# SINGLE-EVENT EFFECT MITIGATION IN PIPELINED ANALOG-TO-DIGITAL CONVERTERS

By

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#### CHAPTER I

#### INTRODUCTION

Analog-to-digital converters (ADCs) are necessary circuits in many space, military, and medical circuit applications. Intelligence, surveillance, reconnaissance, and communication missions all require high performance ADCs. Speed, resolution, and power are concerns in high performance designs. Unlike commercial applications, space, military, and some medical electronics must also be able to function in a radiation environment [1]-[5]. This additional complexity magnifies an interesting and needed area of research.

One type of radiation effect can occur when a single ionizing particle passes through the microelectronic circuit. An ionizing particle will generate charge in semiconductor materials in the form of electron-hole pairs. The positive carriers, holes, and negative carriers, electrons, may harmlessly recombine, but may also be collected on circuit nodes causing erroneous current and voltage perturbations in the circuit operation. An electrical change in transistor operation caused by an ionizing particle is called a single-event effect (SEE). A single-event upset (SEU) occurs when an SEE causes a flip in a logic state. A single-event transient (SET) is a current and/or voltage perturbation, and if sufficient in size may propagate through logic.

Ionizing particles can be found at high altitudes, space, and in some medical applications. Also, ionizing particles can be created as secondary or tertiary particles from neutron collisions with other atoms. Single-events can disrupt ADC operation

producing erroneous output codes. One of the first heavy-ion irradiation tests of an ADC showed that low LET particles will cause a complex distribution of errors [6]. The errors occur in small-magnitude Gaussian-like distributions around the expected output code, and also large magnitude errors [6], i.e., codes far from their expected values. In a follow-up analysis these error types were categorized as a noise component (small magnitude) and offset (large magnitude) [7]. The single-event error response of ADCs can be much more complicated than noise and offset errors. Temporary data errors, lingering offset errors, zero outputs, and linearity issues all occurred in a different ADC heavy ion test [8]. Even the ADC response to proton testing provided a complex response including a non-linear error response seen to occur over sample-rate and upsets lasting multiple clock cycles [9]. Laser testing has shown some upsets internal to an ADC can be masked while others can exacerbate large output errors [10], [11]. The complex ADC responses to heavy ions including error magnitudes, rates, and duration have been seen in other tests as well [12], [13].

The goal of this dissertation is to understand SEEs in high-speed ADCs, so the impact of design topologies and mitigation techniques can be evaluated for Department of Defense (DOD) or commercial space deployment. This goal can be broken into two parts. The first part is to characterize and explain the single event effect response. The second part is to provide additional circuit design alternatives that improve SEE response. These goals address a need in the radiation effects community as discussed in the survey performed by Kenneth G. Merkel and Anthony L. Wilson in the 2003 IEEE Proceedings of the Aerospace Conference [14]. The survey concluded that defense space applications have a need for radiation tolerant ADCs of speeds of at least 25 Msps with bit resolutions

of at least 10-12 bits, specifications best suited for the pipelined ADC architecture. The work in this dissertation focuses on the pipelined ADC sub-circuits along the signal path. Digital latches, references, bias circuits, and clock circuits are also known to be sensitive to single-events [1], [13], [15]-[17], but are assumed to be independently hardened. The conclusion of this work will help designers achieve ADCs for the next generation applications, influence experimental testing methodologies, and be applied to other high-speed mixed signal applications.

#### CHAPTER II

#### SINGLE-EVENT EFFECTS

### Introduction

Space and military circuit applications must operate in a more intense radiation environment than commercial electronics on Earth. For this reason careful design and testing must be take place before fielding. This work focuses on one type of radiation event called single-event effects. In this case a single ionizing particle passes through the microelectronic circuit generating excess electron-hole pairs. Unless proper precaution is taken, an erroneous circuit response can occur from devices collecting electron and/or hole pairs.

SEEs in microelectronics were first theorized in 1962 [18]. In 1967, one-dimensional numerical modeling showed a SEE can cause a memory error called a single-event upset (SEU) [19], [20]. A SEU was not observed until almost a decade later. In 1975, the first published account of a single event upset occurring in space was reported [21]. A few years later, 1979, the first SEU in a random access memory was published [1].

SEEs have become a more prevalent issue due to CMOS scaling. In 1965, G. E. Moore proposed that the number of transistors on a chip would double every two years [22]. Since then this statement has become the benchmark for the commercial semiconductor industry and has become famously known as Moore's Law. In order to keep pace with Moore's Law, industry has decreased device dimensions, operating

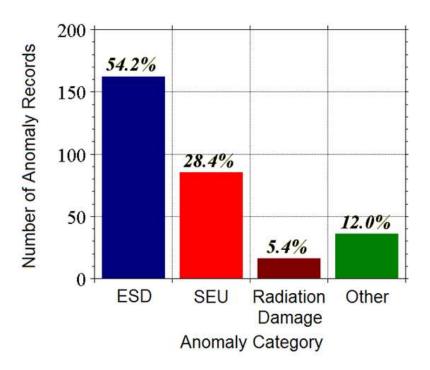


Fig. 1. In 1999, spacecraft anomaly records were categorized into anomaly types (ESD: electrostatic discharge; SEU: single event upset) [24] (data from [3]).

voltage, gate oxide thickness, gate length, nodal separation of the devices, nodal capacitance, etc. with every technology generation. Since 1965, consumers have enjoyed the benefits of significant increases in performance and speed, decrease in integrated circuit cost, and smaller chips with greater functionality for CMOS technology. Unfortunately, these factors have a negative impact of increased SE vulnerability of microelectronics [23]. In 1999, 28% of spacecraft anomaly records were attributed to SEEs as shown by Fig. 1 [3], [24].

## **Radiation Environments**

A detailed understanding of the radiation is required at the start of any radiationhardened circuit design. The distribution of ionizing particles that interact with a space system is dependent on orbit altitude or space flight path. The space radiation

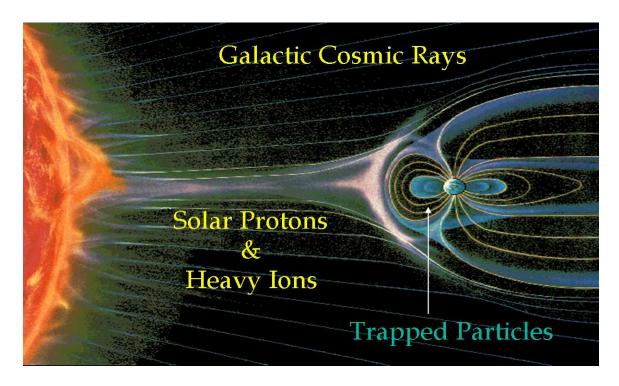


Fig. 2. An illustration of the space radiation environment [25].

environment is broken into three categories: trapped, solar, and cosmic, and is illustrated in Fig. 2 [25]. On Earth, neutron collisions with other atoms can produce ionizing particle recoils; an issue for any flight application. Also there is a history of radioactive contaminants in the microelectronics industry, which have to be carefully screened before fabrication or SEEs will result.

#### *Trapped Radiation Environment*

There is an abundance of charged particles, predominantly protons and electrons, trapped by the Earth's magnetic fields. These regions of trapped particles were first discovered and published by J. A. Van Allen in 1959, and thus subsequently named the Van Allen belts [26]. Trapped protons and electrons are reflected back and forth between Earth's magnetic poles traveling along the magnetic field contours, and at the same time

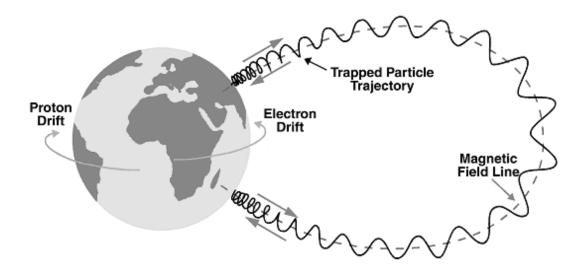


Fig. 3. Motion of trapped charged particles in the Earth's magnetic field [27], [28].

the trapped particles will also revolve around the Earth: electrons drift eastward while protons drift westward. Trapped charged particle motion is illustrated in Fig. 3 [27], [28].

High altitude and space missions are impacted by trapped protons and electrons. Protons are capable of producing SEEs through either direct or indirect ionization; electrons are not yet able to produce SEEs in current technology. Electrons contribute to total ionizing dose (TID), another well-studied radiation effect, but TID effects are not covered in this work. Fig. 4 shows proton fluxes for different energies as a function of L-shell number (distance measured in Earth-radii from Earth's center) [29]. Trapped protons across a wide range of energies can impact electronics at mid-Earth orbits (MEO), 2000 km to 35,000 km, corresponding to L-shells 1.3 through 6.5. At geosynchronous Earth orbit (GEO), 35,786 km, and at further high-Earth orbits (HEO), trapped proton fluxes are dominated by low energy protons (< 1 MeV). Another area of proton concentration is the South Atlantic Anomaly (SAA). Earth's magnetic poles are offset from the rotational axis by 11 degrees. Due to this offset, the Van Allen belts are

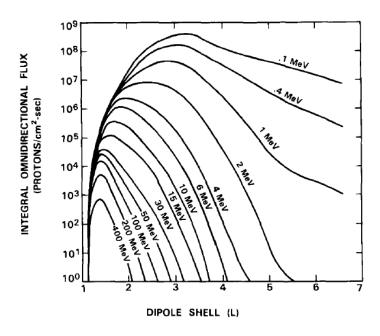


Fig. 4. Equatorial radial profiles for proton fluxes [29].

closest to Earth's surface near Rio de Janerio, Brazil, the region known as the SAA. Protons in the SAA exist in much lower altitudes, only about 300-400 km, impacting electronics at low-Earth orbits (LEO), 160 km to 2000 km. The trapped radiation environment is not constant; instead the flux of particles varies for many reasons. The solar cycle is a major influence on the trapped radiation environment.

# Solar

The solar cycle oscillates over an 11 year cycle. Fig. 5 plots the sunspot variation over 3 cycles and includes proton integral fluences for select large solar proton events [30]. During high activity the Sun becomes very volatile, increasing the occurrence of two types of significant solar energetic particle (SEP) events: solar flares and coronal mass ejections (CMEs). Solar flares are the rapid release of energy from a localized region on the Sun in the form of electromagnetic radiation, energetic particles, and mass motions. Solar flares occur about once a week during the solar minimum but increase to

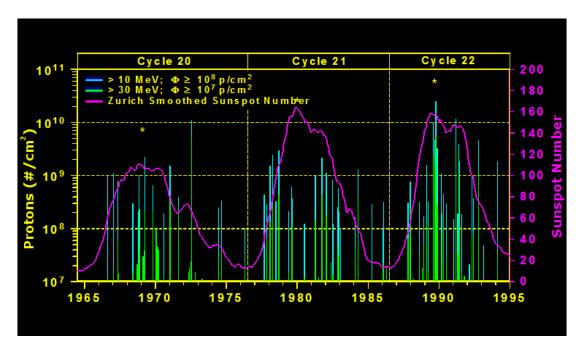


Fig 5. Correlation of proton events with solar cycle [30].

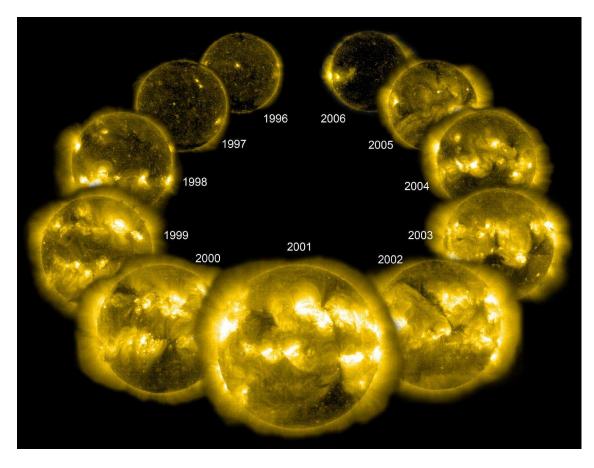


Fig 6. An EIT image in the 284 Angstrom wavelength of extreme UV light from each year of nearly an entire solar cycle [31].

several per day when the Sun is most active. CME is the result of a huge magnetic bubble of plasma that erupts from the Sun's corona. During solar minimum, CMEs occur about once every other day; at solar maximum, CMEs will occur 5-6 times a day. Solar flares and CMEs can also occur simultaneously. Fig. 6 is a sequence of images of the Sun spanning an entire solar cycle from the Solar and Heliospheric Observatory [31]. In addition to protons, SEP events can also contain heavy ions. Fig. 7 plots various particle fluxes observed by three spacecraft (ACE, SAMPEX, GOES-11) during a SEP event on Januaray 20<sup>th</sup>, 2005 [32]. No two SEP events are the same; particle fluences can vary widely from event to event, as shown in Fig 8 [32].

#### Cosmic

During periods of solar minimum, galactic cosmic rays (GCR) are the dominant source of ionizing particles outside the trapped radiation belts. The sources of GCR are

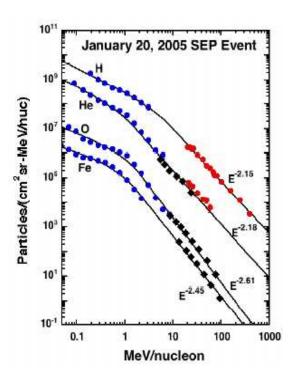


Fig. 7. Particle flux data taken by ACE, SAMPEX, GOES-11 for a SEP [32].

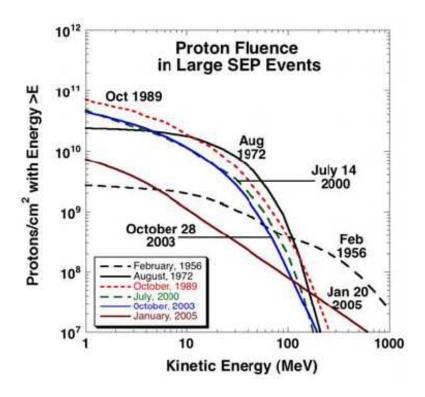


Fig. 8. Proton fluences from different SEP events [32].

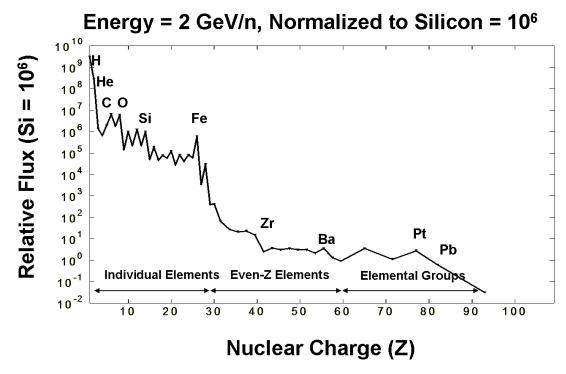


Fig. 9. GCR relative ion composition [30], [33].

mostly unknown, but possible origins are theorized to be the Big Bang and supernovas. Since GCR originate from outside our solar system, particle trajectories are essentially omnidirectional. GCR distributions are dominated by protons; the flux of protons is approximately 10 times larger than then next particle, helium, and over 1000 times larger than iron. Fig. 9 plots the relative flux of ions with an energy of 2 GeV/nucleon that make up GCRs, and has been normalized to Si flux of 10<sup>6</sup> [30], [33].

#### **Terrestrial**

Particle collisions between the Earth's atmosphere and high energy GCRs or solar particles can produce neutrons. Unlike protons and heavy ions, neutrons do not cause direct ionization, but are one of the main sources of SEEs within the Earth's atmosphere. Energetic neutrons can interact with nuclei elastically, displacing the nucleus from its lattice position, or inelastically, causing the nucleus to eject ionizing particles. Terrestrial neutrons are the products of multi-generational particle collisions. Neutrons are an issue at flight altitudes, as shown in Fig. 10 [2], and due to the shape of the magnetic fields, GCRs can reach lower altitudes near the poles, resulting in a 5X-6X increase in the number of neutrons [2]. Neutron flux is also dependent on the 11 year solar cycle and can vary as much as a factor of two.

Impurities in the IC industry also account for terrestrial sources of SEEs. Alpha particle emitters have been a concern for many years. In the late 1970s trace uranium and thorium impurities were discovered to be the dominant cause of soft errors in dynamic random-access memories (DRAMs) [34]. Currently, lead-solder is a common source of alpha particles and has to be screened before use in IC packaging [35]. Another example of impurities in the packaging and fabrication process causing SEEs, is the boron isotope

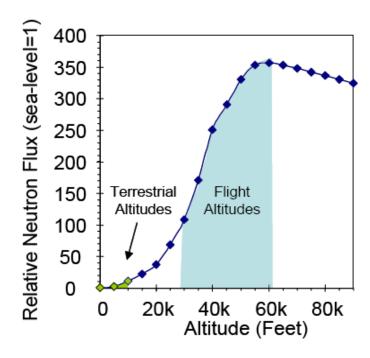


Fig. 10. Neutrons flux increases with increasing flight altitude [2].

<sup>10</sup>B. Boron is commonly used as a p-type dopant and for borophosphosilicate glass (BPSG), an insulator between metal layers. Boron has two isotopes: 80% of boron particles are <sup>11</sup>B while 20% are <sup>10</sup>B. If <sup>10</sup>B absorbs a neutron, it will become unstable, breaking apart and releasing Li and an alpha particle, resulting in a increase in soft error rates [36], [37]. The industry now screens boron for the <sup>10</sup>B isotope, to minimize SEEs.

# **Basic Mechanisms of Single-Events**

A single-event effect occurs when a sensitive device, such as a transistor, collects the charge generated by an ionizing particle. As an ionizing particle passes through a semiconductor it will lose energy to the material. This energy can excite electrons, through Coulombic interaction, to break away from their valance bands leaving behind vacancies (holes), thus generating electron-hole pairs (charge). The particle's energy loss is typically parameterized in the radiation effects community using linear energy transfer

(LET). A minimum of 3.6 eV (E<sub>e-h</sub>) is necessary to generate an electron-hole pair in silicon [38]. LET can roughly be converted to charge generation per path length,

$$\frac{dQ}{dX} = \frac{q \cdot \rho_{Si} \cdot LET(X)}{E_{e-h}},\tag{1}$$

given a silicon density ( $\rho_{Si}$ ) of 2328 mg/cm<sup>3</sup> and an electron energy (q) of 1.6x10<sup>-19</sup> C [38], [39]. An ionizing particle that has a constant LET of 10 MeV-cm<sup>2</sup>/mg will generate 100 fC/ $\mu$ m. However, ionizing particles do not lose energy at a constant rate. Fig. 11 shows the LET of 5 GeV <sup>132</sup>Xe as a function of distance through silicon [40].

Without any external forces, electron-hole pairs will harmlessly recombine. However, integrated CMOS circuits contain billions of p-n doping junctions, many of which will be reversed biased. Electron-hole pairs generated in the depletion regions of the reversed biased p-n junctions will quickly be separated by the electric fields. This

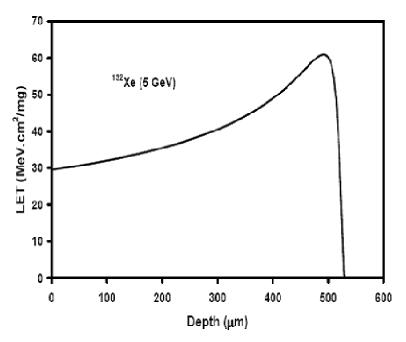


Fig. 11. LET as a function of depth in silicon for a  $^{132}$ Xe ion with energy of 5 GeV. The range is about 520  $\mu$ m and the maximum is referred to as the Bragg peak (from [40]).

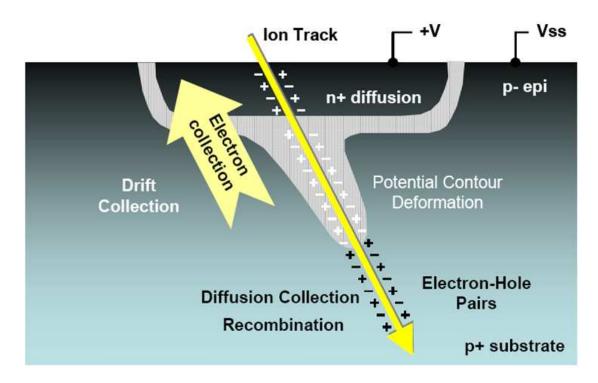


Fig. 12. Illustration of a diffusion region collecting the charge generated by a singleevent. Regions of drift transport, depletion funnel, and diffusion transport are labeled (from [43]).

movement of charged particles is drift current, electrons flowing to the n-doped region and holes moving to the p-doped region. The electric fields will also dynamically change as an ionizing particle generates a dense track of electron-hole pairs, pushing out the depletion region creating a funnel shape. Field-assisted funneling is the drift collection of electrons and holes that were not initially in the p-n junction but became included in the depletion funnel [42].

Charge outside an electric field may still be collected through diffusion; a transport process in which electrons and holes will move from high-density regions to lower-density regions. Diffusion is a much slower transport process than drift, and many of the electron-hole pairs will recombine. Fig. 12 (from [43]) is an illustration of charge collection by a transistor through drift, field-assisted funneling, and diffusion transport.

While heavy ions are the main source of direct ionization, recently protons have been observed to cause upsets [44]. Direct ionization is not the only way electron-hole pairs can be generated; indirect ionization occurs when the primary particle collides with the nucleus of another the particle. The nuclear reaction will produce secondary particles that can ionize near sensitive devices. Nuclear reactions, especially due to particle collisions in the over-layers, have been attributed to low-LET upsets [45].

