



POLITECNICO DI TORINO
Repository ISTITUZIONALE

Hidden magnetism in periodically modulated one dimensional dipolar fermions

Original

Hidden magnetism in periodically modulated one dimensional dipolar fermions / Fazzini, Serena; Montorsi, Arianna; Roncaglia, Marco; Barbiero, Luca. - In: NEW JOURNAL OF PHYSICS. - ISSN 1367-2630. - ELETTRONICO. - 19(2017), pp. 123008-1-123008-8.

Availability:

This version is available at: 11583/2687266 since: 2018-03-26T16:46:08Z

Publisher:

IOP Publishing

Published

DOI:10.1088/1367-2630/aa9037

Terms of use:

openAccess

This article is made available under terms and conditions as specified in the corresponding bibliographic description in the repository

Publisher copyright

iop

-

(Article begins on next page)



PAPER • OPEN ACCESS

Hidden magnetism in periodically modulated one dimensional dipolar fermions

To cite this article: S Fazzini *et al* 2017 *New J. Phys.* **19** 123008

View the [article online](#) for updates and enhancements.

Related content

- [Interaction-dependent photon-assisted tunneling in optical lattices: a quantum simulator of strongly-correlated electrons and dynamical Gauge fields](#)
Alejandro Bermudez and Diego Porras
- [Density-induced geometric frustration of ultra-cold bosons in optical lattices](#)
T Mishra, S Greschner and L Santos
- [Incommensurate phases of a bosonic two-leg ladder under a flux](#)
E Orignac, R Citro, M Di Dio et al.



PAPER

Hidden magnetism in periodically modulated one dimensional dipolar fermions

OPEN ACCESS

RECEIVED

27 May 2017

REVISED

7 September 2017

ACCEPTED FOR PUBLICATION

2 October 2017

PUBLISHED

6 December 2017

Original content from this work may be used under the terms of the [Creative Commons Attribution 3.0 licence](#).

Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

S Fazzini¹, A Montorsi¹, M Roncaglia¹ and L Barbiero^{2,3}¹ Institute for condensed matter physics and complex systems, DISAT, Politecnico di Torino, I-10129, Italy² CNR-IOM DEMOCRITOS Simulation Center and SISSA, Via Bonomea 265, I-34136 Trieste, Italy³ Dipartimento di Fisica e Astronomia 'Galileo Galilei', Università di Padova, I-35131 Padova, ItalyE-mail: Luca.Barbiero@ulb.ac.be**Keywords:** string order, Hubbard model, density matrix renormalization group calculations, phase diagram, dipolar fermions, correlated hopping

Abstract

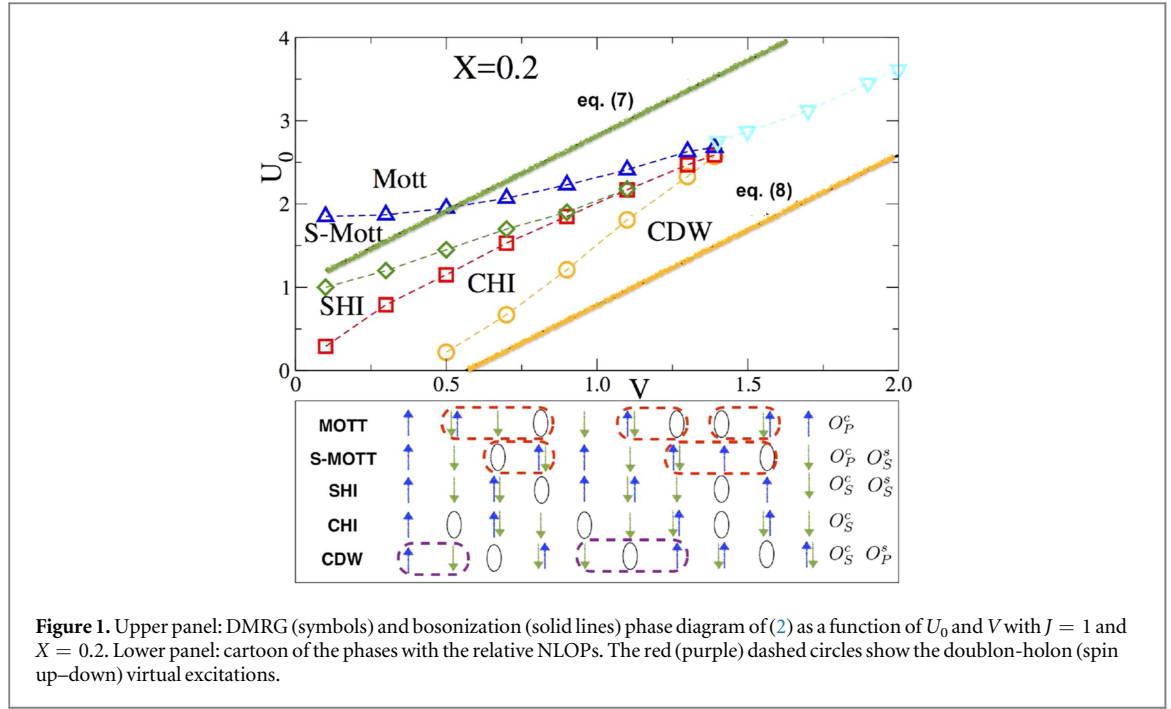
The experimental realization of time-dependent ultracold lattice systems has paved the way towards the implementation of new Hubbard-like Hamiltonians. We show that in a one-dimensional two-components lattice dipolar Fermi gas the competition between long range repulsion and correlated hopping induced by periodically modulated on-site interaction allows for the formation of hidden magnetic phases, with degenerate protected edge modes. The magnetism, characterized solely by string-like nonlocal order parameters, manifests in the charge and/or in the spin degrees of freedom. Such behavior is enlightened by employing Luttinger liquid theory and numerical methods. The range of parameters for which hidden magnetism is present can be reached by means of the currently available experimental setups and probes.

