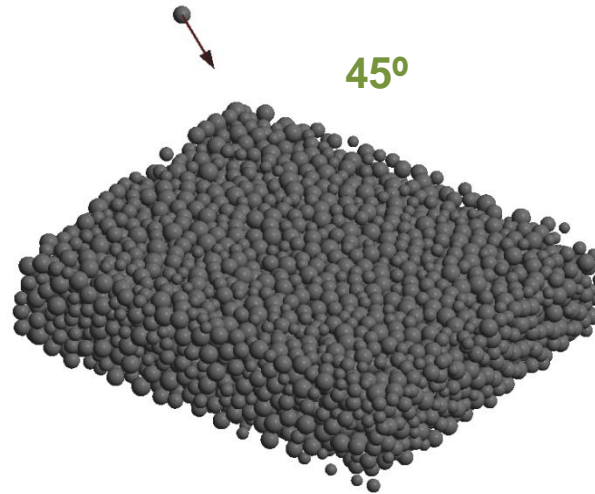
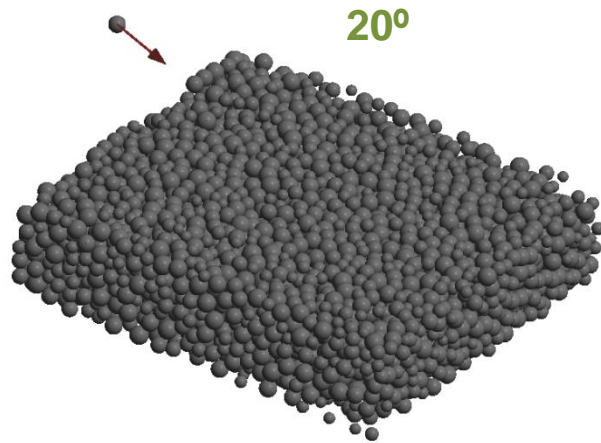
## Ballast stones projection:



Kaltenbach, H.J. et al. T. Assessment of the aerodynamic loads on the trackbed causing ballast projection: results from the DEUFRAKO project aerodynamics in open air (AOA). Seoul, 2008.

# TEST RESULTS

## Ballast stones projection:



### Ballast properties

Density (kg/m <sup>3</sup> )	2700	Friction coeff.	0.6
Young Modulus (Pa)	1.2e8	Restitution coeff.	0.4
Poisson ratio	0.18	Rolling friction coeff.	0.33
Mean diameter (m)	0.05		

