

**Understanding and mapping
water resources by
multidimensional statistics
and fuzzy logic:
Missouri River basin case**

Boris Shmagin & Din Chen

2006 Western SD Hydrology Conference April 18, 2006
Rushmore Plaza Civic Center – Rapid City, South Dakota

Photo courtesy of Carol Johnston, 2004

Topics

- Spatial-temporal variations of stream runoff for Upper Missouri River watershed

- * Hydrologic regime as structure

- * Land cover or landscape

- * Map with fuzzy boundaries

- * Applications

- * Decision making about water resources or Scientist vs. Lawyer



Experimental Program to Stimulate Competitive Research

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**U.S. EPA - Science To Achieve
Results (STAR) Program**

Grant # **R829643**

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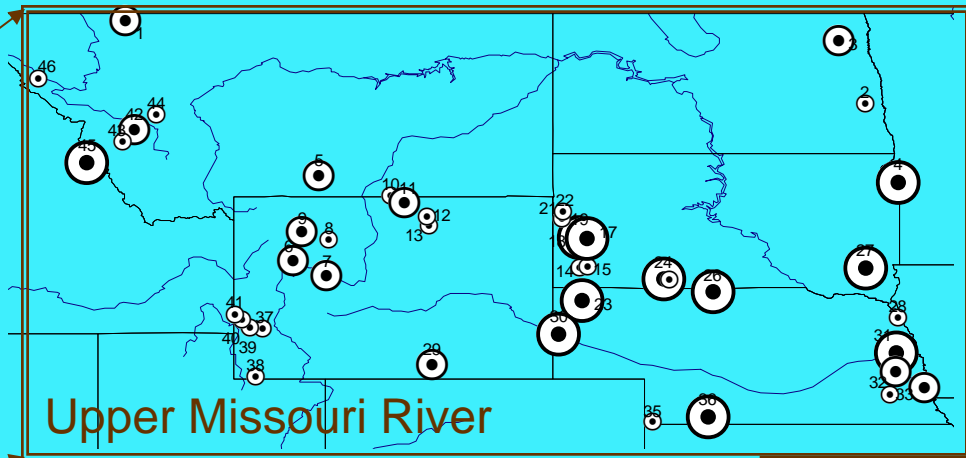
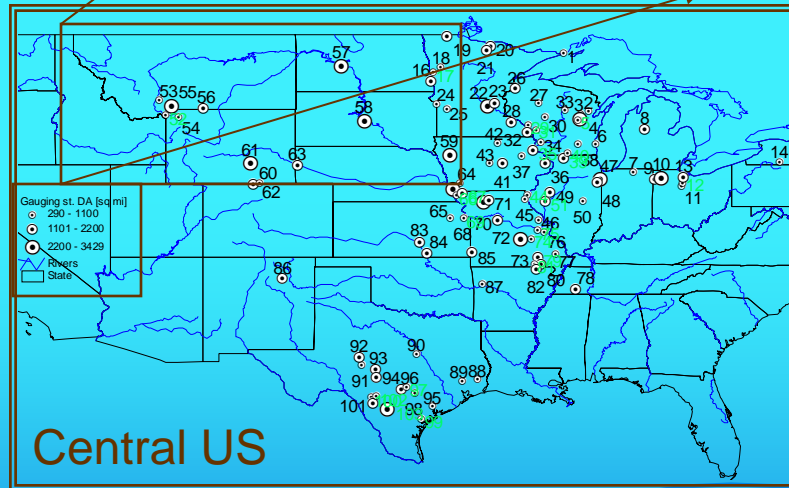
- * Applications

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Matrixes for statistical analysis

Gauging station locations and drainage area (DA) distribution for Central US (DA: 290-3429 sq mi) & Upper Missouri River (DA: 113-398)



Initial Matrixes:

$$\{Q_{UMR}^{28 \times 46}\} \text{ \& \ } \{Q_{US}^{31 \times 101}\}$$

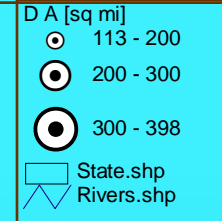
Factor analysis:

$$Q_{t^*p} = F_{t^*k} * A_{k^*p} + E_{t^*p}$$

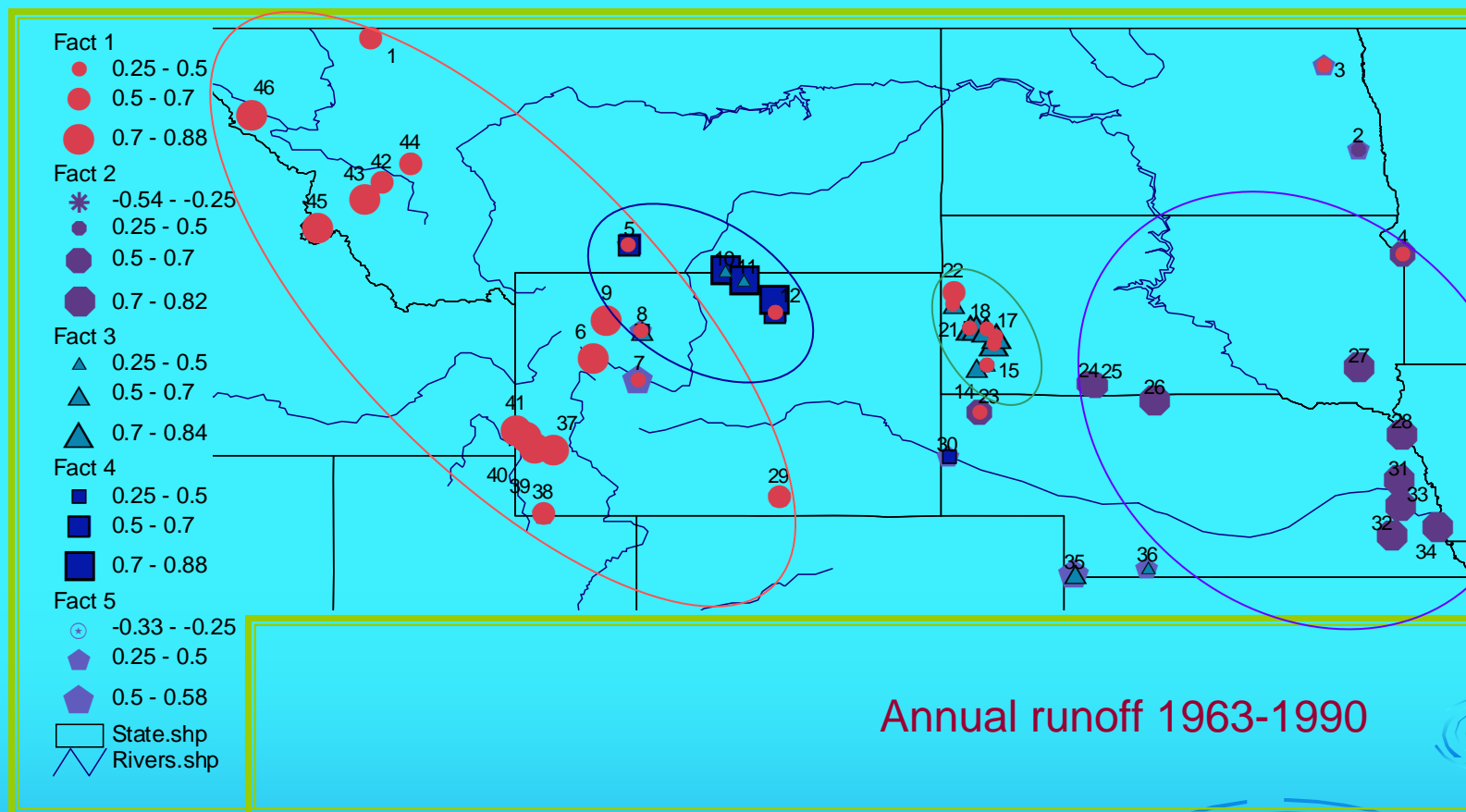
Matrixes of results:

A_{k^*p} – factor loadings,
as dimensions of process (k),
grouping by types of regime (p);