Since the Haldane's discovery of a gapped phase with no local order in 1983 [1], hidden magnetic orders [2] have attracted huge interest. In this context two very recent experiments involving organic molecular compounds [3] and an oxide of nickel spin chain [4] have obtained relevant results. Nowadays cold atomic systems offer an ideal platform to simulate fundamental quantum physics [5]. Indeed proposals for the realization of hidden charge magnetism [6–10] have been carried out. Meanwhile the possible realization of interaction induced hidden spin orders in fermionic systems is still an unexplored scenario.

At the same time, investigations of periodically modulated quantum systems [11] have predicted very interesting effects [12–14]. They have stimulated impressive experimental achievements like frustrated classical magnetism [15], gauge potentials [16], ferromagnetic domains [17] and the realization of new particle-hole symmetric Hubbard-like Hamiltonians with correlated hopping processes (CHPs) [18]. The latter are believed to be responsible for fundamental still open questions [19], one of these being the celebrated η -superconductivity [20].

A configuration closer to real materials [21] can be realized in trapped ultracold atomic systems with strong long-range dipolar interaction, like magnetic atoms [22–24] and polar molecules [25–27]. In case of Er magnetic atoms, this research line has produced the recent experimental realization [28] of a paradigmatic model in condensed matter, the extended Bose–Hubbard model. Furthermore out-of-equilibrium dipolar systems have been both used to generate quantum magnetic Hamiltonians [29, 30] and proposed to study disorderless many-body localized regimes [31].

Motivated by the aforementioned reasons, in this paper we investigate the properties of a dipolar fermionic mixture subject to a rapid time periodic modulation of the on-site interaction and trapped in a one-dimensional (1D) optical lattice. In this regime Floquet theory can be applied. It allows to derive an effective time independent model where an additional term of CHPs appears. When we treat the effective model within bosonization approach [32], its behavior is reduced to that of two spin-charge separated sine-Gordon models. The latter turns out to capture well the charge sector, predicting in particular the presence of hidden charge order; and to only partly describe the behavior in the spin sector, since Haldane spin order appears to be ruled out. In fact, once



quasi-exact density matrix renormalization group (DMRG) [33] calculations are performed, a further spin gapped region is found with respect to bosonization predictions. Noticeably, this is characterized by the presence of hidden magnetic order in the spins. This magnetism can be solely detected by the non-vanishing of string-like nonlocal order parameters (NLOPs). Finally we discuss how all our achievements can be experimentally reproduced with the ongoing experimental setups involving magnetic atoms.

Model

We consider a balanced unit density two components ($\sigma = \uparrow, \downarrow$) dipolar Fermi mixture of N particles⁴ with onsite periodically modulated interaction trapped in a 1D optical lattice. Within a single band approximation, i.e. for a deep optical lattice, the extended Fermi-Hubbard model [21] gives an accurate description of the system

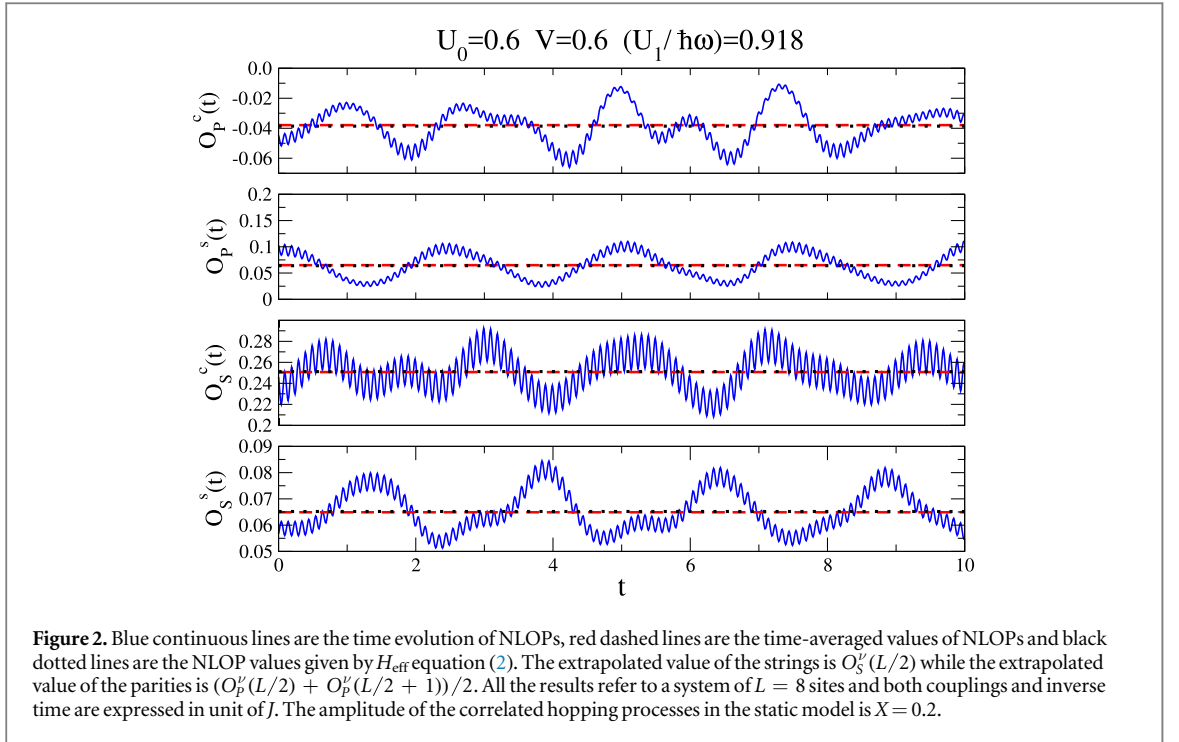
$$H = -J \sum_{\langle ij \rangle} \sum_{\sigma=\uparrow,\downarrow} (c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.}) + U(t) \sum_j n_{j\uparrow} n_{j\downarrow} + V \sum_{j,r \geq 1} \frac{n_j n_{j+r}}{r^3}, \quad (1)$$

