

# **From Blood Oxygenation Level Dependent (BOLD) signals to brain temperature maps**

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## Abstract

A theoretical framework is presented for converting Blood Oxygenation Level Dependent (BOLD) images to temperature maps, based on the idea that disproportional local changes in cerebral blood flow ( $CBF$ ) as compared with cerebral metabolic rate of oxygen consumption ( $CMRO_2$ ) during functional brain activity, lead to both brain temperature changes and the BOLD effect. Using an oxygen limitation model and a BOLD signal model we obtain a transcendental equation relating  $CBF$  and  $CMRO_2$  changes with the corresponding BOLD signal, which is solved in terms of the Lambert  $W$  function. Inserting this result in the dynamic bio-heat equation describing the rate of temperature changes in the brain, we obtain a non autonomous ordinary differential equation that depends on the BOLD response, which is solved numerically for each brain voxel. In order to test the method, temperature maps obtained from a real BOLD dataset are calculated showing temperature variations in the range:  $(-0.15, 0.1)$  which is consistent with experimental results. The method could find potential clinical uses as it is an improvement over conventional methods which require invasive probes and can record only few locations simultaneously. Interestingly, the statistical analysis revealed that significant temperature variations are more localized than BOLD activations. This seems to exclude the use of temperature maps for mapping neuronal activity as areas where it is well known that electrical activity occurs (such as V5 bilaterally) are not activated in the obtained maps. But it also opens questions about the nature of the information processing and the underlying vascular network in visual areas that give rise to this result.

## 1. Introduction

The balance between metabolic heat production (due to the oxidation of glucose), heat removal by cerebral blood flow ( $CBF$ ), and conductive heat loss from the region of interest (ROI) to neighbouring regions, characterize the temperature dynamics in the ROI (Trübel et al., 2006). Thus, it has been proposed (Yablonskiy et al., 2000) that disproportional changes in cerebral metabolic rate of oxygen consumption ( $CMRO_2$ ) and  $CBF$  evoked by neuronal activity can explain the variation in brain tissue temperature (in the range of  $\pm 0.2^\circ C$ ) revealed by functional studies in humans (Yablonskiy et al., 2000; Shevelev et al., 1993; Gorbach et al., 2003) and animals (Trübel et al., 2006; Serota and Gerard, 1938; McElligot and Melzack, 1967; Melzack and Casey, 1967; Hayward and Baker, 1968; LaManna et al., 1989; Gorbach, 1993; Shevelev and Tsicalov, 1997; Shevelev, 1998).

Conventional methods for measuring brain temperatures require invasive probes and can monitor only one or a few locations simultaneously (Le Bihan, 1995). Clearly, a reliable non-invasive method is highly desirable and could have many clinical uses. Non-invasive methods like microwave or infrared based measurements allow temperature to be measured only to a limited depth. Compared to them, magnetic resonance (MR) imaging has the advantage of producing three-dimensional anatomic images of any part of the body in any orientation with high resolution, and the frequency of the MR signal is temperature dependent (Hindman, 1966). It has been demonstrated that this effect can be used for estimating tissue temperature changes (Parker et al., 1983; Kuroda, 1996). On the other hand, changes in the MR imaging (MRI) signal intensity due to blood oxygenation level-dependent (BOLD) contrast (Bandettini et al., 1992; Frahm et al., 1992; Kwong et al., 1992; Ogawa et al., 1992), i.e., the functional MRI (fMRI) signal, is currently the most widely used signal for brain mapping and studying the neural basis

of human cognition. The origin of the BOLD effect is that haemoglobin is diamagnetic when oxygenated and paramagnetic when deoxygenated. Thus, the presence of deoxyhaemoglobin produces a slight alteration in the local MR signal. Then, the larger increase in  $CBF$  than  $CMRO_2$  following neuronal activity results in a net decrease of the amount of deoxyhaemoglobin present, which produces an increase in the MR signal, the BOLD response (Buxton et al., 2004). Since both BOLD and temperature responses have the same common origin in  $CBF$  and  $CMRO_2$  changes, it is tempting to propose a model for coupling them.

In this paper, we rewrite the coupling between oxygen consumption and cerebral blood flow given by the oxygen limitation model (Buxton and Frank, 1997) as a gamma function. When substituting this new equation in the BOLD signal model of Davis et al (1998) we obtain a transcendental equation relating  $CBF$  and BOLD responses, which is solved in terms of the Lambert  $W$  function (Corless et al., 1996). Thus, given the BOLD signals we are able to calculate the underlying  $CBF$  and  $CMRO_2$  changes. These equations for  $CBF$  and  $CMRO_2$  as functions of the BOLD signal, are inserted in the dynamic bio-heat equation Pennes, 1948; Yablonskiy et al., 2000; Trübel et al., 2006) that describes the rate of temperature changes in the ROI. If we have the BOLD time series for each brain voxel, then we can calculate the corresponding temperature response by solving numerically a non-autonomous differential equation. In this paper we investigate with simulations the temperatures responses associated to different BOLD time series. We also show temperature maps calculated from real BOLD data (Büchel and Friston, 1997).

