

Energy damage index based on capacity and response spectra

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ABSTRACT

To assess the expected seismic damage of a structure, non-linear dynamic analysis and the damage index of Park-Ang have been often used. Depending on the size of the structure and on the duration of the record, the computational effort in dynamic analyses is usually high. In this research a new damage index is proposed based on nonlinear static analysis. The damage index is a linear combination of two energy functions: 1) the strain energy associated to the stiffness variation and the ductility of the structure and 2) the energy dissipated associated to hysteretic cycles. These two energy functions are obtained from the capacity curve of the structure and from the energy balance with the spectral acceleration. To show the ability of the index to represent damage, low-rise steel buildings subjected to seismic actions expected in Mexico City are studied. The results obtained with the new method show a good agreement with those calculated by means of dynamic analyses using the Park-Ang damage index. In average, the Park-Ang damage index is well fitted by the combination of 62% of the strain energy and 38% of the energy dissipated by hysteresis. Moreover, this new damage index allows linking damage to certain characteristics of the seismic actions as, for instance, intensity and duration of the applied seismic action. Therefore, the new approach results in a practice and powerful tool for estimating the seismic damage in buildings, especially when considering probabilistic approaches, where massive computations are needed.

Keywords: Capacity curve; damage assessment; strain energy; energy dissipated by hysteresis; Monte Carlo simulations.

1 Introduction

When assessing the seismic performance of buildings, the Non Linear Dynamic Analysis (NLDA) has proved to be the most realistic, suitable, but also sophisticated, numerical tool which allows estimating the response of a structure as a function of time. When using the NLDA for assessing the seismic response, the input is, in general, a group of accelerograms, that can be recorded, synthetic or both. If the NLDA is performed by increasing the ordinates of the selected accelerograms, we are faced with the Incremental Dynamic Analysis (IDA) [1]. The use of IDA makes possible obtaining curves relating a measure of the seismic response of a structure (the roof displacement, the maximum inter story drift, etc.) to a variable which describes the seismic intensity like, for instance, the peak ground acceleration (PGA). The IDA has been used as the most appropriate tool for assessing the damage in structures subjected to dynamic actions [1]. It is important to note that, from the dynamic response of a structure, several damage indices can be calculated [2,3], which are related to the capacity reduction of the structural elements of

buildings. Several investigations have proposed damage indices for reinforced concrete and steel buildings considering different parameters such as, for example, the displacement ductility [4,5], strength and stiffness degradation [3], energy dissipation [6,7], cyclic fatigue [8], change of the natural period of the structure [9], or a combination of the above parameters [10–13]. Most of the damage indices proposed up to date, take values in the range from 0 to 1, where 0 indicates no damage and 1 collapse. Park and Ang [11] proposed one of the most used seismic damage indices for reinforced concrete buildings that considers both the maximum structural response and the cyclic load effect [14–16].

For calculating damage curves based on IDA, an important computational effort is required. In order to avoid this large computational effort, the nonlinear static analysis (NLSA) offers an interesting alternative due to its simplicity [17,18], but it is necessary to ensure that the obtained results are in good agreement with those provided by IDA. Several researchers have employed the NLSA for estimating parameters related to the dynamic response of structures [19–23] or in risk studies at urban level [24–27]. In the present article, a new damage index for steel buildings, which can be obtained from the capacity curve, is proposed. This damage index exhibits a good fit with the damage index of Park and Ang. The mathematical formulation of the new damage index is based on energy functions and on the idea proposed by Pujades et al. [22] of using a calibration parameter to determine the contribution to damage of two or more simple functions and, thus, to obtain a good agreement with a relatively more complex damage index. Nevertheless, new functions considering two types of energy from the capacity curve are used herein: 1) the strain energy and 2) the energy dissipated by hysteresis [28,29]. When combining both functions, a new damage index, compatible with the damage index of Park and Ang, is obtained. In order to consider the effect of the seismic hazard, the performance point is based on the concept of energy balance [30] and the application the seismic evaluation is based on the study of Leelataviwat et al. [31]. As a testbed, a three stories steel building, subjected to seismic actions expected in Mexico City, is employed. In order to formulate the new damage index, a deterministic case is presented first. A probabilistic approach based on the Monte Carlo method and on the Latin Hypercube Sampling (LHS) technique is also included. The cases studied in this article show that the new damage index for the steel structures typology analyzed herein allows assessing the expected damage directly from the capacity curve, in a straightforward way, thus avoiding the large of computational effort involved in dynamic simulations.

2 Damage model based on energy

2.1 Damage index of Park and Ang

The damage index of Park and Ang (PA) [11] allows estimating the damage level of structures starting from a post-process of the nonlinear dynamic response; it is calculated as the sum of the maximum displacement divided by the ultimate displacement with a term related to the dissipated energy. For a structural element, the damage index, DI_{ePA} (δ), is given by the following equation:

$$DI_{ePA}(\delta) = \frac{\delta}{\delta_u} + \frac{\beta}{Q_y \delta_u} \int_0^{\delta} dE \quad (1)$$

where δ/δ_u is the ductility defined as the ratio of the maximum displacement of the structural element subjected to a specific earthquake, δ , to the ultimate displacement under monotonic loading, δ_u . Q_y is the strength at the yielding point; if the strength, Q_u , corresponding to the ultimate displacement, δ_u , is lower than Q_y , then Q_y is substituted by Q_u . $\int_0^{\delta} dE$ represents the hysteretic energy absorbed by the element during the earthquake and β is a non-negative strength deteriorating parameter. The global damage index of a structure is obtained by calculating the weighted damage index, $DI_{PAw}(\delta)$. The following equation was proposed by Park and Ang [11] in order to calculate the $DI_{PAw}(\delta)$:

$$DI_{PAw}(\delta) = \sum_{i=1}^N \lambda_i DI_{ePA}(\delta)_i \quad (2)$$

where $DI_{ePA}(\delta)_i$ is the damage index of the structural element i as defined in equation (1); N is the number of the damaged elements and λ_i is the ratio of the energy dissipated by hysteresis in the element i to the total hysteretic energy dissipated in the entire structure. Values of the damage index higher than 1.0 indicate structural collapse. In this article, the Park and Ang damage index is used as a reference of the expected damage for validating the new damage index proposed herein. Because that, the proposed damage index is based on similar concepts of ductility and energy dissipated by hysteretic cycles of the Park and Ang index.

2.2 The proposed damage index

Chopra [32] showed that the damping exhibited when the earthquake ground motion drives a structure into the inelastic range can be viewed as a combination of the viscous damping, inherent to the structure, and the hysteretic damping. Hysteretic damping is related to the area inside the loops defined by earthquake force - structural displacement diagrams. Hysteretic damping can be represented as equivalent viscous damping, ξ_{eq} , associated with a maximum displacement and it can be estimated by means of the following equation [32]:

$$\xi_{eq} = \frac{1}{4\pi} \frac{E_D}{E_{so}} \quad (3)$$

where E_{so} is the maximum strain energy associated to a cycle of motion, that is, the area under the secant stiffness at the ultimate point (D_{ci} , F_{ci}) of the capacity curve, which can be calculated as:

$$E_{so} = \frac{(D_{ci} * F_{ci})}{2} \quad (4)$$

E_D is the energy dissipated by the structure in a single cycle of motion, that is, in a single hysteretic loop. A graphic representation of E_D and E_{so} is shown in

Figure 1. E_D can be calculated starting from the bilinear representation of the capacity curve as the area enclosed within a single hysteretic loop, equivalent to the area of the large parallelogram shown in

Figure 1. The bilinear representation is obtained as follows: i) the area under the bilinear curve must be equal to the area under the original capacity curve, A_c ; ii) the initial slope, K_i , must be equal in both curves and iii) the coordinates of the ultimate capacity point (D_{ci} , F_{ci} and D_{bi} , F_{bi}) must match both curves. Based on the later conditions the following equations can be used for calculating the coordinates of the yield point (D_y , F_y):

$$D_y = \frac{2 A_c - (F_{ci} * D_{ci})}{(K_i * D_{ci}) - F_{ci}} \quad (5)$$

$$F_y = (K_i * D_y) \quad (6)$$

Starting from the points defined by the bilinear curve, E_D is calculated by using the following equation [28,32]:

$$E_D = 4(F_y * D_{bi} - D_y * F_{bi}) \quad (7)$$

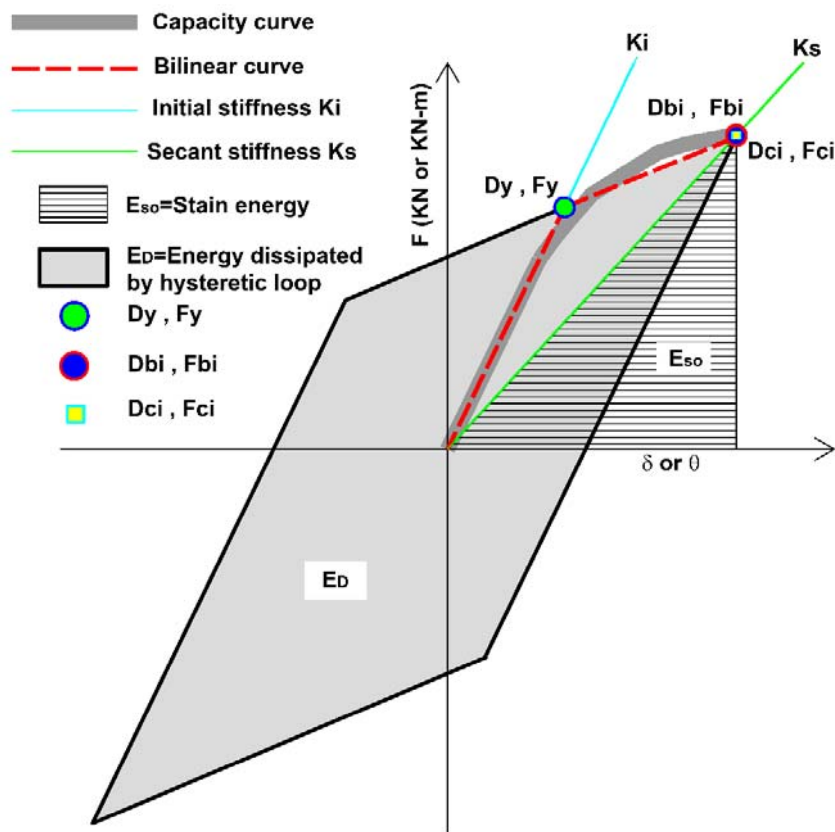


Figure 1 Capacity curve, bilinear curve (force-deformation relation) and equivalent viscous damping due to hysteretic energy dissipation.

