# Friends or Foes? The Interrelationship between Angel and Venture Capital Markets\*

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#### Abstract

This paper develops a theory of how angel and venture capital markets interact. Entrepreneurs first receive angel then venture capital funding. The two investor types are 'friends' in that they rely upon each other's investments. However, they are also 'foes', because at the later stage the venture capitalists no longer need the angels. Using a costly search model we derive the equilibrium deal flows across the two markets, endogenously deriving market sizes, competitive structures, valuation levels, and exit rates. We also examine the role of legal protection for angel investments.

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## 1 Introduction

Investments by wealthy individuals into start-up companies are typically referred to as angel investments. Over the last decade angels have become a more important source of early stage funding for entrepreneurs. According to Crunchbase (www.crunchbase.com), the US angel market grew at an annual rate of 33% between 2007 and 2013. In a 2011 report of the OECD, the size of the angel market was estimated to be roughly comparable to the venture capital (VC henceforth) market (OECD, 2011). For 2009 the report estimates the US (European) venture capital market at \$18.3B (\$5.3B), and the US (European) angel market at \$17.7B (\$5.6B). The rise of the angel market coincides with a shift in VC investments towards doing more later-stage deals. As a result the funding path of growth-oriented start-ups typically involves some initial funding from angels, with subsequent funding coming from venture capitalists (VCs henceforth). Facebook and Google, two of the most successful start-ups in recent history, both received angel financing prior to obtaining VC.

With this bifurcation in the funding environment of entrepreneurial companies, the question arises how these two types of investors interact, and whether angels and VCs are friends or foes? Angels have limited funds and typically need VCs to provide follow-on funding for their companies. At the same time VCs rely on angels for their own deal flow. As they play complementary roles in the process of financing new ventures it might seem that angels and VCs should be friends. However, in practice angels and VCs often see each other as foes. In particular, there is a concern about so-called "burned angels". Angels frequently complain that VCs abuse their market power by offering unfairly low valuations. Expectations of low valuations at the VC stage then affect the willingness of angels to invest in early stage start-ups. Michael Zapata, an angel investor, explains it as follows (Holstein, 2012):

In cases where the VCs do see a profit opportunity, they have become increasingly aggressive in low-balling the managements and investors of emerging companies by placing lower valuations on them. [...] Angels call these actions 'cram downs' or 'push downs'. The market has been very rough on the VCs and they are making it tougher on the angels. They are killing their future deal flow by cramming them down, crashing them out.

The main objective of this paper is to examine the interdependencies between two types of investors, angels and VCs. Our goal is to provide a tractable model of the equilibrium dynamics between two sequentially related markets, and generate a rich set of empirical predictions. We are particularly interested in identifying the underlying determinants of market size and market competition (which depends on the entry rates of entrepreneurs, angels and VCs), as

well as company valuations and success rates. Special attention is given to analyzing the full equilibrium implications of the "burned angels" problem.

From a theory perspective, the challenge is to obtain a model of the two connected markets that generates tractable comparative statics for key variables. To this effect we develop a search model with endogenous entry by entrepreneurs, angels and VCs. Companies require angels for seed investments, and could require VC for funding their growth options. The model generates predictions about the level of competition in both the angel and VC market. It predicts the expected length of fundraising cycles (i.e., the time it takes to raise angel and VC funding), as well as the rate at which companies fail, progress from the angel to the VC market, or achieve an exit. We also derive equilibrium company valuations at both the angel and VC stage.

Our model has three key building blocks that build on previously disparate literatures. First we draw on the staged financing literature (Admati and Pfleiderer, 1994; Berk, Green and Naik, 1999), introducing a dynamic investment structure where start-ups first obtain seed funding in the angel market, then follow-up funding in the VC market. This simple dynamic structure allows us to capture the basic interdependencies between angels and VCs: angels invest first but need the VCs to take advantage of a company's growth options. Central to the model are two feedback loops. The first is the forward loop of how the angel market affects the VC market. The key linkage is that outflow of successful deals in the angel market constitute the deal inflow in the VC market. Here we can think of angels and VCs are 'friends'. The second is the backward loop of how the VC market affects the angel market. The key linkage here is that the utilities of the entrepreneurs and angels at the VC stage affect the entry rates of entrepreneurs and angels at the angel stage. A key insight is that at the VC stage, VCs no longer need the angels to make the investment. The angels' investment is sunk and they provide no further value to the company. This creates a primal friction between angels and VCs, i.e., this is where angels and VCs become 'foes'.

Second, we draw on the search literature. Inderst and Müller (2004) explain how a search model à la Diamond-Mortensen-Pissaridis allows for a realistic modeling of imperfect competition in the VC market. We expand their model to two interconnected markets. We also augment their specification with a death rate for entrepreneurs. Our model highlights the consequences of imperfect competition in the VC market on the angels' bargaining position: while a monopolist VC would have a lot of power over angels, such bargaining power get dissipated in a more competitive VC market.

Third, to examine further determinants of the relative bargaining strengths of entrepreneurs, angels and VCs, we consider the issue of minority shareholder protection (La Porta, Lopez-de-Silanes, Shleifer and Vishny, 2000). In his work on the "burned angels" problem, Leavitt (2005) provides a detailed legal analysis of the vulnerabilities of angels at the time of raising VC. As new investors, VCs can largely dictate terms. They can also use option grants as a

way of compensating the entrepreneur for the low valuation offered to angels. Leavitt argues that legal minority shareholder protection can mitigate the burned angel problem, but cannot fully resolve it. Based on this, we consider a hold-up problem between the angel and the entrepreneur at the time of the follow-up round. The term "hold-up" only applies for the expost relationship between angel and entrepreneur. The VC cannot hold up the angel or the entrepreneur, as he has no prior contractual relationship with them. In our context hold-up means that entrepreneur colludes with the VC to pursue the venture alone without the angel. While the threat remains unexercised in equilibrium, the hold-up potential redistributes rents from the angel to the entrepreneur and VC. Our analysis traces out the equilibrium effects that such hold-up has on the returns and investment levels of angels and VCs.

Our model generates a large number of comparative statics results. Throughout the analysis we consider the joint equilibrium across the two markets. We find that our within-market effects are consistent with results in the prior literature (e.g., Inderst and Müller, 2004), so our main contribution is the analysis of cross-market effects. Here we discover several new insights. For example, a standard within-market result is that while higher search costs for the investor lead to less competition, higher search costs for the entrepreneur lead to more competition (because investors can capture more of the rents). However, this result does not apply in a cross-market setting. We show that there is less angel competition when there are higher search costs at the VC stage for either the VC or entrepreneur. This is because both of these search costs reduce the utilities of the entrepreneur and angel investor.

One of the most interesting results concerns the effects of angel protection. One might conjecture that the ability to take advantage of angels increases entrepreneurial entry. However, we show that in equilibrium there is lower entry by entrepreneurs. This is because the direct benefit for entrepreneurs from holding up angels at a later stage is outweighed by the indirect cost of a thinner angel market. Intriguingly, we find opposite effects for entrepreneurial entry and survival. Weaker angel protection actually leads to better entrepreneurial incentives (because it is allows the entrepreneur to capture additional rents) and therefore to higher success rates.

We also consider the choice of projects, and the timing of exits. Some angels have been advocating early exits as an attractive investment approach (Peters, 2009). Accordingly, start-ups focus on projects that can be sold relatively quickly. The advantage of such a strategy is that the entrepreneurs and angels can avoid the various challenges of securing follow-on investments from VCs. The disadvantage is that they could fail to achieve their full potential. In a model extension we allow for a choice between two development strategies: a safe strategy, where the venture is sold in an early exit, versus a risky strategy, which either leads to failure, or generates higher returns, namely if the company succeeds in developing a growth option and obtaining VC financing. The safe strategy of early exits becomes more likely when angel protection is low, such as when the value of the start-up resides mainly in the entrepreneur's human capital.

Consistent with this we note that many early exists take the form of so-called "acqui-hires" where the acquirer is more interested in the human capital of the start-up.

Our theory implies a series of testable predictions about the size of angel and VC markets, their competitive structure, as well as the valuations obtained. We discuss these by focusing on alternative explanations for the recent rise of angel markets. We distinguish between explanations based on better angel protection, lower start-up costs, greater market transparency, greater entrepreneurial urgency, and supply shocks in venture capital. For example, better angel protection and lower start-up costs both predict larger and more competitive angel markets. However, better angel protection is associated with lower success rates, whereas lower start-up costs lead to higher success rates. Moreover, valuations at the venture capital stage increase with better angel protection, but are not affected by lower start-up costs.

The remainder of the paper is structured as follow. Section 2 discusses the relation of this paper to the literature. Section 3 introduces our main model. We then derive and analyze the angel market equilibrium in Section 4, and the VC market equilibrium in Section 5. Section 6 analyzes how limited legal protection of angels affects the angel and VC market equilibrium. Section 7 examines early exits. Section 8 discusses the empirical predictions from our model. Section 9 summarizes our main results and discusses future research directions. All proofs are in the Online Appendix, which is available on the authors' websites.

