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# High-Rate Uncorrelated Bit Extraction for Shared Secret Key Generation from Channel Measurements

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**Abstract**—Secret keys can be generated and shared between two wireless nodes by measuring and encoding radio channel characteristics without ever revealing the secret key to an eavesdropper at a third location. This paper addresses bit extraction, i.e., the extraction of secret key bits from noisy radio channel measurements at two nodes such that the two secret keys reliably agree. Problems include 1) nonsimultaneous directional measurements, 2) correlated bit streams, and 3) low bit rate of secret key generation. This paper introduces high-rate uncorrelated bit extraction (HRUBE), a framework for interpolating, transforming for decorrelation, and encoding channel measurements using a multibit adaptive quantization scheme which allows multiple bits per component. We present an analysis of the probability of bit disagreement in generated secret keys, and we use experimental data to demonstrate the HRUBE scheme and to quantify its experimental performance. As two examples, the implemented HRUBE system can achieve 22 bits per second at a bit disagreement rate of 0.54 percent.

Index Terms—Wireless networks, multipath fading, physical layer, cryptography, key generation.

## **1** INTRODUCTION

THIS paper investigates the generation of shared secret L keys from the observation and processing of reciprocal radio channel properties. Shared secret keys are necessary for private communication over an open channel. Public key cryptography has been the most common method for the establishment of such keys, but concerns about its limitations has spawned interest in new methods for key sharing. For example, quantum cryptography [1], [2], [3] does not use public keys, but is prohibitively expensive for most applications. Shared secret key generation from radio channel measurements, on the contrary, is very inexpensive and can be done with any standard radio devices which can receive and transmit on the same frequency channel. We envision its application in mobile and portable radio communications systems, such as IEEE 802.11 or 802.15.4, which communicate on time-division duplex (TDD) channels.

Shared secret key generation from channel measurements is an application which benefits from the randomness of the multipath channel. It would not, for example, work in a truly free-space environment (such as deep space radio links). Secret sharing benefits from:

- Reciprocity of the wireless radio channel: The multipath properties of the radio channel (gains,
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phase shifts, and delays) at any point in time and on any given frequency channel are identical on both directions of the link.

- Temporal variations in the radio channel: Over time, the multipath channel changes due to movement of either end of the link, and any motion of people and objects in the environment near the link. An application may specifically request a user to move or shake her wireless device in order to generate more temporal variation.
- Spatial variations: The properties of the radio channel are unique to the locations of the two endpoints of the link. An eavesdropper at a third location more than a few wavelengths from either endpoint will measure a different, uncorrelated radio channel [4].

Essentially, the radio channel is a time and space-varying filter, that at any point in time has the identical filter response for signals sent from a to b as for signals sent from b to a.

Although the radio channel is reciprocal, *measurements* of the radio channel are not reciprocal. Additive noise contributes to each measurement as it does in any received signal. Also, the transceiver hardware used by the two nodes is not identical and affects the signal in each direction in a different way. Furthermore, measurements in both directions of the link cannot typically be made simultaneously.

Finally, interference power is asymmetric. The proposed system is susceptible to denial-of-service by jamming, in the same way that the wireless link is susceptible to jamming. If nodes cannot communicate, then they also cannot measure signal strength and share a secret key. However, if multipleaccess interference is infrequent, and two nodes can receive many packets from each other, they will have many measurements of signal strength, marginally impacted by

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Fig. 1. Flow chart of high-rate uncorrelated bit extraction.

interference, with which to encode a secret key. This assumes that an acknowledgement protocol is applied so that two nodes agree on which packets are to be used in the proposed system.

We refer to these sources of nonreciprocity collectively as "noise" because they are the ultimate cause of bit disagreements between the secret keys generated at nodes *a* and *b*.

Bit extraction, i.e., the extraction of secret key bits from noisy radio channel measurements at two nodes such that the two secret keys reliably agree, is a major statistical signal processing problem in shared secret key generation. As opposed to communications signal processing, it has no interest in obtaining the transmitted data from another device. We refer to this problem as a *radio channel signal processing* problem since measurements of the radio channel are the signal of interest. This paper contributes a statistical framework and algorithm for bit extraction which extracts a high bit rate with given reliability and ensures a bit vector with nearly zero correlation. This framework is a significant improvement on the state of the art in the research area.

Recent results have both suggested and demonstrated bit extraction from a variety of different radio channel measurement modalities (e.g., time delay, amplitude, phase, and angle). These results are reviewed in Section 2. Several works limit the number of bits per measurement to one or zero. Several works have decreased the measurement rate because correlation between measurements leads to correlation between bits in the secret key, which is detrimental to the security of data encoded with that key. Both compromises reduce the bit rate of generated secret keys. In addition, solutions are ad hoc; each measurement modality requires a separate methodology for secret key generation.

This work provides a framework for bit extraction using three signal processing methods:

- Fractional interpolation: Introduces different fractional delays at each node to account for the fact that the two directional measurements are not measured simultaneously.
- 2. Decorrelation transformation: Produces a measurement vector with uncorrelated components via a Karhunen-Loève transformation of the original channel measurement vector.
- 3. Multibit adaptive quantization (MAQ): Converts realvalued channel measurements into bits adaptively based on the measured value, using communication so that both nodes agree on the quantization scheme.

The flow chart of the proposed method is shown in Fig. 1. In this paper, we use these procedures in order to transform correlated, real-valued radio channel signal measurements at two nodes into uncorrelated binary data which has a high probability of bit agreement. We refer to the combination of the methods as *high-rate uncorrelated bit extraction* (HRUBE).

As discussed in Section 2, there are methods, called information reconciliation methods, to resolve bit disagreements between two nodes without giving away the entire secret key. These methods do give away some information to an eavesdropper; if enough information can be obtained, an eavesdropper could perform a brute-force search to find the secret key. It is best to minimize the number of bit disagreements and to know a priori the probability of bit disagreement so that an information reconciliation method can be designed efficiently. This paper provides a theoretical framework to design systems with low probability of bit disagreement.

This paper is organized as follows: In Section 2, we discuss the work in the area of secret key extraction from radio channel measurements, and position this work in that frame. In Section 3, we provide an adversary model. In Section 4, we describe the fractional interpolation method used to correct for nonsimultaneous radio channel measurements. Section 5 presents the decorrelation of the measured radio channel signal, and Section 6 presents the multibit adaptive quantization method. Sections 4-6 provide the methodology and analysis of high-rate uncorrelated bit extraction. In Section 7, the HRUBE method is implemented in wireless nodes and the bit disagreement rate is shown and compared to the analytical results. Finally, future work and conclusions are presented in Section 8.

## 2 RELATED WORK

There have been several papers on the topic of secret key generation from radio channel measurements. In the earliest work [5], it was suggested to send two unmodulated continuous wave (CW) signals in both directions through a channel and measure and quantize the phase difference between the two at each end of the link to generate a shared secret. Phase differences between multiple channels have been further explored in [6], [7].

Time delay and gain are also features of the radio channel that are reciprocal and can be used for secret generation. The impulse response, in particular, the amplitude of multipath at many time delays, can be used as a shared secret [8], [9], [10]. While Madiseh et al. [8] and Wilson et al. [10] use ultrawideband (UWB) radios to measure the impulse response, Ye et al. [9] estimate channel gains and delays from relatively narrowband cellular signals.

Amplitude or channel gain is the most common reciprocal channel feature used for secret generation in literature [11], [12], [13], [14], [15], [16], [17]. Amplitude can be more easily measured than time delay or phase on most existing hardware, and thus is more readily applicable to common wireless networks.

Angle-of-arrival (AOA) itself is not reciprocal—the AOA at the two ends of a link is different. However, steerable directional antennas can be used as in [14] to measure reciprocal channel gains, which are reciprocal, and generate shared secret keys. The antenna used in [14] is a relatively simple directional antenna, but requires access points to have additional physical space for a multielement antenna. In Section 7, we use measurements of amplitude for its ease of implementation. However, the HRUBE methods are generally applicable across channel measurement modalities discussed above.

A critical part of practical systems will be the ability to generate arbitrarily long secret keys. Research has addressed the use of multiple measurements to increase the size of the secret. As mentioned, Aono et al. [14] used multiple different beam patterns to allow for multiple measurements. Multiple measurements can also be made at many different frequencies [12]. Multiple measurements over time are used in [11], [13], [15], [6], [16], [17] to increase the number of bits in the secret. In this work, we provide a method to decorrelate an arbitrary vector of collected measurements. Previous works have often used correlated measurements to generate the secret key, which may be less robust to attacks.

