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1 Replacement and late formation of atmospheric N₂ on 2 undifferentiated Titan by impacts

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1 Saturn's moon, Titan, has remarkable surface features—a massive N₂ atmosphere and
2 hydrological cycle of CH₄—that are often compared with that of Earth¹. However, the
3 origin and evolution of Titan's atmosphere remains largely unknown. The proposed
4 formation mechanisms for Titan's N₂ require a prolonged, warm proto-atmosphere during
5 accretion²⁻⁴. These mechanisms accordingly would not have worked efficiently if Titan
6 stayed cold, as indicated by the incompletely differentiated interior observed by Cassini⁵.
7 Because formation of a massive secondary atmosphere on a planetary body would
8 associate with a major differentiation of its solid body during accretion⁶⁻⁸, the presence of
9 such an atmosphere on undifferentiated cold Titan poses a serious dilemma on our view of
10 how planetary bodies develop atmospheres. Here we propose a new mechanism for the
11 post-accretion formation of Titan's N₂ to resolve this problem: conversion and
12 replenishment of N₂ from NH₃ contained in Titan by impacts during the late heavy
13 bombardment (LHB)⁹. Our results show that Titan, regardless of its thermal history,
14 would acquire sufficient N₂ to account for the current atmosphere during the LHB and
15 that most of the pre-LHB atmosphere would have replaced by impact-induced N₂. This is
16 the first scenario capable of generating a N₂-rich and nearly primordial Ar-free
17 atmosphere on undifferentiated cold Titan. We also suggest that Titan's N₂ was delivered
18 from a different source in the solar nebula compared with Earth and that the origins of N₂

1on Titan and Triton are fundamentally different with that of N₂ on Pluto.

2 Why Titan possesses a massive N₂ atmosphere is a longstanding question. One of the
3most important constraints on the origin of Titan's atmosphere is perhaps the low abundance of
4primordial Ar¹⁰ (³⁶Ar/N₂ ≈ 2.8 × 10⁻⁷) observed by Cassini–Huygens, suggesting that Titan's N₂
5is of secondary origin, as with N₂ on Earth. If Titan's N₂ had been originated directly from the
6solar nebula, significant amounts of ³⁶Ar would have been present in the satellitesimals that
7formed Titan⁸ (³⁶Ar/N₂ ≈ 10⁻¹ to 10⁻²). Therefore, the above observation suggests that N₂ was
8delivered to Titan in a less-volatile form, probably NH₃^{8,11,12}.

9 Previous studies have proposed three mechanisms for the conversion of NH₃ to N₂:
10photolysis², atmospheric shock heating³, and endogenic⁴. However, there is at least one critical
11problem with these mechanisms: they all require a 'warm Titan' during its early history. For
12photolysis and shock heating, Titan would have required a prolonged, thick and warm NH₃
13proto-atmosphere generated by substantial melting and vapourization of surface materials during
14accretion^{7,8}, which would have resulted in the rock–ice differentiation required for the
15production of endogenic N₂⁴. However, recent gravitational data from Cassini⁵ reveal that Titan's
16interior is incompletely differentiated, suggesting that substantial melting and vapourization
17would have been unlikely^{7,13}. Consequently, the proto-atmosphere would have been tenuous and
18short-lived^{7,13}, meaning in turn that photolysis and shock heating are unlikely to have been

1 effective in converting NH_3 into N_2 .

2 We investigate the importance of post-accretion exogenic events in converting NH_3 to
3 N_2 , especially cometary impacts during the LHB, which occurred at ~ 3.9 billion years ago⁹.
4 Given both a high impact velocity ($v_{\text{imp}} \approx 11 \text{ km/s}^{14}$) and a large total impactor mass ($\sim 3 \times 10^{20}$
5 kg^{13} , compared to $\sim 5 \times 10^{19} \text{ kg}$ after the LHB¹⁴), the LHB would have been one of the most
6 energetic events affecting Titan, as well as the other large icy satellites. Although the direct
7 delivery of N_2 from comets has been proposed¹⁵, a key factor in explaining the low $^{36}\text{Ar}/\text{N}_2$ ratio
8 in Titan's atmosphere is the decomposition of NH_3 contained in Titan as a consequence of
9 impacts. However, a lack of experimental studies of impact-induced N_2 formation has prevented
10 investigating quantitatively the effect of the LHB on the origin of Titan's N_2 .

