



# Towards NASA's In House Lattice-Boltzmann Solver

Joseph G. Kocheemoolayil, Michael F. Barad,  
Gerrit-Daniel Stich, Cetin C. Kiris  
Computational Aerosciences Branch  
NASA Ames Research Center

High-Fidelity Industrial LES/DNS Symposium (HiFiLeD)  
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## ✓ Computational Requirements

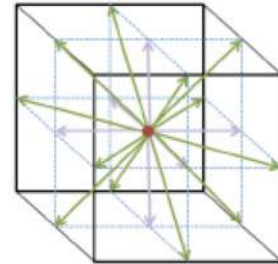
- Space-time resolution requirements for acoustics problems are demanding
- Resources used for Cartesian Navier-Stokes examples shown above:
  - Launch Environment: ~200 million cells, ~7 days of wall time (1000 cores)
  - Parachute: 200 million cells, 3 days of wall time (2000 cores)
  - Contra-Rotating Open Rotor: 360 million cells, 14 days (1400 cores)
  - Launch Abort System: 400 million cells, 28 days of wall time (2000 cores)
  - Landing Gear: 298 million cells, 20 days of wall time (3000 cores)
- LAVA Cartesian infrastructure has been re-factored into Navier-Stokes (NS) and Lattice Boltzmann Method (LBM)
  - 10-50 times speed-up can be achieved with LBM vs NS-WENO without any compromise in accuracy or robustness



# LAVA LBM: Governing Equations



$$\underbrace{f_i(\vec{x} + c\vec{e}_i\Delta t, t + \Delta t) - f_i(\vec{x}, t)}_{\text{Streaming}} = \frac{1}{\tau} \underbrace{(f_i(\vec{x}, t) - f_i^{eq}(\vec{x}, t))}_{\text{Collision}}$$



## Physics:

- Governs space time evolution of Density Distribution Functions
- Equilibrium distribution functions are truncated Maxwell-Boltzmann distributions
- Relaxation time related to kinematic viscosity
- Pressure related to density through the isothermal ideal gas law
- **Lattice Boltzmann Equations (LBE) recover the Navier-Stokes equations in the low Mach number limit**

## Numerics:

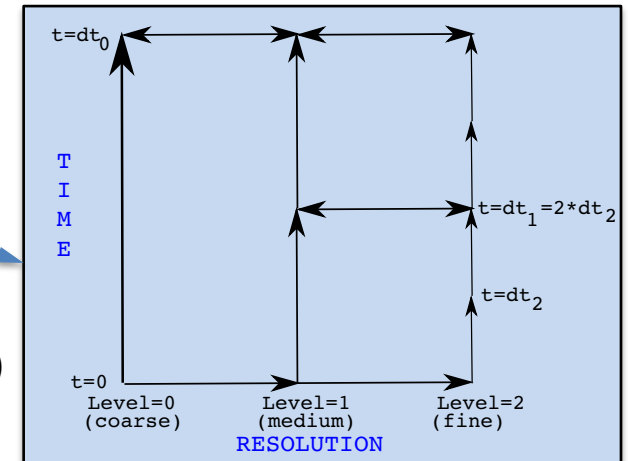
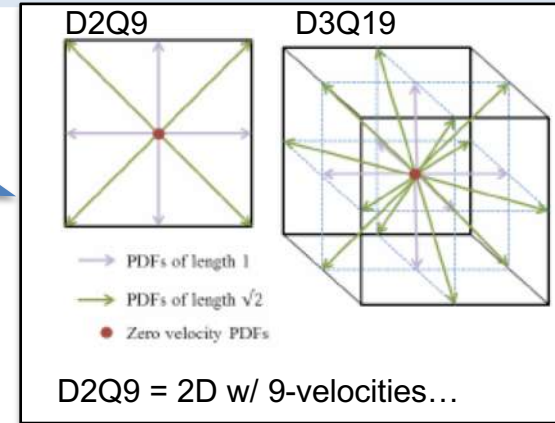
- **Extremely efficient** 'collide at nodes and stream along links' discrete analog to the Boltzmann equation
- Particles bound to a regularly spaced lattice collide at nodes relaxing towards the local equilibrium
- Post-collision distribution functions hop on to neighboring nodes along the lattice links – Exact, dissipation-free advection from simple 'copy' operation
- Macroscopic quantities such as density and momentum are moments of the density distribution functions in the discrete velocity space

# LAVA LBM: Progress



## Implementation to Date:

- **Lattices:** including D2Q9, D3Q15, D3Q19, D3Q27, D3Q39 ...
- **Collision Models:**
  - Bhatnagar-Gross-Krook (BGK)
  - Multi-Relaxation Time (MRT)
  - Entropic and positivity preserving variants of BGK
  - Entropic Multi-Relaxation Time (EMRT)
  - Regularized BGK
- **Turbulence Models:** Smagorinsky, Vreman, Sigma and Spalart-Allmaras models
- **Wall Models:** Tamm-Mott-Smith boundary condition, filter-based slip wall model, Wall functions based on log law and power law
- **Parallelization:**
  - Structured adaptive mesh refinement (SAMR) based LBM requires parallel ghost cell exchanges:
    - Fine-fine for communication within levels
    - Conservative Coarse-fine interface treatment
    - Efficient parallel I/O
- **Multi-Resolution with Recursive Sub-Cycling**
- **Boundary Conditions:**
  - No-slip and slip bounce back walls
  - Accurate and robust curved walls (stationary and moving)
  - Inflow/outflow, and periodic

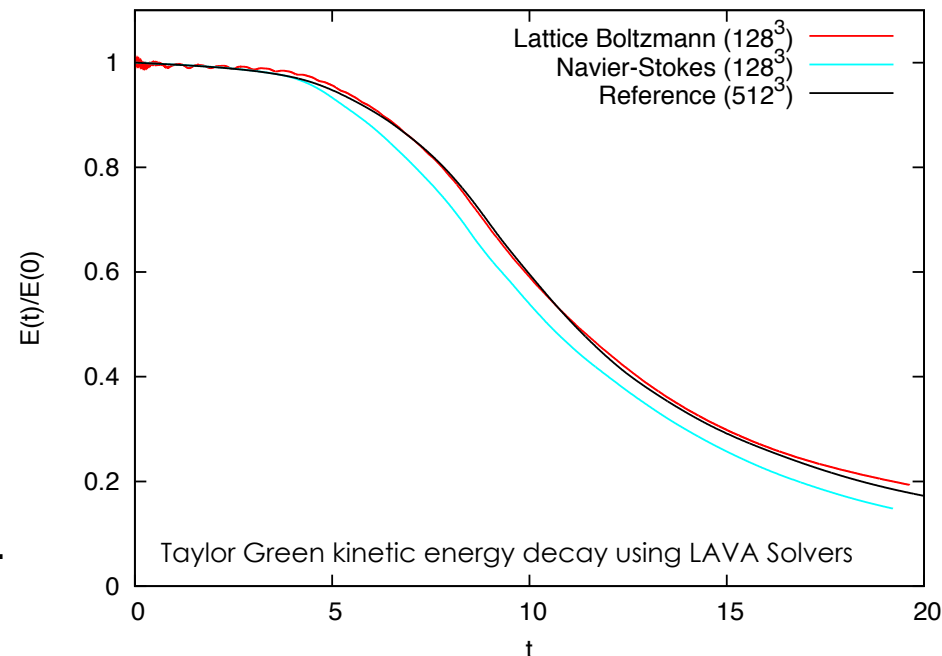
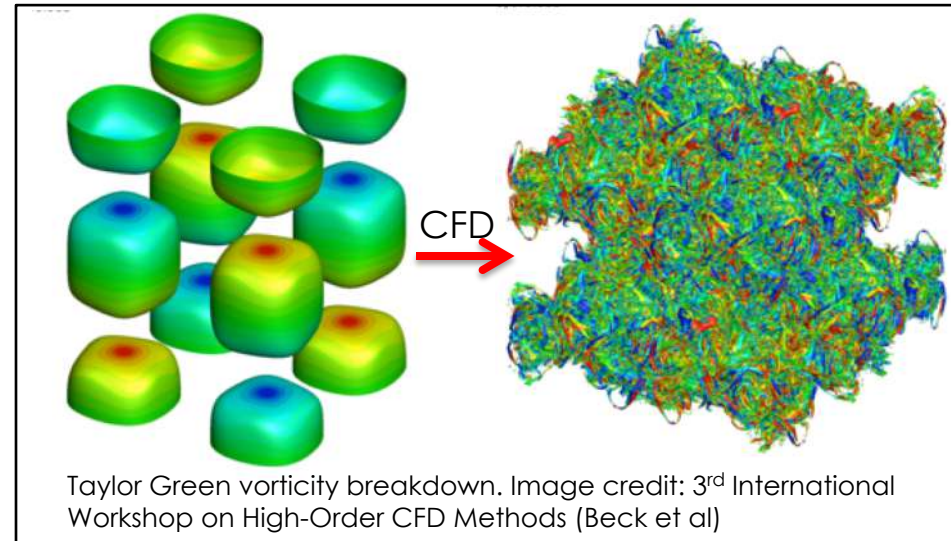


# LAVA LBM: Verification and Validation



## Turbulent Taylor Green Vortex Breakdown Test Case:

- **Motivation:**
  - Simple low speed workshop case for testing high-order solvers
  - Illustrates ability of solver to simulate turbulent energy cascade
  - Periodic boundary conditions
- **Setup:**
  - Analytic initial condition
    - Mach = 0.1
    - Reynolds Number = 1600
  - Triply periodic flow in a box
- **Comparisons:**
  - LAVA's Lattice Boltzmann (LB) solver captures the turbulent kinetic energy cascade from large scales to small scales extremely well.
  - Performance compared to LAVA's Cartesian grid Navier-Stokes WENO solver showed a **factor of 50 speedup**.



# LAVA LBM: Verification and Validation



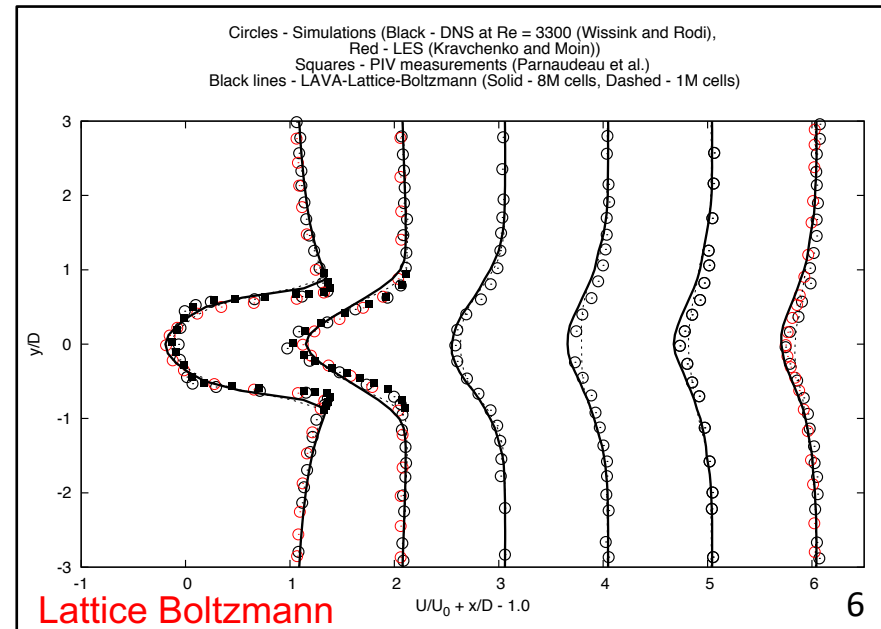
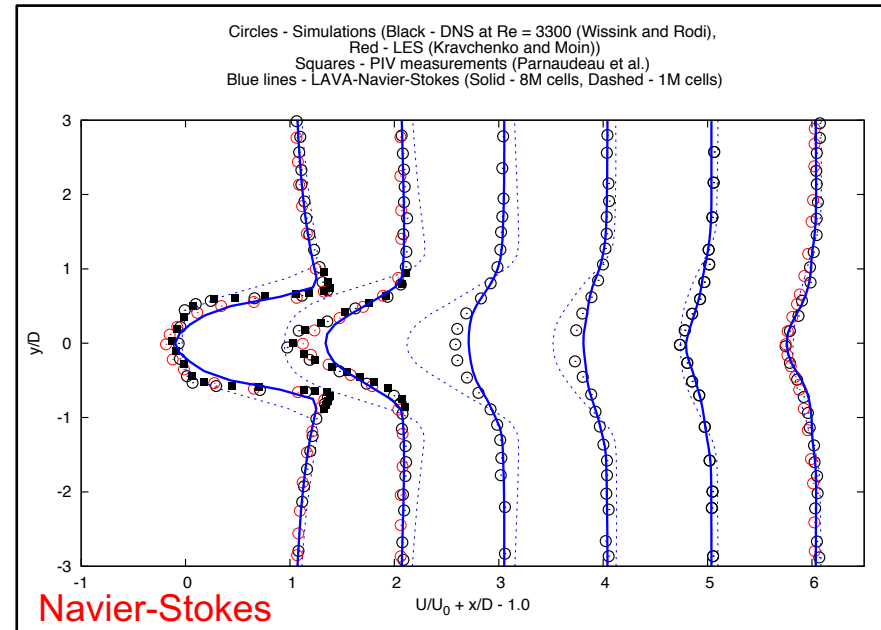
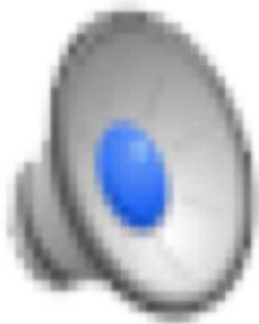
## LES of Flow Past a Cylinder