Note that E_{so} and E_D can be calculated from the capacity curve as a function of the roof displacement, δ , in an incremental manner. Thus, two energy functions are defined as follows: 1) strain energy function, $E_{so}(\delta)$ and 2) energy dissipated by hysteretic function, $E_D(\delta)$. Based on the mathematical development of Chopra [32] for $E_{so}(\delta)$ and $E_D(\delta)$, the former can be related to the stiffness and ductility and the latter to the energy dissipation; both functions depend on the intensity of the earthquake.

Based on these functions, a damage index can be derived adopting two following the criteria: i) Both functions are normalized to 1 for the value related to the ultimate displacement, δ_u , of the capacity curve; ii) both functions will have a value equal to zero for $\delta \leq \delta_{Dy}$ because, within the linear range of the structure, the expected damage should be zero. Thus, the normalized energy functions $E_{so}(\delta)_{NN}$ and $E_D(\delta)_{NN}$ can be calculated by means of the following equations:

$$E_{so}(\delta)_{NN} = \begin{cases} 0 & 0 \leq \delta \leq \delta_{Dy} \\ \frac{E_{so}(\delta)}{E_{so}(\delta_u)} & \delta_{Dy} < \delta \leq \delta_u \end{cases}, 0 \leq E_{so}(\delta)_{NN} \leq 1 \quad (8)$$

$$E_D(\delta)_{NN} = \begin{cases} 0 & 0 \leq \delta \leq \delta_{Dy} \\ \frac{\sum_{j=0}^n E_D(\delta)}{\left[\sum_{j=0}^n E_D(\delta) \right]_{\max}} & \delta_{Dy} < \delta \leq \delta_u \end{cases}, 0 \leq E_D(\delta)_{NN} \leq 1 \quad (9)$$

where j represents each increment in the displacement of the capacity curve, n represents the ultimate increment. Using equations 8 and 9, the following damage index, $DI_{EC}(\delta)$, is then proposed:

$$DI_{EC}(\delta) = \eta E_{so}(\delta)_{NN} + (1 - \eta) E_D(\delta)_{NN} \cong DI_{PAW}(\delta) \quad (10)$$

Observe that $DI_{PAW}(\delta)$ can be used to calibrate the value of the parameter η . The parameter η is directly related to the percentage of the contribution to the damage of the strain energy function, while their counterpart in Eq.10, corresponds to the contribution of the energy dissipated due to the hysteretic function. The two energy functions can be obtained from the capacity curve of the building; although, can also be obtained from the bending moment M rotation θ curve of a structural element; and $DI_{ePA}(\delta)$ is used to calibrate the value of the parameter η . This new damage index is referred hereinafter as energy capacity damage index, $DI_{EC}(\delta)$. The calculation and implementation of $DI_{EC}(\delta)$ are presented in the next section.

3 Example of implementation the new damage index

3.1 Structural model

A three stories steel building with four spans is used to illustrate the computation of the proposed energy capacity damage index. This building has been studied extensively by Diaz et al. [33] in order to study its performance and its expected seismic damage for the Mexico City conditions. The main geometric characteristics and structural

sections of the building are show in Figure 2. The structural system of the building is a special moment frame (SMF) composed of beams and columns with W sections (American wide flange section), which are joined by means of prequalified connections [34] type Fully Restrained (FR). This building was designed as an office building considering the provisions of NTC-DF [35] and ANSI/AISC 341-10 [36]. The design of the SMFs satisfies the criterion of strong column-weak beam. The nonlinear structural analyses, both static and dynamic, were performed using Ruaumoko 2D software [2]. Beams and columns were modeled as FRAME type members, with plastic hinges at their ends. Plastic hinges follow the Bi-Linear Hysteresis rule with hardening and strength reduction based on its ductility factor. See Appendix A - Ruaumoko 2D [2]. Due to the limitations of the adopted model, which only reproduces the failure by bending moment, the interaction between moment and axial force is not considered. In addition, most of the damage for this type of building is expected to occur at the ends of the elements, mainly because of the effects of the bending moment. The interaction of yield surface is defined for columns and beams by the diagram relating the bending-moment with the rotation. Moreover, the values of strength and ductility for the hysteresis rule were calculated according to the modified Ibarra–Medina–Krawinkler (IMK) model [37–39]. The panel zones were modeled by using the rotational stiffness in connections, according to the model of Krawinkler [40] included in FEMA 355C [41]. For the damping, it is assumed the Rayleigh model and a damping ratio of 2% [42,43]. The fundamental period, T_1 , of the building model is 0.63 s.

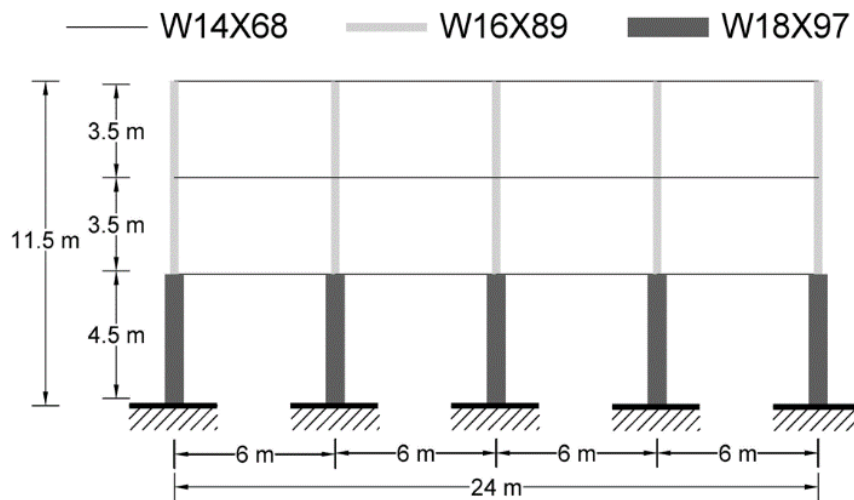


Figure 2 Geometry and structural section of the archetype building.

3.2 Seismic actions

In order to calibrate the new damage index, $DI_{EC}(\delta)$, it is necessary to obtain damage curves using the IDA method. Acceleration records of Mexico City were used in this example. The design spectrum for the IIIa seismic area, according to NTC-DF [35], was taken as target spectrum. The selection method proposed by Vargas et al. [21] was applied to a database that contains 2554 accelerograms recorded in the Mexico City area [44]. Four accelerograms

were thus selected whose response spectra are compatible, in mean, with the target spectrum. The main characteristics of these accelerograms are shown in Table 1.

Table 1– Characteristic of the seed accelerograms used of the seismic zone IIIa in Mexico City.

Acc.	Station	Date	Duration (seconds)	Epicenter			Magnitude (Mw)	Component	PGA (cm/s ²)	Epicenter distance (km)	Azimut Station-Epicenter
				Latitude	Longitude	Depth (Km)					
1	AL01	18/04/2014	165.77	17.18 N	101.19 W	10	7.2	S00E	28.86	330.89	221.04
2	HJ72	18/04/2014	167.47	17.18 N	101.19 W	10	7.2	N90W	32.19	331.06	221.39
3	MJSE	15/06/1999	144.01	18.18 N	97.51 W	69	7.0	N76W	13.76	222.31	128.79
4	TL55	30/09/1999	173.86	15.95 N	97.03 W	16	5.2	N90E	15.62	447.59	149.67

Each one of the accelerograms of Table 1 was used as a seed within a probabilistic spectral matching technique [33,45] to get 5 new accelerograms whose response spectra show a good agreement with the target spectra. Thus, a set of 20 matched accelerograms were obtained, considered suitable to deal with the uncertainties in the seismic actions in order to validate the proposed damage index in a probabilistic environment. Figure 3a shows the seed accelerogram 1 and one of the matched accelerograms which is used for performing the IDA analysis. Figure 3b shows the target spectrum, the response spectrum of the seed accelerogram 1 and the response spectrum of the matched accelerogram.