In highly-scaled circuits there can be more complex responses to a single-event, one example is parasitic bipolar conduction [46]. Charge generation in the thin well structures of the CMOS process will be confined. The flow of carriers to nearby well-contacts across the resistive well will cause localized potential drops in the transistor channel regions. If the potential drops sufficiently low, a reversed bias source diffusion can inject carriers into the channel which are then collected by the drain, enhancing the collected charge above normal drift and diffusion collections.

# Simulating Circuit Response to Single-Events

Computer modeling can help analyze single-event charge collection mechanisms, the resulting circuit-response, and identify hardening techniques. Circuit-level, simulation programs with integrated circuit emphasis (SPICE), simulations are commonly used to assist circuit design. Single-events can be modeled in SPICE using a current source. For correct current polarity, it is important to identify the diffusion-type at a node. Conventional current (positive carrier flow) will flow from an n-drain into the p-doped bulk, typically grounded, or from an n-doped bulk, typically biased at VDD, into a p-drain. An example of using a current source to model a single-even is shown in

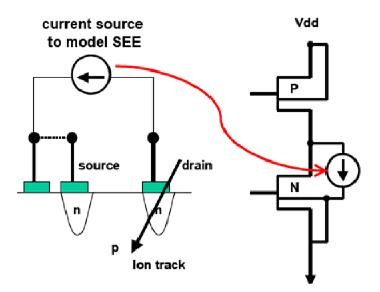


Fig. 13. Illustration showing the use of a current source to model a single-event in SPICE (from [47]).

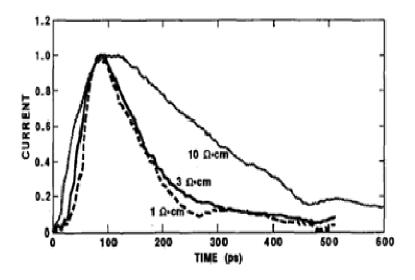


Fig. 14. Measured diode current profiles caused by 5 MeV alpha particles incident on different size diodes (from [49]). The initial current spike is charge collection through drift, while the tail current is charge collection through diffusion.

Fig. 13 (from [47]). The traditional SPICE current model is a double-sided exponential approximating a diode response to a single-event [39], [48]. Examples of measured single-event current at a p-n junction diode are shown in Fig. 14 (from [49]). However, a

double-exponential current source is not necessarily an accurate SE-model for advanced digital circuits. Transistor size, node impendence, and current drive can all affect the shape of the SE-current [50]. Different SE-current profiles can be implemented in SPICE using piece-wise linear current sources calibrated to device-level single-event, technology computer aided design (TCAD), single-event simulations. SE-response of circuits can also be performed by using mixed-mode simulations, a combination of SPICE and TCAD. The nearby semiconductor devices surrounding an ionizing particle strike are modeled in TCAD while the remaining transistors are connected through SPICE. Mixed-mode simulation can capture the dynamic circuit response to a SE-strike but can be time-intensive to setup and require high-performance computer networks.

# Conclusion

This chapter presented background on the single-events. Trapped, solar, cosmic, and terrestrial sources of ionizing particles in the radiation environment have been described. Also explained were charge collection mechanisms from ionizing particles. Finally, this chapter concluded with a brief description of single-event models used for circuit-level simulation analysis. The following chapter will present background on analog-to-digital converters necessary for discussion on SEs in ADCs.

#### CHAPTER III

#### ANALOG-TO-DIGITAL CONVERTERS

### Introduction

Given the real-world environment is inherently analog, and the majority of integrated chip (IC) processing is digital, analog-to-digital converters (ADCs) are required to interface the two domains. Intelligence, surveillance, reconnaissance, and communication missions all require high performance ADCs. This chapter explains basic ADC operation, introduces the common performance metrics, and concludes with a discussion on the pipelined ADC architecture.

# **Basic ADC Operation**

An ADC converts a continuous analog signal into discrete digital values [51]. Typically, the output of an ADC is in binary; the total number of output bits is defined as resolution. Therefore a 1-bit ADC will have 2 possible discrete values, a 2-bit ADC will have 4 possible discrete values, a 3-bit ADC will have 8 possible discrete values, and so forth. The least significant bit (LSB) of the binary output is the smallest unit step size and is equal to full input range divided by the number of discrete values. Distances between output codes are often measured in terms of LSBs. There are many types of ADCs with resolutions as little as 1-bit to larger than 20-bits. The ADC's conversion speed is given in terms of the number of samples-per-second; typical speeds range from

kilo-samples-per-second (ksps), to mega-samples-per-second (Msps), and even giga-samples-per-second (Gsps).

# **Common ADC Performance Metrics**

The output response of ADCs is inherently nonlinear since they convert analog signals into discrete values. The output is similar to a staircase, an example of a 3-bit ADC output response is shown in Fig. 15. Most ADCs have a shifted output transfer function such that quantization error, deviation from the ideal infinite ADC response, is limited within  $\pm$  0.5 LSB. In practical ADCs, the size of each discrete step in not uniform

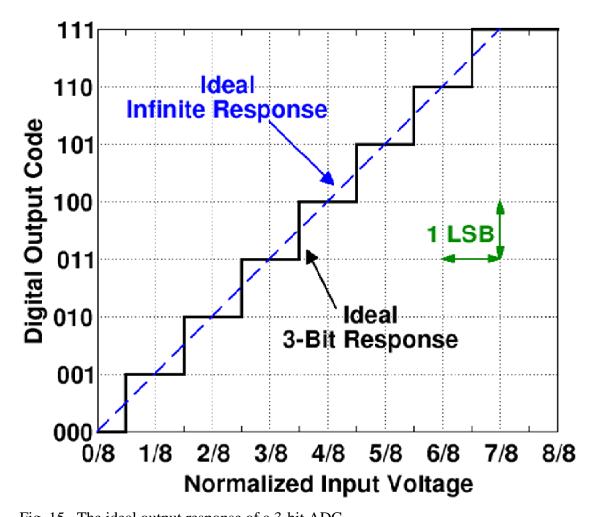


Fig. 15. The ideal output response of a 3-bit ADC.

and is characterized using differential nonlinearity (DNL) and integral nonlinearity (INL). DNL measures the difference between the actual step width and the ideal width; an example 3-bit ADC transfer function containing DNL errors is plotted with the ideal response in Fig. 16. The ideal step width of all bit codes except the first and last codes is 1 LSB. Due to the shift in response, the step size for the first code is only 0.5 LSB and the last code is 1.5 LSBs. Two DNL errors are labeled in Fig. 16; the code '010' has an actual step size of 1.5 LSBs instead of and ideal 1 LSB thus the DNL for this code is a 0.5 LSB. Also the actual response for code '100' is only 0.5 LSB wide, resulting in a DNL error of -0.5 LSB. Even though Fig. 16 has a missing code at '011', an ADC with missing codes may still be used if the bit resolution is greater than the system specifications. INL characterizes difference between the actual response and the ideal straight line response; an example is shown in Fig. 17.

Another common ADC performance metric is signal-to-noise ratio (SNR), the ratio of rms (root mean square) signal to rms noise. Even an ideal ADC will have a finite SNR because of the quantization error. The ideal SNR equation,

$$SNR_{IDEAL} = 6.02N + 1.76dB$$
, (2)

assumes only quantization error as the noise source, where N is the number of bits [52]. Real ADC testing will include harmonic distortion due to nonlinearity of the internal amplifiers. Harmonic distortion, like noise, decreases ADC performance, and is measured as signal to noise-plus-distortion ratio (SNDR), also known as signal-to-noise and distortion ratio (SINAD). While ADCs are designed to have N-bit resolution, non-

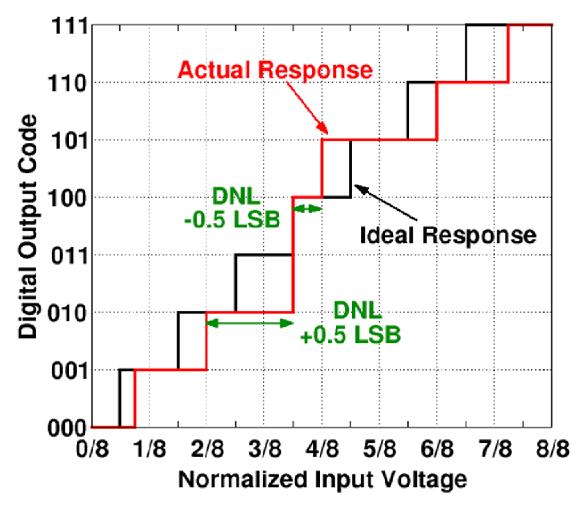


Fig. 16. An example of differential nonlinearity (DNL) in a 3-bit ADC.

idealities will cause an actual SNDR, or SNR, to be less than the ideal SNR. Bit resolution can be adjusted accordingly by solving for N in equation (2). Thus the effective number of bits (ENOB) will be

$$ENOB = \frac{SNDR - 1.76dB}{6.02} \,. \tag{3}$$

# Common ADC Architectures

There are two general categories of ADC architectures: Nyquist and oversampling. The Nyquist criterion states a signal must sample greater than twice the

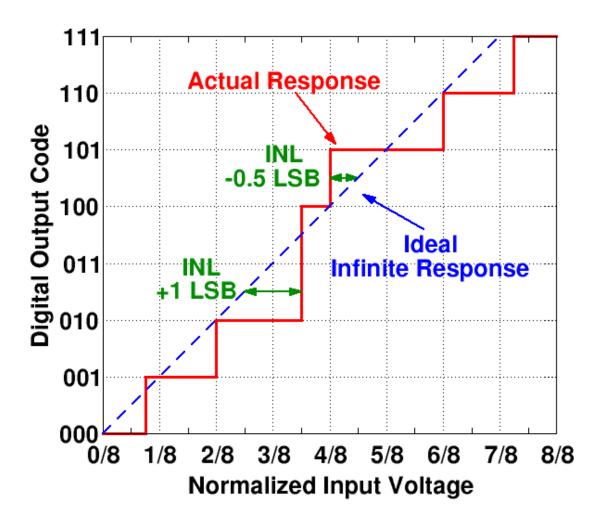


Fig 17. An example of integral nonlinearity (INL) in a 3-bit ADC.

maximum signal frequency in order for the original signal to be recoverable. ADCs that sample near the Nyquist criterion are considered Nyquist-rate converters. A design challenge for these converters is aliasing; signals with higher frequencies than the bandwidth of the ADC are indistinguishable from the signals inside the ADC's bandwidth. The frequency of an aliased signal is the difference between the high-frequency component and the ADC's sampling rate. Nyquist-rate converters require an anti-aliasing filter with a sharp cutoff frequency at half the sampling frequency to prevent high frequency signals from corrupting the data. In some applications, the anti-aliasing filter requirements are relaxed by oversampling. Resolution can be increased by 0.5 bit

for every 2X increase in sampling speed. Oversampling converters often have high resolution but due to the oversampling ratio the maximum signal frequency is lower than Nyquist-rate converters.

There are many types of ADC architectures; each having its own typical range of resolution and speed often determining the application. Flash ADCs can operate at Gsps speeds, but will have a maximum resolution of 8-bits. This architecture uses a ladder structure of comparators, each ladder rung providing an additional quantization level. Successive-approximation ADCs can quantize 20 or more bits but have slow sampling speeds on the order of ksps. This architecture uses an iterative guess-and-check algorithm for determining each bit starting with the MSB. Sigma-delta ( $\Sigma$ - $\Delta$ ) ADCs combine an oversampling 1 bit ADC with feedback to provide noise shaping. Resolution can be increased by the sum of the order of loop filter and a 0.5 bit for every 2X increase in sampling speed.  $\Sigma$ - $\Delta$  ADCs are popular in narrowband wireless applications where resolutions greater than 10 bits are necessary and the signal bandwidths are less than 1 MHz, such as Global System for Mobile Communication (GSM). The focus of this research is pipelined ADCs; this topology offers a combination of both resolution (10-16 bits) and speed (1-500 Msps).

#### Pipelined ADC

**Topology** 

Pipelined ADCs offer high resolutions (10-16 bits) and high speeds (1-500 MHz), a balance not found in other ADC architectures [53], [54]. The topology consists of a cascade of stages as shown in Fig. 18. The signal is quantized using an assembly line

approach where each stage quantizes a small portion of the analog signal, amplifies the remaining signal residue, and passes it on to the next stage. Internally, a stage consists of a low-resolution flash ADC, encoder logic, and a multiplying digital-to-analog converter (MDAC).

The low-resolution ADC in each stage uses the flash topology; comprised of  $2^{N}$ -2 comparators and  $2^{N}$ -1 resistors, where N is the stage resolution. The resistor string provides reference voltages for the comparators. Typically, a pipeline stage will not quantize the top bit code (i.e. all 1's), as this extra bit code is used to create 1-bit overlap with the following stage. The bit overlap is used to decrease output residue by a half, allowing extra range for digital error correction (DEC). The DEC relaxes the requirements for the comparators, correcting any error within  $\pm 0.5$  LSB of the input reference. Each comparator compares the input voltage to a different voltage from the reference resistor string. The comparator outputs generate a thermometer code, where the number of comparators generating a logic 1 output value changes according to the magnitude of the input voltage (which conceptually looks like a thermometer rising and falling, hence the name).

## 1.5-Bit Stage

The minimum stage resolution typically used is 1.5-bits. Each 1.5-bit stage includes two comparators and an encoder, as shown in Fig. 19, to calculate three possible most significant bit - least significant bit (MSB-LSB) pairs, '00', '01', and '10'. Since the output is comprised of two bits but only three of the four possible bit outputs are used, the typical nomenclature for its bit resolution is 1.5-bits. The excluded bit output '11' is not used to allow DEC.

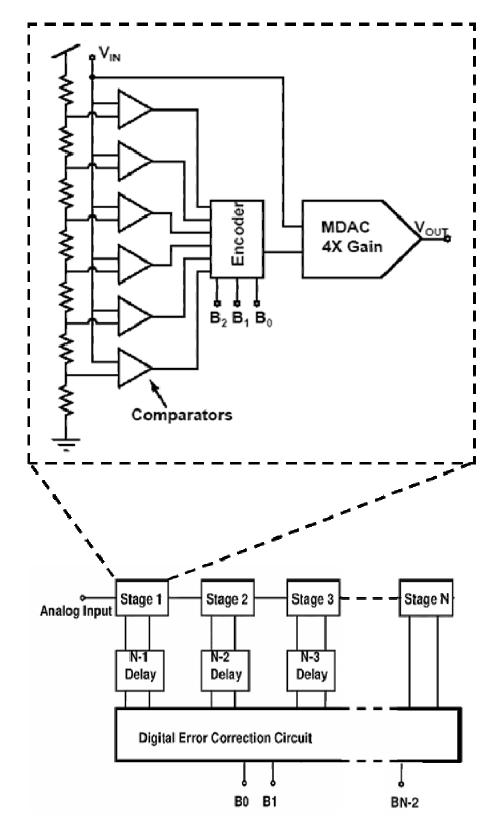


Fig. 18. Block diagram of an N-stage pipelined ADC. A 3-bit block diagram of a stage is also shown.

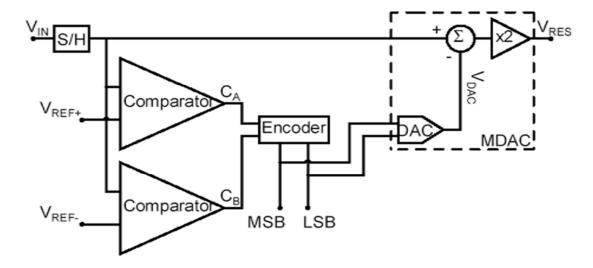


Fig. 19. Simplified pipelined ADC 1.5-bit stage architecture.

The output MSB is binary summed with the previous stage's LSB and the carry from the sum of the LSB and next stage's MSB. The comparators evaluate the sampled analog input to generate a two-bit digital thermometer code at outputs  $C_A$  and  $C_B$ . The encoder logic for the MSB is

$$MSB = C_A \cdot C_B \tag{4}$$

The simplest logic for the LSB is

$$LSB = \overline{C}_A \cdot C_B \tag{5}$$

Multi-Bit Stage

Larger bit-resolution stages are also used in pipelined ADCs. Unlike 1.5-bit stages, the bit-code is usually not directly converted from the comparator output. Instead, the thermometer code is converted to a 1-of-N code composed of all logic 0's except for a logic 1 at the thermometer code's transition from 1's to 0's. Each bit in the 1-of-N code  $(10fN_i)$  is determined from thermometer code bits  $(T_n)$ . This encoding process is commonly performed using one of two possible minimal encoder topologies. The 1-of-N

code can be either determined by taking the complement of the subsequent bit with the current and previous bits,

$$1ofN_i = \overline{T}_{n+1} \bullet T_n \bullet T_{n-1}, \tag{6}$$

or it can be determined from the complement of the next two subsequent bits with the current bit,

$$1ofN_i = \overline{T}_{n+2} \bullet \overline{T}_{n+1} \bullet T_n. \tag{7}$$

The thermometer to 1-of-N code conversion typically uses 3-input NAND gates to implement either (6) or (7). The 1-of-N code is then used to access the correct output bit code from a ROM (read-only memory) table, and also selects the correct MDAC input references.

Unlike minimum bit resolution (1.5-bit) stages, there is no unique nomenclature for stages using DEC; it is assumed the stages overlap. For example, even though there are 7 output codes for 3 bits, excluding the top code, a stage is not described as 2.33-bit resolution; it is still defined as a 3-bit resolution stage.

## Comparator

One of the important pipelined ADC sub-circuits is the comparator. Fig. 20 (a) shows a typical switched-capacitor CMOS comparator as commonly used in pipelined analog-to-digital converters. This comparator is composed of a capacitive input sampling/subtraction network, a pre-amplifier, and an output latch. A reference voltage is subtracted from the input signal, amplified, and will latch a logic '1' if the difference is positive or a logic '0' if the difference is negative.

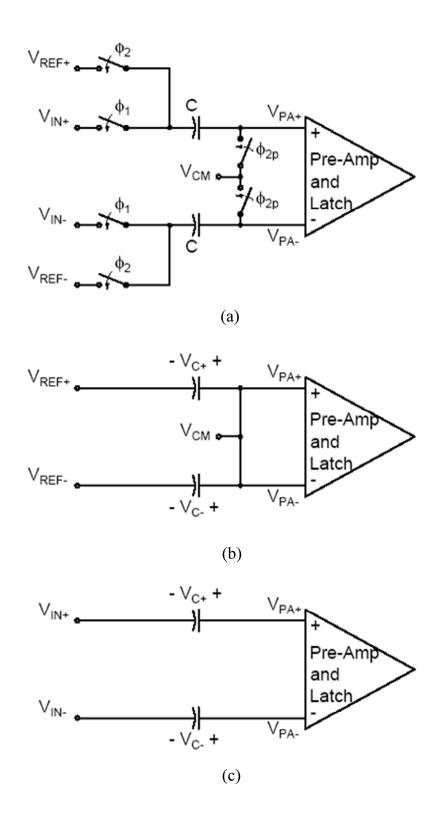


Fig. 20. (a) The switched-capacitor comparator operates in two phases: (b) reset phase and (c) evaluation phase.

The switched-capacitor comparator operates in two phases controlled by non-overlapping clocks  $\Phi_1$  and  $\Phi_2$ . During the reset phase, when  $\Phi_2$  is high and  $\Phi_1$  is low, as shown in Fig. 20 (b), the differential reference voltage with respect to common-mode voltage is sampled onto the capacitors,

$$V_{C+} = V_{CM} - V_{REF+}$$
 
$$V_{C-} = V_{CM} - V_{REF-}$$
 (8).

When  $\Phi_1$  is high and  $\Phi_2$  is low, as shown in Fig. 20 (c), the circuit is in evaluation phase. The input voltage is summed with voltage stored across the capacitors from the reset phase, resulting in the difference between input and reference voltages at the pre-amplifier inputs,

$$\begin{split} V_{PA+} &= V_{IN+} + V_{C+} = V_{IN+} + V_{CM} - V_{REF+} \\ V_{PA-} &= V_{IN-} + V_{C-} = V_{IN-} + V_{CM} - V_{REF-} \\ &\therefore V_{PA+} - V_{PA-} = \left(V_{IN+} - V_{IN-}\right) - \left(V_{REF+} - V_{REF-}\right) \end{split} \tag{9}.$$

If the differential input voltage is greater than the different reference then a logic '1' will be latched, otherwise the circuit will latch a logic '0'

Multiplying Digital-to-Analog Converter

Another important pipelined ADC sub-circuit is the MDAC. Once the quantizer determines the bit-code, the MDAC generates an appropriately amplified residue voltage as the input for the next stage in the pipeline, with each stage quantizing the next most significant portion on the input signal. Example residue voltage transfer curves for 1 V input range, 1.5-bit stage and 3-bit stages are shown in Figs. 21 and 22. The residue voltage (V<sub>RES</sub>) transfer curve is a piecewise linear function with each segment having the same slope equal to gain (G) of the MDAC. The gain is determined by 2 to power of N,

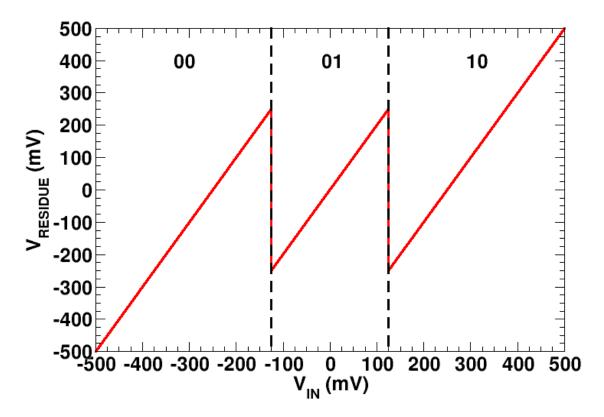


Fig. 21. The residue voltage transfer function for a 1.5-bit stage.

where N is number of bits, and then also divided by 2 to provide range for DEC. For example the gain of a 1.5-bit resolution (2 total bits) stage is 2, while multi-bit stages have gains of 4, 8, and 16 for 3-bit, 4-bit, and 5-bit resolutions, respectively. The number of piecewise segments in the residue transfer function is equal to number of output codes, and the position of each segment is determined by an integer constant (k) shift along the x-axis dependent on the output code. The general equation for  $V_{RES}$  is

$$V_{RES} = G * V_{IN} - k * V_{REF}. \tag{10}$$

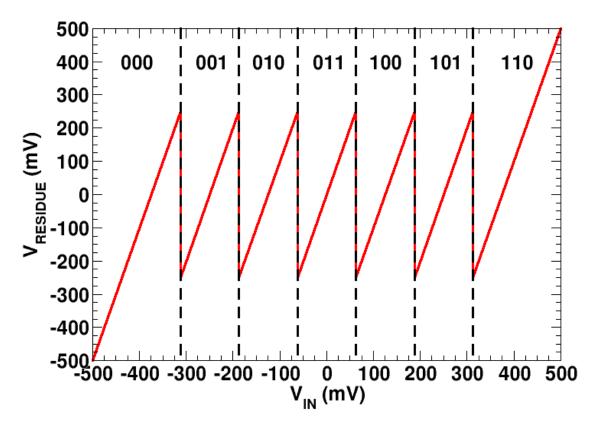


Fig. 22. The residue voltage transfer function for a 3-bit stage.

