# Proteomics in the Light of Integral Value Transformations 

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#### Abstract

In this paper, Proteomics have been studied in the light of Integral Value Transformations (IVTs) which was introduced by the Sk. S. Hassan et al in 2010. For case study, a Human olfactory receptor OR1D2 protein sequence has been taken and then different IVTs have been used to evolve OR1D2 into some other proteomic like sequences. It has been observed that some of the generated sequences have been mapped to another olfactory receptor in Human or in some other species. Also it has been corroborated through fractal dimension that some of the fundamental protein properties have been nearly intact, even after the mapping. This study will help to comprehend proteomic evolutionary network with the help of IVTs.


Keywords: Olfactory Receptors (ORs), Box-counting dimension, Proteomics.

## 1. Introduction:

The study of proteins such as structures, functions and evolutions is universally known to as Proteomics, was first coined in 1997 to make an analogy with Genomics, the study of the genes [1]. After genomics, proteomics is considered the next step in the study of biological systems. The study of proteomics is important because proteins are responsible for both the structure and the functions of all living things. Genes are simply the instructions for making proteins. Therefore, a proper quantitative understanding of proteins characteristics and their inter network are required. In this paper, an olfactory receptor OR1D2 has been considered for the proteomics study. Interestingly, on applying the IVT systematically, we have been able to show that each of the DNA sequence at various discrete time instances in IVT evolutions can be directly mapped to another specific proteomic sequences existing in different species. A number of certain fundamental properties namely percentage of accessible residues, Alpha helix (Chou \& Fasman), Amino acid composition (\%), Beta sheet (Chou \& Fasman), Beta turn (Chou \& Fasman), Coil (Deleage \& Roux), Hydrophobicity (Aboderin) and Total beta strand have been considered to ensure protein properties of the IVT generated sequences. All protein plots for all the IVT generated sequences including OR1D2 using Matlab (bioinformatics toolbox) have been generated. Then box-counting dimensions for each of the protein plot have been calculated through BENOIT ${ }^{\mathrm{TM}}$. Since protein properties remain intact in the bijective IVT generated sequences, we claim that in the event of replacement of proteomic sequence (which may take place for various reasons like diseases), we may follow the inverse map of the bijective IVTs to get back the same with usual properties. This study will help us to ascertain potential new drugs for the treatment of disease.

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## 2. Some Reviews and Fundamentals

In this section, we describe very briefly about IVTs, Fractal and proteins.

### 2.1 Notion of Integral Value Transformation (IVT):

Let us define the Integral Value Transformations (IVTs) in $\mathbb{N}_{0}{ }^{K}$ as the following [2, 3, 4, 5]:

$$
\begin{aligned}
& \operatorname{IVT}{ }^{p, k_{j}}: \mathbb{N}_{0}{ }^{\mathrm{K}} \rightarrow \mathbb{N}_{0} \\
& \operatorname{IVT}{ }^{p, k}{ }_{j}\left(\left(n_{1}, n_{2}, \ldots n_{k}\right)=\right. \\
& \left(f_{j}\left(a_{0}{ }^{n_{1}}, a_{0}^{n_{2}}, \ldots, a_{0}{ }^{n_{k}}\right) f_{j}\left(a_{1}^{n_{1}}, a_{1}{ }^{n_{2}}, \ldots, a_{1}^{n_{k}}\right) \ldots \ldots f_{j}\left(a_{l-1}^{n_{1}}, a_{l-1}{ }^{n_{2}}, \ldots, a_{l-1}{ }^{n_{k}}\right)\right)_{p}=m \\
& \text { where } n_{1}=\left(a_{0}{ }^{n_{1}} a_{1}^{n_{1}} \ldots . a_{l-1}^{n_{1}}\right)_{p}, n_{2}=\left(a_{0}{ }^{n_{2}} a_{1}^{n_{2}} \ldots . a_{l-1}^{n_{2}}\right)_{p}, \ldots . . n_{k}=\left(a_{0}^{n_{k}} a_{1} n_{k} \ldots . a_{l-1}{ }^{n_{k}}\right)_{p}
\end{aligned}
$$

$$
f_{j}:\{0,1,2, \ldots, p-1\}^{k} \rightarrow\{0,1,2, \ldots, p-1\}
$$

m is the decimal conversion from the p adic number.