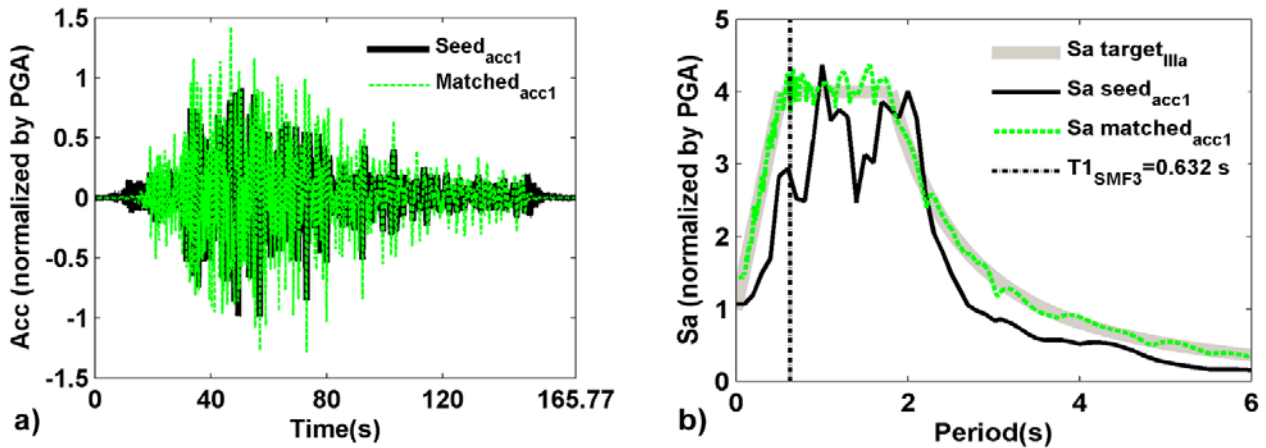


Figure 3 a) The seed accelerogram 1 and the matched accelerogram, and b) the target spectrum (IIIa) and the response spectra for seed accelerogram 1 and the matched accelerogram.

3.3 Capacity curve

The capacity curve is obtained by means of an adaptive pushover analysis (P_{ad}), implemented in the Ruaumoko software [2]. This method is independent of the initial loading pattern as the method adapts this pattern at each step of the P_{ad} according to the shape of the first vibration mode of the structure. The ultimate capacity is set when one of the following criteria is fulfilled: i) ω^2 is less than $10^{-6} \omega^2$ at the first step, being ω the tangent fundamental

natural frequency in the Modified Rayleigh Method; ii) the Newton Raphson iteration is not achieved within a maximum number of specified cycles; iii) the stiffness matrix becomes singular and iv) a specified maximum structure displacement is reached. In the NLSA's of the studied models, a large number of cycles for the Newton Raphson method has been considered. Moreover, a large maximum limit for the structure displacement has been considered too; thus, it is expected that the failure criteria be related to criteria i or iii. The conventional pushover and the P_{ad} for buildings with structural response dominated by their fundamental mode provide similar capacity curves; however, in this research, the P_{ad} is preferred, because it includes predefined criteria to determine the ultimate capacity point, previously mentioned. Which is useful in the probabilistic assessments to define the collapse in each analysis. In addition, these predefined failure criteria in the capacity curve allow obtained a compatibility with the ultimate capacity point achieved the IDA. Moreover, for the methodology presented in this study, the conventional pushover can also be used, if the ultimate capacity point is adequately defined. Figure 4a shows the plastic hinges formed in the ultimate capacity point of the building and in the Figure 4b its respective inter-story drift. The size of each plastic hinges in the building corresponds to the degree of plasticization in each structural element, when the building reaches its ultimate capacity. Finally, in the Figure 5a shows the obtained capacity curve.

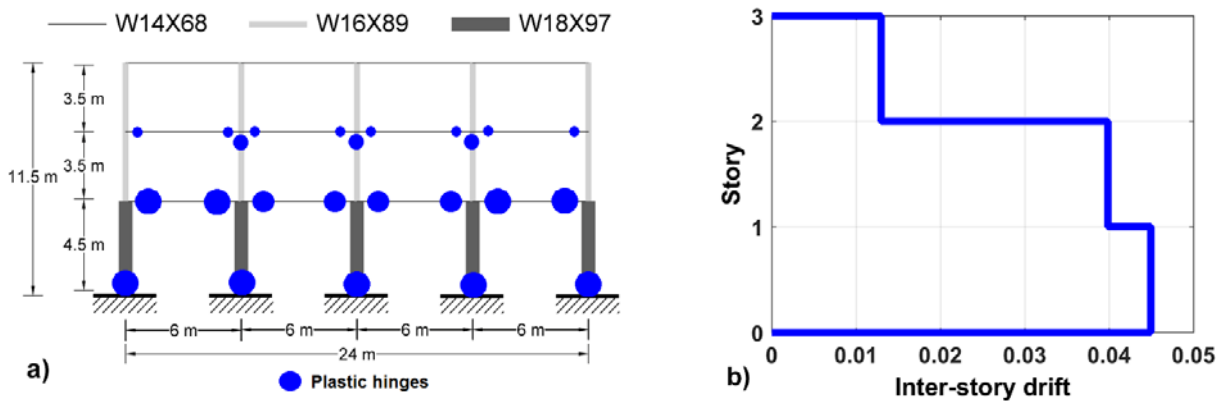


Figure 4 a) Plastic hinges formed when the building reaches its ultimate capacity and b) its respective inter-story drift.

3.4 Incremental dynamic analysis

The incremental dynamic analysis is performed for the studied building using the matched accelerogram shown in Figure 3a. The PGA of the record has been increased until the collapse of the structure, established in terms of ultimate displacement δ_u , was reached. The collapse displacement of the building, in this case, corresponds to a PGA of 1 g. The $DI_{PAW}(\delta)$ function of the roof displacement, δ , for the building is shown in Figure 5a. The capacity curve and the $DI_{PAW}(\delta)$ are used in subsequent sections for calibrating the new damage index.

In order to prove that the new damage index can also be applied to a structural element, having the results of the IDA for the building, one can extract: i) the relation between $DI_{ePA}(\theta)$ and the rotation θ , ii) the bending moment

M - rotation θ curve of one of the beams on the first floor in the building, that is referred hereinafter BEAM 1 and shown in the Figure 5b.

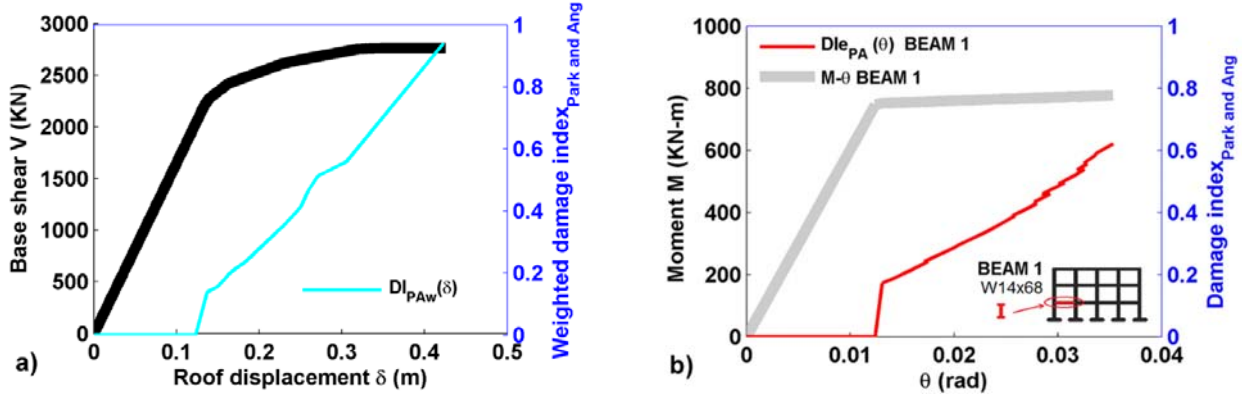


Figure 5 a) Capacity curve and the $DI_{PAW}(\delta)$ by IDA of the building; and b) the $DI_{ePA}(\theta)$ and M- θ diagram of the BEAM 1.

3.5 Proposed energy damage index for a structural element

As a first step, the damage index for a structural element is implemented, so that it can be calibrated with $DI_{ePA}(\theta)$. This is done for the structural element, BEAM 1. Based on the M- θ curve, the two energy functions depending on the angular deformation, $E_{so}(\theta)_{NN}$ and $E_D(\theta)_{NN}$, are obtained (see Figure 6). Afterwards, the energy capacity damage index for a structural element, $DI_{EC}(\theta)$, is calibrated by taking into account the $DI_{ePA}(\theta)$. The parameter η is obtained by means of a least squares fit of Eq 10. For the case discussed herein, the parameter η was set to 0.78. The contribution to the damage index of the strain energy function, $E_{so}(\theta)_{NN}$, is 78%, while the contribution of the energy dissipated by hysteretic, $E_D(\theta)_{NN}$, is 22%. Figure 6 shows the $DI_{ePA}(\theta)$ and $DI_{EC}(\theta)$ for the BEAM 1. The $DI_{EC}(\theta)$ is in excellent agreement with the $DI_{ePA}(\theta)$. The parameter η allows a good fit of the new index, $DI_{EC}(\theta)$, to the expected damage in a structural element subjected to seismic actions.