The 1.5-bit MDAC switched-capacitor network is shown in Fig. 23. During sample phase,  $\Phi_1$  is off and  $\Phi_2$  is on, the input signal is sampled across both equal-sized sampling and feedback capacitors,  $C_S$  and  $C_F$ :

$$Q_{samp+} = (V_{SIN+} - V_{cm}) * 2C$$

$$Q_{samp-} = (V_{SIN-} - V_{cm}) * 2C$$
(11)

During evaluate phase,  $\Phi_1$  is on and  $\Phi_2$  is off, the sampling capacitors' bottom plate is connected to  $V_{REF}$  and the feedback capacitors are connected into negative feedback. The output signal holds the difference between twice the input signal and the reference signal:

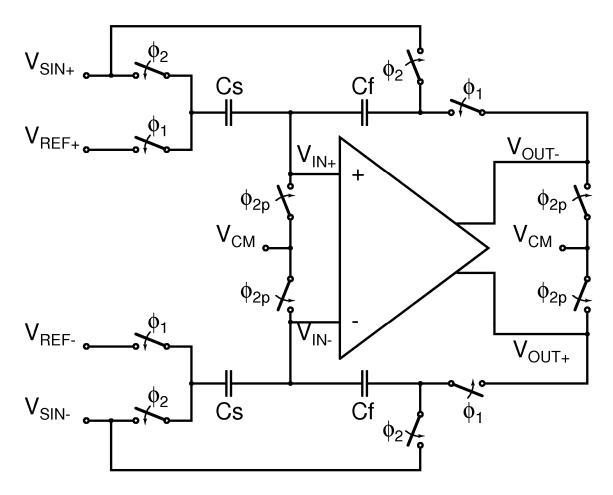


Fig. 23. Schematic of a multiplying digital-to-analog converter switched-capacitor network used in a 1.5-bit pipelined ADC stage.

$$Q_{eval\_s+} = (V_{REF+} - V_{CM}) * C$$

$$Q_{eval\_s-} = (V_{REF-} - V_{CM}) * C$$

$$V_{OUT+} = \frac{Q_{samp-} - Q_{eval\_s-}}{C} + V_{CM}$$

$$V_{OUT-} = \frac{Q_{samp+} - Q_{eval\_s+}}{C} + V_{CM}$$

$$\therefore (V_{OUT+} - V_{OUT-}) = -1 * [2 * (V_{SIN+} - V_{SIN-}) - (V_{REF+} - V_{REF-})]$$
(12)

There are three possible k factors in the 1.5 bit topology: -1, 0, and 1 for the '00', '01', and '10' bit codes respectively. To satisfy equation (10), a -1 k is created by using a negative  $V_{REF}$  fully differential bias (i.e.  $V_{REF+} = -V_{REF}/2$  and  $V_{REF-} = V_{REF}/2$ ). A 0 k is created by either shorting  $V_{REF+}$  and  $V_{REF-}$  together or connecting them both to the common-mode voltage,  $V_{CM}$ . Finally a +1 k is created by applying a positive  $V_{REF}$  fully differential bias.

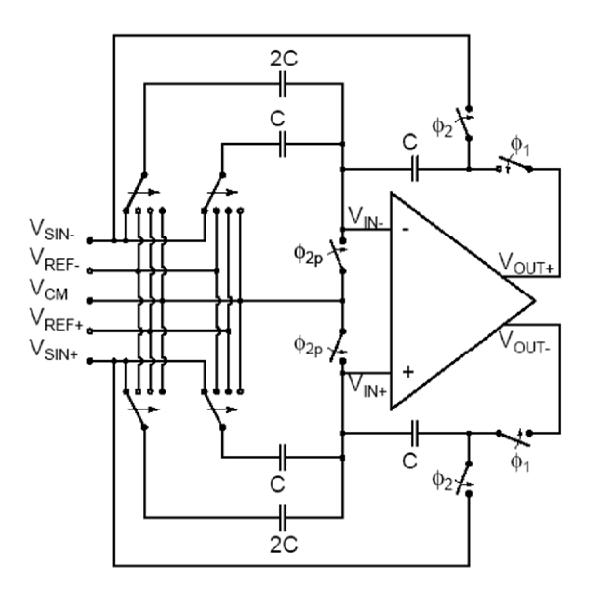


Fig. 24. Schematic of a multiplying digital-to-analog converter switched-capacitor network used in a 3-bit pipelined ADC stage.

MDAC used in multi-bit stages are slightly different. Fig. 24 shows the fully-differential switched-capacitor network MDAC for a 3-bit stage. A second sampling capacitor,  $C_S$ , is added in parallel and is twice the size of the original  $C_S$ . Similar to the 1.5-bt MDAC, during the sampling phase all  $C_S$  and  $C_F$  are connected to the input signal. During the evaluate phase the possible k factors are -3, -2, -1, 0, 1, 2, and 3 for bit codes '000', '001', '010', '101', '100', '101', and '110" respectively. The polarity of k is achieved the same way as the 1.5-bit MDAC by the polarity of the applied  $V_{REF}$ . The magnitude of k is created by connecting a subset of the sampling capacitors to  $V_{REF}$  such that the ratio of the connected  $C_S$  to  $C_F$  is equal to k. The sampling capacitors not connected to  $V_{REF}$  are connected instead to  $V_{CM}$ .

# Conclusion

This chapter presents background on analog-to-digital circuits. The purpose of ADCs is to discretize an analog signal to be stored and/or processed by digital circuitry. Non-idealities in ADC performance can be measured with a variety of metrics, including differential and integral nonlinearity and signal-to-noise ratio. The focus of this research is on the pipelined ADC topology, since it offers a competitive balance of both high speed and high resolution. The next chapter presents a background on single-event phenomena in pipelined ADCs.

#### CHAPTER IV

#### SINGLE-EVENT EFFECTS IN PIPELINED ANALOG-TO-DIGITAL CONVERTERS

#### Introduction

Pipelined analog-to-digital converters (ADCs) are a preferred topology for space and military integrated circuits because the resolution and speed performance fit a wide range of applications. Also pipelined ADCs provide an interesting medium to study single-events due to the complex nature of both analog and digital operation. This chapter provides background on previous radiation testing and simulation analyses performed on pipelined ADCs.

# **Heavy Ion Testing**

Only a limited number of results from heavy ion irradiation of pipelined ADCs have been published [55]-[60]. The first pipelined ADC heavy ion testing was performed in 1994 on the 12-bit 5 MSPS AD42961, a device with 4 stages, and stage bit resolutions of 3, 4, 4, and 4 sequentially. This ADC was designed to be radiation-hard against neutron damage, total dose, and single-event latchup (SEL). However, the design did not include any hardening targeted against single-event upsets or single event transients. Errors were calculated by subtracting pre- from post-irradiation histograms of output [6]. The traditional cross-section was modified to include the dynamic sampling operation of an ADC, changing cm²/device to cm²/MS (Mega-sample). Cross-section test results for errors occurring in any bit, defined as raw errors, and also errors occurring only in the 7

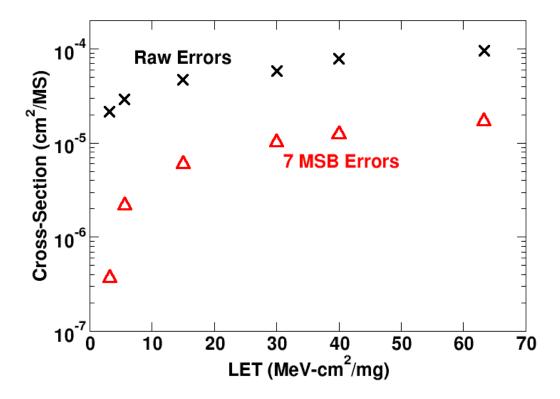


Fig. 25. Heavy ion testing results for the 12-bit 5 MSPS AD42961. Cross-section of all errors is plotted as well as errors only occurring in the 7 MSBs (re-plotted from [55]).

MSBs are shown in Fig 25. The saturated cross-section of errors occurring in the 7 MSBs is about 5 times smaller than the raw errors. Turflinger, et al., attributes the lack of a strong dependence of LET on cross-section in the raw error data to charge collection in the analog circuitry since this circuitry doesn't have a specific critical charge [55]. Using 25% of saturated cross-section as the threshold, the errors in the 7 MSBs have a threshold LET of 10 MeV-cm²/mg. The Turflinger, et al. paper, also estimated the error rates for three different orbits; upsets in the 7 MSBs will occur at rates of about 3, 13, and 62 errors/day for LEO, proton belt, and GEO respectively [55].

Heavy-ion irradiation results of the 12-bit 3 MSPS AD1672 were published in 1999 [55]. The pipelined architecture consists of 4 stages, with stage bit resolutions of 4, 4, 3, and 4 sequentially. The input voltage was swept across the full range and the

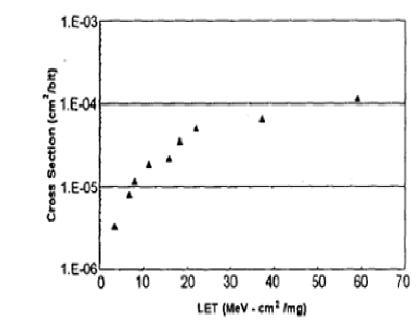


Fig. 26. Heavy ion testing results for the 12-bit 3 MSPS AD 1672 (from [56]).

resulting output was compared to a non-irradiated reference device. The results are shown in Fig. 26. The smallest tested LET, 3 MeV-cm<sup>2</sup>/mg, produced upsets in the AD1672, but no further analysis was performed.

Heavy ion tests of the 12-bit 3 MSPS AD9223 were performed in 2001 using 3 different fixed analog input voltages and comparing the outputs of the device under test (DUT) to a golden chip [57], [58]. The pipelined architecture consists of 4 stages, with stage bit resolutions of 5, 4, 3, and 3 sequentially. Experimental noise prevented any analysis on the last 5 bits, but the authors analyzed errors occurring the 7 MSBs and also errors occurring in only the 4 MSBs. Results from the experiment are shown in Fig. 27 (re-plotted from [57]). The authors did not observe any dependence on input voltage. The lowest LET energy tested, 1.8 MeV-cm<sup>2</sup>/mg, produced upsets in the 7 MSBs while the minimum energy to cause an upset in the 4 MSBs was only 11.2 MeV-cm<sup>2</sup>/mg.

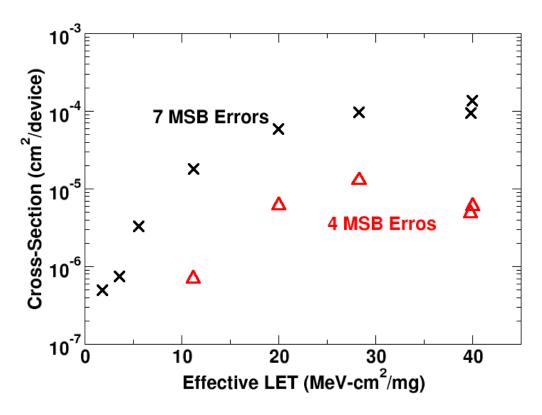


Fig. 27. Heavy ion testing results for the 12-bit 3 MSPS AD9223. Error cross-section in the 7 MSBs and 4 MSBs are shown (re-plotted from [57]).

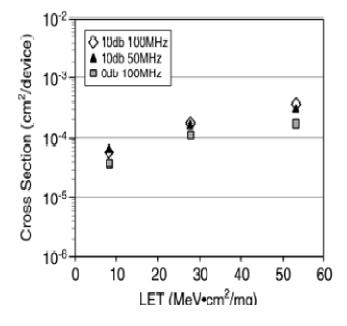


Fig. 28. Heavy ion testing results for the 14-bit 105 MSPS ADS5424 (from [59]).

Heavy ion cross-section measurements on the 14-bit 105 MSPS ADS5424 were performed in 2007 [59], [60]. The pipelined architecture consists of 3 stages, with stage bit resolutions of 5, 5, and 6 sequentially. Input voltage was operated dynamically at 2 different frequencies (50 MHz, and 100 MHz) and also one test was performed using a fixed analog input. The results are shown in Fig. 28 (from [59]). Errors occurred at all tested ion energies. M. D. Berg, et al., planned further analysis, but none has been published at this time [59].

#### **SE** Analysis

# Pipelined ADCs

The first SE simulation analysis on pipelined ADCs was in 2003-2004 [61], [62]. The analysis focused on SPICE simulations of a single 2-bit pipeline stage designed in a 0.8 µm SOI process. SE strikes were simulated at every node for different fixed input voltages and across conversion cycle time. Errors were counted if the simulated SE caused a digital upset or an analog voltage perturbation exceeding 1 LSB. The analysis used error count to determine node sensitivity and temporal window of vulnerability; however error magnitude was not analyzed. Upsets due digital logic and latches were found to be prevalent across the majority of the conversion cycle.

A Monte-Carlo methodology was applied to SPICE analysis of single-events in a 10-bit pipelined ADC, designed in 130 nm bulk CMOS, consisting of all 1.5-bit stages [63], [64]. There are many variables that can affect the response of an ADC to SEs: input voltage, node location, temporal location, and ion energy; Monte-Carlo methodology provides a good compromise between completeness and total analysis time. Results

showed the most frequent errors occurred from SEs in the analog circuitry, MDAC and sample-and-hold amplifier (SHA), however these errors were typically small in magnitude. Large error magnitudes originate from SE strikes in the first couple stages and occurred most frequently due to upsets in the comparators and latches. Error resulting from comparator upsets also showed a dependence to input voltage, primarily due to encoder logic masking and digital error correction.

#### Flash ADCs

The comparators and encoding circuitry in each stage of a pipelined ADC make up a small flash ADC. Previous single-event analyses on flash ADCs will aid in the understanding of single-events in pipelined ADCs. M. Singh, et al., used comprehensive fault injection and nodal weighting, to analyze various ADC architectures, including a flash ADC [65], [66]. The comparators were found to be the most sensitive sub-circuit in the flash ADC topology. Pouget, et al., used a pulsed laser to inject charge at targeted areas of a flash ADC [67]. In addition to using the laser to search for sensitive nodes in the ADC, it was also synchronized to the ADC clock to investigate clock cycle sensitivities. The largest errors came from strikes into the registers storing the MSBs during the clock cycle after the latch operation. S. Buchner, et al., used a pulsed laser to investigate the dependence of input voltages on overall sensitivity of a flash ADC [10], [11]. The tests were performed because there were discrepancies between predicted error rates and on-orbit data. During certain time periods the on-orbit data agreed with the predicted error rates, however other time periods of on-orbit data did not match with the predictions. The on-orbit flash ADC input code was not always the same as what was used for the predictions. This dependence on input voltage for flash ADCs was

confirmed using the pulsed laser. Resulting errors would have different distributions in magnitude and in number depending on the input voltage code and could vary as much as an order of magnitude. It was determined that the encoding logic would sometimes mask errors from the comparators.

# **SE Hardening**

There are many potential sources of SE-induced errors in pipelined ADCs. Reference, clock, and the internal sub-circuits can all be vulnerable to single-event upsets. If one assumes that the clock circuits and reference circuits are independently hardened, then vulnerable subcircuits within the pipeline can be hardened.

Kauppila, et al., recommended using temporally-hardened latches [61], [62]; simulations showed a significant decrease in the window of vulnerability. Sternberg, et. al., recommended increasing the size of the sampling capacitors in the comparator and MDAC sub-circuits and adding resistive feedback to the latches [63], [64]. E. Mikkola, et al., showed auto-zeroing switched-capacitor architectures can limit the duration of upset in the comparators [68]. P. Bellandi, et al., suggested using triple-modular-redundancy (TMR) to protect the digital output registers [69].

M. Singh, et al., presented several recommendations for improving flash ADCs [65], [66]. First, sensitivity analysis should be performed across multiple possible sub-circuits to identify and thus implement the least sensitive sub-circuit. Pattern detection can be used to correct or detect errors resulting from the comparators in a flash ADC. Finally, the size of critical nodes in the comparators should be increased to increase nodal capacitance therefore decreasing the size of injected transients.

## Conclusion

This chapter presents background on single-events in pipelined analog-to-digital circuits. Every experimental test shows a low threshold LET for errors and a high cross-section, including errors in the MSBs. Unless hardening techniques are used, pipelined ADCs will be sensitive to single-events. Previous analyses have shown large magnitude errors can occur from SEs in latches in comparators. Comparator sensitivity to single-events is also seen in Flash ADCs. The more abundant smaller magnitude errors are dominated by the MDAC and S&H sub-circuits.

There is a lack of SE metrics for analyzing the contributions of both error magnitude and frequency. Also previous SE-analyses have focused on minimum stage resolution, even though advanced high-performance pipelined ADC design use multi-bit stages. The current recommendations for hardening are limited; novel radiation-hardened-by-design (RHBD) techniques are needed.

#### CHAPTER V

## FREQUENCY DOMAIN ANALYSIS

The following chapter is a complete excerpt from a previously published manuscript [70].

#### Introduction

The analysis of system-level single-event vulnerability of mixed-signal circuits can be very challenging due to the fact that transients and upsets internal to the analog and digital components do not necessarily appear at the system level. The extent of the single-event response at the system level often does not correlate with the extent of single-event response at the component level. Operating conditions may strongly affect the overall single-event vulnerability of the system. In experimental testing of flash analog-to-digital converters (ADCs), erroneous output data vary widely depending on the chosen fixed input voltage for test [6], [7], [55], [71]. These factors make the single-event analysis of mixed-signal circuits using cumulative individual responses of sub-circuits to obtain the response of the whole system very difficult.

Even comprehensive simulations can lead to complex analysis. In one such study, Sternberg, et al., derives cross-section curves using Monte Carlo simulations of a pipelined ADC [63], [64]. These curves are dependent on the minimum magnitude of error to be considered an upset, a variable that must be chosen by the designer. Furthermore, it is difficult to evaluate and compare single event vulnerabilities when

different design choices for a given circuit topology lead to widely varying error magnitude and frequency distributions. Consequently, concise SEE metrics for complex mixed-signal circuits have been elusive. Such metrics would be particularly useful during the design phase when determining the best techniques for mitigating single-event errors.

Previous work has used frequency domain analysis to evaluate single events in analog circuits [72], [73]. Furthermore, the performance of a commercial mixed-signal circuit is often characterized in the frequency domain. One reasonable approach for an SEE metric is to use some type of frequency domain measurement as a means of comparing the single-event hardness of different mixed-signal circuits or systems. In an ADC application, single-event transients can be considered as externally injected noise, i.e. unwanted disturbances that interfere with the actual signal. Since ADCs are inherently limited by quantization noise, their performance has long been quantified using frequency domain metrics. Therefore, the noise added to the system by single-event transients can be quantified using frequency domain metrics.

Parameters such as signal-to-noise ratio (SNR) and spurious free dynamic range (SFDR) are typically used to evaluate performance in ADCs. In particular, SNR is a parameter that is straightforward to calculate and applicable to a very wide range of analog and mixed-signal systems. This work demonstrates a new method for comparing the single-event hardness of different mixed-signal circuit designs. A SNR metric is used, for the first time, to evaluate tradeoffs between single event vulnerability, area, and power though the use of triple mode redundancy (TMR) [74] in the comparators of a pipelined ADC. This metric enables the designer to optimize a mixed-signal circuit by

comparing the effectiveness of different radiation-hardened-by-design (RHBD) choices via simulation.

# Analysis Example: A Pipelined ADC

# Operation

To illustrate how signal-to-noise ratio can be used to evaluate single-event vulnerability, a pipelined analog-to-digital converter was analyzed. Pipelined ADCs calculate the digital output using an assembly line approach. A simplified block diagram of a pipelined ADC is depicted in Fig. 29. Each stage in the pipeline calculates one or more bits in the digital output word, with the first stage to the last stage generating the most significant bit to the least significant bit, respectively. The pipelined architecture provides a good blend of speed and resolution at the expense of latency, i.e. the time from when the analog signal is first sampled to the time the least significant bit is determined.

