Generation of a superposition of multiple mesoscopic states of radiation in a resonant cavity

P. K. Pathak * and G. S. Agarwal *

Department of Physics, Oklahoma State University, Stillwater, OK-74078 (Dated: February 1, 2008)

Using resonant interaction between atoms and the field in a high quality cavity, we show how to generate a superposition of many mesoscopic states of the field. We study the quasi-probability distributions and demonstrate the nonclassicality of the superposition in terms of the zeroes of the Q-function as well as the negativity of the Wigner function. We discuss the decoherence of the generated superposition state. We propose homodyne techniques of the type developed by Auffeves et al [Phys. Rev. Lett. 91, 230405 (2003)] to monitor the superposition of many mesoscopic states.

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I. INTRODUCTION

The interaction of a single atom with a high quality cavity has vielded many important results which can be understood in terms of the Javnes-Cummings model [1]. The advances in this field are extensively reviewed in the literature [2, 3, 4, 5]. The generation of a superposition of mesoscopic coherent states has a fundamental place in quantum theory as such a state exhibits quantum interferences and the nonclassical character of the radiation field [6, 7]. Eiselt and Risken [8] had discovered that if a cavity contains a coherent field with large photon numbers, say of the order of 10, then the state of the field for certain times splits into two parts. Each part can be characterized approximately by a coherent state. Several authors have studied many aspects of such splittings [9, 10]. Auffeves et al [10] made a successful observation of this splitting. They also devised a novel homodyne method to observe interferences. We note that previously such superpositions were produced using dispersive interactions in a high quality cavity [11, 12] or by using Raman transitions between the center of mass degrees of freedom of trapped ions [13].

Earlier studies of the superpositions of more than two coherent states have found many novel features of such states. For example, Zurek [14] noticed that such superpositions lead to structures in phase space which are smaller than Planck's constant. Clearly, we need efficient methods to produce such superpositions. One of the early suggestions [15] for the production of such states was through the passage of a field in a coherent state through a Kerr medium. However Kerr nonlinearities are usually too small. Another possibility is via the dispersive interaction [12, 16] in the cavity. In this paper we present yet another possibility by using the resonant interaction between the atom and the cavity. We show how successive passage of atoms can be used to produce superpositions involving many coherent states. We specifically concentrate on a superposition of four coherent states.

The organization of the paper is as follows. In Sec II we present the details of our proposal to produce a superposition of four coherent states. We examines the Wigner function and the Q-function for such states. We present a comparison of exact and approximate phase space distribution functions. We further study zeroes of the Q-function which are a signature of the nonclassical properties of the field. In Sec. III we show how the passage of the third atom can be used to monitor the superposition of four coherent states. In Sec.IV we examine the scale over which such a superposition can decohere.

II. PREPARATION OF A SUPERPOSITION OF FOUR MESOSCOPIC STATES OF THE FIELD

In a recent experiment, Auffeves *et al* [10] have observed a superposition of two distinguishable states of the field in a high quality cavity using resonant interaction between an atom and the field inside the cavity. This observation is in agreement with the theoretical prediction of Eiselt and Risken [8]. When a two level Rydberg atom interacts with a microwave field, it splits the field into two parts whose phases move in opposite directions. If the interaction time is chosen such that the phase difference between the split parts becomes π , then the cavity field can be projected into a superposition similar to a cat state, $|\alpha\rangle + |-\alpha\rangle$.

In this section, we show that the above method can be used for the preparation of a superposition of four mesoscopic states of the field. We consider a two level Rydberg atom having its higher energy state $|e\rangle$ and lower energy state $|g\rangle$ and the cavity has a strong coherent field $|\alpha\rangle$. The atom passes through the cavity and interacts resonantly with the field. The Hamiltonian for the system in the interaction picture is written as

$$H = \hbar g \left(|e\rangle \langle g|a + a^{\dagger}|g\rangle \langle e| \right), \tag{1}$$

where g is the coupling constant for the atom with the cavity field, and $a(a^{\dagger})$ is the annihilation (creation) op-

^{*}On leave: Physical Research Laboratory, Navrangpura, Ahmedabad-380 009, India

erator. The state of the atom-cavity system is written as

$$|\psi(t)\rangle = \sum_{n} \left(c_{en}(t) | e, n \rangle + c_{gn}(t) | g, n \rangle \right).$$
 (2)

