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Optimisation of schedules for the inspection of railway tracks

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Review of Railway Track Inspection Schedule Optimisation

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Abstract

Railway track inspection involves a high volume of short-duration tasks (e.g. visual inspection, vehicle-based inspection and measurement, etc.) each of which is repeated at different frequencies and time intervals. It is important to gain as many benefits as possible from the inspection tasks, which incur huge expenses. To date, various optimisation methods have been incorporated into the schedule generation to determine an inspection order for known number and geographical location of tracks. Due to the specific requirements of certain tracks or inspection problem —for example, the number of schedule parameters and one-off or incremental type schedules—researchers have developed more sophisticated and problem-dependent optimisation methods. However, an introduction of new inspection scheduling problem in order to cope with new operational and business constraints. Thus, this paper conducts a review and gap analysis of previous studies of track inspection scheduling problems from an optimisation point of view. Apart from that, we discuss several potential research interests resulting from the gap analysis undertaken. This study shows that heuristic methods are popular among researchers in searching for an optimal schedule subject to single or multiple optimisation function(s) while satisfying various technical and business constraints.

Keywords

Visual inspection, scheduling optimisation, constrained optimisation problem, railway track, track maintenance management, disruption

Introduction

As stated under the Health and Safety at Work Act (HSWA) 2 of 1974, it becomes a duty of the railway infrastructure 3 manager (RIM) to provide a reliable track system, which Λ in turn ensures the safety of passengers, including staff¹. 5 Failing to maintain the service performance of tracks at an adequate level can negatively affect an overall railway 7 infrastructure (RI) performance, which is a function of 8 safety, train punctuality, overall capacity utilization and 9 costs². For that purpose, track maintenance and renewal 10 (TMnR) works are generally planned and executed to 11 meet a specific range of safety i.e. what is reasonably 12 practicable^{3;4}. Besides complying with safety regulations, 13 e.g. the HSWA, track maintenance offers substantial benefits, 14 such as a reduction in the risk of train derailment⁵ and 15 controlling noise and vibration emissions for passenger 16 comfort⁶. Realising TMnR is regular every year and a costly 17 activity, thus the pressure motivates the development of 18 track maintenance model (TMM), see⁷, which thereby it can 19 assist RIM organisations in many aspects, such as resource 20 utilisation, possession costs and time periods between two 21 consecutive maintenance interventions^{8;9}. In addition, a life 22 extension of life track components can be gained. 23

Figure 1 depicts a basic decision model of TMnR which consists of two main blocks (referring to the dashed square), track condition analysis and decision-making. To answer the core question in a decision-making block, which is when track maintenance is necessary and when the best time for track renewal is, the block demands an up-to-date, i.e., near to real time, condition status of track and the associated 30 components which can be acquired from the deterioration 31 models^{10;11}. Some references, e.g.^{12–14}, identified condition 32 based maintenance (CBM) as a reliable strategy/approach 33 that can provide a real (or near to real) assessment of a 34 component that instantaneously inform IMs if the monitored 35 component is no longer in normal condition or a fault is 36 impending. 37

As its name suggests, CBM reaches a maintenance 38 decision based on useful information gathered through 39 condition monitoring. Condition of the targeted component 40 may be monitored on-line (automated, continuous) or off-41 line (manual, regular, on-site). Currently in the United 42 Kingdom, regular condition monitoring which requires RIMs 43 to perform on-site inspections on the targeted components 44 at determined time intervals, still the primary way of 45 measuring and gathering track geometric characteristics and 46 track structure condition data. Those gathered information 47 is then analysed to facilitate recovery from defects and 48 damages, improvements in ride comfort, and elimination 49

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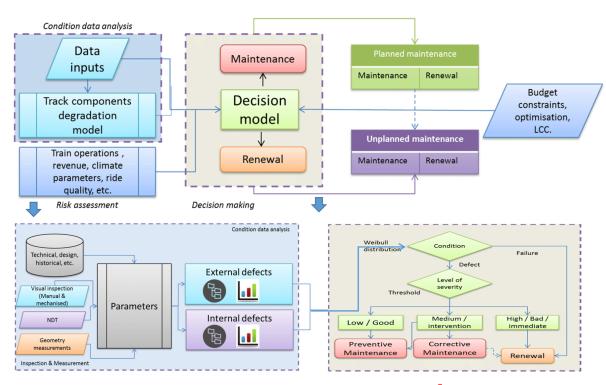


Figure 1. A representation of basic track maintenance decision model, redrawn from Guler

of potential safety hazards^{15;16}. Visual track inspection that cover both foot (manned) and mechanised inspection style 2 will dominate the market for many years to come until a 3 self-inspection (automated) regime is ready for full-scale 4 implementation¹⁷. Note that, on-line condition monitoring 5 may be the best approach for critical, high-valued assets and has short Potential-Functional (P-F) failure intervals. With none of the features, an organisation will suffer a high capital 8 investment for system acquisition, office arrangement and safety, data management and personnel training. 10

Despite their clear contribution to the track maintenance 11 process, track inspections are fraught with issues, such as 12 causing train delays, the high frequency of line closures, and 13 staff safety. For example, in 2012, the train 2W06 struck 14 the off-track inspector who was standing too close to the 15 inspected track, near to Bulwell station, in Nottingham. 16 In fact, track inspections involve a high volume of short-17 duration tasks (in the range of one to four hour(s))¹⁸, and it 18 is important to perform them systematically and objectively 19 as inspections incur a possession cost. Longer possession 20 interval result in higher possession cost, particularly on 21 heavily loaded sections where the unavailable slots were 22 likely to have been sold to a freight operator^{19;20}. Those 23 issues could, however, be relaxed by incorporating the 24 discipline of scheduling theory when finding the optimized 25 sequence of inspection tasks on a vector of geographically-26 separated tracks. 27

Scheduling theory enables users to gain optimal benefits 28 from predetermined activities or tasks subject to a set of 29 constraints²¹. From a RIM perspective, the main goal of 30 scheduling track inspections is to maximize the probability 31 of recording irregularities in track condition data from 32 inspection activities by optimally ordering the tracks to 33 be inspected²². To date, researchers have formulated track 34 inspection schedules (TIS) for the last decade of conditions 35

involving both single- and multi-objective function(s), and 36 subject to no constraints or a combination of soft and 37 hard constraints. As different requirements exist from one 38 track inspection problem to another-based on inspection 39 order and railway network size, among other factors-more sophisticated and problem-dependent methods have been 41 developed. This situation, which exhibits the limitations of 42 existing optimisation methods and highlights the significance 43 of problem characteristics in scheduling, appears to be a good inspiration to review literature concerning TIS.