- Well documented prototypical turbulent separated flow
- Detailed comparisons made with measurements and benchmark simulations

• **Setup:** Reynolds number = 3900

### • Comparisons:

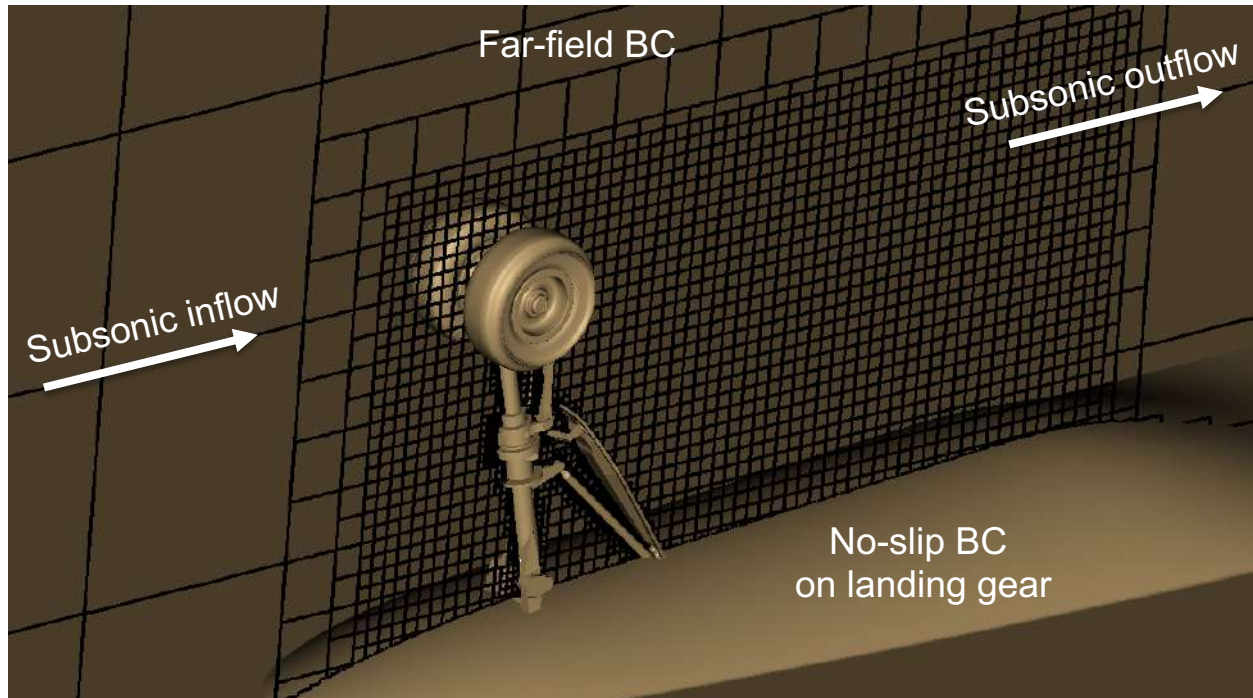
- LBM at 1M and 8M compares well with DNS @ 400M (M = million points)
- 20x speedup even with embedded geometry
- Good comparison with benchmark datasets (PIV, LES, DNS) even with just 8 lattice nodes across the cylinder
- More accurate than high-order upwind biased NS schemes for identical resolution



# Cavity-Closed Nose Landing Gear



## Grid Topology and Computational Setup



Mach = 0.166  
Re = 66423 ( $D=D_{\text{strut}}$ )  
 $U_{\text{ref}} = 58.32$  m/s  
 $T_{\text{ref}} = 307.05$  K  
 $P_{\text{ref}} = 98605$  Pa

LAVA Cartesian options:

- LBM uses EMRT with D3Q27
- NS uses WENO5 or WENO6 (as noted)

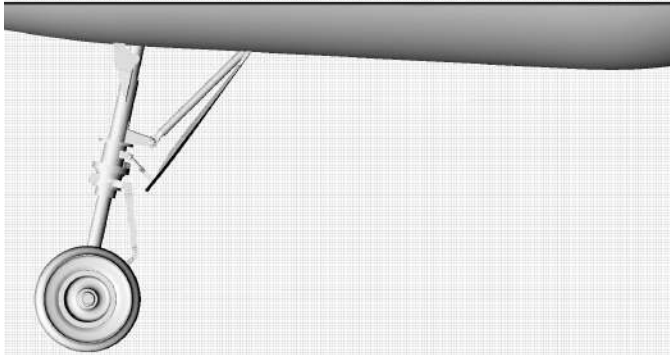
Setup follows the partially-dressed, cavity-closed nose landing gear (PDCC-NLG) noise problem from [AIAA's Benchmark problems for Airframe Noise Computations \(BANC\)](#) series of workshops. (Problem 4. [Nose landing gear](#))

[https://info.aiaa.org/tac/ASG/FDTC/DG/BECAN\\_files/\\_BANCIII.htm](https://info.aiaa.org/tac/ASG/FDTC/DG/BECAN_files/_BANCIII.htm)

# Cartesian Grid Resolution

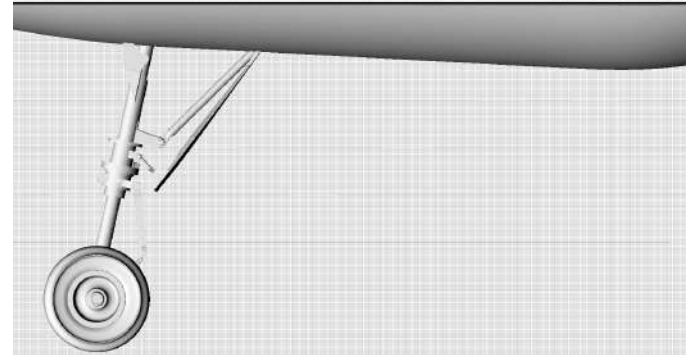


**9 Levels (56M)**



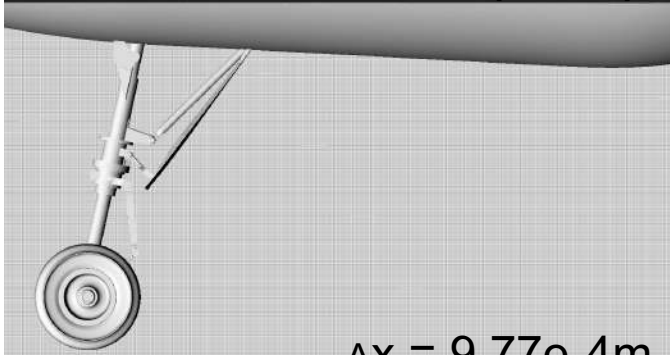
$$\Delta x = 3.91e-3m$$

**10 Levels (91 M)**



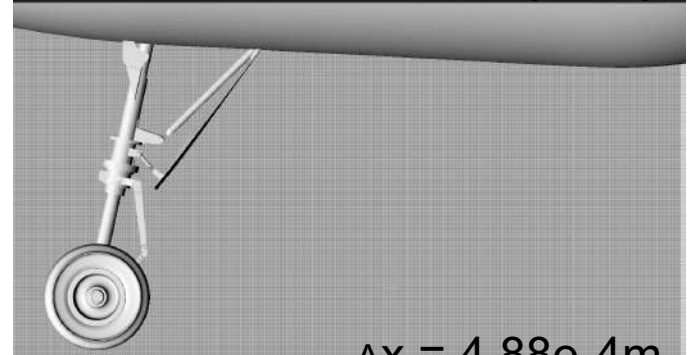
$$\Delta x = 1.95e-3m$$

**11 Levels (260M)**



$$\Delta x = 9.77e-4m$$

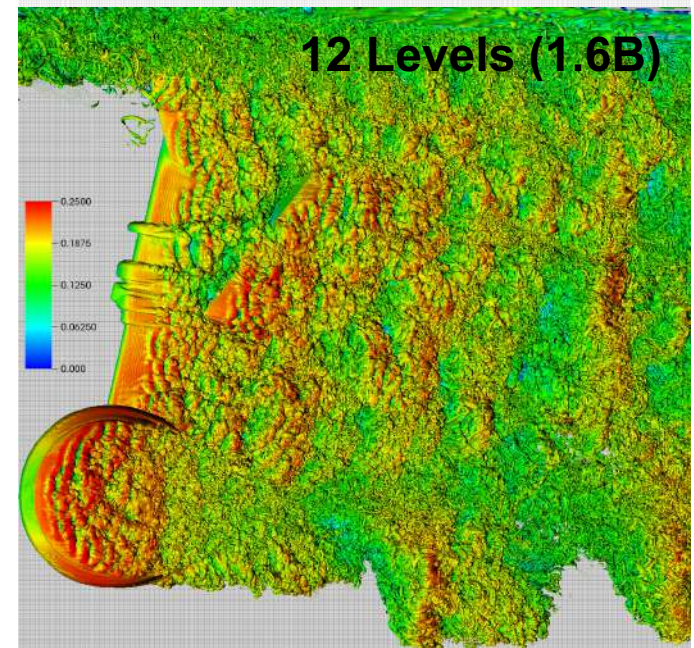
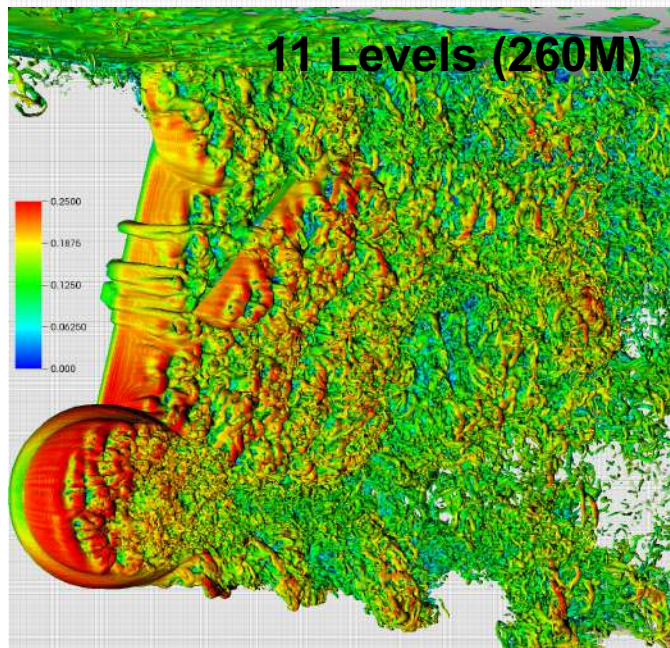
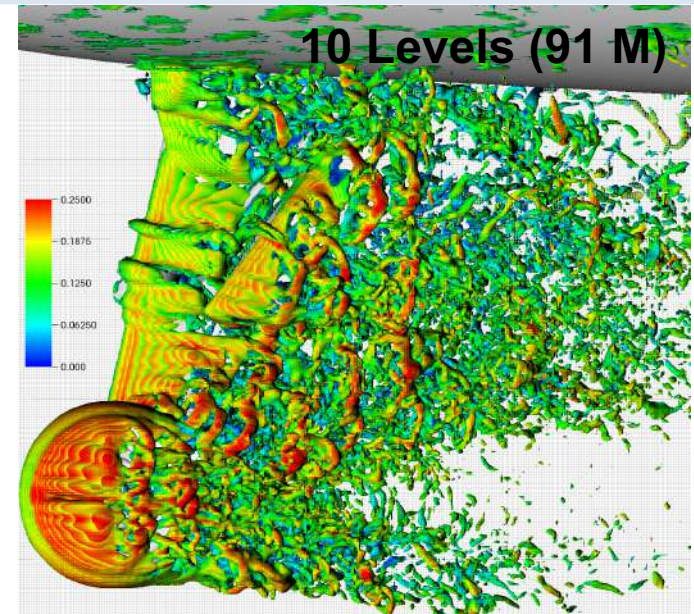
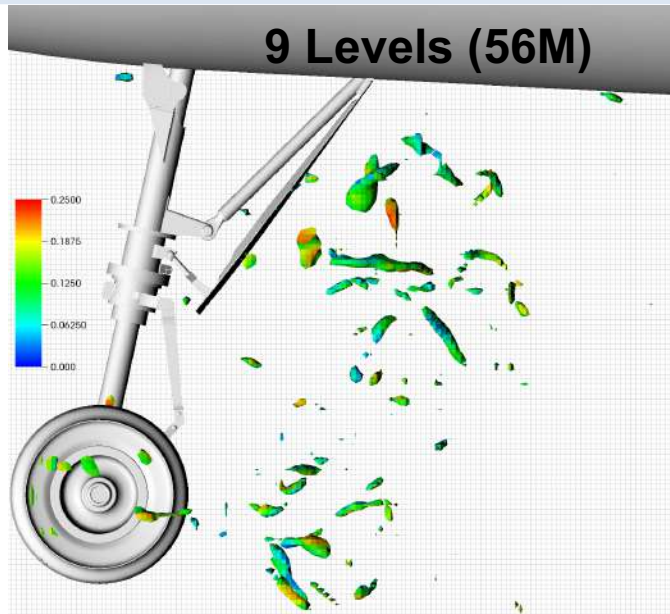
**12 Levels (1.6B)**