Let us fix the domain of IVTs as $\mathbb{N}_{0}(\mathrm{k}=1)$ and thus the above definition boils down to the following:

$$
\operatorname{IVT}^{\mathrm{p}, 1}{ }_{\mathrm{j}}(\mathrm{x})=\left(\mathrm{f}_{\mathrm{j}}\left(\mathrm{x}_{\mathrm{n}}\right) \mathrm{f}_{\mathrm{j}}\left(\mathrm{x}_{\mathrm{n}-1}\right) \ldots \ldots \ldots \mathrm{f}_{\mathrm{j}}\left(\mathrm{x}_{1}\right)\right)_{\mathrm{p}}=\mathrm{m}
$$

where $m$ is the decimal conversion from the $p$ adic number, and $x=\left(x_{n} x_{n-1} \ldots \ldots x_{1}\right)_{p}$.

Now, let us denote the set of IVT ${ }^{\mathrm{p}, 1}{ }_{\mathrm{j}}$ as
$T^{p, 1}=\left\{\begin{array}{c|c}\operatorname{IVT}^{p, 1}{ }_{j}\end{array}: \mathbb{N}_{0} \rightarrow \mathbb{N}_{0}\left\{\begin{array}{c}0 \leq \mathrm{j}<\mathrm{p}^{\mathrm{p}}, \quad \mathrm{IVT}^{\mathrm{p},{ }_{j}}(\mathrm{x})=\left(\mathrm{f}_{\mathrm{j}}\left(\mathrm{x}_{\mathrm{n}}\right) \mathrm{f}_{\mathrm{j}}\left(\mathrm{x}_{\mathrm{n}-1}\right) \ldots \ldots \ldots \mathrm{f}_{\mathrm{j}}\left(\mathrm{x}_{1}\right)\right)_{\mathrm{p}}=\mathrm{m} \\ \text { where } \mathrm{m} \text { is the decimal conversion from the padic number } \\ \text { and } \mathrm{x}=\left(\mathrm{x}_{\mathrm{n}} \mathrm{x}_{\mathrm{n}-1} \ldots \ldots \mathrm{x}_{1}\right)_{\mathrm{p}}\end{array}\right\}\right.$

Let us define the IVT in $\mathbb{N}_{0}$ in 4 -adic number systems. There are $256\left(4^{4^{1}}\right)$ one variable four state CA rules. Corresponding to each of those CA rules there are 256 IVTs are there in 4 adic system in one dimension.
$\mathrm{IVT}^{4,1}{ }_{\#}$ is mapping a non-negative integer to a non-negative integer.
$\operatorname{IVT}^{4,1}{ }_{\#}(a)=\left(\left(f_{\#}\left(a_{n}\right) f_{\#}\left(a_{n-1}\right) \ldots f_{\#}\left(a_{1}\right)\right)_{4}=b\right.$
Where ' a ' is a non-negative integer and $a=\left(a_{n} a_{n-1} \ldots a_{1}\right)_{4}$ and ' b ' is the decimal value corresponding to the 4adic number.

For an example, let us consider $a=225=(3201)_{4}$ and $\#=120 \operatorname{sof}_{\#}(0)=0 ; f_{\#}(1)=2 ; f_{\#}(2)=$ 3 and $f_{\#}(3)=1$
Therefore, $\mathrm{IVT}^{4,1}{ }_{120}(225)=\left(\mathrm{f}_{120}(3)\left(\mathrm{f}_{120}(2)\left(\mathrm{f}_{120}(0)\left(\mathrm{f}_{120}(1)\right)_{4}=(1302)_{4}=114\right.\right.\right.$.
Consequently, IVT ${ }^{4,1}{ }_{120}(225)=114$.
Let us denote $\mathfrak{T}^{4,1} \#$ as set of all IVT ${ }^{\mathrm{p}, \mathrm{k}}$ \# transformations. It is worth nothing that there are $4!=24$ number of Bijective functions are there in $\mathfrak{T}^{4,1}{ }_{\#}$. So of the $256\left(4^{4^{1}}\right)$ transformations in $\mathfrak{T}^{4,1} \#$ four are linear and rest are nonlinear [6].