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This paper first provides a review of methods, along with algorithms to solve the TIS optimisation problems. Following, this paper discusses opportunities to further study the applicability and suitability of scheduling for on-site track inspections to be equipped with an exit point/policy in the occasions of disruptions. It should be clear that disruption is an event not a process and its presence is unpredictable due to existing of low (poor) probability distribution function. The exit point will allow a planner of TIS to reschedule the remaining prescribed TIS to minimise the impacts of disruptions. One may think stability of the prescribed TIS, adjustments time and costs, and failure risk of rescheduling TIS as some measures to be handled with or without carrying optimisation during an execution of disruption management. Other potential studies to improve effectiveness of an implementation of TIS are part of the discussion session before we make some conclusions about the future of TIS, in particular.

Track inspection schedule problem

Model formulation

A majority of researchers formulate TIS as an optimisation 66 problem. In doing so, the track inspection schedule problem 67 should present at least one objective function to be 68

optimised and a set of constraints, if possible. Although an unconstrained optimisation problem is less complicated to 2 solve, the given solution might become less feasible if some changes occur during execution times. Presenting constraints in the problem formulation restricts the search for solutions 5 only in a feasible region defined by the limitations and challenges that the schedule could face in reality.

The recent studies of a constrained optimisation problem for TIS are presented by^{23;26}. Two objectives are captured 9 in their model where the first one is to minimise total 10 inspection times to complete the predetermined number of 11 inspections in the given inspection period. The total time 12 is a summation of total times to inspect all the tracks and 13 travel times among the inspected tracks. In order to benefit 14 as much as possible from the travelling decisions, a quality 15 measure was introduced. The measure is a degree of safety 16 importance of inspections and the study aims to maximize 17 the safety measurement as well. Both objectives are hardly to 18 solve either separately or simultaneously in the presence of 19 nine technical constraints. Among them, a time gap between 20 two consecutive inspections on a same track is imposed. 21 An introduction of this constraint can be viewed as an 22 achievement of past experiment-based studies on railway 23 asset management. For example, Lam and Banjevic³¹ 24 proposed an intelligent asset health monitoring system. This 25 system alerts an asset manager with an optimal situation to 26 conduct asset inspection before proper maintenance jobs are 27 assigned. A decision is made based on the level of risk to 28 failure which uses information about the hazard of asset as 29 an input for the system. Kim and Frangopol³⁰ conducted 30 research with a similar purpose but they used a probabilistic 31 approach to a fatigue-sensitive structure. The statistical-32 based model generates an inspection schedule that requires a 33 low inspection cost but is able to guarantee inspection quality 34 , at least at an acceptable level. In their proposed model, the 35 cost is calculated based on costs of inspection and expected 36 cost of failure. Benefits of the proposed model are evident 37 not only on the inspection section but they also extend 38 to monitoring scheduling. A similar concept can be found 39 in Kashima²⁹, that is, a condition-based inspection regime 40 was proposed which in turn means an optimal inspection 41 time interval is determined quantitatively using a structural reliability theory. A series of life cost analyses shows the 43 effectiveness of the proposed method. 44

Reliability techniques were also applied in large scale 45 railway network systems, as presented in⁶⁵. Generally, the 46 reliability centered maintenance (RCM) techniques offer 47 ground benefits, such as technical insight into planning 48 of preventive maintenance (PM), which allows various 49 levels of adjustments in selected maintenance processes, 50 and clear decision diagrams. In addition, maintenance staff 51 who are consulted for the first time are expected to gain 52 better personal encouragement from the interdisciplinary 53 approach used to make the analysis. From a railway 54 infrastructure case study, the authors demonstrated a wide 55 range of specific benefits, such as reduction in time taken 56 for information extraction, an increase in equipment life 57 that positively affects corrective maintenance costs, and 58 an overall improvement in company productivity. Due to 59 the limited level of risk and uncertainty assessment,⁶⁶ 60 revised the generic methodology of the traditional RCM 61

methodology. Under dedicated uncertainty assessments, a matrix score is used to evaluate a series of tasks i.e. identification, categorisation and summarisation, with respect to uncertainty factors. The obtained scores are integrated with thetask and interval assessments, both components being common parts of the RCM framework. The embedded assessment part, enriching the risk and uncertainty assessment in which uncovered uncertainties in 69 the assumptions are made in the standard RCM analyses, are well addressed. On another occasion,⁶⁷ proposed a system reliability-based methodology to construct a non-periodic PM schedule for deteriorating complex repairable systems. The methodology makes an estimate of system reliability as the condition variables functions differently depending on the current scenario in the system. In each scenario, an 76 optimal PM schedule is obtained by solving a constrained minimisation problem, which incorporates properties of a specific reliability-based PM model. The proposed methodology offers a basic rule of rescheduling PM, which requires involvement of domain experts experiences. However, no specific guidelines are provided.

Andrade and Teixiera⁶⁸ put forward a Bayesian model to assess the evolution of uncertainty in model parameters over a limited life-cycle in rail track geometry degradation. In doing so systematically, a framework to update the initial uncertainties was developed. The uncertainty at the design stage, quantified by fitting a prior probability distribution to the model parameters, is sequentially updated as more inspection data becomes available after operation starts. Following this, posterior probability distributions are used to assess the reduction in uncertainty in geometry degradation parameters. Negotiation of life-cycle maintenance costs could take place upon completion of posterior probability distribution computation. An extended version of the authors work can be found in⁶⁹.