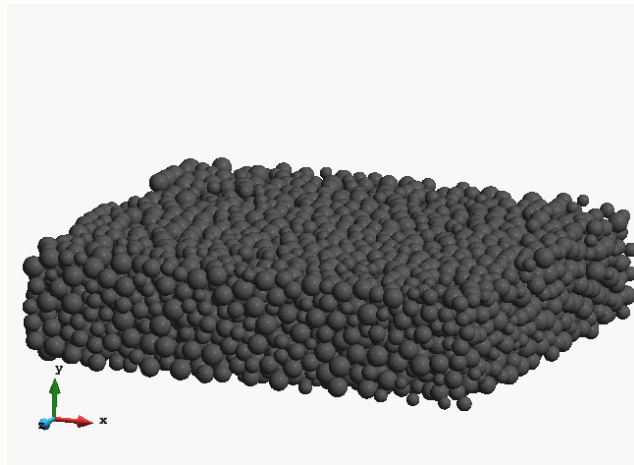
### Input parameters

Projected stone radius (m)	0.05
----------------------------	------

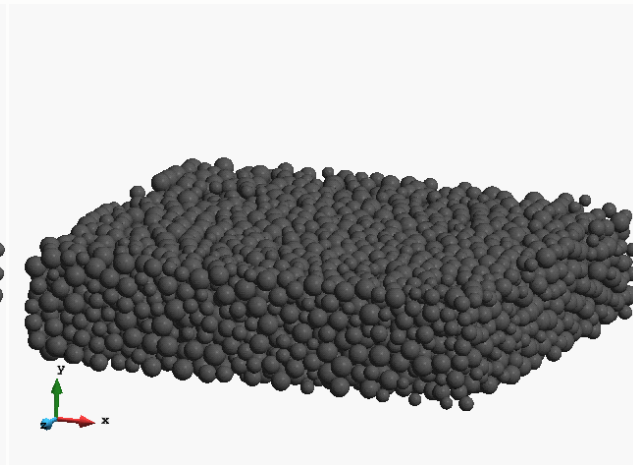
# TEST RESULTS

## Ballast stones projection:

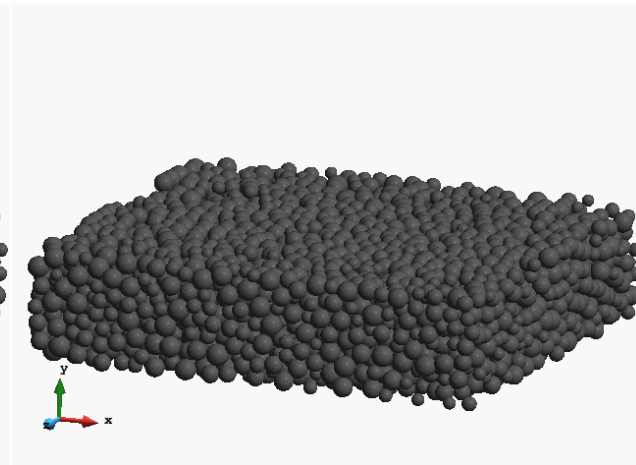
1000 J



20°



45°

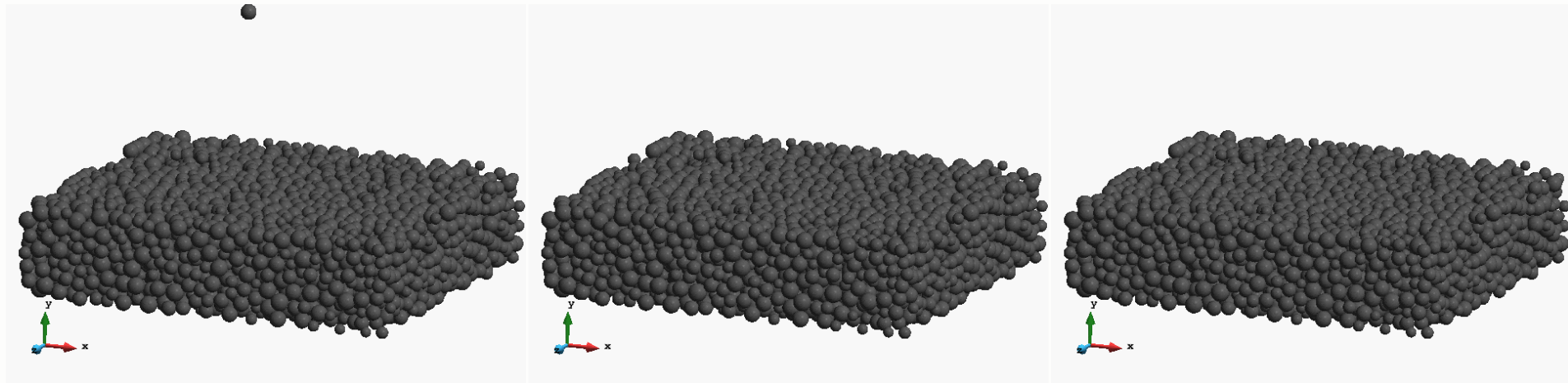


80°

# TEST RESULTS

## Ballast stones projection:

80°



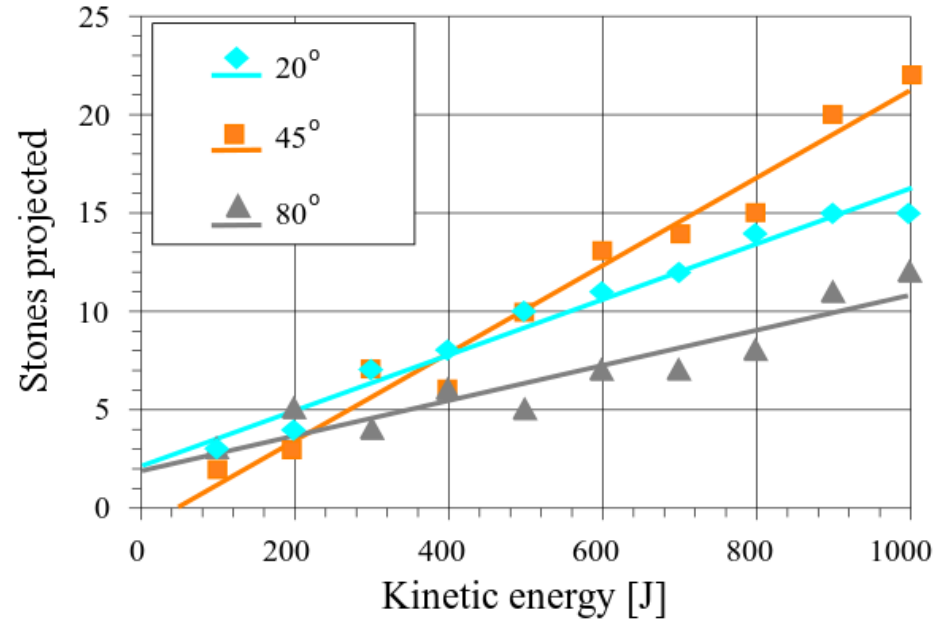
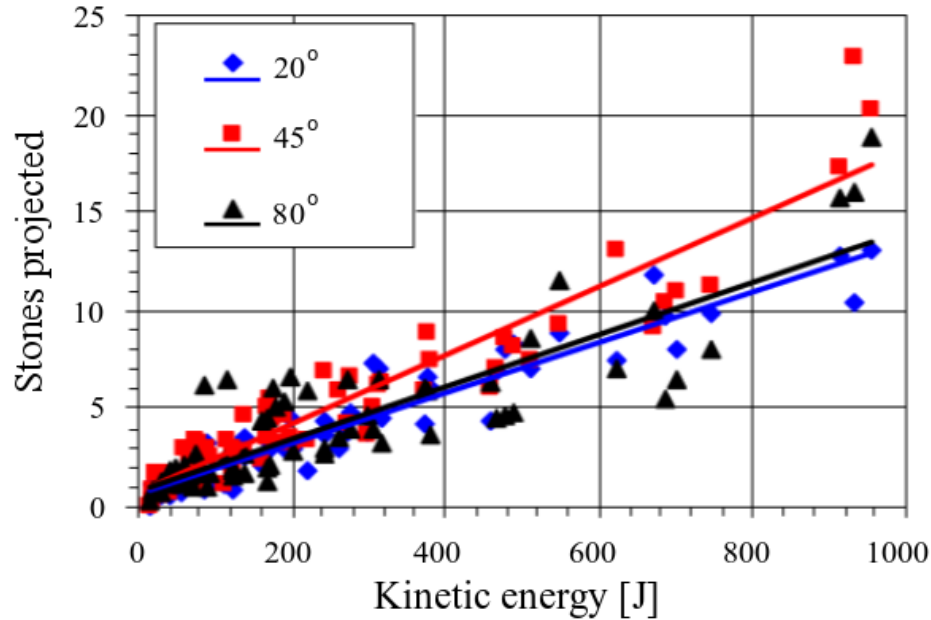
100 J