11 In the present study, we conducted impact experiments to determine the efficiency of
12 N_2 production from ammonium hydrate ($\text{NH}_3\text{-H}_2\text{O}$) ice. Because of both the difficulties in direct
13 measurements of impact-induced gas species due to chemical contamination (such as, gun debris
14 and combustion gases) by powder and light-gas guns and in the preparation of ice targets,
15 impact chemistry of planetary ices has been poorly investigated. We develop a new experimental
16 system: a chemically clean technique to accelerate projectiles with a high-energy laser pulse
17 (laser gun) combined with isotopic-labelling and target-preparation techniques for $^{15}\text{NH}_3\text{-H}_2\text{O}$
18 ice (see Methods). This experimental system allows us to quantify impact-induced N_2

1production via measurements of $^{15}\text{N}_2$ with mass spectrometry.

2 Figure 1 shows the results of experiments on the efficiency of impact-induced N_2
3production from $\text{NH}_3\text{-H}_2\text{O}$ ice as a function of peak shock pressure. The efficiency exhibits a
4linear increase as a function of pressure. Based on a linear fit to the experimental data, we
5obtained peak shock pressures for incipient and complete N_2 degassing at ~ 8 and ~ 23 GPa,
6respectively. This figure also indicates that N_2 production efficiency does not depend on the NH_3
7concentration in the target very much, suggesting that the experimental data are applicable to
8planetary impacts of icy materials with various NH_3 concentrations. The present result suggests
9that impact-induced N_2 conversion proceeds efficiently in cometary impacts on Titan, but is
10inefficient in satellitesimal impacts during accretion (Fig. 1).

11 Based on the present experimental results, we calculated the N_2 supplied by a cometary
12impact on Titan, based on numerical impact simulations using a three-dimensional smoothed-
13particle-hydrodynamics (SPH) method (Supplementary Information). The mass for partial and
14complete N_2 degassing in the target reaches ~ 8 times the impactor mass. More than 90% of
15supplied N_2 is derived from the dissociation of NH_3 in Titan, when the concentrations of NH_3 ,
16 n_{NH_3} , in both the impactor and target are the same. To investigate the evolution of Titan's N_2
17inventory during the LHB, we conducted a one-box model calculation considering the impact-
18induced supply and loss of N_2 (Supplementary Information). We consider that the supplied N_2 is

1 distributed in the atmosphere and surface based on the saturation vapour pressure of N_2 at a
2 given surface temperature¹⁵. We take into account the loss of atmospheric N_2 by subsequent
3 impacts, using the atmospheric–erosion model given by three-dimensional multi-material
4 hydrocode calculations¹⁶, and the impact-induced ballistic escape of surface N_2 ice, based on the
5 present SPH results (Supplementary Information).

6 We consider two extreme primordial Titans as initial conditions: an airless cold Titan
7 and a relatively warm Titan, as proposed previously, with substantial N_2 and CH_4 on its surface¹⁷.
8 Even if Titan starts with an airless, cold environment (surface temperature $T_{\text{surf}} \approx 60$ K), its N_2
9 inventory reaches a pressure of one to several bars in the LHB aftermath, depending on n_{NH_3} on
10 Titan and impactor radius r_p (Fig. 2a). Accumulation of the current N_2 inventory on a cold Titan
11 requires only 1–2% of n_{NH_3} on Titan (Figs 2a and 3), which is consistent with both the proposed
12 n_{NH_3} level in the satellitesimals that formed the Saturnian system (~ 0.5 – 4.5%)^{11,12} and constraints
13 from Enceladus' plume (~ 1 – 4% ; see the caption to Fig. 3)¹⁸.

14 If Titan possessed substantial N_2 and CH_4 before the LHB, impacts would have
15 replaced most of the preexisting atmosphere during the LHB. A relatively high T_{surf} (~ 70 – 85
16 K)¹⁷, resulting from greenhouse effects, would have increased the mass of the atmosphere,
17 leading in turn to efficient atmospheric erosion. The present results suggest that efficient
18 atmospheric erosion would have resulted in the loss of most of the pre-existing N_2 during the

1LHB, and impact-induced N_2 would have become dominant in the aftermath of the LHB (Fig. 22b). To accumulate the current N_2 inventory on a warm Titan, n_{NH_3} on Titan would have been 3~2–4% (Fig. 3), which is also within the range of the proposed n_{NH_3} in satellitesimals, although 4close to the upper limit. Such a n_{NH_3} might have been achieved in the NH_3 -rich ocean beneath 5Titan's surface^{5,8}. Alternatively, CH_4 may have been lost as a result of impacts, which would 6have led to a decline in T_{surf} and accumulation of N_2 . Based on these results, we conclude that 7Titan acquired significant N_2 during the LHB.