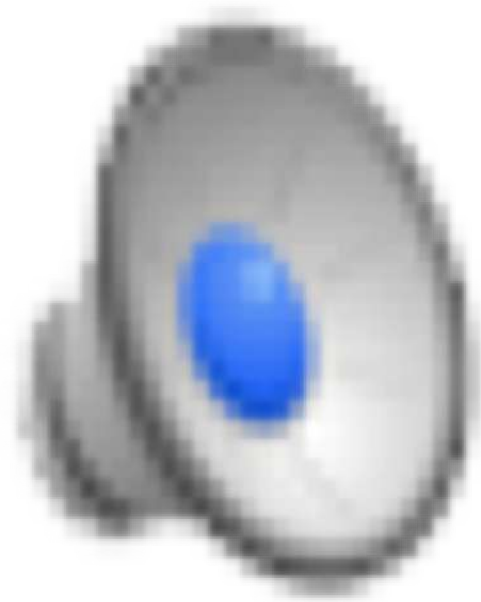
$$\Delta x = 4.88e-4m$$



# Grid Sensitivity: Vorticity Colored by Mach

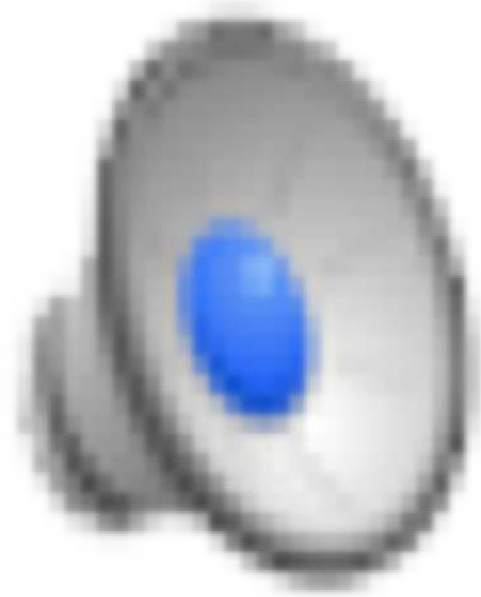


# Velocity Magnitude (Center-plane)



LBM @ 1.6 billion: expense = 7.9 normalized wall time units (relative to 260M calc)

# Passive Particle Colored by Mach Number

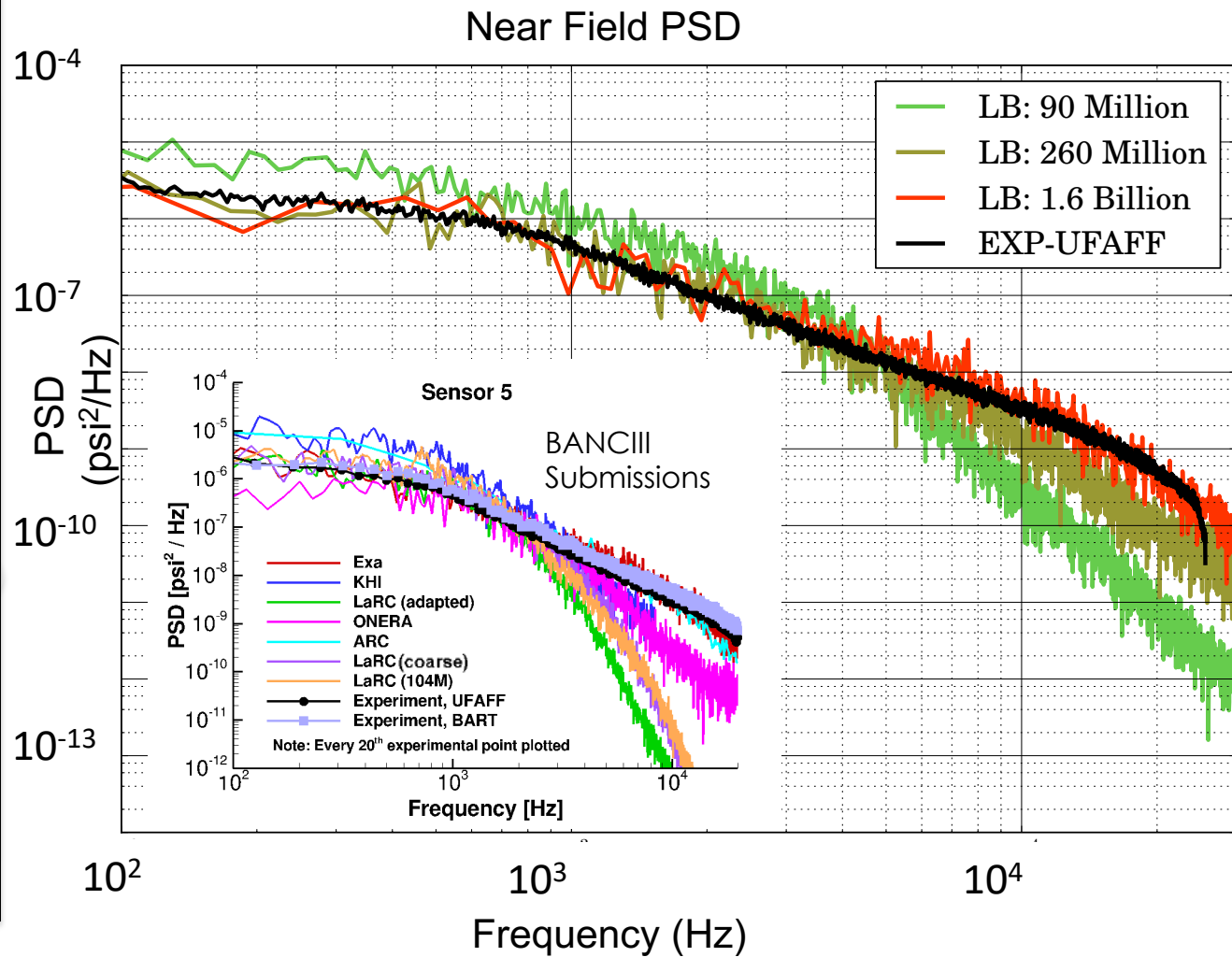
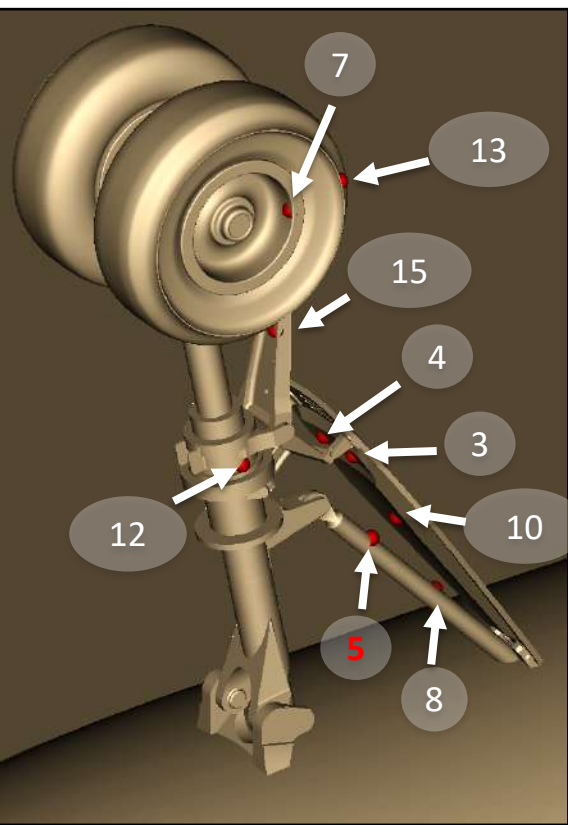


LBM @ 1.6 billion

# Grid Sensitivity - PSD



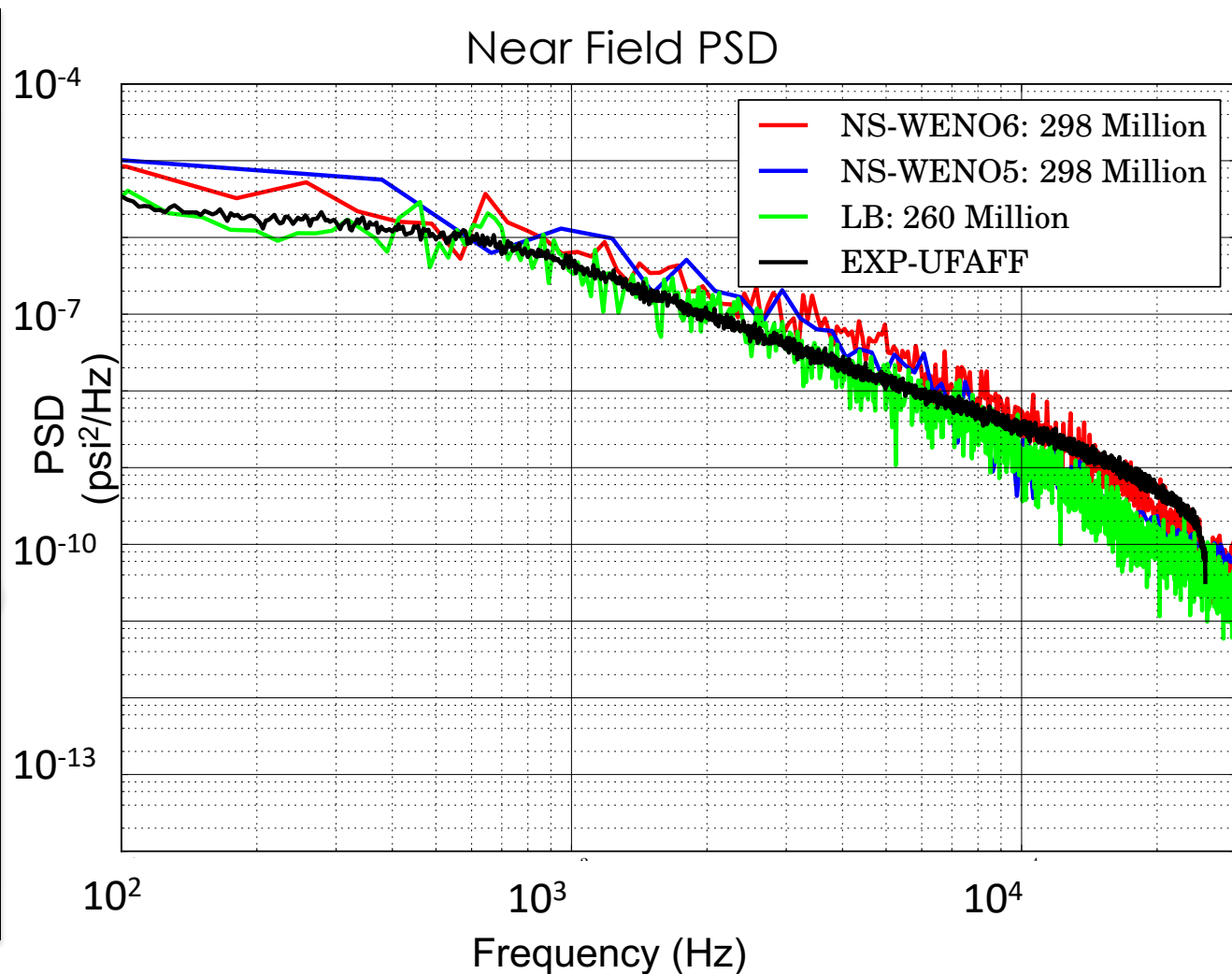
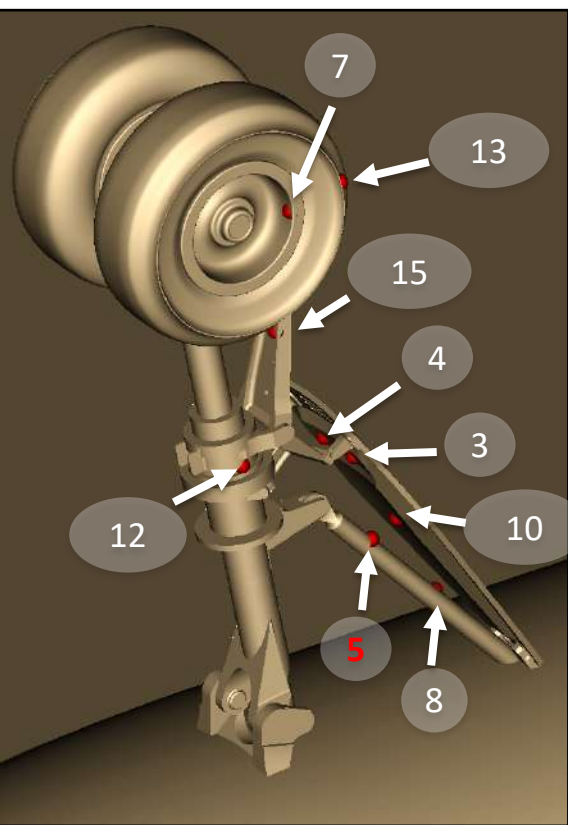
## Channel 5: Upper Drag Link



