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Scheduling Workforce Relief Breaks In Advance Versus In Real-Time

Abstract

This paper focuses upon employee rest breaks, or reliefs, in workforce scheduling. Historically, the workforce scheduling literature has largely ignored reliefs, as less than 18% of the 64 papers we surveyed scheduled reliefs. The argument has been that one need not schedule reliefs in advance, since they can easily be scheduled in real-time. We find this argument to be flawed. We show that failing to schedule reliefs in advance will have one of two undesirable outcomes. First, there will be a less profitable deployment of labor should all reliefs actually be taken in real-time. Second, if some reliefs are never assigned or if relief-timing restrictions are relaxed so that more reliefs may be assigned in real-time, there will be a disgruntled and less productive workforce and perhaps violations of contractual obligations. Our findings are supported by anecdotal evidence drawn from commercial labor scheduling software.

Keywords

manpower planning, scheduling, relief breaks

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SCHEDULING WORKFORCE RELIEF BREAKS IN ADVANCE VERSUS IN REAL-TIME

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Abstract

This paper focuses upon employee rest breaks, or reliefs, in workforce scheduling. Historically, the workforce scheduling literature has largely ignored reliefs, as less than 18% of the 64 papers we surveyed scheduled reliefs. The argument has been that one need not schedule reliefs in advance, since they can easily be scheduled in real-time. We find this argument to be flawed. We show that failing to schedule reliefs in advance will have one of two undesirable outcomes. First, there will be a less profitable deployment of labor should all reliefs actually be taken in real-time. Second, if some reliefs are never assigned or if relief-timing restrictions are relaxed so that more reliefs may be assigned in real-time, there will be a disgruntled and less productive workforce and perhaps violations of contractual obligations. Our findings are supported by anecdotal evidence drawn from commercial labor scheduling software.

Keywords

Manpower planning; Scheduling; Relief breaks

Scheduling Workforce Relief Breaks In Advance Versus In Real-Time

1. Introduction

Managers of services such as customer contact (call-in) centers, grocery stores, emergency rooms, and restaurants typically have faced uncertain levels of customer demand during various times of the day. Today, even businesses such as airports with largely reservation-based demand face unpredictability in customer demand at their various services. For example, lines at the ticket counter and the subsequent lines for security screening depend on when and how many passengers initially opt to check their baggage. To improve the customer service levels while minimizing labor, managers like the option of adjusting staffing in real-time. Typical strategies are allowing surplus workers take their break or go home early if demand is lower than expected or keeping workers longer or postponing breaks if demand is higher than expected (Thompson, 1999b). In order to gain this flexibility, managers commonly schedule coffee breaks or reliefs (short breaks) in advance and then make adjustments during the work day. As these reliefs and other breaks are typically required in most labor contracts, it is important to look at how well these strategies work in achieving the objectives of meeting customer demand while minimizing labor costs and providing for the required breaks. Towards this goal, this paper compares two methods of relief scheduling, in-advance and real-time, on the relevant measures of cost and percentage of assigned breaks.

Workforce scheduling is comprised of four distinct tasks (Thompson, 1993). Task one (FORECAST) forecasts customer demand for the service (Thompson, 1998a). Task two (TRANSLATE) translates the forecasts of customer demand into employee requirements, using, as one input, the value that customers place on good, quick service (Thompson, 1998b). Task three (SCHEDULE) develops a workforce schedule that, ideally, only has employees working when they are necessary to deliver the service (Thompson, 1999a). Task four (CONTROL) controls the delivery of the schedule in real-time (Thompson, 1999b). CONTROL is necessary since actual customer demand rarely equals that forecast, and because the employees may fail to perform as scheduled. For example, employees may be sick or late, or they may have to stay home to care for a sick child. FORECAST, TRANSLATE and SCHEDULE are planning activities, while CONTROL is a control activity.

There is an extensive literature on workforce scheduling. The primary reasons for this interest are that workforce scheduling is a difficult problem facing managers of service delivery systems and the fact that labor is often the greatest expense under managerial control. The majority of the literature has focused on SCHEDULE (Beaumont, 1997; Bechtold et al., 1991; Bechtold and Jacobs, 1990; Brusco and Jacobs, 1993, 1998; Easton and Rossin, 1991; Li et al., 1991; Loucks and Jacobs, 1991; Mabert and Showalter, 1990; Thompson, 1990, 1992). Several papers have addressed TRANSLATE or the linkage between TRANSLATE and SCHEDULE (Goodale and Tunc, 1998; Goodale et al., 2003a, b; Thompson, 1993, 1995b, 2004). However, the literature on CONTROL is scant (the

38 exceptions being Hur et al., 2004; Thompson, 1999b). This is despite the fact that CONTROL is
 39 crucial to efficient delivery of the service. A service system whose manager performs FORECAST,
 40 TRANSLATE, and SCHEDULE very well, but CONTROL poorly, will likely have a lower level of
 41 service at a higher cost than a system who has a manager that is particularly adept at CONTROL.

42 In this paper, we examine the scheduling of reliefs—breaks of 15 minutes or less (typically
 43 the ‘‘coffee break’’). As shown in Table 1, reliefs have largely been ignored in the workforce
 44 scheduling literature, with under 15% of the 75 papers we surveyed incorporating reliefs. The offered
 45 rationale is that they can be taken in real-time; that is, dealt with during the work day. Undoubtedly,
 46 leaving the scheduling of reliefs solely to real-time increases the difficulty of performing CONTROL
 47 well. Also, we believe that deferring the scheduling of reliefs to CONTROL offers a convenient
 48 means of avoiding the increase in problem complexity that reliefs pose. For example, the problem
 49 environment we describe in Section 3 contains 89,651 unique shifts when reliefs are considered, but
 50 only 3566 unique shifts when reliefs are ignored. Consider the effect of this difference on problem
 51 complexity for a work schedule containing 50 shifts. Assume, for the sake of illustration, that 0.01%
 52 of the possible combinations of 50 shifts without reliefs are feasible schedules, but that only
 53 0.000000000001% of the possible combinations of 50 shifts with reliefs are feasible schedules. There
 54 are then $0.0001 * (3566)^{50} = 4.065E+173$ feasible solutions when reliefs are not scheduled, while
 55 there are $0.00000000000001 * (89,651)^{50} = 4.244E+233$ feasible solutions when reliefs are
 56 scheduled, or $1.044E + 60$ times as many solutions. Clearly, reliefs greatly increase problem
 57 complexity.