Using Hamiltonian (1), the Schrödinger equation in terms of c_{en} and c_{qn} is

$$\dot{c}_{en-1} = -ig\sqrt{n}c_{gn},\tag{3}$$

$$\dot{c}_{gn} = -ig\sqrt{n}c_{en-1}.\tag{4}$$

We assume that the atom enters the cavity in its lower state $|g\rangle$ and after interacting with the field for time t_1 , it is detected in the same state $|g\rangle$. Thus, effectively, the atom absorbs no photon but it projects the cavity field into the state

$$|\psi_c\rangle = \sum_n c_n \cos(g\sqrt{n}t_1)|n\rangle,$$
 (5)

$$= \frac{1}{2} \sum_{n} c_n e^{ig\sqrt{n}t_1} |n\rangle + c_n e^{-ig\sqrt{n}t_1} |n\rangle, \quad (6)$$
$$c_n = \frac{\alpha^n}{\sqrt{n!}} e^{-|\alpha|^2/2}.$$

As a result the cavity field splits into two parts whose phases move in directions opposite to each other. Now we consider the passage of a second identical atom through the cavity. The second atom enters the cavity in its lower state $|g\rangle$ and after interacting with the field for time t_2 , is detected in the same state $|g\rangle$. The state of the field inside the cavity after passing the second atom is

$$\begin{aligned} |\psi_{c}'\rangle &= \sum_{n} c_{n} \cos(g\sqrt{n}t_{1}) \cos(g\sqrt{n}t_{2})|n\rangle, \quad (7) \\ &= \frac{1}{4} \sum_{n} c_{n} e^{ig\sqrt{n}(t_{1}+t_{2})}|n\rangle + c_{n} e^{-ig\sqrt{n}(t_{1}+t_{2})}|n\rangle \\ &+ c_{n} e^{ig\sqrt{n}(t_{1}-t_{2})}|n\rangle + c_{n} e^{-ig\sqrt{n}(t_{1}-t_{2})}|n\rangle. \quad (8) \end{aligned}$$

Thus after passing second atom, the state of the field inside the cavity splits into four parts.

In the coherent state $|\alpha\rangle$, the photon distribution follows Poisson statistics, so in Eq.(8), most of the contribution to the summation comes from the terms $n \approx |\alpha|^2$. Thus we can expand \sqrt{n} in phase terms around the average number of photons $\bar{n} = |\alpha|^2$ in Eq.(8). In fact for $\bar{n} \sim 10$, only the terms up to second order in $(n - \bar{n})$ are significant and other terms are negligible.

$$\sqrt{n} = \sqrt{\bar{n}} + \frac{n - \bar{n}}{2\sqrt{\bar{n}}} - \frac{(n - \bar{n})^2}{8\bar{n}^{3/2}}.$$
(9)

If we substitute the value of \sqrt{n} from Eq.(9) in Eq.(8), the term proportional to n will change the phase of the coherent field while the second and higher order terms in $(n - \bar{n})$ will distort the shape of the coherent state in phase space. For simplification, in order to understand the nature of the generated superposition state, we do not consider the distortion in the coherent state. Then Eq.(8) can be approximated by

$$\begin{aligned} |\psi_{c}'\rangle &= \frac{1}{4} \left[e^{i(\eta_{1}+\eta_{2})} |\alpha e^{i(\theta_{1}+\theta_{2})}\rangle + e^{-i(\eta_{1}+\eta_{2})} |\alpha e^{-i(\theta_{1}+\theta_{2})}\rangle + e^{i(\eta_{1}-\eta_{2})} |\alpha e^{i(\theta_{1}-\theta_{2})}\rangle + e^{-i(\eta_{1}-\eta_{2})} |\alpha e^{-i(\theta_{1}-\theta_{2})}\rangle \right] (10) \\ &= at_{i}\sqrt{\bar{n}} \qquad at_{i} \end{aligned}$$

$$\eta_i = \frac{gt_i\sqrt{n}}{2}, \ \theta_i = \frac{gt_i}{2\sqrt{\bar{n}}}, \ i = 1, 2$$
(11)