500 J

1000 J

# TEST RESULTS

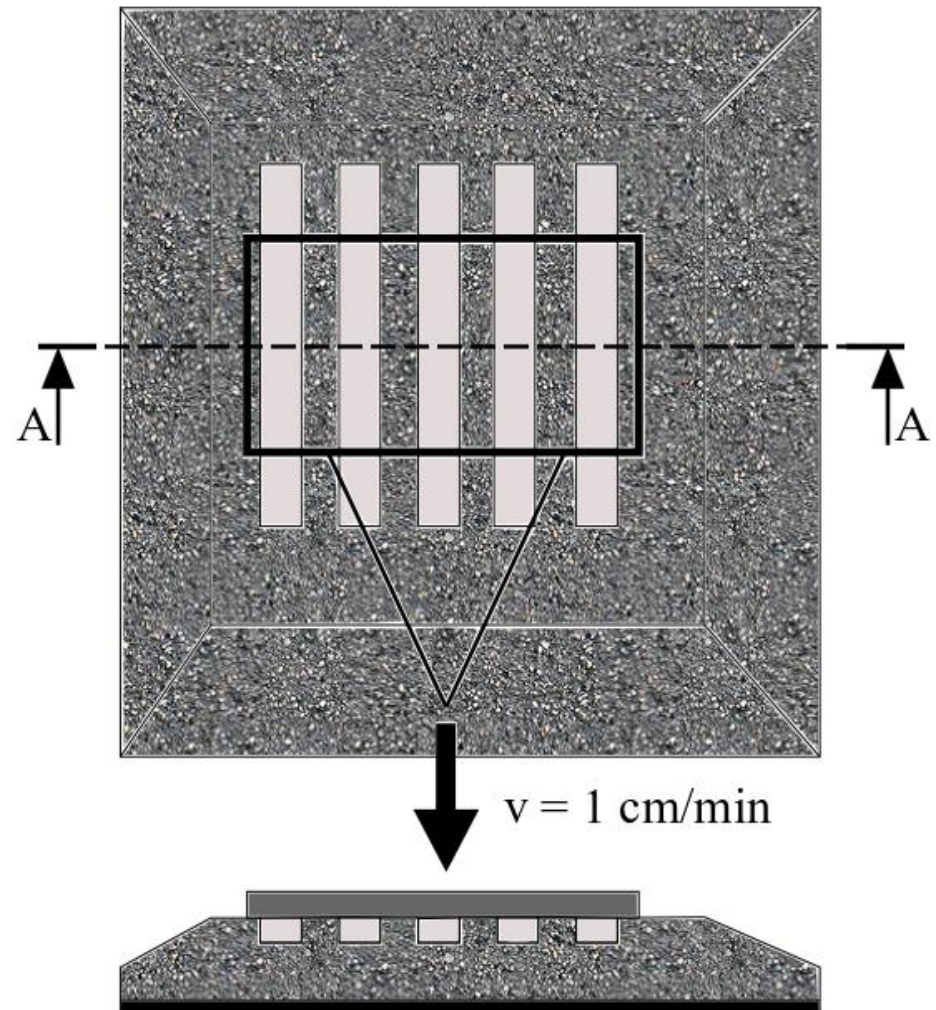
## Ballast stones projection:



# TEST RESULTS

## Lateral resistance test:

**Vertical load = 0 N**  
**Sleepers Velocity = 0.0001667 m/s**



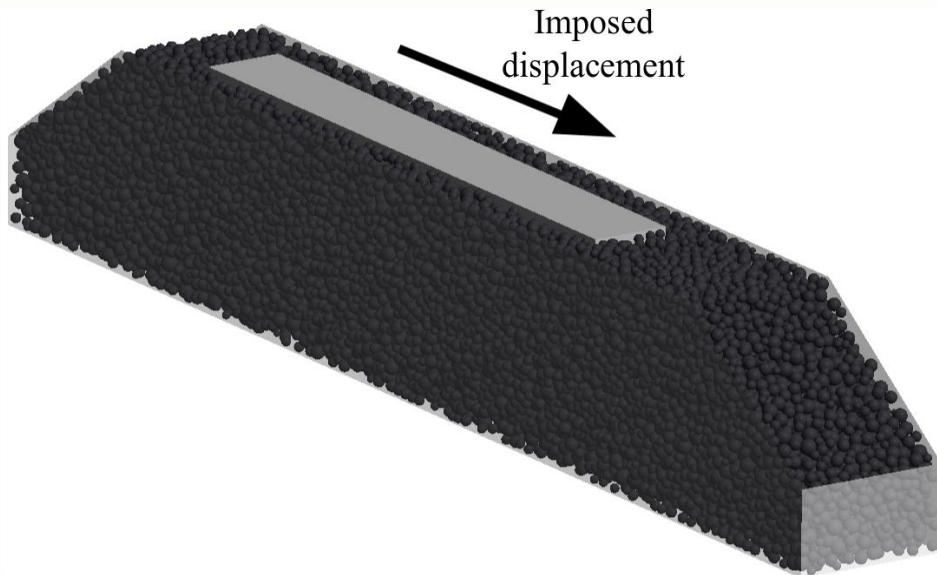
**Zand and Moraal (1997)**

**Roads and Railways Research Laboratory**

**Technical University of Delft**

# TEST RESULTS

## Lateral resistance test:



### Ballast properties

Density (kg/m <sup>3</sup> )	2700
Young Modulus (Pa)	5.1e9
Poisson ratio	0.18
Mean diameter (m)	0.05
Friction coeff.	0.6
Friction coeff. ballast/sleeper	0.7
Restitution coeff.	0.4
Rolling friction coeff.	0.33