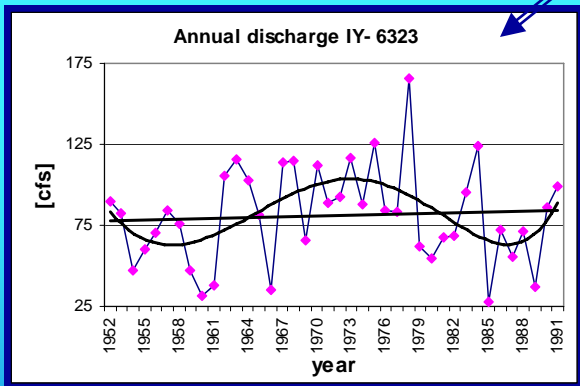
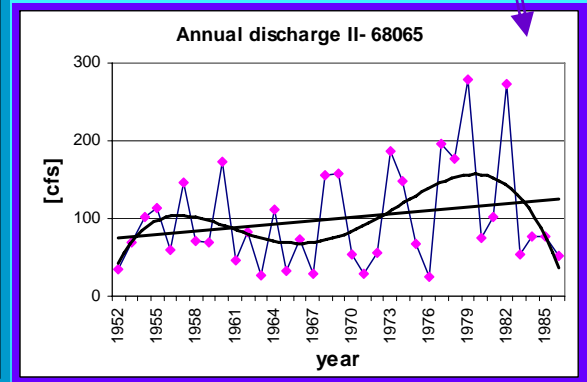
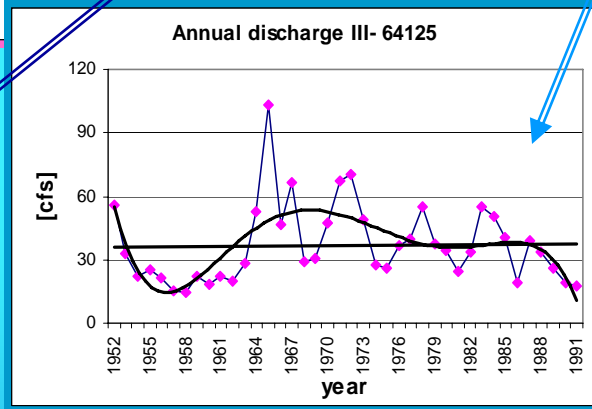
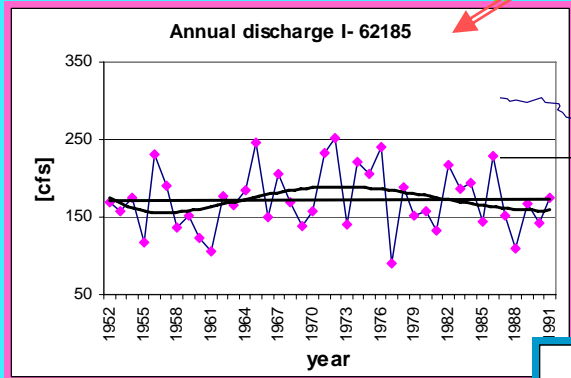
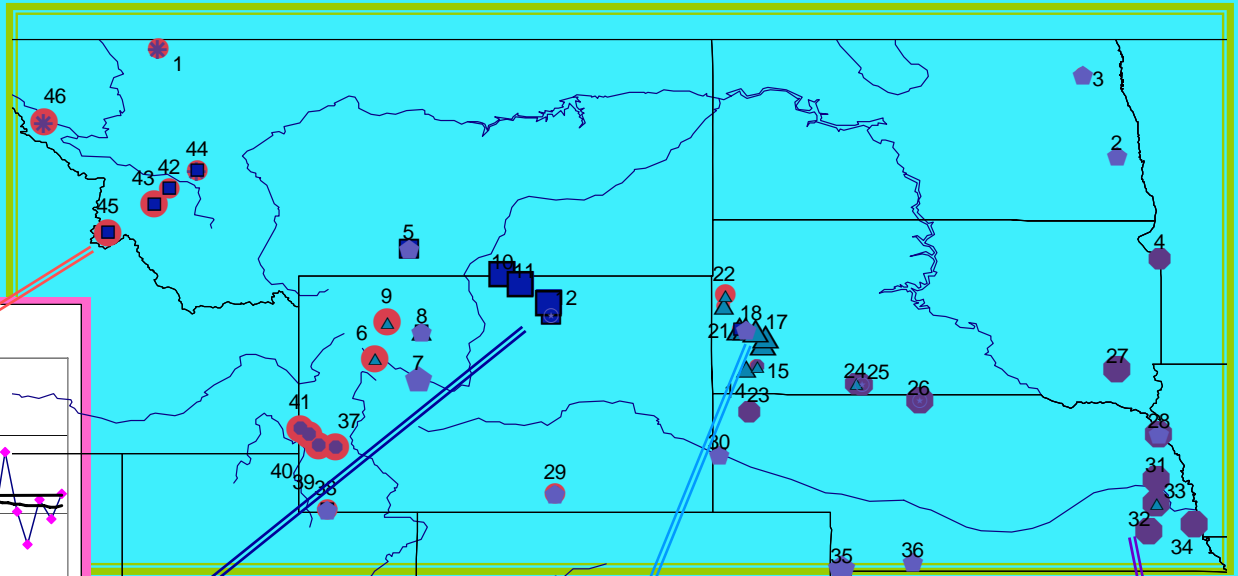
F_{t^*p} – factor scores,
as components for types of regime



Factor Loadings of 46 gauging stations



Patterns of stream runoff in Upper Missouri



Factor Loading of 46 gauging stations and graphs of annual runoff 1953 -1990 for four typical watersheds

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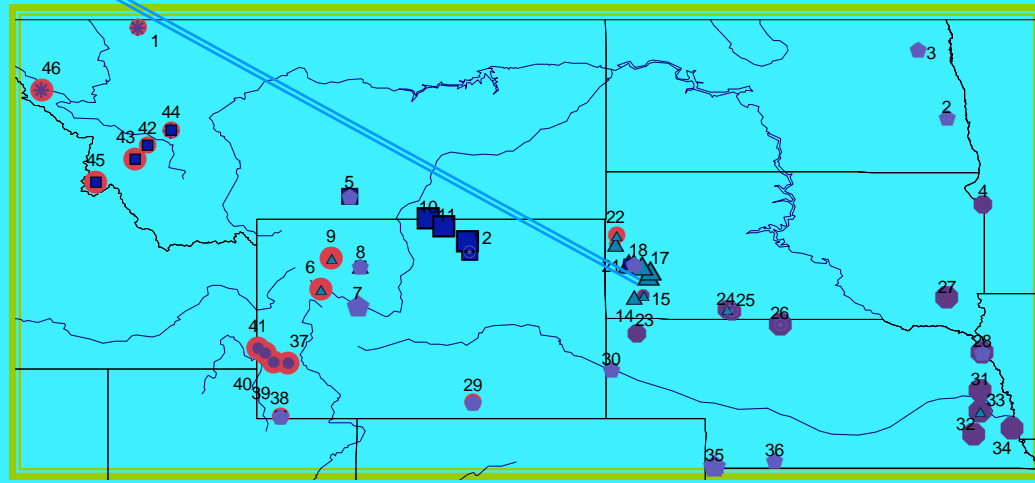
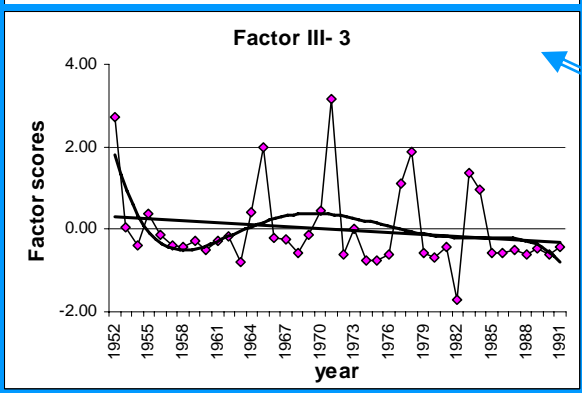
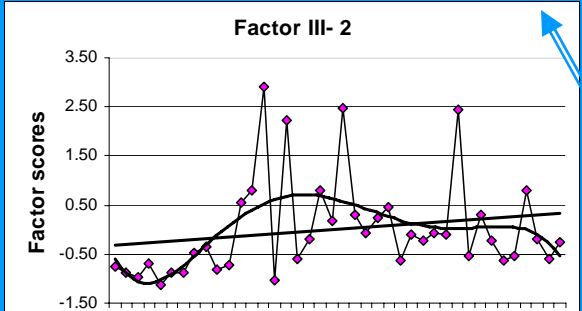
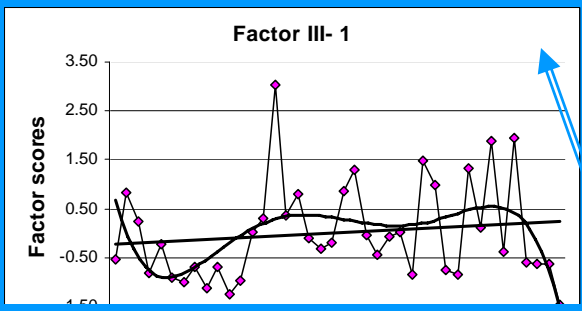
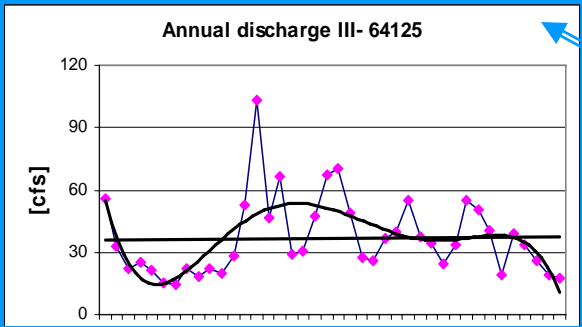


Table of seasonal runoff for four typical watersheds

	October	November	December	January	February	March	April	May	June	July	August	September	Annual	Expl. Var.
Factor I- 1						0.31			0.90	0.86	0.94	0.83	0.93	4.25
Factor I- 2	0.80	0.80	0.87	0.83	0.78	0.50								3.63
Factor I- 3						0.33	0.83	0.78						1.58
Factor II- 1	0.84	0.91	0.93	0.83	0.43	0.27	0.41	0.40					0.43	3.91
Factor II- 2					0.62		0.57	0.62	0.88				0.69	2.47
Factor II- 3	0.37				-0.25			0.43			0.88	0.44	0.29	1.55
Factor II- 4						0.60	0.44			0.76		0.56	0.46	1.72
Factor III- 1	0.79	0.81	0.93	0.85	0.85	0.79	0.45						0.37	4.75
Factor III- 2									0.72	0.90	0.90	0.88	0.64	3.42
Factor III- 3							0.70	0.90	0.49				0.64	2.12
Factor IV- 1	0.84	0.90	0.84	0.77	0.70	0.52	0.56						0.81	3.98
Factor IV- 2									0.84	0.88	0.31		0.46	2.43
Factor IV- 3						0.67					0.62	0.86		1.79
Factor IV- 4				0.38			0.38	0.88	0.30					1.68