# LBM vs NS - PSD



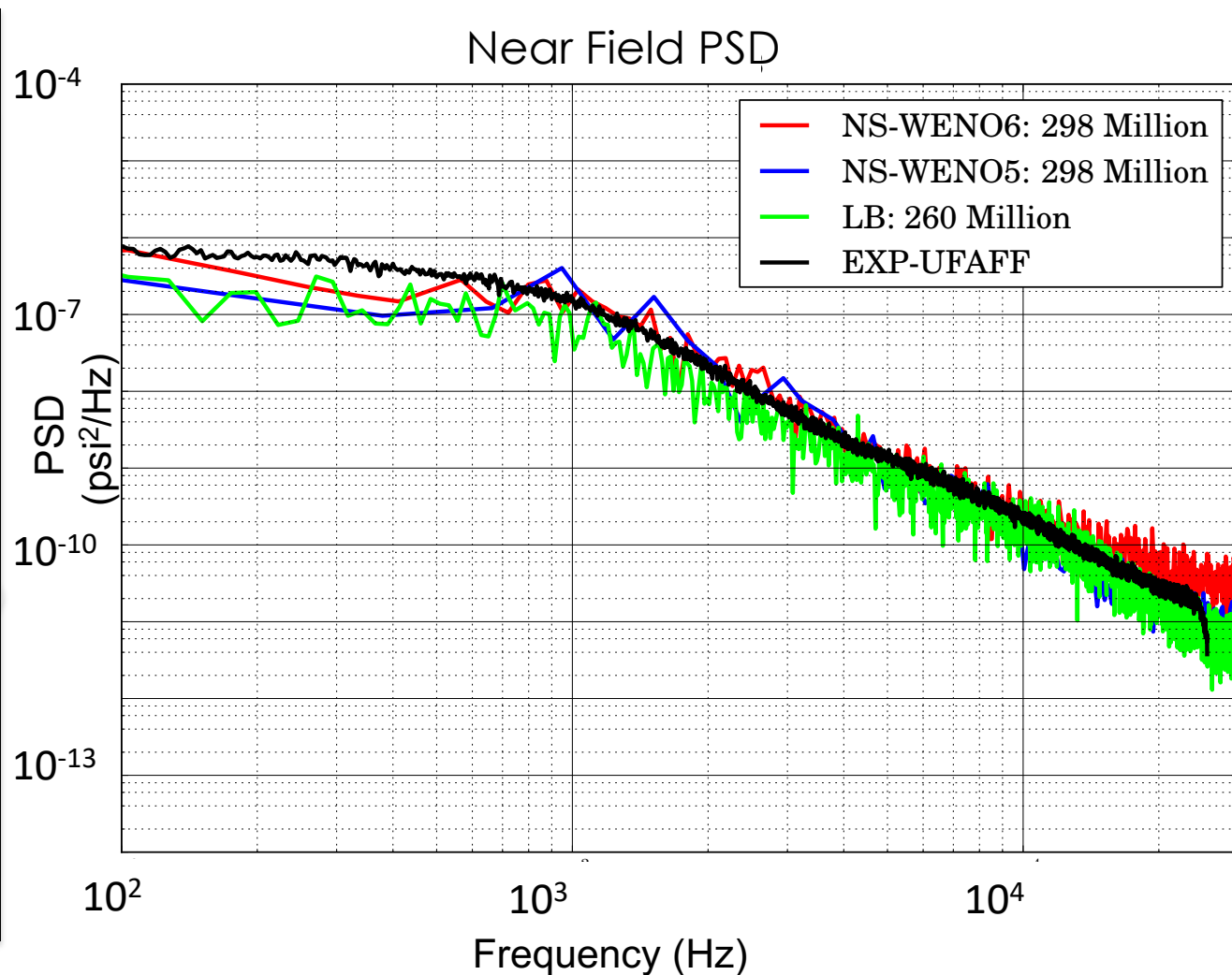
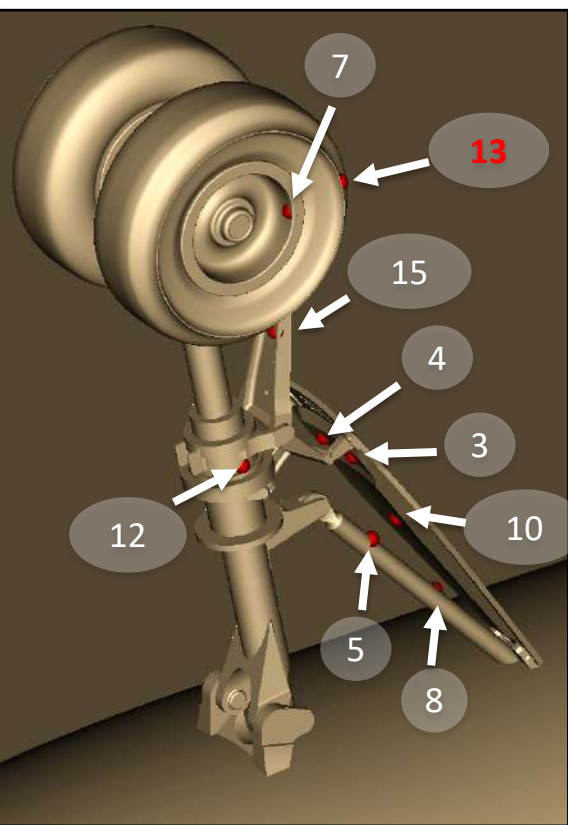
## Channel 5: Upper Drag Link



# LBM vs NS - PSD



## Channel 13: Outer Wheel





Method	CPU Cores (type)	Cells (million)	Wall Days to 0.19 sec	Core Days to 0.19 sec	Relative SBU Expense
NS-GCM	3000 (ivy)	298	20.5	61352	12.1
NS-IIM	9600 (has)	222	6.1	58490	15.3
LBM	1400 (bro)	260	2.25	3156	1

- For a comparable mesh size, **LBM is 12-15 times faster computationally than Navier-Stokes** and is **equally accurate**. “Apples-to-apples” comparison with the exact same mesh & CPU-type is ongoing. Note: LBM code is not yet optimized, and we output volume data every 50 steps!
- **LBM at 1.6 billion cells is ~2 times faster than NS at 298 million**. This is a key enabler for unprecedented high resolution simulations.
- Performance details:
  - Both Cartesian Navier-Stokes and LBM are memory-bound (not compute-bound) algorithms, the latter much more so than the former.
  - Non-linear, LBM collision operation where all the work happens is entirely local!! Data locality is critical to the computational efficiency of LBM relative to high-order Cartesian NS codes.

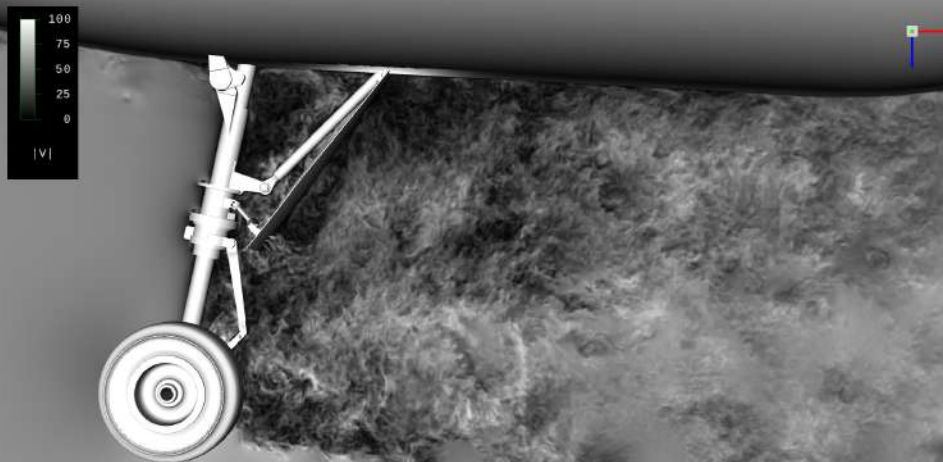
# Velocity Magnitude (Center-plane)



NS-IIM @ 222 million: : expense = 15.3



NS-GCM @ 298 million: expense = 12.1



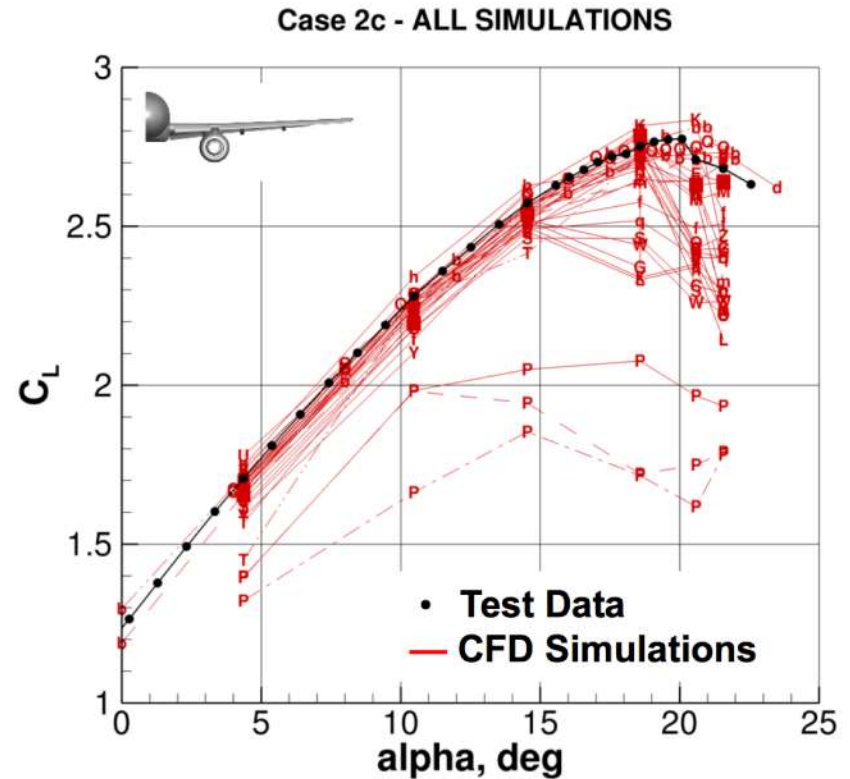
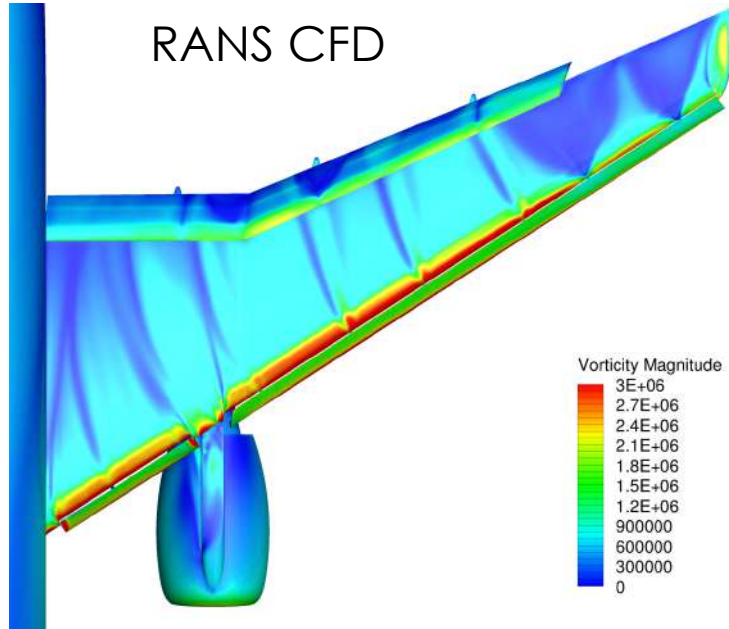
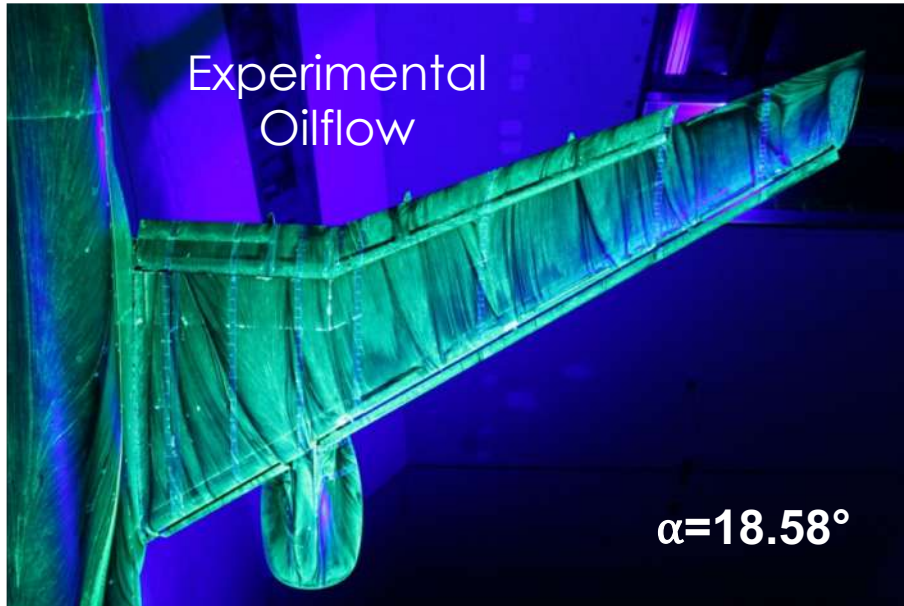
LBM @ 260 million: expense = 1.0



LBM @ 90 million: expense = 0.182



# AIAA High Lift Prediction Workshop 3



- RANS unreliable beyond 14°
- Higher fidelity approaches with fast turnaround times necessary

# NASA 2-D Hump – Experimental Setup



- ✓ Assess ability of CFD solvers to predict flow separation from a smooth body (caused by adverse pressure gradient) as well as subsequent reattachment and boundary layer recovery.