58 A key assumption in the paper is that management desires that employees receive reliefs.
 59 There are two drivers for this assumption. First, contractual obligations often require that employees
 60 be given reliefs. Second, there is a body of literature showing the benefit of reliefs on productivity (for
 61 example, Janaro and Bechtold, 1985; Morgan and Pitts, 1985). Given our assumption, if reliefs are not
 62 scheduled in advance, they must be taken in real-time.

63 The objective of this paper is to conclusively determine whether reliefs should be scheduled
 64 in advance, or scheduled in real-time.¹ That is, we wish to determine whether or not researchers will
 65 have to confront the growth in problem complexity that reliefs pose, or if they may, in good
 66 conscience, continue to avoid scheduling reliefs. The paper thus offers one of the first investigations
 67 into a CONTROL-related workforce scheduling issue in an environment with overlapping shifts
 68 (shifts that can start at any time of the day rather than predefined day, swing, and graveyard shifts).
 69 The criterion used in the investigation is schedule cost, i.e., cost required to schedule employees to
 70 meet a specified service criterion.

¹ A related issue is whether reliefs should be scheduled in advance, but rescheduled in real-time. This investigation is beyond the scope of the current paper.

71 The structure of the paper is as follows. Section 2 presents the formulation of the workforce
 72 scheduling problem that we employ. Section 3 describes a set of test problems we developed and the
 73 approaches we used to evaluate the outcomes of scheduling and failing to schedule reliefs in advance.
 74 Section 4 presents and discusses the results of the investigation. Finally, Section 5 presents our
 75 conclusions, including suggestions for additional research.

76

77 **2. The workforce scheduling problem**

78 Throughout the investigation, we use the representation of the workforce scheduling problem
 79 presented by Dantzig (1954). His representation, which we call WSP, is

$$80 \quad \text{Min } Z = \sum_{t \in T} c_t x_t \quad (1)$$

$$82 \quad \text{subject to } \sum_{t \in T} a_{tp} x_t \geq r_p \text{ for } p \in P \quad (2)$$

$$84 \quad x_t \geq 0 \text{ and integer for } t \in T, \quad (3)$$

86 where

87 P = set of planning intervals in the daily operating horizon;

88 T = set of unique shifts that can be scheduled

89 x_t = number of employees working shift t

90 $a_{tp} = \begin{cases} 1 & \text{if period } p \text{ is a working period of shift } t \\ & \text{otherwise} \end{cases}$

91 r_p = number of employees needed in period p to deliver the specified level of service.

92 WSP's objective (1) measures the total cost associated with the schedule. Constraint set (2) ensures
 93 that sufficient staff are present in each planning period to deliver the specified level of customer
 94 service. Constraint set (3) imposes the integer nature of the variables.

95 Breaks are incorporated into this model ((1)–(3)) via the a_{tp} coefficients, where a_{tp} takes a
 96 value of one in a working period of a shift and a value of zero otherwise. For example, consider the
 97 case of a daily planning horizon of sixty four 15-minute planning intervals and a 6-hour shift that
 98 starts in period one and that has single-period reliefs in its 5th and 18th periods and a four-period meal
 99 break beginning in its 10th period. The a_{tp} coefficients for this shift would be four consecutive ones
 100 (for the first work stretch), a zero (for the first relief), four consecutive ones (for the second work
 101 stretch), four consecutive zeros (for the meal break), four consecutive ones (for the third work
 102 stretch), a zero (for the second relief), six consecutive ones (for the fourth and final work stretch), and,

103 finally, 40 consecutive zeros (for the non-work periods from the end of the shift to the end of the
104 planning horizon).²

105 With WSP, r_p is the ideal staff size for period p . A perfectly-matched schedule will exactly
106 match capacity to demand by providing the ideal number of staff in each period. All perfectly-
107 matched schedules are not necessarily optimal, however. For example, since we assume that reliefs
108 are paid, a perfectly-matched schedule with 20 shifts (with two reliefs per shift) would typically be
109 less costly than a perfectly-matched schedule with 21 shifts (with two reliefs per shift), since the latter
110 includes 42 periods of paid, but unproductive relief time while the former included only 40 such
111 periods. Further, an optimal schedule is not necessarily perfectly-matched, since limited flexibility, by
112 precluding satisfying the ideal staffing levels in all periods, can lead to over scheduling of labor.

113

114 **3. An experiment in relief scheduling**

115 In this section we describe the set of problems we developed to investigate relief scheduling, and the
116 four approaches to relief scheduling that we evaluated.

117

118 **3.1. Test environment**

119 This subsection describes a set of 100 test problems we developed to determine whether
120 reliefs should be scheduled in advance or deferred to real-time. In developing the test problems we
121 strove to create problems representative of those occurring in a diverse range of service environments.
122 Each problem has a 16-hour operating day broken into 64 15-minute intervals.

123 The problems varied on three dimensions: the “shape” of the ideal staffing levels (four factor levels);
124 the mean ideal staffing levels (five levels); and the variation in the ideal staffing levels across periods
125 (five levels). The four “shapes” had one, two, three, and numerous daily peaks in the ideal staffing
126 levels. One daily peak in demand often occurs in retail facilities on weekends. Two daily peaks are
127 often observed in service environments where demand is related to commuters; for example, drop-off
128 and pick-up demand at dry cleaners. Three daily demand peaks commonly occur in restaurants.

129 Numerous daily peaks are observed in service environments where there are multiple components of
130 customer demand, for example, counter staffing requirements in airport terminals.