# 2 Relationship to literature

The introduction briefly discusses how this paper builds on a variety of literatures. In this section we explain in greater detail the connections to the prior literature. The natural starting point is the seminal paper by Inderst and Müller (2004). They were the first to introduce search into a model of entrepreneurial financing, focussing on how competitive dynamics affect VC valuations. Silveira and Wright (2006) and Nanda and Rhodes-Kropf (2012a) also use similar model specifications for other purposes. One theoretical advance of this paper is that it examines the relationship between two interconnected search markets. A limitation of all these search models (including ours) is that they require homogenous types. Hong, Serfes, and Thiele (2013) consider a single-stage VC financing model with matching among heterogeneous types.

A growing number of papers examine the implications of staged financing arrangements. Neher (1999) and Bergemann, Hege, and Peng (2009) study the design of optimal investment stages. Admati and Pfleiderer (1994) and Fluck, Garrison, and Myers (2005) consider the differential investment incentives of insiders and outsiders at the refinancing stage. Building on recent work about tolerance for failure (Manso, 2011), as well as the literature on soft budget constraints (Dewatripont and Maskin, 1995), Nanda and Rhodes-Kropf (2012a) consider how

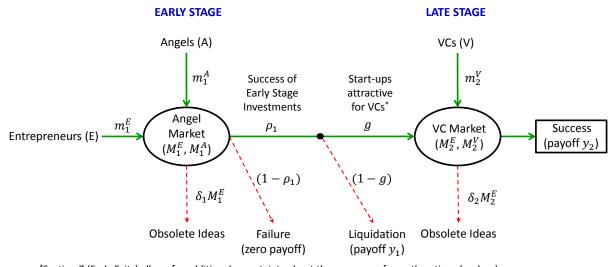
investors optimally choose their level of failure tolerance in a staged financing model. These models all assume that the original investors can finance the additional round. Our model departs from this assumption by focusing on smaller angels who do not have the financial capacity to provide follow-on financing.

The theory closest to ours is the recent work by Nanda and Rhodes-Kropf (2012b) on financing risk. They too assume that the initial investors cannot provide all the follow-on financing. Their analysis focuses on the possibility of multiple equilibria in the late stage market, and shows how different expectations about the risk of refinancing affects initial project choices. Our model does not focus on financing risk, but instead focuses on the hold-up problem at the refinancing stage.

Our model distinguishes between angels and VCs on the basis of the investment stage and the amount of available funding: angels only invest in early stages and have limited funds; VCs only invest in later stages and have sufficient funds to do so. The empirical evidence of Goldfarb, Hoberg, Kirsch and Triantis (2012) and Hellmann, Schure and Vo (2013) is broadly supportive of these assumptions. The latter paper also provides empirical evidence on the financing dynamics, showing how some companies obtain only angel financing (possibly exiting early), whereas others transition from the angel to the VC market.

Our model cannot capture all the nuances of reality. First, it is sometimes difficult to draw a precise boundary between what constitutes an angel investor versus a VC. Shane (2008) and the OECD report (OECD, 2011) provide detailed descriptions of angel investing, and the diversity within the angel community. Second, we do not model value-adding activities of angels versus VCs. Chemmanur and Chen (2006) assume that only VCs but not angels can provide value-added services. By contrast, Schwienbacher (2009) argues that both angels and VCs could provide such services, but that angels provide more effort because they still need to attract outside investors at a refinancing stage. See also the related empirical work of Hellmann and Puri (2002) and Kerr, Lerner and Schoar (2013). Third, in our model both angels and VCs are pure profit maximizers. The work of Axelson, Strömberg, and Weisbach (2009) suggests that the behavior of VCs could be influenced by agency considerations. Moreover, angels can be motivated by non-financial considerations, such as personal relationships or social causes, as discussed in the work of Shane (2008) and Van Osnabrugge and Robinson (2000). Finally, while we motivate our paper with angels and VCs, our theory applies more broadly to the relationship between early and late investors. Further examples of early investors include friends and family, accelerators, and university-based seed funds. Further examples of late investors include corporate investors, bank funds, and growth capital funds.

Our paper is also related to the literature on the staged commercialization of new venture ideas. Teece (1986), Anand and Galetovics (2000), Gans and Stern (2000) and Hellmann and Perotti (2011) all consider models where complementary asset holders have a hold-up opportu-



\*Section 7 (Early Exits) allows for additional uncertainty about the presence of growth options (prob.  $\gamma$ ).

Figure 1: Financing Stages – Angel and VC Markets

nity at a later stage. They mainly ask how this hold-up problem impacts the optimal organization of the early stage development efforts. This paper focuses on the challenges of financing ventures across the different commercialization stages.

## 3 The base model

Our objective is to build a tractable equilibrium model that endogenously derives the size and competitive structure of the early stage (angel) and late stage (VC) market. Conceptually we want a model with endogenous entry to determine market size, and with a continuum between monopoly and perfect competition to determine the level of competition. This naturally leads us to a search model in the style of Diamond, Mortensen and Pissaridis (see Pissarides, 1979, 2000; Mortensen and Pissarides, 1994; Diamond, 1982, 1984). This model has free entry, and it endogenously generates a market density that is a continuous measure of competition. Moreover, the real-life search process of entrepreneurs looking for investors closely resembles the assumptions of pairwise matching used in such search models (Inderst and Müller, 2004).

We consider a continuous time model with three different types of risk-neutral agents: entrepreneurs, angels, and VCs. The length of one period is  $\Delta \to 0$ , and the common discount rate is r>0. In each period a number of potential entrepreneurs discover business opportunities. The cost for an entrepreneur to start his business is  $l\in [0,\infty)$ , which is drawn from the distribution F(l). We interpret l as the personal labor cost associated with establishing the new venture (e.g., the cost of developing a business plan). The endogenous number of start-ups founded in each period is  $m_1^E$ ; see Figure 1 for a graphical overview.

Entrepreneurs are wealth-constrained, so they require external financing for their start-up companies. Specifically, each entrepreneur needs an early stage investment  $k_1$ , and a late stage investment  $k_2$ . What we have in mind is that entrepreneurs first need funding to develop prototypes of their products (early stage financing) to prove the viability of their business models. They then require follow-on investments to bring their developed products to market (late stage financing). We assume that early and late stage financing is provided by two distinct types of investors. For clarity of exposition we associate angels with early stage investments, and VCs with late stage investments. In reality VCs could sometimes also invest in early stage deals, and angels in late stage deals. This does not affect the basic insights from our model; all that matters is that the company needs to find a new investor at the late stage. This could be either because the early stage investor does not have the funds to fully finance the late stage investments, or because early and late stage investors have different skills and information, making them both essential to the success of the venture. For expositional convenience we also assume that early stage investors do not participate in the late stage investment.<sup>1</sup>

In the early stage each entrepreneur needs to find an angel investor, who can make the required investment  $k_1$ . We assume a monopolistically competitive search market with free entry. Specifically, in each period  $m_1^A$  angels enter the early stage market and seek investment opportunities, where  $m_1^A$  is endogenous and satisfies the zero-profit condition for angels. We denote  $M_1^A$  as the equilibrium stock of angels in the early stage market at a given point in time, and  $M_1^E$  as the equilibrium stock of entrepreneurs.

Entrepreneurial opportunities often depend on speedy execution, so that delays in fundraising can be costly for the entrepreneurs. We therefore augment the standard search model with a parameter that measures urgency, i.e., the cost of delay. Specifically we assume that a fraction  $\delta_1 M_1^E$  of business ideas becomes obsolete in each period, generating a zero payoff (see Figure 1). We refer to  $\delta_1$  as the *death rate* of early stage ventures, which reflects the urgency for start-up companies to receive angel investments. The death rate  $\delta_1$  therefore constitutes an indirect cost for entrepreneurs when searching for early stage financing.

Our model includes the standard search model parameters. We denote the individual search cost for entrepreneurs in the early stage market by  $\sigma_1^E$ , and the search cost for angels by  $\sigma_1^A$ . Naturally we focus on the case where the angel market exists, which requires that  $\sigma_1^A$  is not too large. The expected utilities from search in the early stage market is  $U_1^E$  for entrepreneurs, and  $U_1^A$  for angels. We use a standard Cobb-Douglas matching function  $x_1 = \phi_1 \left[ M_1^A M_1^E \right]^{0.5}$  with

<sup>&</sup>lt;sup>1</sup>Allowing early stage investors to finance part of the later stage investment would not change anything. All that matters for the model is that angels do not have enough wealth to finance both stages. Conversely we also assume that VCs cannot be the sole investor in both the early and the late stage market. Our assumptions closely matches industry behavior where early stage investors typically seek syndication partners for the later investment stages.

constant returns to scale, where  $x_1$  is the number of entrepreneur-angel matches in each period, and  $\phi_1 > 0$  is an efficiency measure of the matching technology in the early stage market.

Once matched, the angel and entrepreneur bargain over the allocation of equity. We use the symmetric Nash bargaining solution to derive the equilibrium outcome of this bilateral bargaining game. The angel then invests  $k_1$  in the new venture, and the entrepreneur exerts private effort  $e_1$ . The entrepreneur's disutility of effort  $c(e_1)$  is strictly convex, with c(0) = c'(0) = 0. Note that our model includes entrepreneurial incentives, which allows us to generate predictions about the rate at which entrepreneurs move from the angel to the VC market.

