Modeling, Design and Simulation of Active Suspension System Root Locus Controller using Automated Tuning Technique.

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Abstract
Car suspension system is a mechanism that separates the car from the tire. The objective of the suspension system is to improve a ride quality by ensuring passenger’s comfort and good car road handling when the car is subjected to an input excitation. The dynamics of the suspension system was mathematically modeled. The system transfer function determined. The suspension system performance characteristics of overshoot and settling time set as not more than 5% and 5 seconds respectively. PID controller was designed by using the MATLAB function sisotool in the automated tuning technique. The result of the simulation indicated that the overshoot and settling time 3.53% and 4.92 seconds respectively. The design requirement satisfied.

Keywords: Suspension, active, Root Locus.

1. Introduction
Suspension system can be classified into; passive, semi-active and active suspension system. Traditional suspension consists springs and dampers are referred to as passive suspension, then if the suspension is externally controlled it is known as a semi active or active suspension. An early design for automobile suspension systems was focused on unconstrained optimizations for passive suspension system which indicate the desirability of low suspension stiffness, reduced unsprung mass, and an optimum damping ratio for the best controllability Alleyen and Hedrick, (1995). Thus the passive suspension system, which approach optimal characteristics had offered an attractive choice for a vehicle suspension system and had been widely used for passengers. However, the suspension spring and damper do not provide energy to the suspension system and control only the motion of the car body and wheel by limiting the suspension velocity according to the rate determined by the designer. To overcome the above problem, active suspension systems have been proposed by various researchers. Active suspension systems dynamically respond to changes in the road profile because of their ability to supply energy that can be used to produce relative motion between the body and wheel. Typically, the active suspension systems include sensors to measure suspension variables such as body velocity, suspension displacement, and wheel velocity and wheel and body acceleration Esmailzadeh and Taghirad, (1997). An active suspension is one in which the passive components are augmented by actuators that supply additional forces. These additional forces are determined by a feedback control law using data from sensors attached to the vehicle. The focus of this thesis is on active suspension system controller design. “The process of selecting controller parameters to meet given performance specifications is known as controller tuning” (Ogata, 2002, p. 682). A variety of theoretical approaches have been used to produce PID-tuning formulas for a first-order plant with time delay. A heuristic time-domain analysis (Hang et al., 1991) used set-point weighting to improve Ziegler and Nichols’ (1942) original PID-tuning formulas, which were also determined empirically. “Repeated optimizations using a third-order Padé approximation of time delay produced tuning formulas for discrete values of normalized dead time” (Zhuang and Atherton, 1993). Barnes et al., (1993) used open-loop frequency response to design PID
controllers by finding the least squares fit between the desired Nyquist curve and the actual curve. In reviews of the performance and robustness of both PI- and PID-tuning formulas, tuning algorithms optimized for set point change response were found to have a gain margin of around 6 dB, and those that optimized for load disturbance had margins of around 3.5 dB (Ho et al., 1995; Ho et al., 1996). PID-tuning formulas were derived by identifying closed-loop pole positions on the imaginary axis, yielding the system’s ultimate gain and period. Dynamics are said to suffer, however, for processes where time delay dominates “due to the existence of many closed-loop poles near the imaginary axis, where the effect of zero addition by the derivative term is insignificant to change the response characteristics” (Mann et al., 2001). The root locus diagram is used as a design tool when there is only one parameter normally the forward path gain is to be adjusted. But when the root cannot be placed at the desired location with a single parameter variation, lag-lead compensators are incorporated at suitable location in the structure of the system to meet the design specifications.

2. Mathematical Modelling of Automobile Active Suspension for Quarter Car Model

Designing an automobile suspension system to meet performance specification of ride comforts and good road handling is an interesting and challenging control problem. For ease of design, analysis and simulation, quarter automobile suspension system model is used to simplify the problem. This model represent an active suspension where an actuator is included that is able to generate the required control force to control the automobile dynamics. From the quarter car model, the design can be extended into full car model.

Figure 1 above shows a basic two – degree – of freedom system representing the model of a quarter car, where the quarter mass of the automobile is represented with $M_S$, referred to as sprung mass in control and dynamics literature. $M_U$ is the mass of the wheel (unsprung mass). The spring constant of the suspension is $K_S$, $K_t$ is spring constant of the wheel and tire respectively. The damping constant of the suspension system is $C_S$ while $C_t$ is the damping constant of the wheel and tire respectively. $U$ is the control force of the actuator. From the figure 1 above and using the Newton’s law, we can obtain the system equations of motion below:

For $M_S$,

$$F = Ma,$$

$$M_S\ddot{Z}_S(t) = C_S[\dot{Z}_u(t) - \dot{Z}_S(t)] + K_S[Z_u(t) - Z_s(t)] + U(t)$$