## 2. Model development

### 2.1 Modelling temperature changes

The dynamic bio-heat equation describes the rate of temperature change in the brain,  $\dot{T}(t)$ , when the resting state is disturbed by global changes in blood flow, incoming blood temperature, or oxygen consumption (Pennes, 1948; Yablonskiy et al., 2000; Trübel et al., 2006):

$$C_t \dot{T}(t) = (\Delta H^\circ - \Delta H_b) CMRO_2|_0 m(t) - \rho_B C_B CBF|_0 f(t)(T(t) - T_a) - \frac{C_t}{\tau} \left(1 - e^{-\frac{t}{\tau}}\right) (T(t) - T_0) \quad (1)$$

where  $m(t)$  and  $f(t)$  are  $CMRO_2$  and  $CBF$  normalized to rest, respectively. The physiological interpretation and values of the parameters of this equation are shown in Table 1. The first term at the right side of equation (1) accounts for the amount of heat locally generated per gram of brain tissue per minute due to the oxidation of glucose from which most of the energy required for brain activity is generated. The second term is the rate of heat removal from brain tissue by cerebral blood flow, and the third term describes conductive heat loss within brain tissue (Trübel et al., 2006). By substituting  $\dot{T} = 0$  in (1) we found the temperature at rest ( $T_0$ ):

$$T_0 = T_a + \frac{(\Delta H^\circ - \Delta H_b) CMRO_2|_0}{\rho_B C_B CBF|_0} \quad (2)$$

If  $E(t)$  is the oxygen extraction fraction, that is, the ratio of oxygen consumption to oxygen delivered, then the following equation holds (Buxton et al., 2004):

$$m(t) = f(t) \frac{E(t)}{E_0} \quad (3)$$

where  $E_0$  is the oxygen extraction fraction at rest. Several works have modelled the relationship between  $m(t)$  and  $f(t)$  (Buxton and Frank, 1997; Hyder et al., 1998; Vafae and Gjedde,

2000; Zheng et al., 2002; Takuya et al., 2003). Particularly, the oxygen limitation model proposed by Buxton and Frank (1997) has been widely employed as part of biophysical models of the generation of the BOLD signal (Buxton et al., 1998; Friston et al., 2000; Friston et al., 2003; Babajani and Zoltanian-Zadeh, 2006; Riera et al., 2006; Riera et al., 2007; Babajani et al., 2008; Blockley et al., 2009):

$$E(f) = 1 - (1 - E_0)^{\frac{1}{f(t)}} \quad (4)$$

Nevertheless, in order to solve the transcendental equation (3) for  $f(t)$ , is necessary to write (4) in a more suitable way. For this, we generated  $E(t)$  data using equation (4) and adjusted to it the gamma function (5) for a  $f$  range of  $[0.7 - 2]$ :

$$\frac{E(f)}{E_0} = af^c(t) e^{-bf(t)} \quad (5)$$

Estimated values for  $a$ ,  $b$ , and  $c$  are displayed in Table 1. With this approximation, the relationship between oxygen consumption and blood flow given by (3) becomes:

$$m(t) = af^{c+1}(t) e^{-bf(t)} \quad (6)$$

BOLD signal changes  $\frac{\Delta S}{S_0}$  can be expressed in terms of  $f(t)$  and  $m(t)$  as (Davis et al., 1998):

$$\frac{\Delta S(t)}{S_0} = \frac{S(t) - S_0}{S_0} = A(1 - f^{\alpha-\beta}(t) m^\beta(t)) \quad (7)$$

Substituting (6) in (7) and rearranging terms:

$$f(t) e^{-\frac{b\beta}{\alpha+\beta c} f(t)} = \left( \frac{\left( A - \frac{\Delta S(t)}{S_0} \right)^{\frac{1}{\alpha+\beta c}}}{Aa^\beta} \right) \quad (8)$$

Multiplying both sides by  $-\frac{b\beta}{\alpha + \beta c}$ :

$$-\frac{b\beta}{\alpha + \beta c} f(t) e^{-\frac{b\beta}{\alpha + \beta c} f(t)} = -\frac{b\beta}{\alpha + \beta c} \left( \frac{\left( A - \frac{\Delta S(t)}{S_0} \right)^{\frac{1}{\alpha + \beta c}}}{A a^\beta} \right) \quad (9)$$

This is a transcendental equation. For obtaining an analytic solution for  $f(t)$  we use the fact that an equation of the form:

$$z e^z = x \quad (10)$$

has solution in terms of the Lambert  $W$  function (Corless et al., 1996):

$$z = W(x) \quad (11)$$

This function is implemented in softwares like Maple, Matlab and Mathematica.