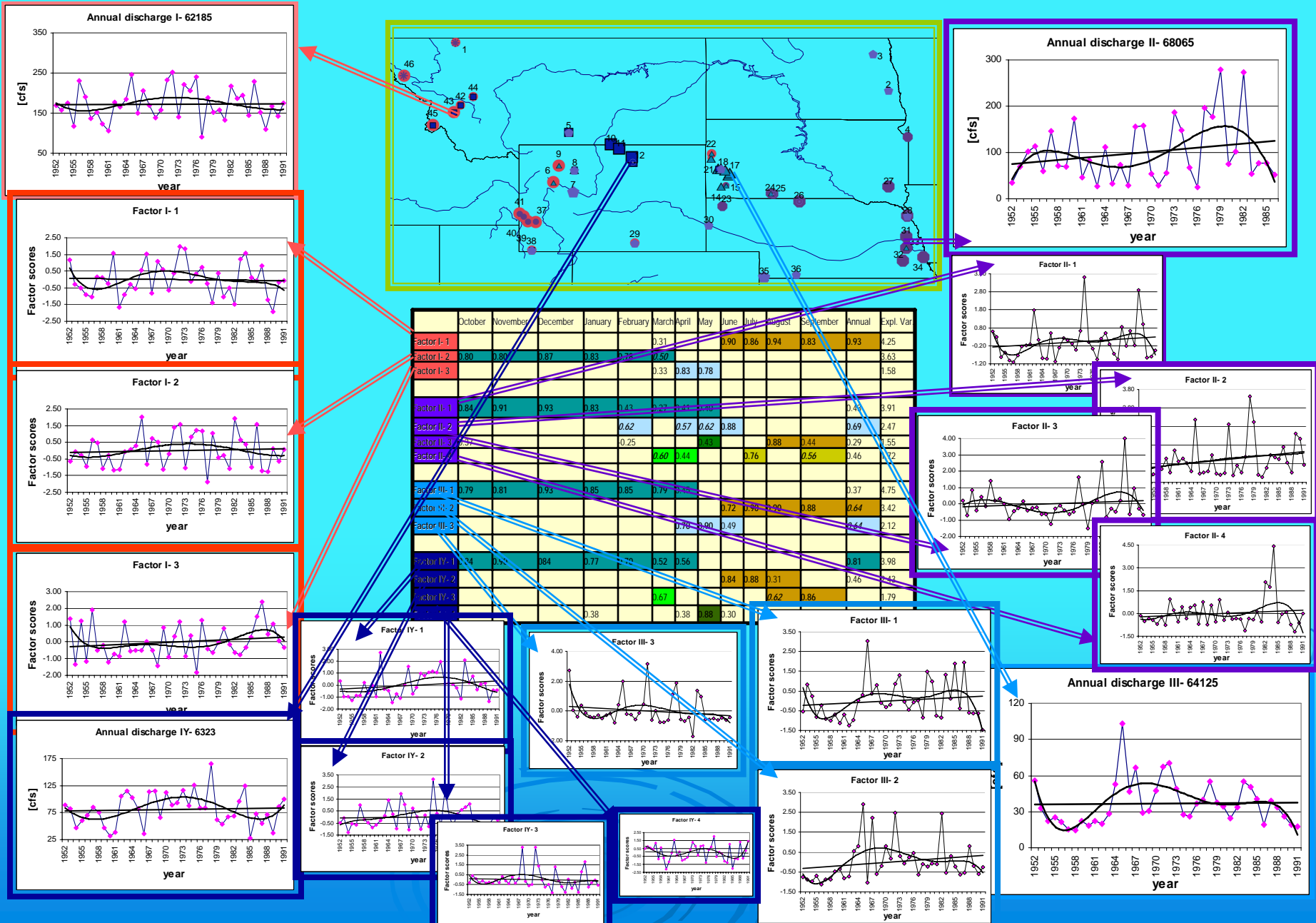
Different number of seasons, composition and influence on annual

Annual and seasonal stream runoff of third regime type in Upper Missouri

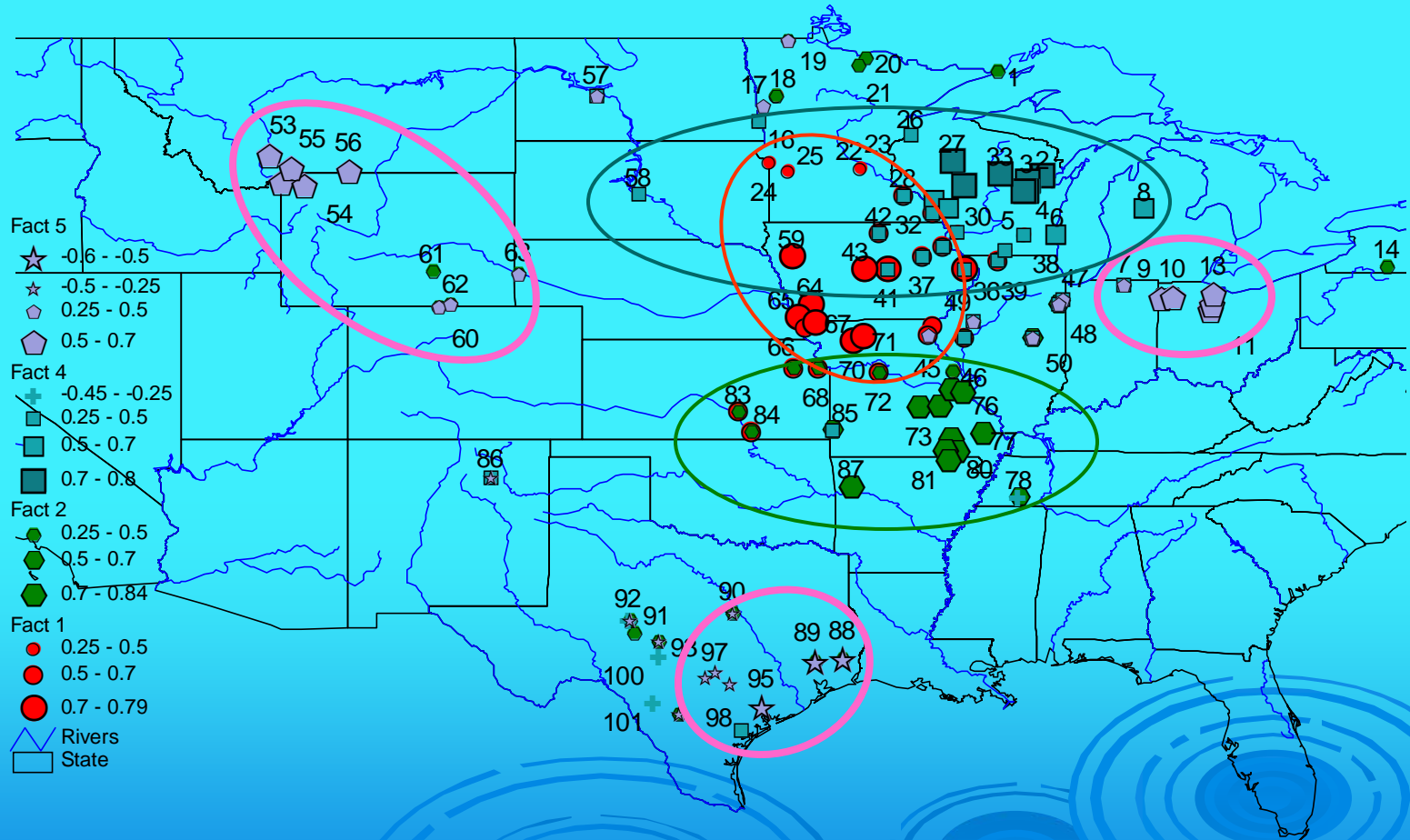


	October	November	December	January	February	March	April	May	June	July	August	September	Annual	Expl. Var.
Factor I- 1						0.31			0.90	0.86	0.94	0.83	0.93	4.25
Factor I- 2	0.80	0.80	0.87	0.83	0.78	0.50								3.63
Factor I- 3						0.33	0.83	0.78						1.58
Factor II- 1	0.84	0.91	0.93	0.83	0.43	0.27	0.41	0.40					0.43	3.91
Factor II- 2					0.62		0.57	0.62	0.88				0.69	2.47
Factor II- 3	0.37				0.25			0.43			0.88	0.44	0.29	1.55
Factor II- 4						0.60	0.44			0.76		0.56	0.46	1.72
Factor III- 1	0.79	0.81	0.93	0.85	0.85	0.79	0.45						0.37	4.75
Factor III- 2									0.72	0.90	0.90	0.88	0.64	3.42
Factor III- 3							0.70	0.90	0.49				0.64	2.12
Factor IV- 1	0.84	0.90	0.84	0.77	0.70	0.52	0.56						0.81	3.98
Factor IV- 2									0.84	0.88	0.31		0.46	2.43
Factor IV- 3						0.67					0.62	0.86		1.79
Factor IV- 4				0.38		0.38		0.38	0.30					1.68

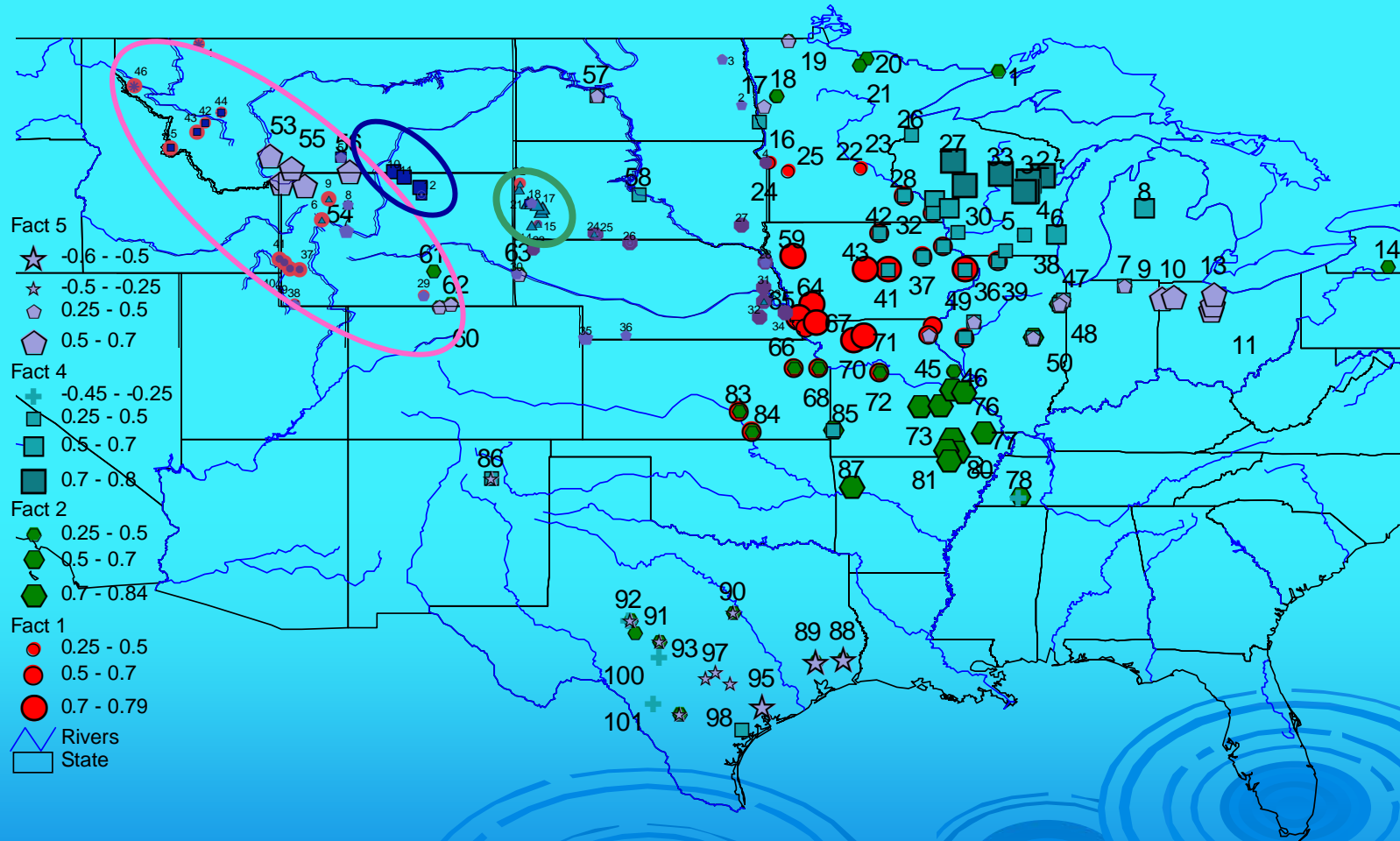
Structure of time spatial variability of stream runoff for Upper Missouri



