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ELASTIC-PLASTIC ANALYSIS OF FRAMES -

INCLUDING AXIAL FORCE EFFECT ON MOMENT CAPACITY

by a second s

Bruce A. Bott

A Thesis Presented to the Graduate Faculty of Lehigh University in Candidacy for the Degree of

Master of Science

in

Civil Engineering

21

LEHIGH UNIVERSITY

1966

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This thesis is accepted and approved in partial fulfill-

ment of the requirements for the degree of Master of Science.

1966 May 26 Date

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Dr. Le-Wu Lu Professor in Charge

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Dr. Lynn S. Beedle Head of the Department (Acting)

ACKNOWLEDGMENTS

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Dr. Lynn S. Beedle is Director of the Laboratory and Acting Head of the Department. The study was part of a general investigation "Plastic Design in High Strength Steel" sponsored jointly by the Welding Research Council and the Department of the Navy, with funds supplied by the American Institute of Steel Construction, American Iron and Steel Institute, Bureau of Ships, and Bureau of Yards and Docks.

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Statics Marix (A) for Example Frame

Matrix of Applied Loads (PL)

Sequence of Input Data

Program Output Sequence

5 Section Properties Listed by Radius of Gyration

<u>A B S T R A C T</u>

A method is presented for analyzing the elastic-plastic behavior of frames which account for the reduction of plastic moment capacity due to the presence of axial force. A computer program, based on the one originally developed by Wang and modified by Harrison, is presented. While the original program could produce the elastic-plastic 10ad-deflection curve for a frame, it could not account for the gradually decreasing bending capacity of the frame members which resulted from the increasing axial force present in them. The reported program has been modified to include this effect.

An explanation of the basic method used by the original pro-

gram is presented. Following a discussion on the interaction of axial force with moment capacity, the new method is presented and the required modifications to the original computer program are described.

Explanation of input data and sample runs have been included. Some possibilities for design use of the program are pre-

Problems and limitations encountered in the use of the program are discussed and several suggested solutions to these difficulties are outlined.

1. INTRODUCTION

When a structural steel section is subjected to some axial force P, its full plastic moment, M_p , is reduced to some lesser value which is called the reduced plastic moment and is denoted by M_{pc} . The relation between P and M_{pc} can be determined analytically for most cross-sections.^{1,2} Consequently, if P has some known value and if the relationship between the loads applied to the member and the moments induced in it is known, then the load required to form a plastic hinge at some point in the member can also be determined. (When the moment in a member reaches M_p (of no axial force is present) or M_{pc} , a plastic hinge is said to have formed. Rotation can occur with no change in moment.)

However, if this member is a part of some frame its axial force

will usually be some complex function of the loads on the structure. The problem of finding the frame load required to form a plastic hinge at a particular location therefore becomes much more involved. A direct solution to this problem is difficult and a trial-and-error procedure becomes the logical approach in the analysis.

A method is presented in this report for determining the loaddeflection history of a frame, accounting for this axial force effect.

For the purpose of explanation and illustration the simple onebay, one-story frame shown in Fig. la will be considered. This frame is used to approximate the behavior of the bottom story of the six-story

frame in Fig. 1b.

297.21

Each column top load of 5W corresponds to one-half of the gravity loading on the upper stories of the larger frame. The lateral load used will be some percentage of the total gravity load. Designation of a particular percentage fully defines the relative proportions of the lateral and gravity loads.

The analysis reported is based upon a method for performing a first-order, elastic-plastic analysis of a general plane frame which ignores the effect of axial load. The method was originally developed by C. K. Wang³ of the University of Wisconsin and later modified by H. B. Harrison⁴ at Lehigh University. The approaches to the elastic-plastic analysis developed by Wang and Harrison relied heavily on the use of a computer as does the approach presented here. However, an understanding of the mechanics of the computer program used here is not necessarily a pre-requisite to an understanding of the method. The report is organized

with this purpose in mind. In the second chapter the theory of the simple-plastic computer analysis as Wang and Harrison developed it is presented. The chapter also explains the interaction between axial force on a member and its moment capacity. Chapter 3 deals with the effect that axial force has on the analysis of a frame.

The computer program used in the analysis is presented in chapter four. Examples of input data and output results are discussed and some of the major difficulties encountered are mentioned. The fifth chapter contains an analysis of the example frame mentioned above. Much of the data obtained from the computer program is explained and discussed. Q

It is hoped that this explanation along with the accompanying examples will enable one who is unfamiliar with computer methods to make

intelligent use of the program. Also, for the benefit of those who may wish to attempt further modifications and for those who have some programming background and desire more detailed information, a flow diagram for the main program is contained in Appendix A. A listing of each subroutine used in the Fortran program is contained in Appendix B.

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2. BASIS OF ANALYSIS

2.1 THE ELASTIC, SIMPLE-PLASTIC ANALYSIS

The elastic simple-plastic analysis, as developed by Wang and Harrison, provides the foundation for the method of analysis reported here. A schematic load-deflection curve, typical of Harrison's solution is shown in Fig. 2, where H is the lateral load and $\Delta_{\rm H}$ is the sway deflection of the column tops.

The method begins with an elastic analysis of the frame which determines the slope of line \overline{OA} . Point A represents the formation of the first plastic hinge in the frame and it is located as follows. At each of i possible plastic hinge locations in the frame, the moment corre-

sponding to a given load can be expressed as:

(1)

in which m_i is the moment resulting from the application of a unit load to the frame and H is the applied load. If axial load is assumed to have no effect, a plastic hinge will form at a point when $M_i = M_{pi}$. The location and load corresponding to the formation of the first plastic hinge can be determined by substituting M_{pi} for M_i in Eq. 1, solving for H, and then selecting the lowest value.

The analysis continues by inserting a real hinge in the frame at the location of the plastic hinge (shown as (1) in Fig. 2) and performing another elastic analysis. In this way, new values of m_i are found, and the slope of the second segment is determined. A new version of Eq. 1 can be written in order to locate point B which corresponds to the formation of the second plastic hinge.

 ${}^{\mathrm{m}}\mathbf{i}\mathbf{1} {}^{\mathrm{H}}\mathbf{1} {}^{\mathrm{H}}\mathbf{i}\mathbf{2} {}^{\mathrm{H}}\mathbf{2} {}^{\mathrm{H}}\mathbf{1} {}^{\mathrm{H}}\mathbf{1}$

Double subscripts have been introduced to the m's to indicate which point or location on the frame they refer to (i) and which elastic analysis they result from (1 or 2). For values of load between H_1 and H_2 (see Fig. 2), Eq. 2 computes the moment at each point. (Note that $m_{12} = 0$ for the first plastic hinge location due to the presence of a real hinge there). As before, substituting M_{pi} for M_i , solving for H_2 , and selecting the lowest value will locate point B on the plot.

The procedure of analyzing a successive series of elastic

-6

(2)

(3)

frames with real hinges at the plastic hinge locations is continued until a failure mechanism forms, as indicated by a horizontal line for some appropriate load-deflection plot for the frame.

In general, the equations which govern the loads corresponding to the various stages of hinge formation and the locations of these hinges can be written in the following form.

 $m_{1,1}$ H_2 + $m_{1,2}$ H_2 + $m_{1,h-1}$ H_{h-1} + $m_{1,h}$ H_h = M_{p1} $m_{2,1}H_1 + m_{2,2}H_2 + \dots + m_{2,h-1}H_{h-1} + m_{2,h}H_h = M_{p2}$

 $m_{a,1} H_1 + m_{a,2} H_2 + \cdots + m_{a,h-1} H_{h-1} + m_{a,h} H_h = M_{pa}$

in which h is the number of the plastic hinge under investigation and a is the number of possible hinge locations for the frame.

The values of H are known between H_1 and H_{h-1} inclusive by previous calculations. Also, once H_1 , H_2 , \ldots H_{h-1} are found, their values do not change as additional load is applied. Therefore, Eqs. 3 are a series of equations in one unknown with each equation resulting in some value for H_h . Comparison of these values determines the location of the new hinge. A similar series must be examined for each new hinge. Because the values of H_1 , H_2 \ldots H_{h-1} do not change after they are first determined, one pass up the load-deflection curve is sufficient to evaluate the complete load-deflection history of the frame. In other words, once a plastic hinge forms at some point, it is not influenced by any additional load that may be placed on the frame at a later time.

It should be noted that regardless of the magnitude of the column top loads in Fig. 2 they have no effect on the capacity of the frame when it is analyzed in the above manner, since it is assumed that the presence of axial load in a member has no effect on its moment capacity. The validity of this assumption is investigated next.

2.2 THE EFFECT OF AXIAL FORCE ON MOMENT CAPACITY

If a member is subjected to some axial force P, its available moment capacity M is reduced. This reduced value of M_p, defined as M_{pc} , can be determined analytically, and for most sections, curves and equations have been developed which relate P to M_{pc} once M_p and the yield load P_y are known.^{1,2} For most wide-flange shapes bent about their major axis, such curves fall in a relatively narrow band, and simple expressions can be used to approximate them.

Figure 3 shows a non-dimensional plot of the moment versus axial force relationship for strong-axis bending of wide-flange shapes. The solid curves represent the upper and lower limits of the exact interaction relations for wide-flange shapes.² The dotted straight lines are the usual approximations for these curves as suggested in Ref. 1. The approximate curves are expressed analytically by the following equations:

$$M_{pc} = M_{p}$$
 (0 ≤ P ≤ .15 P_y) (4)

 $M_{pc} = 1.18 M_{p} (1 - P/P_{y}) \quad (.15 P_{y} < P \le P_{y}) \quad (.5)$

Note that Eq. 4 indicates there is no reduction of moment

capacity due to axial force if P is less than $0.15 P_y$. The limits imposed on the application of Eq. 4 therefore provide an upper bound to the axial loads which may be present in a structure if an elastic simple-plastic analysis of it is to be valid. If the axial loads reach some value greater than $0.15 P_y$ Eq. 5 must be used and various modifications in the analysis are required. These modifications are the subject of the next chapter.

<u>3. INCLUSION OF THE AXIAL FORCE</u> EFFECT IN A FRAME ANALYSIS

The effect of axial force can be included in the analysis by modifying the equations which govern the formation of plastic hinges in the frame. Previously, all plastic hinges had to satisfy the requirements imposed by Eq. 3. If the effect of axial force is considered, these requirements are applicable only to those plastic hinges which form under an axial force less than 0.15 P_y, as is shown by Eq. 4. All other plastic hinges must satisfy Eq. 5.

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The generalized forms of Eqs. 4 and 5 are



where n is the unit axial force in the member, b is the number of the point on the load-deflection curve which is currently being computed, and h is the number of the plastic hinge the equation is being applied to. Note that b is always greater than or equal to h. The reason for this will be seen below. Equation 6 was presented and discussed in Chapter 2 (as Eq. 3), but some additional explanation will be of value in understanding its function in the modified analysis.





As load is placed on the structure, a bending moment equal to the unit moment m times the applied load will be induced at the point. The line segment AC is the moment present at the point $(m_1 \text{ times } H_1)$ when the first plastic hinge forms in the frame. (The first plastic hinge is assumed to form somewhere other than at the point in question.) Additional increments of load on the frame will result in similar additions to the moment at the point, such as CD, which is equal to m_2 times H_2 . If the

(8)

point in question is involved in the failure mechanism for the frame, the bending moment at the point will finally reach M_p and a plastic hinge will form. At this stage in the loading, Eq. 6 is satisfied as shown below:

 $m_1 H_1 + m_2 H_2 + m_3 H_3 = M_p$ (AC + CD + DB = AB)

Axial force had no effect in the above case because it was less than the critical value of 0.15 P_{i} .

If the axial force at some point exceeds 0.15 P_y , the behavior of the point through various stages of loading can be traced with the aid of the diagram below.

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As before, let the line AB represent M_p for the point. When the first increment of load is applied to the frame, some moment and some axial load will be induced at this location. Because the axial force P is assumed to exceed 0.15 P_y, some reduction in M_p will take place. When the first plastic hinge forms in the frame, conditions at this point are represented by a reduction in capacity DB due to axial force and a bending moment at the point equal to AC. Of the remaining bending capacity that portion which is usable (M_{pcl}), is now CD rather than CB as in the previous case. If the second plastic hinge forms at this location, the next increment of load will cause the added moment CE and

reduction in capacity due to axial force ED to meet at point E thereby satisfying Eq. 7 for this location in the frame. As more load is applied to the frame, no additional moment will occur at this location because a real hinge is inserted at the location of each plastic hinge for the purpose of each subsequent elastic analysis. Hence all further unit moments for this point will be zero. This is not the case for the unit axial force at this location. In most cases, the unit axial force will continue to have some value other than zero until the mechanism load is reached. Unless the formation of a hinge at the point under discussion resulted in the formation of a failure mechanism, additional frame loads will be added to those already present. In order to reach this mechanism

load Eq. 7 shows that at the location in question, the additional axial

force resulting from this increase in frame loads causes M to decrease. pc to decrease. This in turn requires adjustment of segments AC and CE in order to maintain equilibrium at the point.

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In summary the analysis of a frame can be thought of as the determination of a series of points on its load-deflection curve. Each of these points represents the formation of one new plastic hinge. The curve becomes horizontal and the analysis terminates when enough hinges, have formed to produce a failure mechanism. At each of the points on the load-deflection curve, all the plastic hinges then formed must satisfy either Eq. 6 or Eq. 7 depending on the value of axial force at each point. Those for which Eq. 7 is applicable experience a weakening or an inability to carry their previous moment due to an increase in axial force as more load is applied to the frame. Hence, as each of the plastic hinges form, a readjustment or a redistribution of moment must

take place in the frame to account for the weakening of the previous hinges. This redistribution must be such that each hinge will satisfy its pertinent equation. This redistribution can be accomplished in many ways.

One method is to apply some internal moment to each plastic hinge that is effected by axial force. This internal moment would be equal in magnitude to the reduction in moment capacity at each point due to the increase in axial force. Because the value of these internal moments cannot be determined until the increment of load to form the next plastic hinge is determined and because the increment of load cannot be determined until the internal moments are known, the problem is non-linear, and a trial-and-error procedure becomes the most logical

approach for computer analysis. This method has the disadvantage of introducing to the frame an additional degree of freedom for each internal moment applied to the frame. If a computer-matrix solution based on the displacement method is used, the introduction of additional degrees of freedom to the frame will use up a noticeable percentage of the available computer storage space and may severely limit the size of frame which can be handled by a particular machine.

A second approach, and the one which is used by the present analysis, is to make successive adjustments on the various increments of load between the formation of plastic hinges until either Eq. 6 or Eq. 7 is satisfied at each plastic hinge location. This procedure can be exemplified by reference to Fig. 4. The upper curve in Fig. 4 is a schematic of the elastic, simple-plastic load-deflection curve for the frame shown where the effect of axial force on bending capacity is neglected. Points A, B, C, and D represent the formation of plastic hinges on the frame at points 1, 2, 3, and 4 respectively. For the purpose of explaining the method of solution, it will be assumed that the axial force does not alter the order of formation of the plastic hinges from that of the elastic, simple-plastic analysis. For the most part this is a correct assumption for simple frames. However, in complex frames involving a large number of hinges in the failure mechanism, it may not always be true. The solution begins with an elastic analysis of the original unaltered frame which produces unit moments and unit axial loads formeach of the possible hinge locations on the frame. Equation 7. is applied to each of these points and a value of load required to form a plastic hinge at each is determined. If axial force is found to be less than 0.15 P_v , Eq. 6 is substituted for Eq. 7. In an actual

1

analysis, the magnitude of P is checked against 0.15 P_y for the location involved and the proper equation is applied at each hinge. For this explanation, P will be assumed greater than 0.15 P_v for all members. The smallest of these loads determines that the first plastic hinge forms at point 1 on the frame and at a load corresponding to A_1 on the plot. The axial force effect lowers A from A to A $_1$. A real hinge is then inserted at location 1 and a second elastic analysis is performed to determine the slope of the next segment. On the basis of Eq. 7, point B_1 is found and the second plastic hinge forms at location 2 on the frame. The increase in load in moving from A_1 to B_1 increases the axial force at location 1 and thus reduces the moment capacity at that point. In, order to satisfy Eq. 7 at location 1, P_1 must decrease to the value represented by point A₂. Point B is computed again and the cycle is repeated until Eq. 7 is satisfied at points A and B (Locations 1 and 2) simultaneously. Once agreement is obtained for both points, point B

is recorded as a point on the actual load-deflection plot. Next, a third elastic analysis on a frame with two real hinges is performed and the process repeats. Successive hinges are introduced until a mechanism is formed, ending the analysis.