where $\langle \dots \rangle$ denotes nearest neighbors, $c_{j\sigma}$ ($c_{j\sigma}^\dagger$) destroys (creates) a σ -fermion in the j th site of a lattice of length L and $n_j = \sum_\sigma n_{j,\sigma}$ counts the total number of particles at site j . Crucially in cold atomic experiments all the couplings, namely the hopping rate J , the onsite interaction U and the long range dipolar repulsion V may be independently controlled by modifying the lattice depth, the transversal confinement [34, 35], using Feshbach resonances, and/or controlling the orientation and strength of the polarizing field. The time dependence in (1) can be induced by a rapid variation of the scattering length [36] producing a periodic modulation of the form $U(t) = U_0 + U_1 \cos(\omega t)$ which consequently makes $H(t) = H(t + T)$ being $T = 2\pi/\omega$. In the regime $\omega \gg U_0/\hbar, J/\hbar$, Floquet theory can be used [37] to approximately remove the time dependence. Indeed, analogously to the $V = 0$ case [38], we find that this kind of interaction modulation generates an effective time independent Hamiltonian where the hopping processes are renormalized by the density, namely the CHPs

$$H_{\text{eff}} = -J \sum_{\langle ij \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.}) (1 - X(n_{i\bar{\sigma}} - n_{j\bar{\sigma}})^2) + U_0 \sum_j n_{j\uparrow} n_{j\downarrow} + V \sum_{j,r > 0} \frac{n_j n_{j+r}}{r^3}, \quad (2)$$

where $X = 1 - \mathcal{J}_0(U_1/\hbar\omega)$ is the CHPs rate, \mathcal{J}_0 is the first kind Bessel function, and $\bar{\sigma}$ denotes the other component with respect to σ . The model (2) in the $V = 0$ regime has attracted huge interest in the context of cuprate superconductors [39] while the $X = 0$ case has been studied in the context of time independent dipolar fermions, see [40] and references therein. Meanwhile only few partial analysis have tried to approach the full H_{eff} [41–43], in case of just nearest-neighbor repulsion. From the other side, our figure 1 shows how the model (2) presents a rich phase diagram including quantum regimes with hidden magnetic properties and topological

⁴ All our results are obtained by keeping as conserved quantities both the total number of particles $N = N_\uparrow + N_\downarrow$ and the single component species $N_\uparrow = N_\downarrow = N/2$.



order. As explained in the following sections, the latter phases can be characterized solely by means of non-local order parameters.

Nonlocal order parameters

In the context of lattice fermions a very fundamental role is played by NLOPs of parity- and string-like form. Their correlation functions can be written respectively as

$$O_p^\nu(r) = \langle e^{i\pi \sum_{j<r} S_j^\nu} \rangle, \quad (3)$$

$$O_s^\nu(r) = \langle S_1^\nu e^{i\pi \sum_{1 \leq j < l+r} S_j^\nu} S_{l+r}^\nu \rangle, \quad (4)$$

where $\nu = c, s$ refers to the charge and spin degrees of freedom, and the charge and spin operators are defined as: $S_j^c = (1 - n_j)$ and $S_j^s = (n_{j\uparrow} - n_{j\downarrow})$. The relevance of NLOPs lies in the fact that they act as order parameters for gapped 1D phases [2, 6, 44] without breaking any continuous symmetry, thus in agreement with the Mermin–Wagner theorem [45]. Also, non-vanishing NLOPs characterize [46] symmetry protected topological phases [47, 48] obtained by group cohomology. In particular a finite O_s^ν in the thermodynamic limit is a signature of a phase with non-trivial topological properties, noticeably the presence of degenerate edge modes [46, 49], with charge or spin fractionalization. These facts have motivated their intensive use to study 1D fermionic systems [41, 44, 50–52] helping to display physical properties not captured by the usual two-point correlation functions. More precisely, in fermionic systems the role of O_p^ν is to signal the presence of trivial Mott- (BEC-) like orders with virtual excitations consisting of correlated pairs of holon-doublon (for $\nu = c$) or single electrons with up-down spin (for $\nu = s$) [44]. Meanwhile O_s^ν captures hidden non-trivial ‘dilute’ Haldane-like antiferromagnetic orders [1, 41] of holon-doublon ($\nu = c$) or up-down spins ($\nu = s$). Generalization to higher dimension has also been considered recently [53].