Factor Loadings of 101 gauging stations



Patterns of stream runoff in Central US and Upper Missouri



Topic

- Spatial-temporal variations of stream runoff for Upper Missouri River watershed

* Hydrologic regime as structure

* Land cover or landscape

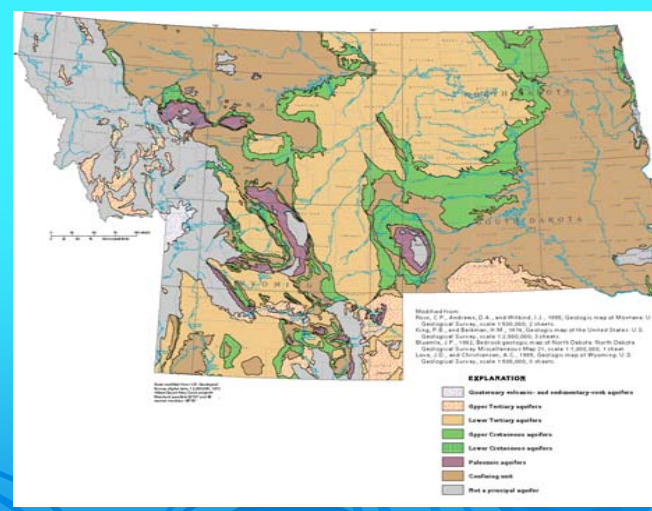
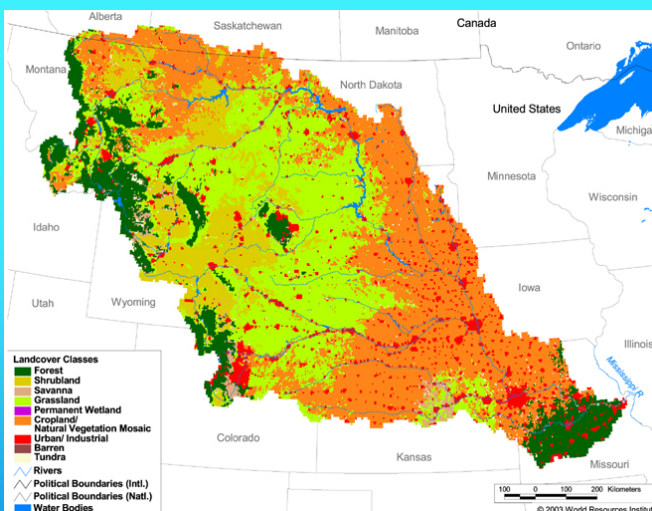
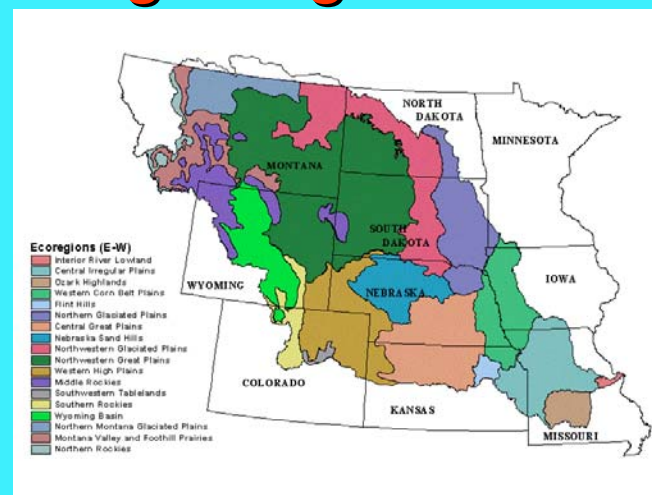
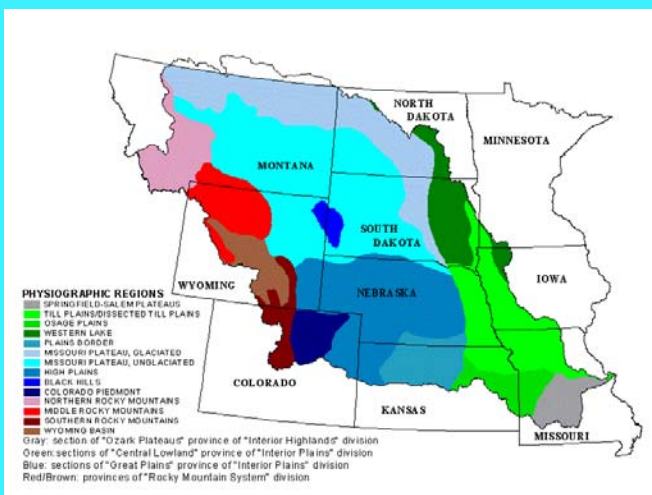
* Map with fuzzy boundaries

* Applications

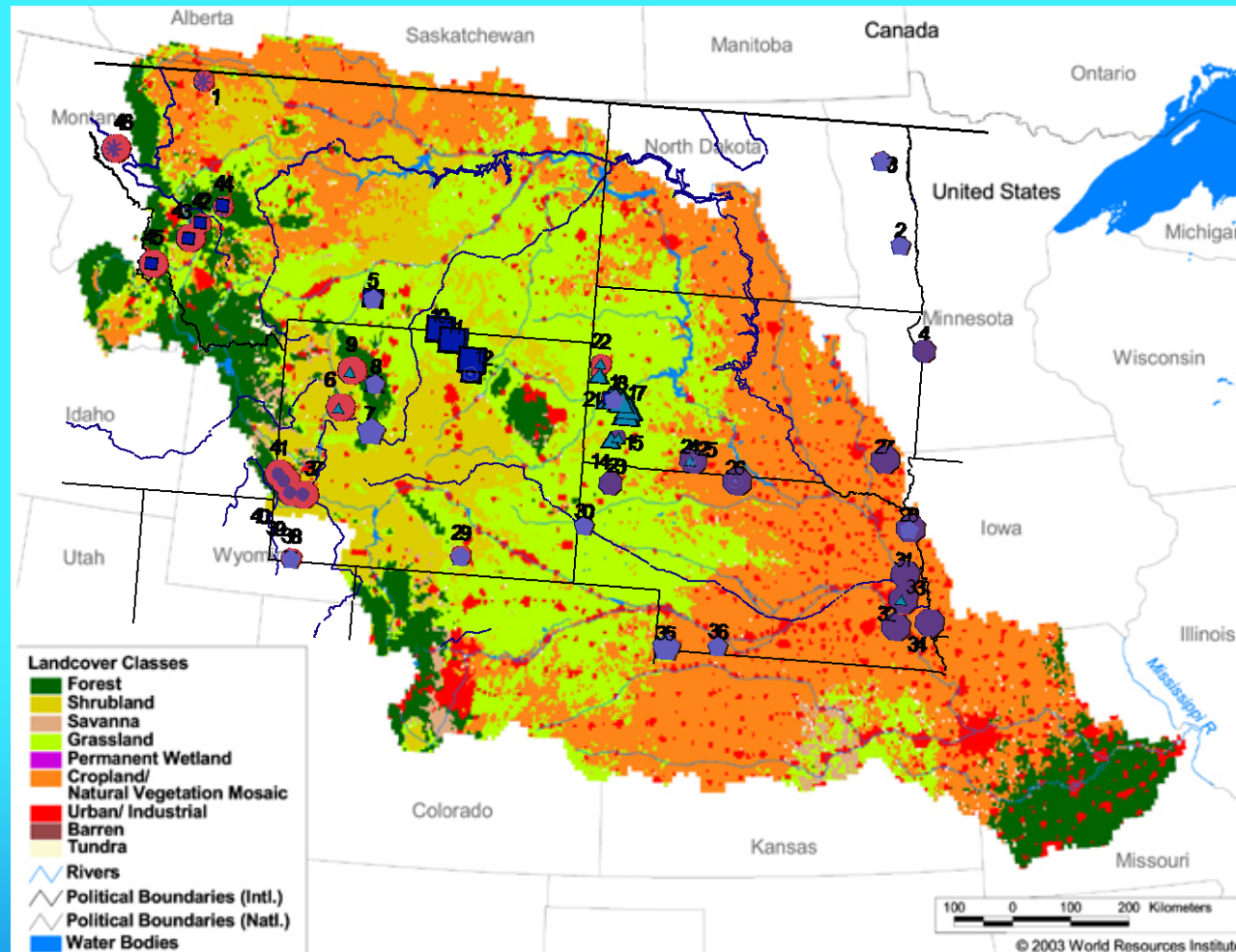
* Decision making about water resources or Scientist vs. Lawyer