Significant research has addressed the more general topic of obtaining a shared secret key from observations of correlated random variables [18], [19]. An eavesdropper can also observe a correlated random variable, and the secrecy information rate is shown to be a function of the mutual information between these three observed random variables. Analysis of the secrecy rate for UWB channels in [8], [10] and for fading channels in [13] have applied this analysis to the case in which the correlated random variables correspond to measured radio channel characteristics. Information-theoretic results have shown that two nodes cannot achieve an arbitrarily small bit disagreement rate without communicating some information over a common channel [18].

Because of these results, most reported research has used limited feedback [11], [9], [10], [13], [14], [6], [17] to correct small amounts of disagreement between the secret generated at the two ends of a link. This communication is referred to as "information reconciliation," "public feedback," or "error correction." In this paper, we assume that information reconciliation will be part of the system design, but we do not explore its use. We explore minimizing the rate of bit disagreement in order to reduce the quantity of information reconciliation that must be performed in order to reliably agree on a shared secret key.

As an alternative to information reconciliation, Sayeed and Perrig [7] suggest that when bit disagreements are seen in a secret key, nodes should simply regenerate a new secret until the secret key agrees. The work in [7] explores the energy trade-off between secret regeneration and transmit power (to increase the SINR at the ends of the link to reduce the probability of bit disagreement).

The majority of reported research has addressed system development from simulation and analysis using standard statistical channel models [8], [7], [11], [9], [10], [13], [15], [6]. Statistical channel fading models such as Rayleigh, Ricean, and Gaussian have been applied. These models can be used to compute the probabilities of secret key bit agreement, the probabilities that retransmission is necessary, and the bit rate which can be generated either in theory or by a particular encoding algorithm.

Notably, several researchers have reported experimental results and implementations [10], [12], [14], [16]. In [10],

several bidirectional UWB measurements are made and used to compute the number of secret key bits which could be generated. In [12], an implementation using the universal software radio peripheral (USRP) and GNU software radio generates and receives the required multicarrier signal and evaluates the bit rate of the system. Two implementations in [16] use both off-the-shelf and testbed 802.11a devices to implement secret sharing and achieve about a 1 bit per second rate. In [14], researchers use a steerable directional antenna in combination with Zigbee radio hardware to generate a secret between two nodes and test what an eavesdropper would have received. This work also demonstrates its techniques using a Zigbee radio implementation, but the techniques reported here are fundamentally unlike those reported in [14]. This paper reports in detail a new method for reliably estimating a high-rate uncorrelated bit stream from radio channel measurements.

We have not seen any secret key bit rate reported as high as achieved in our experiments, up to 22 bits/sec. In [16], an experimental implementation achieves about a 1 bit/sec rate, for which the authors target a  $10^{-8}$  bit disagreement rate. In this paper, we report experimental bit rates from 3 bits/sec at the lowest probability of bit disagreement (0.04 percent) to a rate of 22 bits/sec at the highest probability of bit disagreement (2.2 percent). There is a trade-off in secret key generation between high bit rate of the secret key and low probability of bit disagreement, and the proposed method can be used to provide a variety of achievable points, particularly at higher bit rates than previously reported.

#### 3 ADVERSARY MODEL

In our adversary model, we assume that the adversary, Eve, can listen to all the communication between Alice and Bob. Eve can also measure both the channels between herself and Alice and between herself and Bob at the same time when Alice and Bob measure the channel between them for key extraction. We also assume that Eve knows the key extraction algorithm and the values of the parameters used in the algorithm. However, we assume that Eve cannot be very close (less than a few multiples of the wavelength of the radio waves being used [16]) to either Alice or Bob while they are extracting their shared key. This will ensure that Eve measures a different, uncorrelated radio channel [4]. We assume that Eve cannot jam the communication channel between Alice and Bob. We also assume that Eve cannot cause a man-in-the-middle attack, i.e., our methodology does not authenticate Alice or Bob. In other words, the proposed system works against passive adversaries. In this aspect, the technique of key extraction from wireless signal strengths is comparable with classical key establishment techniques such as Diffie-Hellman, which also use message exchanges to establish keys and do not authenticate Alice or Bob. However, classical key exchange techniques make use of unproven assumptions about the computational hardness of different problems such as the discrete logarithm problem. In contrast, the proposed key extraction technique provides information-theoretic secrecy and does not assume any bound on the computational power of the adversary.

Even without an authentication mechanism, the Diffie-Hellman scheme has found widespread use in network security protocols and standards (e.g., for providing Perfect Forward Secrecy, Strong password protocols, etc.). We expect that our scheme will provide a strong alternative to the Diffie-Hellman scheme in wireless networks. There is a growing amount of work in authenticating wireless devices based on their physical and radiometric properties (e.g., [17], [20]). These and future authentication mechanisms can be used in conjunction with our secret key establishment scheme.

## 4 FRACTIONAL INTERPOLATION FILTERING

Channel measurements for secret key generation will almost certainly be half duplex, that is, the transmission from node a to node b is not made at the same time as the transmission from node b to node a. Standard transceivers cannot transmit and receive simultaneously, so nonsimultaneous measurements in the two directions must be dealt with regardless of the type of radio channel measurements made. As described in Section 2, many methods use sequential measurements over time in order to generate arbitrarily long secret keys. In this paper, we use fractional interpolation filters to allow nodes to estimate what the measurements would have been if they had been measured simultaneously.

For channel measurement, we assume that nodes repeatedly transmit packets in a TDD protocol.<sup>1</sup> Each node receives a packet from the other node and uses it to measure the channel characteristic. Let  $\mathbf{w}_a(i)$  be the *i*th channel measurement at node *a* made at time  $\tau_a(i)$ . We assume that the constant packet rate means the *i*th measurement is made at time  $\tau_a(i) = \tau_a(i-1) + T_{R,a}$  where  $T_R$  is the time since the previous measurement. Similarly, node *b* makes *i*th measurement  $\mathbf{w}_b(i)$  at time  $\tau_b(i) = \tau_b(i-1) + T_{R,b}$ .

We assume that channel measurements are made at greater than the Nyquist rate for the channel. For a fading channel, the Nyquist rate is twice the maximum Doppler frequency,  $f_d$ . Previous works have assumed that channel probes in the two directions are much more frequent than  $f_d$  [16]. In this work, probing requirements are relaxed somewhat because the signal can be reconstructed at simultaneous probe times as long as the probes are taken more often than  $\frac{1}{2f_d}$ , i.e., we always have  $T_{R,c} < \frac{1}{2f_d}$  for  $c \in \{a, b\}$ .

In general, given that samples are taken at least as fast as the Nyquist rate, interpolation can be performed regardless of whether  $T_{R,a}$  and  $T_{R,b}$  are constant over time, or if  $T_{R,a} \neq T_{R,b}$ . Thus, multiple-access delays, or delays due to retransmission, are acceptable within a limit. As a simple example, one might perform linear interpolation between samples to approximate the value of  $\mathbf{w}_a$  at time  $\tau$  with  $\tau_a(i-1) \leq \tau \leq \tau_a(i)$  as

$$\mathbf{w}_{a}(i-1) + [\tau - \tau_{a}(i-1)] \frac{\mathbf{w}_{a}(i) - \mathbf{w}_{a}(i-1)}{\tau_{a}(i) - \tau_{a}(i-1)}.$$
 (1)

If nodes agreed to interpolate to halfway between their probing times, then both nodes would use  $\tau = \frac{1}{2} [\tau_a(i) + \tau_b(i)]$  in (1). Since each node would be able to record transmission or reception times,  $\tau_a(i)$  and  $\tau_b(i)$  for all *i*, on its own clock, no

explicit synchronization is required in this procedure. Other approximation algorithms can use  $\tau_a$  and  $\mathbf{w}_a$  from multiple recent samples to perform higher order interpolation.

Here, for computational simplicity, we choose to implement a protocol which allows nodes a nearly constant packet rate. Thus, we assume  $T_R = T_{R,a} = T_{R,b}$  for all time. We define two fractional interpolation filters, one for each node. We define the fractional sampling offset  $\mu$  as

$$\mu = \frac{1}{2} \left[ \frac{\tau_b(i) - \tau_a(i)}{T_R} \right]. \tag{2}$$

Without loss of generality, assume that  $\tau_a(i) < \tau_b(i)$ , so that  $\mu > 0$ . If node *a* delayed its *i*th sample by  $(1 + \mu)T_R$ , and simultaneously, node *b* delayed its samples by  $(1 - \mu)T_R$ , we would have had simultaneous measurements. To estimate these delayed samples, we specify a fractional delay  $\mu_c$  and integer delay  $\bar{m}_c$  for each node:

$$egin{array}{ll} \mu_{a} = \mu, & \mu_{b} = 1-\mu, \ ar{n}_{a} = 1, & ar{m}_{b} = 0. \end{array}$$

After using a fractional interpolation filter to delay its signal by  $\mu_a = \mu$ , node *a* will also add an additional unit sample delay. Node *b* uses its fractional interpolation filter to delay its signal by  $\mu_b = 1 - \mu$ , and does not add any additional unit delays.