Dynamics versus effective model

In order to check the validity of the Floquet theory we compare the finite size NLOP values obtained by simulating both the time dependent model (1) and the derived time independent effective model (2). The time-dependent simulations are performed by means of exact diagonalization starting from the initial ground state with couplings J , U_0 , V and at $t > 0$ a time periodicity $U(t)$ is applied in order to get CHPs of strength $X = 0.2$. After that, we monitor the time evolution and we evaluate the time-averages of the NLOPs⁵. As clearly shown in

⁵ The time-averages are shown in the time interval $2 < t < 10$. We checked that the $2 < t < 6$, $2 < t < 8$ and $2 < t < 10$ averages actually converge to the same value.

figure 2 all the time averaged NLOP values are in good agreement with the ones obtained by exactly diagonalizing (2) with couplings⁶ J, U_0, V, X . The latter result allows us to safely study H_{eff} in order to get the full phase diagram of (1) without losing some fundamental aspect encoded in the time dependence.

Luttinger liquid analysis

Here we report the results of a bosonization analysis [32] of H_{eff} , which details can be found in [54]. The Hamiltonian can be regarded as the sum of three contributions: $\mathcal{H} = \mathcal{H}_c + \mathcal{H}_s + \mathcal{H}_{cs}$. In the weak coupling limit, each of the first two contributions has the form of a sine-Gordon model in the ν sector, namely

$$\mathcal{H}_\nu = \int dx \left[H_{0\nu} + \frac{m_\nu v_\nu}{2\pi a^2} \cos(\sqrt{8\pi} \phi_\nu) \right] \quad (5)$$

with $H_{0\nu} = \frac{v_\nu}{2} \left[K_\nu (\partial_x \theta_\nu)^2 + \frac{1}{K_\nu} (\partial_x \phi_\nu)^2 \right]$. The contribution $\mathcal{H}_{cs} = \frac{M_{cs}}{\pi a} \int dx \cos(\sqrt{8\pi} \phi_c) \cos(\sqrt{8\pi} \phi_s)$, which couples the spin and the charge sectors, is irrelevant in a renormalization group analysis, having scaling dimension 4 and therefore it is usually neglected. The massive phases of the two decoupled sine-Gordon models can be analyzed in the asymptotic limit by studying the renormalization group flow equations. In ν sector the transition line to a gapped phase is determined by the competition between the kinetic and the mass terms, which generates the equation

$$2(K_\nu - 1) < |m_\nu|. \quad (6)$$

The sign of m_ν causes the field ϕ_ν in equation (5) to pin to one of the two values 0 or $\pm\sqrt{\pi/8}$, which correspond to the appearance of two distinguished nonlocal orders, namely the parity and the Haldane string orders. In fact, in the continuum limit, when the field is pinned, the NLOPs become [41]: $O_p^\nu \rightarrow \langle (\cos \sqrt{2\pi} \varphi_\nu)^2 \rangle$ and $O_s^\nu \rightarrow \langle (\sin \sqrt{2\pi} \varphi_\nu)^2 \rangle$. This observation also allows to connect a non-vanishing Haldane string order with the presence of degenerate edge modes typical of a non-trivial symmetry protected topological phase. Indeed, within the bosonization framework, they are observed at the edge between the trivial ($\phi_\nu = 0$) and the non-trivial ($\phi_\nu = \pm\sqrt{\pi/8}$) phases [46, 49], and are characterized by fractional charge (for $\nu = c$) or spin (for $\nu = s$). The solution of inequality (6) in the charge sector produces the following transition line

$$U_{0c} = \frac{3}{2} \zeta(3) V + \frac{16}{\pi} X. \quad (7)$$

For $V \neq 0$, it marks the boundary between two gapped phases, which can be distinguished by means of different NLOPs. Indeed, as U_0 crosses this critical point from higher to lower values, the topological nature of the insulating state changes from trivial ($O_p^c \neq 0$) to non-trivial ($O_s^c \neq 0$).

On the other hand, it is found that the spin sector is gapless if $U_0 \geq U_{0s}$, where

$$U_{0s} = \frac{3}{2} \zeta(3) V - \frac{16}{\pi} X. \quad (8)$$

Instead, the gapped phase obtained for $U_0 < U_{0s}$ is characterized by a parity order: $O_p^s \neq 0$.

Summarizing, we find that bosonization analysis predicts the presence of three insulating phases, separated by the two transition lines (7) and (8), as illustrated in figure 1, where the bosonization results are represented by the green and yellow solid lines. For $U > U_{0c}$, the state is characterized by finite O_p^c , thus configuring as a Mott insulating phase with trivial topological properties. Instead, between the two solid lines, i.e., for $U_{0s} < U_0 < U_{0c}$, the system is ordered by O_s^c , which identifies a charge Haldane insulator (CHI). Finally, for $U < U_{0s}$ the charge Haldane order coexists with a spin parity order, thus designating the presence of a charge density wave (CDW) locally ordered phase [41].

In the end, we would like to stress that, since the $su(2)$ spin invariance of the Hamiltonian imposes constraints on the coefficients of the sine-Gordon model in the spin channel, within the one loop bosonization analysis no phases with hidden spin order can be present. In other words, the approach described in this section is not able to predict the presence of possibly existing phases with $O_s^s \neq 0$. In fact, as we will see in the next section, the numerical analysis shows the evidence of this order for limited regions inside both the Mott and the CHI phases. The bosonization approach can be improved by releasing the requirement of spin-charge separation and by including the effect of higher order harmonics.

⁶ We checked that a different choice of the couplings does not affect the substantial agreement.