Figure 5 is a schematic plot comparing the curves produced by the elastic, simple-plastic analysis of Wang and Harrison (dashed) and the analysis including the effect of axial force (solid). The general trend is for axial force to decrease the slope of each segment on the curve. Straight lines are not strictly correct for the lower curve beyond the first segment. Each segment is a curve which starts at the lower point, tangent to the elastic slope for the frame (the slope of the corresponding segment of the upper curve) and gradually curves to reach the next higher point. The curves have been drawn straight because the information which is necessary to produce the exact line is not produced by the analysis presented in this report.

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4. THE COMPUTER PROGRAM

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4.1 INDEXING SYSTEMS

To write a successful computer program for even the simplest of problems it is necessary to institute some convenient and logical system of identifying the quantities involved. Some of the systems used by the program are shown in Fig. 6.

Figure 6a shows the method of identifying members in a frame. Each point of load application is considered to be a joint in the frame and as a result, a beam subjected to quarter point loading is broken down into three members. (Intermediate supports in a continuous beam would be treated in the same manner.) Each member is assigned a number

(circles on Fig. 6a) as is each member end (squares on Fig. 6a). The

even end number is equal to twice the member number and the odd end number is taken as one less than the even number.

These member end numbers are used to identify the internal forces acting on the member ends. The sign convention for these internal forces (Fig. 6b) is moment positive counter-clockwise on the member end and axial force positive in tension. The choice of a sign convention is purely arbitrary and any consistent convention can be used. The numbering of these end forces is exemplified in Fig. 6b. The member numbering system is also used to identify which location the unit moments and axial loads produced by each elastic analysis pertain to. These unit quantities are indexed in exactly the same manner as the member end forces and the same sign convention is followed.

The second indexing system, shown in Fig. 6c, arises from the need to identify deflections and loads. Each joint, unless it is restrained, has three degrees of freedom; a horizontal and vertical deflection and a rotation. For each degree of freedom there is a corresponding load whose point of application and direction coincides with the possible movement.

Although loads will not usually be acting at all possible locations on the frame at one time, the matrix methods used require space to be reserved for all possibilities. Hence, the numbering system for loads and deflections is the same. Figure 6c shows the deflections and loading possibilities for the example frame. There are four vertical, four horizontal, and four rotational deflections possible as well as

their corresponding loads, and they are indicated in their positive directions. The sequence of numbering is completely arbitrary although listing all vertical, all horizontal, and all rotational quantities in sequence lends order to the output.

The step-wise nature of the analysis provides the need for a third indexing system. Each of the initial elastic slopes on the loaddeflection plot is produced by an elastic analysis which also produces the unit moments and axial forces mentioned previously as well as the unit deflections. Each of these pieces of data must be associated with a location on the frame and with the analysis which produced it. For example, a unit moment is of no value unless it is known that it applied to location number 2 and that it was produced by an analysis of the frame with plastic hinges formed at locations 4 and 7. Hence, two subscripts will be necessary to completely identify unit axial loads, moments, and deflections. The first subscript will be the number of the location (2 for the above example) and the second would be a 3 if the analysis of a frame with plastic hinges at locations 4 and 7 is the third one to be performed.

A fourth system of subscripts evolved partly because of the trial-and-error system employed in the analysis and the resulting necessity for the program to be able to refer to previous results, and secondly because of a need for some mechanism to terminate the run if convergence could not be obtained in a reasonable number of tries. The procedure adopted in the program could be improved on to increase its efficiency. However, the method used enjoys the advantage of simplicity over other possibilities.

This fourth system introduces a second subscript to the increment of applied load H indicating which trial number it is a result of. (The first subscript refers to the segment of the load-deflection curve it pertains to.) For example, on the first try at satisfying Eq. 6 and/ or Eq. 7 at each of three plastic hinge locations, $H_{(1,1)}$, $H_{(2,1)}$, and $H_{(3,1)}$ would be produced, while the second try would result in $H_{(1,2)}$, $H_{(2,2)}$, and $H_{(3,2)}$, and so on.

4.2 INPUT DATA

After labeling the various quantities in the manner described in Section 4.1, the data required for an analysis can be assembled.

The program is designed to accommodate more than one analysis with each run so at the start of each analysis an identifying frame number JJ is read in. This number may be any fixed point Integer from 0 to 99999. It is used as an identifying number which appears on the first page of the output for each analysis. In addition, after the data for the last frame to be analyzed, a negative frame number should be included. This will serve as a trigger to terminate the run.

Next, in order that the program might construct internally several of the arrays required by the analysis, two more fixed point integers are input. They are the degrees of freedom L and the number of members NM. (For the example frame L and NM would be 12 and 5 respectively.) From NM two other quantities are found which are also used internally for matrix operations:

where M is the number of member ends in the frame and N is the number of internal forces in the frame.

The statics matrix A which relates the applied loads on the frame to the internal member end forces follows L and NM as input data. The matrix is determined by knowing that for each degree of freedom in the frame an equation of equilibrium can be written.

For example (see Fig. 7) the upper left column top joint on the

frame of Fig. 6 produces 3 equations.

(9)



ΣF_x



 $\Sigma \mathbf{F}_{\mathbf{y}} = \mathbf{0}$

= 0

ΣΜ

-20

(11)

(12)

 $W_{9} = M_{2} + M_{3}$ (13)

Writing equilibrium equations similar to Eqs. 11, 12, or 13 for each degree of freedom in the frame and presenting the results in matrix form results in the statics matrix of Table 1. The size of this matrix is $(L \times N).$

The development of the statics matrix for a non-rectangular frame such as a gable frame is more involved, but the same techniques apply.

A list of section properties for each member in the frame follows the statics matrix. The four variables required are indicated and defined below:



PY = Py.

where E = modulus of elasticity, I = moment of inertia, A = cross-sectional area, and ℓ = member length.

A load set number, KK, is next in the input data. It is treated in much the same manner as was the frame number JJ above. KK is used to identify a particular load set on the output and if it is negative, the program assumes there are no additional load sets to be applied to the current frame and goes to the beginning to see if there is another frame to be analyzed. As mentioned previously, should it encounter a negative frame number there, it will exit from the program. Following KK is a column matrix (L x 1) of the applied loads. The load matrix (PL) for the example frame subjected to gravity loads at the quarter points of the beam and a horizontal force to the right (equal in the magnitude to the gravity loads) applied at the left column top appears in Table 2. Note that all possible applied forces must appear in the array even if they have no value for the given loading case.

For a particular frame, any number of load sets may be applied

during a single run with a negative KK as the final card in the deck of load sets. A sample deck setup for the analysis of two frames with two sets of applied loads each is shown in Table 3.

Experience with the Lehigh GE225 computer has indicated that a card with "END" appearing in the first 3 columns should be the last card in the data deck. With the large number of data cards required for each analysis, it is quite conceivable that one may be lost causing the machine to read into the next analysis or even the next program in its attempt to obtain the required amount of data. Encountering any card with alphaneumeric characters on it will halt the analysis.

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In the preparation of the data for an analysis, care should be taken to use consistent units throughout. All of the numerical examples in this report are based on kips and inches.

4.3 PROGRAM OUTPUT

Copies of the program and some example outputs are contained in their entirety in B and C. Most questions concerning specific difficulties can be resolved by referring to this area. However, some general explanation is in order and this can be found in Table 4.

4.4 PROBLEMS

4.4.1 Storage Space

The program storage requirements severely limit the size of frame which can be accommodated on all but the largest machines. Several

alternative solutions to this limitation are available.

The simplest and perhaps most obvious move would be to use a larger capacity machine. However, this is not always possible or desirable. It seems that regardless of the available machine capacity, there will always be frames of interest which exceed this capacity. Hence, several things have been done to the program to economize on the available capacity within a particular machine.

One way to eliminate wasted storage is to utilize common storage. Ordinarily if each of two subroutines use a variable of the same name, it is considered by the machine to be two separate and discrete quantities in each of the subroutines. If it is desired to transfer the value of

الواقور واقعاد المالي اليواري وساريسا ساليا والمالي المالي والمحمد المالي والمراجع المناقر المقور والمروس المالف

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this variable from one subroutine to the other, it must be listed in the subroutine call statement as an argument. As a result, although both subroutines are using the same variable, two storage locations are required in the machine memory. If this variable is an array of 100 points, 200 locations would then be required. By listing the variable in identical common statements at the beginning of each subroutine, each subroutine will store the value or values of the variable in the same or common storage locations so they will be freely available to each.

Hence, one location is all that is necessary to store one variable. The program contained in this report uses nine subroutines and a main program. The use of common statements reduces its data storage requirements to one-tenth of that required previously.

Additional economy may be obtained through the use of magnetic

tapes. With most installations, it is possible to store segments of a program on tape until they are called for by other segments of the program. It is also possible to store data on tapes for future use. Although, conceptually it is possible to use both of these mechanisms simultaneously to reduce storage requirements, most machines lack the necessary hardware to accommodate the large number of tapes required and only one can usually be used. The reported program uses tapes for data storage. On the GE225 computer, three tapes are needed to accomplish this, which, combined with the systems tape which controls the program execution, equals the total tape capacity of the machine.

Of the methods used to fit a particular size frame into the storage available within a given machine, the above mentioned ones are concerned primarily with making more efficient use of a machine through modifications to the program and its use of machine hardware. However, it is possible in some cases to decrease the size of the data arrays which must be stored. If some beforehand knowledge can be obtained, either through hand calculations, another program, intuition, etc., of the location of the plastic hinges in the failure mechanism, the loads on members which are not directly involved in the mechanism can be replaced with fixed end moments and shears. This, by eliminating some degrees of freedom, will reduce the size of all the arrays involved and may mean the difference between running a problem and not running it on a particular machine.

4.4.2 Change in the Order of Formation of Plastic Hinges

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As was mentioned in Chapter 3, during the trial-and-error

procedure to satisfy either Eq. 6 or 7 at each plastic hinge location on the frame, successive adjustments are made in each of the legs of the load-deflection curve. If, for example, three plastic hinges are present in the frame, the first to form and the lowest on the loaddeflection curve is in the beam (a member insensitive to axial load), the second is in the column (a member sensitive to axial load) and if the point which is being investigated for being the third and next hinge to form is a location with a large amount of remaining moment capacity, the following is likely to occur. With each trial, the location of the first point on the plot will not vary noticeably because

of its comparative insensitivity to axial load. The second point on the

plot will however be lowered due to the increasing axial load at its location resulting from the third increment of load. It is conceivable that the length of the second segment could be reduced to zero or a negative value. Zero indicates that plastic hinge Nos. 1 and 2 now form at identical loads. A negative value for the second segment indicates that now the plastic hinge that previously formed second will form first. In other words, there has been a change in the order of formation of the hinges. This, however, does not imply that if the frame were to be tested the plastic hinges would form in this new order but rather that the equation governing the second hinge now is satisfied at a lower load than that which satisfies the equation governing the first hinge.

The solution to this difficulty can be shown with the aid of Fig. 8. At the point where this change in hinge order occurred, frames A, B, and C had been analyzed. Traveling up the load-deflection curve entailed utilizing the unit moments and axial loads, etc. from these elastic analyses of the frames to satisfy the governing equations at each plastic hinge. (Eqs. 6 and 7) Now, with the negative second segment and with the resulting new order of formation for the hinges, a new frame must be analyzed (Frame E in Fig. 8). After this frame is analyzed the regular analysis can proceed using the unit values of frames A, E, and C in the usual fashion. If by chance the second segment had become exactly zero, analyses of frames A and C would be sufficient and no new frame analysis would be required.

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One of the major difficulties involved in this procedure is how to identify a given frame with hinges at various locations and how to record whether or not it has been previously analyzed. This may seem to be a trivial problem until one considers that for the example frame, with an assumption that four hinges would be required in most failure mechanisms, the computer could be called on to analyze any of more than 50 different frames. In view of the storage problems mentioned above, numbering all 50 would use an excessive number of machine storage locations. The solution to this problem would be based on the creation of a column matrix whose number of columns equals the number of hinges in the failure mechanism (more if the exact number is unknown). Each row would record the analysis of one frame. If hinges formed at locations 4, 7, and 11 (in order), the first four rows would be as shown below:

> 0 0 0 0 4 0 0 0 4 7 0 0

This array indicates that the first frame analyzed contained no plastic hinges, the second contained one at location 4, and so on.

An element by element search of this matrix would determine whether or not a given frame had been analyzed and, if it had been, which one it was (first, second, third, or fourth analysis). Knowing the number of the frame in which certain plastic hinges were present would allow the program to locate the unit axial forces, unit moments, and unit deflections pertaining to that frame. In summary, once a change in hinge formation occurs, reference to the above matrix would determine if the new required frame (Frame E in Fig. 8) had been solved. If not, it would be analyzed and that fact would be recorded in the

. 1

matrix. If it had been previously analyzed and recorded the analysis could continue immediately using the previously computed information. From the standpoint of storage, note that this matrix would require approximately twenty-four locations to record all pertinent data as compared to fifty or more locations if all possible frames which could be analyzed were simply numered. The occurrence of the hinge reversal phenominon increases rapidly as larger frames are encountered, and it is in this area that the ease of identifying frames with this matrix becomes most apparent. For frames only slightly larger than the example frame, the matrix can be expected to require less than one-quarter as many storage locations as there are possible frames to be analyzed.

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5. RESULTS AND DESIGN CHARTS

FOR THE EXAMPLE FRAME

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Much of a computer program's value lies in its ability to perform a large number of computations in a short period of time. The program contained in this report produces a complete load-deflection history of the example frame under some prescribed loading in approximately five minutes on the GE225 machine. Therefore, with only a minimum of effort on the part of the operator, curves can be developed which, for a given frame, will completely predict the behavior of the frame throughout its range of loading possibilities. The development of such curves for the example frame is the subject of this chapter.

5.1 BOUNDS ON POSSIBLE FRAMES

If the only limitation imposed on the construction of a frame is that its geometry must coincide with that of the example frame, an almost unlimited number of such frames could be constructed from the various rolled steel wide-flange shapes available.⁵ However, many of these possible frames would behave in a similar fashion when subjected to the same loading. Therefore, if some bounding cases could be analyzed, nearly all behavior possibilities could be predicted with a minimum of effort.

In order to pick such bounding cases, it is helpful to use some parameters which indicate some of the properties of a given frame.

The first of these is the ratio of the column stiffness to

beam stiffness, G, as shown below⁶

where $I_c =$ the moment of inertia of the column, $\ell_c =$ length of the column, $I_b =$ moment of inertia of the beam, and $\ell_b =$ length of the beam. The second parameter is the slenderness ratio, ℓ/r_x where $r_x =$ the radius of gyration of a section about its major axis.

 $G = \frac{I_c / \ell_c}{I_1 / \ell_1}$

For most building frames, Ref. 6 places the upper and lower limiting values of G at 3.0 and 0.5 respectively. For each of these values of G, several combinations of ℓ/r_x for the beam and column are possible. Using some common values of ℓ/r_x , Fig. 9 represents some theoretical possibilities for each extreme of G.

In general, for most frames and in particular for the example frame, many of the possible combinations of G, ℓ/r_x for the column, and ℓ/r_x for the beam cannot be constructed with the rolled shapes currently available. For instance, for the example frame with

(15)

(17)

(18)

 ℓ = 180", a G of 0.5 would require that

l_c/r_x

 $\ell_{\rm b}/r_{\rm x_1}$

= 30

= 25

and if,

(16)

Then

and

 $r_{x_{b}} = 14.4$

(19)

(20)

 $r_{x_{c}} = 6.0$

The "Plastid Section Modulus Table" of Ref. 5 shows that there are no rolled sections with $r_x \approx 14.4$ whose moment of inertia equals approximately four times the moment of any section with $r_x \approx 6.0$. (The sections listed in the "Plastic Section Modulus Table" have been rearranged and listed for convenience in Table 5 in order of their radius of gyration.) Similarly, several other combinations of ℓ/r_x and G are impossible to construct for the example frame and all such cases are indicated by crosses in the appropriate boxes in Fig. 9.

Frames satisfying the conditions corresponding to each of the remaining boxes in Fig. 9 can be constructed and two typical cases are indicated by circles. The analysis of these two cases will provide the bounds mentioned above on the behavior of the example frame.

5.2 RESULTS FOR EACH CASE

Figure 10 shows the two frames represented by the circles of Fig. 9. The case of G = 0.5 will be referred to as the strong beam-

weak column case while for G = 3.0 the term strong column-weak beam

will be used. The sections indicated on the frames of Fig. 10 were

chosen by the procedure explained above (Eqs. 15 to 20).

As shown in Fig. 1 the example frame is assumed to be the bottom story of a six-story frame which results in a 5:1 ratio between column top loads and beam gravity loads. The ratio of a point load on the beam to the side load is given by β . For the six-story frame the side load is given as a percentage of the total vertical load by 100/12 β .

