

Overview

- Preliminaries
- Conventions & propagation primer
- Mesh Convergence & oversampling
- Results for Cases 1 & 2
- Ground signals for Standard Atm. & Required Atm.
- Cutoff angles
- Carpet noise metrics
- Ground Intercepts, boom carpets & raytubes
- Summary & observations



Wind Convention in sBOOM







- Quasi-1D integration of Burger's equations occurs in tube along the ray path
- Determines the ground intercept of sound emanating from given trajectory point & azimuth
- Ray path determines time required for signal propagation



Wind Effects

- Flight path (+x)· Wind can alter path o · Paths are scaled by Ic 55000 50000 45000 40000 Altitude (ft) 35000 30000 25000 20000 15000 10000 0 10000 5000 20000 0 Downrange (ft) 500 Cr_{OSSrange (ft)} 40000 1000 50000 1500 60000 Raytube from SBPW2 axibody
- · Only consider crossrange and downrange winds (no up/down drafts)



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Mesh Convergence

Sensitivity of noise output to discretization of near field signal

- Propagation code is solving augmented Burgers' via finite difference
- · Need to make sure loudness metrics are sufficiently mesh converged
 - Mesh convergence of propagation is case dependent (on signal, azimuth & atm.)
 - Mesh refinement study done for each near field signal (using Std. and Reqd. Atm.'s)
- Truncation error directly impacts accuracy, resolution requirements are driven by need to minimize error in propagation
- Initial signal typically has < 2000 points
- Propagation typically requires 40000-100000 points (oversampled by 20-50x)
- Discrete ASEL filter can be poorly behaved at high sampling frequencies (> ~250kHz)
 - ➤ this limits maximum allowable oversampling
- How much accuracy is needed?
 - Atmospheric variability generally 2-5 dB, but may be ~10 dB in some cases
 - Generally tried to keep propagation error under ±0.2 dB



Mesh Convergence



Sensitivity of noise outputs to refinement of the propagation mesh

- C25P signals at $\phi = 0^{\circ}$, using from 20k 300k points (80-1230 kHz) for propagation
- Despite similarities in ground signal, mesh convergence of ASEL is quite slow



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Mesh Convergence



Convergence ASEL noise metric with sampling frequency



- ASEL converges slowly

 Need ~600kHz (~150k pts) to converge ASEL to ±0.01dB
- However, discrete ASEL filter starts to have issues at ~250kHz, and blows up ~500kHz
- On this case (C25P) hard to guarantee ASEL error < ± 0.1dB
- Discrete BSEL and CSEL remain well behaved till ~1 & 10 MHz (respectively), so generally easier to mesh converge



Mesh Convergence

Convergence of BSEL, CSEL & PLdB noise metrics with sampling frequency



- BSEL, CSEL and PLdB all show good mesh convergence (all on 1 dB scale)
- FFT used for all metrics except for BSEL, but appears to be well behaved
- C-weighting converges fastest (±0.02 dB @ 200kHz)
- PLdB converges slowest (approx. ±0.1 dB @ 200kHz)



Mesh Convergence



Convergence of BSEL, CSEL & PLdB noise metrics with sampling frequency

- To avoid excessive discretization error in propagation used 500-800kHz sampling frequencies for all workshop cases
- Computed noise metrics with FFT in LCASB (adloud) for ASEL, CSEL and PLdB noise metrics
- Used digital BSEL filter in sBOOM (well behaved at 500-800kHz)





Case 1: C25P Standard Atmosphere

Near field and ground pressure signals



• Near field data provided for half-cylinder {-90°, 90°}, ({-50°, 50°} shown)



• Near field data provided for half-cylinder {-90°, 90°}, ({-50°, 50°} shown)

• Propagation shown used 500kHz sampling frequency (142k pts)



Case 1: C25P Ground Signatures



Propagation altitude = 15760m, ground height = 264m

· Reqired Atm. has profiles of crosswind, temperature, humidity and pressure

– Shows lots of asymmetry, and cutoffs are farther out on both sides

NASA

Case 1: C25P Ground Noise



Compare ground noise metrics across the carpet as a function of azimuth

· Noise at carpet edge drops, but can still be significant

[•] Azimuthal range of carpet with real atm. is much wider than Standard Atm.