We use the Farrow filter, a finite-impulse response implementation which introduces an arbitrary fractional delay [21]. Standard implementations of the Farrow filter are four-tap FIR filters which provide a parabolic or cubic interpolation between samples. Such filters are often used in discrete-time implementations of receiver timing synchronization loops, and are well suited for DSP implementation [22]. We implemented a cubic Farrow filter, parameterized by  $\mu_a$  or  $\mu_b$ . For  $c \in \{a, b\}$ ,

$$\mathbf{h}_{e} = \left[\frac{\mu_{c}^{3}}{6} - \frac{\mu_{c}}{6}, -\frac{\mu_{e}^{3}}{2} + \frac{\mu_{c}^{2}}{2} + \mu_{c}, \\ \frac{\mu_{c}^{3}}{2} - \mu_{c}^{2} - \frac{\mu_{c}}{2}, -\frac{\mu_{c}^{3}}{6} + \frac{\mu_{c}^{2}}{2} - \frac{\mu_{c}}{3}\right]^{T}.$$
(3)

Note that  $\mathbf{h}_c$  requires recalculation only when  $\mu_c$  changes. The input of filter  $\mathbf{h}_c$  are the measurements  $\{\mathbf{w}_c(i)\}_i$ , and we define the output as  $\{\mathbf{x}_e(i)\}_i$ . These outputs are estimates of the radio channel at simultaneous instants, halfway between the original nonsimultaneous measurements. These vectors  $\mathbf{x}_a$  and  $\mathbf{x}_{b}$ ,

$$\mathbf{x}_a = [\mathbf{x}_a(1)^T, \dots, \mathbf{x}_a(N)^T]^T, \\ \mathbf{x}_b = [\mathbf{x}_b(1)^T, \dots, \mathbf{x}_b(N)^T]^T,$$

where N is the desired length of the vector. These vectors become the input for the decorrelation transformation discussed in the following section.

## 5 DECORRELATION TRANSFORMATION

In this paper, we use the discrete Karhunen-Loève transform (KLT) to convert the measured channel vectors  $\mathbf{x}_a$  and  $\mathbf{x}_b$  into uncorrelated components. The KLT has been applied for many different types of signals for purposes of noise

<sup>1.</sup> Whether or not the transmission is a data packet or any arbitrary finite-duration signal, we use the term "packet" to describe the transmission.

reduction and data compression. We apply the KLT for the purpose of generating nearly uncorrelated elements for our secret, which for robustness to attacks, should not contain significant correlation between elements.

The discrete KLT provides an orthogonal basis which decorrelates the input vector, assuming a known model for the covariance structure of the original vector. For particular classes of signals, we can find such statistical models; e.g., for electrocardiogram signals [23], voice signals, internet traffic measurements [24], and fingerprints [25], models have been developed from large sets of measurements. In this paper, we develop such a covariance model using a large set of measurements, and use it to calculate the appropriate KLT.

In the discrete KLT, a linear transformation of an input vector is taken, which results in a vector with uncorrelated elements. Assume that the (length *N*) input vector at node  $c \in \{a, b\}, \mathbf{x}_c$ , has mean  $\mu_c$  and covariance matrix  $R_{\mathbf{x}}$ .<sup>2</sup> A linear transform of the data is

$$\mathbf{y}_c = A^T (\mathbf{x}_c - \mu_c),$$

where *A* is an  $N \times N$  matrix. The mean of  $\mathbf{y}_c$  is zero, and the covariance matrix of  $\mathbf{y}_c, R_{\mathbf{y}}$ , is given by

$$R_{\mathbf{y}} = E[\mathbf{y}_{c}\mathbf{y}_{c}^{T}] = A^{T}R_{\mathbf{x}}A.$$
(4)

Assume the singular value decomposition of  $R_x$  is

$$R_{\mathbf{x}} = USU^T,\tag{5}$$

where U is the matrix of eigenvectors, and  $S = \text{diag}\{\sigma_1^2, \ldots, \sigma_N^2\}$ , a diagonal matrix of the corresponding eigenvalues. We assume that the eigenvectors have been sorted in order of decreasing eigenvalue, so that  $\sigma_1^2 \ge \sigma_2^2 \ge \cdots \ge \sigma_N^2 \ge 0$ . Note that  $U^T U = I_N$ , where  $I_N$  is the  $N \times N$  identity matrix.

The discrete Karhunen-Loève transform simply assigns A = U,

$$\mathbf{y}_c = U^T (\mathbf{x}_c - \mu_c). \tag{6}$$

The vectors  $\mathbf{y}_a$  and  $\mathbf{y}_b$  for nodes *a* and *b*, respectively, become the input for the MAQ scheme described in Section 6. When simplifying (4) we have the result that

$$R_{\mathbf{x}} = U^T R_{\mathbf{x}} U = U^T U S U^T U = S,$$

and the output vector  $\mathbf{y}_c$ , in fact, has a diagonal covariance matrix, indicating uncorrelated elements.

Note that uncorrelated is not the same as independent; while they are the same for Gaussian random vectors, they are not equivalent in general. The KLT guarantees zero covariance between elements, but not higher order cross-moments. Uncorrelated but not independent bits may result in a per bit entropy of less than 1.0; we show in Section 7.7 from experiments an entropy estimate of between 0.96 to 0.98. Depending on the true joint distribution, it may be possible for an attacker to use the higher order cross-moments to predict one value from others. Investigation of

this possibility must involve extensive measurements to allow inference on the joint distribution of the data  $y_{c'}$  and we leave this to future research.

#### 5.1 Bidirectional Measurement Covariance

Although the elements of  $\mathbf{y}_c$  are decorrelated by the KLT, there is still covariance between the  $\mathbf{y}_c$  and  $\mathbf{y}_{\bar{c}}$ , where c,  $\bar{c} \in \{a, b\}$ , and  $\bar{c} \neq c$ . That is, c and  $\bar{c}$  are the indices for the opposite direction measurements of the link between nodes a and b. In fact, a high positive correlation between the two different directions of the link is what enables secret sharing. We denote the covariance matrix of the original measurements to be  $R_{\mathbf{x}_c,\mathbf{x}_r}$ 

$$R_{\mathbf{x}_c,\mathbf{x}_{ar{c}}} \stackrel{ riangle}{=} E[(\mathbf{x}_c-\mu_c)(\mathbf{x}_{ar{c}}-\mu_{ar{c}})^T] = E[(\mathbf{x}_{ar{c}}-\mu_{ar{c}})(\mathbf{x}_c-\mu_c)^T].$$

After the KLT, the vectors  $\mathbf{y}_c$  and  $\mathbf{y}_{\bar{e}}$  have covariance matrix denoted as  $R_{\mathbf{y}_c,\mathbf{y}_{\bar{e}'}}$ 

$$R_{\mathbf{y}_c,\mathbf{y}_{\bar{c}}} \stackrel{\triangle}{=} E\left[\mathbf{y}_c \mathbf{y}_{\bar{c}}^T\right] = U^T R_{\mathbf{x}_c,\mathbf{x}_{\bar{c}}} U.$$
(7)

The *i*th diagonal element of  $R_{\mathbf{y}_c,\mathbf{y}_{\overline{c}}}$ , denoted here as  $[R_{\mathbf{y}_c,\mathbf{y}_{\overline{c}}}]_{i,i'}$  is the covariance of  $y_c(i)$  and  $y_{\overline{c}}(i)$ . The variance of  $\mathbf{y}_c$  is given by  $\sigma_i^2$  and is equal to the variance of  $\mathbf{y}_{\overline{c}}$  since  $c, \overline{c} \in \{a, b\}$ . So the correlation coefficient of the *i*th component, denoted  $\rho_{i'}$  is

$$\rho_i = \sqrt{\frac{[R_{\mathbf{y}_c, \mathbf{y}_c}]_{i,i}}{\sigma_i^2}}.$$
(8)

The correlation coefficient  $\rho_i$  is effectively a measure of the SNR of the measurement of the bidirectional *i*th component of **y**. When the "noise" contributing to both  $\mathbf{y}_a(i)$  and  $\mathbf{y}_b(i)$  is high, the value of  $[\mathbf{R}_{\mathbf{y}_e,\mathbf{y}_e}]_{i,i}$  is low compared to  $\sigma_i^2$ , and  $\rho_i$  is closer to zero. When there is very little noise,  $\rho_i$  is close to 1. In Section 6.4, we show that the value of  $\rho_i$  is the critical component to determine both how many bits to which the *i*th component can be quantized, and the performance of the quantization method, i.e., the probability that the bits generated agree at the two nodes.