### 2.2 Fractal and Fractal Dimension

Our artificial world can be described easily through Euclidean geometric shapes but there are many things in nature such as shape of cloud, geometry of lightening etc. could not be described through Euclidean geometry. Many mathematicians descended the challenge for a fair enough description of natural objects but after a long
period in 1975, B. Mandelbrot took the challenge and gave the birth of a new geometry to describe nature which is known to us as 'Fractal Geometry' in short 'Fractal'. The precise definition of "Fractal" according to Benoit Mandelbrot is as a set for which the Hausdroff Besicovitch dimension strictly exceeds the topological dimension. To gain a quantitative insight of Fractal, some fractal parameters namely Fractal dimension, Hurst exponent, succolarity, lacunarity etc. are also introduced in the literature. A brief discussion follows about one of the well-known methods of calculating fractal dimension namely 'Box-Counting method'.

Box-Counting Method: This method computes the number of cells required to entirely cover an object, with grids of cells of varying size. Practically, this is performed by superimposing regular grids over an object and by counting the number of occupied cells. The logarithm of $\mathrm{N}(\mathrm{r})$, the number of occupied cells, versus the logarithm of $1 / r$, where $r$ is the size of one cell, gives a line whose gradient corresponds to the box dimension [7].

### 2.3 Problem in Protein Structures

Proteins are an important class of biological macromolecules present in all organisms. After the structure of DNA was discovered by James Watson and Francis Crick, who used the experimental evidence of Maurice Wilkins and Rosalind Franklin (among others), serious efforts to understand the nature of the encoding of proteins began. George postulated that a three-letter code must be employed to encode the 20 standard amino acids used by living cells to encode proteins, because 3 is the smallest integer $n$ such that $4^{n}$ is at least 20 [8]. The three-dimensional structures of proteins were first determined by X-ray diffraction analysis; Perutz and Kendrew shared the 1962 Nobel Prize in Chemistry for these discoveries. At the present time, more than ten thousand protein structures were found with their atomic details. The structure of the protein is ultimately defined by its primary structure, or amino acid sequence. There are no theories or computational techniques at the moment which will allow us to predict the new protein folding by its sequence. Even, how proteins were developed during organisms' evolution is blurred. Therefore proper understanding is required in the primary structure level i.e. in the amino acids sequence level of proteins.

## 3. Methods and Results:

### 3.1 Method of Sequence generation through IVTs:

The domain of act of IVTs is set of non-negative positive integers. So it is required to have a numeric sequence corresponding to each of the proteomic sequence. A simple mapping $f$ is used to have as defined below:

Let $\mathcal{P}=\{A, C, D, E, F, G, H, I, K, L, Q, N, P, Q, R, S, T, V, W, Y\}$ be the set of amino acid codes and $\mathcal{N}=$ $\{0,1,2,3, \ldots, 19\}$.

$$
f: \mathcal{P} \rightarrow \mathcal{N} \text { as } f(A)=0 ; f(C)=1, f(D)=2, f(E)=3, \ldots, f(W)=18 \text { and } f(Y)=19
$$

Therefore, a protein sequence is now simply a string of twenty variables namely $0,1,2 \ldots 19$ as per coding scheme $f$.

Starting from a protein sequence to generate another proteomic like sequences, it is required to have the IVTs in a particular $\mathfrak{T}^{p, 1}{ }_{\#}$, which maps $\mathcal{N}$ to itself.

The list of such IVTs in $\mathfrak{T}^{p, 1}{ }_{\#}$ is given below in Table-I.


All the mentioned IVTs are essentially bijective in nature for the purpose of switching one to another. Now we apply Integral Value Transformations (IVT ${ }^{\mathrm{p}, 1}{ }_{\#}$ ) systematically [3, 9, 10] :-

Firstly, Divide the whole one dimensional initial sheet of proteomic sequence (numeric sequence) of length $n$ and divided it into $r$ multiple blocks. We designate the initial sequence as $S\left(t_{0}\right)$.