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Figures 11 and 12 are plots of horizontal load versus horizontal deflection of the column tops for several loading conditions on each frame. Each curve represents a different ratio of horizontal to vertical loading as indicated by the values of β . The horizontal load, as a percentage of the total vertical load, is also shown.

Each point shown on each curve corresponds to the formation of a plastic hinge in the frame. The location and order of formation for these hinges is shown on the small diagram of the frame at the end of each curve. The numbers located next to each plastic hinge indicate. the sequence of formation.

Note the preponderence of sway mechanisms for the strong beam-weak column case and the corresponding presence of beam mechanisms for the strong column-weak beam case. The relative strengths of the beam and column obviously play a key role in the determination of the type of failure mechanism.

In Fig. 11 the case of H = 1% of the gravity load was not produced by the program. This is because, by coincidence, the hinge reversal phenomenon of Section 4.4 occurs for this particular ratio of loads. This is evidenced by comparing the order of hinge formation for $\beta = 4.16$ and $\beta = 16.7$. By introducing slightly different values of β than that corresponding to the 1% case, close approximation to the 1% line could be obtained. However, this was not attempted for this figure. In Fig. 11 the analysis of the frame with $\beta = 16.7$ produced some unusual results. The third and fourth segments of the loaddeflection plot for this case indicate an increase in frame stiffness over that shown by the second segment. This would not normally be expected because the introduction of each successive plastic hinge to the frame brings it closer to failure by removing one degree of indeterminancy. As a result the stiffness of the frame will usually be reduced with the formation of each new plastic hinge. However, in this case, the results produced by the program are correct and they can be explained with the aid of Fig. 13.

The four frames of Fig. 13 are the frames corresponding to each of the four segments of the load-deflection plot of Fig. 11 for $\beta = 16.7$. Because a symmetrical frame subjected to symmetrical gravity loading (W) will experience no sidesway, the unit deflection $(\delta_{\rm H})$ at the column tops of such a frame is a function of horizontal load (H) only as is shown by frames (A) and (C) of Fig. 13. For an unsymmetrical frame, such as (B) or (D) of Fig. 13 symmetrical gravity load will cause some sway. As a result, the unit column top deflection $(\delta_{\rm H})$ for such a frame will be a function of both lateral (H) and gravity (W) loads. The frames analyzed to produce the lower curve of Fig. 11 ($\beta = 16.7$) alternate between the symmetrical and unsymmetrical cases shown by Fig. 13. Hence, only the second and fourth segments of the load-deflection curve are functions of both the gravity and lateral loads.

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If the relative contribution of W to $\delta_{\rm H}$ is much higher than that of H as would be the case for the frame of Fig. 11 with H = 1/2%(W), the value of the unit deflection $\delta_{\rm H}$ for the second analysis (frame B of Fig. 13) would be greater than that for the first analysis (frame A of Fig. 13). A flat slope would appear on the H - $\Delta_{\rm H}$ plot. Following a similar line of reasoning, it can be seen that the slope of the third segment should increase from that of the second segment, which it does.

Note that for the cases of $\beta = 2.08$, 2.78, and 4.16 in Fig. 11, none of the frames analyzed are symmetric after the first. Hence, the above effect does not appear.

This effect can also be seen in the lower three curves of Fig. 12. Here, however, the effect of symmetry explained above is combined with another problem. The failure mechanism for the lower three analyses is a beam mechanism and as a result, the plotting of H versus $\Delta_{\rm H}$ is not too indicative of the behavior of the frames. For these three cases, a plot of H versus vertical beam deflection would be more

appropriate.

In summary, the axial force effect lowers the value of the load required to form a particular mechanism in a frame and quite often will cause the plastic hinges involved in that mechanism to form in a different order. If the influence of the axial force is great enough, a failure mechanism which is at least partly different from that predicted by simple plastic theory (neglecting the effect of axial force on moment capacity) will result.

Usually the stiffness of the structure decreases as the effect of axial force increases. This can be seen by comparing the slopes of corresponding segments on each of two load-deflection plots such as those

in Figs. 11 or 12. Again, note that straight lines are not strictly correct as was explained at the end of Chapter 2. However, the fact that the exact curves for each segment are curves which are concave downward in itself indicates that axial force decreases frame stiffness.

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5.3 DESIGN CHARTS

For any particular frame geometry, non-dimensional interaction curves can be constructed which will allow rapid and easy design of the frame under combined vertical and horizontal loading while at the same time accounting for the effect of axial load. Figure 14 is an example of such curves as developed for the example frame. The nondimensional plots were produced by analyzing the two bounding frames of Fig. 10 under various combinations of loading throughout the range of possible ratios. The limiting cases for these loading combinations

or ratios are simply the case of no horizontal force (H = 0% of W) which produces the simple beam mechanism load and secondly, the case of no vertical force (β = 0) which produces the simple sway mechanism load. All other failure mechanisms will be produced by some combination of loads between these two extremes.

For each of the analyses within the above range, curves similar to those of Figs. 11 and 12 are produced. Picking the peak value of load for each curve and plotting non-dimensionally one-half the vertical "' load over P of one column against the horizontal load H over the simple sway mechanism load results in the curves of Fig. 14. The curves of Fig. 14 indicate the interaction between three quantities: the lateral load, the gravity load, and the section properties of the sections

used. With this plot a knowledge of any two of these will allow the determination of the third. If one of the two known quantities is the frame section properties, the procedure is a direct one. Knowing the section properties, G can be computed and consequently the proper curve in Fig. 14 can be picked. Either H/H_{sway} or 6 β H/P_{y} can be computed from the value of the known load, depending on which load is known. Hence, the point on the plot which indicates the maximum load the frame can sustain is defined by the fact that one of its coordinates is known and it must lie on a given curve.

To design a frame if only the values of the loads are known, it is necessary to pick a set of trial sections first. Knowing the loads and picking some trial section allows the proper curve (value of G) to be chosen and the coordinates of the point defined by the loads to be determined. The relative locations of the point and the curve indicate whether the trial frame has any reserve strength and if so, how much. With a small number of trials, it is possible to pick sections which will cause the point defined by the loads to fall very near the limiting curve. The closer the point falls to the curve the more efficient the frame will be under the given loading.

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The curves of Fig. 14 can also be used to predict the type of failure mechanism and the order of formation of the plastic hinges in each case. To do this it is only necessary to refer back to the loaddeflection plots which were used to produce the curves of Fig. 14.

and-error procedure.

6. SUMMARY

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A method for analyzing frames to determine their elastic-plastic load-deflection behavior has been presented. The method accounts for the weakening effect of axial force on the plastic moment capacity of the members. Both the method of analysis and the computer program which was developed to perform it are based on a method and a computer program developed by Wang and Harrison which neglects this axial force effect. The basic difference between the two methods lies in the fact that an analysis which includes the effect of axial force is non-linear while one which does not include it is linear. As a result of the nonlinearity involved, the method presented in this report uses a trial-

In order to use the reported program to analyze a frame, it is necessary to systematize the various groups of input information that are needed in the course of the analysis. The methods and systems used are explained in Chapter 3 and exemplified in Fig. 6 and appendix C. Typical program output is also given in Chapter 3 and an example run is contained in appendix C.

The two basic problems encountered in the use of the program have been discussed. They are: (1) Storage capacity, that is, how to make efficient use of available machine capacity and how to modify a given problem so that it requires less space in the computer.

(2) Change in the order of formation of plastic hinges during analysis.

The solution to the first difficulty consists of program and input data modifications discussed in Chapter 4. The second problem, that of hinge order reversal, arises from the trial-and-error procedure employed by the program. A detailed explanation and solution have been presented in Chapter 4.

The results of several analyses and some possible uses for the program in design have been presented. In particular, a method for producing a series of curves for a given frame which show; the interaction of frame gravity loads, lateral loads, and some parameters indicating frame properties have been shown.

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7. NOMENCLATURE AND PROGRAM SYMBOLS

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	Text	Program	Definition	
		A	Statics matrix.	
	A		Cross-sectional area.	
		AA	The increased capacity of the point in question.	
			(The x-axis intersection for the straight line	
÷	· .	· · ·	approximation to the interaction formula)	į į.
		ABC	Dummy variable used to read past unwanted sections	
9:			on tape.	
	m _{ii}	AM	Array of unit moments for each elastic frame	
:	÷		analyzed.	
	n ij	AN	Array of unit axial loads for each elastic frame analyzed.	
		ASAT1	Temporary storage array for one column of the	s.,
			matrix ASAT.	
		ASAT	Matrix A times matrix S times matrix A transposed.	

- ASM Subroutine which adjusts the stiffness matrix to account for the formation of the last plastic hinge.
- ATX Array used in the computation of the plastic hinge rotations.
- AX Total axial load at some point due to all increments of load on the frame.

Intermediate variable (no general definition).

The axial load at the point in question which results from previous increments of load on the structure.

Intermediate variable (no general definition). Cumulative axial load at a point.

The axial load at the point in question which results from increments of load being applied to the structure after a plastic hinge has formed at the point.

	Text	Program	Definition	
	. • •	CM	Moment at a point in the frame.	
	M pc	СРМ	Reduced plastic moment capacity.	
<u> </u>		CX	An array of the deflections in the frame at the	
<u>.</u>			formation of a plastic hinge.	
		CXX	Identical to CX.	
		D	Intermediate variable (no general definition).	
		DATA	Subroutine which inputs new frame data.	
	Mi	DD	The moment induced at the point in question due to	
» · · · · ·			previous increments of load being applied to	
	:		the structure.	
		DE LTA P	Subroutine which computes the increment of load	
		· ·	required to form the next plastic hinge.	•.
		DM	Array used in the computation of the plastic hinge	•
			rotations.	
	E		Modulus of elasticity.	
	EAOL	EAOL	Matrix which stores the value of EA/L for each	
			frame member.	•.
	m ij	EE	The unit moment for the point in question for this	

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increment of load.

Ratio of column stiffness to beam stiffness.
A function of the unit axial load for this increment at the point in question.
Horizontal load.

Sway mechanism load.

Counter. Moment of inertia.

Point being investigated for being the next hinge to form.

Number of the location on the frame where the next <u>a</u> plastic hinge is known to have formed or is currently assumed to be forming.

ICYC Cycle number in the trial and error procedure used to find the next increment of load.

Text	Program	Definition
h	IH	Number of the plastic hinge being investigated.
	II	Switching parameter used in subroutine deltap.
	INDEX	Switching parameter which controls where the main
		program goes after control leaves a subroutine.
	IORD	Matrix which records the order of the plastic hinge
		formation.
	IP1	Counter.
b	IPT	Number of the point currently under investigation.
	IT1	Tape number.
	IT2	Tape number.
	IXZ	Index which controls the printing of intermediate
· .		results in subroutine DELTAP.
	J	Counter.
JJ	JJ	Frame number.
	K	Counter.
KK	KK 🔍	Load set number.
	KZ	One less than the number of the hinge currently
		under investigation.
T.	Ť.	

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Degrees of freedom in the frame. ł Length. LDSET Subroutine which inputs the loads. LOWEST Subroutine which picks the next plastic hinge. LP1 Frame degrees of freedom plus one. Twice the number of members in a frame. M,a Μ MATRIX Subroutine which performs an elastic analysis of a frame. MM One less than twice the number of members in a frame. Three times the number of members in a frame. N N Number of frame members. NM NM NPASS Switching parameter which causes the stiffness and statics matrices to be printed at the beginning 2 of each new frame analysis. NPH The number of the location where the next plastic hinge occurs.

Text	Program	Definition
	OUTPUT	Subroutine which prints out a table of information
		summarizing the conditions in the frame after
	·	the formation of each plastic hinge.
	P	Increment of load.
	PHR	Subroutine which computes and prints the internal
		rotations undergone by each plastic hinge at
		collapse load.
· .	PL	Matrix of the applied loads.
M _D	PM	Matrix of the plastic moment capacities for all the
L		frame members.
	РОРҮ	Ratio of P to P _y at a point.
ê tişkiri kir	PP	Final computed load required to form a plastic hinge
		at some location.
	PT	Matrix which stores the value of the load to form
		a plastic hinge at some location for each of
		several tries.
P y	PY	Matrix of the yield loads for all frame members.

RAX Axial load at a point due to loads applied to the structure after a plastic hinge forms at the point. RM Induced moment at a point. RR Axial load at a point due to one increment of load applied after a plastic hinge appears at the point. Radius of gyration. r x RZ Moment induced at a point due to one increment of load. S Stiffness matrix. SAT Matrix S times matrix A transposed. SAT1 Temporary storage array for one column of the matrix.SAT. SAX Axial load at a point due to loads applied to the structure before a plastic hinge forms at the

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point.

<u>Text</u>	Program	Definition
	SB	Intermediate variable (no general definition).
	SC	Intermediate variable (no general definition).
SDAT	SDAT	Matrix which stores the value of EI/L for each
		frame member.
	SS	Axial load at a point due to one increment of load
•		applied before a plastic hinge appears at the
		point.
	TEMP	Temporary variable name.
•	UNDEFL	Subroutine which computes the unit deflection, moments, and axial loads.
	UX	Array of unit deflections for each elastic frame
	- <u>-</u>	analyzed.
W		Vertical load.
β		The ratio of a beam point load to the side load.
		(For the example frame).
${\sf A}_{\mathbf{H}}$		Horizontal deflection.
δ_{H}		Unit horizontal deflection.

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$ \begin{array}{c} \mathbf{Y}_{1} \\ \mathbf{Y}_{2} \\ \mathbf{Y}_{3} \\ \mathbf{Y}_{3} \\ \mathbf{Y}_{4} \\ \mathbf{Y}_{5} \\ \mathbf{Y}_{3} \\ \mathbf{Y}_{4} \\ \mathbf{Y}_{5} \\ \mathbf{Y}_{5} \\ \mathbf{Y}_{5} \\ \mathbf{Y}_{6} \\ \mathbf{Y}_{6} \\ \mathbf{Y}_{6} \\ \mathbf{Y}_{7} \\ \mathbf{Y}_{7} \\ \mathbf{Y}_{8} \\ \mathbf{Y}_{9} \\ \mathbf{Y}_{10} \\ \mathbf{Y}_{11} \\ \mathbf{Y}_{12} \\ \mathbf{Y}_{10} \\ \mathbf{Y}_{10} \\ \mathbf{Y}_{12} \\ \mathbf{Y}_{10} \\ \mathbf{Y}_{11} \\ \mathbf{Y}$			•	м ₁	M_2	м ₃	M ₄	м ₅ .	м ₆	м ₇	M ₈	м ₉	M ₁₀	P.1	P_2	P_3	P ₄	P 5
		1		- 0	0	2/2	2/2	0	0	0	0	0	0	1	0	* 0	0	ο
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	V	1 2		0	0	-2/2	-2/2	1/2	1/१	0	O	0	0	0	0	0	0	0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	» h	1 ₃		0	0	0	0	-1/१	-1/2	2/L	2/2	میرد O	0	0	0	0	0	0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	W	1 4		0	0	Ο	0	0	Ó	-2/2	-2/L	Ö	Ö	0	0	° 0	0	1
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	W	1 5		1/2	1/2	Ō	0	Ο	0	0	0	0	0	0	-1		0	0
	Ŵ	6	j	0	0	0	0	0	0	0	Ο	0	0	0 /	1	=1	0	ρ
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		7 7		0	0	0	0	0	0	0	0	0	0	0	0	1	-1.	0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	K	1 8		0	0	0	0	Ö	0	0	0	1/2	1/2	0	0	Ô	1	0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	K	1 ₉		0	1	1	Ο	0	Ο	Ø	O	0	0	Ö .	0	0	0	0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	i na secondaria da secondari	1 10		0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
$W_{12} \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1$	Ŵ	7 11		0	0	Ö	0	0	1	1	0	0	0	0	0	0	0	0
$w_{5} \xrightarrow{w_{2}} w_{2} \xrightarrow{w_{3}} w_{4}$ $w_{5} \xrightarrow{w_{2}} w_{10} \xrightarrow{w_{1}} w_{12}$ $w_{10} \xrightarrow{w_{1}} w_{12}$ $Uoad Numbering and Sign Convention$ $Member Numbering$	W	12		0	0	0	0	0	0	0	1	1	0	0	0	0	0	0
	الموافقة والموافقة و والموافقة والموافة والموافقة وافقة وافقة وافقة وافقة والموافية والموافية والموافية والموافية وا	· · ·	₩5	W9	T Lo	ad Num ign Co	bering nvention	and n		ч.	1.	, I		mber 1	۶ آ		£12 € €	9

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TABLE 2 MATRIX OF APPLIED LOADS (PL)

 W_1 0 W₂ -1 W₃ -1 W_4 0 W₅ 1 W₆ 0 W₇ 0 W₈ 0 W₉ 0

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TABLE 3 SEQUENCE OF INPUT DATA

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•

		INPUT ITEM(S)	FORTRAN	FORTRAN II	1
a".	1			<u>r Unria I</u>	
in an	а	Frame No.	KK	I 5	
Analysis of First		Degree of Freedom and number of members Statics Matrix	L, NM A	2 I 5 7 F 10.4	
Frame	t trong	Section Properties	SDAT PM EAOL PY	4 F 10.4	
		Load Set Number	KK	I 5	
	Load .	Load Matrix	PL	7 F 10.4	
	Applied to	Load Set Number	КК	I 5	
<i>v.</i>	First	Load Matrix	PL	7 F 10.4	
	Frame	Load Set Number (negative)	KK	I 5	
		Frame No.	KK	I 5	
Analysis of Second	·····	Degree of Freedom and number of members	L, NM	2 I 5	
Frame		Statics Matrix	A	7 F 10.4	
	-	Section Properties	SDAT PM EAOL PY	4 F 10.4	
e e e e e e e e e e e e e e e e e e e		Load Set Number	КК		· · · · · · ·
	Load Applied	Load Matrix	PL	7 F 10.4	
	to	Load Set Number	KK	I 5	
	Second	Load Matrix	PL	7 F 10.4	
		Load Set Number (negative)	КК	I 5	
	· · · · · · · · · · · · · · · · · · ·	Frame No. (negative)	JJ	I 5:	1
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TABLE 4 PROGRAM OUTPUT SEQUENCE

ITEM	COMMENT
1. Frame Number	Printed on the top of the first page for identification purposes.
2. Statics Matrix	Listed for reference and checking (to insure correct punching of input data.)
3. Member Stiffness Matrix	Created internally from section properties. Listed for reference and checking.
4. Load Set Number	Listed for identification.
5. Load Set	Listed for reference and checking.
The following four iter the failure mechanism	ms are repeated in sequence until is formed.
6. Unit Deflections Unit Moments Unit Axial Loads	Produced by each elastic analysis of the frame.