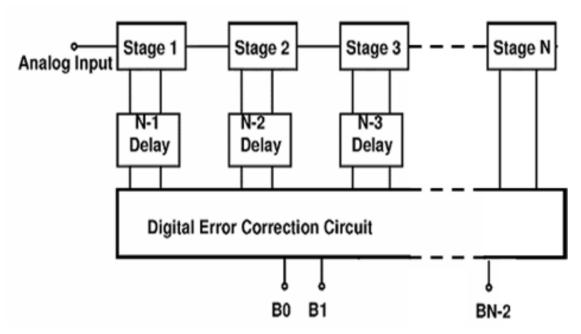


Fig. 29. Simplified pipelined ADC architecture.

However, due to the pipelined approach, the overall conversion rate of the ADC can be quite high since new output data is available at each clock cycle.

# 1.5-bit Stage Design

The pipelined ADC simulated in this work has 10-bit resolution, operates at 100 Megasamples per second (MS/s), and is comprised of nine 1.5-bit stages. Each stage includes a quantizer circuit consisting of two comparators and an encoder to calculate three possible most significant bit-least significant bit (MSB-LSB) pairs, '00', '01', and '10', as shown in Fig. 30. Since the output is comprised of two bits but only three of the four possible bit outputs are used, bit resolution is defined as 1.5-bits. The excluded bit output '11' is not used in order to provide 0.5-bit overlap between stages, thereby allowing for digital error correction (DEC).

The output bit *MSB* becomes part of the ADC digital output, while bit *LSB* is used by the DEC circuit (not shown), except in the last stage of the pipeline. Thus, the first eight stages of the pipeline generate eight output bits, while the last stage generates two output bits to form the complete 10-bit output word.

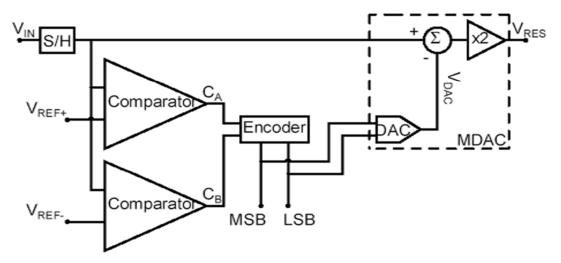


Fig. 30. Simplified pipelined ADC 1.5-bit stage architecture.

TABLE I
OUTPUT STATES OF THE ADC PIPELINED STAGE DECODER

	Thermometer Code		Bit Code		MDAC Offset
Input Value	$C_A$	$C_B$	MSB	LSB	$V_{\mathrm{DAC}}$
$V_{IN} \ge +125 \text{ mV}$	1	1	1	0	+250 mV
$-125 \text{ mV} \leq V_{\text{IN}} < +125 \text{ mV}$	0	1	0	1	0 mV
$V_{IN} < -125 \text{ mV}$	0	0	0	0	-250 mV

Once the quantizer determines the 1.5 bits, the Multiplying Digital-to-Analog Converter (MDAC) generates the residue voltage  $V_{OUT}$  according to the equation

$$V_{OUT} = 2 \cdot (V_{IN} - V_{DAC}) \tag{13}$$

The residue voltage becomes the input for the next stage in the pipeline, with each stage determining the next most significant bit of the ADC output.

MSB and LSB are used to determine the correct MDAC offset. Table 1 shows the range of MDAC offset values assuming a 1 V input range. The comparators evaluate the sampled analog input to generate a two-bit digital thermometer code at outputs CA and CB. The encoder logic for the MSB is

$$MSB = C_A \cdot C_B \tag{14}.$$

The simplest logic for the LSB is

$$LSB = \overline{C}_A \cdot C_B \tag{15}.$$

However, for SEE hardness, an improved LSB logic is

$$LSB = \overline{C}_A \cdot C_B + C_A \cdot \overline{C}_B \tag{16}.$$

The extra encoder logic used for the LSB takes into account the invalid thermometer code, '10'. It ensures that if a single event forces the invalid code then the corresponding error is no greater than the LSB of the stage.

#### Comparator Errors and Triple-Mode Redundancy

One source of significant errors results from single-event upsets in the comparators. If a single event in a comparator forces its output state to flip, then the quantizer will evaluate to an incorrect digital output. Thus, an upset in a comparator can produce an error as large as the most significant bit for that stage. In a pipelined converter with multiple stages, upsets occurring earlier in the pipeline will generally create a much larger error in the digital output word and thus have a much greater effect on SNR than upsets occurring later in the pipeline. Thus, SNR can be used to effectively represent not only the presence of errors but also the severity of the errors at the system level.

At this point it should be emphasized that using SNR to characterize the singleevent errors in a fabricated ADC would have little benefit unless the error rate was extremely high. In most radiation environments, the SNR reduction due to single-event strikes would be extremely small. With a simulator, however, the error rate can be set to any arbitrary level, making the SNR an excellent means of evaluating different design choices.

The application of triple-mode redundancy (TMR) to the comparators at various stages of the pipeline was used to demonstrate the usefulness of frequency domain analysis for evaluating system-level response of pipelined ADC circuits. TMR has significant area and power penalties and is generally avoided unless absolutely necessary.

For a pipelined topology, an acceptable tradeoff would be to limit TMR to just the first few stages. Since each subsequent stage provides a decreasing contribution to the final output value in a pipelined ADC, .the system-level benefit of using comparator TMR on later stages may be essentially negligible depending on the design requirements. Therefore, frequency domain analysis was used to determine the optimum number of stages for maximum benefit at minimum area / power penalty.

## Model Setup

To determine the optimal number of stages for applying comparator TMR, a C++ behavioral model was created for the 10-bit ADC. The model calculates the appropriate analog sinusoid input voltage for the given clock period and the comparator logic then produced the corresponding thermometer code. A table indexed by the thermometer code was used to generate the stage's bit output and the appropriate offset to the MDAC. Finally the residue voltage was calculated using (13). This process was repeated through all the stages using the residue voltage of each stage as the input to the subsequent stage.

Upsets were injected randomly to avoid mathematical artifacts in the frequency domain. A random number generator was used to determine when an upset occurred based on a chosen injected upset rate. The location of the comparator to be upset across the entire ADC was also determined using a random number generator. This information was then used to flip the specific comparator output during the ADC model operation. An ideal digital-to-analog conversion was made on every digital 10-bit output word, and a fast Fourier transform (FFT) was performed on this stream of analog output values. Figs. 31 and 32 show the FFT plots for the pipelined stages without and with injected errors, respectively. SNR was then calculated and used as the metric of comparison.

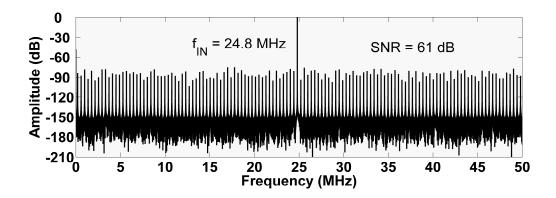


Fig. 31. Example FFT of C++ pipelined ADC model using 2<sup>20</sup> simulated samples.

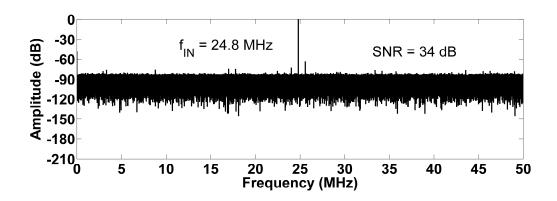


Fig. 32. Example FFT of C++ pipelined ADC model with injected comparator upsets. A single comparator had a probability of 0.1% to upset during a sample. The simulation used  $2^{20}$  simulated samples.

#### 10-bit ADC Results

The results of the using comparator TMR on a limited number of stages are shown in Fig. 33. In this figure, SNR is plotted with respect to the number of stages in which comparator TMR was applied. In each of these cases, comparator TMR was applied to stages consecutively starting with the first stage, which contributes the most significant bit in the final digital word. This figure indicates that the application of comparator TMR to the first half of the 10-bit pipelined ADC produces the best tradeoff in decreasing single event vulnerability versus increasing area and power. Note that the

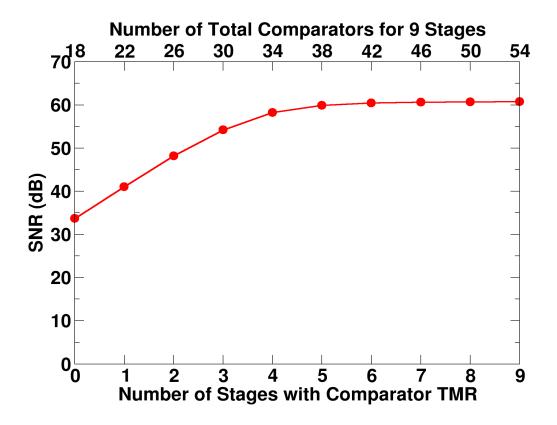


Fig. 33. Signal-to-noise ratio improvement for increasing use of comparator TMR in a 10-bit pipelined ADC. The results shown are for a model with an individual comparator upset probability of 0.1%.

simulated error rate was deliberately set very high to provide an upper bound valid over a broad range of radiation environments.

The SNR metric provides a good comparison between using comparator TMR on varying number of stages. However, it is not clear how comparator TMR affects the distribution of errors resulting from SEUs in the comparators. The raw error data is plotted in Figs. 34 and 35. Fig. 34 is a reverse cumulative distribution function of the error. Fig. 35 shows the probability density function of the raw error data.

As expected, both figures show that using comparator TMR eliminates errors in the stage's corresponding significant bits. Fig. 34 clearly shows the errors occurring in

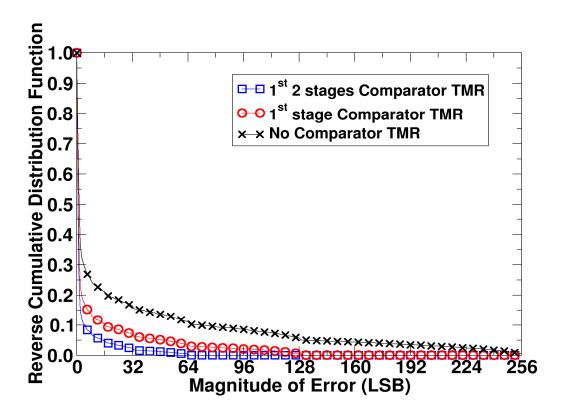


Fig. 34. The reverse cumulative distribution function of the raw data produced when upsets are injected randomly in the comparators of the pipelined ADC. Fraction of occurrence is plotted with respect to the summation of error magnitudes greater than the corresponding x-axis value.

bits further down the pipeline are also reduced. Since the inherent digital error correction (DEC) associated with the pipelined architecture will provide partial error correction, some upsets in a given stage may only generate errors in less significant bits of the ADC output. When comparator TMR is applied to a stage, not only are errors corresponding to the stage's significant bits eliminated, but also errors that would have been partially corrected by the DEC. Fig. 35 has spikes in the probability density function occurring at the most significant bit of each stage. The spikes correspond to the probability density function of a sinusoid. Since a sinusoid is used as an input to the ADC, the input voltage is more often at the extreme magnitudes, and errors are more likely to occur when the

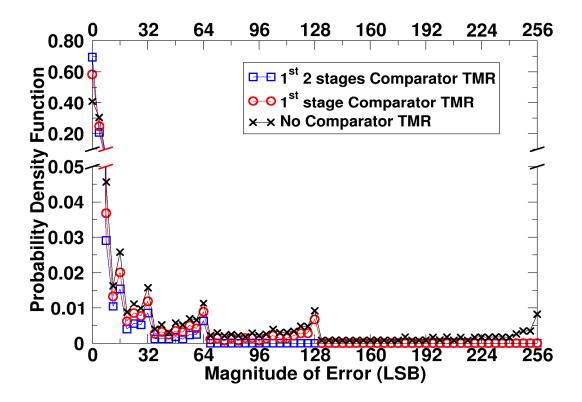


Fig. 35. The probability density function of the raw data produced when upsets are injected randomly in the comparators of the pipelined ADC.

input is at the maximum and minimum values. Even when no comparator TMR is used, not every comparator upset—will produce an error at the output, as some will be completely corrected by the DEC. Fig. 35 shows that full correction occurs 41% of the time when using no comparator TMR, 58% of the time when using comparator TMR on the 1st stage, and 70% of the time when it is used on the 1st two stages.

## 12-bit and 14-bit ADC Results

The results of the 10-bit ADC analysis leads to a new question: is comparator TMR for the first four or five stages sufficient for a pipeline ADC of any resolution, or is the optimum number of hardened stages a function of ADC resolution? To determine the answer, the next set of simulations compared 12-bit and 14-bit ADCs. The results of

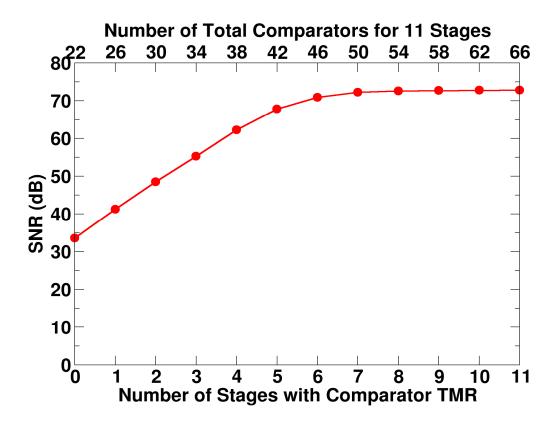


Fig. 36. Signal-to-Noise Ratio improvement for increasing use of comparator TMR in a 12-bit pipelined ADC. The results shown are for a model with an individual comparator upset probability of 0.1%.

these simulations are shown in Figs. 36 and 37. In all three figures (33, 36, and 37) the SNR improvement reaches a point of diminishing return when comparator TMR is applied to the first half of the pipeline. The apparent conclusion is that TMR is best utilized for the same initial percentage of the pipeline regardless of resolution.

# *Upset Injection Rate*

Finally, the effect of upset injection error rate on SNR was simulated. Fig. 38 shows the impact of the error rate on SNR. Error rate is defined as the fractional likelihood a sample contains an injected comparator upset. As the error rate decreases, the SNR increases at the rate of 10 dB per decade. As expected, the SNR due to single-event errors approaches the ideal SNR at very low error rates, with the effective single-

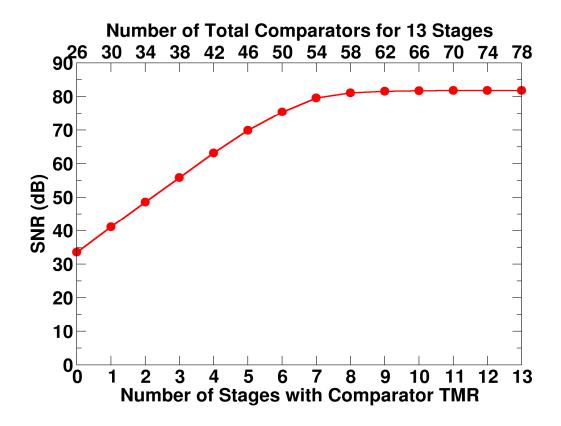


Fig. 37. Signal-to-Noise Ratio improvement for increasing use of comparator TMR in a 14-bit pipelined ADC. The results shown are for a model with an individual comparator upset probability of 0.1%.

event "noise" level merging into the quantization noise floor of the ADC. Maximum error rate simulations were performed in which an upset occurred in one of the comparators on every data sample. Fig. 39 shows the same data as Fig. 33, plus data for the described maximum error rate. Even though this case is obviously not realistic for most applications, it does provide a worst-case boundary. Using this worst-case data leads to the conclusion that a designer should apply comparator TMR only to the first two-thirds of the pipeline at the very most. Even with extremely high SEE error rates, no significant SNR benefit is derived by TMR hardening of the last third of the ADC

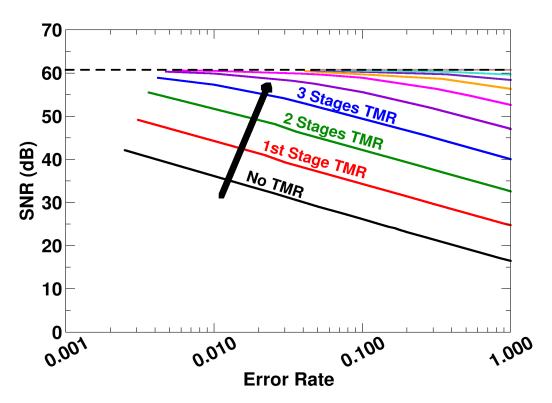


Fig. 38. The pipelined ADC signal-to-noise ratio has a power log relationship with the system error rate. The results shown are calculated from the 10-bit pipelined ADC model. Error rate is defined as the fractional likelihood a sample contains an injected comparator upset.

pipeline. In practice, most designers may choose to limit TMR to the first half (or less) of the pipeline, depending on the expected radiation environment.

## **Conclusions**

Signal-to-noise ratio provides an excellent metric when comparing different single-event mitigation design choices in an ADC. Frequency domain analysis was used to find the point of diminishing returns for the use of TMR on the internal comparators of a pipelined ADC. Even assuming extremely high comparator upset rates, comparator TMR is most effective when applied to the first 50% to 70% of the total number of stages in a 1.5-bit/stage pipelined ADC, regardless of the overall resolution.

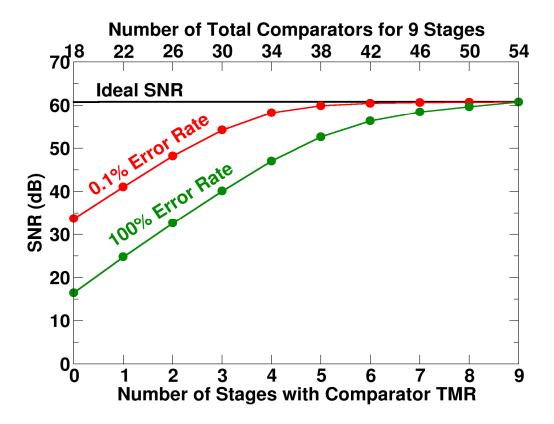


Fig. 39. Comparison of comparator upset probability 0.1% and 100%. The results shown are calculated from the 10-bit pipelined ADC model.

Clearly, the biggest advantage of using SNR is not to evaluate the performance of one particular circuit, but to compare the performance of two or more different RHBD techniques on the same circuit or system, or to compare the relative hardness of two or more different circuit topologies. In such situations, the simulated error rate can be set sufficiently high enough to allow the designer to make a valid comparison between designs. Because signal-to-noise ratio is so commonly used to characterize analog and mixed-signal systems, the SNR metric should prove equally useful in quantifying the benefit of future RHBD techniques applied to a very broad range of designs such as analog-to-digital converters, digital-to-analog converters, RF circuits, and analog signal processing circuits.

#### **CHAPTER VI**

#### **MULTI-BIT STAGES**

The following chapter is a complete excerpt from a manuscript prepared for publication.

#### Introduction

Analog-to-digital converters (ADCs) are essential to many space and military applications. The pipelined ADC topology offers a good balance of speed and resolution. This topology works by employing an assembly-line approach of quantizing a portion of an analog signal, amplifying the un-quantized signal, and passing that signal to the next stage.

Pipelined ADCs were originally designed with a typical stage resolution of 1.5-bits, which provides an optimal tradeoff between speed, area, and power [75]. However, thermal (kT/C) noise due to random fluctuation of charge carriers becomes a major constraint for pipelined ADC resolutions greater than 10 bits [76]. Designs become cumbersome when pipelined ADCs use only 1.5-bit stages, as thermal noise forces the use of large multiplying digital-to-analog converter (MDAC) capacitors which consume valuable area and require more power. These thermal noise requirements can be lessened through the use of multi-bit stages, particularly at the front of the pipeline. Some common examples of commercial pipelined ADCs using multi-bit stages are

Analog Devices's AD9246, Linear Technology's LTC2209, and National Semiconductor's ADC14C080.

Several papers describing methods for selecting the most optimal stage resolutions for pipelined ADCs [75]-[79] have been published, where the number of bits per stage is calculated according to the performance requirements of the desired ADC application. For this paper, the most optimal configuration is not a concern, beyond the assumption that multi-bit stages will be used in a pipelined ADC design.

Many pipelined ADCs have undergone heavy ion testing: examples include Analog Devices's AD42961, AD1672, and AD9223 and Texas Instrument's ADS424 [55]-[60]. LET thresholds for these parts range from 1.8 MeV-cm<sup>2</sup>/mg to 11.2 MeV-cm<sup>2</sup>/mg. Unless SE-RHBD techniques are used, pipelined ADCs will be sensitive to single-events.

There are many potential sources of SE-induced errors in pipelined ADCs. Reference, clock, and the internal sub-circuits can all be vulnerable to single-event upsets. If one assumes that the clock circuits and reference circuits are independently hardened, then vulnerable sub-circuits within the pipeline can be hardened. Previous research involving a comprehensive simulation analysis of 1.5-bit stages concluded that the internal comparators and MDACs were the most sensitive sub-circuits [63] within the pipeline stages. This work also recommended improving SE-hardness in the comparators by increasing capacitance sizes and adding resistive feedback in the latch [63].

Several additional techniques have been developed to improve the SE-sensitivity of the comparator sub-circuits. One technique limits the duration of upset by using an auto-zeroing architecture for comparators [68]. Another technique reduces the

vulnerability of internal floating nodes in sample-and-hold and MDAC sub-circuits [80], [81]. Triple-modular-redundancy (TMR) is recommended to protect the digital output registers [69]. The application of TMR to the comparators in 1.5-bit stages has also been analyzed [70].