Secondly, we apply bijective domain preservative transformations (need not to be all distinct) taken from $\mathfrak{T}^{p, 1} \#$ (for different p starting from 2 to 19) over each of the $r$ different blocks of $S\left(t_{0}\right)$. Thereby, we call this case as Hybrid Application of IVTs. In other words, we are getting $S\left(t_{1}\right)$ from $S\left(t_{0}\right)$ through hybrid application of IVTs. Next, we follow this step successively as long as we wish to iterate.

The results, on applying the proposed systematic technique of application of IVTs on OR1D2 are enumerated in the following subsections.

### 3.2. Results

Here we discuss the results on applying different IVTs in two following cases.

### 3.2.1: On Applying IVT ${ }^{p, 1}{ }_{\#}$

The proteomic sequence of OR1D2 is 312 long (sequence shown below in Text-1). Choose $r=50$, so there are 7 blocks are there. The following IVTs are used to generate $S\left(t_{1}\right)$ as shown in Table-2.

```
MDGGNQSEGSEFLLLGMSESPEQQRILFWMFLSMYLVTVVGNVLIILAIS
SDSRLHTPVYFFLANLSFTDLFFVTNTIPKMLVNLQSHNKAISYAGCLTQ
LYFLVSLVALDNLILAVMAYDRYVAICCPLHYTTAMSPKLCILLLSLCWV
LSVLYGLIHTLLMTRVTFCGSRKIHYIFCEMYVLLRMACSNIQINHTVLI
ATGCFIFLIPFGFVIISYVLIIRAILRIPSVSKKYKAFSTCASHLGAVSL
FYGTLCMVYLKPLHTYSVKDSVATVMYAVVTPMMNPFIYSLRNKDMHGAL
GRLLDKHFKRLT
```

| BLOCK | $S\left(t_{1}\right)$ in 2 adic IVT | $S\left(t_{1}\right)$ in 3 adic IVT | $S\left(t_{1}\right)$ in 4 adic IVT |
| :---: | :---: | :---: | :---: |
| Block-1 | $\mathrm{IVT}^{2,1}{ }_{1}$ | $\mathrm{IVT}^{3,1}{ }_{5}$ | IVT ${ }^{4,1} 99$ |
| Block-2 | $\mathrm{IVT}^{2,1}{ }_{1}$ | $\mathrm{IVT}^{3,1}{ }_{5}$ | IVT ${ }^{4,1}{ }_{114}$ |
| Block-3 | $\mathrm{IVT}^{2,1}{ }_{2}$ | IVT $^{3,1}{ }_{11}$ | IVT ${ }^{4,1}{ }_{147}$ |
| Block-4 | $\mathrm{IVT}^{2,1}{ }_{1}$ | $\mathrm{IVT}^{3,1}{ }_{11}$ | IVT ${ }^{4,1}{ }_{177}$ |
| Block-5 | IVT $^{2,1}{ }_{2}$ | $\mathrm{IVT}^{3,1}{ }_{21}$ | IVT ${ }^{4,1}{ }_{180}$ |
| Block-6 | $\mathrm{IVT}^{2,1}{ }_{2}$ | $\mathrm{IVT}^{3,1}{ }_{21}$ | $\mathrm{IVT}^{4,1}{ }_{210}$ |
| Block-7 | $\mathrm{IVT}^{2,1}{ }_{2}$ | $\mathrm{IVT}^{3,1} 21$ | $\mathrm{IVT}^{4,1}{ }_{225}$ |
| BLOCK | $S\left(t_{1}\right)$ in 5 adic IVT | $S\left(t_{1}\right)$ in 6 adic IVT | $S\left(t_{1}\right)$ in 7 adic IVT |
| Block-1 | IVT ${ }^{5,1}{ }_{194}$ | IVT ${ }^{6,1}{ }_{28565}$ | IVT $^{7,1}{ }_{297051}$ |
| Block-2 | IVT ${ }^{5,1}{ }_{214}$ | IVT ${ }^{6,1} 28595$ | IVT $7,1{ }_{297093}$ |
| Block-3 | IVT ${ }^{5,1}{ }_{294}$ | IVT ${ }^{6,1}{ }_{28745}$ | IVT $7,1{ }_{297393}$ |
| Block-4 | IVT ${ }^{5,1}{ }_{334}$ | IVT ${ }^{6,1}{ }_{28805}$ | IVT $7,1{ }_{297435}$ |
| Block-5 | $\mathrm{IVT}^{5,1}{ }_{414}$ | IVT ${ }^{6,1}{ }_{28985}$ | IVT $7,1{ }_{299109}$ |
| Block-6 | $\mathrm{IVT}^{5,1}{ }_{434}$ | IVT $^{6,1}{ }_{28955}$ | IVT 7,1299151 |
| Block-7 | IVT ${ }^{5,1} 694$ | IVT ${ }^{6,1}{ }_{29860}$ | IVT ${ }^{7,1}{ }_{299793}$ |
| BLOCK | $S\left(t_{1}\right)$ in8 adic IVT | $S\left(t_{1}\right)$ in 9 adic IVT |  |
| Block-1 | IVT $^{8,1}{ }_{5135375}$ | IVT ${ }^{9,1}{ }_{102907844}$ |  |
| Block-2 | IVT ${ }^{8,1}{ }_{5135431}$ | IVT $^{9,1}{ }_{102907916}$ |  |
| Block-3 | IVT $^{8,1}{ }_{5135886}$ | IVT $^{9,1}{ }_{102908572}$ |  |
| Block-4 | IVT $^{8,1}{ }_{5135942}$ | IVT $^{9,1}{ }_{102908644}$ |  |
| Block-5 | IVT $^{8,1}{ }_{5138959}$ | IVT $^{9,1}{ }_{102913676}$ |  |
| Block-6 | $\mathrm{IVT}^{8,1}{ }_{5139015}$ | IVT $^{9,1}{ }_{102913748}$ |  |
| Block-7 | $\mathrm{IVT}^{8,1}{ }_{5139981}$ | IVT $^{9,1}{ }_{102915132}$ |  |