## Wall-resolved LES:

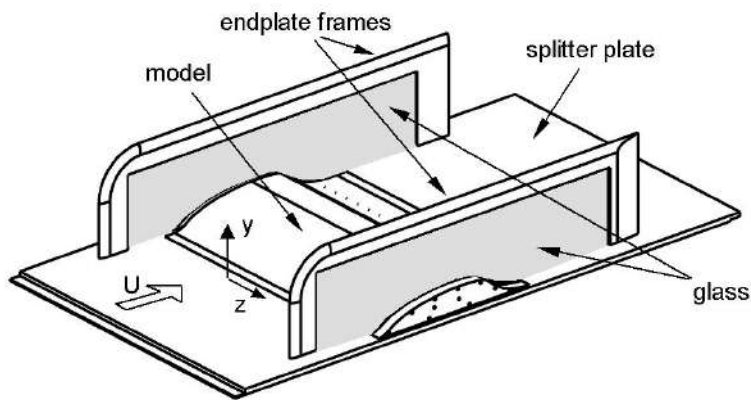
- ✓ Uzun, A. and Malik, M. (AIAA 2017-5308)

## Wall-modeled LES:

- ✓ Iyer, P. and Malik, M. (AIAA 2016-3186)

## Lattice Boltzmann Methods:

- ✓ Duda, B. and Fares, E. (AIAA 2016-1836)

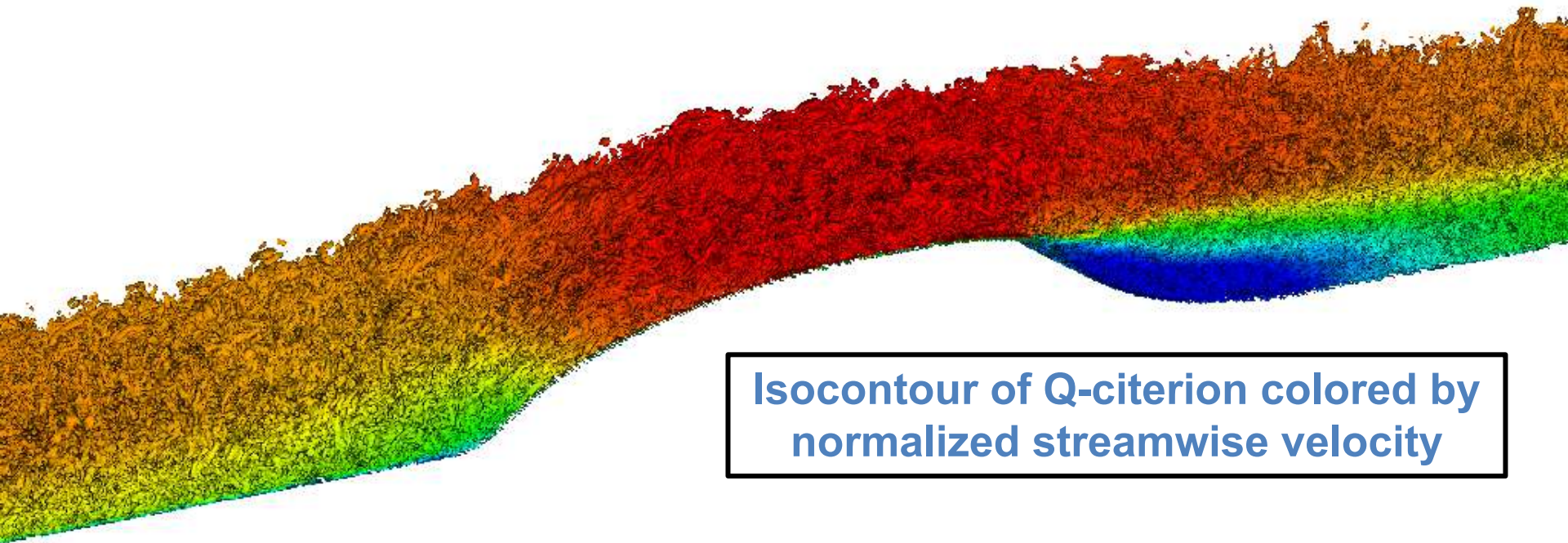


<sup>1</sup> Greenblatt et. Al. "Experimental Investigation of Separation Control Part 1: Baseline and Steady Suction". AIAA Journal, vol 44, no. 12, pp. 2820-2830, 2006

<sup>2</sup> Rumsey C, "Turbulence Modeling Resource", <https://turbmodels.larc.nasa.gov>

<sup>3</sup> Rumsey C, "CFD Validation of Synthetic Jets and Turbulent Separation Control", <http://cfdval2004.larc.nasa.gov>

- ✓ Lattice: D3Q27
- ✓ Collision Model: EMRT
- ✓ Synthetic Eddy Method with scaled DNS Flat plate Data at  $x/c = -3.0$

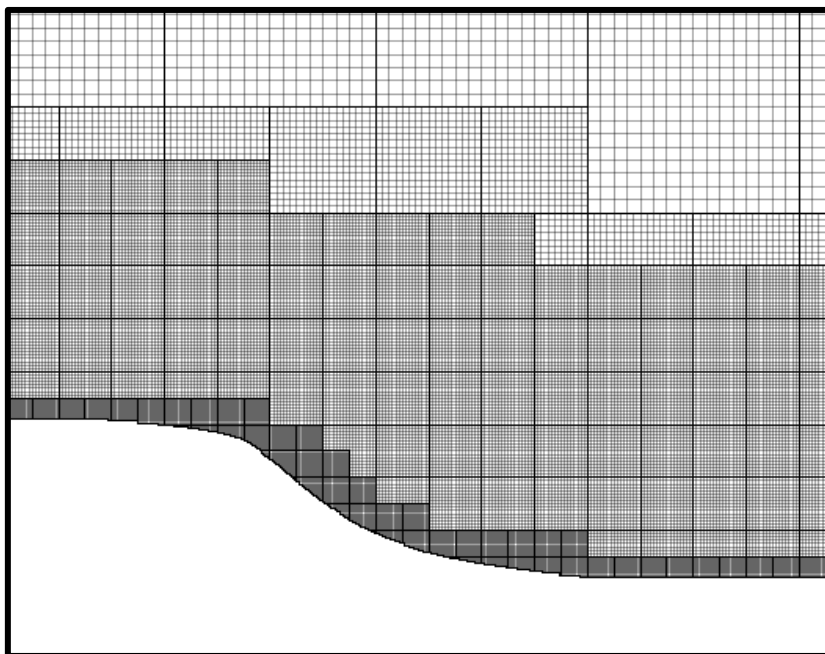
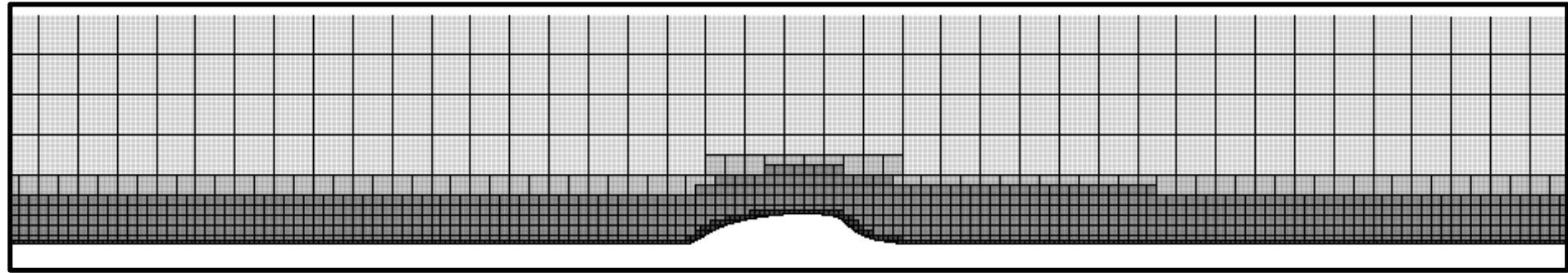


- ✓ Periodic BCs in spanwise direction (Side walls not modeled)

# Application of the Lattice Boltzmann Method

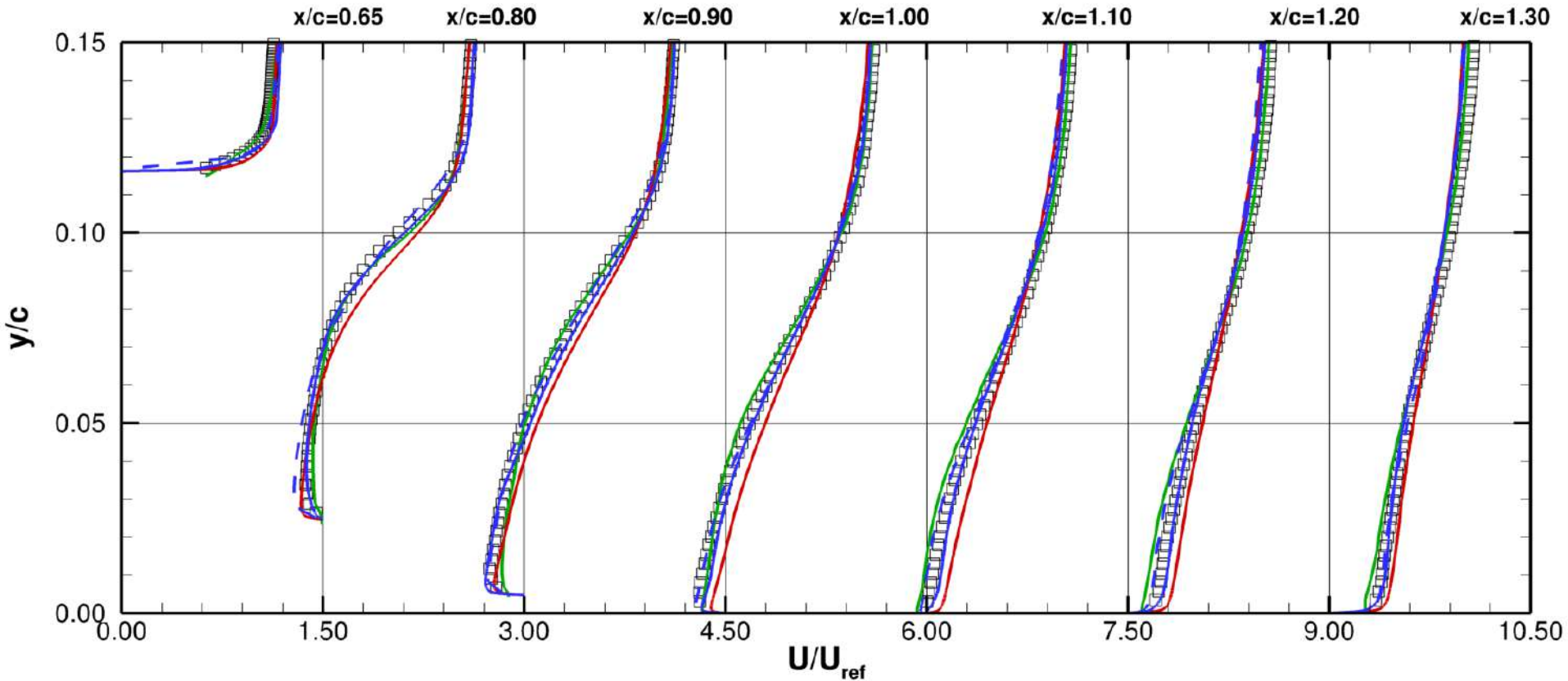
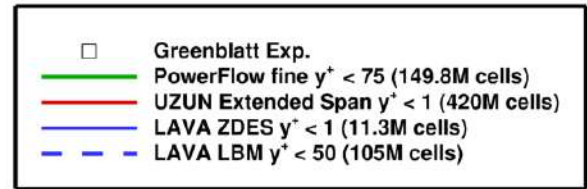


- ✓ Local as well as adaptive mesh refinement well tested in our Cartesian framework.



- ✓ 5 Refinement Levels
- ✓ Refinement ratio of 2:1
- ✓ Level 3 in regions of high vorticity
- ✓ Level 4 on all viscous walls
- ✓ Level 5 from  $x/c = -0.2$  to  $1.3$
- ✓ **105 million points**
- ✓ Spanwise extent =  $0.2c$
- ✓  $\Delta^+ \approx 50$  in viscous wall units

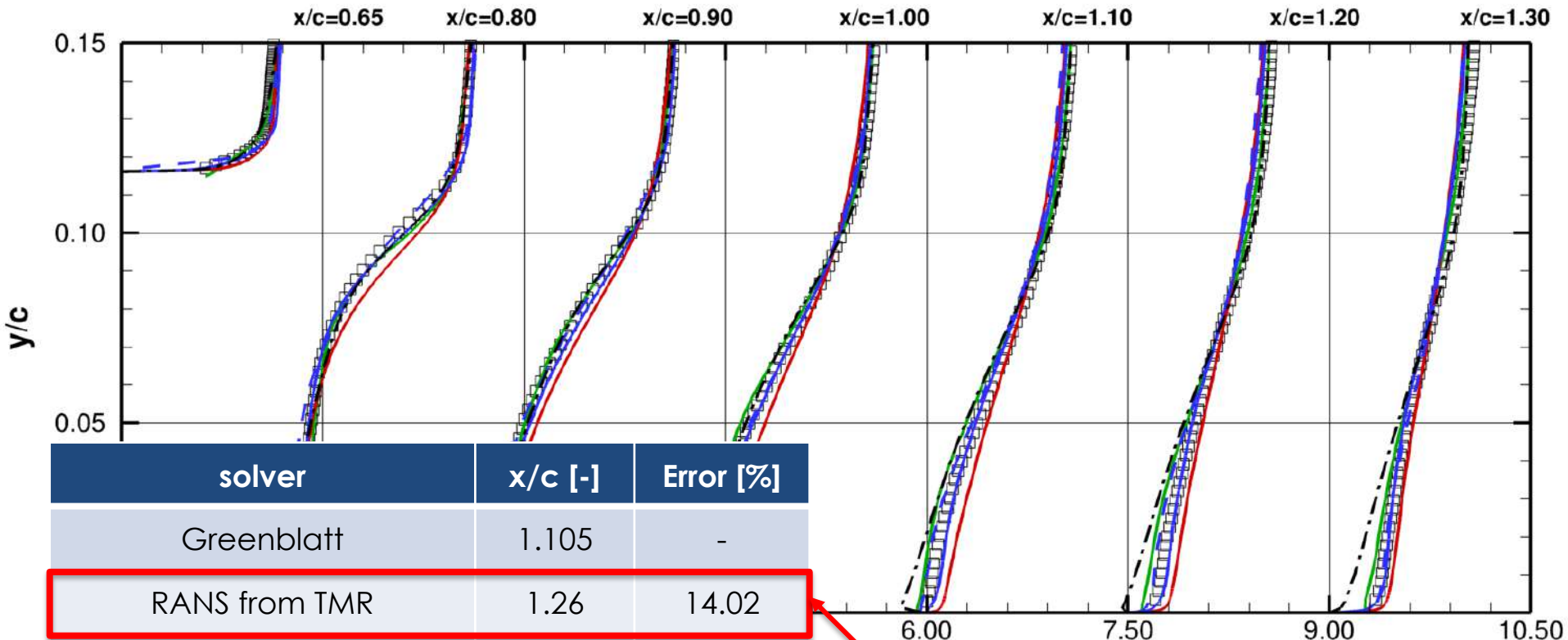
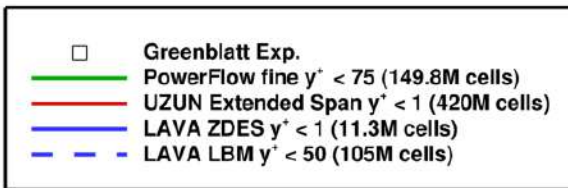
## Streamwise Velocity