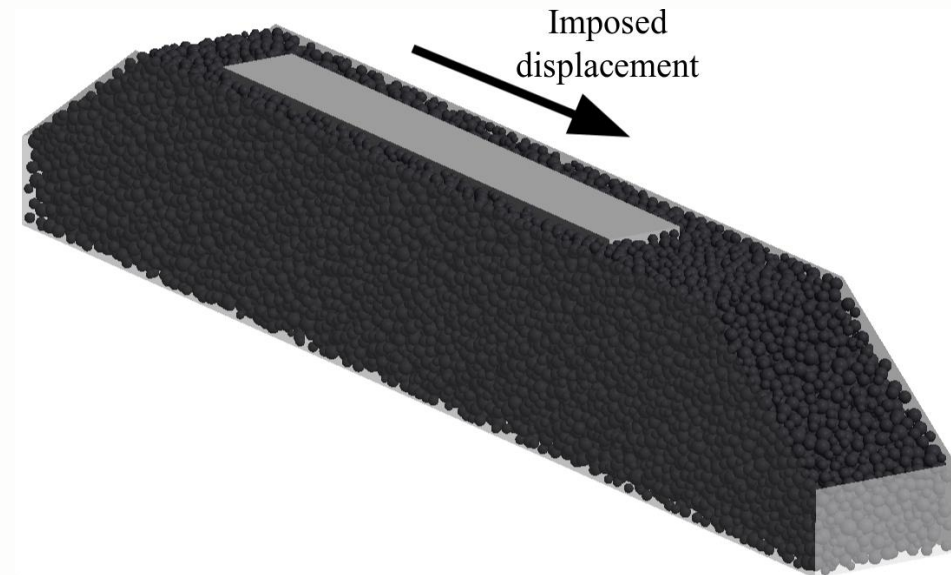
### Input parameters

Stabilization time (s)	1.0
------------------------	-----



# TEST RESULTS

## Lateral resistance test:



### Ballast properties

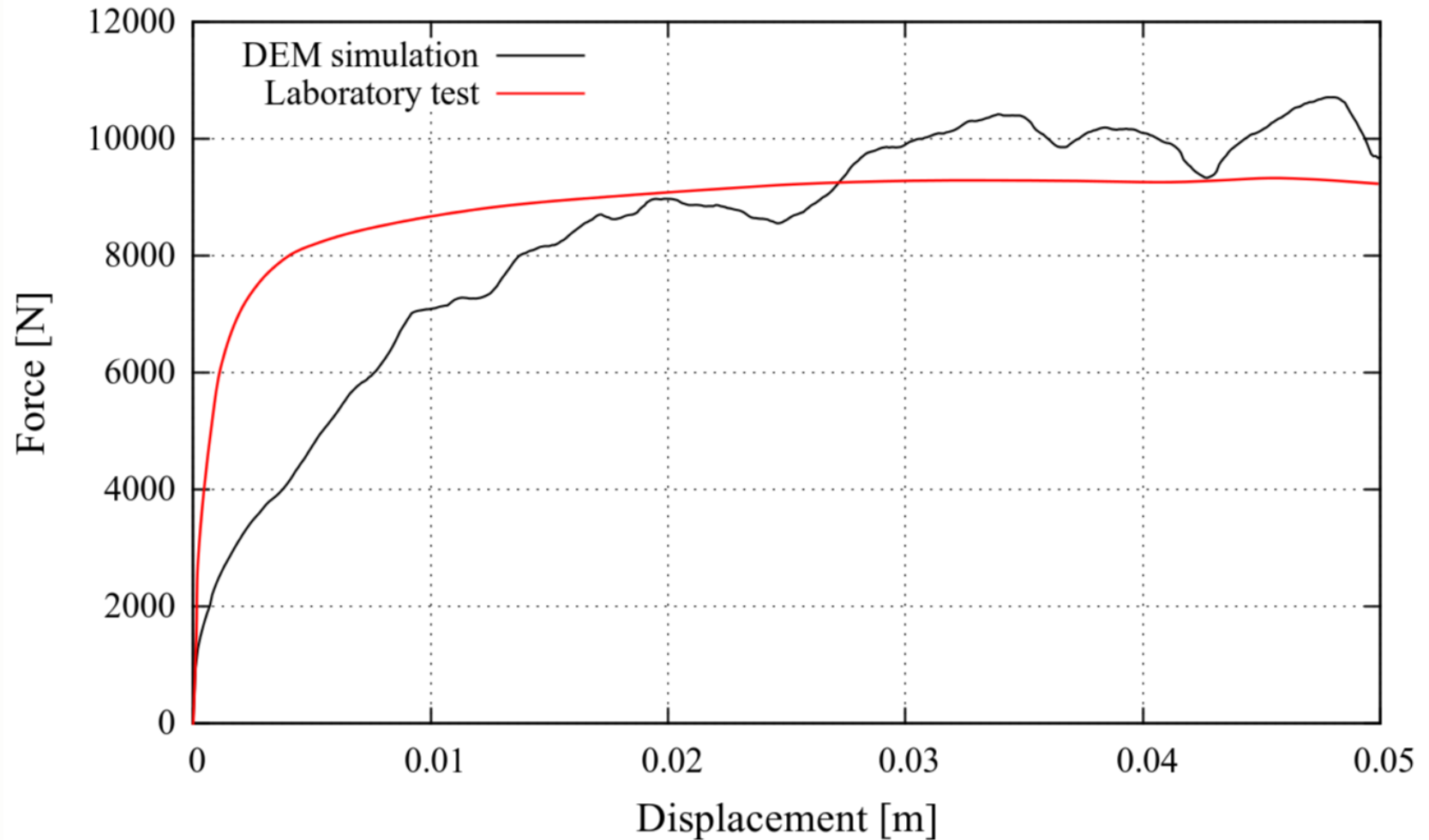
Density (kg/m <sup>3</sup> )	2700
Young Modulus (Pa)	5.1e9
Poisson ratio	0.18
Mean diameter (m)	0.05
Friction coeff.	0.6
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Restitution coeff.	0.4
Rolling friction coeff.	0.33

### Input parameters

Stabilization time (s)	1.0
------------------------	-----

# TEST RESULTS

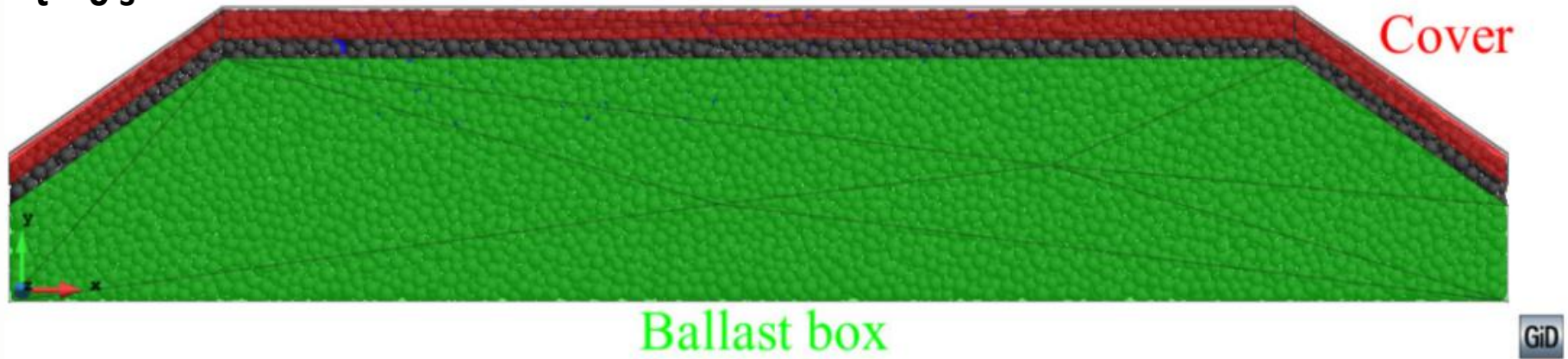
## Lateral resistance test:



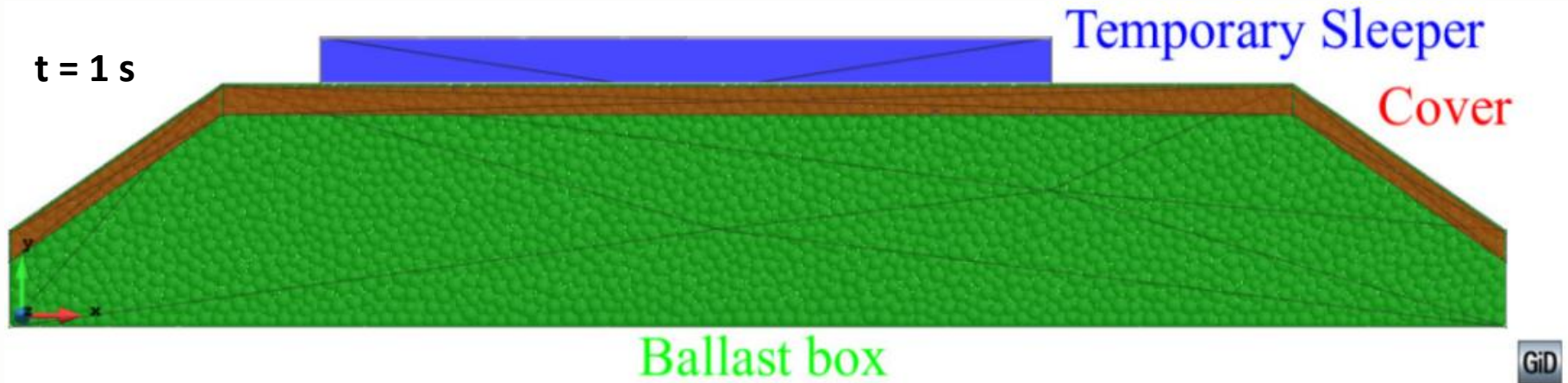
# TEST RESULTS

## Lateral resistance test:

$t = 0$  s

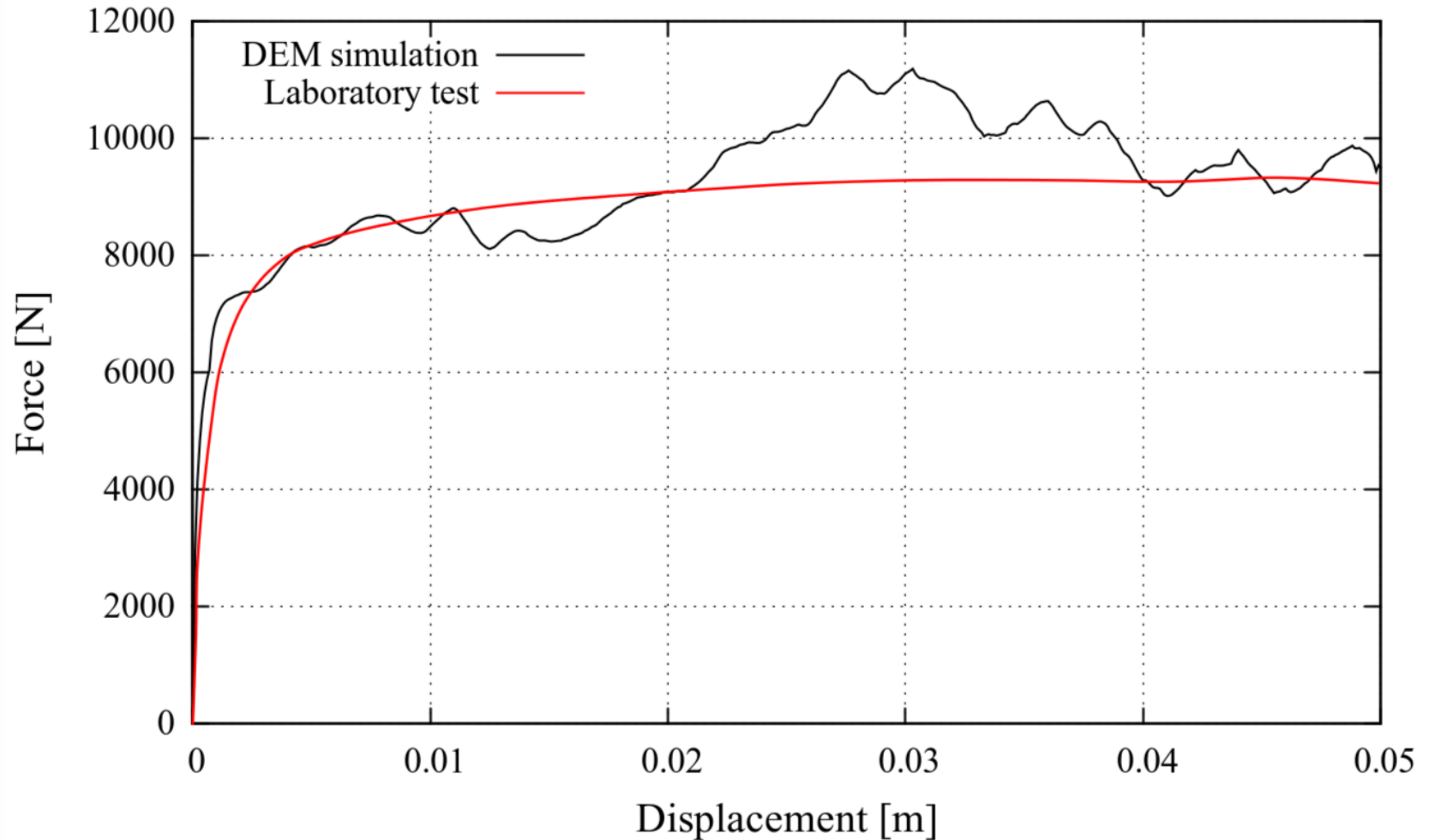


$t = 1$  s



# TEST RESULTS

## Lateral resistance test:



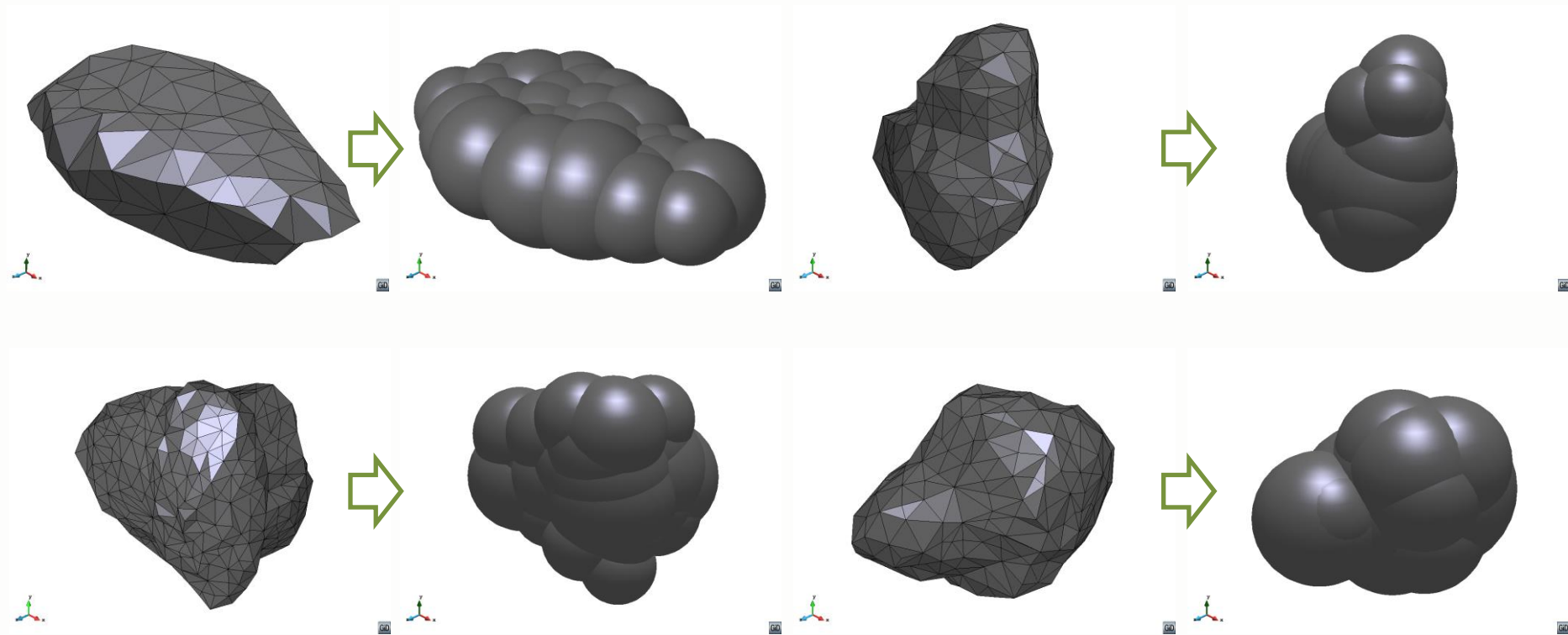
# TEST RESULTS

## Lateral resistance test:



# DIFFERENT PARTICLES SHAPE

## Sphere clusters:



Sphere-Tree Construction Toolkit (<http://isg.cs.tcd.ie/spheretree/>)