Table-2: IVTs from $\mathfrak{T}^{p, 1}{ }_{\#}$ used for generation of $\boldsymbol{S}\left(\boldsymbol{t}_{1}\right)$
Similarly, others $S\left(t_{i}\right)$ can be generated applying the IVTs in different blocks of the $S\left(t_{i-1}\right)$ as tabulated in supl. met.-I. We have generated 90 such $S\left(t_{i}\right)$ s corresponding to OR1D2 in each $\mathfrak{T}^{p, 1}{ }_{\#}$ system (for $\mathrm{p}=2,3 \ldots$ 19) (available in supl. met.-II).

All these generated sequences have been blast in the NCBI database for significant similarity. The blast result is shown in supl. met.-III.

Most of the generated sequences are mapped to olfactory receptors (specifically more closed to OR1D2) in different organisms like homo sapiens, pan troglodytes, lagothrix lagotricha and etc. Some of the sequences are not, due to the fact that they are more conserved sequence than OR1D2.
Also we have been observed that some of the protein primary structural properties (listed below) are intact with respect to the two dimensional protein plot graphs (using bioinformatics toolbox of Mtlab-R2010b) for each of the generated sequences.
The protein properties which we have considered here are as follows:

- Prop-1: Accessible residues (\%)
- Prop-2: Alpha helix (Chou \& Fasman)
- Prop-3: Amino acid composition (\%)
- Prop-4: Beta sheet (Chou \& Fasman)
- Prop-5: Beta turn (Chou \& Fasman)
- Prop-6: Coil (Deleage \& Roux)
- Prop-7: Hydrophobicity (Aboderin)
- Prop-8: Total beta strand

Corresponding to each property of the $S\left(t_{i}\right)$, we have had eight protein plot graphs from which we have calculated box counting dimensions using BENOIT ${ }^{\mathrm{TM}}$.
The data for OR1D2 sequence are stated below in the table-III. The rest all data are available in the supl. met-IV.