✓ Excellent agreement with measurements



## Streamwise Velocity



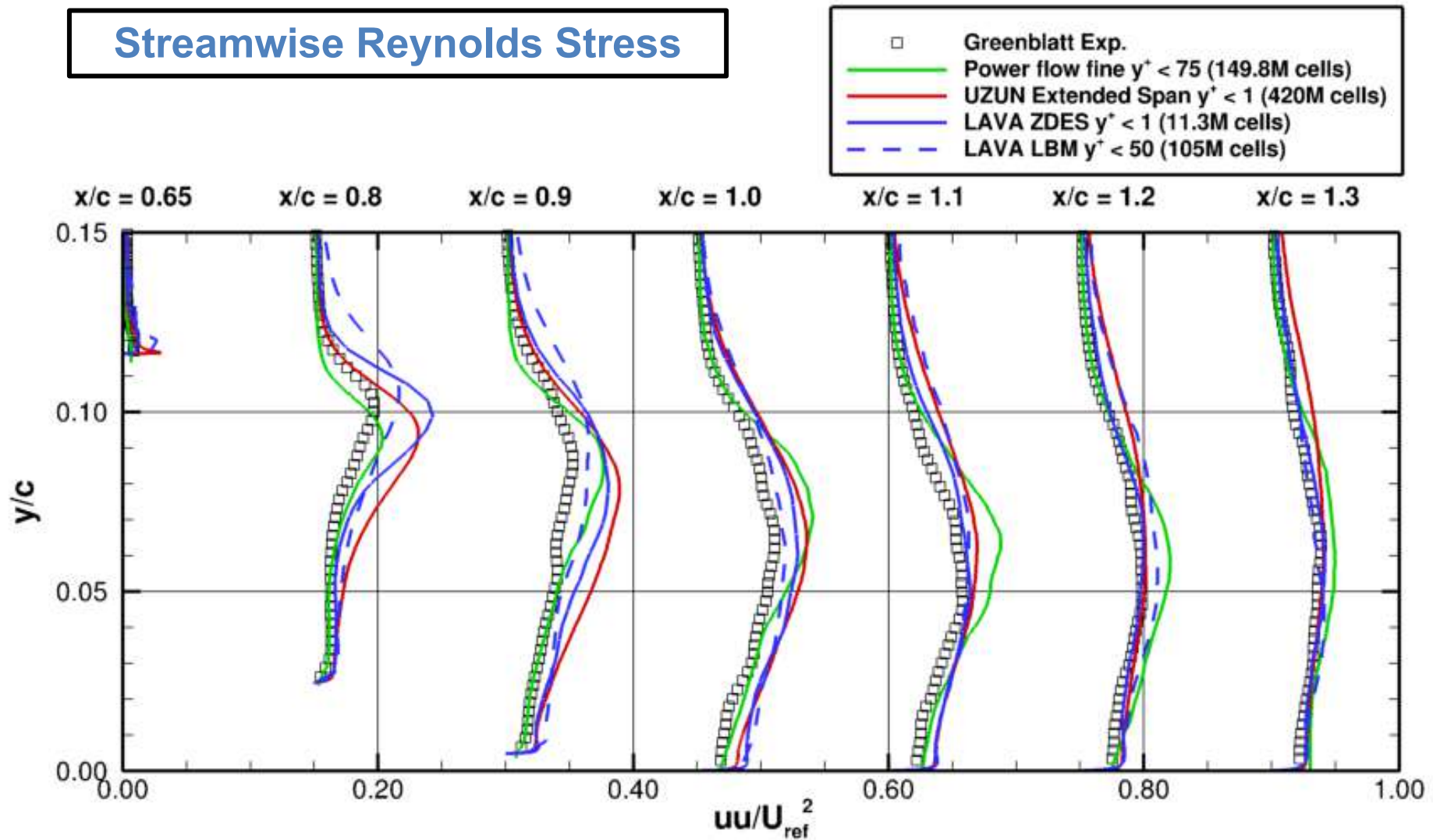
solver	x/c [-]	Error [%]
Greenblatt	1.105	-
RANS from TMR	1.26	14.02
DDES	1.34	21.26
DDES + SEM	1.23	11.31
<b>ZDES + SEM</b>	<b>1.11</b>	<b>0.45</b>

$U_{ref}$

**96 %  
improvement**

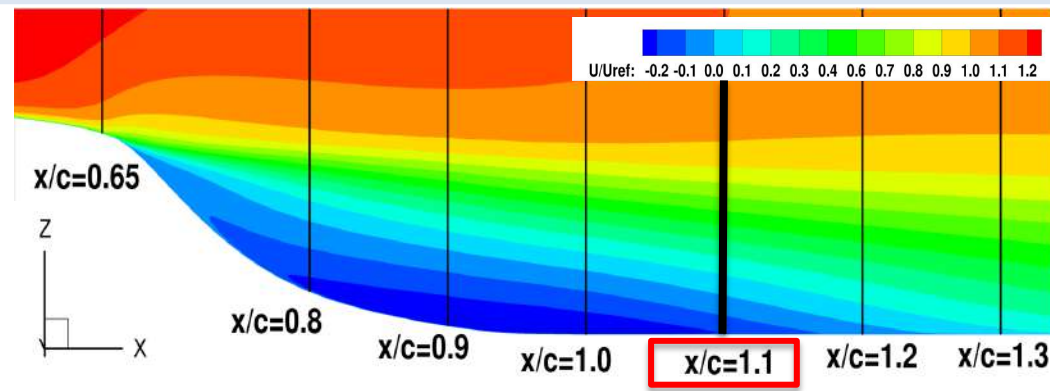


## Streamwise Reynolds Stress

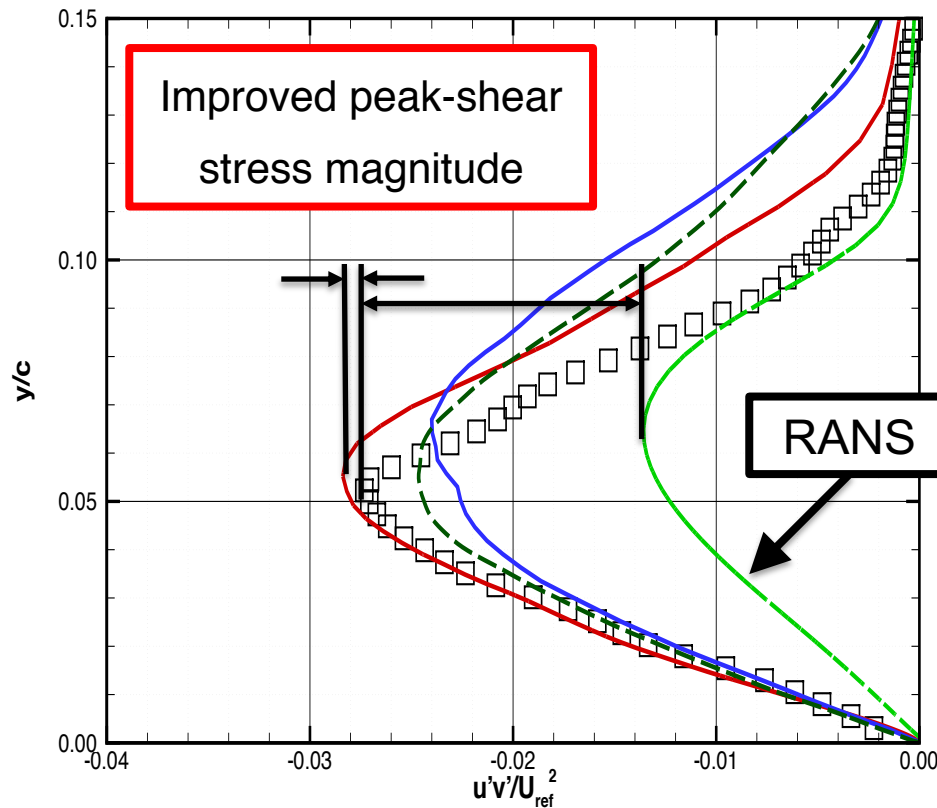


✓ Encouraging agreement with experiment for turbulence intensity profiles

# NASA 2-D Hump – Application of Lattice Boltzmann



- Greenblatt et.al.
- LAVA ZDES Mode 3  $y^+ < 1$  (11.3M cells)
- LAVA LBM  $y^+ < 50$  (105M cells)
- - - UZUN Extended Span  $y^+ < 1$  (420M cells)
- · - · - PowerFlow fine  $y^+ < 75$  (148.9M cells)
- PowerFlow periodic  $y^+ < 75$  (148.9M cells)







## Towards Urban Air Mobility (UAM)

High-Fidelity Modeling and Optimization Method Development  
NASA Revolutionary Vertical Lift Technology Rotary Project (RVLT)

# Isolated UAS Rotor in Hover Validation



## Objective:

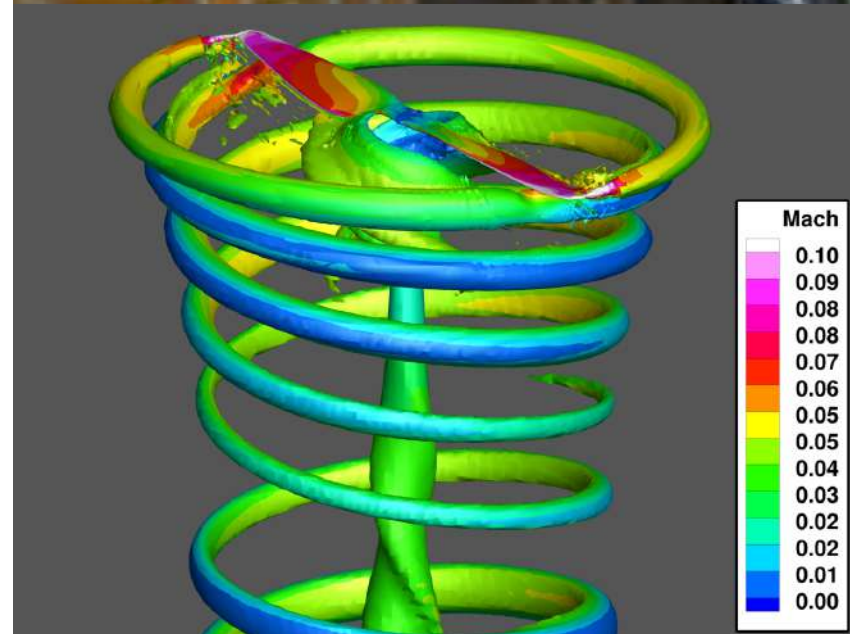
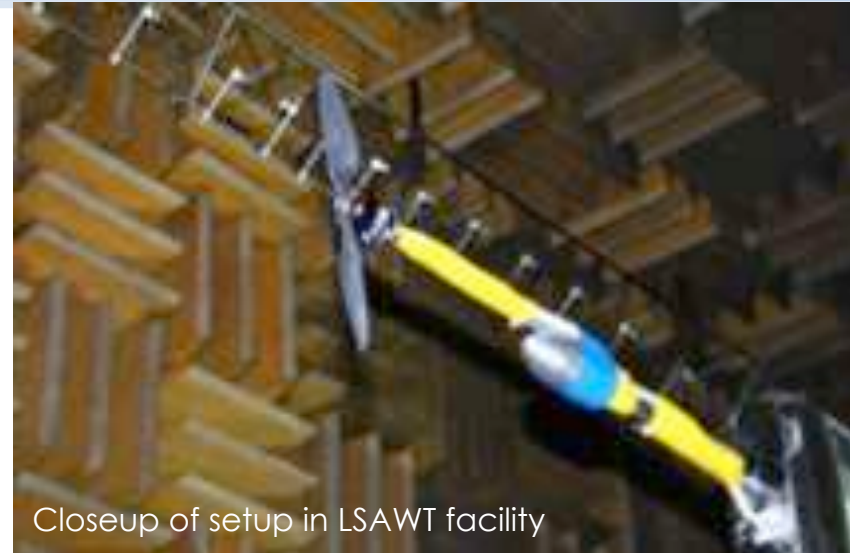
- ✓ Validate LAVA for RVLT applications
- ✓ Assess pros and cons of body-fitted/Cartesian Grid as well as Navier-Stokes/Lattice Boltzmann approaches

## Computational Methodology :

- ✓ Navier-Stokes (NS) URANS solver on Structured Overset Grid
- ✓ Navier-Stokes as well as Lattice Boltzmann (LB) on Cartesian Grid