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7. Number and locat- ion of plastic hinge	Values of each load increment for each trial, as well as the totals for each trial are also output for examination here.
8. Table	The total moment, M_{pc} , M_{p} , axial load, P_{y} , and the ratio P/P_{y} are listed for each member end in the frame.
9. Deflections	The value of the deflection for each of the "L" degrees of freedom in the frame is computed and listed.
 After the failure load produced.	is reached the following item is
10. Hinge Rotations	The internal rotations undergone by each plastic hinge are listed.
If additional load sets again with item 4. If frames do, item 1 will	are to be run, the output begins no load sets remain, but additional appear next. If nothing remains to

be run, the machine will exit from the program.

TABLE 5 SECTION PROPERTIES LISTED BY RADIUS OF GYRATION

L	SECTION	HADIUS LE GYRATICA	UCHENT UF	PLASTIC MODILLS	ARFA	UEPTH n	SECTION	PADIUS OF Gyfation Fx	MONENT OF INENTIA IX	PLASTIC MCLUES	ARFA	DEPTH
)						-						· · · · · · · · · · ·
	31 7	4.15	2.0	7. 3	2.17	3.00	104F 25:	1.26	1 3 2 3	26 . B	1 15	10.00
	31 6	1.28	2.5	1.9	1.64	3.00	1 AWE 39	4.27	200.7	47 0	41.48	J-0 - 108
·.	4 T ¹ 9	1.56	6.7	4.0	2.70	4.00	10WF 29	1.29	157.3	34.7	11.40	10.22
•:	4 () d	1.04	6.5	3.5	2.21	4.00	10WF 45	4.53	248.6	55.0	13.24	10.12
	4M 13	1.65	10.4	6 . 1	3.82	4.00	10WF 54	4.39	305.7	67.1	15.46	10.12
	4 WH 1 3	1.72	11.3	6.3	3.82	4.16	10H 19	4 4 1	96.2	21.6	5.01	10.25
	5 1 1	1.6/	15.0	7.4	4.29	5.00	10WF 60	4.41	343.7	75.1	17.66	10.25
	51 10	2.15	12.1	5.6	2.47	5.00	10WF 66	4.44	382.5	82.8	19.41	10.38
	514 1-0	2.08	23.8	11.1	5.50	5.00	10WF 72	4.40	420.7	91.7	21.JP	10.50
	2WF [0	- 10	<1.5	9.0	4.70	5.00	10WF 77	4.44	451.2	91.7	22.67	10.62
		2 . 1 C	15.A	」] _↓ .4	5.45	5.12	121 50	4.55	311.6	60.7	14.57	12.00
	6 10 4	2.20	€ 0.⊪li 7	10.5	2.02	0.00	104F 89	4.55	542.4	114.4	26.10	10.88
	4 T 1 3	2.007	7.0	2.0	1.50	0.00	JEJR 12	4.5/	72.2	14.3	3.45	12.00
		2 • 4 D	41.H	H . 4	3.61	6.00	10WF100	6.61	625.N	130.1	29.43	11.12
	6H 22	् • भ C दिन्द से जे	41 0	2.5	3.73	6 • 0 0 6 · 0 0		4,65	105.3	20.6	4.86	12.00
	6M 25	2.53	4.7 0	170	7 16	6.00	121 35	4.72	227	14/.5	32.92	11+38
	614 20	2.5/	38.8	14.6	5.88	6.00	101 41	1.72	22/.0	44.4	10.20	12.00
	6B 16	2 50	31 7	4 4 2	4 70	6.00		4 • / / A 11 1	268.9	52.5	11.94	12.00
	OWF 24	2 • 5 2 2 • 6 0	41 7	11.0	5 GH	6 20		• • 0,⊥ Z 0,7	100.1	24.8	2.02	12.16
:	71 20	2.60	41.0	14.4	5.83	7.00	121 22	4.85	215.8	41.6	9.26	12.00
	6WF 25	6.04	53.5	19.0	7.37	6.37	12WF 27 b	500	214.1	29.4	0.4/	12.31
	7.JR 5	2.14	1.2. 1	4.0	1 61	7.00	12wF 31 5	5.11	236.4	44 0	0 12	12 00
	71 15	2.00	30.2	11.9	4.43	7.00	12WF 40	5.13	310 4	5.7 /	7.0 ± 5	
	81 23	3.09	64.2	19.2	6.71	8.00	12WF 30	5,15	28.6 8	51.4	10 30	12 24
	8 JR 5	3.12	16.7	5.4	1.92	8.00	12WF 45	5.15	350.8	54.9	1.5 24	12.00
	PB 13	3.21	39.5	11.4*	3.83	8.00	12WF 50	5.18	304 5	72.6	4 4 71	12 10
	AM 120	3.22	60.7	17.4	- 5.44	8.00	1241 53	5.23	420.2	78.2	15.59	12.06
	8M 22	2.23	68.3	19.7	6.01	8.00	12WF 50	5.20	476.1	86.5	17.00	12.19
	8T 18	3.26	46.9	16.3	5.34	8.00	12WF 19	5 (4	003 0	110 4	23 22	10 30
	88 115	3.24	48.0	13.6	4.43	8.12	12WF 85	5.78	723.3	129.1	24.98	12.50
	8M 28	3.31	90.1	25.6	8.23	00.8	148 17 5	5.40	147.3	24.7	5.05	14.00
	AM 17	3.35	56.4	15.7	5.00	8.00	12WF 92	5.41	788.9	140.2	27.96	12.62
	8WF. 17	3.36	46.4	15.8	5.00	8.00	12HF 99	5.43	858.5	151.8	29.09	12.75
	8M 18	3.30	62.1	17.4	5.44	8.00	12wF100	5.40	930.7	163.4	31.19	12.88
	- 8M (34	3.40	115.5	32.7	10.09	8.00	12wF12U	5. b1	10/1.7	186.4	35.31	13.12
	OWF124	3.42	62.5	23.1	1.06	7.93	14R 22 1	5.52	107.4	33.n	6.47	13.72
		3 • 4 D	49.7	19.1	5.88	R.14	1241133	5.59	1221.2	205.7	39.11	13.30
		7 45	A 5. A	23.3	1.06	P.00	148 26 3	5.63	242.6	39.9	7.65	13.89
		3,49	97.8	27.1	8.23	8.06	12WF1/1	5.70	1541.A	259.2	47.38	13.88
		2,49	117.8	51.6	9.59	H • C D	1447 SD 1	F. 73	5H0.6	47.1	8.41	13.86
	8WF340	3.55	146.3	34.7	11 76	8.12	101 00	D + 7 4	481.1	/.6.5	14.59	15.00
	BWF 48	7.61	183 7	46 0	14 11	0.29 H 50	1948F 43 *	► 87 6 99	425 n	69.7	12.65	13.68
	8WF 50	3.05	227.3	59.9	17.06	8.75	14WF 34	- 0 C	236 0	54 5	50.00 AU 00]4.5R
	BUE 67	2.71	271 B	7 8 1	40 70	0 00		5.50		24.5	10.00	14.00
	101 35	3.70	145 8	35.2	1.0.22	10.00	144F 38 5	F 87	245 Z	· //··›;	14.11	13.81
	10JR: 9	ь <u>к.85</u>	39.0	9.2	2.64	10.60	14WF 53	5.01	542 1	01.47 H7 1	45 20	14•12 ፣ 14 ዓም
	104 29	5.92	131.5	30.9	8.55	9.88	151 43	F 45	276 · 1 241 - 2	- 6	12.07	15 00
	108 15	1 3.95	6H . A	14.0	4.40	10.00	14WF 61	6 0h:	641 5	102 4	17 04	17.04
	108 17	\$ 4.05	H1.8	18.0	4.98	10.12	14WF 68	r . 112	724_1	114	20.00	14.06
••	101 25	4.07	122.1	28.0	7.38	10.00	144F 74	8 N.5	702 0	1.95 2	01 74	4 4 4 4 4
	10M 21	4.14	114.4	23.7	6.10	9.90	14. F 78	۴.۵۶	/ TD • F A51 22	134 = 0	22.04	14.19
	10WF 21	4.14	100.3	24.1	6.19	9.90	14WF 84	r.15	928 4	145/4	24.71	14.18
	100 233	6.10	116 6	26.5	6 73	0 0 0	1 445111	A 01	1046 6			

\$ CHECK SHAPES SO MARKED FOR COMPLIANCE WITH FORMULA (25), SECTION 2.6 OF THE AISC SPECIFICATION, WHEN SUBJECTED TO COMBINED AXIAL FORCE AND PLASTIC BENDING MOMENT AT ULTIMATE LOADING.

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•	SECTION				_								
	SECTION		RADIUS CF	MCMENT OF	PLASTIC	AREA	DEPTH	SECTION	RADIUS OF	MCMENT OF	PLASTIC		
	÷. ↓		GYPATION	INERTIA	HODULUS				GYRATION			ARFA	DEPTH
			~ X	<u> </u>	Z	A	D		EX.	TX TX	7		P
													U
	16H (26		6.24	20P.1	43.9	7.65	15.65	21WF 82	8.53	1750 4	104		
	14UF 97		6.20	1373.1	210.9	34.99	14.50	21WF 68 %	P.59	1479 3	191.6	24.10	20.86
	14WF 136		6.31	14/6.7	225.9	37.33	14.62	21WF 96	8.60	2028.0	226 7	20.02	21.1
	14WF142		6.32	1672.2	254.8	39.98	14.75	21WF 73 \$	8.64	1600.3	172.1	21.46	21.1
	14WF150		6.37	1786.9	270.2	44.08	14.88	21WF 112 24 WF 127	8.92	2620.6	278.0	32.93	21.0
	108 31	\$	6.39	372.5	53.8	9.12	15.84	21wF142	9.03	3017.2	317.8	37.34	21.24
	14WF358		6.40	1900.6	286.3	46.47	15.00	241 100	9.05	2374 0	35/.0	41.76	21.46
	14WF追わ/ 14WF増フト		6.42	2020.A	302.9	49.09	15.12	241 90	9.21	2230.1	205.8	29.25	24.00
	16WE36	*	6.4J 6.49	2149.6	321.3	51.73	15.25	241 120	9.20	3010.8	298.0	35.13	24.00
	14WF184		6.49	2274 8	03.9 777 6	10.59	15.85	241 80 \$	9.46	2087.2	203.0	23.33	24.00
1	14wF193		6.51	2402.4	355.1	56.73	17.38	24WF 68 5	9.53	1814.5	175.5	20.00	23.71
	14WF202		4.54	2538.8	373.6	59.39	15.63	241 100/ 244F 76 \$	9.73	2811.5	273.0	30.98	24.00
1	14WF211		6.56	2671.4	391,7	62.07	15.75	24WF 84 \$	9.00	2090.4	200.1	22.37	23.91
	14WF 219	4	6.59	2798.2	408.0	64.36	15.87	24WF 94 \$	9.85	2663.0	224.0	24.71	24.09
	16HF 58	.0	0.02 6.62	515.5	72.7	11.77	16.00	24wF100 \$	10.08	2987.3	278.3	29.43	24.29
	14WF228		6.62	2942.4	427.2	17.04	15.86	24WF110 \$	10.12	3315.0	307.5	32.36	24.14
	14wF320		6.63	4141.7	592.2	94.12	16.81	244120 \$	10.15	3635.3	336.6	35.29	24.31
	16WF 45	\$	6-64	583.3	82.0	13.24	16.12	244F13U 3	10.24	4009.5	369.2	38.21	24.25
	14WF 237		6.65	JURD 9	445.4	69.69	16.12	24WF145	10.34	4561.0	416.0	42.62	24,49
	164F 50	*	C • D O	833.8	117.9	18.80	16.00	27 NF 84 \$	10.69	2824.8	463.7 243 0	47.04	24.72
`	1411F246		6.68	025.4 3228 0	92.7	14.70	16.25	27WF 94 \$	10.87	3266.7	277.7	27.45	20.09
	181 50		6.70	917.5	123.8	20.46	10.25	7WF102 \$	11.96	3604.1	304.4	30.01	27.07
1	16WF 71		4.70	936.9	131.6	20.86	16 16	27WF114 \$	11.03	4080.5	342.8	33.53	27.22
l	16 WF 78		6.74	1042.6	145.5	22,92	16.32	27WF145 %	11.26	5414.3	452.0	42.68	26.88
~	14WF204		6.74	3526.0	512.4	77.03	10.50	27WF177	11.36	0018.6 6726000	504.5	47.04	27.06
:	16WF AA		* 6.81 4 H7	3912.1	551.6	P4.37	16.81	30WF 99 %	11.7.0	3988.6	312 0	52.1U 29 11	27.31
	14WF 314		6.90	4390 4	169.0	25.87	16.16	30WF108 \$	11.85	4461.0	345.5	31.77	20.82
	164F.96		6.93	1355 4	196 0	92.30	17.19	30WF116 %	12.00	4919.1	377.6	34.13	30.00
د ۱	14 NF 342		6.99	4911.5	673.0	70.27 NU 50	16.32	30WF124 \$	12.11	5347.1	407.4	36.45	30.16
	181 55		7.01	795.5	103.5	15.94	18.00	30wF172 %	12.48	5753.1'	436.7	38.83	30.30
	1425371) 1445264		7.18	5454.2	737.3	08.78	17.94	30WF190 \$	12.57	1825 Q	793.U	50.65	29.88
	14WF470		7.26	0013.7	803.0	16.98	18/31	304F210	12.64	9872.4	733.9	61.7A	30.12
	1 HWF 45	D	7.30	704 =	004.3	27.25	18.69	33WF118 \$	13.02	5886.9	414.3	34.71	32.86
i	18 WH 50	Ð	7.38	804.5	100.8	13 24	17.86	33WF130 \$	13.23	6699.0	466.0	38.26	33.10
	18WF 55	b	7.41	889.9	111.0	16.19	18.12	33WF141 3	13.39	7442.2	513.2	41.51	33.31
}	184F 64	b	7.40	1045.8	131.8	18.80/	17.87	33WF200 6	13.71	H147.6	558.3	44.71	33.50
٠	18WF 20	r	7.47	984.0	122.6	17.64	18.25	33WF220 \$	13.79	12312 4	724.4	50./9	33.00
	18WF 77		7.54	1286 9	144.7	20.56	18.00	33WF240	13.88	13565.1	918.2	70.52	33,25
1	18WF 45		7.5/	1429.9	17/.6	22,00	18.16	36WF135 b	14.01	7796.1	509.1	39.70	35.55
	2n1 45		7.59	1500.7	192.0	27.74	20.00	36WF150 F 36WF160	14.29	9012.1	574.H	44.16	35.84
	<ut 75<="" td=""><td></td><td>7.60</td><td>1203.5</td><td>151.5 /</td><td>21.90</td><td>20.00</td><td>36WF170 \$</td><td>14.4/</td><td>9/38.6</td><td>623.3</td><td>47.19</td><td>36.00</td></ut>		7.60	1203.5	151.5 /	21.90	20.00	36WF170 \$	14.4/	9/38.6	623.3	47.19	36.00
			7.79	1674.7	206.0/	28.22	18.16	3611F182 \$	14.52	ш,џч/((,U) 1,10,81 è	DDC • /	49.98	36.10
			/•/5 7.7H	1852.5	226.5	30.86	18.32	36WF194 %	14.50	12103.4	/10.9	53.54 57 11	36.32
	18WF 1:14		7.74	1901.7	1//.3	24.80	20.00	36#F230 %	14.80	14988.4	942.7	67.75	30.48 35.88
	66 105		7.85	1109.5	137.3	33.51 19.08	18.48	36WF245 #	14.95	16092.2	1018.0	72.03	36.06
į	21wf 55 3	,	8.40	1140.7	125.4	16,18	20.80	36 10 26 1 K	15.00	17235.A	1)76.0	76.56	36.24
			à -	· · · · ·					15.12	18410 7			

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Axial Force Effects



Fig. 3 Interaction Curves



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Schematic Plot Indicating Successive Trials for Fig. 4 the Determination of a Second Plastic Hinge













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•••• Fig. 7 Freebody of the Upper Left Column Top on the Example Frame

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F.