# DIFFERENT PARTICLE SHAPES

## Triaxial test:

**Diameter = 0.305 m**

**Height = 0.61 m**

**Confining pressure = 68.9 kPa**

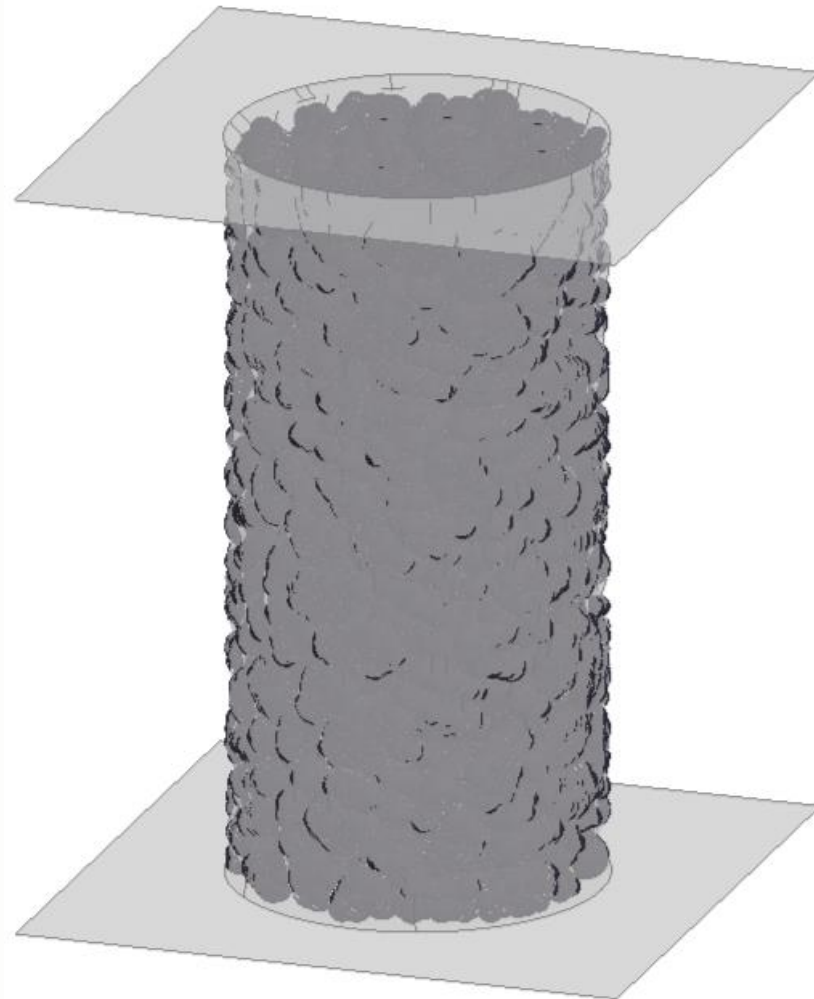
**Shear velocity = 0.038 m/s**



Quian et al. (2013) Triaxial compression test device - University of Illinois

# DIFFERENT PARTICLE SHAPES

## Triaxial test:



### Ballast properties

Density ( $\text{kg/m}^3$ )	2700
Young Modulus (Pa)	5.1e9
Poisson ratio	0.18
Mean diameter (m)	0.05
Friction coeff.	0.4
Friction coeff. ballast/membrane	0.0
Friction coeff. ballast/actuators	0.268
Restitution coeff.	0.4

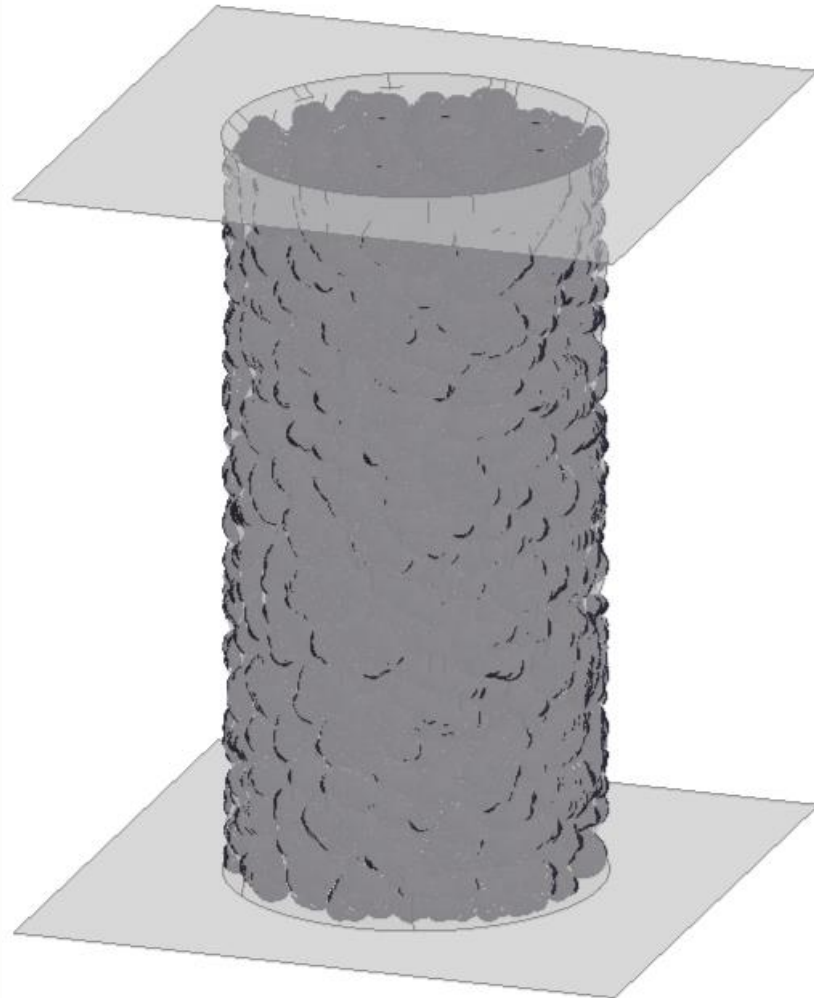
### Membrane properties

Young Modulus (Pa)	1.5e6
Poisson ratio	0.45
Thickness (m)	0.0023
Penalty factor ( $\gamma$ )	100