This paper expands upon previous work in RHBD pipelined ADC design by employing analysis and simulations to compare the differences in single-event response of 1.5-bit stages versus multi-bit stages. The single-event error analysis focuses on the two main sub-circuits of a pipelined ADC stage: the quantizer (comparators and encoder) and the MDAC. An RHBD technique suitable for reducing single-event errors in multi-bit stages is also described. This technique limits single-event bit upsets in the encoder to a maximum of one LSB for any multi-bit stage, with only minimal layout penalty.

# **Background**

The pipelined ADC topology consists of a cascade of stages as shown in Fig. 40. A single stage quantizes a portion of the analog signal, amplifies the remaining signal residue, and passes it to the next stage. A single pipeline stage consists of a low-resolution flash ADC, an MDAC, and the corresponding encoder logic.

The flash ADC is comprised of 2<sup>N</sup>-2 comparators and 2<sup>N</sup>-1 resistors, where N is the stage resolution. The resistor string provides reference voltages for the comparators. Typically, a pipeline stage will not quantize the top bit code (i.e. 11...1), as this extra bit code creates an overlap with the following stage to provide digital error correction. Each comparator compares the input voltage to a different voltage from the reference resistor string. The comparator outputs generate a thermometer code, where the number of

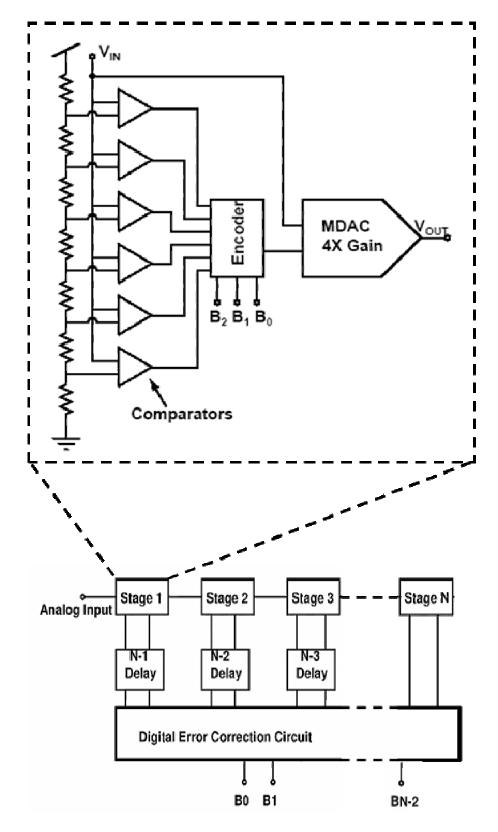


Fig. 40. Block diagram of an N-stage pipelined ADC. A 3-bit block diagram of a stage is also shown.

comparators generating a logic 1 output value changes according to the magnitude of the input voltage (which conceptually looks like a thermometer rising and falling, hence the name). The thermometer code is then converted to a 1-of-N code composed of all logic 0's except for a logic 1 at the thermometer code's transition from 1's to 0's. Each bit in the 1-of-N code  $(1ofN_i)$  is determined from thermometer code bits  $(T_n)$ . This encoding process is commonly performed using one of two possible minimal encoder topologies. The 1-of-N code can be either determined by taking the complement of the subsequent bit with the current and previous bits,

$$1ofN_i = \overline{T}_{n+1} \bullet T_n \bullet T_{n-1} \tag{17},$$

or it can be determined from the complement of the next two subsequent bits with the current bit.

$$1ofN_i = \overline{T}_{n+2} \bullet \overline{T}_{n+1} \bullet T_n \tag{18}.$$

The thermometer to 1-of-N code conversion typically uses 3-input NAND gates to implement either (17) or (18). The 1-of-N code is then used to access the correct bit code from a ROM (read-only memory) table, which is then used to configure the switched-capacitor input network of an MDAC in order to correctly compute the residue voltage for the next stage in the pipeline.

### Single-Event Analysis of the Comparators

SE-Response of 3-Input NAND Encoding Schemes

Comparator metastability and component mismatch are critical design concerns for high-speed flash ADCs, often leading to erroneous 1's or 0's appearing near the transition point in the thermometer code. These errors are commonly referred as bubble errors (analogous to bubbles in a mercury thermometer).

The encoding schemes described in (17) and (18) are typically used in commercial designs because they provide adequate bubble error correction at minimal design cost [82]. Equation (17) will produce the correct 1-of-N code for any single erroneous 1 surrounded by 0's. Similarly, equation (18) will produce the correct 1-of-N code for any single erroneous 0 surrounded by 1's. However, these encoding schemes fail for bubbles on the opposite side of the thermometer code transition. For equation (17), an erroneous 0 surrounded by 1's that is two bits from the transition will produce a incorrect 1-of-N code that is 2-bits apart from the correct 1-of-N code. Likewise, the opposite erroneous case for equation (18) will also occur. Significantly worse are those cases in which the bubble error (a 0 surrounded by 1's in equation (17), or a 1 surrounded by 0's in equation (18)) occurs 3-bits or greater from the thermometer code transition. These cases will produce two 1's in the 1-of-N code, causing multiple ROM rows being accessed and thus a wired-OR response between two output words.

Fig. 41 is an illustration of a thermometer code error causing multiple ROM rows to be accessed. In this example, a 3-bit stage should ideally evaluate the input voltage to a bit code of '010'. However, a bit flip in the thermometer code is exacerbated by two 1's appearing in the 1-of-N code, accessing multiple ROM rows. As a result, both the most significant bit (MSB) and the least significant bit (LSB) are flipped, erroneously generating the top bit code which is reserved for digital error correction. While this may not be a problem for many commercial applications, it is a concern for space and military applications requiring applications to be single-event robust.

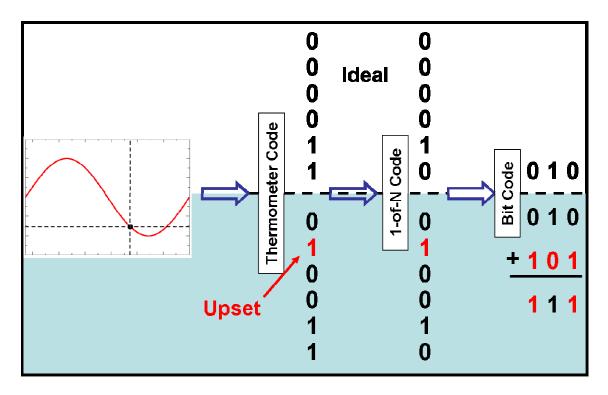


Fig. 41. Illustration of a thermometer code bit flip leading to the 1-of-N code accessing multiple ROM rows. The ideal response is shown in the top-half of the figure, while an erroneous response is shown in the bottom-half. The output is effectively a wired OR of two output words. The final result is an error in the bit code's MSB and LSB.

#### SE-Response of a More Robust Encoding Scheme

Every single-bit error for all possible thermometer codes can be classified into one of three categories. The first category is the correctable errors. These errors are unique to a single specific valid thermometer code, and thus can be corrected. The second category is the errors that cannot be corrected because the erroneous code is identical to (and indistinguishable from) a valid thermometer code. Fortunately, every one of these cases occurs only 1 LSB from the correct code. The final category is partially correctable errors. These errors produce an erroneous code that could have occurred from two possible valid thermometer codes. In each of these cases the two possible valid thermometer codes are 2 LSBs apart. The designer has two choices. One

choice is to arbitrarily assign the erroneous code to one of the valid codes, leading to a potentially correct response or to a 2 LSB error. The other option is to assign the erroneous code to the thermometer code in between the two possible valid codes, limiting any error to at most 1 LSB.

Previous work has investigated alternative encoder topologies in order to improve tolerance to thermometer code errors when compared to encoders implemented using (17) and (18). A more robust quantizing scheme was developed to protect against metastability issues in flash ADCs [83], and later reintroduced to improve SEU tolerance in flash ADCs [84]. However, this technique can also be applied to the encoder of a pipelined ADC stage. This alternative encoding scheme evaluates a 1-of-N code using the equation

$$1ofN_i = \overline{T}_{n+2} \bullet (T_{n+1} \oplus T_n) \bullet T_{n-1}$$
(19).

This encoding scheme eliminates all correctable thermometer code errors. Also, for partially correctable errors, this code assigns these those errors to the thermometer code value between the two possible valid thermometer codes. Unlike standard 3-input NAND logic encoders, this encoding scheme ensures that only a single ROM line will be accessed for any single bit thermometer code upset. Most importantly, this technique limits the maximum word error for the stage to a single LSB, regardless of the resolution of the pipeline stage.

SE-Simulations of the 3 Different Encoding Schemes

The response of the pipelined ADC to single-event upsets originating from the comparators was studied using a behavioral model. The model allowed effective analysis

of various stage design options without the need for a transistor-level design of each circuit. A 10-bit pipelined ADC model was created in C++, which sampled a simulated 1-V<sub>P-P</sub> 24.8 MHz signal at 100 MSPS for a total of 2<sup>20</sup> samples. The ADC's LSB is approximately equal to 0.98 mV. Comparator upsets were injected randomly during operation, with a probability that an individual comparator would upset at any particular sample set to 0.1%. The relatively high probability was chosen to make comparator SEU errors easily distinguishable from quantization error. Comparator upsets were simulated as bit flips in the thermometer code. The ADC behavioral model was created using a 4-bit front-end stage, followed by seven 1.5-bit stages. A count of errors for both NAND encoding schemes, shown in equations (17) and (18), and the more robust encoding scheme shown in equation (19) are depicted in Fig. 42. Errors from ideal are measured in multiples of the ADC's LSB. The error distribution is not symmetric for either of the 3-input NAND logic schemes and error magnitudes can also be quite large, e.g. -896 LSBs for (18), and 349 LSBs for (17). This result is not surprising since upsets can lead to multiple rows of the ROM being accessed, resulting in a convoluted ADC error response. Single-events causing multiple ROM rows to be accessed have also been seen with encoding logic using XOR gates [11]. The response of (19) is significantly better. For a 1-V<sub>P-P</sub> input signal, a 1 LSB error in the 4-bit front-stage will cause a maximum 64 LSB error in the final 10-bit ADC output. The largest errors produced by random comparator upsets in the entire pipelined ADC correspond to a 1 LSB error in the 4-bit front-stage.

To evaluate the effectiveness of this coding scheme, it was necessary to compare the single event response of the multi-bit stage ADC to a 1.5-bit stage ADC. In previous

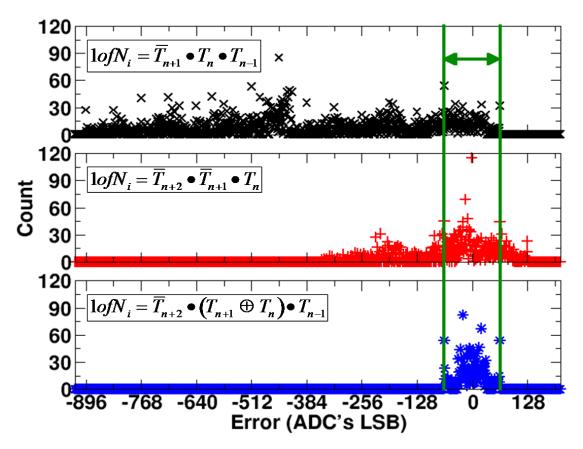


Fig. 42. The count of errors resulting from randomly injected comparator upsets in a 10-bit pipelined ADC. It contains a 4-bit front end stage followed by seven 1.5-bit stages. The response to three different encoder logic schemes in the front-stage is shown. A 1 LSB error in a 4-bit front stage will cause a maximum 64-bit error, illustrated by the green lines, in the final 10-bit ADC output.

work, comparator triple mode redundancy (TMR) in 1.5 bit stages was analyzed using a signal-to-noise (SNR) metric [70], where simulated comparator upsets in an ADC behavioral model were randomly injected, and the results analyzed by performing a fast Fourier transform (FFT) on the resulting signal and calculating the SNR. SEs in mixed-signal applications are normally difficult to evaluate because the complex distribution of errors they vary in rate and magnitude. During analysis, the error probabilities of different designs can be proportionally scaled causing a constant shift of 10 dB/decade in the SNR metric. By setting a high error rate during simulation, the SE response can be

pushed above the noise floor so that comparisons between two different RHBD techniques can be made.

The comparison of a 10-bit pipelined ADC using 1.5-bit and multi-bit stages is shown in Fig. 43. This figure plots SNR with respect to the total number of comparators in the entire 10-bit ADC. For the baseline case of all 1.5-bit stages, (9 stages with a total of 18 comparators) the SNR is 34 dB. The SNR metric can be improved using comparator TMR progressively starting with the first stage (22 total comparators) to obtain an SNR of 41 dB, using it in the first two stages (26 total comparators) to obtain an SNR of 48 dB, and progressing through the pipeline (adding 4 comparators per stage).

The results of using 3-, 4-, and 5-bit front-end stages are plotted in Fig. 43. Multibit stages using a standard 3-input NAND logic encoder do not compare well to the 1.5-bit stages, and consequently should not be used in high radiation environments. Since multi-bit stages have increasing number of comparators, the number of SE vulnerable comparators in 3-input NAND logic schemes also increases, leading to a worsening SE response with increasing resolution as shown in Fig. 43. By contrast, the robust encoding logic scheme of (19) is far more effective against single-event upsets. Unlike standard 3-input NAND logic encoders, where SNR worsens at higher front-end stage bit resolutions, the robust logic encoder improves SNR by limiting the size of the error to the LSB of the stage. For the same pipeline resolution, the 4-bit stage has nearly the same SNR (47 dB) as three 1.5-bit stages where the first two stages utilize comparator TMR (48 dB). Both cases have 26 total comparators, so no significant area penalty results.

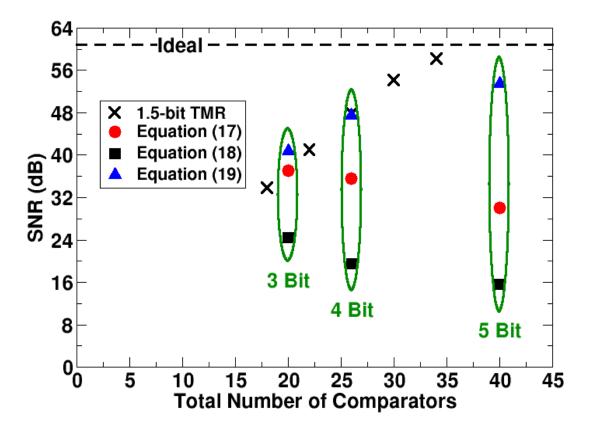


Fig. 43. SNR is used as a metric of comparison for various 10-bit pipelined ADC designs with simulated randomly injected comparator upsets. Three different quantization logic schemes are investigated across three multi-bit (3,4, and 5) frontend stages. Also previous work on the use of comparator TMR in 1.5-bit stages is shown for comparison [70].

As a comparison to the robust encoding logic scheme of (19), comparator TMR could be applied to multi-bit stages. All errors due to comparator upsets can effectively be mitigated (including LSB errors) using TMR, but the area and power penalties are significant, since the number of comparators required increases to  $3*(2^N-2)$ . Consequently, the robust encoding scheme provides a much better cost-to-benefit ratio than brute-force triple-mode redundancy.

Note that the results in Fig. 43 are only applicable for pipelined ADCs where the first stage is multi-bit. It is also worthwhile to evaluate the effectiveness of the robust

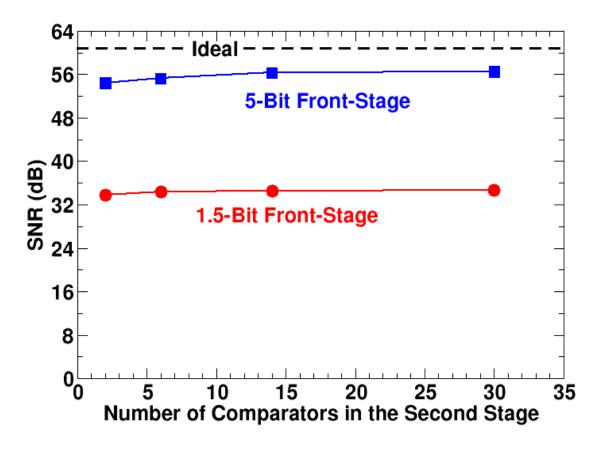


Fig. 44. SNR is used as a metric of comparison for various 10-bit pipelined ADC designs with simulated randomly injected comparator upsets. The robust logic is used for increasing second-stage resolution.

logic encoder in later pipeline stages. Simulated SNR results for 10-bit pipelined ADCs with two different front-stage resolutions (1.5- and 5-bit) and increasing 2<sup>nd</sup>-stage resolutions are shown in Fig. 44. Negligible improvement is seen for increasing second-stage resolution, since the larger errors resulting from upsets in the first stage will dominate.

# Single-Event Analysis of the MDAC

# SE-Response of the MDAC

Assuming the analog single-event-transient (ASET) distributions between multibit MDACs and 1.5-bit MDACS are the same (to the first order), the effect of increased per-stage resolution on the entire ADC can be better understood. First, pipelined ADCs using multi-bit stages will have fewer MDACs, as illustrated in Fig. 45. Shown are three 1.5-bit stages, which is equivalent to a single 4 bit stage. Since every stage contains an MDAC, the design using the 4-bit stage will have two fewer MDACs resulting in a smaller sensitive volume. Also, because of the assembly line approach of the pipeline topology, the error at the output of the entire pipelined ADC ( $\Delta V_{ADC}$ ) is equal to the ASET error at the output of the stage ( $\Delta V_{MDAC}$ ) is divided by the total gain (G) in the pipeline up to that stage and can be represented by the following equation,

$$\Delta V_{ADC} = \left(\prod_{i=0}^{k} \frac{1}{G_i}\right) \bullet \Delta V_{MDAC_k} \pm Q \tag{20}$$

where Q is the quantization error of the ADC. The gain of a 1.5-bit stage is 2, while multi-bit stages have gains of 4, 8, and 16 for 3-bit, 4-bit, and 5-bit resolutions, respectively.

Even though an identical ASET in the MDACs of different stage resolutions will produce a similar response at the output of the MDAC, the final ADC outputs will have errors of different magnitudes. These errors are scaled by the gain of the stage, as shown in equation (20). For example, the response of a 4-bit stage can be compared to the equivalent response of three 1.5-bit stages by considering an ASET with a magnitude of 128 mV. The gain of the 4-bit stage is 8, so the equivalent output error voltage at the

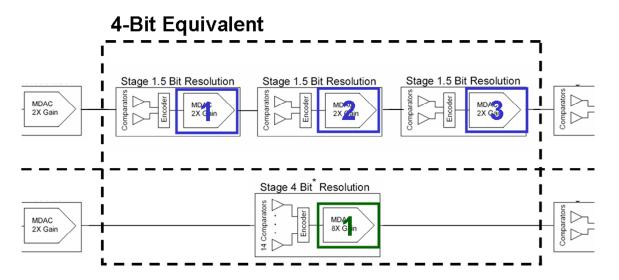


Fig. 45. It takes three 1.5-bit stages to be equivalent to a single 4-bit stage. Since every stage contains an MDAC, a pipelined ADC using a 4-bit stage will contain 2 fewer MDACs than one using all 1.5-bit stages.

system level is only 16 mV. In the case of three 1.5-bit stages, with a gain of 2 in the first stage, the same error at the system level would be 64 mV. In other words, while a 128 mV error in a 4-bit front-end stage MDAC would result in a 16 mV error at the final output, the same ASET could result in a 64 mV error in a 1.5-bit front-end stage MDAC. *SE-Simulations of the MDAC* 

A detailed analysis was performed using SPICE simulations of 1.5-bit and 3-bit MDAC designs, as shown in Fig. 46. The MDACs were designed using IBM 9SF CMOS device models. Simulations were performed across 7 input voltages, 20 temporal locations, and SE strikes of 10 and 40 MeV-cm<sup>2</sup>/mg at every MDAC node. Heavy ion strikes were simulated using calibrated current source models [50].