131 The five levels of mean ideal staffing levels were 5, 10, 20, 40, and 80 employees. The lower
132 staffing levels can be seen in small grocery stores, while the higher levels can be observed in
133 modestly sized telemarketing operations. The five levels of variation in ideal staffing levels had
134 amplitudes of $\pm 20\%$, 40%, 60%, 80%, and 100% of the mean ideal levels. The rationale for including
135 a range of variability is that higher variability makes it harder to provide the ideal number of staff in
136 every period. As such, high variability in the ideal staffing levels should offer greater opportunities for
137 the real-time slotting of reliefs into periods of surplus staffing. Fig. 1 illustrates the employee

² This example is taken from the first shift shown in Table 3.

138 requirements in the eight problems with a mean requirement of 20 employees and lowest and highest
139 variability in the ideal staffing levels. The staffing patterns we considered are consistent with those
140 from a number of earlier studies (see, for example, Thompson, 1996b, 1997).

141 For each of the 100 problems, the operative restrictions on allowable shifts were as follows:
142 shifts are between 6 and 9 hours in length, including an hour-long, unpaid meal break. The meal break
143 is preceded and followed by at least 2.25 and no more than 5 hours of paid time. During each pre- and
144 post-meal break work-stretch, a paid, 15-minute relief is required. Regardless of whether the reliefs
145 are scheduled in advance or real-time, each relief must be preceded and followed by at least 1 hour
146 and no more than 3.75 hours of work.

147 These shift-defining restrictions, coupled with the 64-planning period operating day, resulted
148 in a total of 89,651 unique shifts when reliefs are considered, and a total of 3566 unique shifts when
149 reliefs are ignored. The number of possible workforce schedules is appreciably larger than these
150 numbers, however, as discussed in the introduction, and so the reliefs greatly increase problem
151 complexity.

152

153 **3.2. Relief scheduling approaches**

154 To investigate the issue of whether reliefs should be scheduled in advance or in real-time, we
155 used three approaches to relief scheduling. The first, Relief Scheduling Approach One, or RSA1, is
156 the only approach that schedules reliefs in advance (i.e., simultaneously with shifts). That is, since
157 RSA1 includes reliefs when solving WSP, the workforce schedule is developed while explicitly
158 considering the need for reliefs. For each problem, RSA1 provides the basic schedule against which
159 the other schedules are compared.

160 The second approach, RSA2, does not schedule reliefs either in advance or in real-time. That
161 is, RSA2 solves WSP ignoring reliefs. RSA2's solutions are thus equivalent to initial workforce
162 schedules found in environments where relief scheduling occurs solely in real-time. By comparing
163 RSA2's schedules to those of RSA1, we can determine if there are fundamental differences between
164 schedules developed considering the need for reliefs and those developed without consideration of
165 reliefs.

166 We developed the third approach to further investigate the effect of failing to schedule reliefs
167 in advance. This approach attempts to assign reliefs to previously developed schedules that disregard
168 reliefs. That is, approach three (RSA3) attempts to insert reliefs into the schedule found using RSA2.
169 RSA3 maximizes the number of reliefs that can be assigned to RSA2's schedule, without scheduling
170 fewer than the ideal number of staff required in any period. Since RSA3 only allows the relief timing
171 to vary, it has the effect of slotting breaks into periods of surplus staffing—those periods with more
172 than the ideal number of staff. By examining the number of reliefs that can be assigned into periods of
173 surplus staffing, we can determine the validity of an argument like “one need not schedule reliefs in

174 advance, since reliefs can always be taken in periods of surplus staffing.’’ As we shall see, the ability
 175 to slot reliefs into periods of surplus staffing is curtailed by the timing and amount of surplus staffing.
 176 To match relief to shifts in RSA3, we used the following Relief Assignment Model, or RAM:

$$177 \quad \text{Max} \quad Z = \sum_{j \in S} \left(\sum_{b \in B_j^1} y_{jb}^1 + \sum_{\{b \in B_j^2\}} y_{jb}^2 \right)$$

178 (4)

179 subject to

$$180 \quad \sum_{j \in S} \left(\sum_{\{b | b \in B_j^1, b=p\}} y_{jb}^1 + \sum_{\{b | b \in B_j^2, b=p\}} y_{jb}^2 \right) \leq v_p \text{ for } p \in P,$$

181 (5)

$$182 \quad \sum_{b \in B_j^1} y_{jb}^1 \leq 1 \text{ for } j \in S,$$

183 (6)

$$184 \quad \sum_{b \in B_j^2} y_{jb}^2 \leq 1 \text{ for } j \in S,$$

185 (7)

$$186 \quad y_{jb}^1 = \{0,1\} \text{ for } j \in S, b \in B_j^1,$$

187 (8)

$$188 \quad y_{jb}^2 = \{0,1\} \text{ for } j \in S, b \in B_j^2,$$

189 (9)

190 where

191 S = set of shifts scheduled in the solution to RSA2;

192 B_j^1 = set of valid periods for the first relief of scheduled shift j ;

193 B_j^2 = set of valid periods for the second relief of scheduled shift j ;

194 $y_{jb}^1 = \begin{cases} 1 & \text{if relief 1 of scheduled shift } j \text{ is assigned to period } b; \\ 0 & \text{otherwise} \end{cases}$

195 v_p = surplus of staffing in period p from the solution to RSA1.

196 RAM’s objective (4) is to maximize the number of reliefs assigned. Constraint set 5 ensures that
 197 reliefs can only be scheduled into periods of surplus staffing from the solution of RSA2. Constraint
 198 sets (6) and (7) ensure that no more than one instance of the first and second reliefs are assigned for
 199 each scheduled shift. Finally, constraint sets (8) and (9) impose the binary nature of the relief
 200 assignment variables.
 201

202 We used the commercial software combination of GAMS (Brooke et al., 1992) and OSL
 203 (IBM Corporation, 1991), respectively to generate and solve RAM and the variants of WSP required

204 by RSA1 through RSA3. We limited the solution times to 3 minutes on the equivalent of a Pentium
205 IV-2.0 GHz based personal computer, and used the best integer solution obtained in that interval if the
206 best solution was not verified as being optimal.

207

208 **4. Results and discussion**

209 We begin the presentation of results by showing and discussing the outcomes for the first problem,
210 and then move to a summary of the outcomes for all 100 problems.