The early stage investment succeeds with probability  $\rho_1(e_1)$ , which is increasing and concave in the entrepreneur's private effort  $e_1$ , with  $\rho_1(0)=0$ ,  $\rho_1'(0)=\infty$  and  $\lim_{e_1\to\infty}<1$ . With probability  $(1-\rho_1(e_1))$  the early stage investment fails and generates a zero payoff; see Figure 1. With probability  $\rho_1(e_1)$  it is successful, in which case there are two possible scenarios: With probability g the venture has a growth option and becomes an attractive candidate for VCs to make the follow-on investment  $k_2$ . With probability 1-g the venture has no further growth option, but can be liquidated, generating the payoff  $y_1>0$ . For our base model we assume that the growth option is sufficiently attractive, so that realizing it is always preferred to liquidation. In Section 7 we relax this assumption by introducing risky growth options, and looking at the optimal choice between growth and liquidation (early exit).

The total number of ventures moving into the VC market in each period is given by  $m_2^E \equiv g \rho_1(e_1) x_1$ . Their owners, namely the respective entrepreneur and angel, then search for a VC investor. Again we assume that the late stage market is monopolistically competitive with free entry. We denote  $m_2^V$  as the endogenous number of VCs entering the market in each period. The equilibrium stock of VCs in the late stage market at a given point in time is  $M_2^V$ , and the equilibrium stock of ventures seeking VC financing is  $M_2^E$ . As for the angel market, we assume that a fraction  $\delta_2 M_2^E$  of business ideas becomes obsolete in each period, generating a zero payoff (see Figure 1). The individual search cost in the late stage market is  $\sigma_2^i$ , and the expected utility from search is  $U_2^i$ , with i=E,A,V. To ensure existence of the VC market, we assume that  $\sigma_2^V$  is not too large. For tractability we assume that entrepreneurs and angels, as joint owners of late stage start-ups, incur the same cost when searching for a VC investor, i.e.,  $\sigma_2 \equiv \sigma_2^E = \sigma_2^A$ . The matching function for the late stage market is  $x_2 = \phi_2 \left[ M_2^V M_2^E \right]^{0.5}$ , where  $x_2$  is the number of start-ups that receive VC financing in each period, and  $\phi_2 > 0$  is a measure of the matching efficiency.

Once the owners of a late stage start-up (entrepreneur and angel) found a VC investor, they all bargain over the allocation of equity, as discussed below. After reaching an agreement the

VC makes the required follow-on investment  $k_2$ .<sup>2</sup> The venture then generates the expected payoff  $y_2 > 0$  (with  $y_2 > y_1$ ).

In the late stage market the bargaining game is between three key players. The Shapley value is widely regarded as the most natural extension of the Nash bargaining solution to games with more than two players. It provides an intuitive allocation of equity, which takes into account the marginal contribution of each party to the forward-looking generation of value. It also implicitly assumes that all prior contracts can be renegotiated. While the entrepreneur and angel may want to commit to a specific equity allocation beforehand, the VC never agreed to that, and could therefore ask that all prior arrangements be ignored. In equilibrium the three parties agree on a division of shares that is determined by their outside options.

Given the simple payoff structure of the model, equity is always an optimal security.<sup>3</sup> The angel investor initially receives an equity stake  $\alpha$  in the early stage. This equity stake can be renegotiated into  $\beta^A$  in case of VC financing. The VC receives an equity stake  $\beta^V$ . The so-called post-money valuation is then given by  $V_1 = k_1/\alpha$  for angel rounds, and  $V_2 = k_2/\beta^V$  for VC rounds.

# 4 Angel market

## 4.1 Bargaining and deal values

We start by looking at how entrepreneurs and angels split the expected surplus when making a deal. Our model consists of two investment stages, so the early stage allocation of surplus naturally depends on the partners' expected utilities from search in the late stage market,  $U_2^E$  and  $U_2^A$ . However, the entrepreneur and angel cannot affect these utilities because of their inability to commit not to renegotiate. The early stage equity allocation therefore only determines how the liquidation value  $y_1$  is split, with the angel receiving  $\alpha y_1$  and the entrepreneur keeping  $(1-\alpha)y_1$ .

<sup>&</sup>lt;sup>2</sup>To keep the analysis of the late stage market with trilateral bargaining games tractable, we abstract from private efforts of entrepreneurs in the late stage. Allowing for private efforts would change the late stage payoff structure; however, this would not qualitatively affect our insights with respect to the interrelationship between both markets, which is the main focus of this paper.

<sup>&</sup>lt;sup>3</sup>While our model set-up is suitable for analyzing valuations, it is not meant to generate insights into financial security structures. Angels and VCs sometimes use more elaborate securities, such as preferred equity or convertible notes (see Kaplan and Strömberg, 2003; Hellmann, 2006). In this model none of these more complicated securities can achieve anything better than simple equity. This is because in case of VC financing, the angel's choice of security is irrelevant – the original contract will get renegotiated anyway. Technically we note that none of the coalition values of the Shapley game depend on the securities held by the angel investor. Moreover, in case of liquidation, there is an exogenous liquidation value, rendering security structures unimportant.

We call the utilities at the time of making a deal the *deal values*, and denote them by  $D_1^E$  and  $D_1^A$ . In the angel market they are given by

$$D_1^E = \rho_1(e_1) \left[ g U_2^E + (1-g)(1-\alpha)y_1 \right] - c(e_1) \tag{1}$$

$$D_1^A = \rho_1(e_1) \left[ g U_2^A + (1-g)\alpha y_1 \right] - k_1. \tag{2}$$

For a given equity allocation  $\alpha$ , the entrepreneur then chooses his private effort  $e_1$  to maximize his deal value  $D_1^E$ . The entrepreneur's optimal effort choice  $e_1^*$  is defined by the following first-order condition:

$$\rho_1'(e_1) \left[ gU_2^E + (1-g)(1-\alpha)y_1 \right] = c'(e_1). \tag{3}$$

We can immediately see that the entrepreneur's effort  $e_1^*$  is increasing in his utility from search in the late stage market,  $U_2^E$ , and decreasing in the angel's equity share  $\alpha$ .

The optimal equity share for the angel,  $\alpha^*$ , satisfies the symmetric Nash bargaining solution, which accounts for the outside option of each party. The outside option for the entrepreneur is to search for a new angel investor, which would give him the expected utility  $U_1^E$ . The angel also searches for a new entrepreneur, but free entry implies  $U_1^A = 0$ . Thus,  $\alpha^*$  maximizes the Nash product  $\left\{\left(D_1^E(e_1^*) - U_1\right)D_1^A(e_1^*)\right\}$ . The optimal  $\alpha^*$  always lies on the downward sloping portion of the bargaining frontier. Formally, let  $\widehat{k}_1$  denote the value of  $k_1$  at which the bargaining frontier has a zero slope, i.e., where  $dD_1^E(e_1^*)/d\alpha = 0$ . Our analysis focus on the case where  $k_1 < \widehat{k}_1$ . In the Online Appendix we show that the angel's equilibrium equity stake  $\alpha^*$  is decreasing in the entrepreneur's outside option  $U_1^E$ .

The Nash bargaining outcome is constrained efficient, i.e., it lies on the utility frontier. However, it does not maximize the joint utility (i.e., the sum of utilities), because of the incentive effect of  $\alpha$ . In fact, joint utility would be maximized at  $\alpha=0$ , where the angel gets no equity, and the entrepreneur is fully self-financed. While our model allows for transfer payments between the two parties, the key assumption is that the entrepreneur has no wealth. If the entrepreneur had wealth, he would always want to make a transfer payment to the angel, to get more equity and improve incentives. By contrast the angel never benefits from making a transfer payment to the entrepreneur, as this would only decrease the entrepreneur's equity stake, and further reduce entrepreneurial effort. In the Online Appendix we formally show that the optimal contract involves no transfer payments.