Inspection costs are found to be a primary objective in most works of optimisation problem for TIS^{26;28}. However, in some cases, an inspection cost is defined as a problem constraint. This occurs in the case of a railway company 100 that has a limited budget for inspections, as presented in 101 Higgins et al.²⁷. This work also put forward job sequence, 102 track authorization and travel time as constraints that need 103 to be satisfied when solving the optimisation problem. 104 Two objectives are involved, which are minimisation of 105 disruptions to train services and completion time. The former 106 objective was introduced due to the fact that trains must 107 follow speed restrictions when approaching the inspected 108 area, and to this extent it might cause delays. Too many 109 delays could create a bad perception from the public which 110 is certainly not welcome in a passenger transportation 111 business²⁴. Budai et al.¹⁹ extended the work by introducing 112 generalised costs of track possession as an objective to 113 be minimised. This study is unique as it generates an 114 optimal schedule which involves both preventive and routine 115 maintenance works. 116

An attempt to move away from a periodical practice in 117 managing railway assets can also be observed from the 118 way an optimisation problem is formulated. Ottomanelli 119 et al.³⁵ developed a fuzzy-logic-based decision making to 120 facilitate rail tracks maintenance which provides a track 121 supervisor more flexibility in terms of deciding which 122

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tracks should be accessed and when. With the proposed model, there are no more crisp and rigid decisions and the 2 system will generate a membership value to six maintenance modules, which includes delay of the maintenance as one of them. The fixed periodic inspection always implies a trade-5 off between inspection cost reduction and timely failure detection. To overcome the above challenges on inflexibility of the fixed periodic inspection, and performance concerns 8 about inspection intervals, non-periodic inspection strategies have been proposed. In⁷⁰, the degradation warning threshold 10 was introduced to divide the whole degradation process 11 into normal and warning areas, where a long interval was 12 applied to the normal area, which was then shortened 13 to a predetermined value for the warning area. Overall, 14 the proposed non-fixed periodic inspection strategy is 15 flexible and applicable to precognitive maintenance for 16 the monitoring of system degradation, which can not 17 only improve the inspection efficiency, but also reduce 18 the overall maintenance cost in practice. Theoretically, 19 a non-periodic inspection policy that incorporates recent 20 inspection results and/or environmental condition in the TIS 21 model shows better performance than a periodic policy. 22 However, an implementation of a non-periodic inspection 23 policy for railway track inspection is very challenging due 24 to periodicity of train timetables, prioritisation on track 25 access given to freight companies, and of course, resource 26 constraints. 27

Konur et al.²³ extended their TIS research by discussing 28 the potential of inspection results as an input to a risk of 29 failure analysis of tracks. Reliability and a crack growth 30 approach have been studied as a case study to effectively 31 export track inspection results to a rail-related failure risk 32 measurement analysis. Their primary concern is to optimally 33 utilize track inspection data in the context of track inspection 34 but is not intended to be a primary source of data. \ln^{11} , 35 the risk of failure is controlled by introducing two penalty 36 cost functions for exceeding maintenance thresholds into the 37 total cost of TIS model. With these functions, a different 38 inspection policy i.e. interval could turn out non-optimal 39 due to the function changes. The findings point out that the 40 effect of changes in model inputs on total cost formulation 41 could generate a different inspection strategy. Meanwhile,⁷² proposes a risk of accident cost function which is derived 43 from the cost of derailment and the probability of safety 44 fault occurrence that can cause derailment in the interval 45 between maintenance execution and the next inspection. However, use of proposed risk function is limited under 47 certain assumptions namely tracks are identical regardless 48 of geometric characteristics, location (curve or tangent), 49 substructure characteristics and construction time and 50 maintenance history. Further sensitivity analysis is strongly 51 suggested to justify the claim that tracks with higher 52 degradation rates requires more frequent inspections and 53 PM. 54

It is not an exaggeration to say that both inspection 55 and measurement vehicles are a great creation for track 56 inspection and maintenance. A train-borne with plain line 57 pattern recognition technology, for example, not only 58 increase inspection integrity but also reduces inspection 59 times as compared to a foot patrol³⁴. However, it is crucial 60 to assign those vehicles on tracks at low expenditures 61

without comprising the high quality of safety standards. To 62 achieve both objectives, Podofillini et al.²² developed a risk-63 informed methodology to determine optimal strategies for 64 how to assign the ultrasonic inspection vehicles. Realising 65 the restrictions that underlie the inspection and maintenance 66 procedure in the real world, the study developed a model to 67 verify the workability of the proposed solutions. In addition, 68 no technical constraints have been presented in the problem 69 formulation, unlikely in Peng et al.³⁶. Periodicity constraints, 70 penalty costs imposed due unfinished inspections within the 71 allocated time windows and avoiding task completion by 72 an unauthorized inspection team were taken into account 73 with regards to an optimisation problem for an inspection 74 vehicle. By taking into account the complexity of the 75 abovementioned realistic issues, the single objective problem 76 was formulated as a vehicle routing problem (VRP). VRP 77 is a popular methodology to serve a known number of 78 orders/clients on the given network with a fleet of vehicles 79 of minimum cost while satisfying side constraints such as 80 time windows^{25;33;37}. A solution of the proposed model was 81 found to be superior than one produced through a manual 82 procedure when it was tested for a short-term schedule i.e. 83 a partial complete schedule. Meanwhile, Lannez et al.³² 84 also proposed a single objective VRP but a solution of 85 the problem has a minimum total deadhead distance while 86 satisfying six constraints, where two of them are the vehicles 87 limitations. 88

Solution method selection

A schedule may be described as a sequence of tasks or activities that will be sequentially performed for a given time period. The feature gives track supervisor two options; to either prepare a prescribed (master) inspection schedule, or do it partially as an interval-based routine. The former scheduling mode is the practice of producing a complete schedule before the beginning of a business operation period. Under the time-rigid option, tracks under IM supervision will know in advance about time and inspection tasks that will be performed on them. Besides that, a prescribed schedule offers other benefits, such as the schedules objectives being 100 known prior, in real-time status of company resources e.g. 101 man power and equipment is always available and the 102 planning team have to experience the exhaustive schedule 103 design process only once. To attain those benefits, an 104 associated optimisation problem requires approximation 105 methods to search an optimal schedule(s) as the search space 106 size grows exponentially to a number of problem instances⁴⁴. 107 Should be noted that, there is no global panacea in solving 108 optimisation problem and the solution method selection is 109 generally driven by problem characteristics. Complexity of 110 the problem would increase with participation of constraints 111 and objective functions evaluation. To cope with a rough 112 problem environment, a metaheuristic method is applied to 113 track inspection schedule problems. 114