Using this,  $f(t)$  can be obtained from equation (9) as:

$$f(t) = -\frac{\alpha + \beta c}{b\beta} W(y(t)) \quad (12)$$

where  $y(t)$  is a function of the BOLD signal:

$$y(t) = -\frac{b\beta}{\alpha + \beta c} \left( \frac{\left( A - \frac{\Delta S(t)}{S_0} \right)^{\frac{1}{\alpha + \beta c}}}{A a^\beta} \right) \quad (13)$$

Using equations (6) and (12)-(13), oxygen consumption and blood flow time series are calculated from the corresponding BOLD signal. Then, the temperature in a brain voxel can be obtained from the associated BOLD signal by solving numerically the following non autonomous ordinary differential equation:

$$\dot{T}(t) + p(t)T(t) = g(t) \quad (14)$$

with initial condition given by (2), and  $p(t)$  and  $g(t)$  given by:

$$p(t) = -\frac{\rho_B C_B CBF|_0 (\alpha + \beta c)}{b\beta C_{tissue}} W(y(t)) \quad (15)$$

$$g(t) = a \frac{CMRO_2|_0 (\Delta H^\circ - \Delta H_b)}{C_{tissue}} \left( -\frac{\alpha + \beta c}{b\beta} W(y(t)) \right)^{c+1} e^{\frac{\alpha + \beta c}{\beta} W(y(t))} + T_{arterial} p(t) \quad (16)$$

An alternative solution to equation (14) is given in integral form by:

$$T(t) = \frac{1}{\mu(t)} \left( T_0 + \int_0^t \mu(\lambda) g(\lambda) d\lambda \right) \quad (17)$$

where:

$$\mu(t) = e^{\int_0^t p(\omega) d\omega} \quad (18)$$

### 3. Results

In this section we first use computational simulations to explore the temperature temporal dynamics associated to different BOLD time series. After that, we show temperature maps calculated from actual BOLD data.

#### 3.1 From simulated BOLD data to temperature time series

In this paper we propose that the temperature temporal response  $T(t)$  can be obtained from the BOLD time series by solving the ordinary differential equation (14). We solve this equation numerically with the fourth order Runge-Kutta method. All the parameters values needed are displayed in Table 1. The simulated BOLD data were generated with a step size of  $0.1s$  using



the Metabolic/Hemodynamic Model (MHM) proposed in Sotero and Trujillo-Barreto (2007) with the standard parameters set used in that paper.

Table 1. Values and physiological interpretation of the parameters.

Parameter	Interpretation	Value
$C_{tissue}$	Tissue heat capacity	3.664 J/(gK)
$\Delta H^0$	Enthalpy released in the oxidation of glucose: $C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O$	$4.7 \cdot 10^5$ J
$\Delta H_b$	Enthalpy used for releasing oxygen from hemoglobin	$2.8 \cdot 10^4$ J
$CMRO_2 _0$	Cerebral metabolic rate of oxygen consumption at rest	$0.0263 \cdot 10^{-6}$ mol/(gs)
$CBF _0$	Cerebral blood flow at rest	$0.0093$ cm <sup>3</sup> /(gs)
$E_0$	Oxygen extraction fraction at rest	0.4
$C_B$	Blood heat capacity	3.894 J/(gK)
$\rho_B$	Blood density	1.05 g/cm <sup>3</sup>
$A$	Maximum BOLD signal change that could occur corresponding to complete removal of deoxyhemoglobin from the voxel	0.22
$\alpha$	Steady state flow-volume relation	0.4
$\beta$	Parameter dependent on the field strength	1.5
$T_a$	Arterial blood temperature	309.15 K
$a, b, c$	Parameters of the gamma function fitted from the $E(f)$ vs $f$ curve	0.1870, 0.1572 and -0.6041

Figure 1 displays in the same column the positive BOLD responses (PBRs) and the associated  $CMRO_2$  normalized to baseline ( $m$ ),  $CBF$  normalized to baseline ( $f$ ) and the variation with

respect to baseline of the temperature ( $\Delta T$ ). In the case of PBRs, we found they are associated with a decrease in brain temperature. On the other hand, negative BOLD responses (NBRs) are associated with increases in brain temperature (Figure 2). That is, the assumption that  $CBF$  is always greater than  $CMRO_2$  (imposed by the oxygen limitation model) leads to the conclusion that the sign of temperature is always opposite to the sign of  $CBF$  changes. In the case of PBRs,  $CBF$  increases (see Figure 1), and this evokes a decrease in temperature. In the case of NBRs we found that both  $CMRO_2$  and  $CBF$  decrease (in agreement with Shmuel et al., 2002) which leads to an increase in the temperature.