This example shows that the proposed functions and damage index can replicate the expected damage in the element structural by the Park and Ang index. However, for that, the proposed index can be a viable alternative to reduce the computational times in the probabilistic assessments; this should be calculated directly from the capacity curve, as shown in the next section.

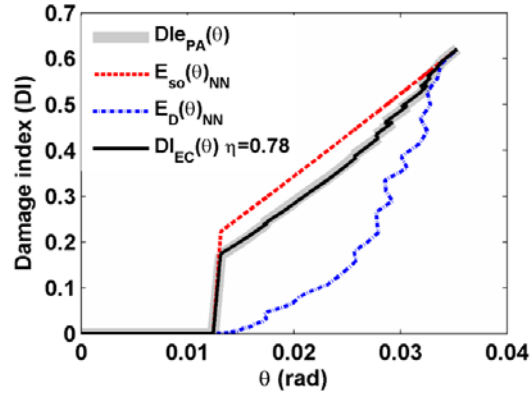


Figure 6 New damage index of $DI_{EC}(\theta)$ and $DI_{PA}(\theta)$ for the BEAM 1.

3.6 Energy capacity damage index for the entire building

In order to calibrate the simplified energy capacity damage index $DI_{EC}(\delta)$, it is considered that the evolution of the damage $DI_{PAW}(\delta)$ is closely related to the roof displacement caused by the seismic action. Observe that it is expected that these displacements be different for different seismic actions because important properties as, for instance, the duration and frequency content of each seismic action can vary, causing a different structural response for equal PGA values.

The IDA method provides the displacement pattern as a function of the PGA. Otherwise, in the NLSA, in order to define the roof displacements as a function of the increased PGA of seismic action, $S_{dpp}(PGA)$, the performance point for each PGA value must be calculated. The performance point can be obtained by applying the capacity spectrum method proposed by Freeman [46] and included in ATC-40 [28], FEMA-273 [47]. Chopra and Goel [29] and Fajfar [48,49] developed an improved version of the capacity spectrum method that uses the constant-ductility design spectrum as demand diagram. In these researches, the concepts of equivalent ductility factors by the R_y - μ_s - T equations introduced by Newmark and Hall [50] and Vidic et al. [51] are used, where R_y is the reduction factor due to the ductility, μ_s is the ductility factor defined as the ratio between the maximum displacement and the yield displacement and T is the period of the demand spectrum. Another proposal for calculating the performance point is that of Mezzi et al. [52] and Leelataviwat et al. [31,53], which is based on the balance between the energy spectrum of the seismic action in the Energy Displacement Response Spectrum (EDRS) format and the energy obtained from the area beneath the capacity curve, named as Accumulated Deformation Energy, ADE. In the present research, the methodology of energy balance is used to obtain the displacement patterns due to seismic actions. In this methodology, the capacity curve obtained from the building, shown in Figure 5a, and the response spectrum of the acceleration shown in Figure 3b, have been used.

The first step for calculating the performance point consists in obtain the accumulated deformation energy, ADE, of the capacity curve, $F(\delta)$, by using the a following equation:

$$ADE(\delta) = \int_0^{\delta} F(\xi) d\xi \quad 0 \leq \xi \leq \delta_u; \quad 0 \leq ADE(\delta) \leq ADE(\delta_u) \quad (11)$$

Figure 7 shows the capacity curve and the $ADE(\delta)$ curve of the building. The yielding roof displacement, δ_y , the yielding base shear, V_y , and the yielding energy E_y are also plotted in this figure. The second step consists in obtaining the input energy spectrum in EDRS format (Sa_{EDRS}) from the pseudo-velocity spectrum, Sv , using the following equation:

$$Sa_{EDRS} = \frac{1}{2} \gamma_E M^* S v^2 = \frac{1}{2} \gamma_E M^* S a^2 \left(\frac{T}{2\pi} \right)^2 \quad (12)$$

$$\gamma_E = \frac{\mu_E}{R_y^2}; \quad \mu_E = 2\mu_s - 1 \quad (13)$$

where M^* is the effective modal mass for the first mode of vibration of the building; T is the period of the demand spectrum; μ_s is the ductility factor; γ_E is the energy factor, in terms of energy ductility μ_E ; R_y is the yield strength reduction factor; and Sa is the pseudo-acceleration spectrum. The values of μ_s and R_y can be easily obtained by using R_y - μ_s - T equations evaluable in the literature [29]. In this research, the equations proposed by Chopra [32] based on the elastic design spectrum of Newmark and Hall [50] have been used:

$$R_y = \begin{cases} 1 & T < T_a \\ (2\mu_s - 1)^{\frac{\beta^*}{2}} & T_a \leq T \leq T_b \\ \sqrt{2\mu_s - 1} & T_b \leq T \leq T_c \sqrt{2\mu_s - 1}/\mu \\ (T/T_c)\mu_s & T_c \sqrt{2\mu_s - 1}/\mu \leq T \leq T_c \\ \mu_s & T > T_c \end{cases} \quad (14)$$

$$\beta^* = \ln\left(\frac{T}{T_a}\right) \ln\left(\frac{T_a}{T_b}\right) \quad (15)$$

where T_a , T_b and T_c are limiting period values that depend on ground motion parameters. Based on the demand spectrum in the Acceleration Displacement Response Spectrum (ADRS) format and by using the Eqs. (12) to (15), the Sa_{EDRS} can be obtained.

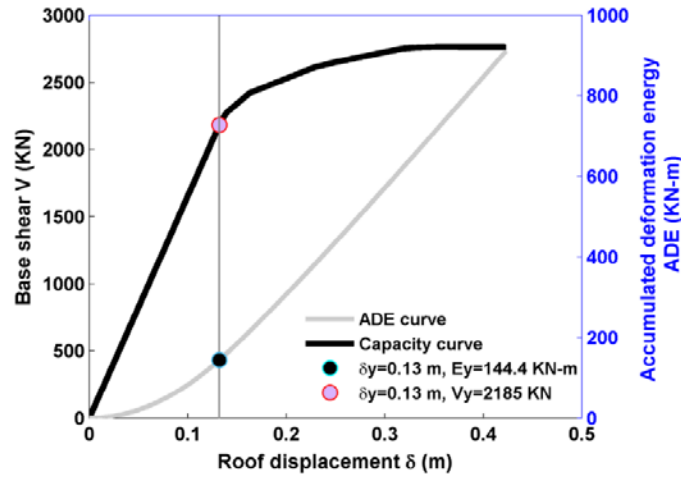


Figure 7 Capacity curve and ADE curve of the building.

In order to assure the energy balance [31,52–54], the following steps should be carried out: i) convert the displacement at the roof of the ADE curve to spectral displacement, S_d , by using the modal participation factor, PF_1 ; ii) normalize the ADE curve and the spectrum of energy demand, S_{aEDRS} , with the corresponding energy value at the yielding displacement, E_y ; iii) obtain the S_{aEDRS} for a ductility, $\mu_s=1$, and cross S_{aEDRS} and ADE curves to find the performance point S_{dPP} ; iv) determine the ductility μ_{PP} of the relation S_{dPP} with the yielding spectral displacement S_{d_y} ; if $\mu_{PP} \leq 1$, then the S_{dPP} is the displacement of performance for the seismic action applied and the structure has a performance in the linear range; if $\mu_{PP} > 1$, perform again the step iii) for a higher μ_s and determine a new S_{dPP} and μ_{PP} ; repeat until $\mu_s \approx \mu_{PP}$ with a predefined error; then the new S_{dPP} is the displacement of performance for the seismic action applied and the structure has a performance in the nonlinear range. Finally, convert S_{dPP} to roof displacement δ , by using the modal participation factor, PF_1 .

For the studied case, $M^*= 215.5 \text{ KN sec}^2/\text{m}$, $\delta_y=0.13 \text{ m}$; $E_y=144.4 \text{ KN-m}$, $PF_1= 1.29$, the $R_y - \mu_s - T$ are taken from Eqs (14) and (15) where $\mu_s=1$, $T_a=1/33 \text{ s}$, $T_b=0.125 \text{ s}$ and $T_c=0.6 \text{ s}$ defined by Chopra [32]. The S_a matched acc1 for a PGA equal to 0.45g shown in Figure 8a is used. Figure 8b shown the respective S_a matched acc1 in EDRS format and normalized to E_y . T_a , T_b and T_c used in the R_y - μ_s - T equations, for the particular case studied, have provided adequate results, this is attributed to that, R_y becomes in constant in the R_y - μ_s - T equations for medium and long periods, so that, its variation affects structures of short periods. Then for the case studied, that have a medium period ($T_1= 0.63 \text{ s}$), the variation of R_y does not have an important influence on the application of the energy balance. However, this may not be the case with other seismic actions and types of buildings, so it is recommended calibrate these boundary periods for each case.