8 The proposed scenario of the replacement of the atmosphere may provide a clue to an 9issue related to the abundance of ^{36}Ar in Titan's atmosphere. Although the low $^{36}Ar/N_2$ ratio is 10consistent with a non-primordial origin of N_2 , the nebular-clathration models do not clearly 11explain the present abundance of ^{36}Ar (no ^{36}Ar ¹² or some higher ^{36}Ar abundance¹¹). Based on our 12scenario, even if primordial ^{36}Ar had been in the preexisting atmosphere, most of it would have 13been lost during the LHB. Consequently, the ^{36}Ar abundance would have approached to a value 14balanced by the input and output by impacts during the LHB. The present results suggest that a 15few percent of Titan's N_2 originated from cometary NH_3 . To achieve the measured $^{36}Ar/N_2 \approx 2.8$ 16 $\times 10^{-7}$ by cometary ^{36}Ar , the $^{36}Ar/H_2O$ ratio in comets would have to be $\sim 10^{-8}$ for an NH_3/H_2O 17value in comets of $\sim 1\%$ ¹⁹. This $^{36}Ar/H_2O$ ratio is consistent with predictions of a nebular- 18clathration model for some comets²⁰, which explains the observed depletion of N_2 with respect

1to CO.

2 Moreover, our experimental results are useful for investigations of impact-induced
3alterations on other icy satellites and dwarf planets. Owing to the strong gravity of gas giants,
4comets collide onto icy satellites with high velocities ($v_{\text{imp}} \approx 6\text{--}60 \text{ km/s}$)¹⁴. Figure 1 suggests that
5impacts at $v_{\text{imp}} > 6 \text{ km/s}$ efficiently dissociate NH_3 on the surface, which may explain the
6absence of any clear evidence for surface NH_3 on Saturnian mid-sized icy satellites²¹, in contrast
7to NH_3 detected in Enceladus' plume from its interior¹⁸. Impact-induced N_2 conversion also
8would occur efficiently on Triton. Our calculation suggests that Triton's N_2 inventory reached
9 $\sim 10^{18} \text{ kg}$ in the LHB aftermath (Supplementary Information), consistent with the proposed
10surface N_2 mass ($\sim 10^{16}\text{--}10^{19} \text{ kg}$)²². In contrast to icy satellites, impact-induced chemical
11alteration of NH_3 is highly inefficient on dwarf planets because of low impact velocities¹⁴ (Fig.
121), suggesting that Pluto's N_2 is not impact-induced secondary material. This view is consistent
13with NH_3 detected on Charon²³. Our results suggest that the origin of N_2 on Triton is different to
14that of Pluto's, even though both of these icy bodies have similar, N_2 -dominated atmospheres.

15 Although our interpretations can explain the observations consistently, one important
16question remains unsolved: the high $^{15}\text{N}/^{14}\text{N}$ ratio in Titan's N_2 ($\sim 5.5 \times 10^{-3}$)¹⁰ relative to that of
17Earth ($\sim 3.7 \times 10^{-3}$). If the above scenario is correct, the high $^{15}\text{N}/^{14}\text{N}$ ratio is primordial,
18regardless of whether hydrodynamic escape induced fractionation in Titan's early history²⁴ or

1not²⁵. We consider that the possible large-scale heterogeneity in the nitrogen isotope in the Solar
2System²⁶ might be interpreted in the similar framework as proposed for explaining that in the
3oxygen isotope^{27,28}. Low temperature ion-molecule reactions²⁹ and N₂ self-shielding³⁰ would
4have formed ¹⁵N-enriched NH₃ ices in the molecular cloud and solar nebula. In the outer solar
5nebula, the NH₃ ices in dust grains were not isotopically exchanged with ¹⁵N-depleted protosolar
6N₂ gas²⁶ at least until the Saturn-forming region. In contrast, Earth's N₂ may have largely come
7from another light N source, such as N components associated with graphite and metal in
8chondrites ($^{15}\text{N}/^{14}\text{N} \approx (3.4 \pm 0.7) \times 10^{-3}$)²⁶, which may have exchanged with the protosolar gas
9and vapourized NH₃ in the inner solar nebula²⁶. We predict that ¹⁵N/¹⁴N values in NH₃ in comets
10and Enceladus' plume would be as high as that of Titan's N₂. Measurements of these values by
11large telescopes and future planetary missions would advance our understanding of the origin
12and distribution of volatiles in the Solar System.