| Sequence | Property | Box-counting dimension |
| :--- | :--- | :--- |
| OR1D2 | Prop1 | 1.91092 |


|  | Prop2 | 1.91103 |
| :--- | :--- | :--- |
|  | Prop3 | 1.90855 |


|  | Prop4 | 1.91141 |
| :--- | :--- | :--- |
| Sequence | Property | Box-counting dimension |
|  | Prop5 | 1.91095 |


|  | Prop6 | 1.91348 |
| :--- | :--- | :--- |
|  | Prop7 | 1.90989 |
|  | Prop8 | 1.91071 |

Table-3: Box-counting dimension for protein plots of OR1D2

We have observed that box-counting dimensions for all the eight protein plots corresponding to each of the protein property for all the generated sequences $S\left(t_{i}\right)$ s are almost same to the same of OR1D2. The data for all the box counting dimension of protein plots for the $S\left(t_{i}\right)$ generated through the $\mathfrak{T}^{2,1}{ }_{\#}$ system is shown below. Hereby we can come to a conclusion that these IVTs preserve the protein properties of the strings. It is to be noted that all these IVTs are bijective; therefore one can switch from one protein to another protein through the IVTs without encumbering the protein properties.

| Sequence | Property | Box-counting dimension |
| :---: | :---: | :---: |
| $S\left(t_{1}\right)$ | Prop1 | 1.92694 |
|  | Prop2 | 1.91117 |
|  | Prop3 | 1.90976 |
|  | Prop4 | 1.91111 |
|  | Prop5 | 1.9113 |
|  | Prop6 | 1.93038 |
|  | Prop7 | 1.91021 |
|  | Prop8 | 1.91144 |
| $S\left(t_{2}\right)$ | Prop1 | 1.91124 |
|  | Prop2 | 1.91099 |
|  | Prop3 | 1.91389 |
|  | Prop4 | 1.90948 |
|  | Prop5 | 1.91064 |
|  | Prop6 | 1.93051 |
|  | Prop7 | 1.91398 |
|  | Prop8 | 1.90983 |
| $S\left(t_{3}\right)$ | Prop1 | 1.91045 |
|  | Prop2 | 1.91049 |
|  | Prop3 | 1.90994 |
|  | Prop4 | 1.91299 |
|  | Prop5 | 1.92765 |
|  | Prop6 | 1.91648 |
|  | Prop7 | 1.92813 |
|  | Prop8 | 1.91448 |
| $S\left(t_{4}\right)$ | Prop1 | 1.91294 |
|  | Prop2 | 1.91495 |
|  | Prop3 | 1.91084 |
|  | Prop4 | 1.9108 |
|  | Prop5 | 1.91155 |
|  | Prop6 | 1.91577 |
|  | Prop7 | 1.9281 |
|  | Prop8 | 1.93043 |
| $S\left(t_{5}\right)$ | Prop1 | 1.91443 |
|  | Prop2 | 1.91431 |


|  | Prop3 | 1.91259 |
| :---: | :---: | :---: |
|  | Prop4 | 1.93055 |
|  | Prop5 | 1.92909 |
|  | Prop6 | 1.91638 |
|  | Prop7 | 1.92901 |
|  | Prop8 | 1.91676 |
| $S\left(t_{6}\right)$ | Prop1 | 1.92863 |
|  | Prop2 | 1.928 |
|  | Prop3 | 1.91431 |
|  | Prop4 | 1.9295 |
|  | Prop5 | 1.91133 |
|  | Prop6 | 1.91751 |
|  | Prop7 | 1.91379 |
|  | Prop8 | 1.91292 |
| $S\left(t_{7}\right)$ | Prop1 | 1.91421 |
|  | Prop2 | 1.928 |
|  | Prop3 | 1.9142 |
|  | Prop4 | 1.91614 |
|  | Prop5 | 1.9101 |
|  | Prop6 | 1.91402 |
|  | Prop7 | 1.9108 |
|  | Prop8 | 1.91314 |
| $S\left(t_{8}\right)$ | Prop1 | 1.9104 |
|  | Prop2 | 1.91378 |
|  | Prop3 | 1.91039 |
|  | Prop4 | 1.91287 |
|  | Prop5 | 1.91177 |
|  | Prop6 | 1.91392 |
|  | Prop7 | 1.90987 |
|  | Prop8 | 1.91378 |
| $S\left(t_{9}\right)$ | Prop1 | 1.91428 |
|  | Prop2 | 1.91129 |
|  | Prop3 | 1.91367 |
|  | Prop4 | 1.91337 |
|  | Prop5 | 1.91263 |