# 4.2 Market equilibrium

We can now characterize the stationary equilibrium of the angel market. Let  $q_1^E \equiv x_1/M_1^E$  denote the deal arrival rate for entrepreneurs, which measures the probability that an entrepreneur

finds an angel investor at a given point in time. The expected utility of an entrepreneur when searching for an angel investor,  $U_1^E$ , is then defined by the following asset equation:

$$rU_1^E = q_1^E (D_1^E - U_1^E) + \delta_1 (0 - U_1^E) - \sigma_1^E.$$
(4)

This equation says that the discounted expected utility from search equals the expected value of getting a deal  $(q_1^E(D_1^E-U_1^E))$ , minus the expected costs when searching for an angel investor: the risk of the business idea becoming obsolete  $(\delta_1U_1^E)$ , and the direct cost of search  $(\sigma_1^E)$ . Solving the asset equation we find the entrepreneur's expected utility from search  $(U_1^E)$ , and likewise the angel's expected utility  $(U_1^A)$ :

$$U_1^E = \frac{-\sigma_1^E + q_1^E D_1^E}{r + \delta_1 + q_1^E} \qquad \qquad U_1^A = \frac{-\sigma_1^A + q_1^A D_1^A}{r + q_1^A}, \tag{5}$$

where  $q_1^A \equiv x_1/M_1^A$  is the deal arrival rate for angels. Because of free entry, the expected utility from search must be zero in equilibrium. Thus, in equilibrium we have

$$q_1^A D_1^A = \sigma_1^A.$$
 (6)

An entrepreneur with entry cost l will only enter the early stage market if  $l \leq U_1^E$ . Thus, there exists a unique threshold entry cost  $\bar{l}$ , with  $\bar{l} = U_1^E$ , so that entrepreneurs enter as long as  $l \leq \bar{l}$ . The endogenous equilibrium number of entrepreneurs entering the angel market in each period,  $m_1^{E*}$ , is then given by

$$m_1^{E*} = F(U_1^E). (7)$$

Moreover, in a stationary equilibrium the stock of entrepreneurs must be constant. This requires that the total outflow of entrepreneurs – because either their business ideas became obsolete  $(\delta_1 M_1^E)$  or they found an angel investor  $(q_1^E M_1^E)$  – is equal to the equilibrium inflow of entrepreneurs  $(m_1^{E*})$ :

$$\delta_1 M_1^E + q_1^E M_1^E = m_1^{E*}. (8)$$

Likewise, in a stationary equilibrium the outflow of angels  $(q_1^A M_1^A)$  is equal to the (endogenous) inflow of angels  $(m_1^A)$ :

$$q_1^A M_1^A = m_1^A. (9)$$

The equilibrium of the angel market is then defined by conditions (5), (6), (7), (8), and (9). Moreover, since the equilibrium is jointly determined in the angel and VC market, it must also satisfy equations (11) - (15), which we will discuss in Section 5.2.

#### 4.3 Results

Entrepreneurs and angels are forward-looking decision makers who take into account their expected utilities in the VC market, given by  $U_2^E$  and  $U_2^A$ . Thus the angel market equilibrium

depends on the characteristics of the VC market, which is the backward feedback loop. Our model also features a forward feedback loop, where the outflows from the angel market (excluding liquidations and failures) constitute the inflows into the VC market. All of our comparative statics results take into account these two equilibrium feedback loops, i.e., we always consider the joint equilibrium between the two markets. We now discuss the results for the angel market, we characterize the VC market equilibrium in Section 5.2.

It is useful to distinguish between market-level and firm-level effects. On the market level we are interested in the extent of entrepreneurial activities within the economy, which in our model is measured by the equilibrium entry of entrepreneurs  $m_1^{E*}$ . We are also interested in the equilibrium number of angels  $m_1^{A*}$  that enter the market in each period to search for investment opportunities. Related to these two variables of interest is the number of angel-backed deals  $x_1^*$  in each period. In equilibrium the inflow of angels equals the number of early stage deals, i.e.,  $m_1^{A*} = x_1^*$ .

We denote the degree of angel market competition by  $\theta_1^*$ , where  $\theta_1^* = M_1^{A*}/M_1^{E*}$ . It measures the number of angels relative to the number of entrepreneurs, and is commonly known as 'market thickness' in the search literature. This measure of competition is also closely related to the expected time for entrepreneurs to find an angel, which is given by  $1/[\phi_1\sqrt{\theta_1^*}]$ .<sup>4</sup> We call this the fundraising cycle, which is negatively related to the market transparency  $\phi_1$  and to the level of competition  $\theta_1^*$ .

On the firm level we want to understand the determinants of the valuation of angel-backed start-ups. We focus on the post-money valuation as given by  $V_1 = k_1/\alpha$ . We also examine the implications for the success rate of angel investments, as reflected by  $\rho_1(e_1)$ .

For parsimony we derive the equilibrium properties of all these variables in the Online Appendix. The next proposition summarizes our comparative statics results, looking at the effects of the early stage parameters.

#### **Proposition 1** (Angel market – early stage parameters) Consider the angel market.

#### Market-level effects:

- (i) The equilibrium inflow of entrepreneurs  $m_1^{E*}$  is increasing in market transparency  $\phi_1$ , and decreasing in the death rate  $\delta_1$ , the search costs  $\sigma_1^E$  and  $\sigma_1^A$ , and the investment amount  $k_1$ .
- (ii) The equilibrium inflow of angels  $m_1^{A*}$ , and therefore the equilibrium number of early stage deals  $x_1^*$ , is increasing in  $\phi_1$ , and decreasing in  $\sigma_1^A$  and  $k_1$ . The effects of  $\delta_1$  and  $\sigma_1^E$  are ambiguous.

<sup>&</sup>lt;sup>4</sup>Formally, the probability that an entrepreneur finds an angel in a given period is  $x_1^*/M_1^{E^*}$ . Using the definitions of  $x_1$  and  $\theta_1$  we find that the equilibrium probability of finding an angel is  $\phi_1\sqrt{\theta_1^*}$ . Thus, the expected time for entrepreneurs to find an investor is  $1/[\phi_1\sqrt{\theta_1^*}]$ .

(iii) The equilibrium degree of competition  $\theta_1^*$  is increasing in  $\phi_1$ ,  $\delta_1$  and  $\sigma_1^E$ , and decreasing in  $\sigma_1^A$  and  $k_1$ .

## Firm-level effects:

- (i) The equilibrium valuation of early stage start-up companies  $V_1^*$  is increasing in  $\phi_1$ , and decreasing in  $\delta_1$ ,  $\sigma_1^E$  and  $\sigma_1^A$ . The effect of  $k_1$  is ambiguous.
- (ii) The equilibrium success rate of angel investments  $\rho_1(e_1^*)$  is increasing in  $\phi_1$ , and decreasing in  $\delta_1$ ,  $\sigma_1^E$ ,  $\sigma_1^A$ , and  $k_1$ .

Our model generates intuitive comparative statics. Higher costs for angels ( $\sigma_1^A$  and  $k_1$ ) lead to less angel entry (lower  $m_1^{A*}$ ), and therefore to fewer early stage deals (lower  $x_1^*$ ), so that entrepreneurs on average need longer to secure early stage financing. And because search is costly, fewer entrepreneurs find is worthwhile to enter the market (lower  $m_1^{E*}$ ). This makes the angel market less competitive, suggesting that the effect on angel entry is more pronounced (as  $\sigma_1^A$  and  $k_1$  have a first-order effect on  $m_1^{A*}$ , and only a second-order effect on  $m_1^{E*}$ ).

Higher direct and indirect search costs for entrepreneurs ( $\sigma_1^E$  and  $\delta_1$ ) result in fewer entrepreneurs entering the early stage market (lower  $m_1^{E*}$ ). This implies on the one hand fewer investment opportunities for angels (which has a negative effect on  $m_1^{A*}$ ), and, on the other hand, a better bargaining position and higher deal values for angels (which has positive effect on  $m_1^{A*}$ ). While the net effect on angel entry ( $m_1^{A*}$ ) is ambiguous, the angel market becomes more competitive. i.e., the ratio of angels to entrepreneurs increases.

The firm-level effects are best understood by looking at the division of equity between entrepreneurs and angels. We know that higher direct and indirect search costs for entrepreneurs,  $\sigma_1^E$  and  $\delta_1$ , weaken their outside option when negotiating a deal with an angel investor, explaining the lower valuations. Higher costs for angels,  $\sigma_1^A$  and  $k_1$ , also decrease valuations. This is because fewer angels enter the market in equilibrium, so that entrepreneurs have a weaker outside option, needing on average longer to find an alternative investor. A lower valuation means that the entrepreneur needs to give up more equity, which in turn curbs effort incentives (lower  $e_1^*$ ), and therefore results in a lower probability of success (lower  $\rho_1(e_1^*)$ ).

The next proposition provides a comprehensive summary of how the equilibrium of the angel market depends on the determinants of the VC market.

<sup>&</sup>lt;sup>5</sup>Intuitively we would expect  $k_1$  to have a positive effect on the equilibrium valuation  $V_1^*$ . Because  $k_1$  also affects  $\alpha^*$ , which in turn is only implicitly defined by Eq. (A.1), we do not get a clear comparative statics result. However, one can show that  $dV_1^*/dk_1 > 0$  when (i)  $k_1$  is sufficiently small, or (ii) the entrepreneur's effort  $e_1$  is exogenous (so that surplus can be perfectly transferred between entrepreneurs and angels through  $\alpha$ ); see the Online Appendix for the formal proof.

#### **Proposition 2 (Angel market – late stage parameters)** Consider the angel market.

Market-level effects: The equilibrium inflow of entrepreneurs  $m_1^{E*}$ , the inflow of angels  $m_1^{A*}$  (and therefore the number of early stage deals  $x_1^*$ ), and the early stage degree of competition  $\theta_1^*$ , are all increasing in VC market transparency  $\phi_2$ , and decreasing in the death rate  $\delta_2$ , the search costs  $\sigma_2$  and  $\sigma_2^V$ , and the investment amount  $k_2$ .

**Firm-level effects:** The equilibrium valuation of early stage start-up companies  $V_1^*$ , and the success rate of angel investments  $\rho_1(e_1^*)$ , are increasing in  $\phi_2$ , and decreasing in  $\delta_2$ ,  $\sigma_2$ ,  $\sigma_2^V$ , and  $k_2$ .