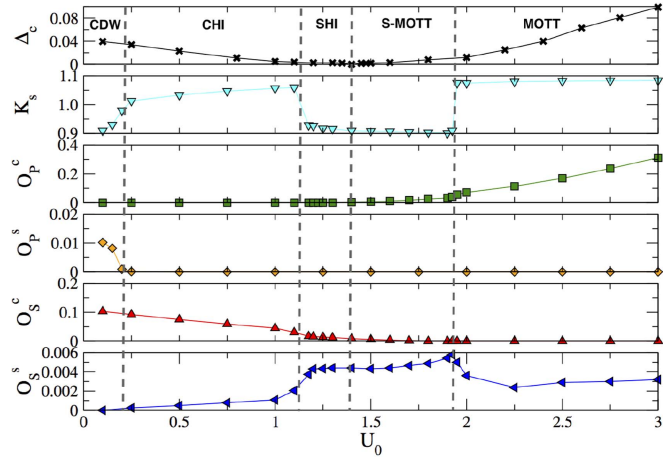


Figure 3. Thermodynamic limit of charge gap, spin Luttinger constant and NLOPs of (2) for $J = 1$, $V = 0.5$ and $X = 0.2$ as a function of U_0 . Δ_c is extrapolated by using open boundary conditions and sizes up to $L = 44$. K_s and the NLOPs are extrapolated by using periodic boundary conditions and sizes up to $L = 36$. The extrapolated value of the strings is $O_s^c(L/2)$ while the extrapolated value of the parities is $(O_p^s(L/2) + O_p^s(L/2 + 1))/2$. In all our DMRG simulations we cut r to three nearest neighbors keeping up to 1600 DMRG states and performing up to 6 finite size sweeps.

DMRG results

The bosonization analysis is expected to give reliable results in the weak coupling regime. Below we perform a further analysis based on quasi exact DMRG simulations to explore the full phase diagram. Since an insulating behavior is expected everywhere except along a critical line, as a first step we evaluate the thermodynamic limit of the charge gap $\Delta_c = (E(N + 2) + E(N - 2) - 2E(N))/2$ being $E(N)$ the ground state energy of N particles. The result is displayed in the upper panel of figure 3 for fixed $X = 0.2$ and $V = 0.5$. It clearly shows that Δ_c vanishes only in one point thus signaling a continuous phase transition between two insulating phases. DMRG results become more crucial when analyzing the behavior in the spin degrees of freedom, where CHPs are known to make bosonization less predictive [55]. Here, as a first step we evaluate the thermodynamic limit of the Luttinger spin constant $K_s = \lim_{q \rightarrow 0} \pi S^s(q)/q$ where $S^s(q) = 1/L \sum_{k,l} e^{iq(k-l)} (\langle S_k^x S_l^x \rangle - \langle S_k^x \rangle \langle S_l^x \rangle)$ is the spin structure factor. Luttinger liquid theory predicts $K_s = 1(0)$ in absence (presence) of a finite spin gap, defined as the energy variation in flipping one spin. Here both logarithmic corrections and finite size effects make very difficult to get sharp 0, 1 values. Nevertheless a well established and accurate approximation, see [56], is to consider a spin gapless (gapped) phase in presence of $K_s > 1(<1)$: the transition point is then fixed by the crossing of the value 1. As clearly visible in figure 3 the analysis based on the thermodynamic limit of K_s surprisingly finds, for small values of V , a further large spin gapped phase ranging in a region around the single point where $\Delta_c = 0$. The above results allow us to identify all the gapped regions of the phase diagram, as reported in figure 1. The nature of each phase can be better characterized by studying the behavior of the different NLOPs (see bottom panels of figure 3). Based on this analysis, for large V , we find a phase with CDW ($O_s^c, O_p^s \neq 0$) order, as expected, in analogy with the nearest neighbor extended Fermi–Hubbard model (see for instance [42]). The similarities extend also to the large U_0 region where a charge gapped Mott phase signaled by O_p^c is present. Between the CDW and Mott regions instead, the fully gapped phase with bond ordering (BOW)—characteristic of the extended Fermi–Hubbard model and signaled by a non-zero value of both parity operators—is destroyed by the CHPs. Indeed figure 3 shows that, at intermediate U_0, V , three different phases characterized by hidden magnetism take place. In particular as predicted by bosonization, a phase having as an order parameter only O_s^c appears (CHI). The latter reproduces in a two-species fermionic system the same charge hidden antiferromagnetic order of the well known topological Haldane phase studied in the context of spin-1 chains [1], extended Bose–Hubbard model [57–59], and multicomponent fermions [60]. Moreover, at variance with the bosonization results, figure 3 also shows that both the Mott and CHI regions are partially replaced by fully gapped phases, due to the presence of the spin string order ($O_s^s \neq 0$) coexisting with the charge order, meaning that \uparrow and \downarrow spins are alternated and diluted in an arbitrary number of holons and doublons properly organized. In particular, at fixed V and by increasing U_0 , we first find a phase with the two strings being simultaneously non-vanishing ($O_s^c, O_s^s \neq 0$), thus describing hidden magnetism in both degrees of freedom: holons and doublons are themselves diluted and alternated. This is called spin Haldane insulator (SHI). By a further increase of the onsite interaction, the hidden antiferromagnetic charge order (O_s^c) is replaced by the Mott-like charge order (O_p^c), where holons and doublons are organized in localized pairs. Meanwhile O_s^s remains finite in a further range, thus giving rise to spin gapped Mott phase (S-Mott). In figure 4, we show the finite size