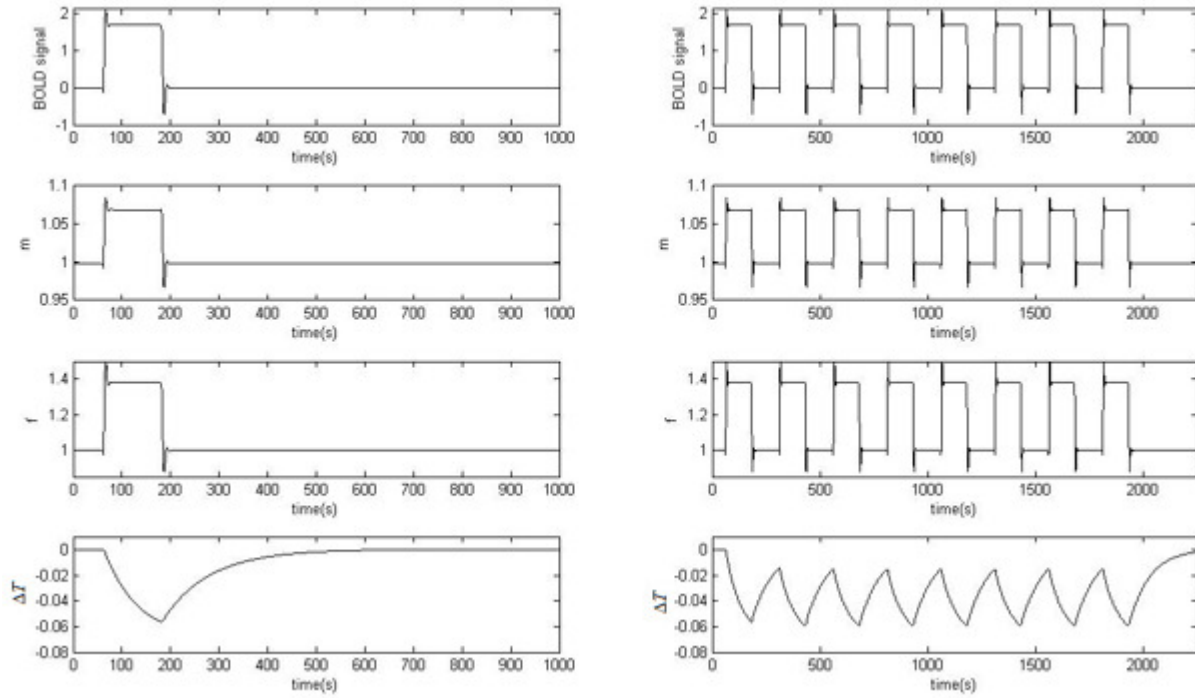


Figure 1. Temperature signals associated to positive BOLD responses. In each column from top to down: BOLD signal,  $CMRO_2$  normalized to baseline ( $m$ ),  $CBF$  normalized to baseline ( $f$ ) and the temperature variation with respect to baseline ( $\Delta T$ ).

While the time characterizing BOLD changes in the brain is in the order of seconds, in the case of temperature changes is in the order of minutes (Trübel et al., 2006). This explains why while

there is no interaction between the multiples BOLD responses in Figure 1 and Figure 2, there is at the resulting temperature signals.

Finally we investigate the influence of one of the parameters, the oxygen extraction fraction at rest ( $E_0$ ) on the results. Figure 3 shows  $\Delta T$  for three values of  $E_0$ , finding that varying  $E_0$  in an small range (0.35–0.45) causes temperature variations one order of magnitude lower (0.002 degrees) than variations due to neuronal activity (Figures 1 and 2).