13

14**Methods**

15The laser gun uses a high-energy laser pulse (a Nd:YAG (oscillator) and Glass (amplifier) laser
16with energy of ~10–40 J and laser spot diameter of ~800 μm) for acceleration of a projectile. A
17laser pulse was irradiated on a gold (Au), platinum (Pt), or copper (Cu) foil (thickness of 2.5 and
1810.0 μm for Au, 5.0 μm for Pt, and 3.0 μm for Cu) set in a vacuum chamber (Supplementary

1Fig. 1). The laser pulse vaporized the front surface ($\sim 1 \mu\text{m}$) of metallic foil and generated a
2plasma vapor plume. The rear side of metallic foil was then accelerated by the reaction of the
3expanding plasma vapor and collided on an $\text{NH}_3\text{-H}_2\text{O}$ ice target. We used an isotopic-labelling
4technique for $\text{NH}_3\text{-H}_2\text{O}$ (i.e., $^{15}\text{NH}_3\text{-H}_2\text{O}$) ice to distinguish impact-induced gas species from
5laser-induced contaminated gas species. An $^{15}\text{NH}_3\text{-H}_2\text{O}$ ice target was produced by cooling 100
6 μl of liquid $^{15}\text{NH}_3$ solution in H_2O at $\sim 80 \text{ K}$. A fresh surface of $^{15}\text{NH}_3\text{-H}_2\text{O}$ ice appeared in the
7vacuum chamber immediately before impact (Supplementary Fig. 2). The gas species formed by
8impacts were analysed with a quadrupole mass spectrometer (QMS) connected with the vacuum
9chamber. We obtained the amount of N_2 production by measuring the QMS signal for $^{15}\text{N}_2$ after
10impact (Supplementary Fig. 3). Impact velocities and peak shock pressures achieved by the
11impacts were calculated by an empirical equation and the one-dimensional impedance-match
12solution with the planar-impact approximation based on the Hugoniot equations, respectively.
13Full methods and any associated references are available in Supplementary Information.

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8

9**Author Contributions** Y.S. designed the ice target system in the experiments, performed the
10experiments, modeled Titan's N₂ inventory, and wrote the manuscript. H.G. performed the SPH
11simulations. T.K. designed the laser gun system. All authors vigorously debated and contributed
12intellectually to the interpretation of the results.

13

14**Additional Information** The authors declare no competing financial interests. Supplementary
15Information accompanies this paper on www.nature.com/naturegeoscience. Reprints and
16permissions information is available online at <http://npg.nature.com/reprintsandpremissions>.
17Correspondence and requests for materials should be addressed to Y.S.

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Figure legends

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3 **Figure 1. Efficiency of impact-induced N₂ production from NH₃–H₂O ice for different NH₃**

4 **contents (red: 50%; blue: 10%) (Symbols; see Methods).** The vertical axis represents
5 the amount of N₂ produced by impacts normalized by that contained in the isobaric core of
6 the target as NH₃. The top axis represents the impact velocity of the H₂O–ice collision,
7 which generates the peak shock pressure shown on the bottom axis (Supplementary
8 Information). Arrows represent the average impact velocities onto icy planetary bodies¹⁴.
9

10 **Figure 2. Evolution of Titan’s N₂ inventory during the LHB.** Vertical dashed lines and

11 horizontal yellow lines show the proposed LHB mass and current N₂ inventory,
12 respectively. The concentration of NH₃, n_{NH_3} , in comets is assumed to be 1%¹⁹. **a**, Cold
13 Titan for different n_{NH_3} values on Titan and impactor radius, r_p (20 and 30 km)¹³. **b**, Titan
14 possessing N₂ (1.4 bar) before the LHB¹⁷ for the surface temperature, $T_{\text{surf}} = 75$ K and 85
15 K, at n_{NH_3} abundances of 3.0% and 4.3%, respectively ($r_p = 20$ km).
16

17 **Figure 3. The concentration of NH₃, n_{NH_3} , on Titan required for accumulating 1.5 bar of N₂**

18 **for various surface temperatures at impactor radius of 20 km (blue line) and 30 km**