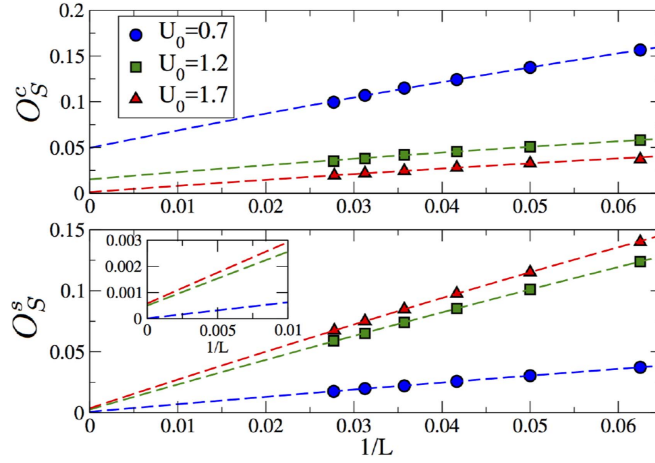


Figure 4. (a) Finite size extrapolation of O_S^c . (b) Finite size extrapolation of O_S^s . Inset zoom of the fit in (b). All the data are obtained by fixing $J = 1$, $X = 0.2$ and $V = 0.5$ for different values of U_0 and lattice sizes L ranging from 16 to 36. The extrapolated value of the strings is $O_S^s(L/2)$. In all our DMRG simulations we cut r to three nearest neighbors keeping up to 1600 DMRG states and performing up to 6 finite size sweeps.

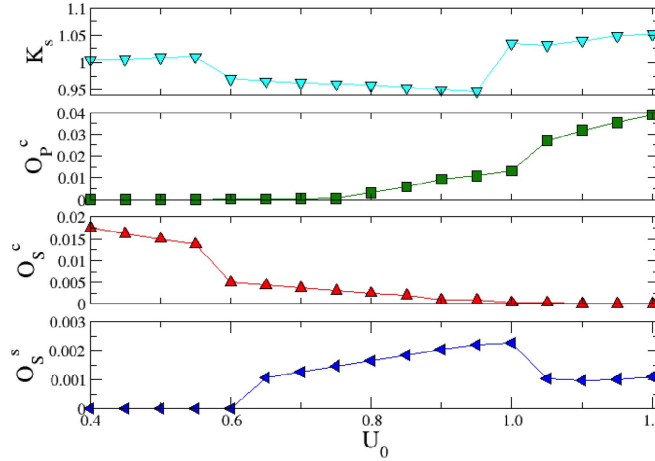


Figure 5. Thermodynamic limit of spin Luttinger constant K_s and NLOPs for $J = 1$, $V = 0.3$ and $X = 0.05$ as a function of U_0 . K_s and the NLOPs are extrapolated by using periodic boundary conditions and sizes up to $L = 24$. The extrapolated value of the strings is $O_S^s(L/2)$ while the extrapolated value of the parities is $(O_p^c(L/2) + O_p^c(L/2 + 1))/2$. In all our DMRG simulations we cut r to three nearest neighbors keeping up to 1200 DMRG states and performing up to 6 finite size sweeps.

extrapolation of the string order parameters for different values of the onsite interaction strength, namely in the CHI, SHI and S-Mott phases.

The full phase diagram is shown in figure 1, where the numerical results (symbols) are compared with the bosonization predictions (solid lines). Moreover, in the lower panel a schematic picture of the phases is drawn to help the reader understand their connotations in terms of nonlocal orders. We have checked that all our phases with hidden magnetism are stable and robust with respect to varying X . In particular, increasing X , the shape of the region with finite O_S^s is preserved, whereas the size of the region with charge string order increases, thus giving rise to an even bigger SHI regime. The crucial point, as shown in figure 5 is that the O_S^s order persists also for very weak X , meaning that CHPs are the solely responsible for these kinds of hidden spin orders.

Discussion

The above DMRG results envisage a new scenario where hidden spin string order is explicitly induced by interaction without breaking the full $su(2)$ spin symmetry of the Hamiltonian, at variance with previous results [49, 61]. Moreover, both the SHI and the S-Mott phases configure as fully gapped phases with no local order, at variance with bosonization predictions.

In fact one may further notice that the presence even for weak coupling of spin gapped phases not predicted by one-loop bosonization was already observed for a similar model [55]. In that case the inclusion of higher order harmonics in the spin channel of bosonization analysis was subsequently proved [62] to induce the opening of the observed spin gapped phase for $\phi_s = 0$. However it must be stressed that here the further spin gapped phase is non-trivial, i.e. it opens in correspondence of $\phi_s = \pm\sqrt{\pi/8}$. This suggests that the spin-charge coupling term \mathcal{H}_{cs} should have not been neglected. Otherwise the $su(2)$ symmetry of the sine-Gordon model would imply $K_s < 1$ only for $m_s < 0$, which solution describes just the trivial phase. In fact, following an approach similar to [42], the role of \mathcal{H}_{cs} in a charge gapped phase can be understood by considering in the spin channel an effective sine-Gordon model with renormalized mass $m_s^* = m_s + M_{cs} < \cos\sqrt{8\pi}\phi_c$, where ϕ_c fixed to 0 (S-Mott) or $\pm\sqrt{\pi/8}$ (SHI). Depending on the sign of M_{cs} , one sees that in this case even for a negative m_s , m_s^* can become positive: in particular, this happens in presence of Haldane charge order iff $M_{cs} < 0$ (SHI phase), whereas for trivial charge order one must have $M_{cs} > 0$ (S-Mott phase). The same approach could also be applied to justify the shift which appears in the CHI-CDW transition line with respect to bosonization predictions, exploring the case $m_s^* < 0$.