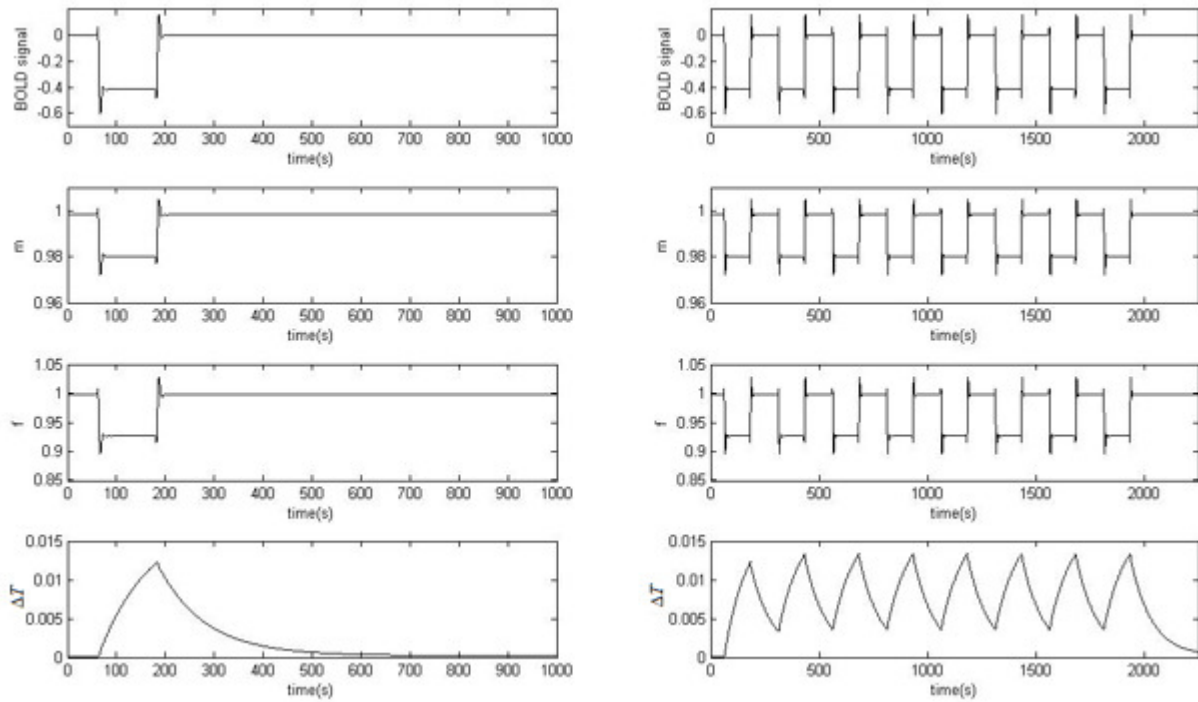


Figure 2. Temperature signal associated to negative BOLD responses. In each column from top to down: BOLD signal,  $CMRO_2$  normalized to baseline ( $m$ ),  $CBF$  normalized to baseline ( $f$ ) and the temperature variation with respect to baseline ( $\Delta T$ ).

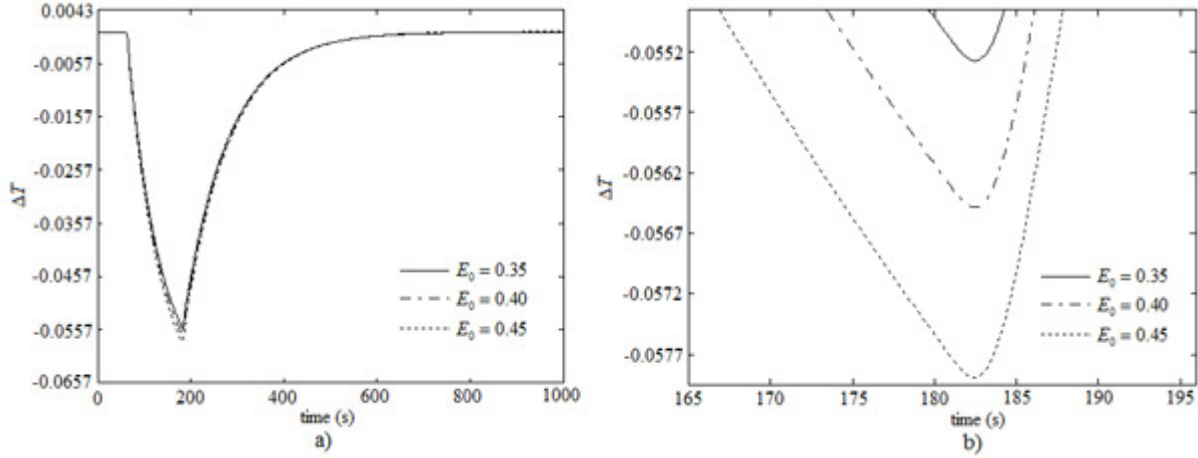


Figure 3. Influence of the oxygen extraction fraction at rest ( $E_0$ ) on the temperature. a)  $\Delta T$  is plotted for three values of  $E_0$  : 0.35, 0.40 and 0.35. b) An augmented detail of b).