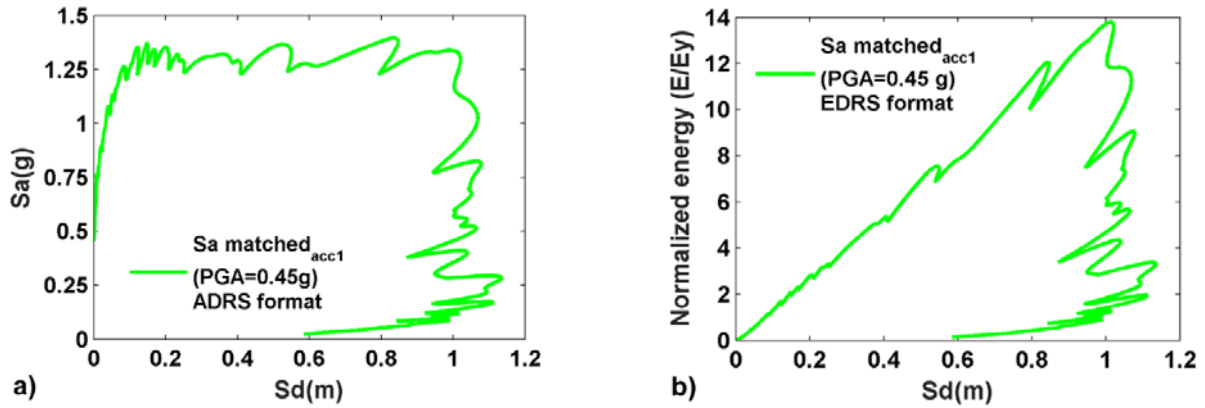


Figure 8 Sa matched acc1 for a PGA equal to 0.45 g in a) ADRS format and b) EDRS format.

Figure 9a shows an example of the energy balance for the building by using $Sa_{\text{matched acc1}}(\text{EDRS format})$ for a $\text{PGA}=0.45$ g and the ADE curve shown in Figure 7; both curves are normalized to E_y . For the considered values $Sd_{\text{pp}}=0.17$ m and $\mu_s=1.64$.

The static roof displacements are then determined assuring the energy balance, considering the PGA incrementally and converting the Sd_{pp} into roof displacements, δ . Based on the IDA of the building, the relation between PGA and the maximum roof displacement, δ is obtained; the values δ of this relation define the dynamic displacement pattern. Figure 9b shows the comparison between the static and dynamic displacement functions that have been obtained by using the IDA and the energy balance respectively. In this case, both displacement functions show a very good agreement.

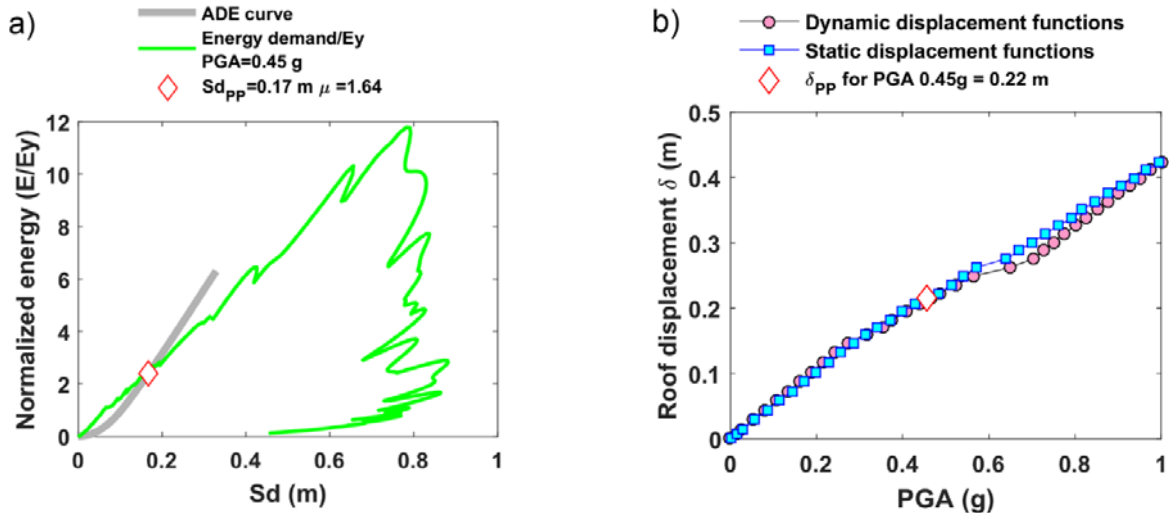


Figure 9 a) The energy balance of the building with the $Sa_{\text{matched acc1}}$ for $\text{PGA} = 0.45$ g; b) static and dynamic roof displacement functions.

Based on the static roof displacement function, the energy functions $E_{\text{so}}(\delta)_{\text{NN}}$ and $E_{\text{D}}(\delta)_{\text{NN}}$ are obtained (see Figure 10a). The $DI_{\text{PAW}}(\delta)$ of the building is used to calibrate the energy capacity damage index obtaining $\eta=0.70$, that

means, the contribution to the damage index of the strain energy function, $E_{so}(\delta)_{NN}$, is 70%, while the contribution of the hysteretic dissipated energy, $E_D(\delta)_{NN}$, is 30%. These percentages would vary for different seismic actions.

Figure 10a shows the energy capacity damage indices $DI_{EC}(\delta)$ and $DI_{PAW}(\delta)$ for the building. Both indices show a very good agreement. Observe that the damage curves calculated can be also related to the PGA by considering the function shown in Figure 10b. This way the proposed energy capacity damage index can be directly related to an intensity measure of the earthquake. Figure 10b shows the $E_{so}(PGA)_{NN}$ and $E_D(PGA)_{NN}$, $DI_{PAW}(PGA)$ and the $DI_{EC}(PGA)$ functions. In the case studied here, the $DI_{EC}(PGA)$ also shows a very good agreement with the $DI_{PAW}(PGA)$.

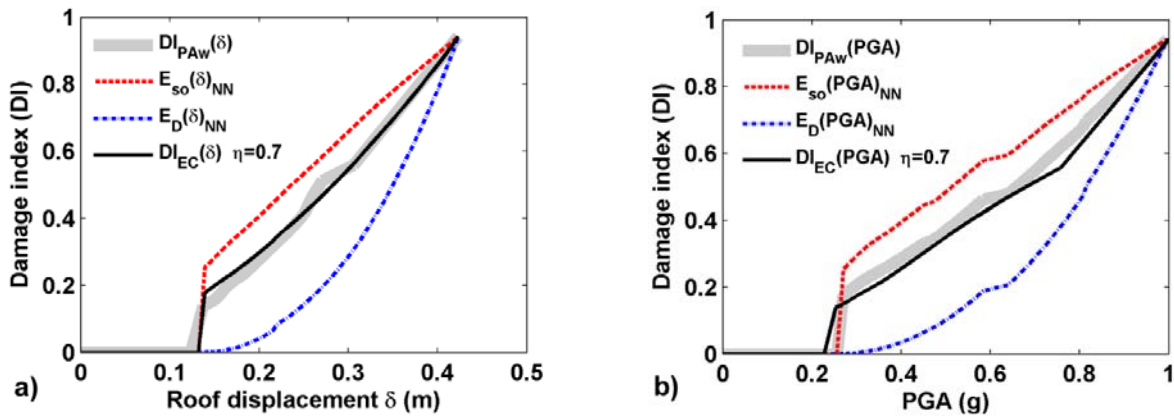


Figure 10 a) $DI_{PAW}(\delta)$ and $DI_{EC}(\delta)$; and b) $DI_{PAW}(PGA)$ and $DI_{EC}(PGA)$ of the SFM 3 building.

4 Probabilistic approach

The model of the studied building is used now to estimate the new damage index from a probabilistic point of view. It will be proved that the proposed damage index fits well the results obtained with the IDA also when several uncertainties are considered in the mechanical properties of the materials and in the seismic action. For the probabilistic approach, the Monte Carlo method [55,56] and the Latin Hypercube Sampling (LHS) technique [57,58] are used to optimize the number of samples. The strength and ductility of the beams and columns are considered as random variables in the modified Ibarra–Medina–Krawinkler (IMK) model [37–39]. The backbone curve of the modified IMK model is defined by three strength parameters: M_y = effective yield moment; M_c = capping moment strength or post-yield strength ratio M_c/M_y and $M_r = k \cdot M$, $k=0.4$, residual moment and by four deformation parameters: θ_y = yield rotation; θ_p = pre-capping plastic rotation for monotonic loading (difference between yield rotation and rotation at maximum moment); θ_{pc} = post-capping plastic rotation (difference between rotation at maximum moment and rotation at complete loss of strength); and θ_u = ultimate rotation capacity (see Figure 11a). The strength parameters can be determined for W sections according to Lignos and Krawinkler [38,39] and from the recommendations of PEER/ATC 72-1[43] using the following equations:

$$M_y = 1.17 \cdot Z \cdot f_y \quad (16)$$

$$M_c = 1.11 \cdot M_y \quad (17)$$

$$M_r = 0.4 \cdot M_y \quad (18)$$

The deformation parameters can be determined for W sections by means of the following multi-variable empirical equations, that were developed by Lignos and Krawinkler [38,39] and included in the PEER/ATC 72-1[43].

$$\theta_y = (M_y/k_o)/L = (1.17 \cdot Z \cdot f_y / 6 \cdot E \cdot I) / L \quad (19)$$

$$\theta_p = 0.0865 \cdot \left(\frac{h}{t_w}\right)^{-0.365} \cdot \left(\frac{b_f}{2 \cdot t_f}\right)^{-0.140} \cdot \left(\frac{L}{d}\right)^{0.340} \cdot \left(\frac{c_{unit}^1 \cdot d}{533}\right)^{-0.721} \cdot \left(\frac{c_{unit}^2 \cdot f_y}{355}\right)^{-0.721} \quad \sigma_{ln} = 0.32 \quad (20)$$

$$\theta_{pc} = 5.63 \cdot \left(\frac{h}{t_w}\right)^{-0.565} \cdot \left(\frac{b_f}{2 \cdot t_f}\right)^{-0.800} \cdot \left(\frac{c_{unit}^1 \cdot d}{533}\right)^{-0.280} \cdot \left(\frac{c_{unit}^2 \cdot f_y}{355}\right)^{-0.430} \quad \sigma_{ln} = 0.25 \quad (21)$$

$$\theta_u = 1.5 \cdot (\theta_y + \theta_p) \quad (22)$$

In these equations, k_o is the initial elastic stiffness; Z is plastic modulus; E is modulus of elasticity; f_y is expected yield strength; I is the inertia moment; c_{unit}^1 and c_{unit}^2 are coefficients for units conversion; h/t_w is the ratio between the web depth and the thickness; L/d is the ratio between the span and the depth of the beam; $b_f/(2 \cdot t_f)$ is the width/thickness ratio of the beam flange, and σ_{ln} is the standard deviation, assuming a lognormal fit of experimental data. The PEER/ATC 72-1 (2010) recommends that, when don't have experimental results of cyclic degradation of stiffness in the structural elements, the parameters θ_p and θ_{pc} must be adapted as follows: $\theta'_p = 0.7\theta_p$ y $\theta'_{pc} = 0.5\theta_{pc}$, as is the case of this study.