(1)

For $M_U$,

$$F = Ma,$$

$$M_u\ddot{Z}_u(t) = C_S[\dot{Z}_S(t) - \dot{Z}_u(t)] + K_S[Z_S(t) - Z_u(t)] + K_t[Z_r(t) - Z_u(t)] + C_t[\dot{Z}_r(t) - \dot{Z}_u(t)] + U(t)$$

(2)

where

$Z_S - Z_U = $ Suspension travel

$\dot{Z}_S = $ Car body Velocity

$\ddot{Z}_S = $ Car Body Acceleration

$Z_U - Z_r = $ Wheel Deflection
\[ Z_U = \text{Wheel Velocity} \]
\[ Z_{\ddot{U}} = \text{Wheel Acceleration} \]

In control theory, the transfer function of a system is defined in terms of an output to input ratio, but the use of a transfer function in system dynamics and vibration testing implies certain physical properties, depending on whether position, velocity, or acceleration is considered as the response (output). From equation (1) and (2), taking \( Z_S \) and \( Z_U \) as output variables and taking \( U \) and \( Z_r \) as input variable respectively. The system transfer function is shown below.

\[
G_1(s) = \frac{Z_S(s) - Z_u(s)}{Z_r(s)} = \frac{(M_S + M_u)S^2 - C_S S + K_S}{M_S C_S S^3 - \dot{K}_t K_S S^2} \quad \text{(3)}
\]

\[
G_2(s) = \frac{Z_S(s) - Z_u(s)}{Z_r(s)} = \frac{(M_S + M_u)S^2 - C_S S + K_S}{M_S C_S S^3 - \dot{K}_t K_S S^2} \quad \text{(4)}
\]

where

\[
\Delta = (M_S S^2 + C_S S + K_S) \cdot (M_u S^2 + (C_S + C_t) S + (K_S + K_t) - (C_S S + K_S) \cdot (C_t S + K_t) \quad \text{(5)}
\]

The quarter – vehicle model parameter are listed in Table 1, (Du et al., 2008) for the following controller design.

Table 1: Parameter for Quarter Car Model

<table>
<thead>
<tr>
<th>( M_S )</th>
<th>( M_u )</th>
<th>( K_S )</th>
<th>( K_t )</th>
<th>( C_S )</th>
<th>( C_t )</th>
</tr>
</thead>
<tbody>
<tr>
<td>973 kg</td>
<td>114kg</td>
<td>42720N/m</td>
<td>101115N/m</td>
<td>1095Ns/m</td>
<td>14.6Ns/m</td>
</tr>
</tbody>
</table>

3. Design Requirements

The key suspension performance requirements are that the automobile should have a satisfactory road holding ability and still able to provide ride comfort when riding over undulating road surfaces, that is if the vehicle experience road disturbance such as falling into pot holes, uneven pavement and cracks, the oscillation that follows should not be too large and must dissipate quickly.

The focus of this project is to design a controller that will control the oscillation such that the output response overshoot will be less than 5% with a settling time shorter than 5seconds such that, when the automobile runs into a pothole of say 100cm (0.1m) the automobile body will oscillate within ± 5mm and becomes steady in less than 5seconds.

4. Root Locus Controller Design

The main idea of root – locus – based design is to use the root locus plot of the open – loop transfer function to estimate the closed – loop response. Adding a controller to the system changes the open – loop root locus plot so that the closed – loop response will also change.

The MATLAB function “sisotool” uses a Graphical User Interface (GUI) window where the Control Architecture and system data are selected and imported respectively then the graphical tuning plot ( Root – locus plot) for tuning/adjusting the value of the compensator and parameters of the system, an analysis plot (Step Response plot) for displaying the characteristics of the system. Integrator, lead network and notch filter are added to the compensator. Moving the locations of the notch filter (notch zeros and notch poles), lead network (lead zero and lead pole), and adjusting the gain of the compensator results in achieving the design specification.
5. Results and Discussion

Table 2. Closed – Loop Step response plot characteristics with 0.1-m high step.

<table>
<thead>
<tr>
<th>Properties</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Peak amplitude</td>
<td>1.03</td>
</tr>
<tr>
<td>Overshoot</td>
<td>3.53%</td>
</tr>
<tr>
<td>Rise time</td>
<td>0.352seconds</td>
</tr>
<tr>
<td>Settling time</td>
<td>4.92seconds</td>
</tr>
<tr>
<td>Final value</td>
<td>1</td>
</tr>
</tbody>
</table>
Figure 3. Closed – Loop Response to 0.1-m High Step

Description for the above figure.

From the table of result, the simulation value satisfied the design requirement. Overshoot is 3.53% which is less than 5%. Also the settling time is 4.92 seconds after tuning which also satisfied the requirement.

References


Du et al., 2008