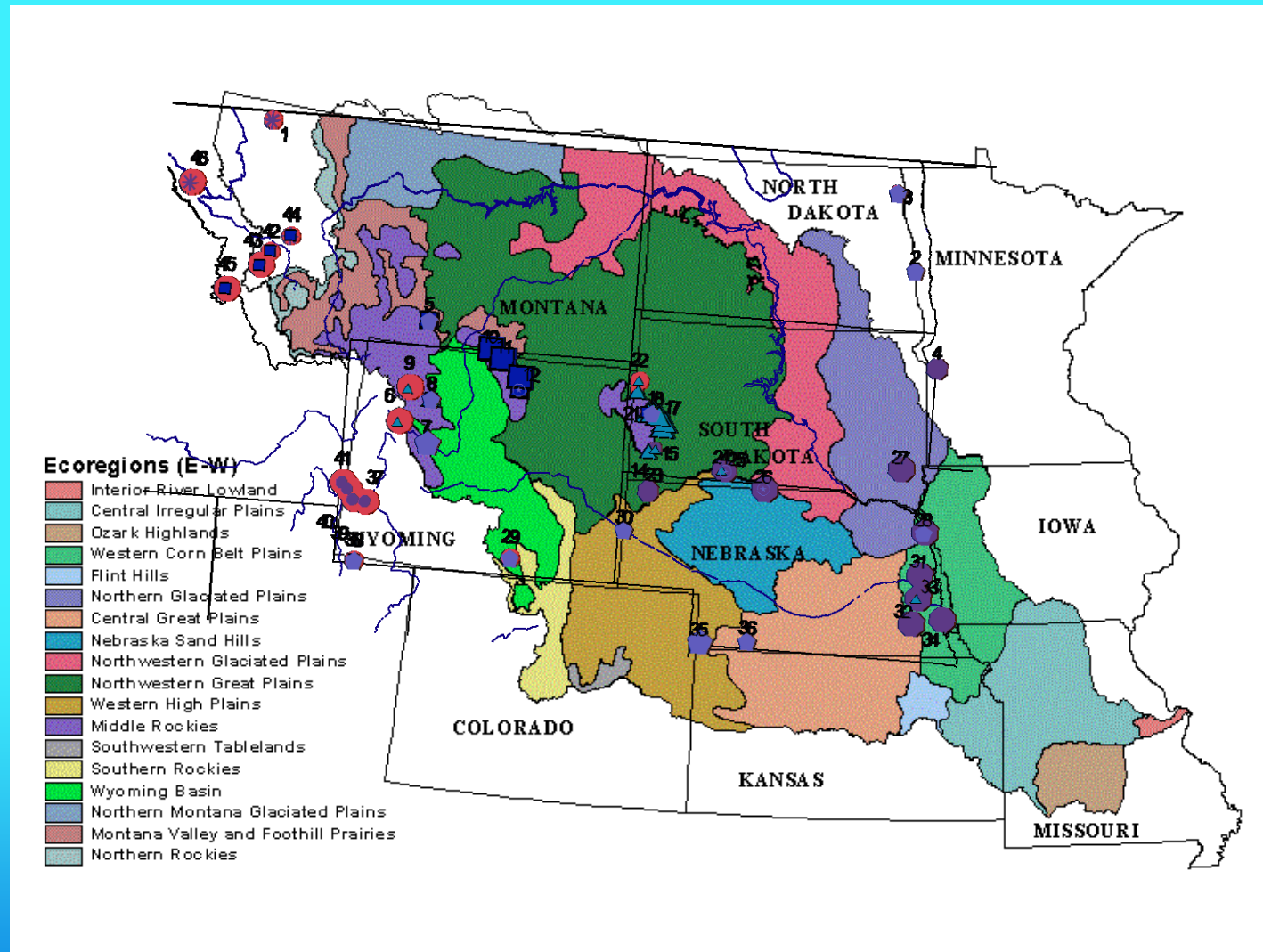
Maps: physiographic, ecoregions, landcovers and hydrogeological