The SE maximum error at the output of the MDAC is dependent on the size of the feedback capacitors ( $C_f$ ). Floating input nodes will exist in the switched-capacitor feedback network during the evaluate phase [80], [81]. Since there is no restoring current

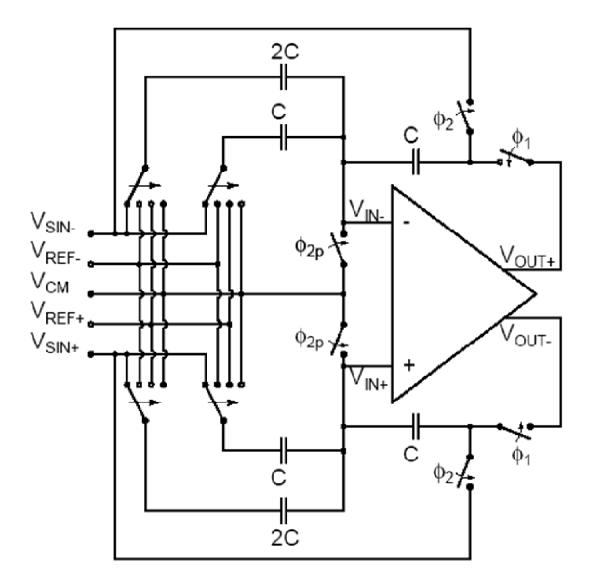


Fig. 46. The schematic of the 3-bit MDAC. The 1.5-bit MDAC is a similar design, except without the 2C sampling capacitors

at these floating nodes, any charge deposited will be stored on the capacitors and show up as a voltage error according to the fundamental equation

$$Q = C \cdot V \tag{21}$$

These floating nodes exist during MDAC operation regardless of bit resolution. Fig. 47 shows the maximum error magnitude at the output of 1.5-bit and 3-bit MDAC for varying  $C_f$  due to a simulated heavy ion with an LET of 40 MeV-cm<sup>2</sup>/mg. There is a negligible

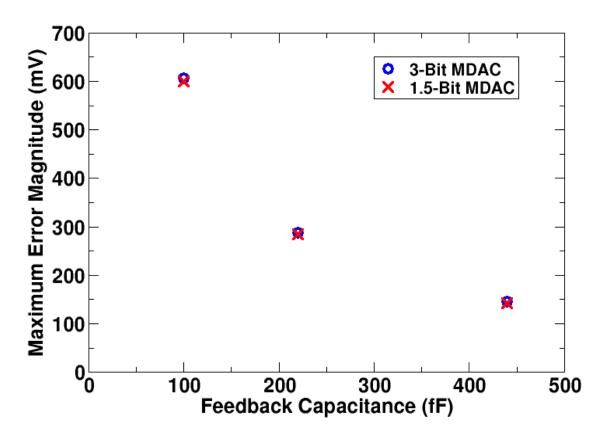


Fig. 47. Maximum error magnitude due to SEs at the MDAC output for varying feedback capacitance. Results are obtained using a simulated SET with an LET of 40 MeV-cm<sup>2</sup>/mg.

difference between maximum error magnitude at the output of the 1.5-bit and 3-bit MDAC, but a clear dependence on  $C_f$  for both circuits.

An MDAC SE sensitivity comparison between pipelined ADCs containing a 1.5-bit or a 3-bit front-stage was simulated using thermal noise constraints as the primary design constraint. Thermal noise equations for pipelined ADCs are available in the literature [54], [76]. Two pipelined ADCs topologies were designed to have equivalent thermal noise with a 1-V<sub>P-P</sub> signal range, fully differential topologies, 10 bits of total resolution, and a minimum allowable capacitor size of 100 fF. The first topology, (A), used nine 1.5-bit stages, while the second topology, (B), contained a 3-bit front-end

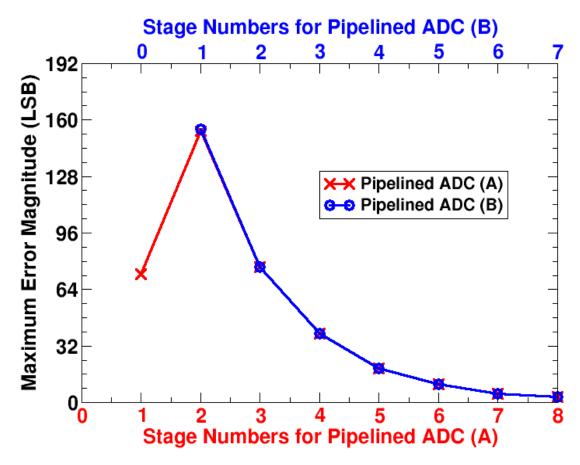


Fig. 48. Maximum error magnitudes per stage are shown for two 10-bit pipelined ADCs with equivalent thermal noise. (A) consists of all 1.5-bit stages, has  $C_f$  of 440 fF in the front-stage while all remaining stages have  $C_f$  of 100 fF. (A) use the bottom x-axis. (B) consists of a 3-bit front-stage with  $C_f$  of 100 fF and all remaining stages are 1.5-bit with  $C_f$  of 100 fF. (B) uses the top x-axis. Errors from ideal are measured in multiples of the ADC's LSB. Pipelined ADC (B) has one fewer stage. Also, the maximum SE error at each stage output in (B) is equivalent to errors starting at  $2^{nd}$  stage in (A). Results are obtained using a simulated SET with an LET of  $40 \text{ MeV-cm}^2/\text{mg}$ .

followed by seven 1.5-bit stages. The value of  $C_f$  in the first stage for the all 1.5-bit topology, (A), was calculated to be 440 fF, while  $C_f$  for the first stage of the 3-bit frontend topology, (B), was calculated to be 100 fF. Both ADC topologies used a  $C_f$  of 100 fF for all MDACs following the first stage.

The maximum error at the output of the ADC due to SE strikes in each stage's MDAC is shown in Fig. 48. The maximum error for the pipelined ADC constructed from

1.5-bit stages, (A), occurred from strikes in the second stage, due to the smaller (100 fF versus 440 fF) capacitors in the second stage. In this example, the pipelined ADC with a 3-bit front end, (B), overlaps the response of the final seven stages of (A), and will have the same maximum MDAC error. However, the all 1.5-bit design has errors produced by an additional stage, the first stage, and thus this circuit will have a larger sensitive area than the pipelined ADC with a 3-bit front-end.

While the number of stages dominated the calculation of the MDAC sensitive area, the increased number of nodes necessary to implement a multi-bit MDAC contributes a second-order effect. For a more detailed comparison of sensitive area, each error was weighted by the SPICE simulation node area. For simulations of SE strikes in the MDACs with LET of 10 MeV cm²/mg, an error of at least 16 LSBs was produced in a total area of 7.3X10<sup>-8</sup> cm² of the all 1.5-bit stages ADC, while the same error was produced in a total area of only 4.8X10<sup>-8</sup> cm² in the ADC with a 3-bit front-end. An LET of 40 MeV cm²/mg produced an error of at least 32 LSBs in areas of 7.7X10<sup>-8</sup> cm² and 5.4X10<sup>-8</sup> cm² in the pipelined ADCs of all 1.5-bit stages and 3-bit front-stage, respectively.

While thermal noise constraints provide a good starting point in determining capacitor size, it may also be necessary to increase  $C_f$  in order to meet SE sensitivity requirements. Fig. 49 shows a decrease in maximum front-end error for increases in  $C_f$  for SE strikes with LET of 40 MeV-cm<sup>2</sup>/mg. Increasing the front-end  $C_f$  to 220 fF decreases the maximum MDAC error from 155 to 77 LSBs. Increasing  $C_f$  to 440 fF does decrease the maximum error occurring in the front-stage to 37 LSBs, but 77 LSB errors still occur from the  $2^{nd}$  stage. SE strikes produced an error of at least 32 LSBs in areas

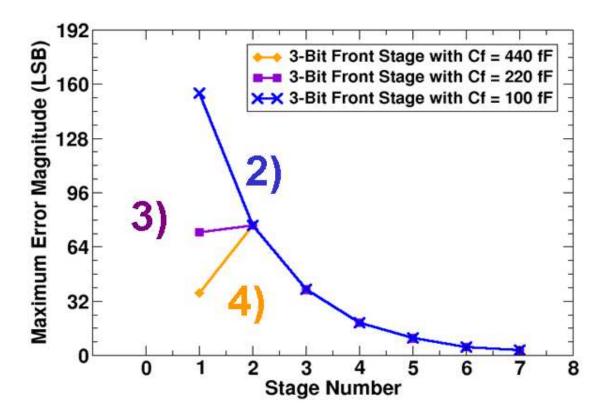


Fig. 49. Maximum error magnitudes per stage for 10-bit pipelined ADCs with consisting of a 3-bit front-stage of varying  $C_f$  followed by all 1.5-bit stages with  $C_f$  of 100 fF. Front-stage  $C_f$  in 2) is 100 fF, in 3) is 220 fF, and in 4) is 440 fF. Errors from ideal are measured in multiples of the ADC's LSB. Results are obtained using a simulated SET with an LET of 40 MeV-cm<sup>2</sup>/mg.

of  $4.8X10^{-8}$  cm<sup>2</sup> and  $4.0X10^{-8}$  cm<sup>2</sup> in the pipelined ADCs with 3 bit front-stage  $C_f$  of 220 fF and 440 fF, respectively.

So what do these results indicate to a designer seeking to minimize MDAC errors due to single-event strikes? For a given ADC resolution, implementing a pipelined ADC with a multi-bit front-end will result in fewer stages with less sensitive area, and smaller areas capable of generating larger multi-LSB errors. However, the need to reduce the magnitudes of single-event error voltages for a particular application may also force a designer to increase capacitor sizes beyond the values required to meet thermal noise

requirements. Consequently, the standard optimization of area versus power versus thermal noise for pipelined ADCs as found in the literature may not be possible in an RHBD circuit.

To summarize, if a designer does choose to implement a multi-bit front end for a high-performance pipelined ADC, hardening that multi-bit stage against single-event errors can be accomplished with acceptable design penalties with respect to multiple 1.5-bit stages, resulting in either equivalent or significantly reduced single-event error magnitudes, depending on whether the MDAC or quantizer is affected.

#### Conclusions

The single-event sensitivity of pipelined ADCs with multi-bit stages has been analyzed and compared to 1.5-bit stage alternatives. Multi bit stages are commonly used in high-resolution pipelined ADC designs to provide reduced thermal noise, area, and power. Multi-bit stages can also provide advantages with respect to single-event vulnerability when compared to 1.5-bit stages. By utilizing a more robust encoding scheme with little area penalty, errors resulting from comparator upsets in a multi-bit stage can be limited to one LSB with a topology nearly as effective as 1.5-bit stages using comparator TMR in the first pipeline stage. Pipelined ADCs with multi-bit stages will also have fewer MDACs, leading to less sensitive area, although it may be necessary to increase capacitor values in order to decrease SE errors resulting from strikes in the MDACs. These results indicate that with proper design, pipelined ADCs using multi-bit stages can be as effective as, and much more robust than, their 1.5-bit stage counterparts when mitigating single-event errors in radiation environments.

#### CHAPTER VII

#### SINGLE-EVENT EFFECT MITIGATION IN SWITCHED-CAPACITOR CIRCUITS

This chapter presents novel SE-hardening techniques for switched-capacitor fully-differential analog/mixed-signal circuits. First, a complete excerpt from a previously published manuscript demonstrates dual-path hardening on a comparator [80]. Next, a manuscript prepared for publication presents experimental data validating the dual-path hardening technique in both MDAC and comparator circuits. Finally, the chapter concludes with a discussion on analog layout techniques for SE-mitigation in fully-differential analog/mixed-signal circuits.

# Introduction to Dual-Path Hardening on a Comparator

Single-event effects in comparators have been the subject of considerable research over the past two decades. Much of this research has focused on the analysis and characterization of the single-event response of linear bipolar comparators. Early work investigated the effect of heavy ions on the National Semiconductor LM111H [85]. Later research was expanded to include various testing methodologies, testing facilities, radiation-hardened processes, and simulation models [86]-[97]. In 2001, a radiation-hardened-by-design linear bipolar comparator was presented that utilized triple-mode redundancy (TMR), unique bias circuits for each comparator, and charge dissipation techniques in the voter circuit [98]. This TMR approach was similar to that used to harden digital circuits, with similar penalties in size, area, and power.

In comparison to their linear bipolar counterparts, relatively little research has focused on single-event mitigation in CMOS comparators. In modern CMOS processes, high-performance mixed-signal designs commonly use differential topologies and switched-capacitor input/feedback networks to obtain greater dynamic range, better noise rejection, improved matching, and/or reduced power dissipation relative to their single-ended, continuous-time counterparts [99]. For example, high-speed CMOS data converters typically make extensive use of differential switched-capacitor topologies.

Fig. 50(a) shows a typical switched-capacitor CMOS comparator as commonly used in pipelined analog-to-digital converters. This comparator is composed of a capacitive input sampling/subtraction network, a pre-amplifier, and an output latch. These circuits compare an input voltage to a reference voltage and latch a logic '1' or '0' at the output depending on whether the input voltage is higher or lower than the reference voltage. It is essential that valid comparator operation be ensured even in the presence of single-events. A comprehensive SEE error analysis of the pre-amp and latch circuits has been performed for an SOI CMOS comparator [100], but errors in the capacitive input network were not investigated. Other work showed that an auto-zeroing comparator design can limit upset duration to a single clock cycle between reset phases [68], but such designs again do not address the problem of errors in the capacitive input circuit.

In general, switched-capacitor circuit topologies exhibit much greater single-event vulnerability than their continuous-time counterparts due to the presence of floating nodes in the signal path [81], [101]. Floating nodes have no charge dissipation path, so charge deposited on a floating capacitor by a single-event strike will persist until the next

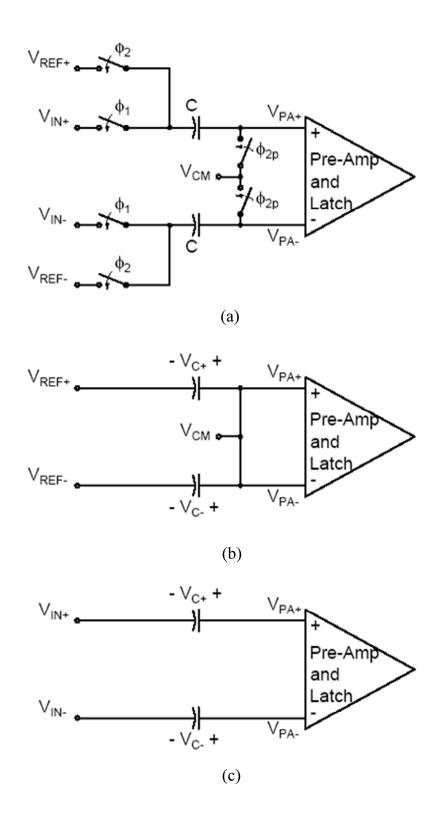


Fig. 50. (a) The switched-capacitor comparator operates in two phases: (b) reset phase and (c) evaluation phase.

clock phase. As shown in Fig. 50(c), the input network of a switched-capacitor comparator is particularly vulnerable when its configuration results in floating input nodes. In at least one design the input capacitor sizes were made much larger to harden these nodes [63], but this "brute force" approach had significant penalties in terms of layout area and maximum operating frequency.

Given sufficient time and restoring currents, a node in a continuous-time circuit can dissipate collected charge at the cost of higher power dissipation. However, switched-capacitor circuits have many advantages over continuous-time circuits in precision high-speed CMOS designs, e.g. improved component matching. Consequently, it is not practical to harden modern mixed-signal circuit designs against single-event effects simply by migrating to continuous-time topologies, or by making capacitors larger.

This research presents a novel solution for hardening the floating capacitive nodes of the comparator input network, based on a modification of the "dual path" design technique recently described for sample-and-hold feedback circuits [81]. This technique can dramatically reduce the vulnerability of floating nodes in the switched-capacitor input network with (at worst) a 2X capacitor area penalty. When combined with digital error correction techniques, dual-path SEE mitigation can completely eliminate bit errors in analog-to-digital converters due to strikes on the floating input circuits of comparators.

#### **Circuit Operation**

The switched-capacitor comparator shown in Fig. 50(a) operates in two phases controlled by non-overlapping clocks  $\phi_1$  and  $\phi_2$ . The switching network subtracts the

differential reference voltage from the differential input voltage. During the reset phase, when  $\phi_2$  is high and  $\phi_1$  is low, the capacitors are precharged to the difference between the differential reference voltage and common-mode voltage, as shown in Fig. 50(b) and (22).

$$V_{C+} = V_{CM} - V_{REF+}$$

$$V_{C-} = V_{CM} - V_{REF-}$$
(22)

When  $\phi_1$  is high and  $\phi_2$  is low, the circuit switches to the evaluation phase, and the capacitors are connected between the input voltage and the pre-amplifier inputs. It is during this phase that nodes connected to the input of the pre-amplifier are floating as shown in Fig. 50(c). The differential voltage that appears at the input to the pre-amplifier is the difference between the input signal and the reference voltages as shown by (23).

$$V_{PA+} = V_{IN+} + V_{C+} = V_{IN+} + V_{CM} - V_{REF+}$$

$$V_{PA-} = V_{IN-} + V_{C-} = V_{IN-} + V_{CM} - V_{REF-}$$

$$\therefore V_{PA+} - V_{PA-} = (V_{IN+} - V_{IN-}) - (V_{REF+} - V_{REF-})$$
(23)

This differential input voltage is amplified and then latched as logic "1" or "0" depending on whether the differential signal voltage or differential reference voltage is greater in value.

#### **Mitigation Technique**

Clearly, a voltage perturbation in the differential data path of the comparator may cause erroneous data to be latched at the comparator output. A dual signal path that provides significant immunity to a voltage perturbation on a single floating node of a

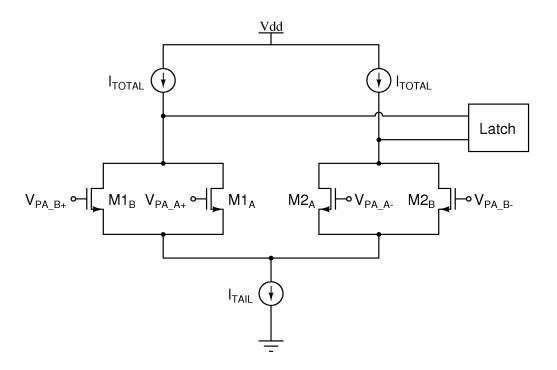


Fig. 51. Simplified circuit schematic of the differential amplifier showing the split input paths.

switched-capacitor feedback amplifier has recently been described [81]. A modified version of this technique can be applied to the input network of the comparator to prevent most errors from generating an erroneous latched value. However, this dual input path must not significantly degrade the performance of the comparator under normal operation.

Fig. 51 shows the comparator circuit with dual inputs implemented in the differential input stage. Input transistors M1 and M2 have each been split into two identical transistors connected in parallel,  $M1_A||M1_B$  and  $M2_A||M2_B$ , such that the width-to-length ratio of each parallel device is half the width-to-length ratio of the original transistor. When the gates of  $M1_A$  and  $M1_B$  are shorted together, this configuration is identical to a standard differential amplifier. However, the mitigation technique requires

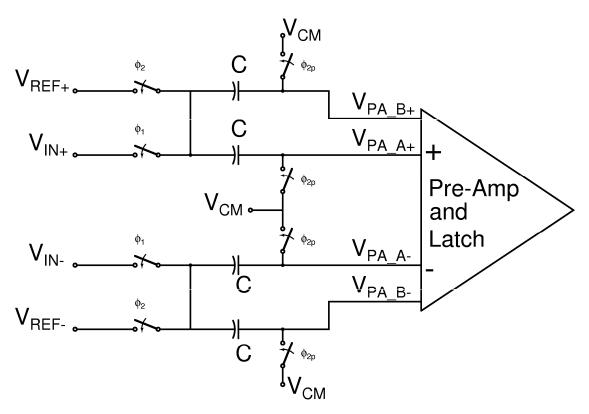


Fig. 52. The switched-capacitor comparator with split differential amplifier input paths to harden the floating nodes against single-event upsets.

the gates to maintain isolated signal paths. Therefore, the switched-capacitor differential input network must also be duplicated as shown in Fig. 52.

The differential amplifier input transistors are halved in size to provide the same effective input transconductance values of the original circuit. However, unlike the application of this technique to a feedback amplifier [81], the capacitors are not halved in size. The capacitors in this comparator design are already sized to a minimum practical value to prevent mismatches due to parasitic interconnect capacitances from affecting the circuit's operation. Since each capacitor is already at minimum size, the dual path topology doubles the total capacitance area.

A single-event strike on the floating node  $V_{PA\_A+}$  will perturb the gate voltage of  $M1_A$  in Fig. 51. If the gate voltage decreases, the drain current  $I_{M1A}$  through transistor

M1<sub>A</sub> will also decrease. Given a large enough perturbation, transistor M1<sub>A</sub> will turn off completely. In a standard differential amplifier, the decrease in current would cause an increase in the current through the M2 branch and a corresponding error voltage at the output of the amplifier. However, because of the dual input transistors, transistor M1<sub>B</sub> provides an alternate signal path. The parallel unstruck floating node for input transistor M1<sub>B</sub> preserves the correct voltage to be compared, and the comparator therefore functions properly.

The parallel input transistor does not provide perfect compensation, as some amount of charge is coupled between the two halves of each input transistor pair by the parasitic capacitances of the devices, thereby introducing a small voltage error onto the other floating input nodes. The amount of current increase for each transistor will depend on the total number on input transistors and the value of the gate-source voltage (i.e. an input transistor with a higher gate-source voltage will receive a larger increase in current). An example of the change in currents is shown in Fig. 53. The comparator in this simulation has a differential voltage of 75 mV at the pre-amp input. A single-event strike deposits 23 fC onto node V<sub>PA\_A+</sub> during the evaluate phase at 163 ns. Before the strike the total current through the M1 branch is 134 µA (67 µA through M1<sub>A</sub> and M1<sub>B</sub>) and through the M2 branch is 46 µA (23 µA through M2<sub>A</sub> and M2<sub>B</sub>). The corresponding current through M1<sub>A</sub> is then forced to zero. By 750 ps after the strike, the total current through the M1 branch is 87  $\mu$ A, and the total current through the M2 branch is 84  $\mu$ A. It is important to note that the current lost through M<sub>1A</sub> does not exactly equal the total increase in current of the remaining input transistors because the differential amplifier current source is not ideal.