A metaheuristic method produces a solution(s) close to an 115 optimum condition but is not an exact solution. The method 116 is initiated with a single or a set of candidate solution(s) and 117 improves them iteratively with regard to identified criterion. 118 To utilize the method, no assumption about the problem is 119 required; however, in some situations, algorithm parameters 120 need users inputs. One of the metaheuristic methods that 121

is popularly and widely used to schedule problems in a class of NP-hard is genetic algorithm (GA)^{24;41}. Readers 2 are referred to Mitchell⁴² and Dorit and Hochba⁴⁰ for fundamental readings about GA and NP-hard problem, respectively. Podofillini et al.²² applied GA to search 5 Pareto efficient inspection/maintenance strategy in their biobjective optimisation problem. Their strategy to not apply decision makers preferences in prior of GA caused too 8 many solutions that were presented for trade-off analysis. At this stage, decision makers can get a preview of any 10 schedule from the solution lists and also understand a 11 relationship between schedules objectives in the decision 12 making process³⁹. A min-max method was introduced 13 upon completion of the search process to downsize the 14 solutions set, where a clear separation could be observed 15 between solutions. An application of GA could also be 16 found in the technical report²³ where the algorithm was 17 used to determine optimal schedules for an ultrasonic 18 inspection vehicle. With application of GA, two objectives 19 of the problem (minimisation of total inspection times and 20 maximisation of inspection quality) were satisfied in the 21 search simultaneously, and the overall results outperformed 22 what they received from greedy heuristic algorithms²⁶. The 23 finding indicates that without considering full specificity of 24 the problem a global optimum schedule can be found for 25 the inspection vehicle. However, it had not always occurred 26 where in most situations, especially involving large-scale 27 problems and/or short scheduling horizon, a heuristic method 28 is sufficient to determine an optimal solution for the NP-hard 29 problem⁴⁵. 30

Scheduling of track inspection can be viewed as a 31 combinatorial problem that easily becomes an NP-hard 32 problem when a large number of tracks are involved. 33 Peng et al.³⁶ customised a traditional heuristic algorithm 34 to handle the complex single-objective routing inspection 35 schedule problem. Algorithm customization was made by 36 incorporating an incremental horizon approach which was 37 able to control the growth of an initial schedule, i.e. short-38 term or long-term horizon. In particular, two subroutines; 39 task-assignment and task-interchange, were embedded in 40 the approach. The former subroutine is a 7-step algorithm 41 that locally improves a solution obtained from the latter 42 subroutine. The proposed heuristic algorithm over-performs 43 a manual scheduling procedure in short-term horizon but an 44 improvement is expected in future for a long-term horizon 45 schedule. 46

In a different project by Peng et al.⁴³, the first author of the work³⁶ and her different research team 48 proposed an integrated framework of clustering algorithm 49 and iterative heuristic algorithm for solving a large-scale 50 track maintenance schedule problem. Under the solution 51 framework, maintenance activities are initially separated 52 based on the probability level of constraints violation 53 before tentatively being assigned to a number of teams by 54 a clustering algorithm. The similar concept of clustering 55 maintenance tasks in prior also can be found in ¹⁹. Contrarily, 56 the latter article aims to group non-cyclic and cyclic 57 maintenance activities and perform them within one track 58 possession. Four heuristic algorithms were applied to the 59 problem which aimed to determine an optimal schedule of 60 railway preventive maintenance. Mixed results from a series 61

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of testing suggest that the selection of algorithm to the problem is very user-dependent.

Meanwhile, a dendrogram (a hierarchical clustering technique) was used to determine groups of descriptive variables related to rail preventive and corrective maintenance⁷⁴. Interestingly, the analysis discovered that greater track length leads to a higher probability of a rail break in track section level. Unlike track, which is a linear asset, estimation of the probability of rail breaks in switch and crossing (S&C) is given by a combination of tonnage and the number of S&C points. In⁷⁵, an assessment of the risk of hazardous material transportation by rail is performed in a segment-specific manner. The research empirically shows that an overall route risk can be reduced through delivering frequent inspections on small numbers of high-risk track segments.

With a specific decomposition technique, as presented in³², an exact optimal schedule can be retrieved from a heuristic method. However, the proposed method was successfully applied to an arc routing-type problem and it is highly probable that it does not directly work in other cases as it is the nature of the heuristic method. Higgins et al.²⁷ also succeeded in obtaining an exact schedule but their heuristic algorithm is based on Tabu search. Despite the method is simple and powerful to solve combinatorial optimisation problem its execution time and overall quality could be affected by neighborhood evaluation scheme and size of search list, respectively³⁸.

Potential research

Depending on the type and size of the railway network, track inspection costs would reach millions of dollars and become a time-consuming technical task ^{18;48}. To perform inspections effectively, scheduling has previously been incorporated where a track supervisor searches for a schedule which optimally achieves several recognized objectives. Past study has shown how conveniently the TIS problem can be solved by modelling it as an optimisation problem. Table 1 summarizes how the selected study dealing with TISs. The number of articles this paper has reviewed actually more than what Table 1 includes but we tabulated pertinent cases that either have unique modelling approach, optimisation criteria, problem constraints or a suggested solution.

Table 1 also shows that most of the studies focused on cost minimisation where a direct (principal) inspection cost was not one of the cost components except in Kim and Frangopol³⁰. This situation appears realistic due to the fact there is very little rail companies can do to reduce their direct costs, which is a function of track length and category^{54;62}. Each category associates with a specific inspection requirement such as minimum number of inspections per year⁵⁵. Any attempt to reduce costs by decreasing inspection frequency must able to present the same range of checks, of at least the same level of accuracy currently achieved by manual methods¹⁷.

