# Gibbs' energy of formation of $YBa_2Cu_3O_{7-x}$ (tetragonal)

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Abstract. The high temperature ceramic oxide superconductor  $YBa_2Cu_3O_{7-x}$  (1-2-3 compound) is generally synthesized in an oxygen-rich environment. Hence any method for determining its thermodynamic stability should operate at a high oxygen partial pressure. A solid-state cell incorporating CaF<sub>2</sub> as the electrolyte and functioning under pure oxygen at a pressure of  $1.01 \times 10^5$  Pa has been employed for the determination of the Gibbs' energy of formation of the 1-2-3 compound. The configuration of the galvanic cell can be represented by:

Pt, O<sub>2</sub>, YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-x</sub>, Y<sub>2</sub>BaCuO<sub>5</sub>, CuO, BaF<sub>2</sub>/CaF<sub>2</sub>/BaF<sub>2</sub>, BaZrO<sub>3</sub>, ZrO<sub>2</sub>, O<sub>2</sub>, Pt.

Using the values of the standard Gibbs' energy of formation of the compounds  $BaZrO_3$  and  $Y_2BaCuO_5$  from the literature, the Gibbs' energy of formation of the 1–2–3 compound from the constituent binary oxides has been computed at different temperatures. The value of x at each temperature is determined by the oxygen partial pressure. At 1023 K for O content of 6.5 the Gibbs' energy of formation of the 1–2–3 compound is  $-261.7 \text{ kJ mol}^{-1}$ .

Keywords. Gibbs' energy; oxygen partial pressure; free energy; stability.

#### 1. Introduction

The high temperature ceramic superconductor  $YBa_2Cu_3O_{7-x}$  (1-2-3 compound) is generally synthesized in an oxygen-rich environment. Hence any method of determining its thermodynamic stability should operate at a high oxygen partial pressure. Kale and Jacob (1989a) and Azad *et al* (1991) have demonstrated the application of fluorine concentration cells for the determination of standard Gibbs' energy mixed oxides in the system YO<sub>1.5</sub>-BaO-CuO, under pure oxygen at a pressure of 1.01 × 10<sup>5</sup> Pa. This paper reports the determination of the standard Gibbs' energy of formation of 1-2-3 compound (from the constituent binary oxides) over the range 993 to 1179 K, using a solid-state galvanic cell incorporating single-crystal CaF<sub>2</sub> as the electrolyte.

#### 2. Experimental

The YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-x</sub> compound used in this investigation was prepared by citrate combustion and subsequent oxygen annealing as described elsewhere (Pankajavalli *et al* 1988). The superconducting oxide was characterized by XRD,  $T_c$  and magnetic susceptibility measurements. It was found to be a pure single-phase material, with a sharp  $T_c$  of 92 K, having a half width less than 2 K. The oxygen content was found to be 6.93 by iodometry, employing NaCuO<sub>2</sub> as the standard (Janaki 1988). The compounds

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 $Y_2BaCuO_5$  and  $BaZrO_3$  were prepared by the standard solid-state reaction route and characterized by XRD (Azad *et al* 1989). The 1–2–3 compound,  $Y_2BaCuO_5$ , CuO and  $BaF_2$  were mixed in equal weight ratio and compacted at a pressure of 100 MPa into a cylindrical pellet of 10 mm diameter and 2–3 mm thickness. The pellet was used as an electrode. The reference electrode was made from a mixture of  $BaZrO_3$ ,  $ZrO_2$  and  $BaF_2$ taken in the weight ratio 1:1:1. The mixture was then compacted into a cylindrical pellet. Cylindrical discs of single crystal  $CaF_2$  of 10 mm diameter and 3 mm thickness (Harshaw Chemical Co., USA) served as the electrolyte.

An open-cell stacked-pellet assembly was used for emf measurements. The cell assembly was held in the constant temperature zone of the furnace. A calibrated Pt-10% Rh/Pt thermocouple, located in the vicinity of the stacked pellet assembly, was used to monitor the cell temperature. High purity oxygen (IOL, India, better than 99·99%), flowing at a rate of  $\sim 1 \text{ dm}^3 \text{ h}^{-1}$  and a pressure of  $1.01 \times 10^5$  Pa was used as the gas atmosphere over the cell. The oxygen was passed through drierite (anhydrous CaCl<sub>2</sub>) traps for the removal of moisture prior to use in the cell. The other experimental details were identical to those reported earlier (Azad and Sreedharan 1987; Azad *et al* 1987, 1989). The following cell configuration was employed in the present study:

$$Pt, O_2, YBa_2Cu_3O_{7-x}, Y_2BaCuO_5, CuO, BaF_2/CaF_2/BaF_2, BaZrO_3, ZrO_2, O_2, Pt.$$