# DIFFERENT PARTICLE SHAPES

## Triaxial test:



### Ballast properties

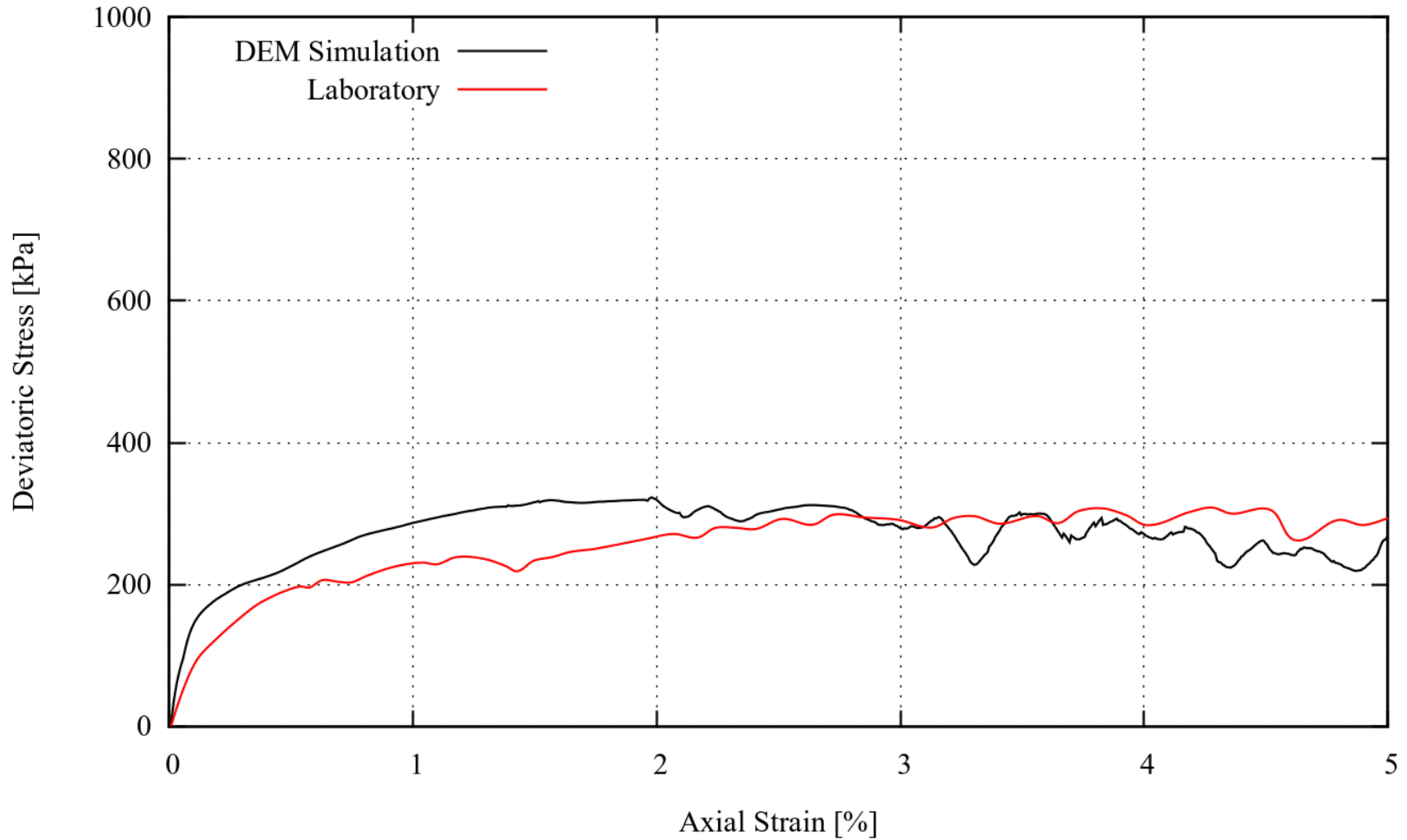
Density (kg/m <sup>3</sup> )	2700
Young Modulus (Pa)	5.1e9
Poisson ratio	0.18
Mean diameter (m)	0.05
Friction coeff.	0.4
Friction coeff. ballast/membrane	0.0
Friction coeff. ballast/actuators	0.268
Restitution coeff.	0.4

### Membrane properties

Young Modulus (Pa)	1.5e6
Poisson ratio	0.45
Thickness (m)	0.0023
Penalty factor ( $\gamma$ )	100

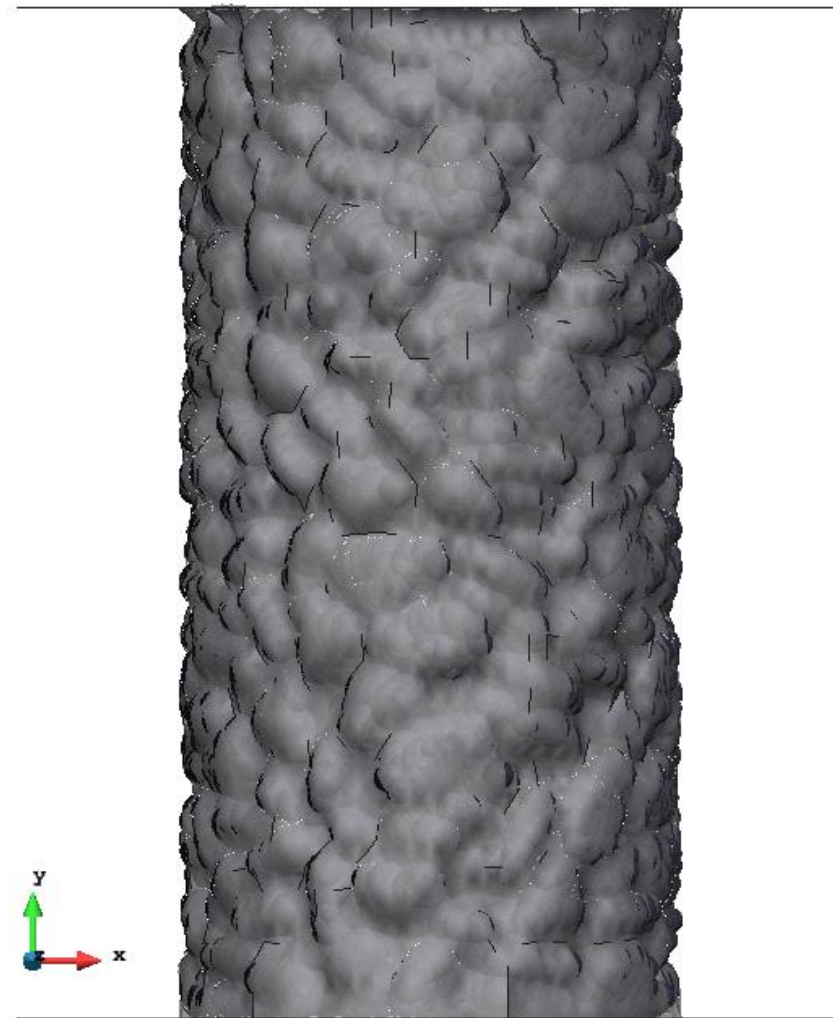
# DIFFERENT PARTICLE SHAPES

## Triaxial test:



# DIFFERENT PARTICLE SHAPES

Triaxial test:

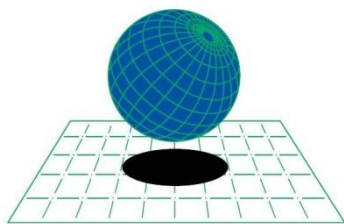


# CONCLUSIONS

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- **The DEM is an appropriate method for the calculation of ballast aggregates**
- **Rolling friction is useful for calculations with a great amount of material**
- **Material stiffness is a key property when measuring deformations**
- **Particle packing is an important variable**
- **Sphere clusters are a good approach to represent real geometries with low computational cost, but more validation work should be developed**

THANK YOU FOR YOUR ATTENTION



**CIMNE**<sup>®</sup>

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Eugenio Oñate ([onate@cimne.upc.edu](mailto:onate@cimne.upc.edu))