211

212 **4.1. Problem one**

213 Table 2 presents the ideal staffing levels for problem one. As we noted earlier, the ideal staff
214 size is the minimum number of employees that delivers the specified service level. Tables 3–5 present
215 the solutions to RSA1 through RSA3. Table 3 shows that RSA1’s optimal schedule contained 14
216 shifts and 9 employee-periods of surplus staffing. Table 4 shows the optimal solution for RSA2. This
217 schedule contains 14 shifts and 27 periods of surplus staffing. One might at first think that 27 of the
218 28 necessary reliefs (=14 shifts times 2 reliefs per shift) for RSA2’s schedule could be assigned to the
219 periods with surplus staffing. The optimal solution for RSA3, presented in Table 5, shows that this is
220 not possible. RSA3’s solution shows that only 18 of the 28 necessary reliefs can be assigned to
221 periods of surplus staffing (due to relief assignment rule constraints), leaving surplus staffing of 9
222 (=27–19) employee-periods and 10 unassigned breaks.

223 Taken as a whole, the schedules illustrated in Tables 3–5 show that there are two noticeable
224 differences between an optimal schedule developed considering reliefs (RSA1’s schedule in Table 3)
225 and a schedule developed for the same problem but in ignorance of reliefs (RSA2’s schedule in Table
226 4). First, since it fails to recognize the lost productive time, the latter approach schedules insufficient
227 work time to cover all the necessary breaks. Second, the times at which the surplus work was
228 scheduled does not match very well with the times that breaks must be taken. Indeed, there was one
229 shift (shift 8 in Table 5) that actually would not have received ANY breaks when breaks were not
230 scheduled in advance. The combination of these shortcomings means that if one MUST give breaks,
231 they WILL result in reduced levels of customer service, since many of the breaks will have to be
232 scheduled at times when surpluses do not occur. Moreover, since too little productive time is
233 scheduled, the employees would never really be able to compensate for the periods with reduced
234 service levels. As we shall see in the next subsection, the results on problem one are very
235 representative of the results across all 100 problems.

236

237 **4.2. All problems**

238 Table 6 summarizes the results of the complete investigation. For each model, it reports the
239 mean schedule cost, MSC; the percentage of reliefs that are assigned, PRA; and the average number

240 of shifts in the schedule, ANS. Table 6 categorizes the results based on the number of daily peaks in
 241 the ideal staffing levels.

242 The complete results in Table 6 show distinct similarities to the results on problem one.
 243 Clearly, there are substantial differences in schedules developed with regard to reliefs (using RSA1)
 244 and those that are developed without regard to reliefs (using RSA2). First, RSA2 tends to schedule
 245 more shifts than RSA1. This result is not surprising, in that RSA2 ignores the fixed charge of paid, but
 246 unproductive relief time.³ However, the increased number of shifts increases the difficulty of real-
 247 time relief scheduling due to the increased number of required reliefs. One avenue we did not
 248 investigate is whether this increase in the number of scheduled shifts may be mitigated by exploiting
 249 the multiple optimal schedules that often exist in workforce schedules. Second, RSA2 fails to
 250 schedule enough labor to allow reliefs to be inserted entirely in periods of surplus staffing. Overall,
 251 only about 40% of the necessary reliefs can be inserted into periods of surplus staffing (see the results
 252 for RSA3). The problems vary greatly in the percentage of reliefs that can be assigned in periods of
 253 surplus staffing—averaging between 12% and 78% of reliefs assigned across the problem categories.
 254 Third, RSA2 frequently fails to schedule enough labor to allow all necessary reliefs to be inserted
 255 without having fewer than the minimum acceptable staff size in some period.

256 Recall that a period's ideal staffing level is the smallest number of staff that will deliver the
 257 ideal level of customer service. Having fewer than the ideal number of staff means that the staff will
 258 not be able to keep pace with customers arrivals, leading to long lines, long delays for service, and
 259 very unprofitable operations. Clearly, then, it is problematic to assign reliefs to schedules developed
 260 without regard to them.

261 Relaxing the relief timing restrictions is one way of increasing the number of reliefs RSA3
 262 can assign in real-time. Consider one scenario where the original relief timing restrictions are valid
 263 (based on contractual obligations, management and employee desires, and productivity
 264 considerations) and a second scenario where the original relief timing restrictions are overly tight (i.e.,
 265 invalid). In the former scenario, relaxing the restrictions risks a less productive and disgruntled
 266 workforce and, perhaps, contract violations. In the latter scenario, it is still unlikely that RSA3 will be
 267 able to assign the necessary 150% more reliefs than it previously assigned.⁴ If the relaxed relief
 268 timing restrictions are indeed valid, then it seems sensible to use these correct restrictions when
 269 developing a schedule that includes reliefs (RSA1).

270 Finally, we have heard the argument that scheduling reliefs is unimportant since demand in
 271 real-time will never be what is forecast. This logic has a major flaw. As the results with RSA3 show,

³ Schedules developed without regard to reliefs will be problematic even if reliefs are unpaid. This is because there is insufficient surplus staffing, at the right times, in which to slot the reliefs.

⁴ Since RSA2 only assigned 40% of the necessary reliefs, on average, 60% of the reliefs were unassigned. Thus 150% more reliefs must be assigned.

272 insufficient labor is generally scheduled when reliefs are ignored. For reliefs to be given in real-time,
273 without having fewer than the ideal staff size in any period, implies that demand forecasts generally
274 exceed actual demand (i.e., there is a particular type of forecast bias). Trying to correctly over-specify
275 demand forecasts so that sufficient but not excess labor is available in real-time to schedule reliefs
276 seems a very indirect and ineffective way of dealing with reliefs compared to scheduling them in
277 advance (and, if desired, rescheduling them in real-time).

278

279 **5. Conclusions**

280 Historically, the high level of flexibility inherent in work schedules with reliefs hindered the
281 search for optimal solutions to scheduling models. Development in the 1990s of implicit
282 representations of workforce scheduling problems (Bechtold and Jacobs, 1990; Thompson, 1995a) has
283 lessened this barrier. Indeed, optimal solutions to integer programming models that would require
284 over 89,000 variables in an explicit formulation often can be found in a few minutes on a PC using an
285 implicit model. With an implicit model we were able to evaluate alternative approaches to the relief
286 scheduling problem.