## 6 MULTIBIT ADAPTIVE QUANTIZATION

The objective of this section is to describe the quantization of the transformed vector  $\mathbf{y}_c$ , for  $c \in \{a, b\}$ , into a secret key bit vector. Quantization in this application has two conflicting goals:

- 1. *Secret length maximization*: Obtain as long of a secret (in bits) as possible.
- 2. *Error minimization*: Keep the probability that the secret key will not match at nodes *a* and *b* as low as possible.

We also must maintain zero covariance between elements of secret key, and thus do not use vector quantization. Instead, we use scalar quantization on each element of  $\mathbf{y}_c$ . Consider this trade-off on a single component, component *i*. The quantizer for component *i* is a function  $Q_i : \mathbb{R} \to \{1, \ldots, 2^{m_i}\}$ , where  $m_i$  is the number of bits to which we quantize the *i*th component.

<sup>2.</sup> We assume that the mean at each node can be different due to the different transmit powers, but that the covariance matrix is the same at both nodes.

#### 6.1 Related Work: Censoring Scheme

Several past works in bit extraction from channel measurements have quantized each measurement to one of two bins and a "censor" region [16], [17], [14], [15]. In these methods, when a measurement has a value near zero, the measurement is not used in the secret, and otherwise, the measurement is quantized by its sign to a "0" or "1." This one bit and censor method, as a standard method used in related work, provides a good point of comparison for the MAQ method presented in this paper.

In the standard censoring method, a low threshold and a high threshold are specified, for example,  $[-\gamma, \gamma]$ . The indices of the values that fall within the threshold region are not encoded. Specifically, node *a* forms the set  $\mathcal{T}_a = \{i : -\gamma \leq x_a(i) \leq \gamma\}$  and transmits the list of the elements in  $\mathcal{T}_a$  to node *b*. Node *b* then similarly forms  $\mathcal{T}_b$  and transmits  $\mathcal{T}_b \setminus \mathcal{T}_a$  to node *a*. The union of both sets,  $\mathcal{T} = \mathcal{T}_a \cup \mathcal{T}_b$  are the indices not used in the shared secret. Let  $\overline{\mathcal{T}} = \{1, \ldots, N\} \setminus \mathcal{T}$  be the indices that will be used in the secret, and let  $t_j \in \{1, \ldots, N_T\}$  be the *j*th element of  $\overline{\mathcal{T}}$ , where  $N_T = |\overline{\mathcal{T}}|$ . Then, the secret key bit vector of node  $c \in \{a, b\}$  is given by  $\mathbf{z}_c = [z_c(1), \ldots, z_c(N_T)]^T$ , where

$$z_c(j) = \begin{cases} 1, & x_c(t_j) > \gamma, \\ 0, & x_c(t_j) < -\gamma. \end{cases}$$
 (9)

We note that the work in [16] does not directly encode  $x_c(i)$ . Instead, only one sample from each "excursion" of  $\{x_c(i)\}_i$  is encoded. An excursion is any sequence of  $\{x_c(i)\}_i$  which are either all above the high threshold or below the low threshold. This method allows high reliability in bit encoding while reducing correlation between subsequent bits.

The benefit of the one bit and censor scheme in general is that data that fall near zero, which would be likely to have opposite sign at the opposite end of the link, are not used in the secret. The value of  $y_a(i)$  would be known to an eavesdropper to be either within or outside of the threshold region, but this provides no information about whether the value is above  $\gamma$  or below  $-\gamma$ . If  $i \in T$ , the measurement is not used in the secret, and if  $i \notin T$ , the eavesdropper has no information about whether  $y_a(t_i)$  is greater than  $\gamma$  or less than  $-\gamma$ . So, the communicated data do not reveal anything about the generated secret key bits.

Compared to the method proposed in this paper, the censoring scheme has two main drawbacks. First, the use of censoring causes loss of bits. The number of bits lost to censoring depends on the measured data. In order to ensure a secret with a consistent number of bits, extra measurements must be gathered prior to bit extraction. In numerical results related in Section 7.6, between 5 percent and 27 percent of the measurements are lost to censoring. The second drawback is that it is not possible to generate more than one bit from each real-valued measurement, that is,  $m_i = 1$  for all *i*.

#### 6.2 Formulation

We propose a MAQ scheme for secret sharing. The MAQ scheme adaptively quantizes each measurement to an arbitrary number of bits without censoring. No fixed quantization scheme is able to achieve a low error rate because when  $y_a(i)$  is very near to a threshold, there is a

TABLE 1Example  $m_i = 1$ -Bit Adaptive Quantization Scheme

Bin	Codeword		е	Interval		
k	$d_1$	$d_0$		of $y(i)$		
1	0	0	0	$(-\infty, F_i^{-1}(0.125)]$		
2	0	0	1	$(F_i^{-1}(0.125), F_i^{-1}(0.25)]$		
3	0	1	1	$(F^{-1}(0.25), F^{-1}(0.375)]$		
4	0	1	0	$(F_i^{-1}(0.375), F_i^{-1}(0.5)]$		
5	1	1	0	$(F_{i}^{-1}(0.5), F_{i}^{-1}(0.625)]$		
6	1	1	1	$(F_i^{-1}(0.625), F_i^{-1}(0.75)]$		
7	1	0	1	$(F_i^{-1}(0.75), F_i^{-1}(0.875)]$		
8	1	0	0	$(F_i^{-1}(0.875), +\infty)$		

high probability that  $y_b(i)$  crosses to the other side of that threshold. As a solution, we propose to change the quantization scheme at both *a* and *b* based on the measurement at one of the nodes. For this discussion, without loss of generality, we assume that node *a* is the "leader" node in the multibit adaptive quantization scheme, and that node *b* is the "follower."

In the MAQ scheme, we first quantize  $y_a(i)$  to  $K \triangleq 2^{m_t+2} = 4 \times 2^{m_t}$  equally likely quantization levels. To achieve equally likely quantization levels, we require the distribution for  $y_a(i)$ . In general, let  $F_i(y) = P[y_a(i) \le y]$  be the cumulative distribution function (CDF) of  $y_a(i)$ . Thresholds for equally likely quantization bins are generated by using the inverse of the CDF,

$$\eta_k = F_i^{-1} \left( \frac{k}{4 \times 2^{m_i}} \right), \quad \text{for } k = 1, \dots, K - 1.$$
(10)

In the following, for ease of notation, let  $\eta_0 = -\infty$  and  $\eta_K = \infty$ . The *k*th quantization bin is the interval  $(\eta_{k-1}, \eta_k]$  for k = 1, ..., K, so k(i) is given by

$$k(i) = \max\{k \text{ s.t. } y_a(i) > \eta_{k-1}\}.$$
(11)

Next, we use a particular type of Gray code to adaptively assign a binary code word to each quantization bin. We do this by defining the following binary variables:

• Define e(k), for  $k = 1, \dots, K$  as

$$e(k) = \begin{cases} 1, & k \mod 4 \ge 2, \\ 0, & o.w. \end{cases}$$

In other words, e(k) is the 2s bit in the binary representation of integer k.

- Create a Gray code word with m<sub>i</sub> bits, that is, an ordered list of 2<sup>m<sub>i</sub></sup> possible m<sub>i</sub>-bit code words. A Gray code word list changes only one bit between neighboring code words in the list.
- Let f<sub>1</sub>(k) = [<sup>k-1</sup>/<sub>4</sub>]. Define d<sub>1</sub>(k) ∈ {0, 1}<sup>m</sup> to be equal to the f<sub>1</sub>(k)th Gray code word. That is, it is the same Gray code word list but with each element repeated four times.
- Let f<sub>0</sub>(k) = [<sup>k+1</sup>/<sub>4</sub> mod K]. Define d<sub>0</sub>(k) ∈ {0,1}<sup>m</sup>, to be equal to the f<sub>0</sub>(k)th Gray code. That is, it is the same list as d<sub>1</sub>(k) but circularly shifted by two.