All cross-market effects are driven by the backward feedback loop. Higher utilities for the entrepreneur and angel investor at the VC stage also benefit the angel market. To fully understand these results we need to draw on some insights about the degree of VC market competition, which we discuss in more detail in Section 5.3. Intuitively a more competitive VC market has the following two effects: First, it reduces the expected time for entrepreneurs and angels to secure follow-on investments from VCs. Second, it improves their bargaining position when striking a deal with a VC, allowing them to capture more of the expected surplus from the investment. Hence a more efficient VC market, as captured by an increase in the market transparency  $\phi_2$ , improves entrepreneurs' and angels' expected utilities from search ( $U_2^E$  and  $U_2^A$ ). This in turn explains why the angel market variables, such as  $m_1^{E*}$ ,  $m_1^{A*}$ ,  $\theta_1^*$ ,  $V_1^*$ , and  $\rho_1(e_1^*)$ , are all increasing in  $\phi_2$ . A similar argument also applies for lower values of  $\sigma_2^V$  and  $k_2$ . However, even though  $\delta_2$  and  $\sigma_2$  both have a positive effect on the level of VC competition (as we will formally show in Section 5.3), we find that the net effect on  $U_2^E$  and  $U_2^A$  is negative. This is because the direct negative effects of these parameters on  $U_2^E$  and  $U_2^A$  always dominate. The angel market variables, such as  $m_1^{E*}$ ,  $m_1^{A*}$ ,  $\theta_1^*$ ,  $V_1^*$ , and  $\rho_1(e_1^*)$ , are therefore decreasing in  $\delta_2$  and  $\sigma_2$ .

It is worth pointing out that cross-market effects have a different logic than within-market effects. This becomes most obvious when looking at the entrepreneurs' search costs. Proposition 1 shows that higher search costs at the angel stage increase angel market competition. This is because of a market power effect, where the angels' stronger bargaining position encourages more angels and fewer entrepreneurs to enter. In contrast Proposition 2 shows that higher search costs at the VC stage decrease angel market competition. This is because of the backward feedback loop, where lower utilities at the VC stage discourage entry and competition at the angel stage. Interestingly the results about the entrepreneurs' search costs are also different from the comparative statics for investors' search costs. Higher VC search costs at the VC stage and higher angel search costs at the angel stage both dampen competition in the angel market.

## 5 VC market

## 5.1 Bargaining and deal values

In the late stage market the owners of each start-up company, the entrepreneur and angel, seek an investment  $k_2$  from a VC. Naturally the angel investment  $k_1$  is now sunk. The total surplus, which we denote by  $\pi$ , is then defined by  $\pi = y_2 - k_2$ . We use the Shapley value to derive the outcome of this tripartite bargaining game. The outside option for the entrepreneur and angel is to go back to the market and search for a new VC investor; the joint value of their outside option is therefore given by  $U_2^E + U_2^A$ . For simplicity we assume that the entrepreneur cannot search without the angel, so that both of their single-coalition values are equal to zero. Intuitively this assumption seems reasonable, as the entrepreneur might need the angel's networks and endorsements to attract the interest of VCs. At the end of Section 6 we relax this assumption. The VC can also search for a new investment opportunity, but free entry implies  $U_2^V = 0$ . For now we assume that the success of a late stage start-up requires the involvement of all three parties, i.e., it is impossible to exclude any of the three partners. In Section 6 we consider a model extension where the entrepreneur and VC can establish a new venture based on the same business idea and exclude the angel investor.

In the Online Appendix we derive the following late stage deal values for the entrepreneur  $(D_2^E)$ , angel  $(D_2^A)$ , and VC  $(D_2^V)$ , using the Shapley value:

$$D_2^E = \frac{1}{3}\pi + \frac{1}{6}\left[U_2^E + U_2^A\right], \quad D_2^A = \frac{1}{3}\pi + \frac{1}{6}\left[U_2^E + U_2^A\right], \quad D_2^V = \frac{1}{3}\pi - \frac{1}{3}\left[U_2^E + U_2^A\right]$$
 (10)

Each entrepreneur and angel gets one-third of the total surplus  $\pi$ , plus a premium which reflects the joint value of their outside option  $(U_2^E + U_2^A)$ . The VC receives the remaining surplus. The equilibrium deal values define the late stage equity shares that all parties agree on, which we denote by  $\beta^i$ , i=E,A,V. For parsimony we state the equilibrium equity shares in the Online Appendix.

# 5.2 Market equilibrium

We now characterize the equilibrium of the VC market. The inflow of start-up companies, denoted by  $m_2^{E*}$ , is endogenously determined by the angel market equilibrium. This forward loop is characterized by the following equilibrium condition:

$$m_2^{E*} = g\rho_1(e_1^*)x_1^* \tag{11}$$

Let  $q_2^E \equiv x_2/M_2^E$  denote the deal arrival rate for entrepreneur-angel pairs, and  $q_2^V \equiv x_2/M_2^V$  the deal arrival rate for VCs. In addition to Eq. (11), the stationary VC market equilibrium is then defined by the following conditions:

$$U_2^A = U_2^E = \frac{-\sigma_2 + q_2^E D_2^E}{r + \delta_2 + q_2^E}$$
 (12)

$$q_2^V D_2^V = \sigma_2^V \tag{13}$$

$$\delta_2 M_2^E + q_2^E M_2^E = g \rho_1(e_1) x_1 \tag{14}$$

$$q_2^V M_2^V = m_2^V. (15)$$

The expected utility for entrepreneurs and angels from search in the late stage market is given by Eq. (12). They are the same because entrepreneurs and angels, as co-owners of a late stage start-up company, have identical search costs ( $\sigma = \sigma_2^E = \sigma_2^A$ ), and identical deal values ( $D_2^E = D_2^A$ ). This simplifies many of our basic comparative statics, although in Section 6 we consider a model extension where the late stage expected utilities of angels and entrepreneurs differ. Condition (13) is the free-entry condition for VCs, which implies that  $U_2^V = 0$  in equilibrium. Condition (14) ensures that the total outflow of new ventures equals the total inflow. Likewise, condition (15) guarantees that the outflow of VCs equals the inflow. The VC market equilibrium is therefore determined by equations (11) - (15). For our analysis we then use the joint equilibrium between both markets, which in fact is characterized by equations (5) - (15).

#### 5.3 Results

For the market-level effects we focus on the entry of VCs  $(m_2^{V*})$ , the number of VC-backed deals  $(x_2^*)$ , and the degree of competition  $(\theta_2^* \equiv M_2^{V*}/M_2^{E*})$ . Again we find that  $m_2^{V*} = x_2^*$  in the stationary equilibrium. Moreover, the measure of competition is inversely related to the VC fundraising cycle, as given by  $1/[\phi_2\sqrt{\theta_2^*}]$ . On the firm level we are interested in how the determinants of the VC market affect the equilibrium valuation of late stage start-up companies. We focus again on the post-money valuation, as given by  $V_2 = k_2/\beta^V$ .

The next proposition summarizes the comparative statics results, focusing on the parameters that are associated with the VC market.

#### **Proposition 3 (VC market – late stage parameters)** Consider the VC market.

#### Market-level effects:

(i) The equilibrium inflow of VCs  $m_2^{V*}$ , and therefore the equilibrium number of late stage deals  $x_2^*$ , is increasing in market transparency  $\phi_2$ , and decreasing in the VC's search

costs  $\sigma_2^V$  and the investment amount  $k_2$ . The effects of the death rate  $\delta_2$  and the entrepreneurs'/angels' search costs  $\sigma_2$  are ambiguous.

(ii) The equilibrium degree of competition  $\theta_2^*$  is increasing in  $\phi_2$ ,  $\delta_2$  and  $\sigma_2$ , and decreasing in  $\sigma_2^V$  and  $k_2$ .

**Firm-level effect:** The equilibrium valuation of late stage start-up companies  $V_2^*$  is increasing in  $\phi_2$  and  $k_2$ , and decreasing in  $\delta_2$ ,  $\sigma_2$  and  $\sigma_2^V$ .

The comparative statics results resemble the effects of early stage parameters for the angel market equilibrium. We therefore do not provide a detailed discussion of the results here, and refer the reader to the explanations right after Proposition 1 in Section 4.3.

The next proposition provides a comprehensive summary of how the equilibrium of the VC market depends on the parameters associated with the angel market.

## **Proposition 4 (VC market – early stage parameters)** Consider the VC market.

#### Market-level effects:

- (i) The equilibrium inflow of start-up companies  $m_2^{E*}$  and VCs  $m_2^{V*}$  are both increasing in market transparency  $\phi_1$ , and decreasing in the angels' search costs  $\sigma_1^A$  and the investment amount  $k_1$ . The effects of the death rate  $\delta_1$  and the entrepreneurs' search costs  $\sigma_1^E$  are ambiguous.
- (ii) The characteristics of the angel market do not affect the equilibrium degree of VC market competition  $\theta_2^*$ .

**Firm-level effect:** The characteristics of the angel market do not affect the equilibrium valuation of late stage start-ups  $V_2^*$ .