287 Commercial labor scheduling systems offer anecdotal evidence of the value in scheduling
288 breaks. Table 7 lists three vendors of commercial labor scheduling systems. To find the commercial
289 vendors, we went to the Yahoo URL listing labor management tools.⁵ From a list of approximately 20
290 companies, we examined their on-line documentation, looking for vendors offering tools with some
291 automated scheduling component (rather than simply an aid to manual scheduling). For such vendors,
292 we also attempted to determine whether their software had the capability to schedule breaks. In fact,
293 the three vendors listed in Table 7 not only were the only ones offering automated scheduling tools,
294 but their systems all scheduled breaks.

295 To summarize, it initially appears that it is better to ignore reliefs (i.e., because RSA2's
296 schedules are less costly than those of RSA1). However, the results show that failing to schedule
297 reliefs in advance will have one of the following undesirable outcomes. First, there will be a less
298 profitable deployment of labor, due to poor service, should all reliefs be assigned in real-time within
299 the established relief-timing restrictions (as shown by the results that RSA3 can schedule only 43% of
300 the necessary reliefs). Specifically, there will be too many shifts and insufficient total labor scheduled
301 when reliefs are ignored. With too many shifts scheduled, too many paid, non-work reliefs must be
302 scheduled, thus increasing costs. With insufficient labor scheduled, the reliefs cannot all be assigned
303 only in periods of surplus staffing, resulting in costly occurrences of short staffing. Second, if some
304 reliefs are not given, there will be a disgruntled and less productive workforce (as shown by the
305 results of RSA3, only about 40% of the required reliefs can be slotted into periods of surplus staffing).

⁵http://dir.yahoo.com/Business_and_Economy/Business_to_Business/Computers/Software/Business_Applications/Scheduling_and_Task_Management/Employee_Scheduling/

306 Third, more reliefs may be assigned in real-time if the relief timing restrictions are relaxed. However,
307 if the original restrictions are valid (based on contractual obligations, management and employee
308 desires, and productivity considerations), this also risks disgruntled and less productive employees
309 and possibly contractual obligations; while if the relaxed restrictions really are valid, then it makes
310 sense to use them when developing the schedule with reliefs. Only by scheduling reliefs in advance,
311 then, can the problems posed by real-time relief scheduling be avoided.

312 Our results illustrate the fallacy of the commonly held assumption that managers can schedule
313 reliefs in real-time with negligible impact on schedule profitability. This finding is consistent with a
314 recent study by Hur et al. (2004), who found that, in a fast service environment, real-time schedule
315 adjustments made by computer-based heuristics were more profitable than adjustments made by
316 experienced managers. Our finding has an exceedingly important implication for research on
317 workforce scheduling. To increase the realism of their work, researchers should incorporate relief
318 scheduling into the procedures they develop. Again, because reliefs were considered in less than 18%
319 of our sample of 64 published studies, the field has significant work to do moving forward to ensure
320 its relevance to practicing managers.

321 Future research also should evaluate strategies that managers use for real-time rescheduling of
322 reliefs. For example, in some industries, we have observed that managers schedule breaks in advance
323 but modify the timing of these breaks based on actual customer demand. Conceivably, managers can
324 further improve profitability by effective relief rescheduling in real-time.⁶

325

⁶ We wish to acknowledge the feedback provided by Michael Brusco on an earlier version of this paper.

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Table 1. Literature summary of reliefs (rest breaks) and meal breaks

Reference	No. breaks scheduled	Meal breaks scheduled	Reliefs (rest breaks) scheduled
Alfaresm (2000)	X		
Alvarez-Valdes et al. (1999)	X		
Aykin (2000)	X		
Bailey (1985)	X		
Bailey and Field (1985)		X	
Baker et al. (1972)	X		
Bard (2004)		X	
Bartholdi et al. (1981)		X	X
Beaumont (1997)		X	
Bechtold and Brusco (1995)	X		
Bechtold et al. (1991)		X	
Bechtold and Jacobs (1990)		X	
Bechtold et al. (1984)		X	X
Bechtold and Showalter (1985)		X	
Bechtold and Showalter (1987)		X	
Brusco and Jacobs (1993)		X	
Brusco and Jacobs (1998)	X		
Brusco and Jacobs (2000)		X	
Brusco and Jacobs (2001)		X	
Brusco and Johns (1995)		X	
Buffa et al. (1976)		X	X
Dantzig (1954)		X	
Easton and Rossin (1991)		X	
Easton and Mansour (1999)		X	
Goodale and Thompson (2004)		X	
Henderson and Berry (1976)		X	X
Henderson and Berry (1977)		X	X
Holloran and Byrn (1986)		X	X
Hur et al. (2004)		X	
Gaballa and Pierce (1979)		X	
Glover et al. (1984)		X	X
Goodale and Tunc (1998)	X		
Goodale et al. (2003a,b)	X		
Jacobs and Bechtold (1993)		X	
Janaro and Bechtold (1985)		X	X
Jaumard et al. (1998)	X		
Keith (1979)		X	X
Kolesar et al. (1975)		X	
Krajewski et al. (1980)		X	
Li et al. (1991)	X		
Loucks and Jacobs (1991)		X	

Reference	No. breaks scheduled	Meal breaks scheduled	Reliefs (rest breaks) scheduled
Mabert and Showalter (1990)		X	
Mabert and Watts (1982)	X		
McGinnis et al. (1978)	X		
Melachrinoudis and Olafsson (1995)	X		
Moondra (1976)		X	
Morris and Showalter (1983)		X	
Parker and Larsen (2003)	X		
Segal (1974)		X	X
Showalter et al. (1977)		X	
Showalter and Mabert (1989)		X	
Thompson (1990)		X	
Thompson (1992)		X	
Thompson (1993a)		X	
Thompson (1993b)		X	
Thompson (1995a)		X	
Thompson (1995b)		X	
Thompson (1996a)		X	
Thompson (1996b)		X	
Thompson (1996c)		X	
Thompson (1997)		X	
Vakharia et al. (1992)	X		
Vohra (1988)		X	
Wilson and Willis (1983)		X	X
Number of references (% of total)	16 (25.0)	48 (75.0)	11 (17.2)

Table 2. Ideal staff sizes by period for problem one

Period	ISL	Period	ISL	Period	ISL	Period	ISL
1	5	17	5	33	6	49	6
2	5	18	5	34	5	50	6
3	4	19	6	35	5	51	4
4	5	20	6	36	5/6	52	4
5	3	21	4	37	6	53	6
6	3	22	5	38	7	54	3
7	4	23	5	39	6	55	4/5
8	5	24	7	40	6	56	4
9	3	25	6	41	7	57	4
10	4	26	7	42	5	58	3
11	5	27	7	43	7	59	5
12	5	28	5	44	6	60	4
13	4	29	7	45	5	61	4
14	6	30	5	46	4	62	5
15	5	31	7	47	4	63	3
16	6	32	6	48	4	64	3

ISL = ideal staffing level.