## Validation:

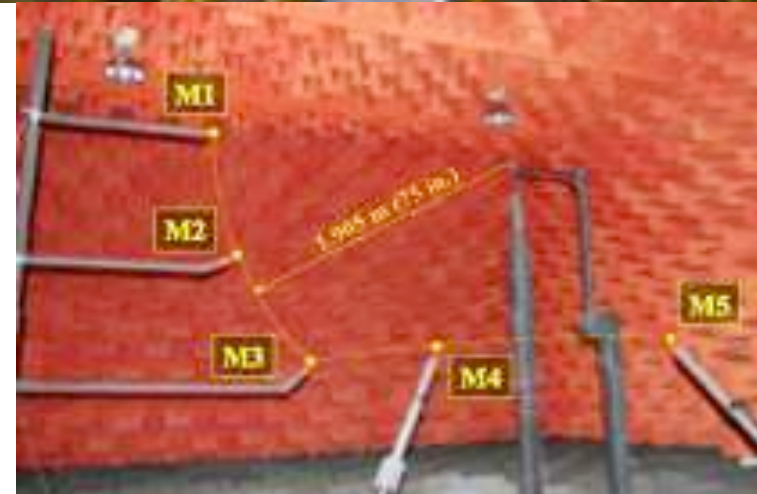
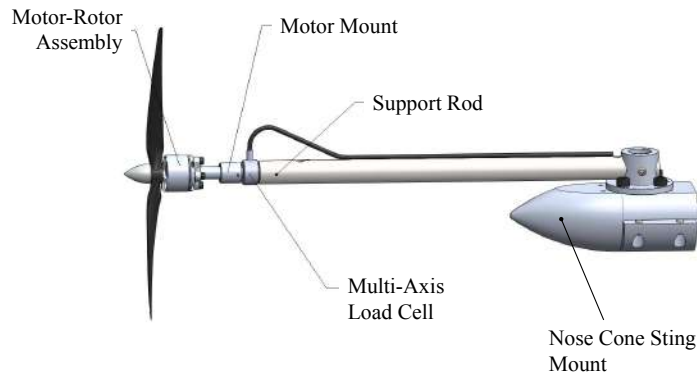
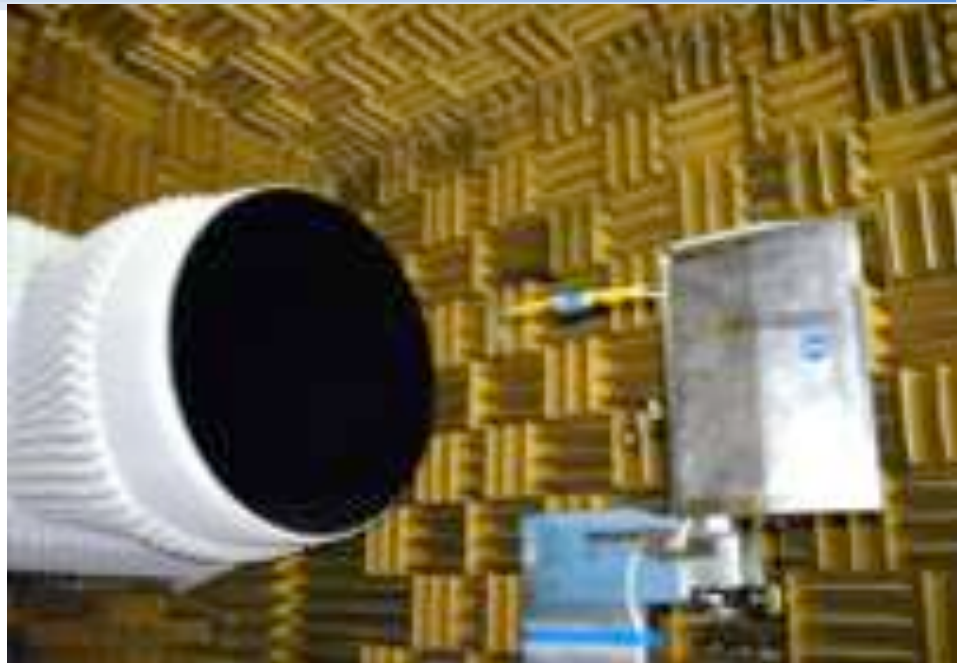
- ✓ Propeller Performance
- ✓ Far-field Acoustics



LAVA uRANS simulation at 5400 RPM

# Isolated UAS Rotor in Hover Validation

<b>Zawodny and Haskin (AIAA-2017-3709)</b>	
Rotor Span R	0.1905 [m]
Microphones (M1-M5)	10R
Considered RPM	5400



- ✓ Experiments conducted at NASA Langley LSAWT as well as in the Structural Acoustics Loads and Transmission (SALT) anechoic chamber.
- ✓ Motor-Rotor Assembly as well as Mount and Support structure not considered in simulations.

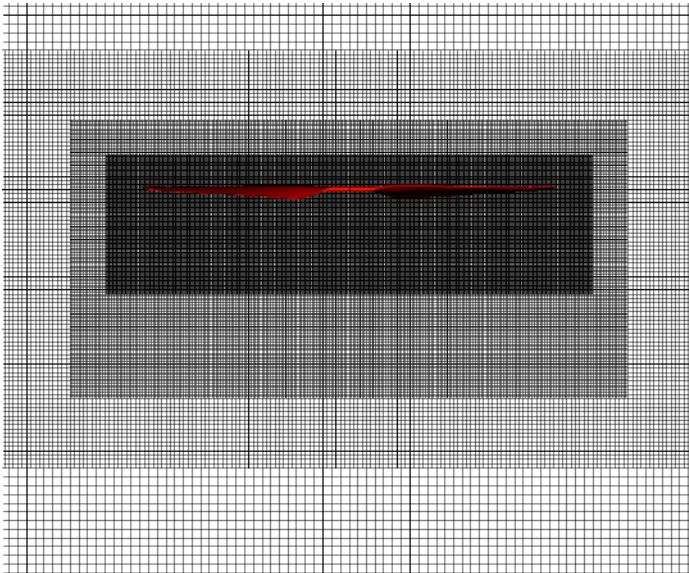
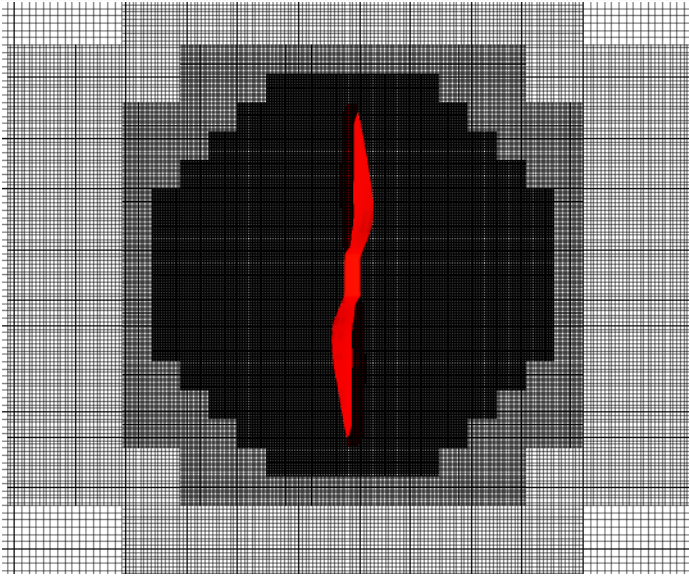
# LAVA Cartesian Methods



Lattice Boltzmann  
(LBM – EMRT)

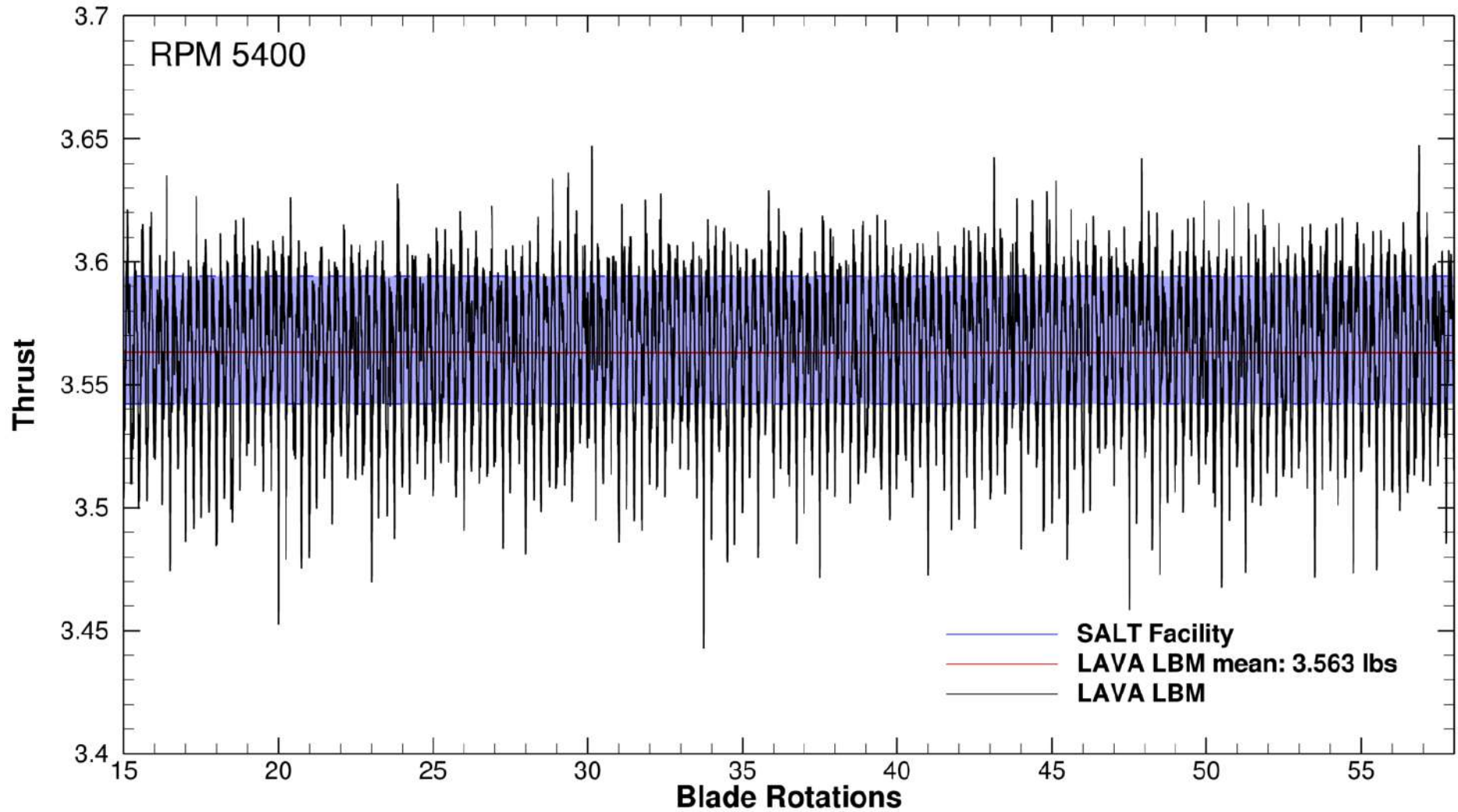
Navier-Stokes  
(NS – WENO6)

- ✓ Refinement ratio of 2:1
- ✓ Very Coarse : 40% tip chord ( 8lev)
- ✓ Coarse : 20% tip chord ( 9lev)
- ✓ Medium : 10% tip chord (10lev)
- ✓ Fine : 5% tip chord (11lev)



Isocontour of Q-criterion colored by Pressure. Simulation on medium Cartesian mesh.

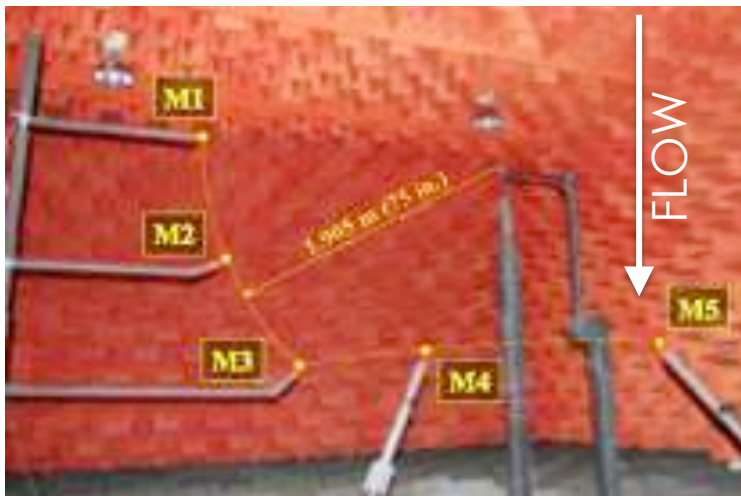
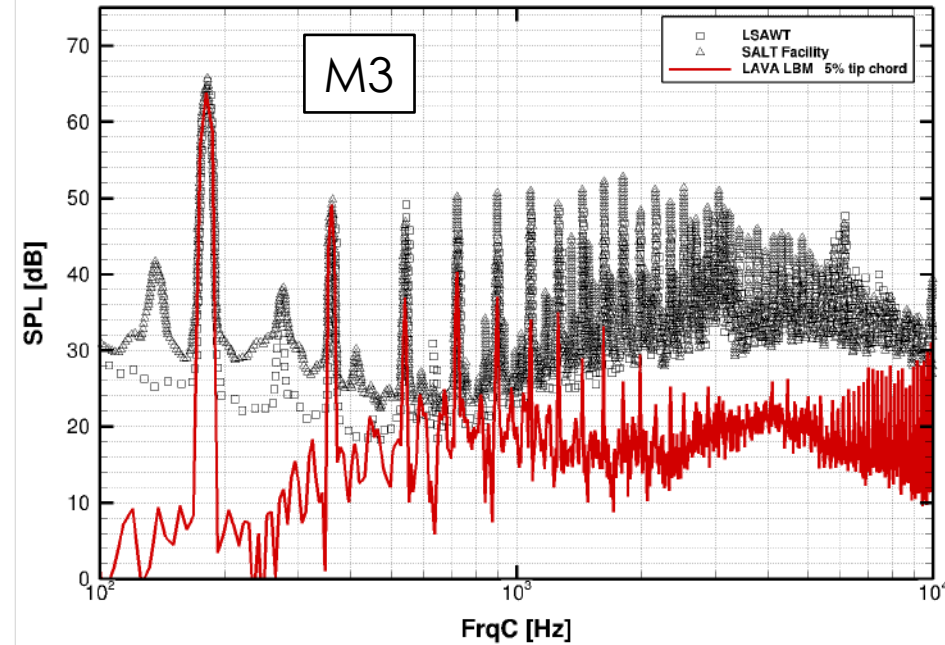
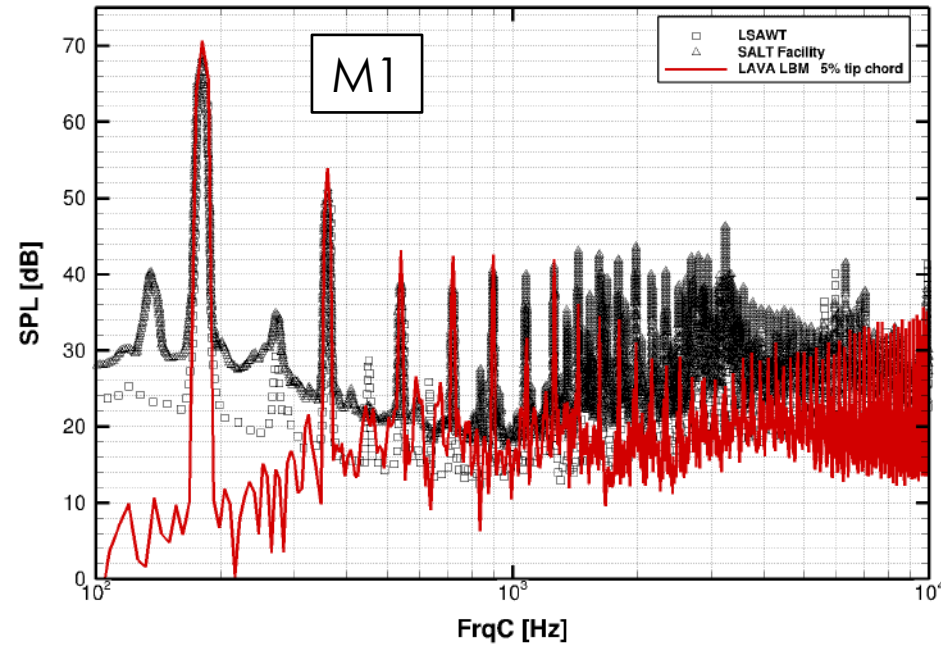
# Lattice Boltzmann Method Rotor Performance at 5400 RPM