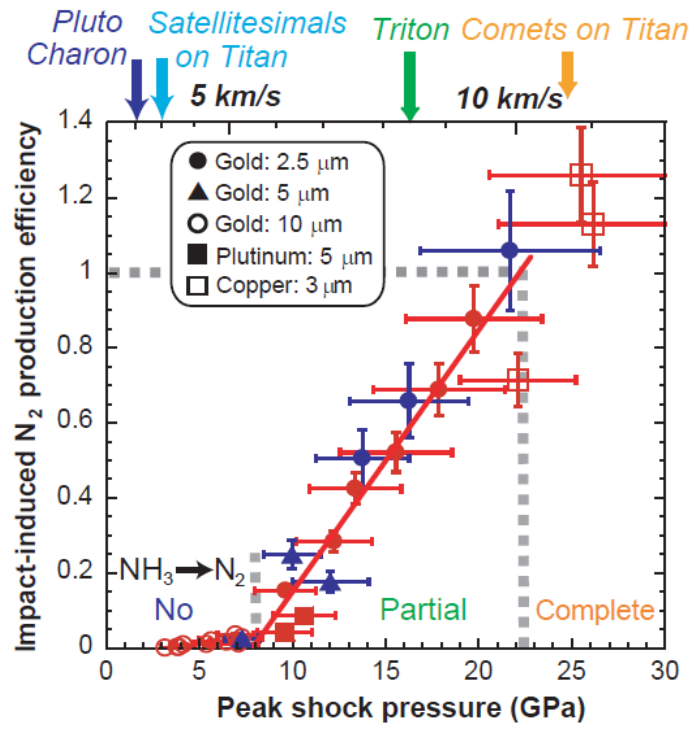
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1 **(red line)**. Black and grey arrows represent the possible ranges of n_{NH_3} in satellitesimals
2 that formed Saturnian satellites, as proposed by nebular models^{11,12} and constrained from
3 observations of Enceladus' plume¹⁸, respectively. n_{NH_3} in Enceladus' plume is $\sim 1\%$ ¹⁸,
4 which provides a lower limit to n_{NH_3} in the satellitesimals. In the case that the plume
5 contains $\sim 1\%$ of N_2 ¹⁸, which formed from NH_3 , an upper limit of the initial n_{NH_3} in the
6 satellitesimals becomes $\sim 4\%$.

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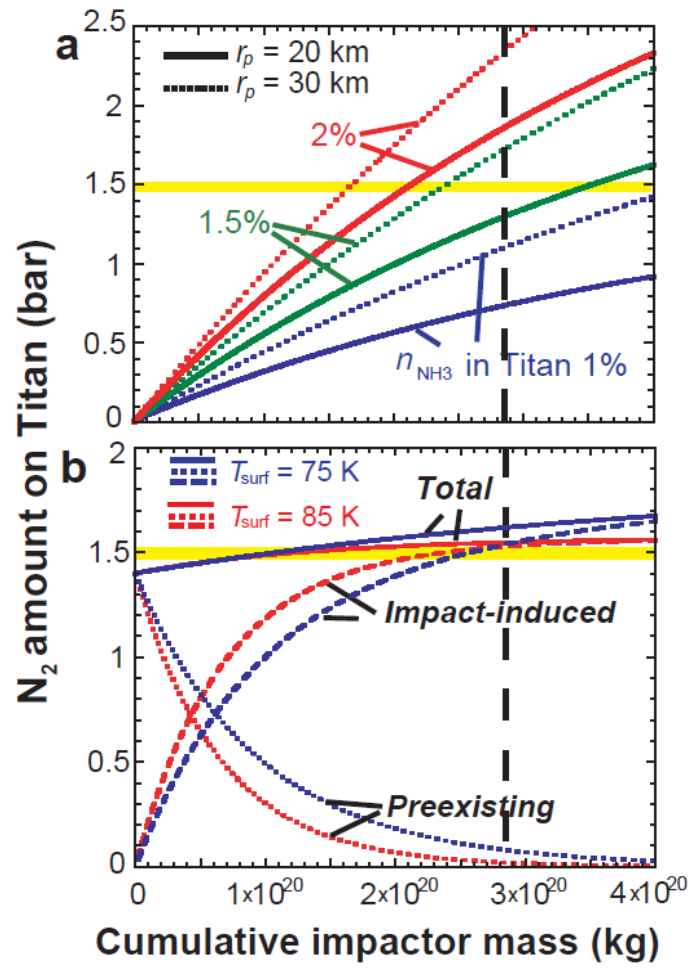
Figures



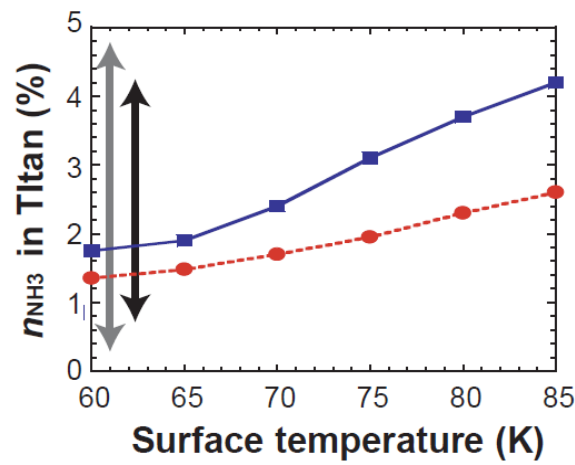
(Figure 1)

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(Figure 2)



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(Figure 3)

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