If we choose interaction times t_1 and t_2 such that $\theta_1 = \pi/2$ and $\theta_2 = \pi/4$, we get the superposition of four mesoscopic coherent states placed in the east, west, north and south directions in phase space.

$$|\psi_{c}'\rangle = \frac{1}{4} \left[e^{-i(\eta_{1} - \eta_{2})} |\alpha'\rangle + e^{i(\eta_{1} + \eta_{2})} |-\alpha'\rangle + e^{i(\eta_{1} - \eta_{2})} |i\alpha'\rangle + e^{-i(\eta_{1} + \eta_{2})} |-i\alpha'\rangle \right]; \qquad (12)$$

where we set $\alpha = \alpha' e^{i\pi/4}$.

Now we calculate the Wigner distribution for the state (7). The Wigner distribution for the state having density matrix ρ can be obtained using coherent states as [17]

$$W(\gamma) = \frac{2}{\pi^2} e^{2|\gamma|^2} \int \langle -\beta |\rho|\beta \rangle e^{-2(\beta\gamma^* - \beta^*\gamma)} d^2\beta.$$
(13)

The density matrix ρ_c for state (7) in terms of number states is

$$\rho_c = \sum_{n,m} \frac{\alpha^n \alpha^{*m}}{\sqrt{n!m!}} e^{-|\alpha|^2} \cos(gt_1\sqrt{n}) \cos(gt_2\sqrt{n})$$
$$\cos(gt_1\sqrt{m}) \cos(gt_2\sqrt{m})|n\rangle\langle m|.$$
(14)

Using equations (13) and (14), the Wigner distribution for the state (7) is

$$W(\gamma) = \frac{2e^{2|\gamma|^2}}{\pi^2} \sum_{n,m} \frac{\alpha^n \alpha^{*m}}{n!m!} e^{-|\alpha|^2} \cos(gt_1\sqrt{n})$$
$$\cos(gt_2\sqrt{n}) \cos(gt_1\sqrt{m}) \cos(gt_2\sqrt{m})$$
$$\int (-\beta^*)^n \beta^m e^{-|\beta|^2} \exp[-2(\beta\gamma^* - \beta^*\gamma)] d^2\beta.$$
(15)

After evaluating the integral, Eq.(15) is simplified to the form

$$W(\gamma) = \frac{2e^{2|\gamma|^2}}{\pi} \sum_{n,m} \frac{(-1)^{n+m} \alpha^n \alpha^{*m}}{2^{n+m} n! m!} e^{-|\alpha|^2} \cos(gt_1 \sqrt{n})$$
$$\cos(gt_2 \sqrt{n}) \cos(gt_1 \sqrt{m}) \cos(gt_2 \sqrt{m}) \frac{\partial^{n+m}}{\partial \gamma^n \partial \gamma^{*m}} e^{-4|\gamma|^2} 6)$$

In the Fig.1 we show the Wigner distributions for the generated superposition state (8) as well as for the approximated state (10) using some typical values of parameters. There are four patches at the corners corresponding to four mesoscopic states of the field and between each pair of states of the field there are interference fringes indicating the coherence between the states. In the central part there are subplanck structures as noticed by Zurek [14] which form as a result of quantum interference between the two diagonal pairs. The comparison of Fig.1 (a) and (b) shows that a significant squeezing perpendicular to the arc of the circle $|z| = |\alpha|$ occurs due to the effects of the higher order terms in $(n-\bar{n})$ (see Eq. (9)). Squeezing in the resonant Jaynes-Cummings model [18] has been studied very well earlier. As a result of small differences in the field statistics, there are differences in the interference patterns. In Fig.2, the Q-distributions for the states (7) and (10) are shown with the same parameters used in Fig.1. We select the interaction times such that there is no overlapping between two states of the field. A comparison of Fig.2 (a) and (b) shows that the states of the field corresponding to the phases $\pm q\sqrt{n}(t_1+t_2)$ [see (8)] in the generated mesoscopic state have more spread along the circle $|z| = |\alpha|$ and squeezing perpendicular to it in phase space because of larger distortion terms. Thus the split states of the field in the generated superposition state are situated at the same position as in the

We further mention that after passing N atoms through the cavity and properly selecting the interaction times we can generate the superposition of 2^N mesoscopic states of the field placed along the arc of a circle of radius $|\alpha|$ in phase space. In Fig.3 we show the Q-distribution for the generated state of the field after passing three atoms through the cavity. It is clear that the generated state is a coherent superposition of eight mesoscopic states.

approximated state but with changed shape.