|  | Prop6 | 1.91431 |
| :--- | :--- | :--- |
|  | Prop7 | 1.91084 |
|  | Prop8 | 1.91413 |
| $S\left(t_{10}\right)$ | Prop1 | 1.91082 |
|  | Prop2 | 1.9108 |
|  | Prop3 | 1.91081 |


|  | Prop4 | 1.91337 |
| :--- | :--- | :--- |
|  | Prop5 | 1.91263 |
|  | Prop6 | 1.91514 |
|  | Prop7 | 1.91084 |
|  | Prop8 | 1.9176 |

Table-4: Box-counting dimension for all protein plots of $S\left(\mathbf{t}_{\mathbf{i}}\right)$ in $\mathfrak{T}^{\mathbf{2 , 1}}{ }_{\#}$
Most of the $S\left(t_{i}\right)$, IVT generated sequences preserve the all eight protein properties. It is to be noted that in the case $\mathfrak{T}^{2,1}{ }_{\#}$ system, the $S\left(t_{1}\right)$ and $S\left(t_{2}\right)$ are both mapped to G-protein-coupled receptor in OR1D2 in human. Also they follow all the protein properties as in OR1D2.
But interestingly, there are many $S\left(t_{i}\right)$ in different $\mathfrak{T}^{p, 1} \#$ systems, which do not map significantly in any organisms but they retain the protein properties as in OR1D2. One of the main reasons is that most of the sequences are conserved (restricted to a few amino acids) whereas OR1D2 is not so. Some of the $S\left(t_{i}\right)$ are not mapped to any of the ORs in any organism although the box-counting dimension for all the protein plots are intact as it is in OR1D2. It is our strong conviction that these $S\left(t_{i}\right)$ serve the purpose for replacement of OR1D2 in genetic evolutionary phase. In the next section we are going to discuss the case on applying the bijective IVTs from $\mathfrak{I}^{20,1}{ }_{\#}$.

### 3.2.2 On Applying IVT ${ }^{20,1}{ }_{\#}$

We have chosen a few bijective IVTs (available in supl. met.-I) from $\mathfrak{T}^{20,1}{ }_{\#}$ system to generate $S\left(t_{i}\right)$ from the protein code for OR1D2 (methodology is discussed in 3.1). Here all the $S\left(t_{i}\right)$ have been blasted in NCBI and they all mapped to G-protein-coupled receptor, OR MOR30-1, hypothetical protein, conserved hypothetical protein etc. in different organisms ranging from human to Plasmodium species (data shown in supl. met.-III). The box counting dimension is still intact for all the protein plots for all the IVT generated sequence in $\mathfrak{I}^{20,1} \#$ system as shown in Figure-I (raw data shown in supl. met-IV).

| Sequence | Property | Box-counting dimension |
| :---: | :---: | :---: |
| $S\left(t_{1}\right)$ | Prop1 | 1.90836 |
|  | Prop2 | 1.91371 |
|  | Prop3 | 1.92937 |
|  | Prop4 | 1.91313 |
|  | Prop5 | 1.92746 |
|  | Prop6 | 1.9128 |
|  | Prop7 | 1.91234 |
|  | Prop8 | 1.91291 |
| $S\left(t_{2}\right)$ | Prop1 | 1.91418 |
|  | Prop2 | 1.91204 |
|  | Prop3 | 1.91182 |
|  | Prop4 | 1.91205 |
|  | Prop5 | 1.91418 |
|  | Prop6 | 1.92998 |
|  | Prop7 | 1.9099 |
|  | Prop8 | 1.91351 |
| $S\left(t_{3}\right)$ | Prop1 | 1.91459 |
|  | Prop2 | 1.91308 |
|  | Prop3 | 1.91151 |
|  | Prop4 | 1.91464 |
|  | Prop5 | 1.91434 |