The main driver of these results is the forward feedback loop, i.e., the fact that the angel market generates the deal flow to the VC market as show by Eq. (11). We know from Proposition 1 that the early stage matching efficiency  $\phi_1$  has a positive effect on these two equilibrium variables, while the direct and indirect costs for angels,  $\sigma_1^A$  and  $k_1$ , have a negative effect. In equilibrium, a higher inflow of start-ups also encourages more VCs to enter the market. This explains why we obtain identical comparative statics results for  $m_2^{V*}$  and  $m_2^{E*}$ . We also discussed in Section 4.3 why the direct and indirect search costs for entrepreneurs,  $\sigma_1^E$  and  $\delta_1$ , have an ambiguous effect on the number of angel investments, which naturally extends to the inflow of start-ups into the VC market.

Another important insight from Proposition 4 is that while the characteristics of the angel market determine the absolute inflow of start-ups and VCs into the late stage market, they do not

affect the equilibrium ratio of investors to companies  $(\theta_2^*)$ . In other words, when the inflow of start-ups increases by x percent, then the number of VCs entering the market also increases by x percent, so that the investor/company ratio remains constant in equilibrium. As a consequence, angel market parameters do not affect the valuation of late stage companies  $(V_2^*)$ , which depends on the level of competition, but not on the size of the VC market.

# **6** Angel protection

## 6.1 Bargaining and deal values

We already noted that one of the fundamental problems for angels is their limited bargaining power at the VC stage. Their investments are sunk and they cannot finance the deals by themselves. At the bargaining table they solely rely on their contractual rights, especially on their right to refuse the VCs' deal. So far the model assumes that angels enjoy full legal protection, in the sense that they can always prevent the entrepreneur from pursuing the venture without them. In this section we allow for the possibility that the entrepreneur colludes with the VC to exclude the angel investor by implementing the growth option in a new venture that the angel is not part of. From the VCs' perspective, such an exclusion is an opportunistic exercise of their market power. From the entrepreneurs' perspective, it constitutes a hold-up of their original angels.

We model the hold-up opportunity in the following way. Suppose the initial investment was successful, and the venture has a growth opportunity which makes it attractive for VC financing (this happens with probability  $\rho_1 g$ ). The angel has a legal stake in the company, but is not creating value going forward. The entrepreneur could now consider closing down the existing company and incorporating a new venture to implement the growth option, thereby excluding the angel investor. This new venture still needs the late stage investment  $k_2$  from a VC. Closing down the existing venture and starting a new venture is obviously not without challenges. Most notably, the angel could mount a legal claim that the growth option belongs to the existing venture. If starting such a new venture is inefficient, the entrepreneur and VC do not actually start a new venture in equilibrium. However, the threat of doing so improves their bargaining position. This changes the payoffs at the VC stage, which has repercussions for the entire equilibrium across both the angel and the VC market.

In the model we define  $\lambda\pi$  as the total surplus that an entrepreneur and VC can obtain when excluding the angel investor. The parameter  $\lambda\in[0,1]$  measures how dispensable the angel is for the late stage value creation process, and therefore measures the hold-up power of the entrepreneur. For example, if the business model is based on a patented idea, and the patent belongs to the original firm, then the entrepreneur cannot incorporate a new venture based on

the same idea without the angel. The angel is then completely indispensable, so that  $\lambda=0$ ; this was the assumption in the base model. However, if the business idea cannot be fully protected by patents or contracts, the entrepreneur can hold up the angel by incorporating the new venture, generating a surplus  $\lambda\pi$ , with  $\lambda\in(0,1)$ . The angel is completely dispensable for  $\lambda=1$ .

Consider now the case of  $\lambda \in (0,1)$  where angel protection is imperfect. The threat of a new incorporation weakens the angel's bargaining position, and forces him to agree to a lower equity stake  $(\beta^A)$  compared to our base model with  $\lambda = 0$ . Formally, for the Shapley value the joint surplus for the entrepreneur-VC subcoalition (which excludes the angel investor) is now given by  $\lambda \pi$ . For now we continue to assume that at the search stage the entrepreneur always needs the angel (we relax this assumption below). This implies that their single-coalition values are still zero. In the Online Appendix we derive the following new deal values for the late stage market:

$$D_2^E = \frac{1}{6} [2 + \lambda_A] \pi + \frac{1}{6} [U_2^E + U_2^A], \quad D_2^A = \frac{1}{3} [1 - \lambda_A] \pi + \frac{1}{6} [U_2^E + U_2^A], \quad (16)$$

$$D_2^V = \frac{1}{6} [2 + \lambda_A] \pi - \frac{1}{3} [U_2^E + U_2^A]. \tag{17}$$

For now fix the expected joint utility from search for the entrepreneur and angel  $(U_2^E + U_2^A)$ . We can then see that weaker angel protection (higher  $\lambda$ ) leads to a lower deal value for the angel  $(D_2^A)$ , and to higher deal values for the entrepreneur  $(D_2^E)$ . For the VC there is no prior contractual relationship with the angel, so we cannot talk of hold-up power. Still, lower angel protection improves the VC's bargaining position and leads to a higher deal value  $(D_2^V)$ . Of course, the equilibrium effect of  $\lambda$  is more complex, as  $\lambda$  also affects the outside options of entrepreneurs and angels  $(U_2^E, U_2^A)$ .

#### 6.2 Results

The next proposition sheds light on how the level of angel protection affects the angel and VC market equilibrium.

**Proposition 5** The effect of late stage hold-up of angels, as measured by  $\lambda$ , is as follows:

(i) Early stage: The equilibrium inflow of entrepreneurs  $m_1^{E*}$ , the inflow of angels  $m_1^{A*}$  (and therefore the number of early stage deals  $x_1^*$ ), the early stage degree of competition  $\theta_1^*$ , and the equilibrium valuation of early stage start-ups  $V_1^*$ , are all decreasing in the hold-up parameter  $\lambda$ . In contrast, the equilibrium success rate of angel investments  $\rho_1(e_1^*)$  is increasing in  $\lambda$ .

(ii) Late stage: The late stage degree of competition  $\theta_2^*$  is increasing in  $\lambda$ , while the valuation of late stage start-ups  $V_2^*$  is decreasing. The effect of  $\lambda$  on the equilibrium inflow of start-up companies  $m_2^{E*}$  and inflow of VCs  $m_2^{V*}$  is ambiguous.

The analysis of angel protection highlights the core tension in the relationship between angels and VCs, as summarized by Holstein's quote in the introduction. At the individual deal level there is a relationship of 'foes', where VCs are happy to collude with entrepreneurs to weaken the angels' bargaining position. Yet for the market level there is also a need for 'friendly' relations, as VCs collectively rely on the angel market for their deal flow. A similar observation pertains to the relationship between angels and entrepreneurs, where at the ex-post deal level, entrepreneurs may like the idea of taking advantage of their angels. However, from an ex-ante perspective, this behavior makes it less attractive for angels to invest in the first place, undermining the collective self-interest of entrepreneurs.

Proposition 5 generates several important insights into the net effects of these competing forces. Consider first the relationship between angels and entrepreneurs. We already saw that weaker angel protection (higher  $\lambda$ ) provides entrepreneurs with higher deal values at the VC stage. By itself this should encourage more entrepreneurs to enter the early stage market. Then, why do fewer choose to enter the market in equilibrium? The reason for this is the diminished supply of angels. Weaker protection at the VC stage makes angel investing less attractive, so fewer angels enter the market. This means that each entrepreneur needs to search on average longer to secure start-up financing, with more ventures dying before ever raising any angel capital. This makes entry less attractive for entrepreneurs. The key insight from Proposition 5 is that the ex-post rent-capture effect is dominated by the ex-ante effect of a thinner angel market. In equilibrium we observe not only less entry by angels, but also less entry by entrepreneurs. Moreover, the angel market is less competitive with longer fundraising cycles.

One might have expected that a less competitive angel market would have resulted in lower valuations and weaker entrepreneurial incentives. Proposition 5 indeed finds that higher  $\lambda$  leads to lower angel valuations. This is because angels are compensated for the expected hold-up by receiving larger equity stakes upfront (i.e., higher  $\alpha^*$ ). However, we also find that a higher  $\lambda$  actually strengthens entrepreneurial incentives (i.e., higher  $e_1^*$ ), and therefore also improves the success rates at the angel stage (i.e., higher  $\rho_1(e_1^*)$ ). The reason is that entrepreneurs are only partly motivated by their payoffs in case of liquidation (given by  $(1-\alpha^*)y_1$ ). The other relevant payoff is in case of entering the VC market, where a higher  $\lambda$  gives them a higher ex-post deal value  $(D_2^E)$ . Our analysis shows that the latter effect dominates the former. We therefore obtain the surprising conclusion that while weaker angel protection reduces entrepreneurial entry, it actually increases entrepreneurial incentives and success rates at the angel stage.