Experimental realization

The previous quantum phases could be studied by using a mixture of Erbium isotopes. In particular fermionic ^{167}Er [63] as well as bosonic ^{168}Er [28] isotopes are currently available in laboratories. The scattering length of the ^{168}Er can be accurately tuned to reach a practically hard-core regime, thus giving rise to an effective two components Fermi mixture⁷. At $30^\circ \leq \theta \leq 90^\circ$ (θ being the angle between the orientation of the dipoles and the interparticles distance,) a recoil energy $E_R = h \times 4.3$ KHz, and an appropriate lattice depth should allow to easily achieve the values $0.5 \lesssim V/J \lesssim 2$ which is exactly the regime where hidden magnetism is predicted. Feshbach resonance to tune ^{167}Er - ^{168}Er onsite interaction should become available [64] and, in order to get CHPs, a rapid time dependent modulation can be applied following the procedure in [18]. Performing measurements in a dynamically environment is very challenging. Nevertheless in a recent experiment [65] involving periodically modulated fermions, local correlations have been probed. This can be done by a sudden frozen of the system and subsequently using techniques used in static configurations where NLOPs have been already experimentally measured [66, 67].

Summary

We have shown that periodical onsite modulation of lattice dipolar fermions allows to realize Hamiltonians with long range dipolar interaction and CHPs terms. These drive the system from the static configuration of the extended Hubbard model to states with hidden magnetism. The latter appears in the charge, spin or both sectors, and can be detected solely by NLOPs. Our findings pave the way towards the study of interaction induced hidden magnetic orders and their non-trivial topological effects, such as the formation of degenerate edge modes. The phases can be detected with the currently available experimental setups and probes.

Acknowledgments

We thank L Dell'Anna, F Meinert and J Simonet for discussions. This work was supported by MIUR (FIRB 2012, Grant No. RBFR12NLNA-002). LB thanks the CNR-INO BEC Center in Trento for CPU time and the DISAT at Politecnico di Torino for the hospitality.

References

- [1] Haldane F D M 1983 *Phys. Rev. Lett.* **50** 1153
Haldane F D M 1983 *Phys. Lett. A* **93** 464
- [2] den Nijs M and Rommelse K 1989 *Phys. Rev. B* **40** 4709
- [3] Janani C, Merino J, McCulloch I P and Powell B J 2014 *Phys. Rev. Lett.* **113** 267204
- [4] Xu G et al 2007 *Science* **317** 1049
- [5] Bloch I, Dalibard J and Zwerger W 2008 *Rev. Mod. Phys.* **80** 885
- [6] Dalla Torre E G, Berg E and Altman E 2006 *Phys. Rev. Lett.* **97** 260401
- [7] Dalmonte M, Di Dio M, Barbiero L and Ortolani F 2011 *Phys. Rev. B* **83** 155110
- [8] Kobayashi K, Okumura M, Ota Y, Yamada S and Machida M 2012 *Phys. Rev. Lett.* **109** 235302

⁷ The fermionic exchange statistics of the bosonic atomic species is achieved via a Jordan–Wigner transformation, which does not alter the hopping terms in (1) nor modify the expressions equations (3) and (4) for the NLOP.