In this research is defined in the behavior of the structural elements by mean of the modified IMK model with its respective adaptation; this model can be implemented in the Ruaumoko (Carr 2002) using the bi-linear hysteresis rule with strength reduction based on the ductility. For this are used the following equations:

$$r = \left[\frac{M_c - M_y}{\theta'_p} \right] / k_o \quad (23)$$

$$DUCT1 = \frac{\theta_y + \theta'_p}{\theta_y} \quad (24)$$

$$DUCT2 = \frac{\theta_y + \theta'_p + [\theta'_{pc}(M_c - M_r) / M_c]}{\theta_y} \quad (25)$$

$$DUCT3 = \frac{\theta_y + \theta'_p + \theta'_{pc}}{\theta_y} \quad (26)$$

where r is hardening factor as a fraction of the initial stiffness, k_o ; DUCT1 is the ductility at which degradation begins; DUCT2 is the ductility at which degradation stops, the strength reduction rule of the Ruaumoko indicates

that the DUCT2, is defined based on the residual strength of the element, by mean of one constant, (RDUCT); in this research, RDUCT is defined as the constant $k = 0.4$ of the modified IMK model; finally, DUCT3 is the ductility at 0.01 of the initial strength (it is recommended to see the Ruaumoko manual (Carr 2002)). Thus, using equations (16) to (26), the expected behavior of the structural elements in the Ruaumoko is modeled. Figure 11a shows the model used based on the parameters of the modified IMK model and the bi-linear hysteresis rule with strength reduction based on the ductility of the Ruaumoko.

For a better representation of the physical randomness in the problem, for each structural element, a random sample of the three parameters used (f_y , θ_p and θ_{pc}) is generated. Afterwards, the properties of strength and ductility of the plastic hinges of each element are estimated. It is assumed that hinges at both ends of the elements are the same. Thus, the 3-stories model with 27 elements (15 columns and 12 beams) has 81 random variables. Table 2 shows the mean value μ , the standard deviation, the coefficient of variation (COV) and the assumed probability distributions of these 3 parameters.

Moreover, and to avoid unrealistic samples in LHS simulations, the normal distribution of f_y and lognormal distributions of θ_p and θ_{pc} were truncated at both ends, the lower and upper limits being determined by the mean value ± 2 standard deviations ($\mu \pm 2\sigma$). The purpose of this truncation is to avoid underestimates or overestimates of the capabilities of the elements with samples without physical meaning.

In summary, for this research, a simplified probabilistic approach is proposed. The method uses the modified IMK model for beams and columns and uncertainties are concentrated on the variables f_y , θ_p and θ_{pc} . Thus, it is assumed that these three variables have a major influence on the linear and nonlinear structural response of buildings; besides, the use of these variables is recommended in the new codes for probabilistic seismic performance assessment of steel buildings [43,59].

Another important issue concerning sampling, is the correlation among variables. Two types of correlations have been considered in this research: intra- and inter-element. The intra-element correlation is given by the relation among the three parameters simulated for the same hinge; these correlations can be derived from Eqs. (20) and (21) [38,39] and they are defined in Table 3. The inter-element is defined based on the research conducted by Idota et al. [60] and Kazantzi et al. [61] on the consistency in workmanship and material quality between different steel structural W sections; an inter-element correlation of 0.65 is used herein for the same section type, and a null correlation is assumed for different sections.

Table 2– Probabilistic property of the strength and ductility random variables.

Structural section	Type	Variable	Mean (μ)	Standard deviation (σ or σ_{ln})	Function
W14X68	Strength	f_y	375.76 MPa*	26.68 MPa (COV=0.071*)	Normal distribution
	Ductility	θ_p	0.054 rad*	$\sigma_{ln} = 0.32^*$	Lognormal distribution

	Ductility	θ_{pc}	0.188 rad*	$\sigma_{ln} = 0.25^*$	Lognormal distribution
W16X89	Strength	f_y	375.76 MPa*	26.68 MPa (COV=0.071*)	Normal distribution
	Ductility	θ_p	0.047 rad*	$\sigma_{ln} = 0.32^*$	Lognormal distribution
	Ductility	θ_{pc}	0.210 rad*	$\sigma_{ln} = 0.25^*$	Lognormal distribution
W18X97	Strength	f_y	375.76 MPa*	26.68 MPa (COV=0.071*)	Normal distribution
	Ductility	θ_p	0.044 rad*	$\sigma_{ln} = 0.32^*$	Lognormal distribution
	Ductility	θ_{pc}	0.183 rad*	$\sigma_{ln} = 0.25^*$	Lognormal distribution

* Based on the report by Lignos & Krawinkler [38] for statistics of material yielding strength, obtained from flanges-webs tests for steel A572 grade.

* For the steel structural W sections are determined by means of the multi-variable empirical equations (20) and (21).

Table 3–Intra-element correlation for random variables of beams and columns.

	f_y	θ_p	θ_{pc}
f_y	1	0	0
θ_p	0	1	0.69
θ_{pc}	0	0.69	1

In order to assess the seismic behavior of the studied building in a probabilistic environment, 200 NLSA's and 200 NLDA's were performed by using the same structural models for both the static and the dynamic analysis. Figure 11b shows an example of the modified IMK model used in the 12 beams W14x68 section of the probabilistic models.

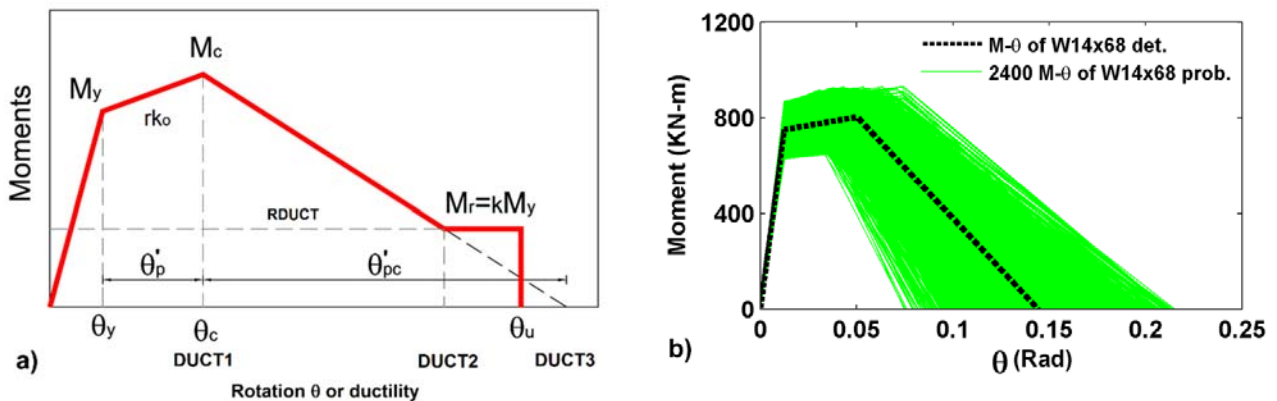


Figure 11 (a) Modified IMK model: monotonic curve; (b) an example of the modified IMK model used in the structural section (W14x68) of the probabilistic models.

The seismic action is also considered in a probabilistic way by using the set of 20 matched accelerograms developed in section 3.2 and their corresponding response spectra shown in Figure 12. It is important to note that the mean of the 20 response spectra represents correctly the target spectrum of the study area (Mexico City). Figure 12 also shows the fundamental period variation of the probabilistic models, T_{1SFM3} prob. For each of the probabilistic IDA, one of the 20 available records is randomly selected, using a uniform probability distribution.