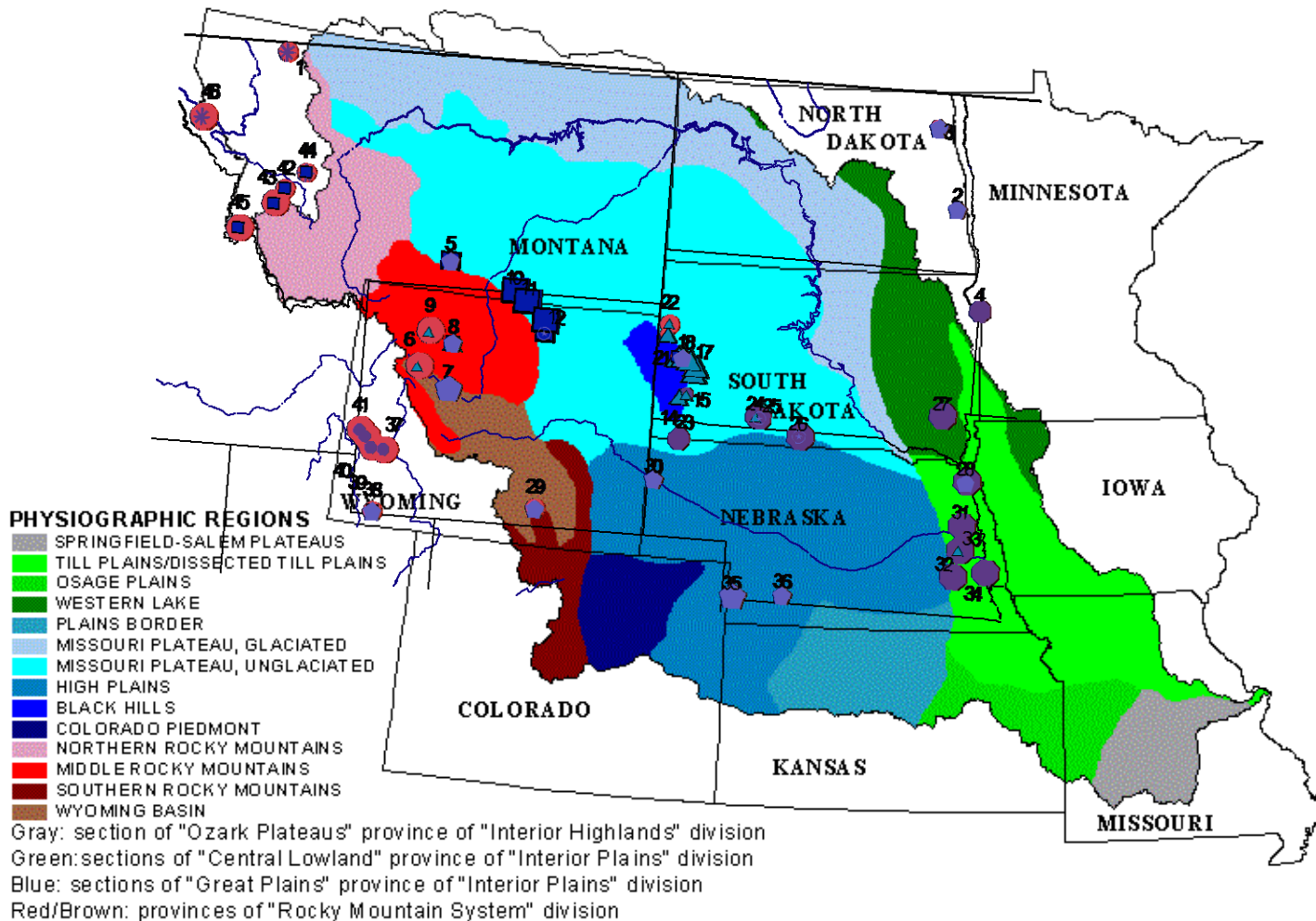
Map: landcovers



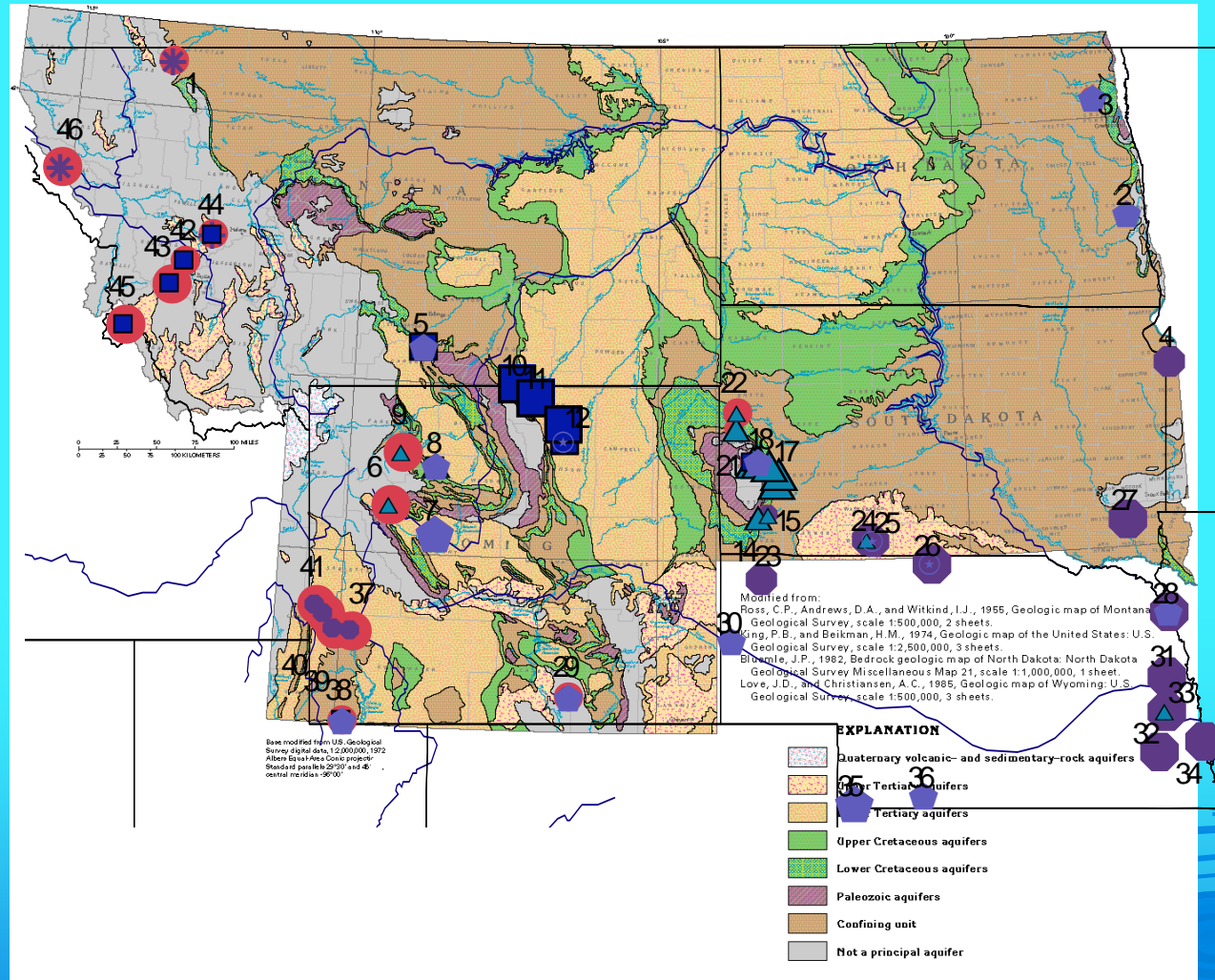
Map: ecoregions



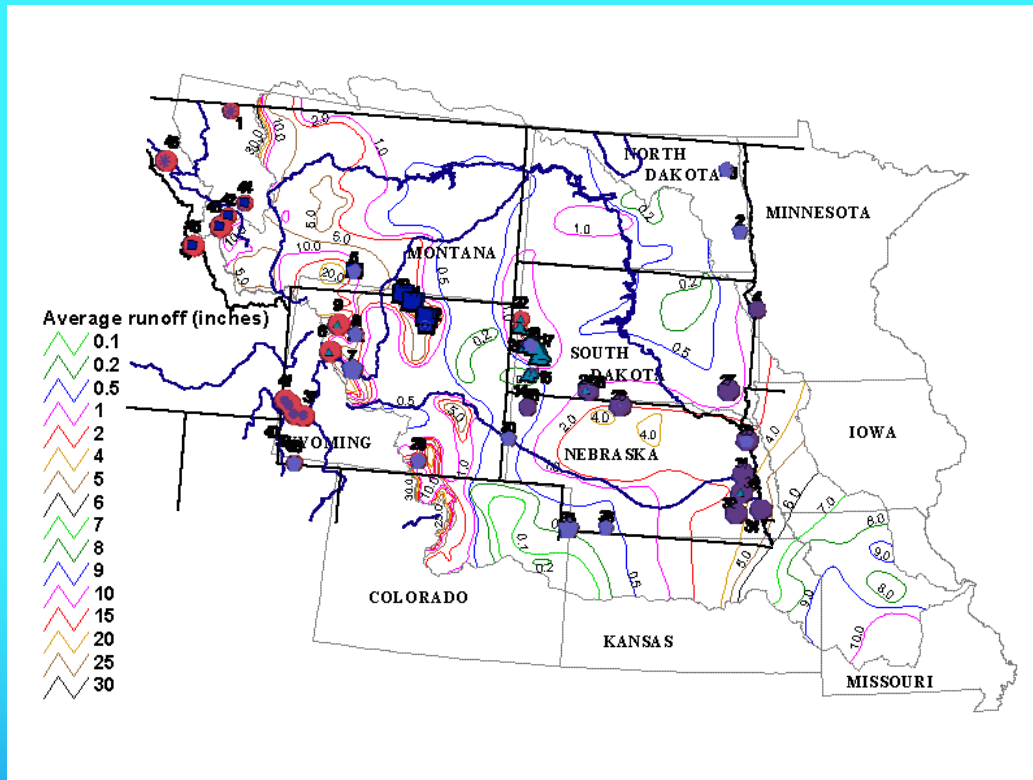
Map: physiographic



Map: hydrogeological



Control of patterns of stream runoff in Central US and Upper Missouri



- * Topography
- * Landscape property like hydrogeology



Topic

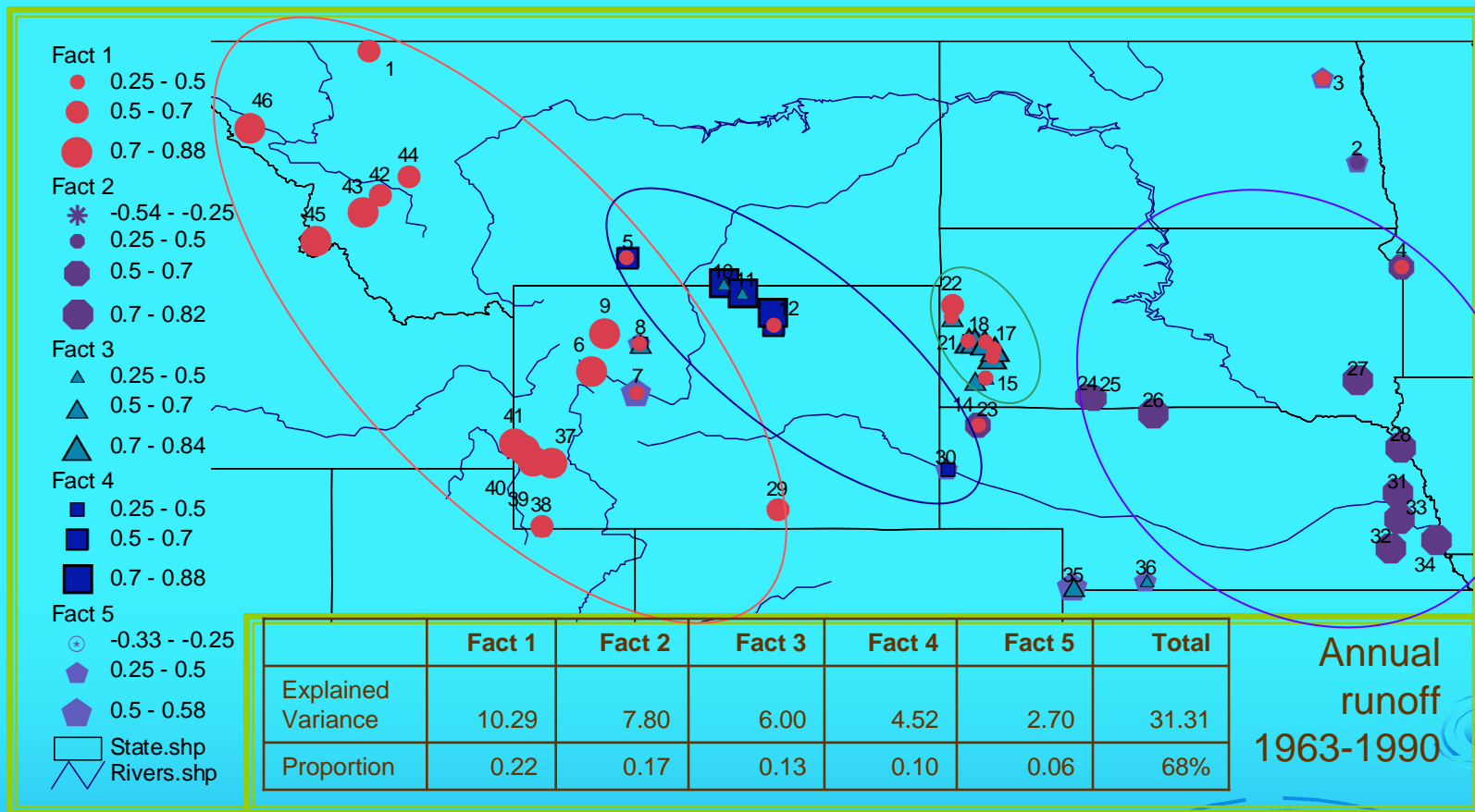
- Spatial-temporal variations of stream runoff for Upper Missouri River watershed
 - * Hydrologic Regime as Structure
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R829643

Patterns of stream runoff in Upper Missouri

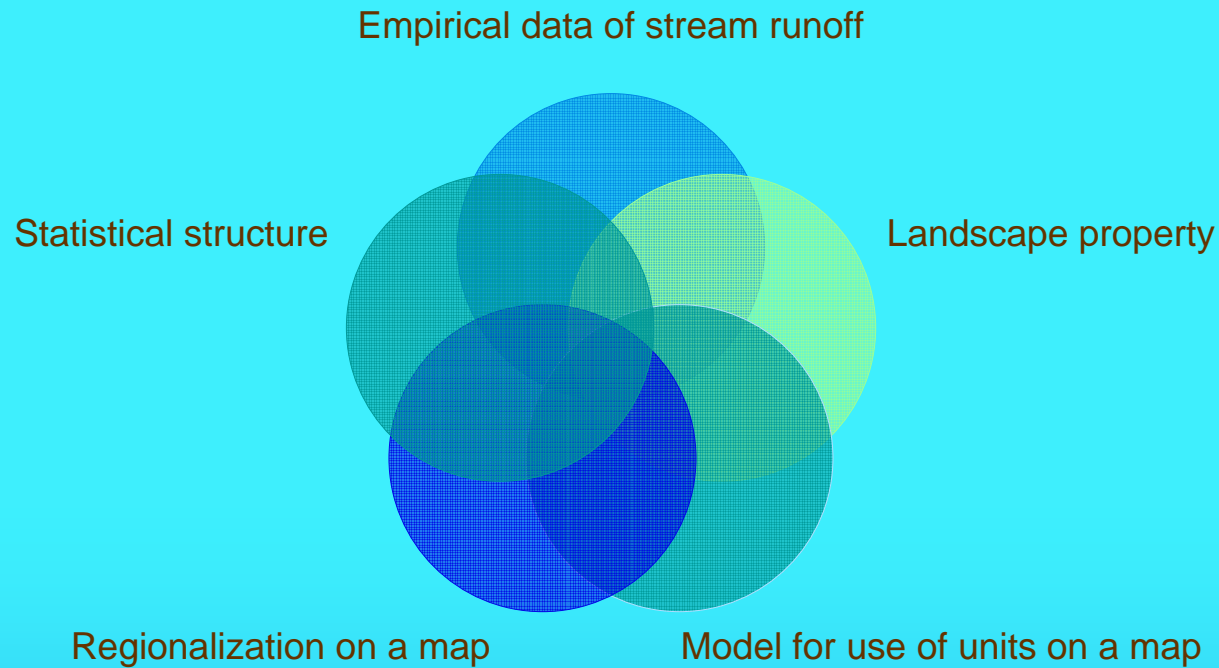


Fuzzy Logic rules for mapping the statistical structure

- * The set of sampled gauging stations (watersheds) with results of factor analysis of stream runoff may be regarded as a fuzzy set
- * Factor Loadings provide the values for grouping by fuzzy membership functions (i.e. degree of fuzziness)
- * Groups with fuzzy membership of watersheds with different stream runoff regime create regional units for map