On the other side, minimisation of indirect costs associated with track inspection or maintenance were extensively studied. At present, the cost was defined by the total travel times and maybe in the future, it could include other factors such as the carbon footprint ⁵⁰ due to the fact that inspection vehicles are fuel-powered machines and make thousands of miles of journeys in a single year

Reference	e Model formulation	Components of cost function	Other optimisation criteria	Constraints	Solution method
36;43	Integration of arc routing problem and time-space network model	Travel costs, side constraints penalty costs	na*	Three categories of side constraints: time windows, mutually exclusive precedence	Modified iterative heuristic with a splitting mechanism
19	Binary programming	Possession costs	na	Time and maintenance work order restrictions and all work must appear at once	Modified greedy heuristics
30	Mixed-integer pro- gramming	Initial cost, inspection cost, expected maintenance and failure cost	na	Single constraint only, which is an optimal inspection interval that should be at least one year	Non-dominated sorting in genetic algorithm
27	Integer programming	na	Minimise a weighted delay function	Time and inspection work order restrictions, crew assignment and cost budget	Tabu search heuris tic
32	Arc routing problem with 0-1 formulation	na	Minimise total dead- head distance	Inspection frequencies and complex operational constraints such as working shift duration, restrictions, vehicle flow, water supply, track outages and a heterogeneous fleet	A cut and column metaheuristic method based on Benders and Dantzig-Wolfe decompositions
23;26	Combinatorial opti- misation problem	Inspection time and travel time	Maximise the impor- tance of inspections	Technical constraints, including a minimum inspection frequency and time gap between two consecutive inspections on the same track	Greedy heuristic algorithm, genetic algorithm
22	Risk/cost model	Operation and maintenance expenditures	Maximise safety information	No constraints in model formulation but they were discussed during trade-off analysis	Multi objective genetic algorithm

Table 1. Summary of selected track inspection schedule problems

of inspection⁶¹. This factor also has an impact on the
 environment which will impact the indirect cost, since rail
 transportation is shifting to be a greener transportation
 mode^{51;52;64}. To quantify both factors in the same units, i.e., a
 generalised cost, one that monetizes time, environmental and
 societal impacts could be applied to the cost calculation⁵³.

Track inspection schedules are heavily dependent on the 7 availability of resources such as staff, machines equipment, 8 budget and the track itself. Running schedules in real time exposes them to disrupted situations. To visualise hazards 10 in a TIS let consider a scheduling problem formulation 11 in Konur et al.²³. The problem was solved under a 12 batch environment in which modelling complexity issue 13 was managed before the search begins. A straightforward 14 approach to reduce model complexity (i.e. decreasing the 15 computational burden) is to avoid elements that are less 16 likely to occur in reality when formulating a problem^{46;59}. 17 Those elements could be identified and studied from an 18 influence diagram⁵⁸. 19

An influence diagram is not a flow chart but it is a 20 simple way to understand the relationship among input 21 uncertainties, structure and decision values. Figure 2 shows 22 an influence diagram associated with the given problem 23 where the oval-shaped block represents uncertainties in the 24 model. Crew strikes, extreme weather, machine breakdowns, 25 authorisations to work, track unavailability, etc., may occur 26 during schedule execution. These might have a negative 27 impact on deteriorating schedule objectives. Anticipating 28 disruptions during schedule execution is problematic, but can 29 at least be reduced by incorporating an incremental approach 30 when designing schedules³⁶. Realizing that most disruptions 31 are unforeseeable, many studies through rescheduling; a 32 recovery action that takes place at the time the disruption 33 arises during the schedule execution. A good review of 34 rescheduling in railway operative management can be found 35 in Cacchiani et al.⁴⁷ and Fang et al.⁴⁹. 36

As presented in the railway asset management financial ³⁷ report of the Network Rail⁶³ as well as inspection ³⁸ manuals¹⁸, foot inspections are still significant in track ³⁹

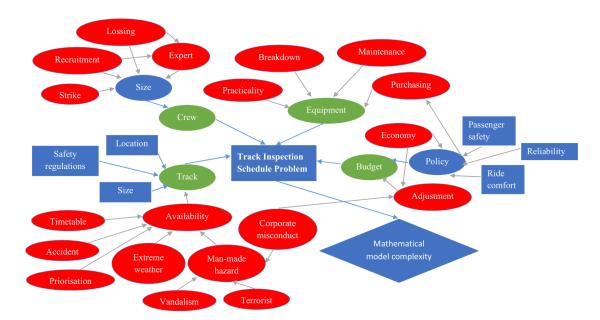


Figure 2. An influence diagram of track inspection schedule problem

inspection programs despite presenting several limitations. However, discussion about integration scheduling of foot 2 and mechanised inspections is rare, as compared to 3 individual type of inspections. Therefore, it is suggested to transfer the current technology of scheduling to mixedstyle of inspections. In terms of problem formulation, 6 most aspects can be studied from previous optimisation 7 problems involving inspection vehicles but certainly with 8 some adjustments, especially regarding constraints. For example, the requirement of being physically present on 10 the inspected tracks could be constrained by several factors, 11 such as: working time, weather, track possession, safety 12 regulations, list of tasks, etc. Mixed scheduling of foot 13 and mechanised inspections has potential to be a new 14 research direction. Apart from that, an introduction of on-15 train measuring systems in railway vehicles⁷³ offers a 16 wide opportunity for multi-modal track geometry inspection. 17 Nevertheless, the traditional dedicated inspection vehicle 18 is still dominant when it comes to track inspection and 19 maintenance, despite an increasing popularity of on-train 20 technologies. Note that on-board inspection technology is 21 still not mature and comes with engineering faults i.e. the 22 technology is still in the growth phase of the product life 23 cycle. Current safety regulations, track accessibility issues 24 and the large volume of old-fashioned track components 25 restrict this technology from full-scale implementation. 26

Previous researchers^{30;31} worked on finding an optimal 27 track inspection interval which resulted in a publication of 28 inspection policy. The policy proposes an expected number 29 of inspections per year for every track category. For example, 30 26 inspections per year are recommended for a switch and 31 crossings type B.7 Logically thinking, there will be another 32 26 inspections the following year, where we think it would be 33 an opportunity to reduce the number. A significant reduction 34 in the direct inspection cost can be unlocked from a small 35 percentage of reductions, particularly when it involves a 36 track category that has a high number of memberships 37 and also requires high inspection frequencies, for instance, 38 switch and crossings. Those savings could be transferred 39

as an initiative to an inspection team to improve their commitment every time they perform an inspection. The concept of Non-Claim Discount, found in vehicle insurance policies, could be a good example and it is worthwhile to study its suitability in track inspections.