### 3.2 From real BOLD data to brain temperature maps

The real BOLD dataset was obtained from the Wellcome Department of Imaging Neuroscience, Institute of Neurology, University College London (<http://www.fil.ion.ucl.ac.uk/spm/data/#epoch>) and is described in Büchel and Friston (1997). The experiment was performed on a 2 Tesla Siemens VISION scanner. Contiguous multislice T2\*-weighted fMRI images were obtained with a TR of 3.22 s. The original data had 32-3 mm slices covering 9.6 cm of the cortex and extending to the upper cerebellum. Subjects were scanned during four runs, each lasting 5 min 22 s. One hundred image volumes were acquired in each run. The first 10 volumes of each run were discarded to allow stabilization of the BOLD signal. Each condition lasted 10 scans or 32.2 seconds.

In this work, image processing and statistical analysis of the BOLD dataset were carried out using SPM2 (<http://www.fil.ion.ucl.ac.uk/spm>). A structural MRI acquired using a standard three dimensional T1 weighted sequence (1x1x3 mm<sup>3</sup> voxel size) was co-registered to the

T2\*-weighted. All the images were spatially normalized to a standard template and the data were smoothed using a 6 mm full width at half maximum isotropic Gaussian kernel.

Using the normalized T1 image, a brain mask was created and BOLD signals for the mask points were extracted from previously T2\* processed images. Then,  $CBF$ ,  $CMRO_2$  and Temperature signals were calculated for each voxel in the mask, using expressions (6) and (12)-(16). For each variable ( $CBF$ ,  $CMRO_2$  and Temperature) the calculated temporal signals were saved as a new image set.

Data activation statistical analysis on BOLD,  $CBF$ ,  $CMRO_2$  and Temperature image sets were performed by modeling the different conditions ('attention to motion', 'no attention to motion', 'fixation' and 'stationary') as reference waveforms in the context of the general linear model as employed by SPM2. To identify brain regions important in early visual processing, the comparison between conditions involving visual motion ('attention to motion' and 'no attention to motion') and 'fixation' was employed.

Figure 4 displays the BOLD data (first row) and the corresponding  $\Delta T$  calculated with our method (second row) at four time instants: 4.83 min, 9.66 min, 14.49 min and 19.32 min. As shown in the legend, the calculated  $\Delta T$  values ( $-0.15:0.1$ ) are within the experimentally observed range. Figure 5 shows the activated regions ( $P < 0.001$ , Bonferroni corrected) obtained from the statistical analysis of BOLD,  $f$ ,  $m$  and  $\Delta T$  data (labelled A, B, C, and D, respectively). For this dataset we obtained that  $f$  and  $m$  present similar activation patterns than the original BOLD data (i.e. activations mainly localized on visual regions V1, V2 and V5/MT). Nevertheless, we found temperature responses to be more localized than the BOLD,  $f$  and  $m$  responses (i.e. activations mainly localized on region V2).