- ✓ Excellent agreement with experimental measurements
- ✓ Differences ( $< 1\%$ ) well within measurement uncertainty (highlighted in blue)

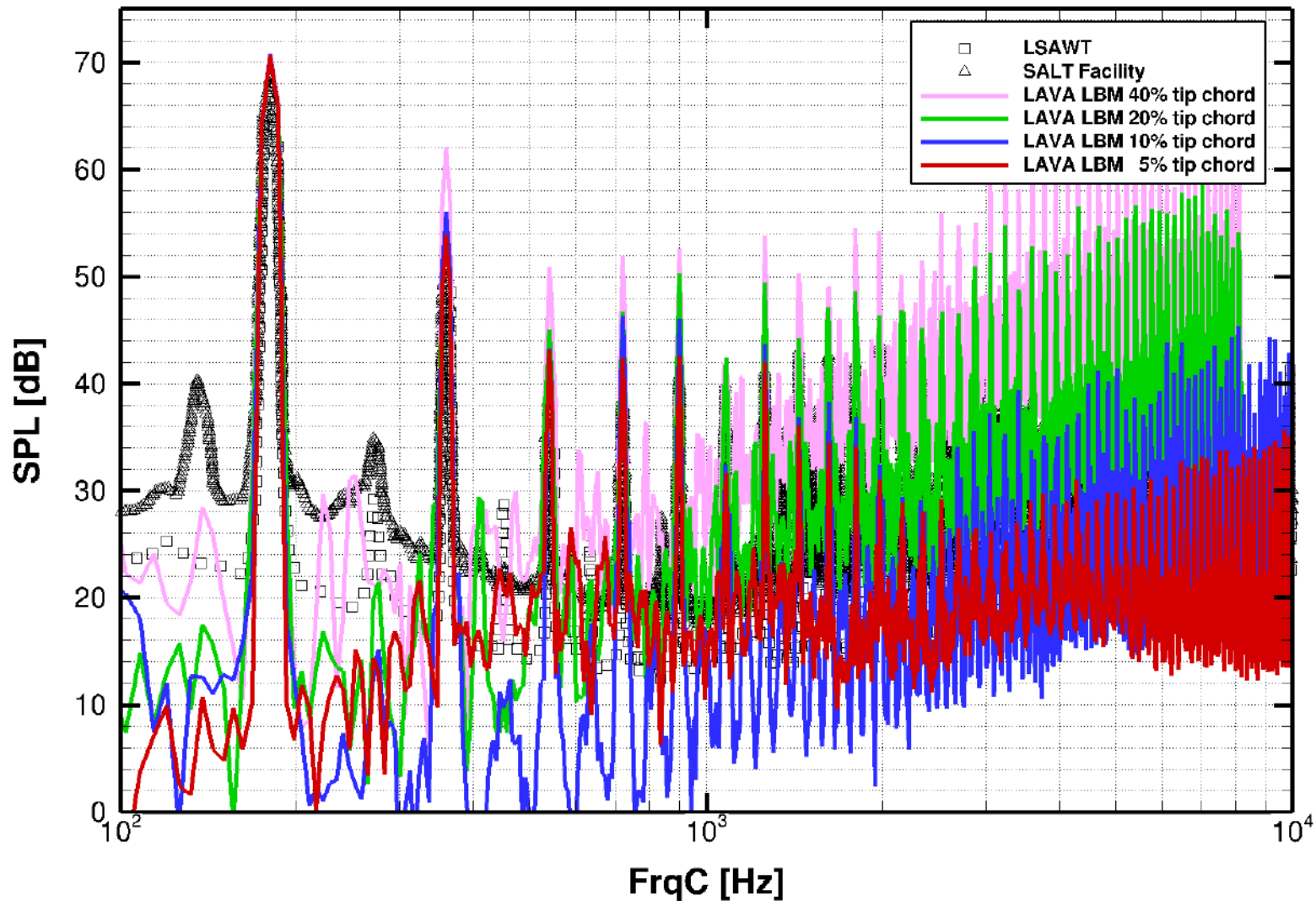
# Lattice Boltzmann Method

## Farfield Noise – SPL Spectrum for Observer M1 & M3



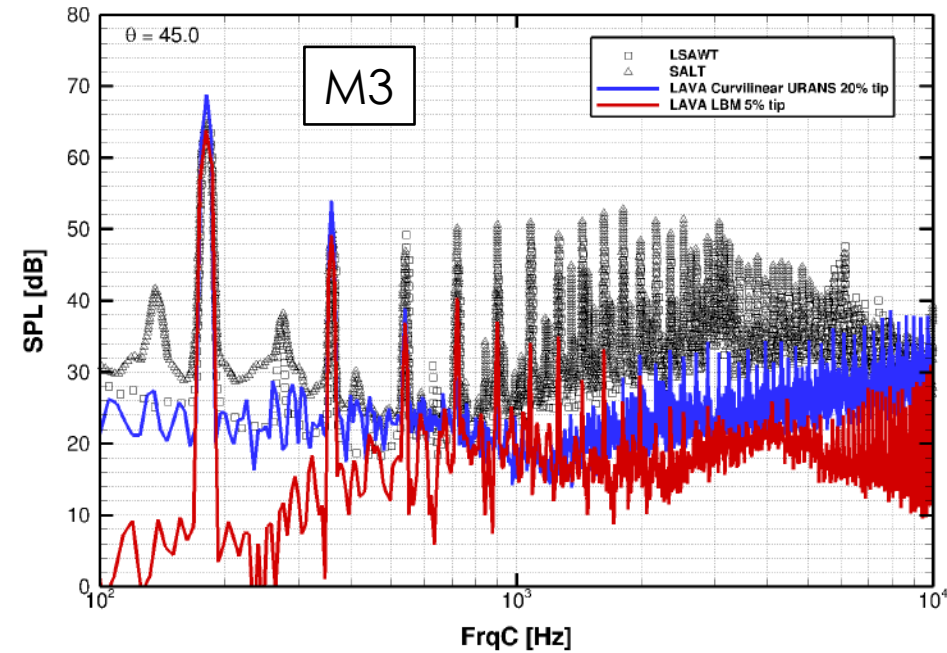
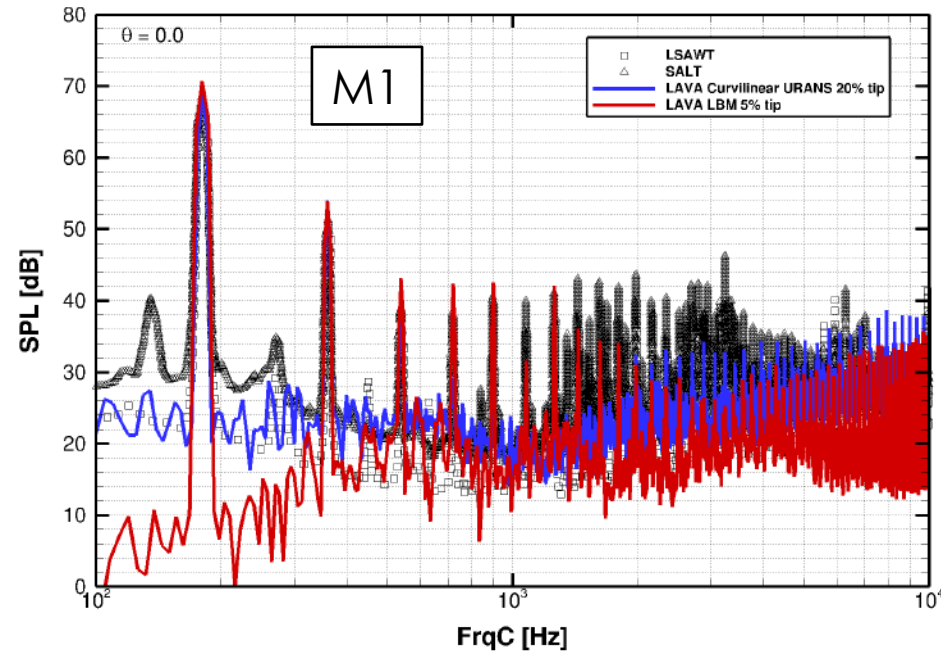
- ✓ Excellent agreement with BPF1-BPF5 for M1 (0.0°) microphone location
- ✓ Excellent agreement with BPF1 & BPF2 for M3 (45.0°)
- ✓ Different FWH formulations (permeable and impermeable) currently under investigation

# Lattice Boltzmann Method Farfield Noise – Mesh Refinement Study



- ✓ Consistent agreement for BPF1 on all mesh levels, BPF2 more sensitive.
- ✓ Good agreement for BPF 1 even on very coarse mesh.

# Comparison between the Approaches



- ✓ Consistent prediction using all three approaches
- ✓ Computational efficiency and complete absence of manual volume mesh generation key advantage of LBM
- ✓ Manual meshing efforts increase significantly upon considering installation effects (e.g. full Quadcopter or tiltwing urban air taxis)

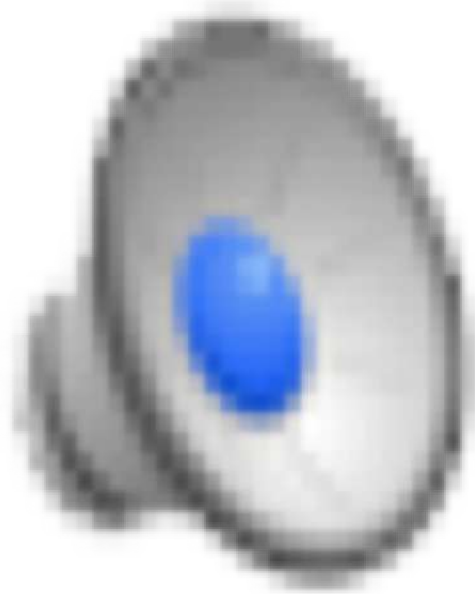


# Summary



LAVA Lattice Boltzmann Solver has made significant progress towards becoming a work-horse for NASA mission critical applications:

- Ultra-high performance without any compromise in fidelity
- Completely automated workflow without labor intensive mesh generation



# Acknowledgments



- ✓ This work was partially supported by the NASA ARMD's Transformational Tools and Technologies (T<sup>3</sup>), Advanced Air Transport Technology (AATT), Revolutionary Vertical Lift Technology (RVLT) projects
- ✓ Computer time provided by NASA Advanced Supercomputing (NAS) facility at NASA Ames Research Center

# Questions?





✓ All simulations performed on NASA Pleiades Cluster using Intel Xeon E5-2680v4

LAVA curvilinear ZDES Mode 3	:	240 CPUh/CTU	2.5x slower
LAVA LBM-LES	:	614 CPUh/CTU	
<i>Exa Powerflow LBM-VLES<sup>1</sup></i>	:	<i>540 CPUh/CTU</i>	very close to LAVA-LBM timings
LAVA curvilinear ZDES Mode 3	:	$\Delta t = 1.8E^{-5}$	39x smaller
LAVA LBM-LES	:	$\Delta t = 4.6E^{-7}$	
LAVA curvilinear ZDES Mode 3	:	11.3M grid points	9x more
Lattice LBM-LES	:	105M grid points	

<sup>1</sup>Duda and Fares. Application of a Lattice-Boltzmann Method to the Separated flow over the NASA hump. (AIAA-2016-1836)