Table 3. Optimal RSA1 solution to problem one

Per	Shift														ISS	ASS	NSS	
	1	2	3	4	5	6	7	8	9	10	11	12	13	14				
1	w	w	w	w	w											5	5	0
2	w	w	w	w	w											5	5	0
3	w	w	w	w	w											4	5	1
4	w	w	w	w	w											5	5	0
5	r	w	w	w	w											3	4	1
6	w	r	r	w	w											3	3	0
7	w	w	w	w	w											4	5	1
8	w	w	w	w	w											5	5	0
9	w	w	w	r	w											3	4	1
10	m	w	w	w	w											4	4	0
11	m	w	w	w	w	w										5	5	0
12	m	w	w	w	w	w										5	5	0
13	m	w	w	w	r	w										4	4	0
14	w	w	w	w	w	w										6	6	0
15	w	m	w	w	w	w										5	5	0
16	w	m	w	w	w	w	w									6	6	0
17	w	m	w	w	w	r	w									5	5	0
18	r	m	w	w	w	w	w									5	5	0
19	w	w	m	w	w	w	w									6	6	0
20	w	w	m	m	w	w	w	w								6	6	0
21	w	w	m	m	m	w	r	w								4	4	0
22	w	w	m	m	m	w	w	w								5	5	0
23	w	r	w	m	m	w	w	w								5	5	0
24	w	w	w	w	m	w	w	w								7	7	0
25		w	w	w	w	w	w	r								6	6	0
26		w	w	w	w	w	w	w								7	7	0
27		w	w	w	w	w	w	w								7	7	0
28			r	w	w	w	w	w								5	5	0
29			w	w	w	m	w	w	w	w						7	7	0
30			w	r	r	m	w	w	w	w						5	5	0
31			w	w	w	m	w	w	w	w						7	7	0
32			w	w	w	m	m	w	w	w						6	6	0
33				w	w	w	m	w	w	w						6	6	0
34				w	w	w	m	m	r	r	w	w				5	5	0
35					w	w	m	m	w	w	w	w				5	5	0
36						w	w	m	w	w	w	w				5/6	6	0
37						w	w	m	w	w	w	w				6	6	0
38						w	w	w	w	w	w	w				7	7	0
39							w	w	w	w	w	r	w			6	6	0
40							r	w	w	w	w	w	r	w		6	6	0

Per	Shift														ISS	ASS	NSS	
	1	2	3	4	5	6	7	8	9	10	11	12	13	14				
41						w	w	w	m	w	w	w	w			7	7	0
42						w	r	r	m	w	w	w	w			5	5	0
43						w	w	w	m	w	w	w	w			7	7	0
44						w	w	w	m	w	w	w	r			6	6	0
45						w	w	w	w	m	m	m	w			5	5	0
46							w	w	w	m	m	m	w			4	4	0
47							w	w	w	m	m	m	w			4	4	0
48							w	w	w	m	m	m	w			4	4	0
49							w	w	w	w	w	w	m			6	6	0
50							w	w	w	w	w	w	m			6	6	0
51								w	w	w	w	w	m			4	5	1
52								w	w	w	w	w	m			4	5	1
53								w	w	w	w	w	w			6	6	0
54									r	r	w	w	w			3	3	0
55									w	w	w	w	w			4/5	5	0
56									w	w	r	w	w			4	4	0
57									w	w	w	r	w			4	4	0
58									w	w	w	w	r			3	4	1
59									w	w	w	w	w			5	5	0
60									w	w	w	w	w			4	5	1
61									w	w	w	w	w			4	5	1
62									w	w	w	w	w			5	5	0
63											w	w	w			3	3	0
64											w	w	w			3	3	0

RSA1 develops a workforce schedule that includes reliefs. Per = planning period; w = work period; m = meal period; r = relief; ISS = ideal staff size; ASS = actual staff size; NSS = net staff size (=ASS – ISS).

Table 4. Optimal RSA2 solution to problem one

Per	Shift														ISS	ASS	NSS
	1	2	3	4	5	6	7	8	9	10	11	12	13	14			
1	w	w	w	w	w										5	5	0
2	w	w	w	w	w										5	5	0
3	w	w	w	w	w										4	5	1
4	w	w	w	w	w										5	5	0
5	w	w	w	w	w										3	5	2
6	w	w	w	w	w										3	5	2
7	w	w	w	w	w										4	5	1
8	w	w	w	w	w										5	5	0
9	w	w	w	w	w										3	5	2
10	m	w	w	w	w										4	4	0
11	m	w	w	w	w	w									5	5	0
12	m	m	w	w	w	w	w								5	5	0
13	m	m	w	w	w	w	w								4	5	1
14	w	m	w	w	w	w	w								6	6	0
15	w	m	m	w	w	w	w								5	5	0
16	w	w	m	w	w	w	w								6	6	0
17	w	w	m	w	w	w	w								5	6	1
18	w	w	m	m	w	w	w								5	5	0
19	w	w	w	m	w	w	w								6	6	0
20	w	w	w	m	w	w	w								6	6	0
21	w	w	w	m	m	w	w								4	5	1
22	w	w	w	w	m	m	w								5	5	0
23	w	w	w	w	m	m	w								5	5	0
24	w	w	w	w	m	m	w	w	w						7	7	0
25		w	w	w	w	m	m	w	w						6	6	0
26		w	w	w	w	w	m	w	w						7	7	0
27		w	w	w	w	w	m	w	w						7	7	0
28			w	w	w	w	m	w	w						5	6	1
29			w	w	w	w	w	w	w						7	7	0
30				w	w	w	w	w	w						5	6	1
31				w	w	w	w	w	w	w					7	7	0
32					w	w	w	w	w	w					6	6	0
33					w	w	w	m	w	w	w				6	6	0
34						w	w	w	m	w	w	w			5	5	0
35							w	w	m	w	w	w	w		5	5	0
36								w	m	w	w	w	w		5/6	5	0
37								w	w	w	w	w	w		6	6	0
38								w	w	w	w	w	w	w	7	7	0
39								w	w	m	w	w	w	w	6	6	0
40								w	w	m	w	w	w	w	6	6	0