Two examples are presented in Tables 1 and 2, for the case of  $m_i = 1$  and  $m_i = 2$ , respectively.

TABLE 2Example  $m_i = 2$ -Bit Adaptive Quantization Scheme

Bin	Codeword		e	Interval		
k	$d_1$	$d_1 = d_0$		of $y(i)$		
1	01	00	0	$(-\infty, F_i^{-1}(0.0625)]$		
2	01	- 00	1	$(F_i^{-1}(0.0625), F_i^{-1}(0.125)]$		
3	01	01	1	$(F_i^{-1}(0.125), F_i^{-1}(0.1875)]$		
4	01	01	0	$(F_i^{-1}(0.1875), F_i^{-1}(0.25)]$		
5	11	01	0	$[F_i^{-1}(0.25), F_i^{-1}(0.3125)]$		
6	11	01	1	$(F_i^{\perp 1}(0.3125), F_i^{\perp 1}(0.375)]$		
7	11	11	1	$[(F_i^{-1}(0.375), F_i^{-1}(0.4375)]]$		
8	11	11	0	$(F_i^{-1}(0.4375), F_i^{-1}(0.5)]$		
9	10	11	0	$(F_i^{-1}(0.5), F_i^{-1}(0.5625)]$		
10	10	11	1	$(F_i^{-1}(0.5625), F_i^{-1}(0.625))]$		
11	10	10	1	$(F_i^{-1}(0.625), F_i^{-1}(0.6875)]$		
12	10	10	0	$(F_i^{-1}(0.6875), F_i^{-1}(0.75)]$		
13	00	10	0	$[F_i^{-1}(0.75), F_i^{-1}(0.8125)]$		
14	00	10	1	$(F_i^{-1}(0.8125), F_i^{-1}(0.875)]$		
15	00	00	1	$(F_i^{-1}(0.875), F_i^{-1}(0.9325))$		
16	00	00	0	$(F_I^{-1}(0.9325), +\infty)$		

Multibit adaptive quantization proceeds as follows: First, from the values of  $y_a(i)$ , leader node *a* determines the quantization bin k(i) for all components *i*. Node *a* transmits the bit vector  $\mathbf{e} = [e(k(1)), \ldots, e(k(N))]^T$  to the follower node *b*. Both nodes then encode their secret key using code word  $d_1$  whenever e = 1, and code word  $d_0$  whenever e = 0. Specifically, the secret key is

$$\mathbf{z} = [d_{e(k(1))}(k(1)), \dots, d_{e(k(N))}(k(N))],$$

where k(i) is given in (11).

## 6.3 Discussion

The above MAQ scheme provides a new method for a multibit adaptive quantization for each component of vector y. No components are "censored," and instead, a leader node decides upon the quantization scheme from two options which is least likely to cause disagreement between the two nodes. When disagreements occur, due to the use of Gray coding, it is very likely that only one bit of the multibit code word will be in error.

Further, the passing of the vector e does not provide an eavesdropper with any information about the secret key bits. Knowing e(k(i)) eliminates half of the possible quantization levels. But code words are equally likely given the knowledge of e(k(i)). For example, for the  $m_i = 1$  case, if e = 1, then the eavesdropper knows that  $y_a(i)$  is neither very high in magnitude nor very low in magnitude. However, there are four possible equally likely bins with e = 1, two of which would be encoded with  $d_1 = 1$  and two with  $d_1 = 0$ . The eavesdropper has no information to which bit the component will be encoded.

## 6.4 Analysis of Probability of Bit Disagreement

The performance of a particular MAQ scheme is measured by its probability of bit disagreement ( $P_{BD}$ ), that is, the probability that nodes *a* and *b* encode a bit differently. We use the term "disagreement" rather than "error" because there is no notion of the "correct" bit to which *a* and *b* should have encoded when they disagree.



Fig. 2. Diagram showing area of  $F_i^{-1}(y_a)$ ,  $F_i^{-1}(y_b)$  where generated bits at *a* and *b* will agree (gray area) and disagree (white area) for the 1-bit adaptive quantization scheme.

In this section, we analyze bit disagreement probabilities as a function of the number of quantization bits  $m_i$  and the joint distribution of  $y_a(i)$  and  $y_b(i)$ . Let the joint probability distribution function (pdf) be  $f_{Y_a(i),Y_b(i)}(y_a, y_b)$ . As discussed, the two marginal distributions are identical, so we refer to the marginal pdf as  $f_i(y)$  and the CDF as  $F_i(y)$ . The conditional CDF of  $y_b(i)$  given  $y_a(i)$  is written as  $F_{Y_b(i)|Y_a(i)}(y_b|y_a)$ .

We first discuss the probability of code word disagreement, and then provide an approximation for the probability of bit disagreement. The two are the same in the  $m_i = 1$  case, but different in general.

For certain combinations of  $(y_a(i), y_b(i))$ , the code word at node *a* will be encoded differently than at node *b*, and these combinations can be viewed graphically on a 2D plot. Recall that node *a* is the leader node, and so  $y_a$  decides the quantization scheme. Given  $y_a(i)$ , the value of  $y_b(i)$  thus decides whether or not a bit disagreement occurs. For example, for the 1-bit adaptive quantization scheme displayed in Table 1, the combinations of  $(y_a(i), y_b(i))$  which result in bit agreement are shown in Fig. 2 as the gray shaded area. There is a wide diagonal area, where  $y_a(i)$  is close to or equal to  $y_b(i)$ , which would result in code word agreement.

If we refer to the shaded area of the diagram (the bit agreement area) as A, then the probability of code word agreement, denoted  $P_{CA}$ , is

$$P_{CA} = \int_{\mathbb{A}} \int_{\mathbb{A}} f_{Y_a(i),Y_b(i)}(y_a,y_b) dy_a dy_b.$$

Another way to write this equation is

$$P_{CA} = \int_{y_a} P[CA|y_a] f_i(y_a) dy_a, \qquad (12)$$

where  $P[CA|y_a]$  is the probability of code agreement given  $y_{a}$ ,

$$P[\operatorname{CA}|y_a] = \int_{y_b \in A(y_a)} f_{Y_b(i)|Y_a(i)}(y_b|y_a) dy_b,$$

and  $A(y_a) = \{y_b : (y_a, y_b) \in A\}.$ 

#### 6.5 MAQ Performance in Gaussian Case

For the case that  $y_a(i)$  and  $y_b(i)$  are jointly Gaussian and zero mean, we can find a more direct expression for the



Fig. 3. Analytical approximation for the probability of bit disagreement from (17) as a function of number of bits per code word, m, and correlation coefficient,  $\rho$ .

probability of code agreement. Note that we know that the marginal variances of  $y_a(i)$  and  $y_b(i)$  are identical, which we denote as  $\sigma_i^2$ . Let the correlation coefficient of  $y_a(i)$  and  $y_b(i)$  be  $\rho_i$ . Then the conditional pdf of  $Y_b(i)|Y_a(i)$  has mean  $\rho_i Y_a(i)$  and variance  $\sigma_i^2(1-\rho_i^2)$ . Thus,  $P[CA|y_a]$  for the 1-bit adaptive quantization case can be written as

$$P[CA|y_a] \ge \Phi\left[\frac{F^{-1}(\alpha_{y_a}) - \rho_i y_a}{\sigma_i \sqrt{1 - \rho_i^2}}\right] - \Phi\left[\frac{F^{-1}(\beta_{y_a}) - \rho_i y_a}{\sigma_i \sqrt{1 - \rho_i^2}}\right],$$
(13)

where  $\Phi(x)$  is the unit-variance Gaussian CDF, and  $\alpha_{y_a}$  and  $\beta_{y_a}$  are the high and low limits for a given  $y_a$  of the segment of  $y_b$  which results in code word agreement. For the 1-bit adaptive quantization case, it can be seen from Fig. 2 that

$$\alpha_{y_a} = \begin{cases} 0.25, & F_i(y_a) \le 0.125, \\ 0.5, & 0.125 < F_i(y_a) \le 0.375, \\ 0.75, & 0.375 < F_i(y_a) \le 0.625, \\ 1, & 0.625 < F_i(y_a), \\ 0.5, & 0.375 \le F_i(y_a) < 0.375, \\ 0.25, & 0.375 \le F_i(y_a) < 0.625, \\ 0.5, & 0.625 \le F_i(y_a) < 0.875, \\ 0.75, & 0.875 \le F_i(y_a). \end{cases}$$