The relation between the Q-distribution and the Pdistribution for a state is given by

$$Q(\gamma) = \int P(\alpha) e^{-|\alpha-\gamma|^2} d^2 \alpha.$$
 (17)

From Eq. (17), it is clear that for Q = 0 the Pdistribution will oscillate between +ve and -ve values. The negative value of P is a signature of the nonclassical nature of the state. Thus the exact zeros of the Q-distribution are also signatures of nonclassical nature. Here it will be interesting to analyze the exact zeros of the Q-distribution of the approximated state (12). The Q-distribution for state (12) is

$$Q(\gamma) = \frac{1}{\pi} \left| \langle \gamma | \alpha' \rangle e^{-i(\eta_1 - \eta_2)} + \langle \gamma | - \alpha' \rangle e^{i(\eta_1 + \eta_2)} \right. \\ \left. + \langle \gamma | i \alpha' \rangle e^{i(\eta_1 - \eta_2)} + \langle \gamma | - i \alpha' \rangle e^{-i(\eta_1 + \eta_2)} \right|^2.$$
(18)

The exact zeros of $Q(\gamma)$ will be given by

$$\left| \langle \gamma | \alpha' \rangle e^{-i(\eta_1 - \eta_2)} + \langle \gamma | - \alpha' \rangle e^{i(\eta_1 + \eta_2)} + \langle \gamma | i\alpha' \rangle e^{i(\eta_1 - \eta_2)} + \langle \gamma | - i\alpha' \rangle e^{-i(\eta_1 + \eta_2)} \right| = 0.$$
(19)

Thus the Q-distribution shows nonclassical behavior at all phase points γ satisfying the condition (19). For example if we take α' to be real and observe the Q-distribution along the line $\gamma = |\gamma| e^{i\pi/4}$ in phase space,

the condition for nonclassicality (19) simplifies to

$$e^{-\frac{|\gamma|\alpha'}{\sqrt{2}}}\cos\left[\eta_1 + \eta_2 + \frac{|\gamma|\alpha'}{\sqrt{2}}\right] + e^{\frac{|\gamma|\alpha'}{\sqrt{2}}}\cos\left[\eta_1 - \eta_2 + \frac{|\gamma|\alpha'}{\sqrt{2}}\right] = 0.$$
(20)

Now using the values of $\eta_1 = \pi |\alpha'|^2/2$, $\eta_2 = \pi |\alpha'|^2/4$ (see Eq.(11)), the condition (20) can be rewritten as the simultaneous equations

$$\frac{|\gamma|}{\sqrt{2}\alpha'} + \frac{3\pi}{4} = (2n_1 + 1)\frac{\pi}{2\alpha'^2},$$
$$\frac{|\gamma|}{\sqrt{2}\alpha'} + \frac{\pi}{4} = (2n_2 + 1)\frac{\pi}{2\alpha'^2}; \quad n_i = 1, 2, \dots \quad (21)$$

The solution of the equations (21) gives $\alpha'^2 = 2(n_1 - n_2)$ thus α'^2 must be an even integer and the values of $|\gamma|$ are given by

$$|\gamma| = \frac{\pi}{2\sqrt{(n_1 - n_2)}} (3n_2 - n_1 + 1); \quad n_1 > n_2.$$
 (22)

III. DETECTION OF THE GENERATED SUPERPOSITION OF MESOSCOPIC STATES OF THE FIELD

In the previous section, we have shown how the cavity field can be projected into a superposition of 2^N mesoscopic states of the field after passing N atoms through the cavity. The generated state in the cavity can be detected by the conditional probabilities of detection of the atoms used in the preparation itself as the cavity field is entangled with the atomic states. An elegant method can also be homodyne detection [10] which can be implemented in the same experimental set up. After preparing the cavity in the desired superposition state, a resonant external coherent field $|\beta\rangle$ is injected into the cavity. For the sake of simplicity let us assume that two atoms are passed through the cavity in the preparation of the mesoscopic state of the field (Eq.(7)). After adding the external field, the state of the resultant field in the cavity is