Per	Shift														ISS	ASS	NSS
	1	2	3	4	5	6	7	8	9	10	11	12	13	14			
41							w	w	m	w	w	w	w	w	7	7	0
42							w	w	m	m	w	w	w	w	5	6	1
43							w	w	w	m	w	w	w	w	7	7	0
44							w	w	w	m	w	w	w	w	6	7	1
45							w	w	w	m	m	m	w	w	5	5	0
46								w	w	w	m	m	w	w	4	5	1
47								w	w	w	m	m	w	w	4	5	1
48								w	w	w	m	m	w	w	4	5	1
49								w	w	w	w	w	m	w	6	6	0
50								w	w	w	w	w	m	w	6	6	0
51								w	w	w	w	w	m	m	4	5	1
52								w	w	w	w	w	m	m	4	5	1
53								w	w	w	w	w	w	m	6	6	0
54										w	w	w	w	m	3	4	1
55										w	w	w	w	w	4/5	5	0
56										w	w	w	w	w	4	5	1
57										w	w	w	w	w	4	5	1
58										w	w	w	w	w	3	5	2
59										w	w	w	w	w	5	5	0
60										w	w	w	w	w	4	5	1
61										w	w	w	w	w	4	5	1
62										w	w	w	w	w	5	5	0
63												w	w	w	3	3	0
64												w	w	w	3	3	0
UnS	R2		R2	R2	R2		R1, R2			R1	R1	R1	R1				

RSA2 develops a workforce schedule that ignores reliefs. Per = planning period; w = work period; m = meal period; r = relief; ISS = ideal staff size; ASS = actual staff size; NSS = net staff size (=ASS – ISS); UnS = unscheduled reliefs.

Table 5. Optimal RSA3 solution to problem one

Per	Shift														ISS	ASS	NSS	
	1	2	3	4	5	6	7	8	9	10	11	12	13	14				
1	w	w	w	w	w											5	5	0
2	w	w	w	w	w											5	5	0
3	w	w	w	w	w											4	5	1
4	w	w	w	w	w											5	5	0
5	r	r	w	w	w											3	3	0
6	w	w	r	r	w											3	3	0
7	w	w	w	w	r											4	4	0
8	w	w	w	w	w											5	5	0
9	w	w	w	w	w											3	5	2
10	m	w	w	w	w											4	4	0
11	m	w	w	w	w	w										5	5	0
12	m	m	w	w	w	w	w									5	5	0
13	m	m	w	w	w	w	w									4	5	1
14	w	m	w	w	w	w	w									6	6	0
15	w	m	m	w	w	w	w									5	5	0
16	w	w	m	w	w	w	w									6	6	0
17	w	w	m	w	w	r	w									5	5	0
18	w	w	m	m	w	w	w									5	5	0
19	w	w	w	m	w	w	w									6	6	0
20	w	w	w	m	w	w	w									6	6	0
21	w	r	w	m	m	w	w									4	4	0
22	w	w	w	w	m	m	w									5	5	0
23	w	w	w	w	m	m	w									5	5	0
24	w	w	w	w	m	m	w	w	w							7	7	0
25		w	w	w	w	m	m	w	w							6	6	0
26		w	w	w	w	w	m	w	w							7	7	0
27		w	w	w	w	w	m	w	w							7	7	0
28			w	w	w	w	m	r	w							5	5	0
29			w	w	w	w	w	w	w							7	7	0
30				w	w	r	w	w	w							5	5	0
31				w	w	w	w	w	w	w						7	7	0
32					w	w	w	w	w	w						6	6	0
33					w	w	w	m	w	w	w					6	6	0
34						w	w	m	w	w	w					5	5	0
35							w	m	w	w	w	w				5	5	0
36								w	m	w	w	w	w			5/6	5	0
37								w	w	w	w	w	w			6	6	0
38								w	w	w	w	w	w	w		7	7	0
39								w	w	m	w	w	w	w		6	6	0
40								w	w	m	w	w	w	w		6	6	0

Per	Shift														ISS	ASS	NSS
	1	2	3	4	5	6	7	8	9	10	11	12	13	14			
41							w	w	m	w	w	w	w	w	7	7	0
42							w	r	m	m	w	w	w	w	5	5	0
43							w	w	w	m	w	w	w	w	7	7	0
44							w	w	w	m	w	w	r	w	6	6	0
45							w	w	w	m	m	m	w	w	5	5	0
46								w	w	w	m	m	w	r	4	4	0
47								w	r	w	m	m	w	w	4	4	0
48								w	w	w	m	m	w	w	4	5	1
49								w	w	w	w	w	m	w	6	6	0
50								w	w	w	w	w	m	w	6	6	0
51								w	w	r	w	w	m	m	4	4	0
52								w	w	w	w	w	m	m	4	5	1
53								w	w	w	w	w	w	m	6	6	0
54										w	r	w	w	m	3	3	0
55										w	w	w	w	w	4/5	5	0
56										w	w	r	w	W	4	4	0
57										w	w	w	r	W	4	4	0
58										w	w	w	w	W	3	5	2
59										w	w	w	w	W	5	5	0
60										w	w	w	w	R	4	4	0
61										w	w	w	w	W	4	5	1
62										w	w	w	w	W	5	5	0
63												w	w	W	3	3	0
64												w	w	W	3	3	0

RSA3 takes the workforce schedule developed ignoring reliefs (i.e., RSA2's schedule), and attempts to assign as many reliefs as possible to periods with surplus staffing. Per = planning period; w = work period; m = meal period; r = relief; ISS = ideal staff size; ASS = actual staff size; NSS = net staff size (=ASS - ISS).