|  | Prop6 | 1.91216 |
| :---: | :---: | :---: |
|  | Prop7 | 1.91306 |
|  | Prop8 | 1.91321 |
| $S\left(t_{4}\right)$ | Prop1 | 1.91087 |
|  | Prop2 | 1.91468 |
|  | Prop3 | 1.90957 |
|  | Prop4 | 1.90991 |
|  | Prop5 | 1.92755 |
|  | Prop6 | 1.9159 |
|  | Prop7 | 1.9104 |
|  | Prop8 | 1.91369 |
| $S\left(t_{5}\right)$ | Prop1 | 1.91448 |
|  | Prop2 | 1.91485 |
|  | Prop3 | 1.92691 |
|  | Prop4 | 1.914 |
|  | Prop5 | 1.9123 |
|  | Prop6 | 1.91203 |
|  | Prop7 | 1.92751 |
|  | Prop8 | 1.92845 |
| $S\left(t_{6}\right)$ | Prop1 | 1.91315 |
|  | Prop2 | 1.91176 |
|  | Prop3 | 1.91169 |
|  | Prop4 | 1.91317 |


|  | Prop5 | 1.91348 |
| :---: | :---: | :---: |
|  | Prop6 | 1.91507 |
|  | Prop7 | 1.91141 |
|  | Prop8 | 1.92879 |
| $S\left(t_{7}\right)$ | Prop1 | 1.91258 |
|  | Prop2 | 1.91057 |
|  | Prop3 | 1.91388 |
|  | Prop4 | 1.91508 |
|  | Prop5 | 1.92907 |
|  | Prop6 | 1.91605 |
|  | Prop7 | 1.91244 |
|  | Prop8 | 1.91098 |
| $S\left(t_{8}\right)$ | Prop1 | 1.92725 |
|  | Prop2 | 1.92767 |
|  | Prop3 | 1.91331 |
|  | Prop4 | 1.91074 |
|  | Prop5 | 1.91459 |
|  | Prop6 | 1.91608 |


|  | Prop7 | 1.90883 |
| :---: | :---: | :---: |
|  | Prop8 | 1.91143 |
| $S\left(t_{9}\right)$ | Prop1 | 1.90984 |
|  | Prop2 | 1.92917 |
|  | Prop3 | 1.9154 |
|  | Prop4 | 1.91098 |
|  | Prop5 | 1.91336 |
|  | Prop6 | 1.91545 |
|  | Prop7 | 1.91013 |
|  | Prop8 | 1.92845 |
| $S\left(t_{10}\right)$ | Prop1 | 1.91286 |
|  | Prop2 | 1.91425 |
|  | Prop3 | 1.91506 |
|  | Prop4 | 1.91402 |
|  | Prop5 | 1.92938 |
|  | Prop6 | 1.91632 |
|  | Prop7 | 1.91337 |
|  | Prop8 | 1.9125 |

Table-5: Box-counting dimension for all protein plots of $\mathbf{S}\left(\mathbf{t}_{\mathbf{i}}\right)$ in $\mathfrak{T}^{\mathbf{2 0 , 1}} \#$
It is noted that the number of bijective, domain preservative IVTs is increased as p increased in $\mathfrak{T}^{\mathrm{p}, 1}{ }_{\#}$. Consequently the sequential conservation is inversely proportional to p .

## 4. Summary and Concluding Remarks:

In summary, we have seen that IVTs steer a given OR sequence of a species to another of the same or different (most likely) species, preserving the protein properties of the original sequence. This methodology will be helpful to mimic the genomic evolution procedure artificially, which is required for genetic replacement therapy. IVTs may also be considered to be a platform to comprehend the morphological connections among the various species.
A naïve question to the Biologists can be raised as in the following:
Suppose, we are given an olfactory receptor orl of a species $s l$ which help it to identify the odors $x l, x 2 \ldots$
Now, we apply the proposed methodology to orl and obtain a new olfactory receptor or2 (supposedly) of species $s 2$.
So, does or 2 help $s 2$ in identifying the same odors $x 1, x 2, \ldots$ ?
In near future, we are really interested to explore the underlying biological methodology that governs the entire process.

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