In general, for an  $m_i$ -bit quantization scheme,

$$\begin{aligned} \alpha_{y_a} &= \min\{1, \left\lceil F_i(y_a) + 2^{-(m_i+2)} \right\rceil_{2^{-(m_i+1)}}\},\\ \beta_{y_a} &= \max\{0, \left| F_i(y_a) - 2^{-(m_i+2)} \right|_{2^{-(m_i+1)}}\}, \end{aligned} \tag{14}$$

where we define the u-multiple floor and ceiling functions which return the highest multiple of u lower than its argument, and the lowest multiple of u higher than its argument, respectively

$$\lfloor x \rfloor_{u} = u \Bigl\lfloor \frac{x}{u} \Bigr\rfloor, \quad \lceil x \rceil_{u} = u \Bigl\lceil \frac{x}{u} \Bigr\rceil.$$
(15)

Equation (13) is less than or equal to the exact *P*[agreement] because we only consider the main diagonal area of agreement. For example, we do not consider the top-left area



Fig. 4. Diagram showing area of  $(y_a, y_b)$  where generated bits at a and b will agree (gray area), disagree (white area), and will be censored (crosshatched area) for the censoring scheme.

and bottom-right area in Fig. 2. These nondiagonal elements will typically have a very small probability, because they correspond to observing nearly opposite values on the two directional measurements. Since the two measurements have high positive correlation, it is highly unlikely to observe nearly opposite values.

Using (12) and (13), we can solve for a lower bound on the probability of agreement. We note that for the Gaussian case,  $F_i^{-1}(x) = \sigma_i \Phi^{-1}(x)$  where  $\Phi^{-1}(x)$  is the inverse of the zero-mean unit-variance CDF. A substitution of  $v = y_a/\sigma_i$  results in the expression,

$$P_{CA} \ge \int_{v=-\infty}^{\infty} \left\{ \Phi \left[ \frac{\Phi^{-1}[\alpha_{\sigma_i v}] - \rho_i w}{\sqrt{1 - \rho_i^2}} \right] - \Phi \left[ \frac{\Phi^{-1}[\beta_{\sigma_i v}] - \rho_i v}{\sqrt{1 - \rho_i^2}} \right] \right\} \frac{e^{-v^2/2}}{\sqrt{2\pi}} dv.$$

$$(16)$$

Note that (16) is not a function of  $\sigma_i$ , the variance of the *i*th component of **y**. Instead, it is solely a function of  $\phi_i$  and  $m_i$ . Note that the probability of code disagreement  $P_{CD} = 1 - P_{CA}$ , from the lower bound in (16), we have an upper bound on  $P_{CD}$ . Borrowing from digital communications analysis of Gray coded symbol constellations, for low  $P_{CD}$ , we can approximate the probability of *bit* disagreement,  $P_{BD}$ , as

$$P_{BD} \approx P_{CD}/m_i. \tag{17}$$

This expression (16) is solved numerically, and results for the  $P_{BD}$  are plotted in Fig. 3.

## 6.6 Censoring Scheme Performance in Gaussian Case

The multibit adaptive quantization scheme offers the possibility of encoding a component with more than one bit, which is not possible in the existing censoring scheme. However, for the  $m_i = 1$  case, we can compare the two bit extraction schemes and evaluate their relative benefits.

We begin by formulating the probability of bit disagreement in the censoring scheme. The bit is censored whenever either *a* or *b* measures a value between  $-\gamma$  and  $\gamma$ . Agreement occurs whenever both  $y_a(i) < -\gamma$  and  $y_b(i) < -\gamma$ , or whenever both  $y_a(i) > \gamma$  and  $y_b(i) > \gamma$ . These cases are shown in Fig. 4, which is analogous to Fig. 2 for the 1-bit MAQ scheme.



Fig. 5. Analytical probability of a bit being censored in the censoring scheme versus  $\rho$  and  $\gamma.$ 

Assuming a joint Gaussian distribution for  $(y_a, y_b)$ , as assumed in Section 6.5, we can calculate the probability of censoring, P[Cens], and the probability of bit disagreement.

$$P[\text{Cens}] = \int_{v} P[\text{Cens} |v] \frac{e^{-v^{2}/2}}{\sqrt{2\pi}} dv, \qquad (18)$$

$$P[\operatorname{Cens} |v] = \begin{cases} 1, & \operatorname{if} -\frac{\gamma}{\sigma_i} \le v < \frac{\gamma}{\sigma_i}, \\ \Phi\left[\frac{\gamma/\sigma_i - \rho_i v}{\sqrt{1 - \rho_i^2}}\right] - \Phi\left[\frac{-\gamma/\sigma_i - \rho_i v}{\sqrt{1 - \rho_i^2}}\right], & \operatorname{o.w.} \end{cases}$$

This expression is only a function of  $\gamma/\sigma_i$  and  $\rho$ , and is plotted in Fig. 5. Similarly, the probability of bit disagreement for the censoring scheme (given that it is not censored) is given by

$$P_{BD} = \frac{1}{1 - P[\text{Cens}]} \int_{v} P[\text{BD} | v] \frac{e^{-v^{2}/2}}{\sqrt{2\pi}} dv,$$

$$P[\text{BD} | v] = \begin{cases} 1 - \Phi\left[\frac{\gamma/\sigma_{i} - \rho_{i}v}{\sqrt{1 - \rho_{i}^{2}}}\right], & v < \frac{-\gamma}{\sigma_{i}}, \\ \Phi\left[\frac{-\gamma/\sigma_{i} - \rho_{i}v}{\sqrt{1 - \rho_{i}^{2}}}\right], & v > \frac{\gamma}{\sigma_{i}}, \\ 0, & \text{o.w.} \end{cases}$$
(19)

The performance of the censoring scheme should be judged on the probability of bit disagreement given that the bit is used in the secret (is not censored). This is why the conditional probability of bit disagreement is divided by the factor of (1 - P[Cens]). The result is plotted in Fig. 6.

#### 6.7 Performance Discussion and Comparison

We can compare the results in Fig. 6 to the m = 1 line in Fig. 3. For low thresholds  $\gamma$ , the censoring scheme results in a higher probability of bit disagreement than the 1-bit MAQ scheme. At high  $\gamma$  (e.g., the  $\gamma/\sigma = 0.2$  case) censoring can provide a lower bit disagreement probability than 1-bit MAQ. However, at high  $\gamma$ , many bits are censored. For example, for  $\gamma/\sigma = 0.2$  and  $\rho = 0.96$ , the censoring scheme achieves conditional probability of bit disagreement of 0.01 compared to 0.03 for the 1-bit MAQ scheme, but the censoring scheme must censor 24.7 percent of components.

For a moment, ignoring the loss of bits caused by the censoring scheme, we consider when to use the censoring scheme instead of the MAQ scheme. When the correlation



Fig. 6. Analytical probability of bit disagreement from (19) versus  $\rho$  and censoring threshold  $\gamma$ , given that the bit is not censored.

coefficient  $\rho$  is low, the threshold can be set high, and the conditional probability of bit disagreement can be made lower in the censoring scheme. For example, if one wishes to design for highest possible bit rate with  $P_{BD} \leq 0.04$ , one would choose m = 1 for  $0.95 < \rho < 0.98$ , m = 2 for  $0.98 < \rho < 0.993$ , and m = 3 for  $0.993 < \rho < 0.998$ . For the m = 1 case, the censoring scheme could be used in order to lower the probability of bit disagreement at the expense of higher probability of censoring. In this example, if we have components *i* with  $\rho_i > 0.98$ , the MAQ scheme offers more bits per measurement component.

## 7 EXPERIMENTAL IMPLEMENTATION

In this section, we present the collection of a set of testbed RSS measurements on a bidirectional link and use the data to provide an example of the implementation and performance of the HRUBE method.

## 7.1 Setup

We use Crossbow TelosB wireless sensors which are connected via a USB connection to a laptop in order to record the collected data for postprocessing and analysis. The TelosB mote is a low power wireless sensor module equipped with an IEEE 812.15.4-compliant RF transceiver (the TI CC2420), built-in antenna and a microcontroller. In general, wireless sensors are designed for low data rate and low computation and memory capabilities, and the TelosB can send 250 kbps. We choose the hardware to show the ability of simple hardware devices to collect channel data useful for secret key exchange.