Table 6. Summary of results for the three approaches on the 100 problems

Demand peaks		1	2	3	Numerous	Overall
# Prob		25	25	25	25	100
RSA 1	MSC	1923.92	2485.40	2460.88	2526.36	2349.14
	PRA	100.00	100.00	100.00	100.00	100.00
	ANS	62.76	107.88	100.68	105.40	94.18
RSA 2	MSC	1803.44	2305.80	2340.00	2481.68	2232.73
	PRA	0.00	0.00	0.00	0.00	0.00
	ANS	81.20	108.88	101.40	105.92	99.35
RSA 3	MSC	1803.44	2305.80	2340.00	2481.68	2232.73
	PRA	12.16	40.27	42.62	78.10	43.29
	ANS	81.20	108.88	101.40	105.92	99.35

RSA1 develops a workforce schedule that includes reliefs. RSA2 develops a workforce schedule that ignores reliefs. RSA3 takes the workforce schedule developed ignoring reliefs, and attempts to assign as many reliefs as possible to periods with surplus staffing. Demand peaks = number of peaks in the ideal staffing pattern. MSC = mean schedule cost, in labor-period-equivalents. PRA = percentage of reliefs assigned. ANS = average number of shifts in the schedule.

Table 7. Summary of three commercial labor scheduling systems found at the Yahoo site^a

Company name	URL	Product name	Breaks scheduled
Atlas Business Solutions, Inc.	http://www.abs-usa.com	Visual Staff Scheduler® PRO 5.0	Yes
Global Management Technologies	http://www.gmtcorp.com	GMT Planet	Yes
Schedule Source	http://www.schedulesource.com	eSchedule 4.1	Yes

^ahttp://dir.yahoo.com/Business_and_Economy/Business_to_Business/Computers/Software/Business_Applications/Scheduling_and_Task_Management/Employee_Scheduling/

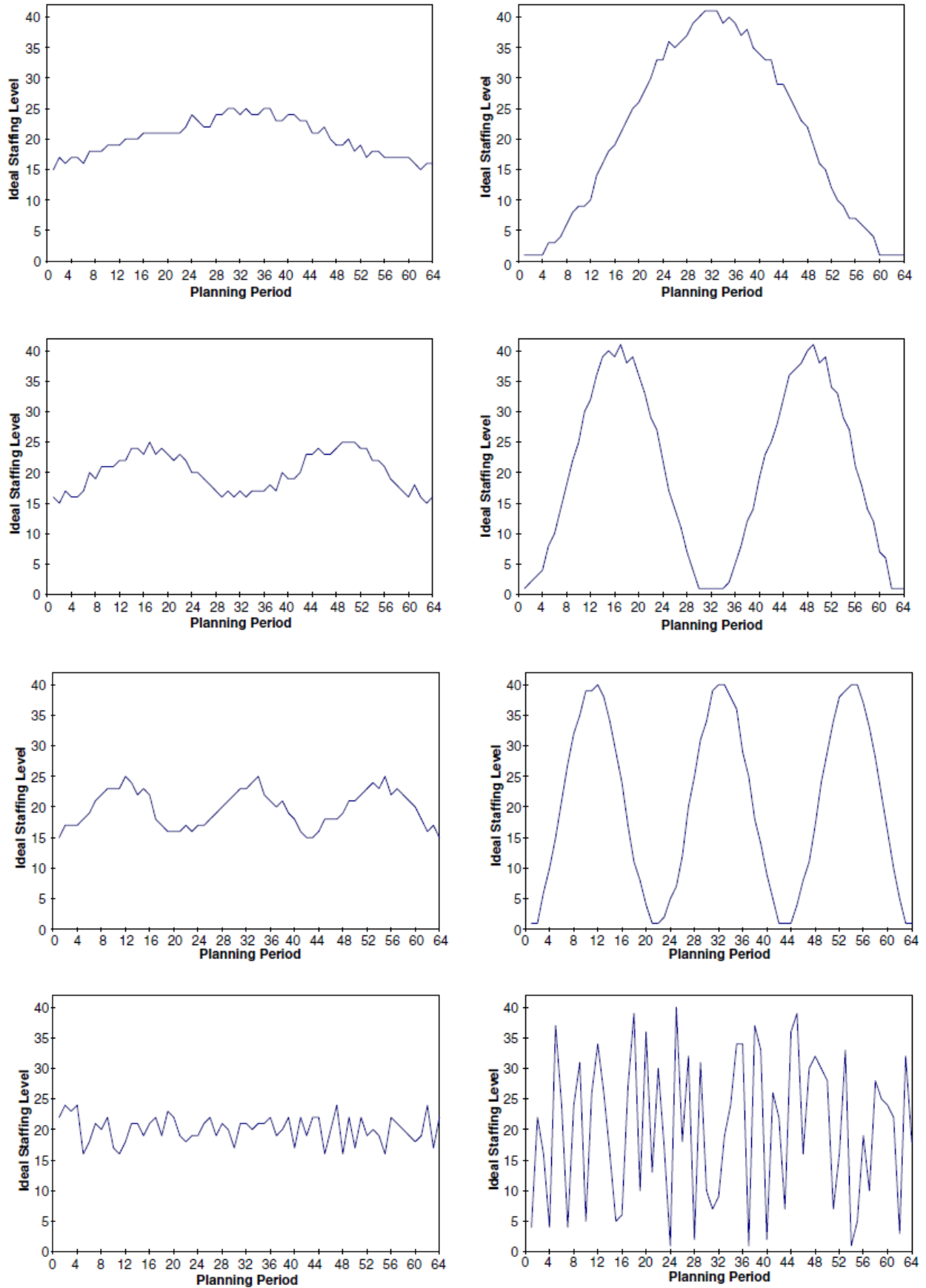


Figure 1. Eight examples of the ideal staffing level patterns.