$$C_{h}\rangle = \sum_{n} c_{n} \cos(gt_{1}\sqrt{n}) \cos(gt_{2}\sqrt{n})D(\beta)|n\rangle,$$

$$= \sum_{m} \sum_{n} c_{n} \cos(gt_{1}\sqrt{n}) \cos(gt_{2}\sqrt{n})\langle m|D(\beta)|n\rangle|m\rangle,$$

$$= \sum_{m} F_{m}|m\rangle$$
(23)

$$F_m = \sum_{n=1}^{m} c_n \cos(gt_1\sqrt{n}) \cos(gt_2\sqrt{n}) \langle m|D(\beta)|n\rangle, \quad (24)$$

where $D(\beta) \equiv e^{\beta a^{\dagger} - \beta^* a}$ is displacement operator. Now we bring the third atom in its lower energy state $|g\rangle$ to probe the cavity field. The probability of detecting the FIG. 1: (Color online) The Wigner distributions $W(\gamma)$ for (a) the generated state (8) and (b) the approximated state (10), using parameters $\alpha = 4$, $gt_1 = 3.7\pi$, $gt_2 = 1.9\pi$.

FIG. 2: (Color online) The Q-distribution function $Q(\gamma)$ for (a) the generated state (8) and (b) the approximated state (10), using same parameters as in Fig.1.

probe atom in its lower state $|g\rangle$ after crossing the cavity in time t_p is

$$P_g = \sum_m |F_m|^2 \cos^2(gt_p\sqrt{m}).$$
⁽²⁵⁾

The interaction time t_p for the probe atom is selected such that if there are photons in the cavity it leaves the cavity in its higher energy state $|e\rangle$ with larger probability. We have shown in the earlier section that all the states of the field in the superposition lie on a circle of radius $|\alpha|$ so if we choose the external field $|\beta\rangle$ having amplitude $|\alpha|$ and phase ϕ , the probe atom will leave the cavity in its ground state with larger probability when the value of $\pi + \phi$ will match to the phases of the states of the field in the generated superposition. Thus the probability of the probe atom leaving the cavity in its lower state $|g\rangle$ would, as a function of ϕ , have peaks corresponding to the positions of the centers of the superposed mesoscopic states. In Fig.4, we plot the probability of detecting the probe atom in its lower state with ϕ . It shows four peaks at the positions of the four states of the field in the generated superposition state. The small oscillations in the background are because of the interference effects of residual field components after adding the external field to the cavity.

IV. DECOHERENCE OF THE GENERATED SUPERPOSITION STATE

Next we study the decoherence of the generated superposition state (8). We are interested in the coherent superposition of four well separated mesoscopic states of the field. The decoherence of such a state will be equivalent to the decoherence of the state (12). This can be done using the master equation

$$\dot{\rho} = -\frac{\kappa}{2}(a^{\dagger}a\rho - 2a\rho a^{\dagger} + \rho a^{\dagger}a), \qquad (26)$$

where κ is cavity field decay parameter and we carry analysis in the absence of thermal photons. For initial

FIG. 3: (Color online) The Q-distribution function $Q(\gamma)$ for the generated state after passing three atoms through the cavity, for $\alpha = 8$. The interaction times for the first atom, second atom and the third atom are chosen such that $gt_1 = 8\pi$, $gt_2 = 4\pi$, $gt_3 = 2\pi$.

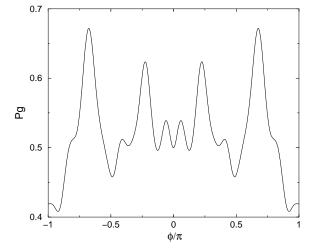


FIG. 4: The probability of detecting probe atom in its ground state as a function of ϕ for the generated superposition (7). The parameters used are same as in Fig.1 and the interaction time for the probe atom is selected such that $gt_p = 1.5\pi$.

state (12) we find the density matrix after time t

FIG. 5: The decoherence of the approximated state (12) in terms of Wigner function at different times, (a) for $\kappa t = 0$, (b) for $\kappa t = 1/2|\alpha|^2$, (c) for $\kappa t = 1/|\alpha|^2$, (d) for $\kappa t = 2/|\alpha|^2$, for $|\alpha| = 4$.