In the same vein, an application of Big Data could be incorporated in the post-inspection process that aims to analyse the risk of switching an inspection regime from periodic to non-periodic mode during an execution period. Large volumes of condition data and geometric measurement can become an asset after successfully turning it into available information. As measurement and monitoring technologies have advanced, and become cheaper and more ubiquitous, data-to-information has morphed into a broader discussion about how to manage Big Data^{57;60}. However, like many developing opportunities, Big Data also presents a number of challenges. Heterogeneity, inconsistencies and incompleteness, merging data, timelines and privacy of data are the main challenges encountered for performing Big Data analysis⁵⁶.

Conclusion

This paper reviews almost all publicly accessed articles about 61 railway track inspection schedules from an optimisation 62 point of view. Due to the limited number of publications 63 available on the selected topic, track maintenance scheduling 64 studies are incorporated together with reviews involving 65 solution methods. We first delivered a background of 66 the scheduling of railway track inspection, focusing on 67 advantages of approaching TIS problems in a structured 68 optimisation framework. This was followed by an in-depth 69 discussion of diversity among TIS problems, particularly in 70 the consideration of objective functions and constraints, that 71 had led to the existence of a heterogeneous collection of 72 optimisation-based schedule models. As a result, we were 73 able to determine the main characteristics of both heuristic 74 and metaheuristic solution methods currently applied in TIS 75 optimisation. In terms of future research in TIS from an 76

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optimisation viewpoint, a wide range of opportunities has been discussed according to the knowledge gained from the 2 compiling of results.

The TIS problem has attracted the development of a new heuristic method to solve a single objective 5 optimisation problem. In case of solving multiple objectives simultaneously, the use of a problem-independent algorithm is sufficient. Slow but steady progress was observed in 8 the research topic that urges much more research to be 9 done. This paper suggests that further research could start 10 from studying a new type of track inspection schedule; 11 for example, or explore the possibility of having an 12 integrated foot and mechanised visual inspection schedule. 13 Other than that, an expansion of the current problem 14 formulation, by considering quality measures for schedules, 15 redefining the problem constraints, or introducing a mixed 16 scheduling approach is recommended. Further research 17 also can be initiated in developing a benchmark database 18 about performance of optimisation methods/algorithms in 19 solving track inspection schedules. To date, sophisticated 20 heuristic algorithms are required to generate a near-to-21 optimal schedule where the use of metaheuristic method 22 actually is sufficient but the given problem has to be 23 approached differently. Apart from that, a potential of 24 multi-objective optimisation in solving the track inspection 25 schedule problem still needs to be identified. 26

Finally, the track inspection schedule problem can be 27 defined as a function of track, equipment, manpower and 28 time. The complexity of solving constrained optimisation 29 problems can be reduced if interdependent issues among 30 the components can be managed separately without causing 31 a serious degradation in their functionality; either as an 32 individual or a whole schedule. Furthermore, recovery 33 actions such as rescheduling, in the event of a disruption can 34 be implemented directly with the affected components. 35

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References 45

- 1. Rail Safety and Standards Board. Taking safe decisions-how 46 Britain's railways take decisions that affect safety. RSSB, 2014. 47
- 2. Network Rail. Asset management strategy. Network Rail 48 Technical Report, 2014. 49
- 3. Safe Work Australia. How to determine what is reasonably 50 practicable to meet a health and safety duty. Safe Work 51 Australia, 2013. 52
- 4. Office of the National Rail Safety Regulator. Meaning of 53 duty to ensure Safety So Far As Is Reasonably Practicable -54 SFAIRP. Australia ONRSR, 2016. 55
- 5. Remennikov AM and Kaewunruen S. A review of loading 56 conditions for railway track structures due to train and track 57
- vertical interaction. Struct Control Hlth 2008; 15(2): 207-234. 58

- 6. Zoeteman A. Life cycle cost analysis for managing rail infrastructure: Concept of a decision support system for railway design and maintenance. Eur J Transport and Infrastr Res 2001; 1(4): 391-413.
- 7. Guler H. A decision support system for railway track maintenance and renewal management. J Comput Civil Eng 2012; 27(June): 292-306.
- 8. Jimenez N, Barragan A, Cembrero P et al. Automated and Cost Effective Maintenance for Railway - (ACEM-Rail). Procedia Soc Behav Sci 2012; 48: 1058-1067.
- 9. Liu X, Saat MR and Barkan CPL. Benefit-cost analysis of heavy haul railway track upgrade for safety and efficiency. Proc Int Heavy Haul Assoc Conf 2011; 1-8.
- 10. Cherkashin UM, Zakharov SM and Semechkin AE. An overview of rolling stock and track monitoring systems and guidelines to provide safety of heavy and long train operation in the Russian Railways. Proc Inst Mech Eng F J Rail Rapid Transit 2009; 223(2): 199-208.
- 11. Berggren EG. Efficient track maintenance: methodology for combined analysis of condition data. Proc Inst Mech Eng F J Rail Rapid Transit 2010; 224(5): 353-360.
- 12. Li H, Parikh D, He Q et al. Improving rail network velocity: A machine learning approach to predictive maintenance. Transport Res C-Emer 2014; 45: 17-26.
- 13. Vale C, Ribeiro IM and Calada R. Integer programming to optimize tamping in railway tracks as preventive maintenance. J Transp Eng 2012; 138(January): 123-132.
- 14. Yokoyama A and Takikawa M. JR East aims at condition-based maintenance. Railway Gazette International 2014; 170(1): 37-39.
- 15. Kaewunruen S, Sussman JM and Matsumoto A. Grand challenges in transportation and transit systems. Frontiers Built Enviro 2016; 2(4): 1-5.
- 16. Kaewunruen S and Remennikov AM. Integrated field measurements and track simulations for condition assessment of railway tracks. In 1st International conference on structural condition assessment, monitoring, and improvement. Perth, Australia, pp. 391–398.
- 17. Roberts C, Kent S, Rusu M et al. Modular, self-inspecting infrastructure. Technical Report 265722, 2014.
- 18. Al-Nazer L, Raslear T, Patrick C et al. Track inspection time study. FRA, U.S. Department of Transportation, 2011.
- 19. Budai G, Huisman D and Dekker R. Scheduling preventive 2004 IEEE International railway maintenance activities. conference on systems, man and cybernetics 2004; 5: 4171-4176.
- 20. Putallaz Y and Rivier R. Strategic maintenance and renewal policy of a railway corridor, taking into account the value of capacity. In World conference on rail research. pp. 1-18.
- 21. Tanaev V, Gordon W and Shafransky YM. Scheduling theory. single-stage systems. Netherlands: Springer, 2012.
- 22. Podofillini L, Zio E and Vatn J. Risk-informed optimisation of railway tracks inspection and maintenance procedures. Reliab Eng Syst Safe 2006; 91(1): 20-35.
- 23. Konur D, Farhangi H, Long S et al. Track inspection planning and risk measurement analysis. Missouri University of Science and Technology, 2014.
- 24. Balcombe R, Mackett R, Paulley N et al. The demand for 116 public transport: A practical guide. Transport Policy 2004; 13: 117 295-306. 118