(E)

111



The quantity in parenthesis indicates the length . 5 of the second segment on the load-deflection plot for the frame.

Fig. 8 Change in the Order of Formation of Plastic Hinge

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5

STRONG BEAM-WEAK COLUMN

G = 0.5Уь

r_b

ø

r c

X c

rc

40

55

6

WEAK BEAM-STRONG COLUMN



40

60

• · · *

Fig. 9 Possible Bounding Cases for the Construction of the Example Frame

STRONG BEAM-WEAK COLUMN

4



56

STRONG COLUMN-WEAN BEAM



~~~ 111

Fig. 10 Bounding Frames







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(A)



• •

δ<sub>H</sub> = f (H)

•

 $\delta_{H} = f(H, W)$ 

59



# Fig. 13 Effect of Frame Symmetry on Unit Horizontal Deflection





## APPENDIX B PROGRAM LISTINGS

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 2182, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, JRR, RM, NPH, CAX, POPY, CPM, INDEX, II EQUIVALENCE (A(1), ASAT(1), AM(1)), (A(166), AN(1)), (S(295), DM(1 1)], [S[309], ATX[1]], [S[1], SAT[1], UX[1], PY[1]], [S[15], PM[1]] 2. [S[391], PT[1]], [S[49], [ORD[1]], [S[57], PP[1]], [S[71], P[1]], 3[S[323] GXX[1]], [PL[1] GM[1]], [SDAT[1], CX[1], SAT1[1], ASAT1[ 41]] DIMENSION A(15,21), S(21,21), SDAT(7), EAOL(7), PL(15), PM(14), 1PY[14], CX[15], CM[14], SAT[21,15], ASAT[15,16], PP[14], UX[15,8], 2SATX[28], AM[15,11], AN[15,11], IORD[8], P[8,40], PT[40], DM[14], 3ATX[14], GXX[15], SAT1[15], ASAT1[15] 90 CALL DATA GO TO 199, 871, INDEX 87 CALL LDSET GO TO 1 907 911, INDEX 91 CALL MATRIX GO TO 1 90, 106, 1.1. INDEX 1 CALL UNDEFL GO TO 1100, 106, 981, INDEX 100 CALL DELTAP GO TO 8 985 99, 108, 112, 871, INDEX 108 CALL LOWESP GO 90 1 106, 100), INDEX 112 CALL OUTPUT CALL ASM GO 70 91 106 CALL PHR GO TO 87 98 PRINT 96 96 FORMAT (48HNONSENSE TEST RESULT---- INDEX VALUE IN ERROR, 1

99 CALL EXIT

PAGE 1

END

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: 1 1 PAGE SUBROUTINE DATA -COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 218Z, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II EQUIVALENCE (A(1), ASAT(1), AM(1)), (A(166), AN(1)), (S(295), DM(1 1)], (S(309), ATX(1)), (S(1), SAT(1), UX(1), PY(1)), (S(15), PM(1)) 2, [S[391], PT[1]], [S[49], [ORD[1]], [S[57], PP[1]], [S[71], P[1]], 3(S(323), CXX(1)), (PL(1), CM(1)), (SDAT(1), CX(1), SAT1(1), ASAT1( 41]] DIMENSION A(15,21), S(21,21), SDAT(7), EAOL(7), PL(15), PM(14), 1PY[14], CX[15], CM(14], SAT(21,15], ASAT(15,16], PP[14], UX[15,8], 25ATX[21], AM(15,11), AN(15,11), JORD(8), P(8,40), PT(40), DM(14), 3ATX(14), CXX(15), SAT1(15), ASAT1(15) С READ THE FRAME NUMBER, EXIT IF NEGATIVE C C 9 READ 13, 4J 13 FORMAT [15] IF (JJ) 88,5,5 88 INDEX = 1 RETURN 5 REWIND 2 REWIND 3 **REWIND 4** C READ DEGREES OF FREEDOM AND NUMBER OF MEMBERS С С READ 23. L, NM 23 FORMAT [215] NM ¢ NM 2

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د: س

| | SUBROUTINE LDSET | |
|---------|--|--|
| | COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, K
1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, | K, |
| | 218Z, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, | |
| | 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II | |
| | EQUIVALENCE [A[1], ASAY[1], AM[1]], [A[166], AN[1]], [S[29>], D | M[1 |
| | 11,0 [S[907], A A[]], [S[], SA[], VA[1], PY[1], [S[12], PM[| 1)) |
| | $2 \cdot [3[39]]_0 P[[1]]_0 [3[49]_0]URD[1]_0 [3[57]_0 PP[1]]_0 [3[71]_0 P[1]_0 P$ |]]) |
| | AIII
AIII | 124 |
| | THENSION AI15,211, SI21,241, SDATI71, FADI (7), PI (15), PM (14), | |
| | 1PY(14), CA(15), CM(14), SAT(21.15), ASAT(15.16), PP(14), UX(15) | 81, |
| | 25ATX121], AM115,11], AN(15,11), PORD(8), PIB.40], PT(40), DM(14 | 14 |
| | 3ATX (14) / CXX (15), SAT1 (15) / ASAT1 (15) | |
| | | |
| | READ THE LOAD SET NUMBER. IF IT IS NEGATIVE, READ A NEW FRAME | |
| | NO,,. | |
| | | |
| | 708 READ 13, KK | |
| | 13 FORMAT [19] | ······································ |
| | IF [KR01]09, 81, 81 | × |
| | OF THE A T | · ` |
| | RETURN | |
| | SET ALL THE ELEMENTS OF THE STIFFNESS MATRIX TO ZFRO | · |
| | 81 DO 160 I # 1,N | |
| | DO 160 J = 1,N | |
| | 160 S[[,J] = 0. | |
| | REWIND 2 | |
| | | |
| | REWIND D | |
| | REWIND 3 | |

-64

REAU IAPE 2. ADL READ TAPE 2, ABC READ TAPE 2, [SDAT[1], I = 1, NM] READ TAPE 2, (EAOLII), I # 1, NM] C CONSTRUCT THE STIFFNESS MATRIX FROM KNOWN DATA C Č DO 161 I # 1.M. 2 K = 1/2 + 1 SII.II = 4.0 + SDATIK) S[1010101] = S[1.1] Stio1, 1 0.5 . Sti.I) 161 S[], [\$4] 0 S[]\$4,1] DO 11 V 2 MM, N JojoM 11 S(P,I) = EAOL(J) C IF NPASS IS POSITIVE, C PRINT OUT TITLES, THE STATICS MATRIX, AND THE STIFFNESS MATRIX C C 100 - 10 g - 10 g IF [NPASS] 707, 82, 82 82 PRINT 97, JJ . E

С

C С

97 FORMAT [18HIANALYSIS OF FRAME, I3, //] PRINT 7 7 FORMAT [19HOTHE STATICS MATRIX//] DO 1 181,L 1 PRINT 21, 10 [A[[, J]0 J010N] 21 FORMAT(4HOROW, 13, 1%, 7616, 7/(8×,7616,7)) PRINT 17 17 FORMAT (23H1THE STIFFNESS MATRIX//] DO 2 801.N 2 PRINT 81, 8 (S[1, J], J=1, N] NPASS 5 -1 707 PRINT 27, KK 27 FORMAT (13HILOAD SET NO., 13) READ IN AND PRINT OUT THE LOAD SET. READ 39, [PL[I], I=1,L] 35 FORMAT (7F10.4) DO 3 191.L 3 PRINT 21, 1, PL(I) IH s Û WRITE PAPE 2, (PL(I), I = 1, L) WRITE TAPE 2, ((S(1, J), I = 1, N), J = 1, N) INDEX # 2

RETURN

END

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1

SUBROUTINE MATRIX

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IHa IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 218Z, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II EQUIVALENCE [A[1], ASAT[1], AM[1]], [A[166], AN[1]], [S[295], DM[1 1)], [S[309], ATX[1]], [S[1], SAT[1], UX[1], PY[1]], [S[15], PM[1]] 2, [\$[391], PT[1]], [\$[49], SORD[1]], [\$[57], PP[1]], [\$[71], P[1]], 3[5[323], GXX[1]], [PL[1], CH[1]], [SDAT(1], CX[1], SAT1[1], ASAT1[41]] DIMENSION A[15,21], S[21,21], SDAT[7], EAOL[7], PL(15], PM(14], 1PY[14], CX[15], CM[14], SAT[21,15], ASAT[15,16], PP[14], UX[15,8], 2SATX[21], AM[15,11], AN[15,11], IORD[8], P[8,40], PT[40], DM[14], **3AT**×[14], G××[15], SAT1[15], ASAT1[15] **15** IM B [H + 4 IF (1H/2 · 2 · 1H) 67, 68, 92 92 INDEX 8 1 RETURN 67 IT1 = 3 172 = 4 GO TO 69 68 171 = 4 172 = 3 CONSTRUCT THE MATRIX SAT I S TIMES A TRANSPOSED! LALL THE FOLLOWING MATRIX OPERATIONS STORE THEIR INTERMEDIATE RESULTS ON TAPE.] 69 DO 97 1 ≅ 1, N DO 20 J=1.L SA71(J) = 0. DO 20 K91.N

| | EU SAILIUJ - SAILUJ - SIIJKJ VALUJKI | | |
|---------------------|---|--------------------------------|--------------------------------------|
| . W | 57 WRITE PAPE IT1, [SAT1[II], II # 1, L] | | |
| с, <u>,</u> | REWIND IT1 | | |
| | | · · | |
| | | | |
| \$ | DE REAU TAPE ILLO (SATIIOJ) JA 10 LI SATING | | |
| | REWINDITS | | |
| | WRITE PAPE IT1, [[SAT[I,J], I = 1, N], J= 1, L] | | |
| С | | | |
| C CC | INSTRUCT THE MATRIX ASAT IA TIMES & TIMES A TRANSPOSED! | | |
| C | | | |
| • | | | |
| | | V | •••••••••••••••••••••••••••••••••••• |
| | | | |
| | DO 40 K=1.N | | |
| | ASAT1[J] = 0. | | |
| | 40 ASATI[J] = ASATI[J] +A[I,K] + SAT[K,J] | | |
| | 63 WRITE TAPE IT1, LASATILIII, IT = 1, LI | | |
| | | | |
| | | | |
| | NEAD TAPE LILD ABU | | |
| | | | |
| 4 | 04 READ YAPE YY1, LASAT [I, J], J= 1, L] | مستنبه ومعارب عروا عرام فالم ع | |
| | REWIND IT1 | | |
| | READ TAPE IT1, ABC | | |
| · · | LP1=L+1 | 1. 1. 1. 1. | • |
| +9 = + <u>−</u> 2 ° | | | |
| • | | | |

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SOLVE THE EQUATIONS FOR THE UNIT DEFLECTIONS

DO 60 1810L IP18101 TEMPOABSF (ASAT(1,1)) Kat DO 61 JoloL'

50 ASATII, LP11 = PLIT

IF [AB8F[ASAT[J, 1]]-TEMP] 61,61,62

62 Køj

TEMP & ABSF (ASAT (J. 1)] 61 CONTINUE .

IF (K-1) 72,71,72 72 DO 45 JOIOLP1

TEMP = ASAY(1,J)

ASATELOJI & ASATEK.JI

45 ASAT(K, J) & TEMP 71 IF CASATCIJI 16,147,16

147 PRINT 547

347 FORMAT (30HODIVISION BY ZERO IN INVERSION)

INDEX 0 2 RETURN

16 TEMP = 1./ASAT(I,I)

DO 70 JEIOLP1

70 ASATII, JIGASATII, JI+TEMP DO 60 J=1.1

IF [1-1] 99,60,59 59 TEMPOASAT(J, 1)

DO 80 KOIP1, LP1

80 ASATIJOKIBASATIJ,KI-TEMP+ASATII,KI

60 CONTINUE

INDEX 9 3 RETURN END

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SUBROUTINE UNDEFL

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 2IBZ, AA, BB, CC, DP, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, GAX, POPY, CPM, INDEX, II EQUIVALENCE (A(1), ASAT(1), AM(1)), (A(166), AN(1)), (S(295), DM(1 1J), (S(309), ATX(1)), (S(1), SAT(1), UX(1), PY(1)), (S(15), PM(1)) 2, (S(391), PT(1)), (S(49), IORD(1)), (S(57), PP(1)), (S(71), P(1)), 3(S(323), GXX(1)), (PL(1), GM(1)), (SDAT(1), CX(1), SAT1(1), ASAT1(41)) DIMENSION A(15,21), S(21,21), SDAT(7), EAOL(7), PL(15), PM(14), 1PY(14), CX(15), CM(14), SAT(21,15), ASAT(15,16), PP(14), UX(15,8),

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2SATX[21], AM[15,11], AN[15,11], IORD[8], P[8,40], PT[40], UX[15,8], 3ATX[14], GXX[15], SAT1[15], ASAT1[15]

ADD A COLUMN TO THE UNIT DEFLECTION MATRIX

PRINT 511
511 FORMAT [17H1UNIT DEFLECTIONS]
KZ s [H = 1
IF (IH = 19 92, 74, 73
73 READ TAPE IT2, LUXII, J], I = 1, L], J = 1, KZ]
74 DO 51 [S10L
UXII, JH] © ASAT(I, LP1]
UXII, JH] © ASAT(I, LP1]
WRITE TAPE IT1, LUXII, J], I = 1, L], J = 1, IH]
REWIND IT1
READ TAPE IT1, L(SAT(I, J), I = 1, N), J = 1, L]
READ TAPE IT1, ABC

CHECK TO SEE IF THE DEFLECTIONS EXCEED AN ARBITRARY MAXIMUM LIMIT

IF THEY DO; SAY SO AND GO ON TO COMPUTE THE HINGE ROTATIONS С С DO 311 1=1,1 TEMP B ABSPIASATII, LP11] - 1.E+02 IF [YEMP] 311,647,647 311 CONTINUE GO 70 903 647 PRINT 047 847 FORMAT (21HODEFLECTION TOO LARGE) INDEX 0 2 RETURN COMPUTE AND PRINT UNIT MOMENTS AND AXIAL LOADS С ALSO ADD COLUMNS TO THE UNIT MOMENT AND UNIT AXIAL LOAD MATRICES Č IF THE VALUE OF THE MOMENT COEF IS BELOW A GIVEN VALUE, SET IT TO С ZERC. C 303 DO 120 I=1,N 1 · · · SATX[] = 0. · · · · · · · · · · DO 120 K=17L 120 SATX[I]=SATX[I]+SAT[I,K]+ASAT[K,LP1] PRINT 522 3