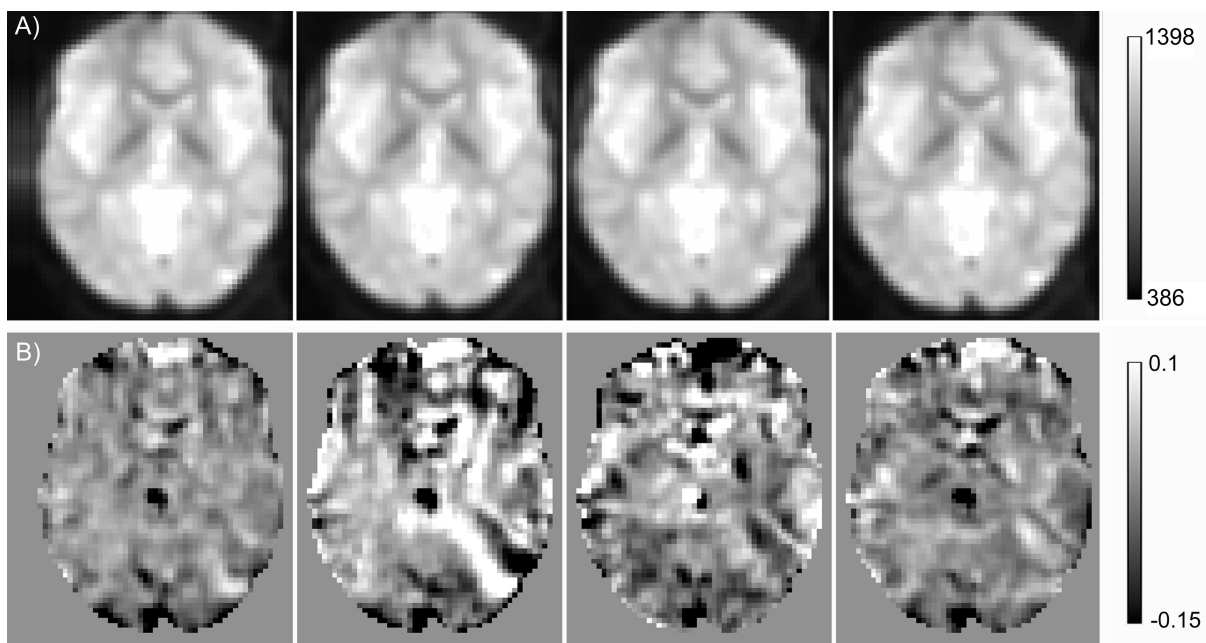


Figure 4. Temperature maps obtained from an actual BOLD dataset at four time instants: 4.83 min, 9.66 min, 14.49 min and 19.32 min. A) original BOLD dataset. B) Temperature variations.

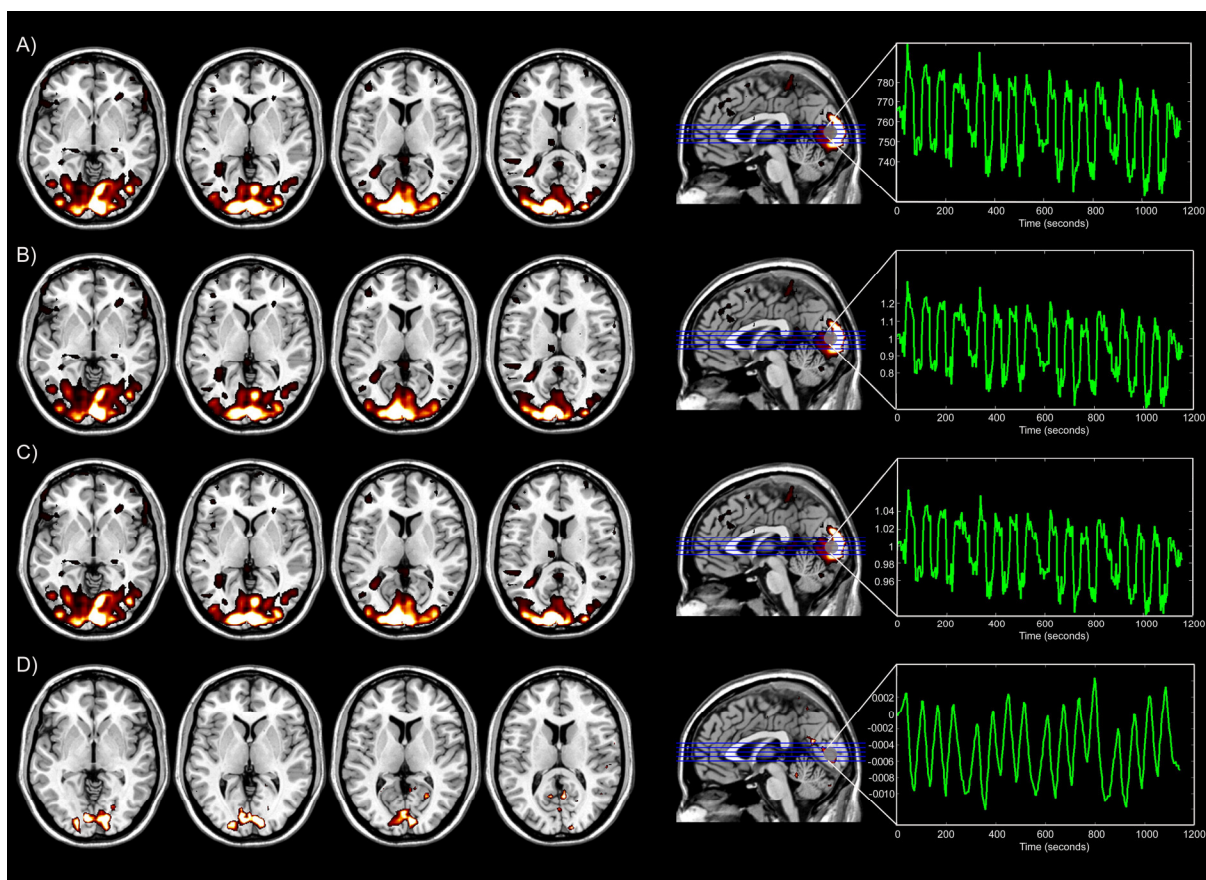


Figure 5. Activated maps obtained from the statistical analysis of the maps shown in Figure 4 ( $P < 0.001$ , Bonferroni corrected). A) BOLD, B)  $CBF$  normalized to baseline ( $f$ ), C)  $CMRO_2$  normalized to baseline ( $m$ ), D) temperature variation with respect to baseline ( $\Delta T$ ). At the end of each row a time series extracted from the activated region is shown.