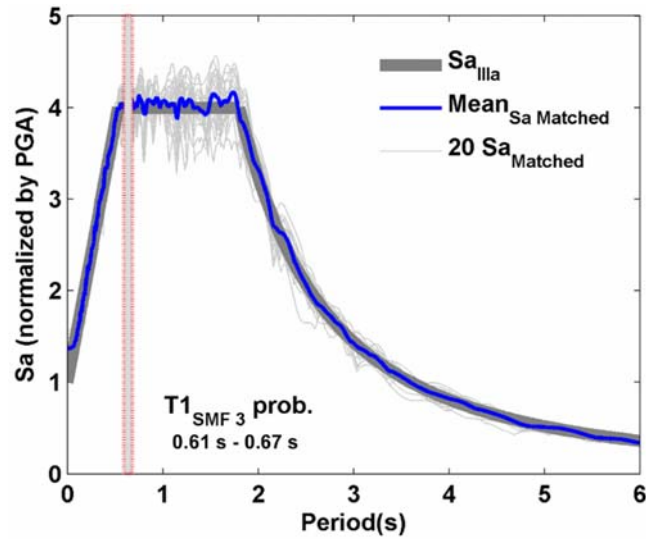


Figure 12 Response spectra of the 20 matched accelerograms and the mean spectrum. The fundamental periods of the probabilistic models are also depicted.

Figure 13a shows the probabilistic capacity curves obtained by using the procedure explained in section 3.3, and the curve representing the 50th percentile (median) of the curves. Figure 13b shows the corresponding ADE curves calculated from the capacity curves depicted in Figure 13a. Figure 14a shows the probabilistic $DI_{PAW}(\delta)$ and Figure 14b the probabilistic $DI_{PAW}(PGA)$, both obtained with IDA analysis, in accordance with the procedure explained in section 3.4; their respective 50th percentiles (medians) are also depicted.

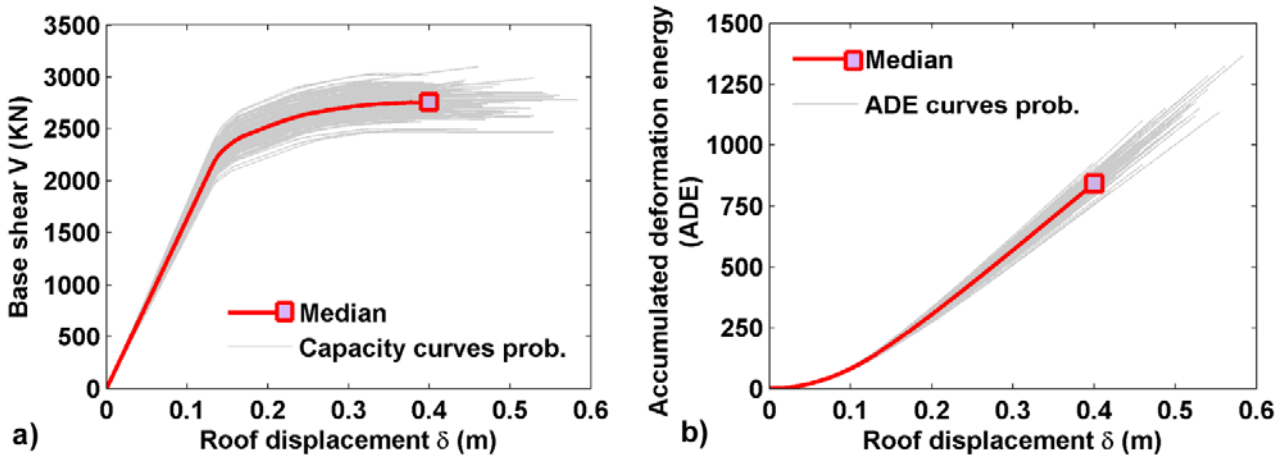


Figure 13 a) Probabilistic capacity curves and b) their respective ADE curves of the building.

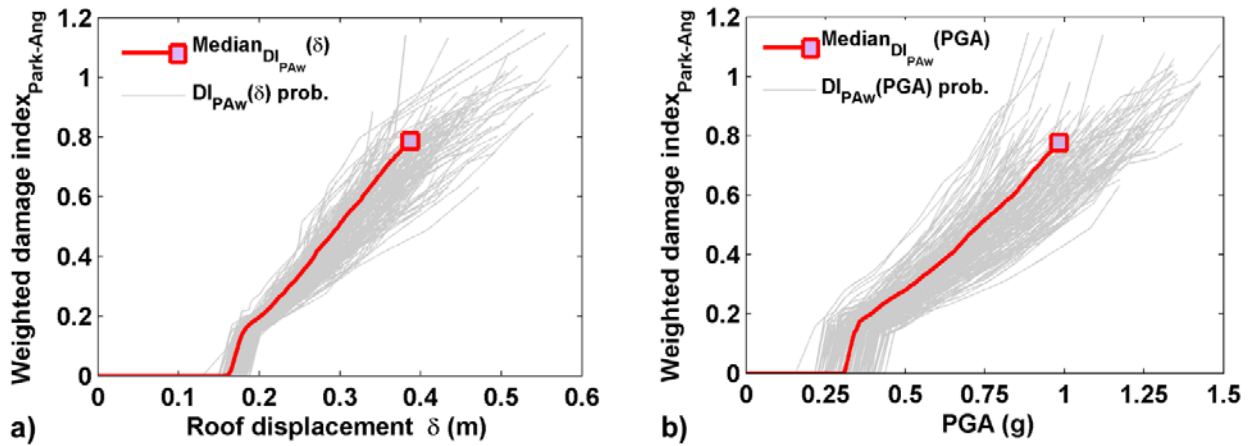


Figure 14 a) The $DI_{PAW}(\delta)$ probabilistic and b) the $DI_{PAW}(PGA)$ probabilistic.

The static displacement function of each probabilistic model are determined on the basis of the energy balance between their ADE curve and the response spectrum in EDRS format of the matched accelerogram that was used in the IDA in the same probabilistic model.

Afterwards, the energy capacity damage index, $DI_{EC}(\delta)$, is calculated and calibrated with the corresponding $DI_{PAW}(\delta)$. Figure 15a shows the obtained curves. In this figure, the $DI_{PAW}(\delta)$ curves calculated via IDA are shown together with the corresponding $DI_{EC}(\delta)$ curves. The median curves are also shown in Figure 15a. The median $DI_{EC}(\delta)$ curve shows a good fit to the median $DI_{PAW}(\delta)$ curve for a parameter $\eta=0.62$; so for probabilistic cases, it is obtained that the contribution to the $DI_{EC}(\delta)$ of the strain energy function, $E_{so}(\delta)_{NN}$, is 62%, while the contribution of the energy dissipated by hysteretic cycles, $E_D(\delta)_{NN}$, is 38%. The $DI_{EC}(\delta)$ can be well fitted to the $DI_{PAW}(\delta)$. Figure 15b shows the $DI_{PAW}(PGA)$ and the $DI_{EC}(PGA)$ probabilistic functions. Again, in all the cases, a very good agreement is obtained, especially in the median value. Therefore, the new damage index can be used also for establishing appropriately the expected damage in function of the intensity of the seismic action.

Finally, it is worth to mention that the parameter η is crucial in the energy damage index. Notice that each $DI_{PAW}(\delta)$ curve is obtained for a specific seismic action. It can be expected that different seismic actions lead to different Park and Ang index values and, therefore, to different values of the parameter η . Thus, the parameter η allows the new index, $DI_{EC}(\delta)$, fitting properly the response and the expected damage when the building is subjected to different seismic actions.

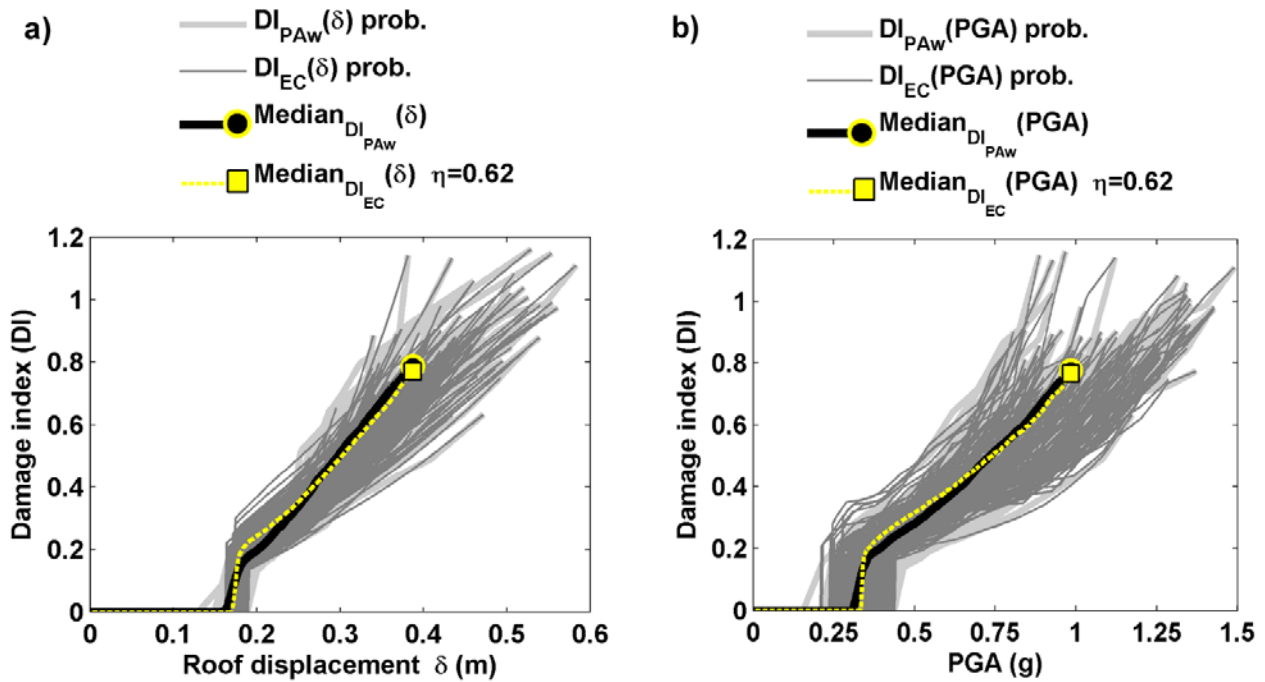


Figure 15 a) The $DI_{PAw}(\delta)$ and the $DI_{EC}(\delta)$ probabilistic, and b) the $DI_{PAw}(PGA)$ and the $DI_{EC}(PGA)$ probabilistic.