- 25. Eksioglu B, Vural AV and Reisman A. The vehicle routing problem: A taxonomic review. <u>Comp Ind Eng</u> 2009; 57(4): 1472–1483.
- 4 26. Farhangi H, Konur D, Long S et al. Bi-objective Track
 5 inspection scheduling: Formulation and solution analysis. J
 6 Transp Res Board 2015; 1–18.
- 7 27. Higgins A, Ferreira L and Lake M. Scheduling rail track
 8 maintenance to minimise overall delays. In Ceder A (ed.)
 9 Transportation and Traffic Theory. Amsterdam: Elsevier, 1999.
 10 pp. 779–796.
- Holland F, Caines M and Kerr M. Mechanised track patrol.
 In <u>Conference on railway engineering</u>. Melbourne, Australia:
 ARRB Group Limited, pp. 87–93.
- 14 29. Kashima T. Reliability-based optimization of rail inspection.
- PhD Thesis, Massachusetts Institute of Technology, Cam-bridge, MA, 2004.
- 30. Kim S and Frangopol DM. Cost-based optimum scheduling of
 inspection and monitoring for fatigue-sensitive structures under
 uncertainty. J Struct Eng 2011; 137(11): 1319–1331.
- 20 31. Lam JYJ and Banjevic D. A myopic policy for optimal
 21 inspection scheduling for condition based maintenance. <u>Relia</u>
 22 Eng Syst Safe 2015; 144: 1–11.
- 32. Lannez S, Artigues C, Damay J et al. A railroad maintenance
 problem solved with a cut and column generation matheuristic.
 J Netw 2015; 66(1): 40–56.
- 33. Montoya-Torres JR, López Franco J, Nieto Isaza S et al. A
 literature review on the vehicle routing problem with multiple
 depots. Comput Ind Eng 2015; 79: 115–129.
- 29 34. Network Rail. How we will get there: our operating
 a0 environment. NR Technical report, 2014.
- 35. Ottomanelli M, Pace P and Pascoschi G. Intelligent decision
 support tools for optimal planning of rail track maintenance,
 2002.
- 36. Peng F, Ouyang Y and Somani K. Optimal routing and
 scheduling of periodic inspections in large-scale railroad
 networks. J Rail Transp Plann Manag 2013; 3(4): 163–171.
- 37. Zachariadis EE, Tarantilis CD and Kiranoudis CT. Designing
 vehicle routes for a mix of different request types, under time
 windows and loading constraints. <u>Eur J Oper Res</u> 2013; 229(2):
 303–317.
- 38. Bland JA and Dawson GP. Tabu search and design
 optimization. <u>Comput Aided Des</u> 1991; 23(3): 195–201.
- 39. Deb K, Rao NUB and Karthik S. Dynamic multi-objective
 optimization and decision-making using modified NSGA-II: A
 case study on hydro-thermal power scheduling. In: Obayashi S,
- ⁴⁶ Deb K, Poloni C, Hiroyasu T and Murata T (eds.) Proceedings
- 47 of 4th international conference of evolutionary multi-criterion
 48 optimization. Matsushima, Japan: Springer Berlin Heidelberg,
 49 2007, pp. 803-17
- 40. Dorit E and Hochba S. Approximation algorithms for NP-hard
 problems. SIGACT News 1997; 28(2): 40–52.
- 41. Gogna A and Tayal A. Metaheuristics: Review and application.
 J Exp Theo Artif Intell 2013; 25(4): 503–526.
- 42. Mitchell M. <u>An introduction to genetic algorithms</u>. Cambridge, MA: MIT Press, 1998.
- ⁵⁶ 43. Peng F, Kang S, Li X et al. A heuristic approach to the railroad
 ⁵⁷ track maintenance scheduling problem. <u>Comput Aided Civil</u>
 ⁵⁸ Infrastr Eng 2011; 26(2): 129–145.
- 44. Sun Y, Zhang C, Gao L et al. Multi-objective optimization
 algorithms for flow shop scheduling problem: a review and
- 61 prospects. Int J Adv Manuf Tech 2011; 55(5): 723–739.