Components of analysis uncertainty of stream runoff for a region



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Analysis of stream runoff of type V watershed with monthly teleconnection indexes

	VF1	VF2	VF3
ANN		0.93	0.26
OCT	0.91		
NOV	0.91		
DEC	0.94		
JAN	0.94		
FEB	0.90		
MAR	0.77	0.28	0.25
APR	0.29		0.75
MAY			0.87
JUN		0.87	
JUL		0.94	
AUG		0.96	
SEP		0.90	

Seasonal structure of runoff for V typical watershed

Regressions and correlations analysis for annual and seasonal stream runoff characteristics of V type regime watershed (06191500) with monthly teleconnection indexes as Arctic Oscillation, North Atlantic Oscillation (ⁿ), Antarctic Oscillation (APR^a) and Pacific/ North American (P). Months from previous year indicated with -₁.

Predictor	BETA	St. Err. of BETA	B	St. Err. of B	t(35)	p-level
VF						
R= .8492 R²= .7212 Adjusted R²= .6762						
JAN ^P	-0.58	0.10	-234.92	39.36	-5.97	0.00
NOV ^P ₁	-0.28	0.10	-166.92	60.07	-2.78	0.01
NOV ⁿ ₁	-0.47	0.10	-295.50	63.13	-4.68	0.00
AUG ⁿ	0.33	0.10	389.19	120.26	3.24	0.00
SEP ₁	0.29	0.10	331.76	120.21	2.76	0.01
VF1						
R= .6016 R²= .3619 Adjusted R²= .3039						
AUG ⁿ ₁	0.40	0.14	0.71	0.24	2.90	0.01
MAR ^P	0.35	0.14	0.27	0.11	2.53	0.02
JUL ^P ₁	0.29	0.14	0.66	0.32	2.09	0.04
VF2						
R= .8108 R²= .6574 Adjusted R²= .5889						
JAN ^P	-0.53	0.11	-0.33	0.07	-4.69	0.00
JUL ₁	0.27	0.11	0.58	0.24	2.46	0.02
AUG ⁿ	0.38	0.11	0.70	0.21	3.39	0.00
SEP ⁿ ₁	0.29	0.11	0.44	0.17	2.60	0.01
MAR	0.29	0.11	0.21	0.08	2.69	0.01
NOV ⁿ ₁	-0.32	0.11	-0.31	0.11	-2.83	0.01
VF3						
R= .7130 R²= .5084 Adjusted R²= .4469						
DEC ^P ₁	-0.35	0.13	-0.24	0.09	-2.82	0.01
APR ⁿ	0.48	0.13	0.63	0.17	3.70	0.00
NOV ⁿ ₁	-0.45	0.13	-0.44	0.12	-3.53	0.00
JUN ^P	-0.30	0.13	-0.51	0.22	-2.27	0.03

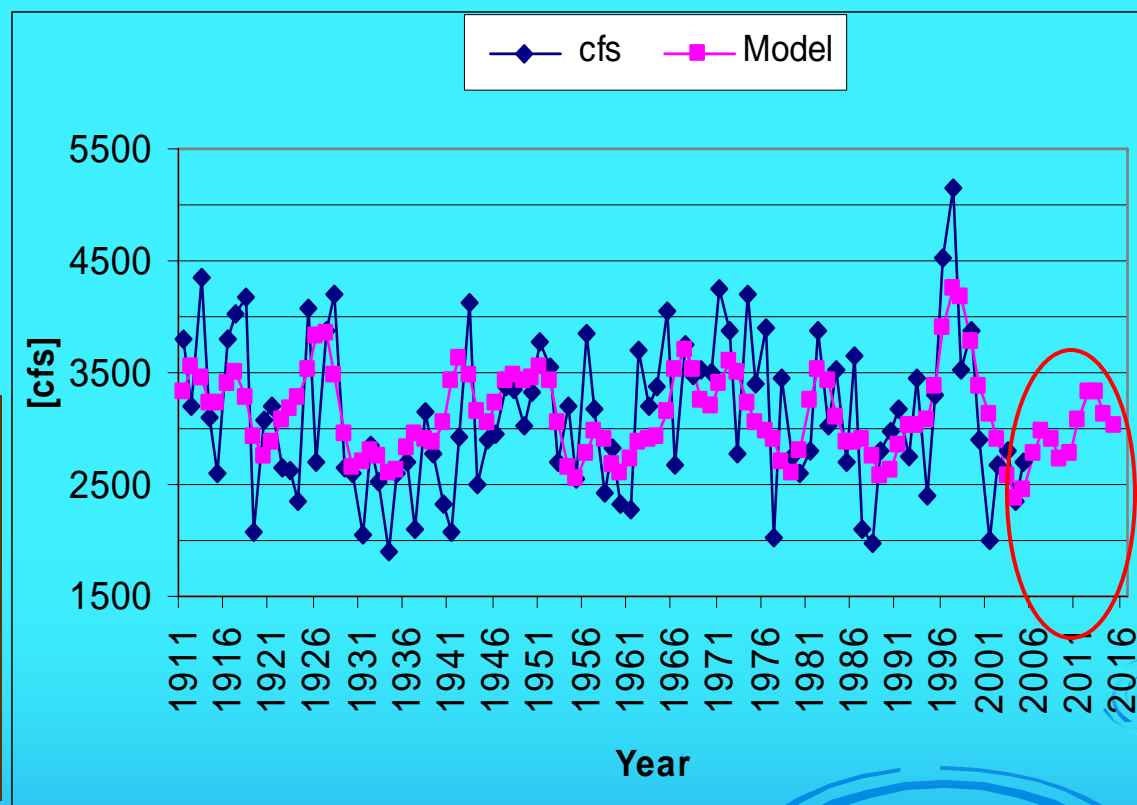


Chart of annual observed stream runoff for 1911-2005 and as a harmonic model

Model:

$$X_t = X_0 + \sum_{i=1}^K A_i \cos\left(\frac{2\pi}{T_i} t - \varphi_i\right) + Z_t,$$

No	T- period [year]	A- amplitude [cfs]	φ - faze	Z- error [cfs]
1	5.0	175.9	2.54	661
2	8.0	187.3	0.06	661
3	12.0	165.5	1.78	657
4	14.0	245.7	1.27	642
5	17.0	162.3	1.36	659
6	25.0	321.4	2.18	641



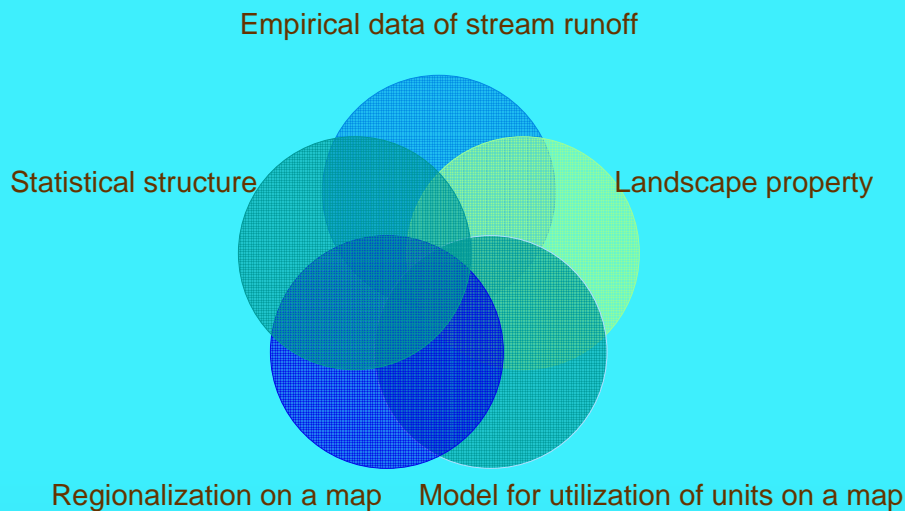
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Decision making about water resources make sense only with use of “Model for utilization of units on a map”