[•] Real atm. (with wind) reduces peak loudness by ~1dBA, ~0.5dBB, ~0.4dBC & ~0.7PLdB

Case 1: C25P Ground Carpet



Project raytube ground intercepts on aircraft ground track

- Boom carpet computed from the intercepts of raytubes on the ground-plane projection of the trajectory. Showing both standard and required atmospheres
- · Crossrange wind profile makes the required atm. asymmetric
- Cutoff angles: Std. Atm = [±50.8°], Req. Atm = [-78.4°,+69.1°]
- Long propagation distances near signal cutoff imply that these raytubes take a long time to reach the ground
 - Raytube for φ = -78.4° takes over 6 mins in Required atm.
 - Mesh convergence near signal cutoff is not nearly as good as at low azimuth angles
 - Higher discretization error due to much longer propagation
 - Propagation for signal cutoff used higher sampling frequency (800 kHz)
- Ground track for required atm is ~160 km, more than 2x as wide as standard atm. (~70 km)



Case 2: C609

Preliminary design of X-59 Low Boom Flight Demonstrator

Conditions:

 $M_{\infty} = 1.4$ Altitude = 16.4592 km (54k ft) Ground height = 110.011 m (54k ft) Lref = 27.43 m (90 ft) r/L = 3 at signal extraction Ground reflection factor = 1.9 Heading East ($\beta = 0^{\circ}$)

Atmospheric Profiles:

- 1. Required Atm: with profiles for wind, temp, pressure & humidity
- 2. Standard Atmosphere

Case 2: C609 Near Field Signals





- Near field signals provided for 23 azimuths from -70° to +70° $\phi = [0, \pm 10, \pm 20, \pm 30, \pm 40, \pm 50, \pm 60, \pm 62, \pm 64, \pm 66, \pm 68, \pm 70]$
- Signals symmetric ±φ





Case 2: C609 Ground Signals

Propagation altitude = 16460m, ground elevation = 110m



• Reqired Atm. includes profiles of crosswind, temperature, humidity and pressure – Very asymmetric, with much wider cutoffs on both sides

• Amplitude of ground signal in real atmosphere significantly reduced from Std. Atm.



Case 2: C609 Ground Noise



Compare ground noise metrics across the carpet as a function of azimuth

- · Azimuthal range of carpet with Required Atm. is much wider than Standard Atm.
- · Despite wind & reduced ground amplitude, Real Atm. and Std. Atm. have similar loudness
- Noise at carpet edge drops significantly in Required Atm.



Case 2: C609 Ground Carpet



Project raytube ground intercepts on aircraft ground track

- Boom carpet computed from the intercepts of raytubes on the ground-plane projection of the trajectory. Showing both standard and required atmospheres
- · Crossrange wind profile makes the required atm. asymmetric
- Cutoff angles Req. Atm = [-64.1°, 70.6°], Std. Atm = [±44.9°]
- Long propagation distances near signal cutoff imply that these raytubes take a long time to reach the ground
 - Raytube for φ = -64.1° cutoff takes over 8.5 mins in Reqd. atm.
 - Mesh convergence near signal cutoff is not nearly as good as at low azimuth angles
 - Higher discretization error due to much longer propagation
 - Propagation for signal cutoff rays used higher sampling frequency (800 kHz)
- Ground track for required atm is ~160 km, more than 2.7x as wide as standard atm. (~60 km)





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Summary

- · Applied sBOOM v2.82 & LCASB to all required and optional steady propagation cases
- Mesh convergence studies across the carpet to ensure accuracy of the ground signal and loudness metrics. Error in noise metrics can be 2-4x higher near signal cutoff.
- · Mesh convergence is relatively slow on intricate non-smooth input signals
- Real atmosphere is usually quieter than Standard Atmosphere, (but not always e.g. case 2)
- Ground track of real atmosphere can be nearly 3x wider than Standard day. Crosswinds generally increase track width and can result in large cutoff azimuths
- On windy days, boom may not arrive off-track for over 5 mins after a/c passes (case 2 took 8 mins!)
- Raytube visualization shows potential for loud off-track azimuths to be blown back under-track

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