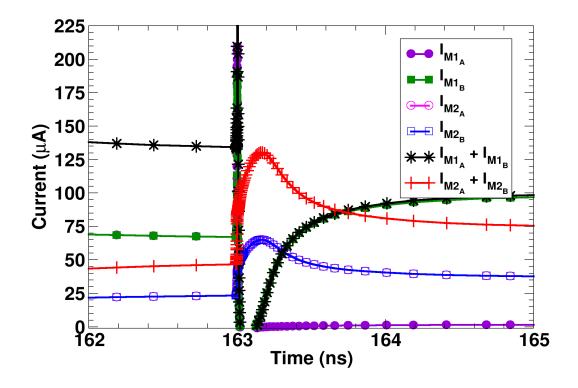


Fig. 53. Currents through the differential input transistors during a single-event strike during the evaluation phase. The differential input voltage to the comparator pre-amp was 75 mV and the single-event deposited 23 fC on the floating node  $V_{PA\_A+}$ . Even though  $M1_A$  is forced off, the dual path RHBD technique preserves the correct response, since the increase in current through  $M1_B$  remains greater than the sum of currents through  $M2_A$  and  $M2_B$ . The comparator will latch the correct logic state.

Unfortunately, this design technique cannot prevent upsets if the differential input voltage is too small. Fig. 54 shows the dual-path RHBD technique failing for a smaller input voltage. The SEE and comparator operating conditions were kept the same as in Fig. 53 except the differential input voltage was decreased to 45 mV. In this case the total current through the M1 branch after the strike remained less than the total current through the M2 branch causing an erroneous latch.

Finally, for this mitigation technique to function effectively, a single-event strike must turn off an input transistor rather than force it into ohmic operation. Therefore, if the amplifier has n-type input transistors, the capacitor switches must also be n-type

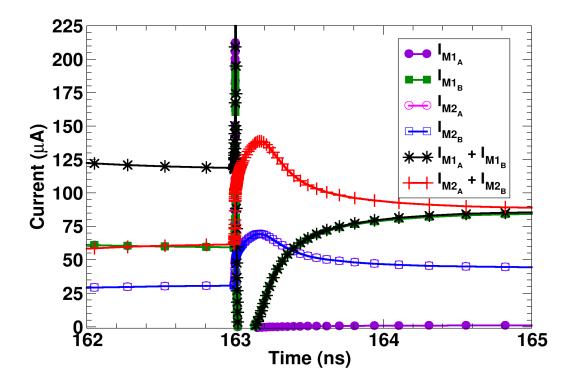


Fig. 54. Currents through the differential input transistors during a single-event strike during the evaluation phase. The differential input voltage to the comparator pre-amp was 45 mV and the single-event deposited 23 fC on the floating node  $V_{PA\_A+}$ . In this case the total current through the  $M1_A$  and  $M1_B$  remained less than the total current through  $M2_A$  and  $M2_B$  post strike, resulting in the latching of an incorrect logic state. Clearly, the dual path RHBD technique cannot prevent errors if the pre-amp input voltage is too small.

transistors, to ensure that a single-event transient will decrease the corresponding gate voltage and force the input transistor off.

#### <u>Analysis</u>

Comprehensive SPICE simulations were used to analyze the circuit mitigation technique across 100 evenly spaced times during one clock cycle, 101 evenly spaced input voltages, and 17 different charge depositions. The switched-capacitor comparator was operated at 100 Megasamples/second (MS/s) during the simulations. This sample

rate was chosen as a typical value useful for many high-speed applications, with no attempt made to optimize comparator speed. The current source used to model the SET was generated from a physical 3D TCAD model of a 90 nm CMOS technology, calibrated to the electrical SPICE model with a linear energy transfer (LET) of 1 MeV-cm<sup>2</sup>/mg [50]. This current pulse deposits 5.8 fC of charge. The other sixteen current sources were generated by adjusting the magnitude of the 5.8 fC source by integer multiples. Transistor size, node impendence, and current drive can all affect the shape of the SE-current [50], [102]. However, for this design the most sensitive nodes of the switched-capacitor network are the floating input nodes. Since no dissipation path exists for the deposited charge, the cumulative charge determines the error voltage, rather than the current profile of the strike. Additional simulations confirmed that the current pulse shape had no significant effect on the results. The same cumulative charge was modeled using the current pulse described above, two square wave pulses of different peak magnitudes, and two triangle wave pulses of different peak magnitudes. The transition region between no-upset and upset differed no more than 5 mV between the five different SE current pulse models. Also, since the sensitive nodes are floating nodes, the time location in which a single-event effect occurs is dependent only on the clock phase in which the floating nodes occur, i.e. the evaluation phase. The simulations showed that the nodes were sensitive during the entire evaluation phase, and insensitive for the entire reset phase.

As previously discussed, one technique for hardening switched-capacitor circuits is to increase the capacitor sizes, thereby reducing the error voltage for a given amount of deposited charge. Since this mitigation scheme doubles the input network area by

doubling the number of capacitors, an obvious question to be answered is if the increased hardness of the comparator is simply due to the larger capacitor area, or if the dual input path topology truly provides additional benefit. Consequently, as a "sanity check" the dual-input comparator design was also compared to a standard switched-capacitor design with each capacitor doubled in size.

### Discussion

### Results of the Dual Path RHBD Topology

Splitting the differential inputs to the comparator provides a dramatic improvement in single-event hardness as seen by the contour plots of Fig. 55. The differential input voltage is shown on the x-axis while the deposited charge is shown on the y-axis. The dark region indicates an upset condition versus the light region indicating no upset. For the standard circuit topologies of Figs. 55(a) and 55(b), the susceptible input voltage region increases with deposited charge according to the fundamental capacitor equation V = Q/C. This increase is not strictly linear, as higher deposited charges eventually create a dissipation path by forcing the floating node to become so negative that the switching transistor connected to the node turns on.

The single-event-hardened dual-path topology does not follow this semi-linear relationship. In fact, the upset-susceptible input voltage region in Fig. 55(c) quickly saturates. This saturation occurs because the struck node (e.g. node  $V_{PA\_A+}$ ) quickly turns off the amplifier's input transistor (M1<sub>A</sub>), and additional deposited charge cannot turn it "more" off. The results in Fig. 55(c) show upsets can still occur when the magnitude of

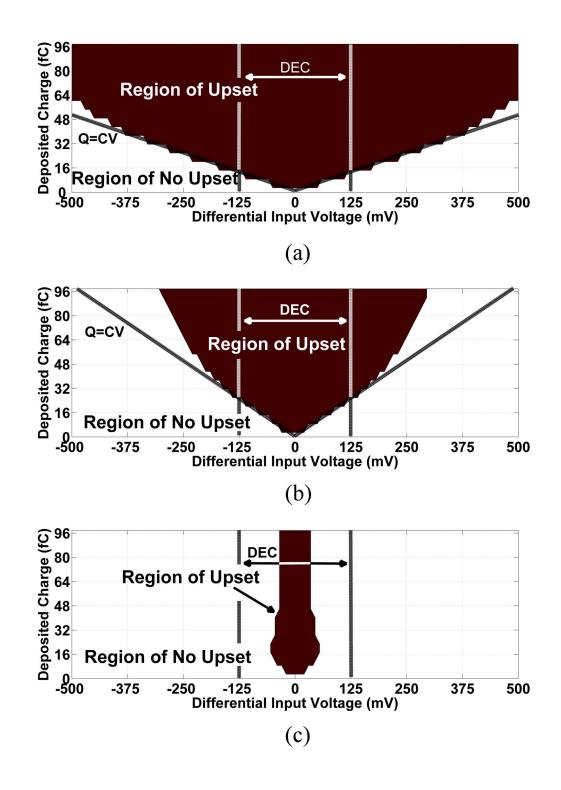


Fig. 55. Contour plots of differential pre-amp input voltage vs. deposited charge for (a) standard SC comparator design, (b) standard design with doubled capacitor size, and (c) splitting the comparator input nodes.

the input voltage of the pre-amplifier is less than 50 mV. In addition, the sensitive area of the comparator's input network is effectively doubled since the number of switching transistors is doubled. Nevertheless, the dual-input path design provides a dramatic reduction in single-event errors despite these drawbacks.

#### Error Correction in Pipelined ADCs

High-performance pipelined analog-to-digital converters (ADCs) typically use switched-capacitor comparators in every stage. A pipelined stage resolving 1.5 bits includes a 1 bit overlap for error correction. Standard digital error correction (DEC) circuitry will correct errors within +/- 0.5 LSB (relative to V<sub>REF</sub>) in each pipelined stage. For a differential voltage swing of 1 V, +/- 0.5 LSB will equal +/- 125 mV. This region in which the DEC will correct errors is also shown in Fig. 6. For the dual-path design of Fig. 55(c), the upsets that occur in the capacitive input network are completely bounded within the DEC region. Consequently, even though the number of sensitive nodes is doubled, the bit errors that do occur can be completely corrected, resulting in no error at the output of the ADC.

# Open Loop Versus Closed Loop Response

There is an important distinction to be noted when the dual-path RHBD technique is used in an open loop versus closed loop circuit. In the sample-and-hold circuit the switched capacitor network provided a closed loop feedback path around the amplifier [81]. The negative feedback and virtual short circuit across the amplifier inputs forced the sister transistor to compensate for all the lost current, resulting in no change in current for the other input branch of the differential amplifier.

Circuits with open loop amplifier topologies, such as the comparator, behave somewhat differently. If an input transistor is forced off by a single-event strike, capacitive coupling will force a voltage change on all of the floating input nodes of the comparator. Instead of the lost current being compensated for by only the sister transistor, the current is distributed across all the input transistors. If the differential input voltage is small enough, the dual input path topology may still fail, as the case in Fig. 54. As shown in Fig. 55(c), errors can still occur if the differential input voltage to the preamplifier is 50 mV or less.

The effectiveness of the technique for open loop circuits can be further improved by increasing the number of input paths. There are two reasons why adding more input transistors will improve the single-event hardness of the switched-capacitor floating nodes. First, the percentage of current lost from the total branch current will be reduced. The maximum current loss in the dual-path design is one half of the total branch current, since at most one of the two dual input paths can be turned off. By switching to a quad-path design the maximum current loss would decrease to one quarter of the total branch current. The second reason is due to the way the lost current is redistributed. The redistribution of lost current will depend on the total number on input transistors and the gate-source voltages. In the worst case of the dual-path design, only three of the four input transistors will be operational during a single-event strike. This means the branch being affected by the single event will contain only one of the total three transistors receiving the lost current redistribution. For the quad-path design this improves to three of the total seven operational transistors. Since the lost current is distributed across all

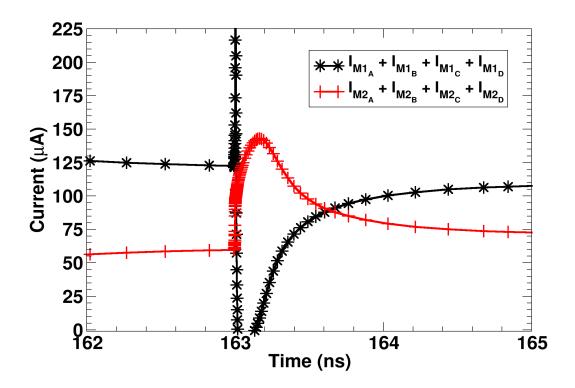


Fig. 56. Total currents through the differential input branches of using quad-path RHBD during a single-event strike. The single-event and operating conditions were the same as Fig. 54. The differential input to the comparator pre-amp was 45 mV and the single-event deposited 23 fC on the floating node  $V_{PA\_A+}$ . Unlike in Fig. 54 in which the dual-path RHBD did not work, the current through the M1 branch of the quad-path does return to being greater than the current through the M2 branch. The comparator will latch the correct logic state.

the input transistors, adding more inputs transistors will decrease the region in which an error will still occur.

The total current through each branch during a single-event for the quad-path design is shown in Fig. 56. The comparator operating/single-event conditions are the same as Fig. 54. The comparator in this simulation has a differential pre-amp input voltage of 45 mV. A single-event deposits 23 fC onto node  $V_{PA\_A+}$  during the evaluate phase at 163 ns. However, unlike in Fig. 54 in which the dual-path design fails to recover the correct response, the quad-path does successfully recover. The current through the M1 branch returns to a higher value than the current through the M2 branch after 670 ps.

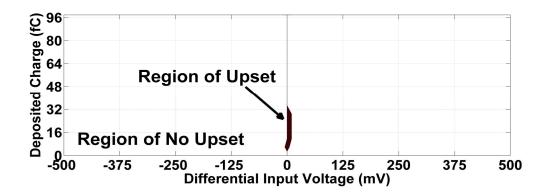


Fig. 57. The result of the proposed RHBD technique applied to four parallel paths per input.

Results of the simulations of a design using the RHBD technique for four paths per input instead of two is shown in Fig. 57. For this case, errors do not occur until the minimum differential input voltage drops to 10 mV. From a practical design standpoint, the layout penalty of increasing the number of input paths beyond this point may not justify further improvement in single-event hardness.

#### **Tradeoffs**

The layout of the baseline and RHBD comparators were performed in anticipation of fabrication in the IBM CMOS 9SF process, as shown in Fig. 58. The areas of the footprints are  $871~\mu\text{m}^2$  and  $1688~\mu\text{m}^2$  for the baseline and RHBD comparator respectively. The main design penalty for the dual-path RHBD comparator is the doubling of capacitor area. The area tradeoff, however, is specific to the pipelined ADC application, and assumes that the capacitors of the baseline design are already at minimum size. Depending on the application, it may be possible to halve the sizes of the capacitors when splitting the input paths, while still maintaining acceptable matching and noise performance. In such a case, the dual-path RHBD technique would have minimal area penalties when compared to the baseline design.

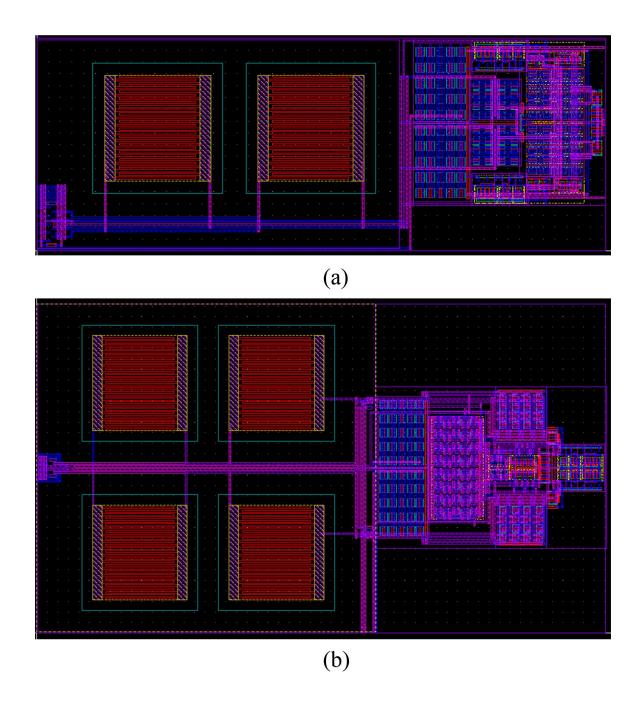


Fig. 58. The completed layout designs for (a) baseline and (b) RHBD comparator. The process used is the IBM CMOS 9SF.

Speed penalties are dependent on the application. If the capacitors can be halved in size, then the total capacitance for the circuit will not change, and the dual-path design will have no significant speed penalties. However, the capacitors were kept the same size in the ADC comparator application, and by implementing the dual-path design the total capacitance of the system doubled. As long as the switches driving the capacitors are replicated in each path, or their width-to-length ratios are doubled, the RC time constants will not increase. Speed penalties will also depend on the circuits driving the  $V_{IN}$ ,  $V_{REF}$ , and  $V_{CM}$  inputs. If these circuits are slew-rate limited then maximum sampling speed will at worst be halved. However, if these circuits are not slew-rate limited then there is no speed penalty.

The dual-path topology has negligible power penalties. There is effectively no increase in power in the pre-amp and latch subcomponents. Even though the dual-path RHBD technique doubles the number of input transistors, the width-to-length ratios are halved, with no resulting changes in current. Although the number of capacitors is doubled and the number of switches is increased, any increase in power in the switched-capacitor subtraction network is negligible when compared to the power dissipation of the pre-amp and latch. Simulation of a sinusoid input to both baseline and RHBD comparators shows an average power of  $101~\mu W$  for both designs.

Transistor and capacitor mismatch are also of concern in analog differential topologies. Switched-capacitor topologies provide greater precision than continuous-time circuits, since it is easier to match capacitors than resistors. However, if an input transistor is forced off in a dual-path circuit, the result is an effective 1:2 mismatch between the differential inputs, resulting in an input offset voltage. (For a quad-path

design the mismatch ratio will be 3:4). While many switched-capacitor circuit designs can correct for offset errors caused by mismatches [51], [68], [99], [103]-[105], the digital error correction in a pipelined ADC significantly reduces the matching requirements of the comparators by correcting any offset voltage errors up to one-half of an LSB. Conceptually it can be seen in Fig. 6 and Fig. 8 that any input offset voltage induced by an input transistor being shut off must fall within the  $\pm$  50 mV and  $\pm$  10 mV upset ranges in the simulations, and therefore be well within the  $\pm$  0.5 LSB correction range of the DEC circuitry of the pipelined ADC.

### Conclusions to Dual-Path Hardening on a Comparator

The dual-path RHBD technique provides a simple but effective means of hardening the floating input nodes for a switched-capacitor comparator. By splitting the input nodes into separate parallel signal paths, a dramatic improvement in single-event hardness is observed. For a pipelined ADC, the input voltage region over which the comparator does upset can be completely bounded by digital error correction, effectively eliminating all bit errors due to the single-event strikes on the input networks of the comparators. These results indicate that the dual-path RHBD technique should be extremely effective at reducing single-event errors for a broad range of switched-capacitor circuits, with or without feedback.

The tradeoff for using the dual-path technique is increased layout complexity, an increase in the number of switching transistor, and a doubling of overall capacitor area, assuming that the input capacitors were originally at minimum size. However,

simulations show that the effectiveness of this hardening scheme easily justifies this design penalty for high-performance mixed-signal applications.

## Introduction to Dual-Path Hardening Experimental Validation

In modern CMOS processes, high-performance mixed-signal designs commonly use differential topologies and switched-capacitor input/feedback networks to obtain greater dynamic range, better noise rejection, improved matching, and/or reduced power dissipation relative to their single-ended, continuous-time counterparts [99]. In general, switched-capacitor circuit topologies exhibit much greater single-event vulnerability than the continuous-time analogs due to the presence of floating nodes in the signal path [81]. Floating nodes have no charge dissipation path, so charge deposited on a floating capacitor by a single-event strike will persist until the next clock phase.

Previous work in hardening switched-capacitor circuits involves increasing the size of the inputs capacitors [63]. This "brute force" approach has significant penalties in terms of layout area and maximum operating frequency. Similarly, given sufficient time and restoring currents, a node in a continuous-time circuit can dissipate collected charge at the cost of higher power dissipation. The circuit-performance advantages of switched-capacitor topologies outweigh the complications of hardening these circuits for single-event effects. The drawbacks of these techniques make it impractical to harden modern mixed-signal circuit designs against single-event effects simply by migrating to continuous-time topologies, or by making capacitors larger.

This research presents experimental results for hardening the floating capacitive nodes of switched-capacitor circuits, based on using the dual-path hardening technique

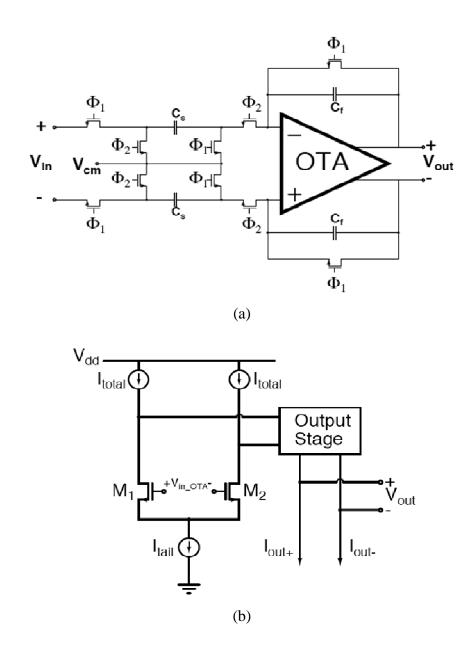


Fig. 59. The (a) switching network and (b) differential input for a basic sample-and-hold amplifier.

recently described for sample-and-hold feedback circuits and comparators [80], [81]. This technique can dramatically reduce the vulnerability of floating nodes in the switched-capacitor input network with, depending on application, at best negligible impact to area, power, and speed and, at worst, a 2X area penalty.

## **Hardening Switched-Capacitor Circuits**

The differential sample-and-hold amplifier (SHA) shown in Fig. 59 uses a switched-capacitor sampling network with a fully differential operational transconductance amplifier (OTA) and operates on two non-overlapping clocks,  $\Phi_1$  and  $\Phi_2$ . During the evaluate phase,  $\Phi_1$  is off and  $\Phi_2$  is on, and the input nodes to the OTA floats, with no current dissipation path to remove any charges. If during evaluate phase, additional charge is collected by these floating nodes, the sampling and feedback capacitors,  $C_s$  and  $C_f$ , act as ideal current integrators for this charge resulting in erroneous data at the circuit output [80], [81].