## 4. Discussion

In this paper we presented a theoretical framework for obtaining  $CBF$ ,  $CMRO_2$  and temperature responses from registered BOLD signals. This could have potential clinical applications, as conventional methods for measuring brain temperatures require invasive probes and can monitor only one or a few locations simultaneously (Le Bihan, 1995). Using simulated BOLD data we confirmed that PBRs are linked to decreases in brain temperature, whereas NBRs are associated to temperature increases. We also demonstrated that stimulations paradigms producing multiple non-interacting BOLD responses can produce interacting temperature responses, due to the slower temporal dynamics of temperature changes. In addition, we converted real BOLD data (Büchel and Friston, 1997) into  $CBF$ ,  $CMRO_2$  and temperature datasets. The calculated  $\Delta T$  values ( $-0.15:0.1$ ) are within the range experimentally observed, being smaller than the ones reported in Yablonskiy et al. (2000) and consistent with the more moderate values obtained by Gorbach et al. (2003).

Interestingly, the data analysis found that statistically significant temperature variations are more localized than BOLD activations, failing to show activations in brain areas where it is well known that electrical activity occurs, such as V5 bilaterally. Thus the most parsimonious interpretation of this result is that temperature data provide a less sensitive mapping of brain activity than fMRI. This result also opens questions about the nature of the information processing

and the underlying vascular network in visual areas that give rise to the difference in temperature found here (Figures 4 and 5).

In the present paper, temperature responses were obtained by solving numerically (fourth order Runge-Kutta method) a non-autonomous differential equation that depends on the BOLD signal (see (14)-(16) ). An alternative to solving this differential equation is to numerically calculate two integrals (see (17)-(18)) with a quadrature method. In the case of our simulated data, which was generated with a temporal resolution of  $0.1s$ , both alternatives gave the same result (not shown here). Nevertheless, actual BOLD signals have a poorer temporal resolution. For data simulated with  $1-3s$  temporal resolution we found the Runge-Kutta method to have better accuracy than quadrature methods like trapeze and Simpson. Finding a more efficient numerical method is a topic for future research.

The method proposed here deals only with the temporal dynamics of the temperature. For obtaining the spatial distribution in the brain (temperature maps as shown in Figure 4) we calculate the temperature voxel by voxel. For modeling the spatial distribution of brain temperature, partial differential equations need to be employed (Collins et al., 2004; Sustanskii and Yablonskiy, 2006). The oxygen limitation model (Buxton and Frank, 1997) and the model for the BOLD signal change (Davis et al., 1998) are also temporal models. Then, the spatial correlations in CBF,  $CMRO_2$  and temperature maps are forced by correlations in the BOLD signals, and not due to model design.

In the calculations presented here, we have assumed that the parameters (see Table 1) do not vary across the brain tissue. Nevertheless, it has been reported (Dunn et al., 2005) a slight spatial dependence in the power law coefficient ( $\alpha$ ) relating changes in CBF and cerebral blood volume (CBV). Additionally, the oxygen consumption at rest ( $CMRO_2|_0$ ) should be affected by



the inhomogeneities found in cortical tissue. That is, the motor cortex, for example, has a relatively sparse population of neurons, while sensory cortices tend to be more densely populated than the average. Furthermore, even within a given cytoarchitectonic region neuronal densities vary considerably (Abeles, 1991).  $CBF|_0$  should also have spatial variations, as we know that vascular density is area specific (Weber et al., 2008). Nevertheless, despite these spatial variability in oxygen consumption and blood flow, there is a relatively uniformity of  $E_0$  across the brain (Gusnard and Raichle, 2001). Using simulations we found that  $\Delta T$  doesn't change appreciably in the  $E_0$  range: 0.35:0.45 (see Figure 3).

In this work, by using the oxygen limitation model we have assumed a tight coupling between blood flow and oxygen consumption. Thus, it is important to note that experimental evidences suggest that energy demand does not directly control  $CBF$  increases (Attwell and Iadecola, 2002), and in fact global changes of  $CBF$  independent of local energy needs have been found (Reis and Golanov, 1997). Nevertheless, changes in  $CBF$  do correlate with oxygen usage during functional activation (Hoge et al., 1999). Thus, the oxygen limitation model is used here only as a practical way of coupling  $CBF$  and oxygen consumption, without deepening in the complex nature of that link.

Finally, our model is deterministic. Nevertheless, several studies have shown the importance of the physiological noise contribution to fMRI signal fluctuations (Biswal et al., 1995; Krüger and Glover, 2001). Thus, future refinements of the present model should include physiological noise.

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