- 45. Zhao W and Ramamritham K. Simple and integrated heuristic algorithms for scheduling tasks with time and resource constraints. J Syst Softw 1987; 7(3): 195–205.
- 46. Brugnach M, Pahl-Wostl C, Lindenschmidt KE et al. Complexity and uncertainty: rethinking the modelling activity. In Jakeman AJ, Voinov AA, Rizzoli AE et al. (eds.) <u>Environmental modelling, software and decision support: state</u> of the art and new perspectives. Amsterdam: Elsevier, 2008.
- 47. Cacchiani V, Huisman D, Kidd M et al. An overview of recovery models and algorithms for real-time railway rescheduling. Transport Res B-Meth 2014; 63: 15–37.
- Daniels LE and The National Academis. Track maintenance costs on rail transit properties. Technical Report TCRP Project J-7, Fair Oaks, California, 2008.
- Fang W, Yang S and Yao X. A survey on problem models and solution approaches to rescheduling in railway networks. <u>IEEE</u> <u>Trans Intell Transport Syst</u> 2015; 16(6): 2997–3016.
- 50. Krezo S, O Mirza, He Y et al. Carbon emissions analysis of rail resurfacing work: a case study, practical guideline and systems thinking approach. In <u>Proceedings of the second international</u> <u>conference on railway technology: research, development and</u> <u>maintenance</u>. Ajaccio, Corsica, France: Civil-Comp Press, 2014.
- Lin C, Choy KL, Ho GTS et al. Survey of green vehicle routing problem: Past and future trends. <u>Expert Syst Appl</u> 2014; 41(4, Part 1): 1118–1138.
- 52. Krezo S, Mirza O, He Y et al. Field investigation and parametric study of greenhouse gas emissions from railway plain-line renewals. Transport Res D-TR E 2016; 42: 77–90.
- 53. Litman T. Transportation cost and benefit analysis: Techniques, estimates and implications. Technical report, Victoria, 2009.
- Liu X, Lovett A, Dick T et al. Optimization of ultrasonic raildefect inspection for improving railway transportation safety and efficiency. <u>J Transp Eng</u> 2014; 61801: 1-10.
- 55. Office of Rail Regulation and RailKonsult Balfour Beatty Rail Technologies. Asset inspection, condition assessment and decision making. Technical Report BBRT-2012-RP-0001, United Kingdom, 2012.
- Otero C and Peter A. Research directions for engineering big data analytics software. <u>IEEE Intelligent Systems</u> 2014: 1–7.
- Kaewunruen SI. Monitoring structural deterioration of railway turnout systems via dynamic wheel/rail interaction. <u>Case Stud</u> <u>NDT Eval</u> 2014; 1: 19–24.
- 58. Renooij S and Van der Gaag LC. Decision making in qualitative influence diagrams. In Diane J (ed.) <u>Eleventh</u>
 <u>International Florida Artificial Intelligence Research Society</u>
 <u>Conference</u>. Snibel Island, Florida: AAAI Press, pp. 410–414.
- Snowling S. <u>Evaluation of modelling uncertainty and the role</u> of model complexity in risk assessment. PhD Thesis, Hamilton, Ontario, 2000.
- Thaduri A, Galar D and Kumar U. Railway assets: A potential domain for big data analytics. <u>Procedia Comput Sci</u> 2015; 53: 457–467.
- 61. Vatn J and Svee H. A risk based approach to determine
 115

 ultrasonic inspection frequencies in railway applications. In 6th
 116

 Proceedings of the 22nd ESReDA seminar, volume 9. Madrid,
 117

 Spain: NDT.net.
 118
- 62. Zhang T, Andrews J and Wang R. Optimal scheduling of track maintenance on a railway network. <u>Qual Reliab Eng Int</u> 2013; 120
 29: 285-97. 121

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110

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112

113

- NetworkRail. Network Rails activity and expenditure plans. Network Rails strategic business plan - Maintenance activity and expenditure, 2015.
- 4 64. Low carbon transport: A greener future. In <u>Technical report:</u>
 5 <u>A carbon reduction strategy for transport</u>. United Kingdom:
 6 Department for Transport, 2009.
- ⁷ 65. Carretero J, Prez JM, Garca-Carballeira F et al. Applying RCM
 ⁸ in large scale systems: a case study with railway networks.
 ⁹ Reliab Eng Syst Safe 2003; 82(3): 257-73.
- 66. Selvik JT and Aven T. A framework for reliability and risk
 centered maintenance. <u>Reliab Eng Syst Safe</u> 2003; 96(2): 324 31.
- 67. Lin Z-L, Huang Y-S. and Fang C-C. Non-periodic preventive
 maintenance with reliability thresholds for complex repairable
 systems. Reliab Eng Syst Safe 2015; 142: 145-56.
- 68. Andrade AR and Teixeira PF. A Bayesian model to assess rail
 track geometry degradation through its life-cycle. <u>Res Transp</u>
 Econ 2012; 36(1): 1-8.
- 69. Andrade AR and Teixeira PF. Statistical modelling of railway
 track geometry degradation using Hierarchical Bayesian
 models. Reliab Eng Syst Safe 2015; 142: 169-83.
- 70. Yan HC, Zhou JH and Pang CK. Cost optimisation on
 warning threshold and non-fixed periodic inspection intervals
- for machine degradation monitoring. In <u>IECON 2015 41st</u>
 <u>Annual Conference of the IEEE Industrial Electronics Society</u>,
 Yokohama, Japan: IEEE.
- 71. Soleimanmeigouni I, Ahmadi A, Letot C et al. Cost-based
 optimization of track geometry inspection. In <u>11th World</u>
 Conference on Transport Research, 2016, Milan, Italy: TRID.
- 72. Khouy IA, Larsson-Krik, P-O, Nissen A et al. Cost-effective
 track geometry maintenance limits. <u>Proc. Inst. Mech. Eng. Part</u>
 F J. Rail Rapid Transit 2016; 230(2): 611-22.
- 73. Weston P, Roberts C, Yeo G et al. Perspectives on railway
 track geometry condition monitoring from in-service railway
 vehicles. Vehicle System Dynamics 2015; 53(7):1063-1091.
- 3674. Sderholm P and Bergquist B.Rail breaks: An exploratory37case study.In Current Trends in Reliability, Availability,
- Maintainability and Safety: An Industry Perspective, Encyclo pedia of Global Archaeology/Springer Verlag, 2016, pp. 519 541.
- 40 541.
 41 75. Liu X. Optimizing rail defect inspection frequency to reduce
- the risk of hazardous materials transportation by rail. J Loss
 Prevent Proc 2017; 48:151-61.