We program the TelosB 802.15.4 radios to transmit and receive packets which are used as channel probes. In general, any data could be sent in the probe packets, including application data. In our implementation, the packets include only minimal data: the packet header, a node id, and a sequence number. When one radio receives a packet, it measures and records the RSS and stores it with the packet sequence number. Then, it increments the sequence number and replies with a packet with the incremented sequence number. This process repeats until the two nodes have collected enough probe data. Each packet contains a total of 10 bytes and thus has a duration of 40  $\mu$ s. Processing time dominates the packet duration, and the channel is measured at a rate of approximately 100 probe packets per second, or 50 probes per node.

1200

900

600 300

0.999

0.99

0.9

Variance o

Corr. Coef.p

**Counter Value** Fig. 7. Raw measured RSS values from a to b (+), from b to a (o), and from b to e (\*).

In any implementation, the RSS value measured by a receiver is device specific. On the TelosB, the RSS is a signed 8-bit integer value, a value proportional to the measured average received power over the duration of the packet, in decibel milliwatts (dBm). While this integer value could be converted to a dBm value, it is unnecessary for our purposes, since all testbed radios are TelosB devices and thus have the same RSSI characteristic.

Our experimental tests involve two nodes, a and b, about 0.5 meters apart, measuring link (a, b). The original channel measurement vectors  $\mathbf{w}_a$  and  $\mathbf{w}_b$  are the lists of measured RSS values at nodes a and b, respectively. Fig. 7 shows an example of  $\mathbf{w}_a$  and  $\mathbf{w}_b$  measured over the course of 100 channel probes. It shows some differences between the two directional measurements, but the large-scale changes of the two signals over time are remarkably similar. The tests also include the measurement at an eavesdropper node e which receives but never transmits. Node e is located about 1.5 m from node b and can measure the RSS on the channels (a, e) and (b, e). Fig. 7 also shows the measurement of RSS on link (a, e). The signal at the eavesdropper is qualitatively very different from the true link measurements.

Motion of one of the nodes is used to generate fading changes in the RSS measurements, which is critical to observing fading during short-term experiments in indoor environments. During the experiment, the experimenter continuously moves one of the nodes in a "random" manner, above, below, and around its starting position. Three experiments are conducted, each for a duration of about 1,000 seconds. In this paper, we chose to measure vectors with length N = 50. Since measurements are taken approximately 50 per second, each vector takes 1 second to record. The long duration of the experiment ensures that we have enough data to characterize mean and covariance statistics.

## 7.2 Interpolation

Our measurement protocol lacks explicit time synchronization, but the protocol approximately achieves a fractional time offset of 1/2 at all times. The protocol is synchronized in the sense that each node transmits a packet as soon as it finishes receiving a probe packet from the other node. The delay between reception and transmission is nearly the same at each node because they have the same hardware and run the same software.



10

Component

20

Packets can be delayed or dropped due to interference (nodes operate in the same band as WiFi), but we ignore these effects. We assume that  $\frac{\tau_b(1)-\tau_a(1)}{T_R}$  is approximately equal to 1/2. That is, node *b*'s probes are sent halfway in between the previous and subsequent node *a* probes. This leads to  $\mu = 0.25$  in (2). Our measured values  $\mathbf{w}_a$  and  $\mathbf{w}_b$  are run through the interpolation procedure described in Section 4 and the synchronized data  $\mathbf{x}_a$  and  $\mathbf{x}_b$  are then formed using (4).

#### 7.3 Data Model

We use the measured data from the first experiment (of three) to estimate the mean vectors  $\mu_{\mathbf{x}_a}$  and  $\mu_{\mathbf{x}_b}$ , and covariance matrix  $R_{\mathbf{x}}$  of the data vectors, which is estimated as

$$\mu_{\mathbf{x}_{a}} = \frac{1}{C} \sum_{i=1}^{C} \mathbf{x}_{a}^{(i)}, \quad \mu_{\mathbf{x}_{b}} = \frac{1}{C} \sum_{i=1}^{C} \mathbf{x}_{b}^{(i)},$$
$$\hat{R}_{\mathbf{x}} = \frac{1}{2C - 1} \left[ \sum_{i=1}^{C} \left( \mathbf{x}_{a}^{(i)} - \mu_{a} \right) \left( \mathbf{x}_{a}^{(i)} - \mu_{a} \right)^{T} + \sum_{i=1}^{C} \left( \mathbf{x}_{b}^{(i)} - \mu_{b} \right) \left( \mathbf{x}_{b}^{(i)} - \mu_{b} \right)^{T} \right],$$
(20)

where  $\mathbf{x}_{e}^{(i)}$  is the *i*th 50-length measured RSS vector at node *c*, and W = 49,951 is the total number of RSS vectors which can be formed from the measured data at each node.

Next, we also calculate the covariance between a measurement and the same measurement on the reverse link:

$$\hat{R}_{\mathbf{x}_{*},\mathbf{x}_{e}} = \frac{1}{2C-1} \left[ \sum_{i=1}^{C} \left( \mathbf{x}_{a}^{(i)} - \mu_{a} \right) \left( \mathbf{x}_{b}^{(i)} - \mu_{b} \right)^{T} + \sum_{i=1}^{C} \left( \mathbf{x}_{b}^{(i)} - \mu_{b} \right) \left( \mathbf{x}_{a}^{(i)} - \mu_{a} \right)^{T} \right].$$
(21)

## 7.4 Decorrelation Transform

From  $\hat{R}_{x}$ , we calculate the SVD as given in (5). We plot the eigenvalues of each eigenvector (the variance of each component) in the top subplot of Fig. 8. Then, using the KLT matrix U, we calculate the cross-directional covariance matrix from (7) and use it to calculate the correlation coefficients  $\rho_i$  as given in (8). These correlation coefficients are plotted in the bottom subplot of Fig. 8. The highest





Fig. 9. First nine eigenvectors in the (a) temporal and (b) frequency domains. Frequency domain shows real (black square) and imaginary (gray triangle) components.

correlation coefficient is 0.9965; there are seven components with  $\rho > 0.98$  and 14 components with  $\rho > 0.95$ .

Fig. 9 shows the first nine eigenvectors of  $R_x$ , the columns of U, both in the time domain and in the frequency domain. The results show that the eigenvectors are nearly pure sinusoids. For short periods of time (our measurement vectors are recorded within one second), we can consider the fading signal to be a wide-sense stationary (WSS) random process, and as such, its eigenvectors should be complex exponentials. For longer periods of time, motion may not be WSS because of changes in the nature of the motion in the channel or of the nodes themselves. Future work should address the stationarity of the fading process during secret



Fig. 10. Series of  $y_a(2)$  and  $y_b(2)$  for 23 subsequent measured vectors which show the level of agreement between bidirectional measurements.

TABLE 3 Three System Designs: Analytical Gaussian  $P_{BD}$ and Actual Bit Disagreement Rates

System	Total	Bit Disagreement:				
Number	Bits	Design	Actual Rate			
1	22	0.040	0.0220			
2	10	0.010	0.0054			
3	3	0.001	0.0004			

generation. Future implementations may also wish to use an FFT of the measured RSS values rather than the KLT in order to reduce computational and memory complexity.

Next, we apply the data model to experimental data sets two and three. We transform the measured data vectors  $\mathbf{x}_e$ from these latter two data sets using the KLT to compute the values of  $\mathbf{y}_e = U^T(\mathbf{x} - \mu_e)$ , for  $c \in \{a, b\}$ . Since we have recorded many seconds of RSS values in the two experiments, we have several realizations of  $\mathbf{y}_a$  and  $\mathbf{y}_b$  at nodes aand b, respectively. For example, Fig. 10 shows the values of the second component at nodes a and b for direct comparison. It is clear that the two directional measurements are very similar to each other in comparison with the changes from realization to realization.

#### 7.5 MAQ Implementation

Next, we perform multibit adaptive quantization on the measurements  $y_a$  and  $y_b$ . In this implementation, node a is used as the leader, and node b is the follower. We design three systems for different desired bit disagreement rates. For example, in the first system, we design for a  $P_{BD} = 0.04$ . We are limited in the number of bits per component by the component's correlation coefficient. The correlation coefficients of the first dozen components are listed in the first column of Table 4. Using Fig. 3, for each  $\rho_i$ , we look up the maximum number of bits  $m_i$  which achieves  $P_{BD} \leq 0.04$  (or other system design specification). These are the values of  $m_i$  listed in a column of Table 4. We attempt three different system designs:  $P_{BD} = 0.040$ , 0.010, and 0.001, for system designs 1, 2, and 3, respectively. These specifications are listed in Table 3, along with the total number of bits generated from all components for each system design. Since  $m_i$  must be an integer and is chosen conservatively  $(P_{BD} \leq 0.04 \text{ for all } i \text{ for system design 1})$ , we would expect a lower actual bit disagreement probability than the design.