One interesting consequence of this tension between lower entry rates and higher success rates is that the effect of  $\lambda$  on the outflow into the VC market (as measured by  $m_2^{E*}$ ) is ambiguous. This is precisely because  $\lambda$  has a negative on the size of the angel market  $x_1^*$ , but a positive effect on the success rate  $\rho_1(e_1^*)$ . We can identify cases where one effect dominates the other. If, for example, entrepreneurial incentives are unimportant so that  $\rho_1'$  is close to zero, then the market size effect always dominates, and  $m_2^{E*}$  is decreasing in  $\lambda$ . However, if entrepreneurial incentives are important, the supply of entrepreneurs is sufficiently inelastic, and there is little urgency ( $\delta_1$  close to zero), then the market size effect is small; the success effect dominates, and  $m_2^{E*}$  becomes increasing in  $\lambda$ .

We are now in a position to understand the effect of angel protection on the VC market. With weaker angel protection (i.e., higher  $\lambda$ ), VCs can strike better deals, so investing in late stage start-ups becomes more attractive. This is a 'foes' effect and encourages entry into VC. However, there is also a 'friends' effect through the supply of new deals into the VC market  $(m_2^{E*})$ . As noted in the previous paragraph, the effect of  $\lambda$  on  $m_2^{E*}$  is ambiguous, so we cannot sign the effect of  $\lambda$  on  $x_2^*$  in general. For the particular case with little urgency and an inelastic supply of entrepreneurs, both the 'foes' and the 'friends' effect point in the same direction, so that the VC market size  $x_2^*$  is increasing in  $\lambda$ . For all other cases, the 'foes' and 'friends' effects point in different directions, so that the effect of  $\lambda$  on  $x_2^*$  depend largely on the elasticity of entrepreneurial entry.

While the effect of  $\lambda$  on the size of the VC market remains ambiguous, Proposition 5 shows that our model generates the unambiguous result that weaker angel protection makes the VC market more competitive. The key intuition is that the degree of competition is a relative measure, and does not depend on the level of inflows into the VC market  $(m_2^{E*})$ . Instead, the level of competition is driven by the modified late stage deal values in Section 6.1, with higher rents for VCs attracting more VC entry per unit of deal inflow.

Proposition 5 finally shows that weaker angel protection also leads to lower VC valuations. The main intuition is simply that weaker angel protection gives the VCs more bargaining power. Note, however, that this is a different rationale from the lower valuations in the angel market, which was because angels are being compensated for future hold-up problems.

The analysis so far assumes that angels are dispensable at the bargaining stage, but not at the search stage. This simplifies the analysis by keeping all single-coalition values at zero. However, in the Online Appendix we show that nothing depends on this simplification. We provide a model extension where the entrepreneur can search for a VC without the angel. When searching together, the entrepreneur and angel have symmetric search costs ( $\sigma_2^E = \sigma_2^A = \sigma_2$ ), so that their total search costs are  $2\sigma_2$ ; when searching alone we assume that the entrepreneur has search costs  $\gamma\sigma_2$ , with  $\gamma>2$ . For sufficiently large values of  $\gamma$  the model is the same as before, because searching alone is dominated by stopping. For more moderate values of  $\gamma$ , however,

searching alone is a credible threat that affects the equilibrium deal values. In particular, the entrepreneur now has a positive single-coalition value  $U_2^E(\gamma, \lambda \pi)$  that is increasing in  $\lambda$  and decreasing in  $\gamma$ . In the Online Appendix we show that, even though the equilibrium is now defined by three simultaneous equations, the results from Proposition 5 continue to hold.

# 7 Early exits

So far our analysis takes it for granted that angels always want to bring their companies to the VC market. However, some angels argue that it is better to avoid the VC market altogether, and instead take an early exit (see Peters, 2009). Egan (2014) also shows that start-up companies could redirect their technology strategies towards getting acquired when opportunities for follow-on funding diminish. In this section we consider the endogenous choice of angels and entrepreneurs to take the more risky option of seeking VC financing, versus the safer option of selling the company at an early stage.

To model the endogenous choice between entering the VC market versus an early exit, we consider the simplest possible model extension. In our base model we assumed that a successful project faces one of two scenarios: either the company has a growth option, in which case it is always optimal to raise VC funding; or the company does not have a growth option, in which case it is liquidated (generating the payoff  $y_1$ ). In this section we augment our base model by allowing entrepreneurs and angels to choose between two different commercialization strategies. After achieving success with the initial investment (which happens with  $q\rho_1$ ), entrepreneurs and angels can either choose the safe strategy of selling what they have and taking the liquidation value  $y_1$  (early exit). Or they can pursue the risky option of developing their growth option and seeking out VC financing; see Figure 1. We assume that the entrepreneur and angel receive a signal about the success probability of developing a growth option. Let  $\gamma$  be the probability that the venture develops the growth option and becomes ready for VC financing. However, with probability  $1-\gamma$  the growth option does not work out, so that the venture fails and is worth nothing. That is, by exploiting growth opportunities, the entrepreneur and angel forgo the chance to sell a more market-ready project at price  $y_1$ . In our base model we essentially assumed that  $\gamma = 1$ . Now we assume that  $\gamma$  is a random variable with some distribution  $\Omega(\gamma)$ and support [0,1]. For simplicity we assume that the realization of  $\gamma$  is verifiable.<sup>6</sup>

The entrepreneur and angel investor agree ex-ante on an optimal  $\gamma^*$ , so that they choose an early exit if and only if  $\gamma \leq \gamma^*$ . It is easy to see that  $\gamma^*$  satisfies  $\gamma^* = y_1/(U_2^E + U_2^A)$ . A

<sup>&</sup>lt;sup>6</sup>Assuming that the signal is observable but not verifiable adds some technical complications, but does not affect the main insight. With observability, the entrepreneur and angel can always renegotiate an inefficient decision. The main issue is that the entrepreneur is wealth constrained, which constrains renegotiation choices. This renegotiation closely resembles the analysis in Hellmann (2006).

higher value of  $\gamma^*$  means that the entrepreneur and angel are more likely to choose the safe over the risky option. Thus  $\gamma^*$  measures the equilibrium preferences for the safe project. The next proposition examines how  $\gamma^*$  depends on the characteristics of the VC market.

**Proposition 6** The equilibrium preference for safe projects  $\gamma^*$  is increasing in the death rate  $\delta_2$ , the search costs  $\sigma_2$  and  $\sigma_2^V$ , and the investment amount  $k_2$ , and decreasing in market transparency  $\phi_2$ .

Proposition 6 establishes how the commercialization strategies of entrepreneurs are affected by the structure of the VC market. Entrepreneurs and angels avoid the VC market more often when securing follow-on investments is more costly (higher  $\sigma_2$  and  $\delta_2$ ). The same applies when fewer VCs search for investment opportunities (due to higher  $\sigma_2^V$  and  $k_2$ ), so that on average entrepreneurs and angels search longer before receiving VC. In equilibrium we observe more small entrepreneurial projects, and fewer risky projects that rely on large scale (VC) investments.

A related and interesting question is how the level of angel protection affects the early stage project choice. Consider again our model extension from Section 6, where the parameter  $\lambda$  measures the entrepreneur's late stage hold-up power. We obtain the following result:

**Proposition 7** *More severe hold-up of angels in the late stage market leads to more safe projects being implemented in equilibrium (i.e.,*  $d\gamma^*/d\lambda > 0$ ).

Proposition 7 shows how the level of angel protection affects the commercialization strategies of early stage ventures. We know from the modified late stage deal values in Section 6.1 that, ceteris paribus, less protection means that angels get a smaller and entrepreneurs a larger share of the total surplus  $\pi$ . We formally show in the Online Appendix (see Proof of Proposition 5) that this translates into a lower expected utility for angels  $(U_2^A)$ , and a higher expected utility for entrepreneurs  $(U_2^E)$ . However, VCs also capture a part of the surplus from angels, so that the net effect on the joint utility of angels and entrepreneurs  $(U_2^A + U_2^E)$  is negative. This implies that the anticipation of more severe hold-up of angels in the late stage market discourages owners of early stage ventures to exploit growth opportunities through raising VC.

# 8 Empirical predictions

Our theory has a large number of comparative statics results. In principle all of these generate empirical predictions. In this section we explore in depth those predictions that are empirically most relevant.

## 8.1 Dependent variables

Our model makes predictions about several endogenous outcomes that all lend themselves to be used as dependent variables. At the market level, our model makes predictions about the size of the angel and VC market, i.e. the rate at which angels and VCs make investments. Such market activities are regularly tracked by governments and commercial data providers. While there are important measurement challenges with tracking private deals, electronic data collection has vastly improved the quality of such data in recent years. Our model also endogenizes the number of entrepreneurs, distinguishing between those that are seeking funds and those that actually succeed in raising funds. On electronic matchmaking platforms, such as Angellist, it is now possible to empirically distinguish between companies merely seeking versus actually finding investments.

Another important endogenous variable is the level of competition in the angel and VC market. The most immediate measure is the ratio of investors willing to invest, relative to the number of entrepreneurs seeking funds. The challenge is that this requires estimates for the number of potential investors, as opposed to actual investors. As mentioned above, it is sometimes possible to measure the number of entrepreneurs seeking funds. However, estimating the number of investors that are truly willing to invest remains challenging. Intriguingly, our search model also suggests an alternative measurement approach. As shown in Sections 4.2 and 5.2, the level of competition in a market is inversely related to the length of fundraising cycles, i.e., the expected time to complete a fundraising campaign. This is simply because for a given level of market transparency, greater competition implies shorter expected search time. The interesting observation is that online search markets naturally record the time it takes to raise funds on the platform. This might therefore be used as a proxy for the level of competition.