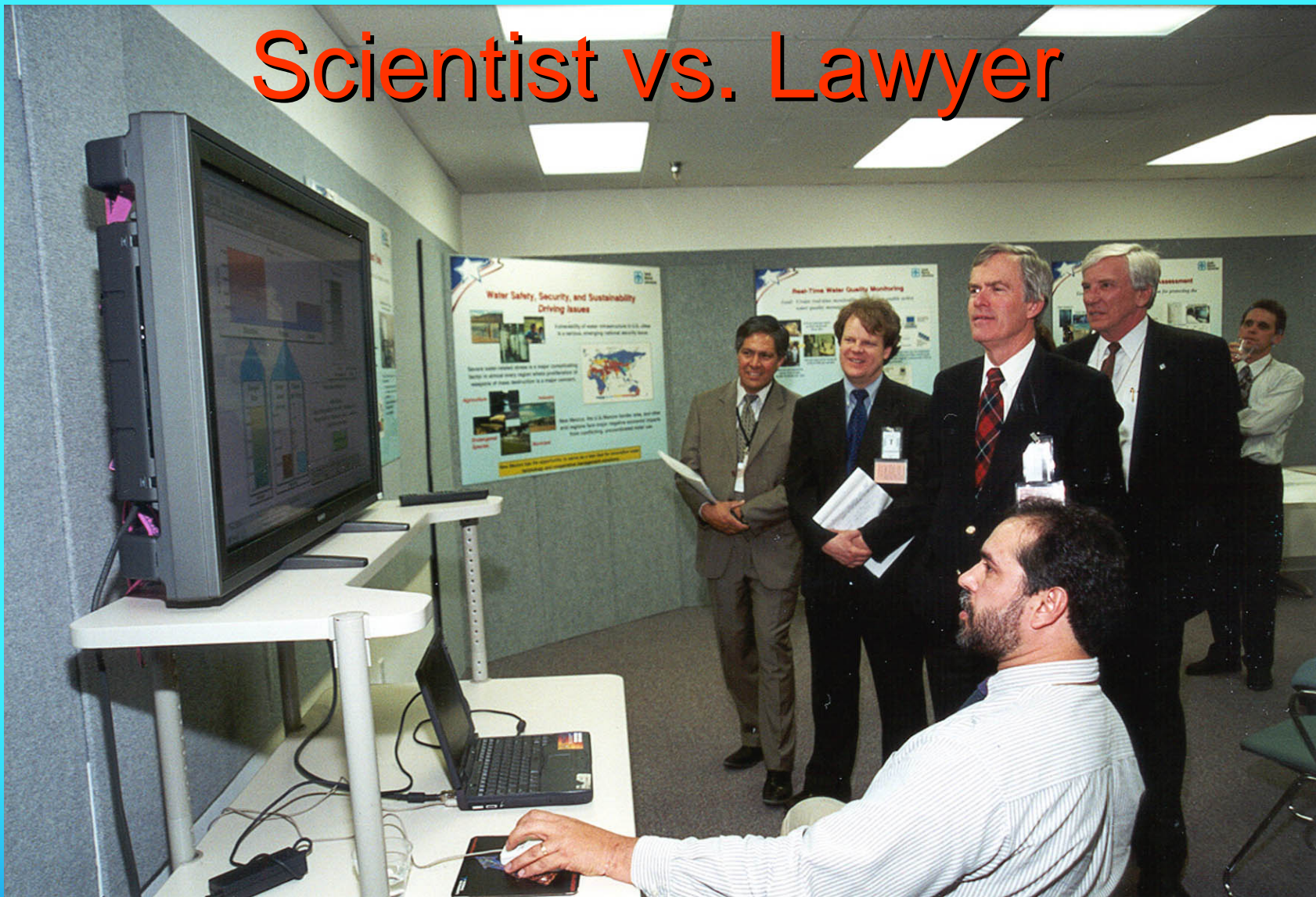
U.S. Supreme Court declines to hear Missouri River appeal

April 2006
U.S. Water News Online

WASHINGTON -- The Supreme Court has refused to hear North Dakota's arguments that the Army Corps of Engineers has violated state water pollution laws in managing the Missouri River's water flows.



Scientist vs. Lawyer



Sandia NL scientist Dr. Steve Conrad demonstrates the Middle Rio Grande Water Budget Model to Sen. Jeff Bingaman (D, NM)

“The total benefits of U.S. National Weather Service (NWS) forecasts are estimated to be \$166 million. The additional benefits potentially Obtainable from a perfect temperature forecast are \$75 million per year. It is estimated that an incremental 1% improvement in the forecast quality (from the current NWS forecast) would be worth an additional \$1.4 million per year.

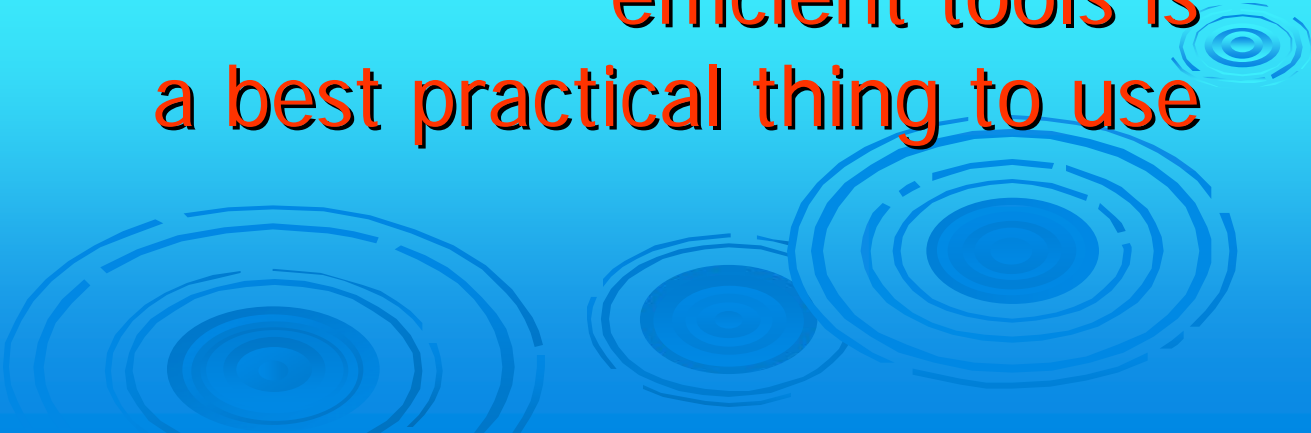
These numbers do not include other possible benefits of forecasts to the electricity industry, such as those from the improved scheduling of plant maintenance.”

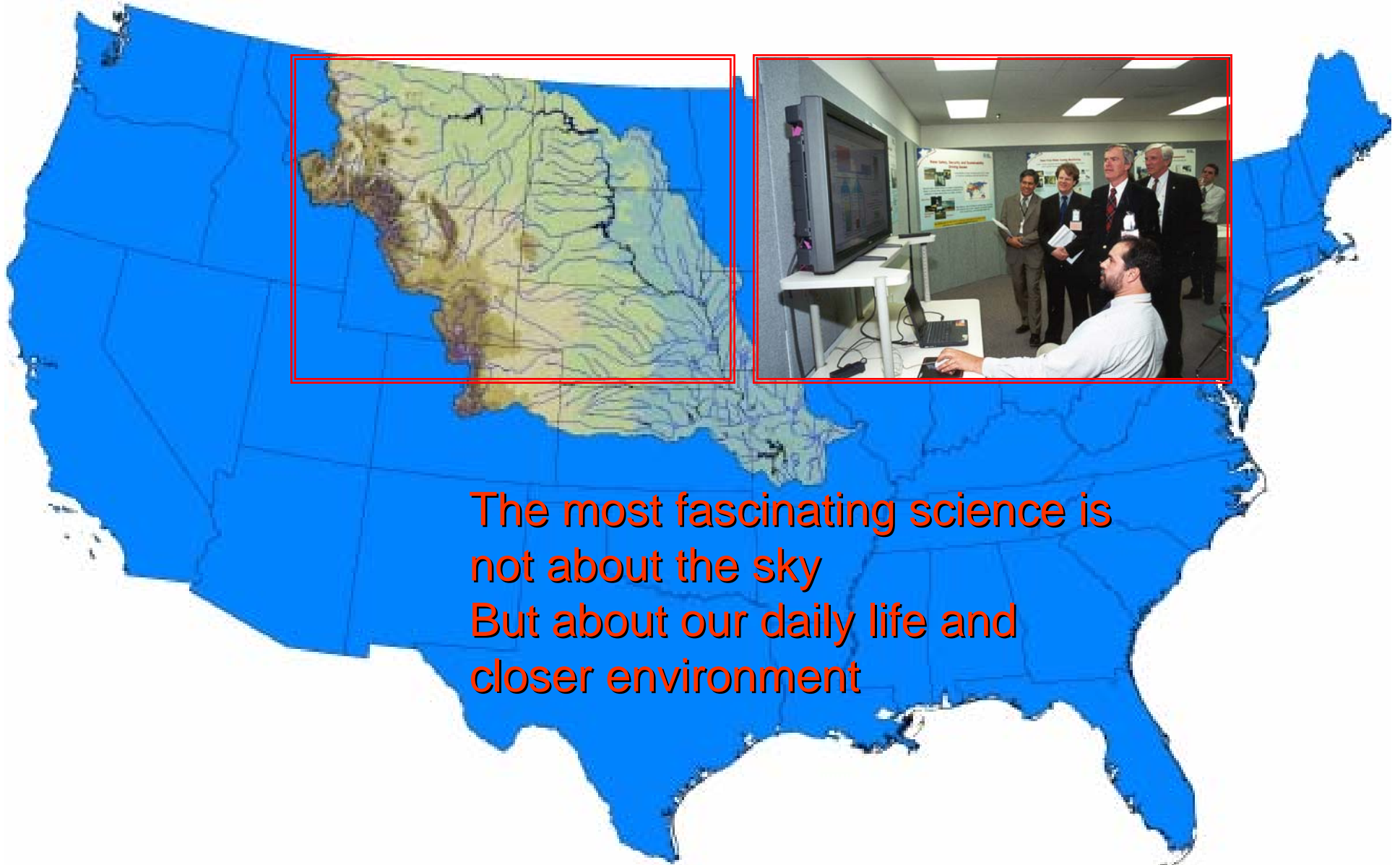
THE ECONOMIC VALUE OF TEMPERATURE FORECASTS IN ELECTRICITY GENERATION

BY THOMAS J. TEISBERG, RODNEY F. WEIHER, AND ALIREZA KHOTANZAD

United States electricity generators save \$166 million annually using 24-h temperature forecasts to improve the mix of generating units that are available to meet electricity demand.

Good theory with
efficient tools is
a best practical thing to use





The most fascinating science is
not about the sky
But about our daily life and
closer environment

Boris Shmagin & Din Chen
SDSU Biocomplexity Studies &
Department of Mathematics
and Statistics SDSU

South Dakota
EPSCoR
Experimental Program to Stimulate Competitive Research

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U.S. EPA - Science To Achieve
Results (STAR) Program
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