```
522 FORMAT [13H1UNIT MOMENTS]
    IF [IH = 1] 92, 76, 75
75 READ TAPE IT2, ((AMEI, J), I = 1, M), J = 1, KZ)
    READ TAPE 172. (CANES.J. I = 1. MJ.J = 1.KZ)
76 DO 94 1 = 1, M
    PRINT 21, 1, SATXITI
21 FORMAT (4HOROW, 13, 1×, 7E16.7/(8×,7E16.7))
    IF ( SATX(1) 56, 94, 56
56 IF [ABBF[SATX[]]] - .001] 54, 54, 94
54 SATA189 = 0.
    PRINT 95, 1
55 FORMAT (24x, 14HUNIT MOMENT AT, 13, 1X, 11HSET TO ZERO)
94 AMILOSHI & SATXINI
   PRINT G
 6 FORMAT (17HOUNIT AXIAL LOADS)
   DO 93 2 & MM. N
   K i i o M
    J = 2 0 K
   PRINT 10, K, SATXIII
10 FORMATE7HOMEMBER, 13, 1X, 816.71
   ANIJOIHI O SATXIII
95 AN(J-101H) & SATXII)
   WRITE PAPE ITL, ((AM(I,J), I = 1, M),J = 1, IH)
   WRITE PAPE IT1, LLANLI, JJ, I = 1, MJ, J = 1, INJ
   REWIND 2
   II n 1
   INDEX 0 1
   REPURN
92 INDEX 8 3
   RETURN
   END
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| A STATE OF A DESCRIPTION OF A DESCRIPTIO | تحجره محذوقات والمحاولات وأركدت سمار الزكر فأو وعكرت للمحر والمترك أردوا والمدراء تسادين وتحصيصا ومحاولات وملولا المحار بمراجعه | المرجوب والمرجوب والمرجوب المرجوب والمرجوب والمحافظ والمحافظ والمرجوب والمرجوب والمرجوب والمحاصر والمحاف والمرجور الم | وأحجاز وتقصيح فأشبع ومرود وأبناه بمسائد بمارا وبالمتحد والمتقاوية ومحمدان والتراجع والمراجع | assisting and a so in running as indian fait the second of the | والمروانية والمروانية والمحالية والمستحدين وستعتز أراد الرمار المتاريقين والما | وجمع المحجم والمعطر الارتباط المحموم فالغالم أأترك ويستأثر تورد خالف جيعتها أرتب والمريبا فلمريبا حجاج المخ | יין אין אין אין אין אין אין אין אין אין | |
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| | SUBROUTINE DELTAP |
|-----------------------|--|
| | PLACE THE FOLLOWING QUANTITIES IN COMMON STORAGE SO THEY WILL BE
AVAILABLE TO ALL SUBROUTINES, |
| ~ | COMMON A, S, SDAT, EAQL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK,
1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC,
2IBZ, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX,
3RR, RM, NPH, CAX, POPY, CPM, INDEX, II |
| | THE FOLLOWING EGUIVALENCE STATEMENTS RESULT FROM THE USE OF
Tapes. No two variables or arrays which are equivalenced to one
another are ever needed at the same time: |
| • | EQUIVALENCE [A[1], ASAT[1], AM[1]], [A[166], AN[1]], [S[295], DM[1
1]], [S[309], ATX[1]], [S[1], SAT[1], UX[1], PY[1]], [S[15], PM[1]]
2, [S[391], PT[1]], [S[49], IORD[1]], [S[57], PP[1]], [S[71], P[1]],
3[S[323], CXX[1]], [PL[1], CM[1]], [SDAT[1], CX[1], SAT1[1], ASAT1[
41]] |
| C
C
C | DIMENSION THE FULLOWING ARRAYS, |
| 2 | DIMENSION A[15,21], S[21,21], SDAT[7], EAOL[7], PL[15], PM[14],
1PY[14], CX[15], CM[14], SAT[21,15], ASAT[15,16], PP[14], UX[15,8],
2SATX[21], AM[15,11], AN[15,11], IQRD[8], P[8,40], PT[40], DM[14],
3ATX[14], CXX[15], SAT1[15], ASAT1[15] |
| С
С
С
С
С | IF CONTROL IS COMING FROM THE SUBROUTINE WHICH PICKS THE LOWEST
VALUE OF LOAD TO FORM THE NEXT HINGE, GO DIRECTLY TO STATEMENT
31 AND REPRODUCE THE PREVIOUS RESULTS. IF CONTROL IS COMING FROM
UNDEF LIF UNIT DEFLECTIONS AND FORCES HAVE JUST BEEN COMPUTED.] |
| Ċ | AND THEREFORE IF THE NEXT PLASTIC HINGE HAS NOT YET BEEN LOCATED. |

C GO TO 1 110, 31), II С THE FOLLOWING 6 STATEMENTS RETURN CONTROL TO THE MAIN PROGRAM TO DETERMINE WHAT MEANING THE THREE VALUES OF INDEX WILL CONVEY TO THE MAIN PROGRAM, REFER TO THAT PROGRAM, C C C C 107 INDEX = 1RETURN 109 INDEX = 2 RETURN 111 INDEX = 4 RETURN C PROM TAPE, READ THE DATA REQUIRED FOR THE COMING SERIES OF C C COMPUTATIONS. C 110 READ TAPE 2, ABC ÷ READ TAPE 2, [PM[I],] = 1, M] READ TAPE 2, [PY[I],] = 1, M] tris i stist IXZ # 1 ÷ С . 1 (-. 2 .• 2 0 :1

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C

C

IF IH IS ONE, THE ARRAYS IORD AND P HAVE NOT BEEN USED YET AND HENCE CANNOT BE READ IN. IF [IH - 11107, 77, 78 78 READ TAPE IT2, [IORD[I] , I = 1, KZ] * READ TAPE IT2, (PLIPT, 1), (PT = 1, KZ) BEGIN LOOP TO DETERMINE THE NEXT INCREMENT OF LOAD 77 DO 28 1A # 1, M IF THE MOMENT GOEFICIENT IS ZERO AT A GIVEN POINT, SET THE VALUE OF P AT A HIGH VALUE AND BEGIN THE LOOP AGAIN. IZERO MOMENT COEFFICIENT INDICATES THAT EITHER A PLASTIC HINGE HAS ALREADY FORMED AT THE POINT OR ELSE BY COINCIDENCE, THE COEFF. IS ZERO AND THEREFORE A PLASTIC HINGE SIMPLY WILL NOT FORM AT THIS POINT DURING THIS INCREMENT OF LOAD. IF LAMEIA, 1411 31, 32, 31 32 PPIIA] = 1000. GO TO 28 INITIALIZE THE CYCLE NUMBER. 31 ICYC = 0INCREMENT THE CYCLE NUMBER. 24 ICYC = ICYC + 1 SET THE TOTAL LOAD FOR THE CYCLE TO ZERO AT THE START.

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PAGE

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PPT = 0.
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IF THIS IS THE FIRST CYCLE, USE THE LAST TRY FOR THE PREVIOUS
               HINGE AS A FIRST GUESS.
               THE VARIABLE KZ IS ONE LESS THAN IH.
         C
         C
               OTHERWISE, START AT THE BEGINNING LAT THE BOTTOM OF THE LOAD
         C
               DEFLECTION CURVES
         C
IF LICYC . 11107, 83, 84
                  83 IPT = KZ
                                                      . . . . . . . .
                     GO TO 22
                  84 IP7 = 0
        C
        C
               IF 40 CYCLES HAVE BEEN COMPLETED WITHOUT CONVERGENCE, SAY SO AND
               REDC THAT PARTICULAR LOOP, PRINTING AS EACH VALUE IS FOUND.
        C
              CALL EXIT WHEN THIS HAS BEEN DONE.
        C
                     IF (ICVC - 40) 22, 22, 4
                  4 PRINT B. IA
                  8 FORMAT [4H1PT., IS, 1X; 17HWILL NOT CONVERGE //]
                    IF (1X2) 5, 107, 42
                 42 IXZ 8 91
                    GO TO 31
                                                                                        £)
                                 . .
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C

C

C C

CC

C

C

INCREMENT THE POINT NUMBER.

22 IPT = 1PT + 1

REFERING TO STATEMENT LABELED 12 BELOW, IT CAN BE SEEN THAT THE QUANTITIES AA, BB, CC, DD, EE, AND GG ARE THE MAJOR VARIABLES INVOLVED IN THE DETERMINATION OF THE LOAD INCREMENT PLIPT, ICYCJ, I THE VARIABLES O AND Q ARE USED ONLY TO INDICATE SIGN.J WHERE® -72

3.

PAGE

AA = THE INCREASED CAPACITY OF THE POINT IN QUESTION. (THE X-AXIS INTERSECTION FOR THE STRAIGHT LINE APPROXIMATION TO THE INTER-ACTION FORMULA.]

BB = THE AXIAL LOAD AT THE POINT IN QUESTION WHICH RESULTS FROM PREVIOUS INCREMENTS OF LOAD ON THE STRUCTURE.

CC = THE AXIAL LOAD AT THE POINT IN QUESTION WHICH RESULTS FROM INCREMENTS OF LOAD BEING APPLIED TO THE STRUCTURE AFTER A PLASTIC HINGE HAS FORMED AT THE POINT.

DD = THE MOMENT INDUCED AT THE POINT IN QUESTION BUE TO PREVIOUS INCREMENTS OF LOAD BEING APPLIED TO THE STRUCTURE. EE = THE UNIT MOMENT FOR THE POINT IN QUESTION FOR THIS INCREMENT

OF LOAD, GG = A FUNCTION OF THE UNIT AXIAL LOAD FOR THIS INCREMENT AT THE POINT IN QUESTION.

THE FOLLOWING TESTS DETERMINE WHERE ON THE LOAD DEFLECTION CURVE THE PRESENT COMPUTATIONS LIE AND CONSEQUENTLY WHETHER OR NOT EACH OF THE VARIABLES ABOVE HAS SOME VALUE OTHER THAN ZERO. ALSO, THE TESTS SERVE TO DETERMINE WHETHER THE POINT IN QUESTION IS A KNOWN PLASTIC HINGE OR WHETHER THE PROGRAM IS JUST TESTING THE POINT TO SEE IF IT IS THE NEXT PLASTIC HINGE:

IF [IPT - 1]107, 116, 117 116 IF [IH+1]107, 118, 119 118 CC = 0. BB = 0.DD = 0. IBZ = IAGO TO 121 119 BB = 0. DD 🕫 O. GO TO 122 _ **117 SB = 0.** KK S IPT-1 IF [IH - IPT] 107, 101, 102 101 IBZ = 1A GO 70 103 102 IBZ= IORD(IPT) 103 DO 123 J 9 1, KK B = P[J.ICYC]+AN[IBZ.J] 123 SB 8 SB + R BB = SB + 1.18 + PM(IBZ) / PY(IBZ) DD z 0, DO 124 J # 1, KK D = P[J,ICYC] + AMIIBZJJ

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PAGE 4

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124 DD = DD + D 122 IFIICYC=11109, 126, 125 125 IF []H-]PT] 107, 126, 127 126 CC 🛛 0. IF (IH - IPT)107, 104, 105 104 IBZ B YA GO 70 121 105 IBZ = YORD FIPTI GO 70 121 127 SC 💷 0, KK 18 807 + 1 IBZ = IORD(IPT) ٦. DO 128 J 4 KK. IH C B P[JoIGYC=1]+AN[IBZ]J] 128 SC & SC + C CC I SC & 1.18 * PM(IBZ) / PY(IBZ) ÷. *7 121 AA 0 1.18 0 PMIIBZ] EE O AM(102, 1PT) GG 🗉 1.18 🗢 PM(IBZ) + AN(IBZ, 1PT) / PY(IBZ) IF THE UNIT MOMENT AT THE POINT HAS A DIFFERENT SIGN THAN THE MOMENT THAT HAS BEEN INDUCED PREVIOUSLY AT THIS POINT, THE VARIABLE & ALTERS THE EQUATION FOR PIIPT, ICYCI SO THAT THE QUANTITY DD WILL PROVIDE ADDITIONAL MOMENT CAPACITY AT THE POINT RATHER THAN LESS AS IS THE USUAL CASE. IF (DD/EE) 6, 7, 7 6 6 GO TO 11 7 Q 🕫 1. IF THE UNIT AXIAL LOAD AT THE POINT HAS A DIFFERENT SIGN THAN THE PREVIOUS AXIAL LOAD AT THE POINT, THE QUANTITY O ALTERS THE EQUAT

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FOR PLIPT, ICYCI SO THAT THE MOMENT CAPACITY AT THE POINT WILL
C
C
       BE INCREASED.
C
           11 IF . ( [. BB. + CC. ]/ GG. ] . 9. 10 . 10
            90 8 01,
               GO TO 12
           10 0 a 1.
C
       COMPUTE THE VALUE OF THE INCREMENT OF LOAD.
C
Ċ
           12 PIPT, ICYCJ # [AA=ABSF[BB + CC]+0 - ABSF[DD]+Q]/[ABSF[EE]+ABSF[GG
             1]]
С
        BEGIN CHECK TO SEE IF AXIAL LOAD REDUCTION IS WARRENTED.
       FIRST, COMPUTE THE AXIAL LOAD AT THE POINT UNDER CONSIDERATION.
C
       TWO CONTRIBUTIONS ARE CONSIDERED. THE AXIAL LOAD SAX DUE TO
PREVIOUS INCREMENTS OF LOAD AND RAX DUE TO LATER INCREMENTS OF
C
С
       LOAD.
C
              SAX = 0.
              DO 129 J # 1, IPT
                                                                     yn er er er stat 🖉 annan af eine eine er en han in samten at angentaat samtenaar.
              SS = ANLIBZ, JJ + PLJ, ICYCI
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| | 129 SAX = SAX + SS | |
|----|---|--|
| | RAX = 0.
IF(IH=1)107, 36, 131 | |
| | 131 IFIICYC-11107, 36, 37 | |
| | 37 IF(IH-1PT)107, 36, 38 | |
| | | |
| | $\mathbf{R} = \Delta \mathbf{N} [1 \mathbf{R} 7, 1] = \mathbf{P} [1, 1 \mathbf{C} \mathbf{Y} \mathbf{C} \mathbf{-1}]$ | |
| | 39 RAX B RAX & RR | |
| | 36 AX = SAX + RAX | |
| | | |
| | NEXT, SEE IN PAPY IS GREATER THAN .15. IF IT IS, SKIP THE NEXT | |
| | TO FORM THE NEXT HINGE NEALECTING THE EFFECT OF AVAILAD | |
| | to the the treat is the inderesting the Ericui of AxIAC COAD. | |
| | IF (ABSF [AA]/PY[IBZ]=,15] 41, 230, 230 | |
| | 230 IF (IXZ) 132, 232, 232 | |
| | | |
| | IF[[PT01]]07, 44, 43
43 KK = 107 = 4 | |
| -, | | |
| | RZ = AM[IBZ,J] + P[J,ICYC] | |
| | 133 RM B RM + RZ | |
| | | |
| | THIS TEST DETERMINES WHETHER THE SIGN OF THE MOMENT HAS CHANGED | |
| | AND IF IN HAS, THE INCREMENT OF LOAD IS COMPUTED AS IF THERE HAD | |
| | CREASE AS USUAL. | |
| | | |
| | IF [RM/AM(18Z0 \$PT)] 48,107, 44 | |
| | 48 PIIPT, ICYCI = [PM[IBZ] + ABSF[RM]] / ABSF[AM[IBZ, IPT]] | |

GO TO 49

4 P[IPT01CYG] = [PM(IBZ] - ABSF[RM]]/ ABSF[AM(IBZ, IPT]]

49 IF (IX2) 231, 232, 232

IF THE AXIAL LOAD AT THE POINT IS LESS THAN ,15 PY PRINT THIS ON THE CUTPUT IF IXZ IS NEGATIVE. [THE VALUE OF IXZ DETERMINES WHETHER OR NOT INTERMEDIATE RESULTS WILL BE PRINTED. IF IXZ IS POSITIVE, PRINTING WILL BE SUPPRESSED. IF IT IS NEGATIVE PRINTING WILL OCCUR.]

231 PRINT 46, IPT

46 FORMAT L23HNO REDUCTION FOR HINGE , 121

PRINT THE VALUE OF THE NEXT INCREMENT OF LOAD.