Beyond this market-level analysis, our model also generates predictions at the company level. In particular, the model allows for endogenous pricing of deals, expressed as post-money valuations. These valuations in turn imply equity stakes for the entrepreneurs, which can be used as a measure for entrepreneurial incentives. In addition, our model generates predictions about entrepreneurial outcomes, namely the rate at which start-ups survive, the rate at which they move from the angel to the VC market, and the rate at which they experience early or late exits. All of these are standard measurable outcomes.

# 8.2 Key independent variables and their predictions

Our theory contains a large number of exogenous model parameters. We focus here on those that are particularly relevant for empirical evaluations. We consider alternative explanations for the recent rise of angels, and ask what additional predictions are associated with each of these explanations.

#### **8.2.1** Angel protection

One argument for the rise of angel investing that angels have become more experienced and sophisticated. This could be because of the creation of national angel investor associations, and the rise of organized angel groups and angel networks (OECD, 2011). According to this argument angels learn over time how to better protect themselves against hold-up in a variety of legal and strategic ways (Leavitt, 2005). Our model predicts that better angel protection leads to a larger and more competitive angel market, more entrepreneurial entry, higher angel valuations, and a higher probability of success. Angel protection has an ambiguous effect on the size of the VC market, but unambiguously decreases VC competition. Thus better angel protection has opposite effects on the level of competition of angel and VC markets, which also implies shorter fundraising cycles in the angel market, but longer ones in the VC market. Finally, better angel protection encourages late over early exits.

The main empirical challenge for testing these predictions is to find credible proxies for angel protection. We propose three different approaches. First, one can examine cross-country variations in the quality of legal protection. A large prior literature focuses on the legal origin in terms of common versus civil law, as well as indices of legal enforcement and minority shareholder protection (see Glaeser and Shleifer, 2002; La Porta et al., 2000). Second, within countries, entrepreneurs' hold-up power is likely to differ across industry sectors. For example, ideas in the software sector are likely to be more portable across ventures, whereas ideas in the life sciences tend to be associated with patents and physical devices that can be better protected. Third, even within sectors there is likely a variation in the relative importance of contractible assets (e.g., physical assets, patents) versus "non-contractible" assets (e.g., non-patented ideas, customer knowledge, entrepreneurial skills). For each of these three approaches it is possible to exploit cross-sectional (and possibly time-varying) variations in the level of angel protection.

#### 8.2.2 Start-up costs

A popular argument for the rise of angels is that the cost of starting a business has dramatically declined in recent years. This phenomenon has been widely discussed in the popular press (The Economist, 2014), and is related to the so-called "lean startup" movement (see e.g. Ries,

<sup>&</sup>lt;sup>7</sup>A related but different approach is to focus on cross-country or inter-state differences in the strength of intellectual property protection. The main hypothesis is that stronger IP protection better protects angels from hold-up by entrepreneurs. Hyde (1998) discusses differences in the enforcement of trade secrets; the work of Gilson (1999) and Marx, Strumsky and Fleming (2009) emphasizes the role of non-compete agreements.

2011; Blank, 2013). In our model, lower start-up costs lead to more entry of entrepreneurs, and even more entry of angels. Overall this generates a more competitive angel market, and results in shorter fundraising cycles. Lower start-up costs also imply lower equity stakes for angels, generating better entrepreneurial incentives and thus higher success rates. All this increases the rate at which angel-backed companies enter the VC market. Free entry ensures that the VC market expands in size accordingly.

For the empirical measurement we can imagine several approaches. One simple approach is to directly exploit the variation in the size of seed investment rounds to look at the role of start-up costs. Another approach is to exploit time variation. Ewens, Nanda and Rhodes-Kropf (2014), for example, argue that the introduction of Amazon's Elastic Compute Cloud (EC2) services lowered the cost of starting a company. Yet another approach is to combine the time variation with some cross-sectional variations. For example, Amazon's EC2 is likely to have a bigger effect on web-based start-ups rather than 'bricks and mortar' start-ups.

#### 8.2.3 Market transparency

Another argument for the rise of angel investing is that angel markets have become more transparent, mostly because of the rise of internet-based investment platforms. Angellist is currently the market leader, but a number of other "crowdfunding" platforms also compete in this space (Nanda and Kind, 2013). So-called "seed accelerators" are likely to further increase the transparency of angel markets.

In our model greater angel market transparency leads to more entry by entrepreneurs, and even more entry by angels. Greater competition leads to higher valuations and better entrepreneurial incentives. Interestingly all of these changes in the angel market imply that the VC market should also expand in size. Moreover, if these electronic platforms also increase the transparency of VC markets, our model further predicts additional entry of VCs, with more competition, shorter fundraising cycles, and higher valuations.

The advent of online investment platforms provides a unique natural experiment for testing these predictions. We can think of two alternative approaches. One approach is to consider a market before and after the adoption of online platforms. This approach might also leverage regional variations in the speed of adoption of online platforms. A second approach is to consider variations in transparency within an online platform. Online platforms themselves are evolving in the way they work, changing their rules of what information gets disclosed.

#### **8.2.4** Entrepreneurial urgency

One could ask how the rise of angels is related to competition among entrepreneurs. Our urgency parameter  $\delta_1$  and  $\delta_2$  captures the competitive pressure for entrepreneurs. The most inter-

esting prediction is that greater urgency leads to a more competitive angel market with shorter fundraising cycles, yet it also leads to lower angel valuations.

The most direct approach to empirically measure urgency is to look at the failure rate of *unfunded* entrepreneurs. Again, this is much easier to observe in online platforms than in traditional data sources. However, because higher failure rates could also be due to lower competition, it is important to separately control for the level of competition (as discussed in Section 8.1 above). Another more indirect approach would be to look at measures of entry and product market competition in fairly narrowly defined industries. Or one could try to measure the length of product development, or the speed at which products or patents become obsolete. For example, it is widely believed that markets moves faster in software than in the life sciences.

#### 8.2.5 VC supply shocks

Finally we examine the possibility that the recent rise of angel investing is due to a retrenchment from venture capital.<sup>8</sup> In our model we capture this (somewhat simplistically) with changes in the VCs' costs, as measured by  $\sigma_2^V$ . Higher VC costs naturally lead to a smaller supply of VC funding. The model then shows that this also implies a less competitive VC market. Most importantly, a supply shock to VC leads to a smaller and less competitive angel market. Valuations are also lower in both markets. The model also predicts a relative increase in early over late exits.

We note that the main empirical predictions do not seem to fit the recent market patterns, where a retrenchment from the VC market was accompanied by a rise in angel investing. This suggests that a supply shock to VC is unlikely to be the sole or main driver behind the recent rise of angel investing.

Overall we note that our theory generates a rich set of empirical predictions. Any empirical analysis would naturally also have to tackle issues of sample selection and econometric identification. However, that is clearly beyond the scope of this theory paper.

# 9 Conclusion

In this paper we develop a theory of the interactions between angel and venture capital markets. Entrepreneurs receive their initial funding from angels, but may need follow-on funding from

<sup>&</sup>lt;sup>8</sup>Historically VC markets have experienced significant supply shocks (see Gompers and Lerner, 2001). Several approaches have been suggested in the prior literature to identify supply shocks to VC, focusing mainly on investment conditions at the limited partner level. Samila and Sorenson (2011) use the returns to local university endowments as an instrument for local VC availability. Mollica and Zingales (2007) adopt a similar approach using the returns of US state pension funds.

venture capitalists. On the one hand the two investor types are 'friends', in the sense that they rely upon each other's investments. On the other hand they are 'foes', because venture capitalists no longer need the angels when they make their follow-up investments. The venture capitalists' bargaining power depends on how competitive venture markets are, and how well angels are legally protected. Using a costly search model we establish a joint equilibrium across the two markets, and endogenously derive the size and competitive structure of both markets. We also identify determinants of angel and venture capital valuations, and generate predictions about the rate at which entrepreneurs proceed across the two markets, and whether they choose strategies to exit early or late. We relate the theory to the recent rise of angel investments, exploring alternative explanations concerning the cost of starting a business, the transparency of angel markets, and the ability of angels to better protect their investments.

Our analysis opens doors for further research into the relationship between early and late investors. One limiting assumption of standard search models is that all types are homogenous. Allowing for heterogenous types is technically much more complicated, but it would allow for a richer set of feedback loops, in particular introducing the possibility that entrepreneurs make endogenous decisions at the angel stage that affect the quality of their deals at the VC stage. A different but equally interesting issue is to what extent investors can build reputations and networks that limit the extent of counter-productive hold-up. Finally, our framework raises some interesting policy questions. For instance, if a government wanted to subsidize VC (presumably because of other market failures), would a subsidy to angels be more or less efficient than a subsidy to VCs? We hope that future research, by ourselves and others, will help to illuminate these important set of next questions.

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