$$\rho(t) = \frac{1}{16} \left[(|\alpha_t\rangle \langle \alpha_t| + | -\alpha_t\rangle \langle -\alpha_t| + |i\alpha_t\rangle \langle i\alpha_t| + | -i\alpha_t\rangle \langle -i\alpha_t|) \right]
+ e^{-2|\alpha|^2 (1-e^{-\kappa t})} \left(|\alpha_t\rangle \langle -\alpha_t| e^{-2i\eta_1} + | -\alpha_t\rangle \langle \alpha_t| e^{2i\eta_1} + |i\alpha_t\rangle \langle -i\alpha_t| e^{2i\eta_1} + | -i\alpha_t\rangle \langle i\alpha_t| e^{-2i\eta_1} \right)
+ e^{-|\alpha|^2 (1-i)(1-e^{-\kappa t})} \left(|\alpha_t\rangle \langle i\alpha_t| e^{-2i(\eta_1-\eta_2)} + | -i\alpha_t\rangle \langle \alpha_t| e^{-2i\eta_2} + | -\alpha_t\rangle \langle -i\alpha_t| e^{2i(\eta_1+\eta_2)} + |i\alpha_t\rangle \langle -\alpha_t| e^{-2i\eta_2} \right)
+ e^{-|\alpha|^2 (1+i)(1-e^{-\kappa t})} \left(|i\alpha_t\rangle \langle \alpha_t| e^{2i(\eta_1-\eta_2)} + |\alpha_t\rangle \langle -i\alpha_t| e^{2i\eta_2} + | -i\alpha_t\rangle \langle -\alpha_t| e^{-2i(\eta_1+\eta_2)} + | -\alpha_t\rangle \langle i\alpha_t| e^{2i\eta_2} \right) \right] (27)
\alpha_t = \alpha' e^{-\kappa t/2}.$$

In Eq.(27) the second, third and the fourth terms reflect the coherent character of the superposition. These are the terms which decohere due to interaction with the environment. The contribution to the Wigner function from the second term in Eq.(27) is

$$\frac{e^{-2|\gamma|^2 - 2|\alpha|^2 (1 - e^{-\kappa t})}}{4\pi} \left\{ \cos[\eta_1 + i(\alpha' \gamma^* - \alpha'^* \gamma)] + \cos[\eta_1 + (\alpha' \gamma^* + \alpha'^* \gamma)] \right\}, \quad (28)$$

which decays as $e^{-2|\alpha|^2(1-e^{-\kappa t})} \approx e^{-2|\alpha|^2\kappa t}$ for $\kappa t << 1$. This term arises from the coherence between the pair $|\alpha'\rangle$, $|-\alpha'\rangle$ and the pair $|i\alpha'\rangle$, $|-i\alpha'\rangle$, and is responsible for the central sub-Planck structures. The term in curly bracket can be written as $\{\cos[\eta_1 + 2\alpha'|\gamma|\sin\theta] + \cos[\eta_1 + 2\alpha'|\gamma|\cos\theta]\}$. Thus in any direction $\theta \neq n\pi/2$ one has an interference pattern which arises from two cosine terms with different periodicity. Thus the sub-Planck structures decohere as $e^{-2|\alpha|^2\kappa t}$. The third and the fourth terms in Eq.(27) show the coherence between other pairs of coherent states, and decay as $e^{-|\alpha|^2\kappa t}$. In Fig.5 we plot the decoherence of the approximated state (12) in terms of the Wigner function at different times. As time

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progresses in Fig.5 from (a) to (d), the central interference patterns decay faster and disappear earlier than the interference fringes between the coherent states, say $|\alpha\rangle$ and $|i\alpha\rangle$, disappear. This is clear from the equation (27) that the central interference patterns decohere two times faster than the interference fringes between the coherent states like $|\alpha\rangle$ and $|i\alpha\rangle$.

V. CONCLUSIONS

In this paper we have shown the possibility for generating the superposition of four mesoscopic states of the field using resonant interaction between atoms and the field in a cavity. We have discussed the properties of the quasi-probability distributions of the generated state and compared with the superposition of four coherent states. We have discussed the time scale over which the state decoheres and shown that the generated state can be monitored using homodyne detection techniques. Another way to detect such superposition is by doing tomography [19] of such states.

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