132 PRINT 135, IPT, ICYC, PLIPT, ICYC) 135 FORMAT (24P1, 12, 14, 12, 44) 0, F10.4, //]

IF THE VALUE OF THE INCREMENT OF LOAD HAS TURNED NEGATIVE, THIS INDICATES THAT THE AXIAL LOAD AT THE POINT HAS BUILT UP TO THE POINT WHERE THE HINGE WILL NOW FORM AT A LOAD LESS THAN THE PREVIOUS PLASTIC HINGE FORMED AT IN OTHER WORDS, THERE HAS BEEN A CHANGE IN THE ORDER OF FORMATION OF THE PLASTIC HINGES IN THE FRAME, [THIS IS NOT TO INDICATE THAT IF THE FRAME WERE TESTED THE

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PAGE HINGES WOULD FORM IN A DIFFERENT ORDER, IT IS JUST THAT FOR THE C PURPOSES OF THE ANALYSIS, THE ORDER HAS CHANGED.] C C 232 IF (P(IPToICYC)) 1, 79, 79 1 IF (1P7 - 1) 107, 32, 2 2 PRINT 5 3 FORMAT [27HIABORT, HINGE ORDER CHANGES] C C TERMINATE THIS RUN. C 5 INDEX # 5 RETURN C IF THIS IS THE FIRST PLASTIC HINGE TO FORM IN THE FRAME, ONE TRY C WILL PRODUCE AN EXACT VALUE FOR THE LOAD INCREMENT. THEREFORE C CHECK THE NEXT LOCATION ON THE FRAME. C OTHERWISE, GO ON TO THE NEXT LEG ON THE LOAD DEFLECTION CURVE. C 79 IF [IH - 11107, 14, 18 14 PPLÍAL # PÉIPT, ICÝČI GO TO 233 18 PPT = PPT & P(IPT, ICYC) IF (1H - 107)107, 19, 22 19 PTIICYCI C PPT CHECK THE QUANTITY IXZ TO SEE IF THE RESULTS OBTAINED SHOULD BR PRINTED, THEY WILL BE PRINTED IF 1] THE HINGE HAS BEEN PICKED AND THE COMPUTATIONS ARE BEING REDONE SO THEY MAY BE LISTED, OR 2) IF CONVERGENCE COULD NOT BE OBTAINED. IF (1X2) 34, 52, 52 34 PRINT 93, PPT 33 FORMAT L 27%, 20HTOTAL FOR THIS CYCLE, F10.4, ///)

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52 IF NICYC - 11107, 24, 25 C IF THE DIFFERENCE BETHEEN THO SUCESSIVE VALUES OF THE TOTAL LOAD REQUIRED TO FORM A PLASTIC HINGE IS LESS THAN SOME ARBITRARY С QUANTITY, CONSIDER CONVERGENCE OBTAINED. OTHERWISE DO THE COMPUTATION AGAIN. C 25 IF [ABSF[PT[ICYC =]] = PT[ICYC]] - .001] 234, 234, 24 234 IF (IXZ) 235, 26, 26 235 PRINT 238, IH 238 FORMAT [30HOCONVERSION OBTAINED FOR HINGE, I3] 26 PP(IA) = Priicyej 233 IF (1X2) 111, 20, 28 C GO BACK AND CHECK THE NEXT POSSIBLE PLASTIC HINGE LOCATION. C 28 CONTINUE INDEX = 3 RETURN END : r. . ; j ' · · · ·

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PAGE 1

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SUBROUTINE LOWEST

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IM, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 218Z, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II

EQUIVALENCE [A[4], ASAT[4], AM[1]], [A[166], AN[1]], [S[295], DM[1 1]], [S[309], ATX[1]], [S[1], SAT[1], UX[1], PY[1]], [S[15], PM[1]] 2. [S[391], PT[4]], [S[49], [ORD[1]], [S[57], PP[4]], [S[71], P[1]], 3[S[323], GXX[1]], [PL[1], CM[1]], [SDAT[1], CX[1], SAT1[1], ASAT1[41]]

DIMENSION A(15021), S(21021), SDAT(7), EAOL(7), PL(15), PM(14), 1PY(14), CA(15), CM(14), SAT(21015), ASAT(15,16), PP(14), UX(15,8), 2SATX(21), AM(15,11), AN(15011), IORD(8), P(8,40), PT(40), UM(14), 3ATX(14), CXX(15), SAT1(15), ASAT1(15)

PICK THE SMALLEST VALUE OF THE LOAD P. DETERMINE THE LOCATION OF THE NEXT PLASTIC HINGE.

| | AA = 1000. | • |
|-----|--|-----|
| | IF [] = 1] 1, 1, 2 | |
| 2 | ITEMP S NPH | |
| 1 | DO 236 I # 1, M | |
| 237 | IF (AA - PP(1)) 236. 239. 230 | |
| 239 | AA = PP(I) | |
| | NPH B 🖞 | |
| 236 | CONTINUE | |
| | IF [ITEMP - NPH] 3, 4, 3 | |
| 4 | PRINT 5 | · • |
| 5 | FORMAT [24H1SAME HINGE PICKED TWICE 1 | |
| | INDEX = 1 | |
| | RETURN | |
| 3 | | |

IA B NPH C PRINT OUT THE LOCATION DECEIDED ON FOR THE NEXT HINGE AND GO BACK C C AND RECALCULATE THE QUANTITIES ASSOCIATED WITH THIS POINT PRINTING AS EACH RESULT IS OBTAINED. C ing in Second 3. С PRINT 242, IH, NPH 242 FORMAT [18H1PLASTIC HINGE NO., I3, 4X, 13HFORMED AT PT., 13,//] II = 2INDEX = 2 RETURN END ۰. λ.

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PAGE 1

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SUBROUTINE OUTPUT

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IM, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 218Z, AA, 88, CC, DD, EE, 8, S8, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II

EQUIVALENCE [A[1], ASAT[1], AM[1]], [A[166], AN[1]], [S[295], DM[1 1], [S[309], ATX[1]], [S[1], SAT[1], UX[1], PY[1]], [S[15], PM[1]] 2, [S[391], PT[1]], [S[49], [ORD[1]], [S[57], PP[1]], [S[71], P[1]], 3[S[323], GXX[1]], [PL[1], GM[1]], [SDAT[1], CX[1], SAT1[1], ASAT1[41]]

DIMENSION A(15,21), S(21,21), SDAT(7), EAOL(7), PL(15), PM(14), 1PY(14), CA(15), CM(14), SAT(21,15), ASAT(15,16), PP(14), UX(15,8), 2SATX(21), AM(15,11), AN(15,11), IORD(8), P(8,40), PT(40), DM(14), 3ATX(14), GXX(15), SAT1(15), ASAT1(15)

ADD ANOTHER ELEMENT TO THE IORD MATRIX (THIS MATRIX KEEPS TRACK OF THE ORDER IN WHICH HINGES HAVE FORMED,]

240 LORD(IH) © NPH WRITE TAPE IT1;[IORD(I]; I = 1; IH] WRITE TAPE IT1; [PIIPT; ICYC]; IPT = 1; IH] PRINT OUT A TABLE GIVING THE VALUES OF TOTAL MOMENT; MPC; PLASTIC MOMENT; AXIAL LOAD; PY; AND THE RATIO OF AXIAL LOAD TO PY FOR EACH POINT ON THE FRAME;

PRINT 241 241 FORMAT (4H1PT., 3X, 9HTOT. MOM., 6X, 3HMPC, 10X, 2HMP, 7X, 8HAX. LOAD, 6X, 22HPY, 10X, 4HP/PY,//) DO 247 1 8 1, M CM(1) 8 0. CAX 0 0.



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249 FORMAT ( 4HOPT., 4X, 10HDEFLECTION,//)
    DO 251 I # 1. L
CXIII # 0:
    DO 250 J 8 1, IH
250 CXIII @ CXIII + PIJ.ICYCI + UXII.JI
251 PRINT 2520 1. CX[1]
252 FORMAT ( 13, E16.7.//)
    WRITE PAPE ITA (CXII) " I . LI
   READ TAPE 2, ABC
                                     .
   READ TAPE 2, ABC
   READ TAPE 2. [PL(I) . I . 1.L]
   READ TAPE 2, [[S[], J], I = 1, N], J = 1, N]
   BACKSPACE 2
   REWIND 3
   REWIND 4
   RETURN
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SUBROUTINE ASM

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 218Z, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II

EQUIVALENCE (A(1), ASAT(1), AM(1)), (A(166), AN(1)), (S(295), DM(1 1)], [\$[309], ATX[1]], [\$[1], SAT[1], UX[1], PY[1]], [\$[15], PM[1]] 2. [\$[301], PT[1]], [\$[40], [ORD[1]], [\$[57], PP[1]], [\$[71], P[1]], 3(S(323), GXX(2)), (PL(1), CM(2)), (SDAT(1), CX(1), SAT1(1), ASAT1(41]]

DIMENSION A[15,21], S[21,21], SDAT[7], EAOL[7], PL[15], PM[14], 1PY(14), CA(15), CM(14), SAT(21,15), ASAT(15,16), PP(14), UX(15,8), 25ATX[21], AM(15,11), AN(15,11), IORD(8), P(8,40), PT(40), DM(14), 3ATX(14), GXX(15), SAT1(15), ASAT1(15)

ALTER THE STIFFNESS MATRIX TO ACCOUNT FOR THE FORMATION OF THE LAST PLASTIC HINGE.

IF ((NPH/2 0 2) - NPH] 211, 210, 210 210 S[NPH-1, NPH-1]=0.75+S[NPH-1, NPH-1] S[NPHONPH] B D. S(NPH-10NPH) D 0. S(NPH,NPH-1) 0 0. GO 70 212 211 S[NPH+1,NPH+1] = 0.75+S[NPH+1,NPH+1] S[NPHONPH] 3 0. S(NPHONPHOL) C 0. SINPHO1,NPH) . O. 212 WRITE TAPE 2, [[S[], J],] = 1, N], J = 1, N] REWIND 2 READ TAPE 2, [[A[I,J],] 🔻 🐛 Lj, Nj 🛎 1, Nj RETURN

END

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SUBROUTINE PHR

COMMON A, S, SDAT, EAOL, PL, L, NM, M, N, MM, I, J, K, NPASS, KK, 1JJ, IH, IT1, IT2, ABC, LP1, IP1, TEMP, KZ, IXZ, IPT, IA, ICYC, 2IBZ, AA, BB, CC, DD, EE, B, SB, D, SC, C, GG, SAX, SS, RAX, AX, 3RR, RM, NPH, CAX, POPY, CPM, INDEX, II

EQUIVALENCE (A(1), ASAY(1), AM(1)), (A(166), AN(1)), (S(295), DM(1 1), (S(309), ATX(1)), (S(1), SAT(1), UX(1), PY(1)), (S(15), PM(1)) 2. (S(301), PT(1)), (S(49), (ORD(1)), (S(57), PP(1)), (S(71), P(1)), 3(S(323), GXX(1)), (PL(1), CM(1)), (SDAT(1), CX(1), SAT1(1), ASAT1(41))

DIMENSION A(15,21], S(21,31), SDAT(7), EAOL(7), PL(15), PM(14), 1PY(14], CA(15), CM(14), SAT(21,15), ASAT(15,16), PP(14), UX(15,8), 2SATX(21), AM(15,11), AN(15,11), IOHD(8), P(8,40), PT(40), UM(14), 3ATX(14), GXX(15), SAT1(15), ASAT1(15)

MATRIX.]

RE-ENTRY POINT FOR THE COMPUTATION OF PLASTIC HINGE ROTATIONS.

47 PRINT 408 408 FORMAT (30HOCOLLAPSE MECHANISM HAS BEEN REACHED) REWIND 2 REWIND 1T2 READ TAPE 2, [[A[1,J], I = 1, L], J = 1, N] READ TAPE 2, ABC READ TAPE 2, ABC READ TAPE 2, iSDAT (I], I = 1, NM] DO 06 I = 1, 6 86 READ TAPE IT2, ABC READ TAPE IT2, [CM[I], I = 1,M] READ TAPE IT2, [CM[I], I = 1, L]

DO 163 I = 1,M DO 163J 🕯 1, M $163 S[1_0] = 0.$ DO I = 1, M, 2 164 · · 01] = 1.0/[3.0 + SDAT[K]] SII S[1020101] [S[1,1] S[10101] 0 00.5+S[1.1] 164 S[1090] 3 S[1.1+1] DO 134 1 0 1, M DO 134 KE17M 134 DM(1) O DM(1) + S(I,K) + CM(K) DO 136 1 0 1, M ATXII 3 0. DO 136 Ka1.L 136 ATXII] = ATXII] + AIK, I]+CXXIK] C PRINT OUT THE ROTATIONS AT EACH POINT. C . PRINT 138 138 FORMAT (16HOHINGE ROTATIONS) PRINT 53 :, :

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53 FORMAT [4H0PT.,4X,8HR0TATION,//] DO 139 I= H B DMEIJ & ATXIIJ 139 PRINT 252, 1, H 252 FORMAT [13, E16.7, //]

RETURN VO THE READ IN POINT FOR KK TO SEE IF THERE ARE ANY MORE LOAD SETS.

RETURN END

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APPENDIX C ANALYSIS OF THE EXAMPLE FRAME

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INDEXING SYSTEMS FOR THIS EXAMPLE



DEFLECTION AND LOAD NUMBERING





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- Member Numbers

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- Member End Numbers

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| .a. | KUW 15 | j e | 0.
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0.4588000E 05 | 0. | | .0 .
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> 0.1890012E UG. 0. n.9453060E 05 0∴ n . υ. n.1890612E Vo 0. 0.9453060E 05 0. £È•. i: 0• 0• ∏.. 0... 0 • 0 • 0. 0. n.1890610E 06 N. 0 • 0 • 1°...

0. n. 0. U. 0. 0. .ñ.. 0. 0 • 0 • 0. 0.1670400E 06 . 40•• О. Л.

0. 0. 0• 0•8352000E 05 υ. Γ. 0. 0. ∩. ∩.1070400È 00 0. 0. 0• n• U:• (••

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|--------------------|-------------|---------------------|-----------------|---|
| | LOAD SE | I NO. 3 | | |
| | FOW 1 | -0.2080000 | E N2 | |
| | K0W 2 | - N • 4 1 6 0 0 N 0 | E 01 | |
| | FOW 3 | -0.4160000 | F :0:1 | ^ |
| | ROW 4 | -0.2080000 | - 02 | |
| | HOW 5 | 0 • 1 0 0 0 0 0 0 E | <u>.</u>
1.1 | |
| | ROW 6 | n. • | | |
| | FOW 7 | 0. | | |
| | POW 8 | Ń. | | |
| (| Eow ∞o | 0. | | • |
| | FOW 10 | 0. | | |
| | 60W 11 | Ŋ. | | - |
| | FOW 12 | 0. | | |
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| | <u>ELFCIICNS</u> |
| HOW 1 | -0.5390036E-n3 |
| RUW 2 | -0.2523466E-n2 |
| FOW 3 | -0.2391322E-02 |
| ₩0₩ 4 | -n.5490522E-n3 |
| 60W 5 | 0 • 9 9 8 3 0 7 9 E - n 3 |
| KOW 6 | 0.9883555E+n3 |
| FOW 7 | 0.9684507E-03 |
| HOW B | 0.9584983E-n3 |
| ROW 9 | -0.2731933E-n3 |
| FOW 10 | -0.2040362E-n3 |
| FOW 11 | 0.2094626E-03 |
| KOW 12 | 0.2237525E-03 |
| UNIT MOM | ENTS |
| FOW 1 | -0.1738613E 01 |
| FOW 2 | -0.8198105F 01 |
| FOW 3 | 0.8198104E nj |
| MOW 4 | 0.2127302E n2 |
| ROW S | -0.2127302F N2 |
| FOW 6 | 0.1781527E n2 |
| HOW 7. | -0.1781527E n2 |
| ROW 3 | -0-1511361E 02 |
| KOW 9 | 0.1511361E n2 |
| ROW 10 | 0.9823117F n1 |
| UNIT AXIA | LOADS |
| MEMBER 1 | -0.2472948F 12 |
| MEMBER 2 | -n.166245nF n1 |
| MEMBER 3 | -0.1662449F n1 |
| MEMBER 4 | -0.16624475 n1 |
| MEMBER 5 | -0.2519052E 02 |

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PLASTIC HINGE NO. 1 FORMER AT PT. A

P[1,1] = 16.0349

| | <u>FT.</u> | TOT. MOM. | MFC | MP | AX. LOAD | PY |
|-----|----------------|--------------|------------|------------------|---|----------|
| | 1 | -27.87R | 244.592 | 402.000 | -396.535 | P25.840 |
| | 2 | -131.456 | 246.592 | 402.000 | ÷396.535 | 825.840 |
| | 3 | 131.456 | 1071.000 | 1071.000 | -26.657 | 1503.360 |
| • | 4 | 341.111 | 10/1.000 | 1071.000 | -26.657 | 1503.360 |
| | 5 | -341.111 | 10/1.000 | 1071.000 | -26.657 | 1503.360 |
| • · | 6 | 285.666 | 10/1.000 | 1071.000 | -20.657 | 1503.360 |
| 5 | 7 | -285.000 | 10/1.000 | 1071.000 | -20.657 | 1503.360 |
| | 8 | -242.345 | 10/1.000 | 1071.000 | -26.657 | 1503.360 |
| | 9 | 242.345 | 242.345 | 402.000 | -403.927 | 825.840 |
| | 10 | 1:57.513 | 242.345 | 402.(100 | -403.927 | 825.840 |
| | TOTAL | DEFLECTIONS | AT THIS ST | AGE. | | |
| | F1. | DEFLECTION | | | | |
| | 1 - | 0.8642870E-0 | 2 | | , | i |
| | 2 • | 0.4046353E-0 | 1 | | * | |
| | 3 - | 0.3834462E-0 | 1 | 6 | 10 - 10 - 10 - 10 - 10 - 10 - 10 - 10 - | |
| | 4 - | 0.8803999E-0 | 2 | | | л. |
| | 5 | 0.1600777E-0 | 1 | | | • |
| | 6 | 0.1584818E-0 | 1 | | 4: | |
| | 7 | n.1552901E-0 | 1 | | 1 9 - | |
| | 8 | n.1536943E-0 | 3 | | | : |
| | 9 - | 0.43P0628E-0 | 2 | | | : |
| | 10 - | 0.3271700E-0 | ? | | 1 | |
| | 11 | A.33-8713E-0 | 2 | I | | j. |
| | 12 | 0.3587849E-0 | 2 | • | | |
| | | | | •. | | i: |
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P/PY 0.480 U.480 **0.18**