# 3. Results

The emf of cell I is shown in figure 1 for temperatures ranging from 993 to 1179 K. The least-square regression analysis gives the expression:

$$E(\pm 0.5)/mV = 93.8 - 0.02468 T/K.$$
 (1)

The cell voltages were measured over a much wider range (770 to 1180 K). The voltages above 1180 K were irreproducible, while those below 990 K exhibited an unacceptably large temperature dependence, presumably due to the non-attainment of equilibrium. The reproducibility of the emf was verified by thermal cycling and microcoulometric titration.



Figure 1. Temperature dependence of the emf of cell I.

## 4. Discussion

The half-cell reactions corresponding to cell I can be written as:

$$3 \operatorname{ZrO}_{2} + 3 \operatorname{BaF}_{2} + 3/2 \operatorname{O}_{2} + 6e^{-} \longrightarrow 3 \operatorname{BaZrO}_{3} + 6F^{-}$$
(2a)  
$$2 \operatorname{YBa}_{2}\operatorname{Cu}_{3}\operatorname{O}_{7-x} + 6F^{-} \longrightarrow \operatorname{Y}_{2}\operatorname{BaCuO}_{5} + 5\operatorname{CuO} + 3\operatorname{BaF}_{2} + (2-x)\operatorname{O}_{2} + 6e^{-}.$$
(2b)

The overall virtual cell reaction is:

$$2 \operatorname{YBa}_{2}\operatorname{Cu}_{3}\operatorname{O}_{7-x} + 3 \operatorname{ZrO}_{2} \longrightarrow \operatorname{Y}_{2}\operatorname{Ba}\operatorname{CuO}_{5} + 3 \operatorname{Ba}\operatorname{ZrO}_{3} + 5 \operatorname{CuO} + (0.5 - x)\operatorname{O}_{2}.$$
(2c)

The standard Gibbs' energy change  $(\Delta G_R^{\circ})$  for the virtual cell reaction, calculated from the emf, is given by:

$$\Delta G_{R(2)}^{\circ}(\pm 0.3)/\mathrm{kJ} = -54.3 + 0.01429\,\mathrm{T/K}.$$
(3)

This is related to the standard Gibbs' energies of formation of various compounds in (2) by the expression:

$$\Delta G^{\circ}_{R(2)} = \Delta G^{\circ}_{f}(Y_{2}BaCuO_{5}) + 3\Delta G^{\circ}_{f}(BaZrO_{3}) + 5\Delta G^{\circ}_{f}(CuO) - 3\Delta G^{\circ}_{f}(ZrO_{2}) - 2\Delta G^{\circ}_{f}(YBa_{2}Cu_{3}O_{7-x}).$$
(4)

The standard Gibbs' energy of formation of the ternary or quarternary oxides from the constituent binary oxides in their respective standard states may be represented by  $\Delta G_{f,ox}^{\circ}$ . In the case of the nonstoichiometric 1–2–3 compound, this can be done only at a temperature where O content is 6.5. Thus when the nonstoichiometric parameter x has a value of 0.5, (4) can be rewritten as:

$$\Delta G_{R(2)}^{\circ} = \Delta G_{f,ox}^{\circ} (\mathbf{Y}_2 \mathbf{BaCuO}_5) + 3 \Delta G_{f,ox}^{\circ} (\mathbf{BaZrO}_3) - 2 \Delta G_{f,ox}^{\circ} (\mathbf{YBa}_2 \mathbf{Cu}_3 \mathbf{O}_{6\cdot 5}).$$
(5)

Levitskii (1978) has determined the  $\Delta G_{f.ox}^{\circ}$  for BaZrO<sub>3</sub> by using a similar galvanic cell with CaF<sub>2</sub> as the electrolyte:

$$\Delta G_{f, \text{ ox}}^{\circ} / \text{kJ mol}^{-1} = (-134.3 \pm 6.7) - (2.1 \pm 4.6) \times 10^{-3} \text{ T/K}.$$
 (6)