- [9] Cohen I and Retzker A 2014 *Phys. Rev. Lett.* **112** 040503
- [10] van Bijnen R M W and Pohl T 2015 *Phys. Rev. Lett.* **114** 243002
- [11] Eckardt A 2017 *Rev. Mod. Phys.* **89** 011004
- [12] Eckardt A, Weiss C and Holthaus M 2005 *Phys. Rev. Lett.* **95** 260404
- [13] Greschner S, Sun G, Poletti D and Santos L 2014 *Phys. Rev. Lett.* **113** 215303
- [14] Greschner S, Santos L and Poletti D 2014 *Phys. Rev. Lett.* **113** 183002
- [15] Struck J et al 2011 *Science* **333** 996
- [16] Struck J et al 2012 *Phys. Rev. Lett.* **108** 225304
- [17] Parker C V, Ha L-C and Chin C 2013 *Nat. Phys.* **9** 769
- [18] Meinert F, Mark M J, Lauber K, Daley A J and Nägerl H-C 2016 *Phys. Rev. Lett.* **116** 205301
- [19] Kivelson S, Su W-P, Schrieffer J R and Heeger A J 1987 *Phys. Rev. Lett.* **58** 1899
Gammel J T and Campbell D K 1988 *Phys. Rev. Lett.* **60** 71
Dolcini F and Montorsi A 2002 *Phys. Rev. B* **66** 075112
- [20] Yang C N 1989 *Phys. Rev. Lett.* **63** 2144
Montorsi A and Campbell D K 1996 *Phys. Rev. B* **53** 5153
- [21] See e.g. Lahaye T, Menotti C, Santos L, Lewenstein M and Pfau T 2009 *Rep. Prog. Phys.* **72** 126401 and references therein
- [22] Griesmaier A, Werner J, Hensler S, Stuhler J and Pfau T 2005 *Phys. Rev. Lett.* **94** 160401
- [23] Lu M, Burdick N Q, Youn S H and Lev B L 2011 *Phys. Rev. Lett.* **107** 190401
- [24] Aikawa K, Frisch A, Mark M, Baier S, Rietzler A, Grimm R and Ferlaino F 2012 *Phys. Rev. Lett.* **108** 210401
- [25] Ni K-K et al 2008 *Science* **322** 231
- [26] Wu C-H, Park J W, Ahmadi P, Will S and Zwierlein M W 2012 *Phys. Rev. Lett.* **109** 085301
- [27] Takekoshi T, Reichsöllner L, Schindewolf A, Hutson J M, Le Sueur C R, Dulieu O, Ferlaino F, Grimm R and Nägerl H-C 2014 *Phys. Rev. Lett.* **113** 205301
- [28] Baier S, Mark M J, Petter D, Aikawa K, Chomaz L, Cai Z, Baranov M, Zoller P and Ferlaino F 2016 *Science* **352** 201–5
- [29] Yan B, Moses S A, Gadway B, Covey J P, Hazzard K R A, Rey A M, Jin D S and Ye J 2013 *Nature* **501** 521
- [30] de Paz A, Sharma A, Chotia A, Maréchal E, Huckans J H, Pedri P, Santos L, Gorceix O, Vernac L and Laburthe-Tolra B 2013 *Phys. Rev. Lett.* **111** 185305
- [31] Barbiero L, Menotti C, Recati A and Santos L 2015 *Phys. Rev. B* **92** 180406(R)
- [32] Giamarchi T 2004 *Quantum Physics in One Dimension* (Oxford: Oxford University Press)
Gogolin A O, Nersisyan A A and Tselik A M 1998 *Bosonization and Strongly Correlated Systems* (Cambridge: Cambridge University Press)
- [33] White S R 1992 *Phys. Rev. Lett.* **69** 2863
- [34] Góral K, Santos L and Lewenstein M 2002 *Phys. Rev. Lett.* **88** 170406
- [35] Bartolo N, Papoular D J, Barbiero L, Menotti C and Recati A 2013 *Phys. Rev. A* **88** 023603
- [36] Rapp A, Deng X and Santos L 2012 *Phys. Rev. Lett.* **109** 203005
- [37] Grifoni M and Hanggi P 1998 *Phys. Rep.* **304** 229
- [38] Di Liberto M, Creffield C E, Japaridze G I and Smith C M 2014 *Phys. Rev. A* **89** 013624
- [39] Simon M E and Aligia A A 1993 *Phys. Rev. B* **48** 7471
Arrachea L, Gagliano E and Aligia A A 1996 *Phys. Rev. B* **55** 1173
Anfossi A, Degli Esposti Boschi C, Montorsi A and Ortolani F 2006 *Phys. Rev. B* **73** 085113
- [40] Di Dio M, Barbiero L, Recati A and Dalmonte M 2014 *Phys. Rev. A* **90** 063608
- [41] Barbiero L, Montorsi A and Roncaglia M 2013 *Phys. Rev. B* **88** 035109
- [42] Nakamura M 2000 *Phys. Rev. B* **61** 16377
- [43] Japaridze G I and Kampf A P 1999 *Phys. Rev. B* **59** 12822
Dolcini F and Montorsi A 2013 *Phys. Rev. B* **88** 115115
- [44] Montorsi A and Roncaglia M 2012 *Phys. Rev. Lett.* **109** 236404
- [45] Mermin N and Wagner H 1966 *Phys. Rev. Lett.* **17** 1133
- [46] Montorsi A, Dolcini F, Iotti R and Rossi F 2017 *Phys. Rev. B* **95** 245108
- [47] Pollmann F, Turner A M, Berg E and Oshikawa M 2010 *Phys. Rev. B* **81** 064439
- [48] Gu Z-C and Wen X-G 2009 *Phys. Rev. B* **80** 155131
Chen X, Gu Z-C and Wen X-G 2011 *Phys. Rev. B* **84** 235128
- [49] Keselman A and Berg E 2015 *Phys. Rev. B* **91** 235309
- [50] Chhajlany R W, Grzybowski P R, Stasiska J, Lewenstein M and Dutta O 2016 *Phys. Rev. Lett.* **116** 225303
- [51] Dhar A, Kinnunen J J and Törmä P 2016 *Phys. Rev. B* **94** 075116
- [52] Degli Esposti Boschi C, Montorsi A and Roncaglia M 2016 *Phys. Rev. B* **94** 085119
- [53] Fazzini S, Becca F and Montorsi A 2017 *Phys. Rev. Lett.* **118** 157602
- [54] Fazzini S, Barbiero L and Montorsi A 2017 *J. Phys.: Conf. Ser.* **841** 012016
- [55] Aligia A A, Anfossi A, Arrachea L, Degli Esposti Boschi C, Dobry A O, Gazza C, Montorsi A, Ortolani F and Torio M E 2007 *Phys. Rev. Lett.* **99** 206401
- [56] Sengupta P, Sandvik A W and Campbell D K 2002 *Phys. Rev. B* **65** 155113
Ejima S and Nishimoto S 2007 *Phys. Rev. Lett.* **99** 216403
- [57] Rossini D and Fazio R 2012 *New J. Phys.* **14** 065012
- [58] Deng X, Citro R, Orignac E, Minguzzi A and Santos L 2013 *Phys. Rev. B* **87** 195101
- [59] Batrouni G G, Scalettar R T, Rousseau V G and Grémaud B 2013 *Phys. Rev. Lett.* **110** 265303
- [60] Nonne H, Lecheminant P, Capponi S, Roux G and Boulat E 2010 *Phys. Rev. B* **81** 020408(R)
- [61] Kainaris N and Carr S T 2015 *Phys. Rev. B* **92** 035139
- [62] Dobry A O and Aligia A A 2011 *Nucl. Phys. B* **843** 767
- [63] Aikawa K, Frisch A, Mark M, Baier S, Grimm R and Ferlaino F 2014 *Phys. Rev. Lett.* **112** 010404
- [64] Frisch A, Mark M, Aikawa K, Ferlaino F, Bohn J L, Makrides C, Petrov A and Kotochigova S 2014 *Nature* **507** 475–9
- [65] Bordia P, Lüschen, Schneider U, Knap M and Bordia I 2016 *Nature. Phys.* **13** 460–4
- [66] Endres M et al 2011 *Science* **334** 200
- [67] Hilker T, Salomon G, Grusdt F, Omran A, Boll M, Demler E, Bloch I and Gross C 2017 *Science* **357** 484