U.018 0.018 U.U18 v.018 0.018 u.489 0.489

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| | - |
| UNIT DEFLECTIONS | PLASTIC HINGE NO. 2 FORMER AT RT 10 |
| HOW 1 -0.54594806-83 | P(2, 1) = 3.5718 |
| KOW 2 -0.3662038E-02 | |
| KOW 3 -0.3712537E-02 | |
| ROW 4 -0.5421078E-03 | P[1,2] = 14.3100 |
| 0W 5 0+4017866F-02 | P[2,2] = 5.3361 |
| OW 6 0.4014089E-02 | TOTAL FOR THIS CYCLE 19.640 |
| 0W 7 0.4006534E-02 | P[1, 3] = 137 40580 |
| Q₩' 8 0.4002757F=02 | |
| (QW 9 - A-4576735F-A3 | |
| | |
| 40W 11 0+3150363E=03 | P[1,4] = 13.0371 |
| NW 12 0.4765678E 03 | P[2, 4] = 6.6380 |
| | TOTAL FOR THIS CYCLE 19.67 |
| NIT MOMENTS | |
| OW 1 0.8178591F 01 | |
| CW 2 -0.2642825E 01 | |
| OW 3 0.2642824E n1 | TOTAL FOR THIS CYCLE 19.679 |
| OW 4 0.2921788E n2 | Pl 1 6) = 12.7266 |
| 0W 5 -0+2921788E 02 | P[2,6] = 6.9556 |
| (OW 6 0.3053930F n2 | TOTAL FOR THIS CYCLE 19.682 |
| 0W 7 -0.3153930E 12 | |
| OW 8 -0.4768372E-06 | Pl 1. 7 J = 12.6759 |
| UNIT MCMENT AT 8 SET 10 ZERO. | P.(2, 7) = 7,0075 |
| | TOTAL FOR THIS CYCLE 19.683 |
| UW 1n 0.9464278E n1 | PL 1. AJ = 12.6508 |
| INT AXIAL LOADS | P(02) 8) = 7.0331 |
| темвен 1 - 0.2004809E 0.2 | TOTAL FOR THIS CYCLE 19.683 |
| EMBER 2 -0.6309566E 00 | |
| EMBER 3 -0.6309533E 00 | CONVERSION OBTAINED FOR HINGE 2 |
| TEMBER 4 -0.6309786E 00 | |
| 1EMBER 5 -0.24871915 02 | |

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| | <u>PT.</u> | TOT. MOM. | MPC | MP | AX. LOAD | PY |
|---|------------|----------------------|---------------|---------------------------------------|--|----------|
| . k | 1 | 35.526 | 193.472 | 402.000 | -489.014 | 825.840 |
| | 2 | -122.300 | 193.472 | 402.000 | -489.014 | 825.840 |
| | 3 | 127.300 | 1071.000 | 1071.000 | -25.469 | 1503.360 |
| | .4 . | 4/4.613 | 10/1.000 | 1071.000 | -25.469 | 1503.360 |
| | 5 | -4/4.013 | 10/1.000 | 1071.000 | -25.469 | 1503.360 |
| 1 | •0 | 440.163 | 10/1.000 | 1071.000 | -25.469 | 1503.360 |
| | 7 | -440.163 | 1071.000 | 1071.000 | -25.469 | 1503.360 |
| | 8 | -191/200 | 1071.000 | 1071.000 | -25.469 | 1503.360 |
| • | 9 | 191.20n | 191.834 | 402.000 | -493.607 | 825.840 |
| - | 10 | 191.834 | 191.834 | 402.000 | -493.607 | A25.840 |
| | <u>10</u> | AL DEFLECTIONS | AT THIS ST | AGE. | х
1 | ai a |
| • | <u>FT.</u> | DEFLECTION | 1 | · · · · · · · · · · · · · · · · · · · | 2007 - 20 | |
| | ٤1 | -0.1065854E-0 | 1 | | • | |
| | 2 | -0.5767935E-0 | 1 | | ************************************** | 1 |
| | 3 | -0.5636279E-0 | 1 | | i
4
.1 | |
| 6 | 4 | -0.1075865E-0 | 1 | | - | |
| ÷ | 5 | 0.4088741E-0 | 1 | | | |
| | 6 | 0-4073493E-0 | '1 ' c | | | |
| | 7 | 0.4042999E-0 | 1 | | | |
| (| 8 | 0.4027752E-0 | 1 | н.
Г | | 1 |
| | 9 | -0.6674977E-0 | 2 | 19 | | |
| ومالي والمحمدين | 10 | -0.4811488E-0 | 2 | | | -1 |
| | 11 | 0.#8 45552E-0 | Ż | | 1 | •1 |
| | 12 | 0.6182395E-0 | 2. | | 3 <u>14</u> | |
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| UNIT DE | FLECTIONS | | |
|-------------|-----------------|---------------------------|-----------------|
| ROW 1 | -0.5430028E-03 | 5
- | |
| FOW 2 | -0.3941991E-92 | |
1 |
| ROW 3 | -0.3915028E-02 | :i | i. |
| FOW 4 | -0.5450530E-03 | •
• | |
| KOW 5 | 0.5448868E-02 | · | |
| FON 6 | 0.5448868E-n2 | | |
| FON 7 | 0.5448868E-02 | | |
| RON 8 | 0.5448867E-02 | | , |
| RON 9 | -0.5150484E-03 | | ; |
| ROW 10 | -0.3369616E-n3 | | |
| ROW 11 | 0.3380688E-n3 | | |
| ROW 12 | 0.5049607E-03 | , | |
| UNIT NOM | IENTS | | |
| FOW 1 | 0.1358903E 02 | | r. |
| F0W 2 | 0.1411018E 01 | | |
| FOW 3 | -0.1411019E 01 | | :, |
| FON 4 | 0.3225827E n2 | | |
| 60W 5 | -0.3225827E n2 | | |
| HOW 6 | 0.3155276E 02 | | |
| FOW 7 | -0.3155276E N2 | | |
| RON 8 | -0.4768372E-06 | l
 | |
| KOW O | 0 . | at 1990 Style Bar ()
1 | D. O.E. IV ZERU |
| FOW 10 | 0. | | |
| UNIT AXI | AL LOADS | | |
| MEMBER | 1 -0.2491297E 0 | 2 | |
| MEMBER | 2 r.3814697E-0 | 5 | |
| MEMBER | 3 r.5245209E-0 | 5. | |
| -
Member | 4 -0.4673004E=0 | .4. | |

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| Ρ | LASTIC | HINGE | NO. | FORMER AT PT. 1 |
|---------|--------|--------------|--------|-----------------------------|
| P (| 3, 1] | = | 5.661 | |
| | | | | TOTAL FOR THIS CYCLE 5.661 |
| Ρĺ | 1, 2] | ± | 9.889 | 4 |
| P (| 2,21 | : = . | 6.433 | |
| Ρſ | 3.21 | - | 7.380 | |
| | 07 21 | ал
К. | | LOTAL FOR THIS CYCLE 23.703 |
| P (| 1, 3] | .2. | 9.344 | i. |
| PI | 2, 31 | F | 5.951 | |
| P (| 3, 3] | Ŧ | 8.013 | |
| | | | | TOTAL FOR THIS CYCLE 23.309 |
| Ρĺ | 1, 4] | Ē | 9,269 | |
| Ρl | 2, 4] | z | 5.644 | к. |
| P (| 3, 4) | = | 8.295 | e ² |
| | , | | | TOTAL FOR THIS CYCLE 23.209 |
| Ρί | 1, 9] | ÷, | 9.327 | |
| Ρl | 2, 9] | = | 5.243 | :
_ |
| Pſ | 3, 9] | H | 8.594 | |
| ،
مر | | | | TOTAL FOR THIS CYCLE 23.164 |
| Pl | 1,10] | = | 9.3299 | |
| P (| 2,10] | 2 | 5.2322 | |
| Ŕ(| 3,10] | = | 8.6019 | i. |

TOTAL FOR THIS CYCLE 23.1640

CONVERSION OBTAINED FOR HINGE 3

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6.1.4 0.3.7

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| <u>- ۲</u> | . TUT. MOM. | MFC | MP | AX. LOAD | PY |
|---------------|---------------------------|--------------|----------|----------|----------|
| 1 | 143.462 | 143.462 | 402.000 | -576.079 | 925 840 |
| | -78.178 | 143.462 | 402.000 | -576.079 | 825.840 |
| 3 | 78.178 | 10/1.000 | 1071.000 | -18.812 | 1503.360 |
| 4 | 026.031 | 10/1.000 | 1071.000 | -18.812 | 1503.360 |
| 5 5 | -628.831 | 1071.000 | 1071.000 | -18.812 | 1503-360 |
| . 6 | 597.415 | 1071.000 | 1071.000 | -18.812 | 1503.360 |
| 7 | -597.415 | 1071.000 | 1071.000 | -18.812 | 1503.360 |
| 8 | -141.008 | 10/1.000 | 1071.000 | -18.812 | 1503.360 |
| 9 | 141.008 | 141.056 | 402.000 | -580.207 | 825.840 |
| 10 | 141.168 | 141.056 | 402.000 | -580.267 | 825.840 |
| 101 | AL DEFLECTIONS | AT THIS ST | AGE. | | |
| <u>_PT.</u> | DEFLECTION | 1 | | | |
| 1 | -0.1255620E-0 | 1 | | | |
| 2 | -0.7661273E-0 | 1 | | | |
| 3 | -0.7541214E-0 | 1 | • | | |
| 4 | -0.1264750E-0 | d. | | | |
| 5 | n.7720692E-0 | : 1 : | | | |
| 6 | 0.7709430E-0 | 1 | | | |
| - 7 | n.7686907E-0 | 3 . | | | |
| 8 | 0. ⁷ 675645E-0 | j, | | | |
| 9 | -0.9373891E-0 | 2 | | | |
| 10 | -0.6461324E-0 | ? | | | |
| 11 | 0.6510625E-0 | ? . | | | |
| 12 | N.8974699E-0 | 2 | | | |
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|--------------------------|---------------------|----------------|---------------|----|
| UNIT DE | FLECTIONS | | * | |
| KOW 1 | -0.5331299E-03 | 5 | | |
| ROW 2 | -0.4880432E-02 |)
I | - ř: | |
| ROW 3 | -0.4593806E-02 | 1
1 | , | |
| ROW 4 | -0.5549259E-03 | : | ,
7 | |
| ROW 5 | 0.1695467E-n1 | • | | |
| KOM 6 | 0.1695467E-01 | | | |
| ROW 7 | 0.1695467E-n1 | : | | |
| POW 8 | 0.1695407E-n1 | | | |
| FOW 9 | -0.7073771E-03 | N. | | |
| ROW 10 | -0.4035064E-03 | | a tag | |
| ROW 11 | 0 • 41 52766E - n 3 | | | |
| 60W 12 | 0.6001377E-03 | ÷ | | |
| UNIT MO | MENTS | | | |
| ROW 1 | 0. | | | |
| FOW 2 | 0.1500005E n2 | | | à |
| FOW 3 | -0.1500005E n2 | - | | |
| FOW 4 | 0.4245004E 02 | : | i
i | |
| ROW 5 | -0.4245004E 02 | · | ;
; | |
| NOW 6 | 0.3495001E n2 | : | ř | |
| POW 7 | -0.3495001E 02 | | <i>.</i> . | |
| | -0.71525575-64 | | | |
| HOW B | | UNIT MOMENT AT | O CET TO TEDO | |
| FOW 8 | 0 • | UNIT MOMENT AT | R SET TO ZERD | |
| FUW 8
FOW 9
FOW 10 | 0. | UNIT MOMENT AT | R SET TO ZERO | |

| UNIT AXI | AL LOAD | S |
|----------|---------------|--------------|
| MEMBER | 1 - n. | 244600nF 02 |
| MEMBER | 20. | 7629395E-04 |
| MEMBER | 3 -n. | 6484985E-04 |
| FEMBER | 4 0 • | 1525879F-(14 |
| NEMBER ! | 5 - N . | 254600NF 02 |
| | | - |

P[1,9] =

P[2, 9] =

Pl 3, 9] =

P[4,9] = 10.2605

| ۴L | ASTIC | HINGE | NO. 4 | FORMER AT PT. 2 |
|------------|---------------|---|---------|------------------------------|
| Ρŀ | 4, 1] | = | 7.6297 | |
| | | | | TOTAL FOR THIS CYCLE 7.6297 |
| Ρĺ | 1, ?) | = | 5.5598 | * |
| P (| 2 <u>,</u> 2] | = | 4.3857 | ; |
| Ρĺ | 3, 21 | =: " | 7.1289 | |
| Ρĺ | 4, 2] | 2: | 9.5486 | |
| | | | | TOTAL FOR THIS CYCLE 26.6230 |
| Pĺ | 1, 31 | = | 5.7353 | м
М |
| Ρí | 2, 31 | :::
:::::::::::::::::::::::::::::::::: | 3.9156 | |
| Ρι | 3, 3) | 5 | 6.4644 | |
| Ρĺ | 4,3) | ¥ (1 | L0.0619 | |

TOTAL FOR THIS CYCLE 20.1772

Pl 1, 8] = 6.2519 P[2, 8] = 3.5142 P[3,8]= 6.2000 P[4,8]= 10.2605

> TOTAL FOR THIS CYCLE 26.2266 4

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TOTAL FOR THIS CYCLE 26.2264

CONVERSION OBTAINED FOR HINGE 4

6.2552

3.5072

6.2039

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Let | | 247 | |
| | | | | H H | | .р. <u>ү</u> . | P/PY |
| | Ţ | 102.113 | 102,113 | 412.000 | -643.066 | P25.840 | U. 185 |
| | ?
 | 0113 | 102.113 | 402.000 | -640.066 | 825.840 | u.785 |
| | 1 3 | -02.113 | 1071.000 | 1071.000 | -12.611 | 1503.360 | 6.008 |
| - 1. | 4 | 011.621 | 10/1.000 | 10/1.000 | -12.611 | 1503.360 | ່ ^ບ ຸບ()ອ |
| .:
| 5 | -0/1.221 | 10/1.000 | 10/1.000 | -14.012 | 1503.360 | ំ.ប្រដ |
| | 6 | 112.901 | 10/1.000 | 10/1.000 | -1-2.612 | 1503.360 | n.n0¤ |
| | 1 | -112.901 | 10/1.000 | 10/1.000 | -12.012 | 1503.300 | ່ມ ບ () 8 |
| | P | 94.53c | 1071.000 | 1071.000 | -12.612 | 1503.360 | ₫.008 |
| | y | 94.539 | ×4.502 | 402.000 | -661.1/0 | 825.840 | . oU1 |
| | 1 (, | 44.63¢ | 94.582 | 492.000 | -661.176 | 825.840 | U. P01 |
| | UTAL | DEFLECTION | S AT THIS ST | AGE. | ۇ. | Y. March | |

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۲ | L. 7 | | ····· |
|-----------|--------|-------------|-------|
| - | FI. | DEFLECTION | |
| | 1 -0. | 141252-E-01 | |
| | 2 -0. | 10×1598E-CO | |
| • | 3 -n. | 9940210E-01 | |
| · | 4 - 0. | 1441100E-01 | |
| | 5 0. | 2281042E-00 | х. |
| | 6 n. | 2240287E-01 | |
| | 7 n. | 2278777E-00 | |
| | 8 0. | 2218022E-00 | |
| 2 | 9 -0. | 1376740E-01 | - |
| : **
| 10 -n. | 8619118E-02 | |
| | 11 0. | 8773424E-02 | |
| | | | |

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| | ۲T. | TUT. MOM. | MFC | M F. | AX. LUAD | Ρ.γ. | PVPY | UNIT DEFLECTIONS | |
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The author was born on August 6, 1941 in Orange, New Jersey, the son of Mr. Ira Carl Bott and Mrs. Florence Elizabeth Moorhead Bott. His childhood was spent in the town of Boonton, New Jersey and he attended elementary and high schools there. In September of 1959 he entered Lehigh University at Bethlehem, Pennsylvania to work for his Bachelor's Degree in Civil Engineering. He received the degree in June of 1963 and began work as a Field Engineer in Georgetown, South Carolina for the Rust Engineering Company of Pittsburgh, Pennsylvania. In February of 1964, he married the former Gale Ann Hulmes of Boonton. Together, they resided in Georgetown until July 1964 when the author

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