5 Conclusions

In this research a new damage index based on the capacity curve obtained by means of nonlinear static analysis has been developed. Two energy functions are defined. The former is the strain energy, $E_{so}(\delta)$, which is associated to the stiffness variation and to the ductility of the structure as well. The latter is the energy dissipated by damping, $E_D(\delta)$, which is related to the energy dissipated by hysteretic cycles. From a linear combination of these two energy functions by means of a parameter of contribution to damage η , the new damage index, $DI_{EC}(\delta)$, is defined. The parameter η is calibrated by using the well-known Park and Ang damage index, $DI_{PAw}(\delta)$, which is obtained from IDA. Both damage indices show a good agreement. The proposed index is not intended to be better than the Park and Ang index of the IDA, but if it represents a simple and easy technique to implement to quantify the damage based on the capacity curve and the performance point, which are faster methods than the IDA.

Concerning to the damage index for the buildings and the seismic actions studied in this research, in average, the Park and Ang damage index is well fitted by the combination of 62% of the $E_{so}(\delta)$ function and 38% of the $E_D(\delta)$ function.

It has been observed that the energy balance method applied incrementally provides very satisfactory results for determining the static displacement pattern in the studied building to the applied seismic actions. $DI_{EC}(\delta)$ can be expressed in terms of the increase of PGA, $DI_{EC}(PGA)$. The $DI_{EC}(PGA)$ exhibits the great advantage of providing a scenario of the expected damage based on the characteristics of the seismic action to which the building is subjected and also a good similarity with the damage scenario obtained with IDA.

It should be considered that the distribution parameter, η , depends on the characteristics of the seismic action; that is, it can be expected that different seismic actions lead to different $DI_{PAW}(\delta)$ and, therefore, to different values of the parameter η . For instance, a longer duration of the earthquake can lead to a greater contribution of the energy function linked to the hysteresis; what makes that the parameter η be higher, when fitting the $DI_{EC}(\delta)$. It would be interesting to evaluate the sensitivity of the parameter η for seismic actions with different response spectra and different earthquake durations. In addition, can be studying the relation of the parameter η with the type of frame mechanism for different buildings, which we consider can have an influence.

As discussed, the proposed index incorporates the characteristics of the seismic action and the structure through: 1) the displacements of the performance point for the seismic action applied and 2) by the calibration parameter η , that can have values between 0 to 1. In the first case, it will depend directly on the response spectrum used, and a seismic code spectrum of a site can be used, so that, no is necessary using an accelerogram. In the second case, this depends on the calibration with the Park y Ang index; in a probabilistic evaluation, a value that is considered adequate can be used based on the results presented here, or one deterministic case of the building can be calibrated for the different seismic actions will be using.

The most important contribution of this article is that the new damage index based on two energy functions can be obtained directly from the capacity curves in a straightforward way and that it provides adequate results for the assessment of the expected damage in buildings in function of the characteristics of the applied seismic action, such as for instance, the frequency content and duration. Therefore, it can be a useful tool to evaluate the seismic damage of buildings, especially in a probabilistic environment where the computational times can be significantly reduced.

6 Notation

The following symbols have used in this paper

A_c	=	area under the capacity curve;
acc	=	accelerograms;
$ADE(\delta)$	=	accumulated deformation energy of the capacity curve;
$b_f/(2 \cdot t_f)$	=	width/thickness ratio of the beam flange of W section;
COV	=	coefficient of variation of the probabilistic variables;
c^1_{unit} and c^2_{unit}	=	coefficients for units conversion in the modified IMK model;
D_{bi}, F_{bi}	=	coordinates of the ultimate capacity point of the bilinear curve;
D_{ci}, F_{ci}	=	coordinates of the ultimate capacity point of the capacity curve;
$DI_{EC}(\delta), DI_{EC}(\theta)$ or $DI_{EC}(PGA)$	=	energy capacity damage index in function of the roof displacement, rotation and PGA respectively;
$DI_{ePA}(\delta)$ or $DI_{ePA}(\theta)$	=	Park and Ang. damage index of a structural element;
$DI_{PAW}(\delta), DI_{PAW}(\theta)$ or $DI_{PAW}(PGA)$	=	Park and Ang. damage index of a building in function the roof displacement, rotation and PGA respectively;
$\int_0^{\delta} dE$	=	hysteretic energy absorbed by the element during the earthquake;
D_y, F_y	=	coordinates of the yield point of the bilinear curve;
E	=	modulus of elasticity;
$EDRS$	=	Energy Displacement Response Spectrum format;

E_D	=	energy dissipated by the structure in a single cycle of motion;
$E_D(\delta)$	=	energy dissipated function;
$E_D(\delta)_{NN}$, $E_D(\theta)_{NN}$ or $E_D(PGA)_{NN}$	=	normalized energy dissipated in function of the roof displacement, rotation and PGA respectively;
E_{so}	=	maximum strain energy associated to a cycle of motion;
$E_{so}(\delta)$	=	strain energy function;
$E_{so}(\delta)_{NN}$, $E_{so}(\theta)_{NN}$ or $E_{so}(PGA)_{NN}$	=	normalized strain energy in function of the roof displacement, rotation and PGA respectively;
E_y	=	the yielding energy;
$F(\delta)$	=	capacity curve;
FR	=	connections type fully restrained;
f_y	=	expected yield strength;
h/t_w	=	ratio between the web depth and the thickness of W section;
i	=	structural element i ;
I	=	inertia moment of W section;
IDA	=	incremental dynamic analysis;
IMK	=	modified Ibarra–Medina–Krawinkler model;
j	=	each increment in the displacement of the capacity curve;
k	=	residual moment constant;
K_i	=	initial slope of the capacity curve;
k_o	=	initial elastic stiffness;
L/d	=	the ratio between the span and the depth of the beam or column;
LHS	=	Latin Hypercube Sampling;
M	=	bending moment in the structural element;
M_c	=	capping moment strength or post-yield strength ratio;
M_r	=	residual moment;
M_w	=	moment magnitude scale;
M_y	=	effective yield moment;
M^*	=	effective modal mass for the first mode of vibration of the building;
N	=	number of the damaged structural elements in the building;
n	=	ultimate increment in the displacement of the capacity curve;
NLDA	=	nonlinear dynamic analysis;
NLSA	=	nonlinear static analysis;
PA	=	Park and Ang. damage index
P_{ad}	=	adaptive pushover analysis;
PF_1	=	modal participation factor;
PGA	=	peak ground acceleration;
Q_u	=	strength corresponding to the ultimate displacement;
Q_y	=	strength at the yielding point;
R_y	=	strength reduction factor;
S_a	=	acceleration spectrum;
S_{aEDRS}	=	input energy spectrum;
$S_{a_{matched}}$	=	acceleration spectrum of the matched accelerogram;
$S_{d_{pp}}$	=	displacement of the performance point;
S_{d_y}	=	yielding spectral displacement;
SMF	=	special moment frame building;
S_v	=	pseudo-velocity spectrum;
T	=	period;
T_a , T_b and T_c	=	limits period used to define the $R_y-\mu_s-T$ relationship;
T_1	=	fundamental period of the building;
$T_1^{SFMS3\ prob}$	=	the fundamental period of the probabilistic models SMF 3;
V	=	base shear;
V_y	=	base shear in the yielding energy;
Z	=	plastic modulus;
β	=	strength deteriorating parameter in Park and Ang. damage index;

β^*	=	parameter of the R_y in function of the T_a , T_b and T_c ;
γ_E	=	energy factor;
δ	=	roof displacement in the structure;
δ_{Dy}	=	displacement in the yield point of the bilinear curve;
δ_u	=	ultimate roof displacement in the structure;
δ_y	=	roof displacement in the yielding energy;
η	=	calibration parameter in the energy capacity damage index;
θ	=	rotation in the structural element;
θ_p	=	pre-capping plastic rotation for monotonic loading;
θ_{pc}	=	post-capping plastic rotation;
θ_u	=	ultimate rotation capacity;
θ_y	=	yield rotation;
λ_i	=	ratio of the energy dissipated by hysteresis in the element i to the total hysteretic energy dissipated in the entire building.
μ	=	mean value of the probabilistic variables;
μ_E	=	energy ductility;
μ_{PP}	=	ductility of the performance point;
μ_s	=	ductility factor;
ξ_{eq}	=	equivalent viscous damping;
σ	=	standard deviation of the probabilistic variables;
σ_{In}	=	standard deviation, assuming a lognormal fit of experimental data in θ_p and θ_{pc} in the modified IMK model;
ω	=	tangent fundamental natural frequency in the modified Rayleigh method.

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