Note that a MAQ implementation needs to assume the marginal distributions in order to calculate the thresholds  $\eta_i$ . We assume, again, that  $y_a(i)$  and  $y_b(i)$  are zero mean and jointly Gaussian. However, rather than exchange measured

TABLE 4 Three System Designs: Bits by Component

		m <sub>i</sub> for System					m <sub>i</sub> for System		
i	$\rho_i$	#1	#2	#3	i	$\rho_i$	#1	#2	#3
1	0.9965	3	2	1	9	0.9746	1	0	0
2	0.9919	2	2	1	10	0.9706	1	0	0
3	0.9896	2	1	1	11	0.9681	1	0	0
4	0.9869	2	1	0	12	0.9649	1	0	0
5	0.9848	2	1	0	13	0.9600	1	0	0
6	0.9827	2	1	0	14	0.9535	1	0	0
7	0.9802	2	1	0	15	0.9464	0	0	0
8	0.9781	1	1	0	16	0.9413	0	0	0

marginal variances via radio communication, which might give away to an eavesdropper some information about the spread of measured values, we calculate locally the variance  $\sigma_i^2$  at each node from its own collection of measured y values. For example, at node *a*, we use the collected realizations of  $y_a(i)$  through the course of the experiment to compute the variance of  $y_a(i)$  for use at node *a*. Future implementation work will need to study the trade-off between latency and other methods for estimating the variances of each component.

#### 7.6 Experimental Performance

Finally, we run each system through the data collected experimentally. The experimental bit disagreement rate is computed by counting the number of bits for which nodes a and b disagree and dividing by the total number of bits generated in the course of the experiments. Table 3 shows the results. In each system design, the actual bit disagreement rate is lower than the  $P_{BD}$  for which the system was designed. Since  $m_i$  is chosen conservatively, as described in Section 7.5, we expect the design specification to be an upper bound on  $P_{BD}$ .

The system designs also show that a large number of bits can be extracted from the channel measurements. At the highest  $P_{BD}$ , we can extract 22 bits per second. This compares well to [16] which describes an implementation which achieves approximately one bit per second.

Note that the secret key generation rates from the HRUBE method, including the 22 bits/sec system, are not reconciled; at a bit disagreement rate of 2.2 percent, on average, one out of the 22 bits will disagree about 40 percent of the time. Other research has used information reconciliation procedures to reveal small amounts of information between two nodes that permitted correction of limited numbers of bit disagreements, as discussed in Section 2. We assume that such reconciliation will be implemented as part of a secret key generation system which reliably finds keys which agree at the two ends of a link.

## 7.7 Statistical Tests of Correlation

We have designed the HRUBE method so that, any pair of bits within secret key vector z has zero correlation. In this section, we use our large set of measured data to estimate the correlation coefficient between bits and test for nonzero correlation. We estimate two types of correlation coefficients:

- 1. *Pairwise bit correlation coefficients*. We denote  $\rho_{z_i,z_j}$  as the correlation coefficient between the *i*th and *j*th component of vector  $\mathbf{z}$ , for  $i \neq j$ .
- 2. Global bit correlation coefficient. We denote  $\rho_z$  as the correlation coefficient between all pairs of different components of z. A single correlation coefficient is only valid if the correlation between any pair of bits in z is assumed to be identical.

From the measured data, we generate n = 833 realizations of the vector **z** from our data, from which estimated pairwise bit correlation coefficients  $\{\hat{\rho}_{z_i,z_j}\}_{i,j}$  range from -0.10 to +0.12. The estimated global bit correlation coefficient  $\rho_z$  is -0.0036.

Clearly, the *estimated* correlation coefficients will never be precisely zero, even if  $\rho = 0$  exactly. So, for the given number of realizations, we provide hypothesis tests to quantify if these nonzero correlation coefficient estimates are likely, or unlikely, to have been generated if the true  $\rho = 0$ . Formally, the decision is

$$\begin{aligned} H_0: \rho &= 0, \\ H_1: \rho &\neq 0. \end{aligned}$$
 (22)

The hypothesis test is performed on statistic t [26],

where  $\hat{\rho}$  is the correlation coefficient estimated from the data and *n* is the number of realizations used in the estimate, and  $\gamma$  is a threshold, set based on the desired probability of false alarm. The statistic *t* has the Student-t distribution with n - 2 degrees of freedom. Furthermore, in the limit for high *n*, the distribution of *t* approaches the zero-mean unit-variance Gaussian distribution. In practice, n > 100 is high enough for this approximation to hold.

For the pairwise bit correlation coefficients, the estimated *t*-statistics for each pair are group tested; that is, the threshold  $\gamma$  is set so that the total probability of false alarm is 5 percent. For the given parameters,  $\gamma = 3.70$ . For the three systems in Table 3, all of the correlation coefficients  $\rho_{z_b z_j}$  have  $t < \gamma$ . The global bit correlation coefficient,  $\rho_z$ , has t = 1.74, below the threshold  $\gamma = 1.96$  chosen for false alarm rate 5 percent.

We also estimate the entropy of the bit sequence output from the HRUBE system, using the NIST random generator test suite [27]. For systems 1, 2, and 3 (shown in Table 3), the experimental entropies are estimated to be 0.959, 0.981, and 0.981, respectively, per generated bit.

#### 7.7.1 Discussion

Both tests indicate that the correlation coefficient between bits in z is not statistically significantly different from zero. The best estimate of  $\rho_z$  is -0.0036. We have similarly run tests on other sets of collected data; some data sets pass the correlation test and decide  $H_0$ , those that decide  $H_1$  cross the threshold  $\gamma$  only by a small margin. It is fair to say that there may exist small correlations, perhaps  $|\rho| < 0.01$ , but when given a high number of realizations n, a test may detect these small correlations.

Nonzero correlations can be caused by imperfect knowledge of the covariance matrix of the interpolated RSS sample vector **x**. Small changes in the covariance structure over time may occur, and when this occurs, the KLT based on a static transformation matrix U in (6) does not produce a completely uncorrelated sample vector output. Future work should develop methods to adaptively update the KLT from recently measured data to further reduce correlations in bit outputs.

Note that subsequent bit vectors z are not designed for zero correlation with each other. The HRUBE decorrelates a set of *N* RSS samples and then produces a bit vector z. A later set of *N* RSS samples produces another bit vector z' which may be correlated with the first vector z. A system designer should either 1) set *N* high enough such that enough bits can be obtained from one bit vector z, or 2) allow time to pass between the first and second set of RSS samples such that the two sets of samples are uncorrelated. This is a trade-off between latency, computational complexity, and correlation, which must be studied prior to system deployment.

#### 8 CONCLUSION

This paper provides a general framework, which we call HRUBE, for the extraction of secret uncorrelated bit vectors from a series of radio channel measurements. The framework includes interpolation, decorrelation transformation of the data, and then an adaptive quantization scheme to allow each component to be quantized to an arbitrary number of bits. Analysis has been developed to calculate the probability of bit disagreement using the HRUBE scheme, which is used to design systems with a given bound on probability of bit disagreement. Numerical results are reported for the case of bivariate Gaussian measurements. We show, via an implementation of HRUBE, some examples of the bit rate versus  $P_{BD}$  trade-off, including the possibility of achieving 22 bits per second at a bit disagreement rate of 2.2 percent, or achieving 10 bits per second at a bit disagreement rate of 0.54 percent. Experimentally, pairs of bits within one bit vector show a correlation coefficient of -0.0036, close to perfect decorrelation.

Future work must apply the HRUBE method to other modes of radio channel measurements and improve the distributional assumptions. In particular, the joint distribution of  $y_a(i)$  and  $y_b(i)$  should be thoroughly investigated using large sets of measured data. Many of the system design choices (distribution parameters, number of bits per component) might be trained in real time from initial measurements, and research should investigate such methods. For example, quantization levels  $\{\eta_k\}$  could be determined by each node on its own from measured vectors y; or nodes could periodically (perhaps once per secret) communicate to set them. Research should also investigate adaptive update of the KLT in order to achieve even lower correlation between bits. Of course, additional research should be performed from an attacker's perspective: to attempt to "break" secret keys generated from extraction methods which are seen as weak or to deny the ability of two radios to agree on a secret key. Research must design key generation systems to be as robust as possible to such attacks. The general problem of bit extraction for secret key generation, i.e., translating radio channel measurements into shared secret key bits, is generally an open statistical signal processing problem, and one that may have direct impact for the improvement of wireless network security.

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