Azad *et al* (1991) recently reported values for  $\Delta G_{f,ox}^{\circ}$  of Y<sub>2</sub>BaCuO<sub>5</sub> over the range 853 to 1066 K:

$$\Delta G_{f,ox}^{\circ}(\pm 0.7)/\text{kJ}\,\text{mol}^{-1} = -72.5 - 0.0793\,\text{T/K}.$$
(7)

Rearrangement of (5) yields:

$$\Delta G_{f,ox}^{\circ}(\mathbf{YBa}_{2}\mathbf{Cu}_{3}\mathbf{O}_{6\cdot 5}) = 0.5[\Delta G_{f,ox}^{\circ}(\mathbf{Y}_{2}\mathbf{Ba}\mathbf{Cu}\mathbf{O}_{5}) + 3\Delta G_{f,ox}^{\circ}(\mathbf{Ba}\mathbf{ZrO}_{3}) - \Delta G_{\mathbf{R}(2)}^{\circ}].$$
(8)

A general expression for the standard Gibbs' energy of formation of the 1-2-3 compound from the constituent binary oxides and gaseous oxygen, in the temperature range 993 to 1179 K can be written as:

$$\Delta G_{f}^{\circ}(YBa_{2}Cu_{3}O_{7-x})/kJ \,\text{mol}^{-1} = -210.6 - 0.04993 \,\text{T/K}.$$
(9)

The experimentally measured values of  $\Delta G_f^{\circ}$  of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-x</sub>, at O<sub>7-x</sub>, different temperatures and the corresponding values of x are shown in table 1. Since the

T(K)	E(mV)	xª	$\Delta G_f^{\circ}(YBa_2Cu_3O_{7-x})/kJ mol^{-1}$
993.4	68.9	0.451	260-2
1034.0	68·3	0.508	-262.2
1053.0	67·5	0.532	-263-2
1080-9	67·0	0.566	-264-6
1104.9	65.9	0.592	-265.8
1167.0	65-0	0.656	-268-9
1179-3	64.6	0.667	-269.5

**Table 1.** Standard Gibbs' energy of formation of  $YBa_2Cu_3O_{7-x}$  as a function of temperature and nonstoichiometry.

"derived from the work of Kishio et al (1989)

value of x varies with temperature, the temperature-independent term in (9) cannot be identified as the enthalpy of formation.

It is well known that the 1-2-3 compound exhibits an orthorhombic-to-tetragonal transition at high temperature which is dependent on the partial pressure of oxygen. Typically a value of 6.5 has been found to be the upper limit of O/M (x = 0.5) for the orthorhombic-to-tetragonal phase transition in pure oxygen at a pressure of 1.01  $\times 10^5$  Pa (Schuller et al 1987; Murphey et al 1987). Many investigators (Gallagher 1987; Blinovskov et al 1988; Swaminathan et al 1988; Musbah and Chang 1989; O'Bryan et al 1989; Kishio et al 1989) have studied the dependence of the O/M ratio in the 1-2-3 compound on temperature and partial pressure of oxygen. Unfortunately there is very poor consistency among these measurements, either because the solid samples were not single phase or because equilibrium conditions were difficult to reach at low  $p_{0_2}$  and moderate temperatures. From the x- $p_{0_2}$  relation reported by Kishio et al (1989), it is seen that in the temperature range of the present investigation, the 1-2-3phase would exist mainly in the tetragonal modification. Thus combining (6) and (7) with (3), the  $\Delta G_{f,ox}^{\circ}$  of YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6.5</sub> at 1023 K was calculated to be  $-261.7 \text{ kJ mol}^{-1}$ . This result can be combined with the data on the variation of oxygen partial pressure with nonstoichiometric parameter x to calculate the Gibbs' energies of formation at other compositions as a function of temperature. Morss et al (1988) determined the standard enthalpy of formation of  $YBa_2Cu_3O_{\nu}$  (y = 6.25, 6.47, 6.69 and 6.93) at 298.15 K by solution calorimetry. They have reported a value of  $-143 \text{ kJ mol}^{-1}$  at 298.15 K for  $\Delta H_{f,ox}^{\circ}$  (YBa<sub>2</sub>Cu<sub>3</sub>O<sub>6.5</sub>). On the other hand, Tretyakov and Graboy (1990), from their emf studies envisaged that the 1-2-3 compound is unstable and decomposes to BaCuO<sub>2</sub>, Y<sub>2</sub>BaCuO<sub>5</sub> and CuO at temperatures below 973 K. This observation contradicts the large enthalpy of formation reported by Morss et al (1988) and the Gibbs' energy of formation obtained in the present investigation.

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