To mitigate the effect of soft-error-related charge collection at the floating nodes in switched-capacitor circuits, the dual-path hardening technique has been developed. For this novel approach, the OTA differential input paths are doubled, as shown in Fig. 60a. Similarly, the number of OTA input transistors is doubled (Fig. 60b), creating a local feedback path. This increases the number of floating nodes in the circuit. However, if charge is collected on one of the floating nodes, the corresponding OTA input transistor will be forced into cutoff with the "sister" data path maintaining the correct sampled value. Given a shared tail current, the OTA input transistor on the "sister" data path will compensate for current loss and maintain proper linear region operation, ideally

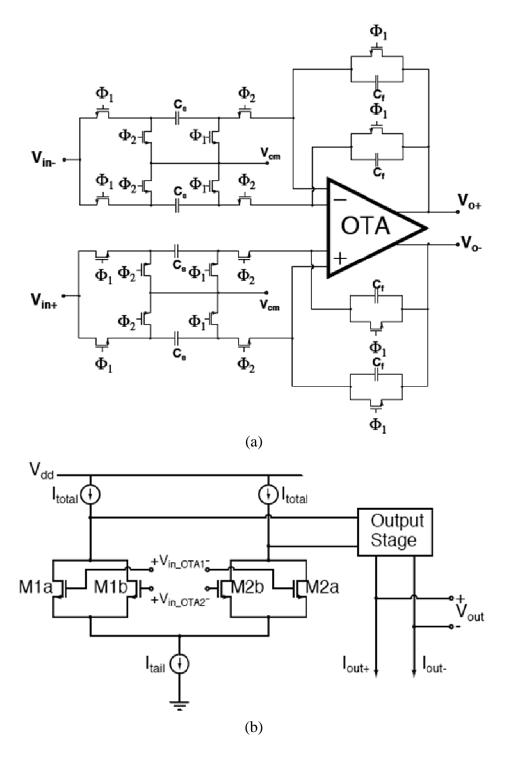


Fig. 60. The dual-path hardening technique doubles the OTA input path in the (a) switching network and (b) OTA.

correcting any error. This technique works best when the amplifier input transistor is forced into cutoff. To ensure this, the switches must be of same type (NFET or PFET) as the OTA input transistors. This design constraint can lead to some difficulty in designing a circuit with strict noise margins, but can be overcome if bootstrapped switches are used.

Area, power, and speed design penalties associated with the dual-path hardening technique are minimal. If capacitor values are set by gain-bandwidth and thermal noise requirements, then the sizes of capacitors, switches, and amplifier input transistors can be divided between the branches, with negligible impact on final area, power and speed [81], as is the case in the present SHA example. In the worst-case scenario, if the capacitor values are small enough to be dominated by parasitic effects, and cannot be halved [80], the circuit area doubles, assuming the design is dominated by capacitor area. In this case, the switching-network power requirements will also be doubled, but is negligible compared to the amplifier power requirements. Speed penalties will depend on the driving circuit; if the driver is slew-rate limited then speed may also be halved.

# Test Chip

### Multiplying Digital-to-Analog Converter

The dual path technique was implemented on a multiplying digital-to-analog converter circuit (MDAC) and a comparator circuit. Baseline (conventional design without the dual paths mentioned above) and hardened (with dual paths) versions were fabricated in AMI  $0.5~\mu m$  bulk CMOS process. Even though results presented in this paper are for  $0.5~\mu m$  process, this technique is equally effective for any advanced technology node.

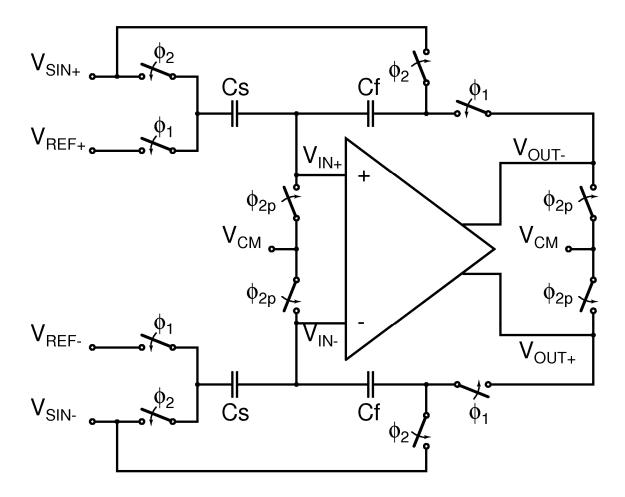


Fig. 61. Schematic of the baseline, 2X gain, multiplying digital-to-analog converter switched-capacitor network.

The baseline, 2X gain, MDAC switched-capacitor network, shown in Fig. 61, is similar to the SHA. During sample phase,  $\Phi_1$  is off and  $\Phi_2$  is on, the input signal is sampled across both equal-sized sampling and feedback capacitors,  $C_s$  and  $C_f$ :

$$Q_{samp+} = (V_{SIN+} - V_{cm}) * 2C$$

$$Q_{samp-} = (V_{SIN-} - V_{cm}) * 2C$$
(23).

During evaluate phase,  $\Phi_1$  is on and  $\Phi_2$  is off, the sampling capacitors' bottom plate is connected to VREF and the feedback capacitors are connected into negative feedback.

The output signal holds the difference between twice the input signal and the reference signal:

$$Q_{eval\_s+} = (V_{REF+} - V_{CM}) * C$$

$$Q_{eval\_s-} = (V_{REF-} - V_{CM}) * C$$

$$V_{OUT+} = \frac{Q_{samp-} - Q_{eval\_s-}}{C} + V_{CM}$$

$$V_{OUT-} = \frac{Q_{samp+} - Q_{eval\_s+}}{C} + V_{CM}$$

$$\therefore (V_{OUT+} - V_{OUT-}) = -1 * [2 * (V_{SIN+} - V_{SIN-}) - (V_{REF+} - V_{REF-})]$$
(24).

Fig. 62 is the micrograph of the baseline and hardened versions of the MDAC.

## Comparator

The switched-capacitor comparator is shown Fig. 63 subtracts the differential reference voltage from the differential input voltage and latches high if the difference if positive. During the reset phase, when  $\Phi_1$  is high and  $\Phi_2$  is low, the capacitors are precharged to the difference between the differential reference voltage and common-mode voltage:

$$V_{C+} = V_{CM} - V_{REF+}$$
  $V_{C-} = V_{CM} - V_{REF-}$  (25).

When  $\Phi_1$  is high and  $\Phi_2$  is low, the circuit switches to the evaluation phase, and the capacitors are connected between the input voltage and the pre-amplifier inputs. It is during this phase that nodes connected to the input of the pre-amplifier are floating. The

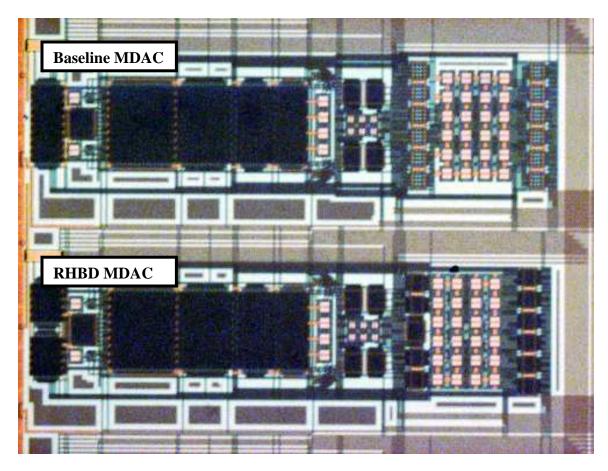


Fig. 62. Micrograph of the baseline and hardened MDACs.

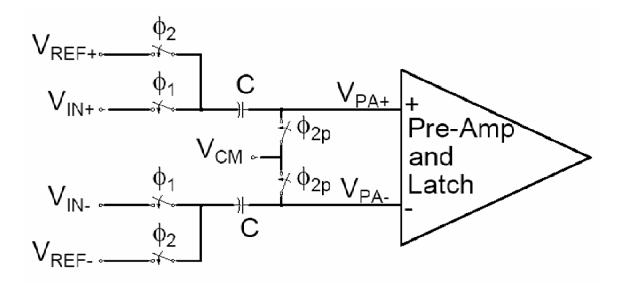


Fig. 63: Schematic of the baseline comparator switched-capacitor network.

differential voltage that appears at the input to the pre-amplifier is the difference between the input signal and the reference voltages:

$$\begin{split} V_{PA+} &= V_{IN+} + V_{C+} = V_{IN+} + V_{CM} - V_{REF+} \\ V_{PA-} &= V_{IN-} + V_{C-} = V_{IN-} + V_{CM} - V_{REF-} \\ &\therefore V_{PA+} - V_{PA-} = \left(V_{IN+} - V_{IN-}\right) - \left(V_{REF+} - V_{REF-}\right) \end{split} \tag{26}.$$

This differential input voltage is amplified and then latched as logic "1" or "0" depending on whether the differential signal voltage or differential reference voltage is greater in value. The micrograph of the baseline and hardened comparators are shown in Fig. 64.

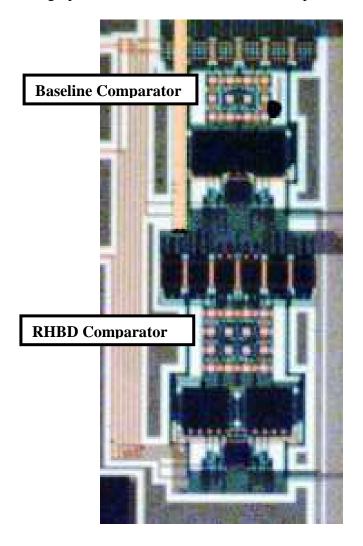


Fig. 64. Micrograph of the baseline and hardened comparators.

# **Experimental Results**

The effectiveness of the hardening technique for fabricated designs is evaluated using a through-wafer two-photon absorption (TPA) laser-induced charge-injection technique performed at room temperature. TPA generates electron-hole pairs in silicon, mimicking a soft error incident by focusing optical pulses through the substrate into the active areas of the circuit, as described in [106]–[111]. The laser is focused such that the resulting Gaussian carrier-density distribution has an approximate diameter of 1.1 μm.

The average and standard deviation laser-induced output perturbation due to strikes on the floating nodes in the baseline and hardened versions of the MDAC are shown in Fig. 65, plotted as the square of the laser pulse energy (PE). In the baseline version the error magnitude increases with increasing laser PE (which will result in

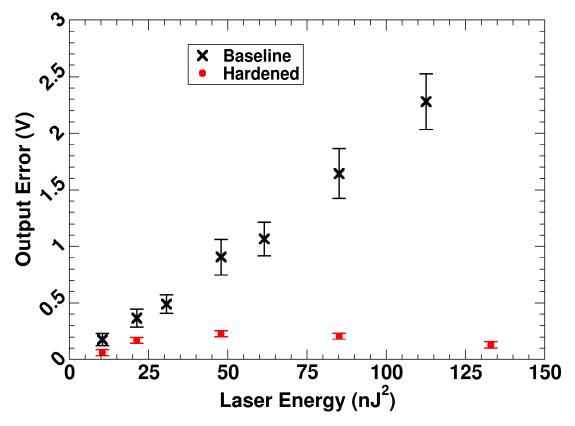


Fig. 65. Test results for baseline and hardened MDAC.

increased charge collection at the floating node), following the fundamental Q=CV relationship. The error in the hardened MDAC saturates quickly, independent of the laser energy. This is due to the turning-off of the affected input transistor and the "sister" path maintaining the correct output voltage.

Fig. 66 shows the laser results for strikes targeting the floating nodes in both comparator designs. Under nominal operation, the comparator output changes state when the differential input and reference voltages are equal. However, a single-event will change the input voltage at which the output state changes. With the differential reference voltage at 0 V, the consequences of the perturbation are quantified by the variation of the differential input voltage required to shift the output state. Increasing

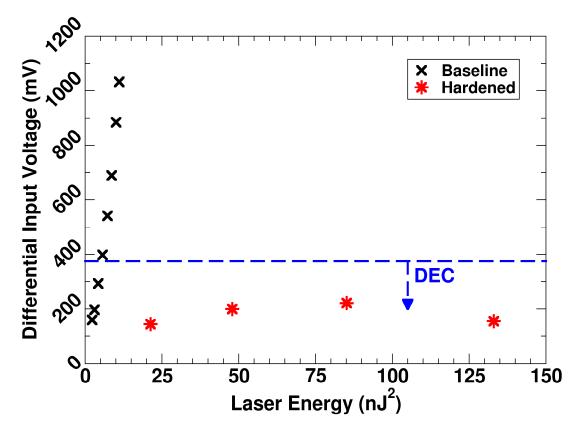


Fig. 66. Test results for baseline and hardened comparator. Comparator errors below the plotted dashed lined will be corrected in a pipelined analog-to-digital converter.

deposited charge forces the baseline comparator to change state at a larger-than-normal differential input voltage. This is analogous to the baseline MDAC response of Fig. 65: the hardened comparator error response quickly saturates with increasing charge injection.

There are comparator applications that can correct the remaining error in the data seen in Fig. 66 for the hardened design. To further clarify the effectiveness of the dual-path hardening technique, consider a pipelined A-to-D converter. Typically each pipeline stage will overlap with the next stage, providing some digital error correction (DEC) for voltage errors less than ½ LSB resulting in the comparators. Assuming a 1.5-bit stage and VREF of 3 V, the DEC will correct all errors less than 375 mV for these designs. Thus, proposed single-event mitigation technique will correct all single-events on the hardened floating nodes.

## Conclusions to Dual-Path Hardening Experimental Validation

The dual-path RHBD technique provides a simple but effective means of hardening the floating input nodes for switched-capacitor circuits. By splitting the input nodes into separate parallel signal paths, a dramatic improvement in single-event hardness is observed. In non-hardened switched-capacitor designs a single-event on the floating nodes will cause an error at the output directly proportional to the amount of charge collected. The dual-path RHBD technique limits the size of any remaining error and decouples the error response from the amount of charge collected. In some switched-capacitor circuit applications the hardening technique will make the floating nodes immune to single-events. For example in a pipelined ADC, the input voltage region over

which the comparator does upset can be completely bounded by digital error correction, effectively eliminating all bit errors due to the single-event strikes on the input networks of the comparators.

### **Introduction to Layout Considerations**

Reduced spacing requirements in sub-micron technologies have introduced charge-sharing effects detrimental to single-event hardening techniques that are traditionally effective in larger (250 nm or greater) processes [46], [112], [113]. This phenomenon can be exploited to mitigate single-event effects (SEE) in fully-differential analog circuits, which have been shown to be sensitive to single-event transients (SET) [17], [63], [81].

In previous work, TCAD simulations of a radiation-hardened by design (RHBD) layout approach were presented using common-centroid transistors in a fully-differential data path to mitigate the effects of single-events with promising results [114]. This chapter presents experimental results of a radiation-hardened by layout (RHBL) technique designed in a 65 nm technology to exploit charge-sharing phenomenon in differential circuitry to mitigate SEEs. The layout technique minimizes the distance between the drains of sister devices in the differential signal path through matched and common-centroid layouts to maximize the likelihood of an ion strike affecting both sides of the differential pair, therefore cancelling some, or all, of the resulting transient. The sensitive area is significantly reduced over the case of no charge sharing. Results from this study indicate that a practice of layout with close drain proximity for sister transistors along the fully-differential signal path will greatly reduce the sensitive area of the circuit.

## **Background**

The advantages in dynamic output range and noise rejection over single-ended circuits make differential topologies the accepted standard for high-performance analog design [113]. The sample and hold amplifier (SHA), shown in Fig. 59, has several examples of "sister" differential devices in the data path. These device pairs feature two transistors connected such that any differential voltage applied to the inputs is amplified, making single events (SE) particularly detrimental. However, assuming a large common mode rejection ratio (CMRR), any common voltage applied to both the inputs is rejected, as illustrated in Fig. 67.

When device matching is a priority in analog layout, a common-centroid approach is used in which devices are arranged around a center location so that the effects of process variation, gradient effects, and random noise are cancelled [115]. This is typical

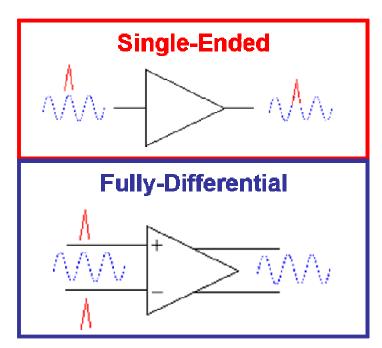


Fig. 67. Illustration of single-ended and fully differential operation. An injected transient on a single-ended amplifier will be propagated with the signal while a transient shared by the inputs of a fully-differential amplifier will be cancelled.

in differential pair inputs, but not necessarily used for other sister devices along a differential signal path such as switching transistors.

For advanced technologies, the density of transistors is sufficiently high that charge generated by a single-event will be collected by the struck transistor and adjacent components. If a common-centroid layout is used to promote charge sharing in a fully differential circuit, the effects of a single-event transient on the circuit can be minimized.

## Test Design and Circuit Operation

Proposed RHBL examples for single-multiplicity (M1) and unit-cell double-multiplicity (M2) transistor differential pairs are shown in Fig. 68. These pairs are arranged with drains located as close as design rules allow or, when applicable, in a common-centroid configuration.

The circuit used in this study to test the effectiveness of the layout technique for mitigating SEEs is shown in Fig. 69. The circuit is designed in a 65 nm process and is based on a charge-sharing measurement circuit described previously [116]. Separate test circuits are available for M1 and M2 configured as in Fig. 68. The bottom panel of Fig. 69 shows the layout for M2.

During an SEE test of this circuit, there are three phases of operation: pre-charge, hit, and evaluate. During pre-charge, the 516 fF target capacitors are charged to a test-controlled voltage and the reference voltage is set. During the laser strike, all of the switches are open and the target nodes are floating. As a result of the hit, some charge stored on the target capacitors is removed. Finally, during the evaluate phase, the sense amps are enabled to compare each transistor to the reference voltage.

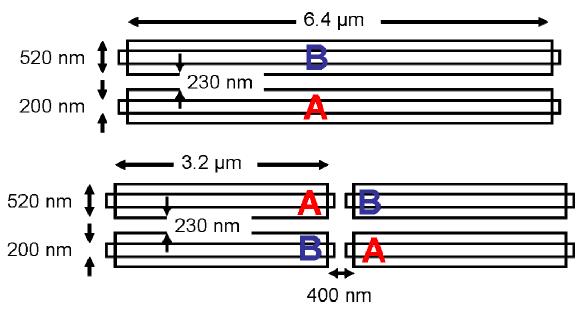


Fig. 68. Proposed charge-sharing layout designs RHBL M1 (top) and RHBL M2 (bottom).

The efficacy of this approach is evaluated using a through-wafer two-photon absorption (TPA) single event upset mapping technique [106]-[111], as previously described in Chapter VII. The pre-charge and evaluate clock cycles for the circuit are synchronized with the laser pulse. The timing of the clocks with the laser ensures each laser pulse hits the target shortly after pre-charging and just before evaluation, ensuring an event occurs at each evaluate phase and that there are no strikes during the pre-charge phase, which would potentially distort the results.

The M1 and M2 target devices were scanned by the laser with a step size of 0.3 µm. Data were taken at a low enough laser pulse energy (2.86 nJ) so no upsets are observed above a 950 mV target voltage in the most sensitive region of the circuit, ensuring that the upset voltage could be observed throughout the circuit. For each location in a scan, pre-charge voltage at the hit nodes is swept in 25 mV steps with respect to the reference voltage. The voltage at which the sense amp switches states is

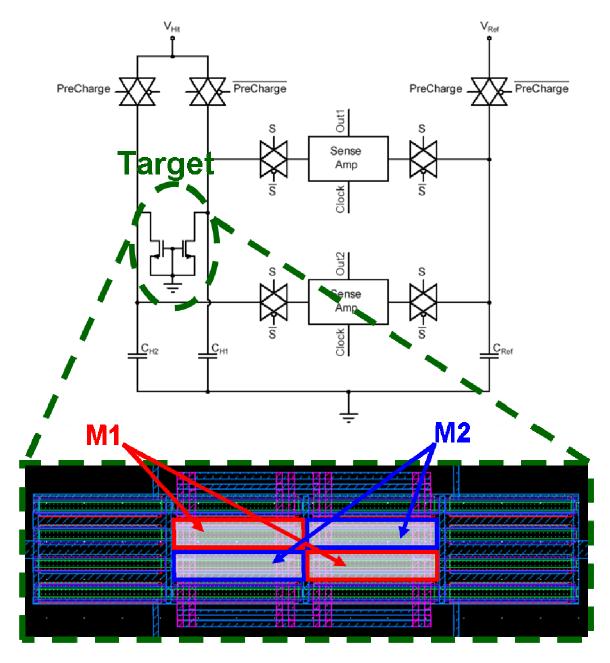


Fig. 69. Schematic of test circuit and the RHBL M2 layout.

recorded and converted to charge using the Q = CV relationship. The 25 mV step size allows a charge resolution of 12.9 fC. The resulting collected charge for each transistor, A and B, is recorded independently for each location in the scan for further data analysis.

### Results

Charge collection results with respect to position for a single transistor are superimposed onto a scale representation of the target circuit in Fig. 70. These maps represent the baseline case without charge-sharing effects. Charge is normalized with respect to the maximum collected charge in the individual maps and represented from low to high by shades from light to dark. The normalization removes die-to-die and day-to-day variations in the data caused by experimental error. The images have been processed to allow smooth contour lines as opposed to pixilated data.

Figure 71 shows maps of M1 and M2 representing the magnitude of the difference in charge collected, or unique charge in transistors A and B at each point in the scan. Qualitatively, this is the amount of charge from an SE that will affect circuit operation if the common charge is cancelled through differential operation. To quantify, Table II shows an approximate 85% reduction in the area of the device that collects at least half the maximum charge, designated as the sensitive area for this example, in each map of Figs. 70 and 71. When charge sharing is promoted, the sensitive area is dramatically reduced in both transistor configurations. There is not an appreciable improvement in sensitive area of one RHBL option over the other.

### Conclusions to Layout Considerations

Experimental results of a RHBL technique designed to exploit charge-sharing phenomenon in differential circuitry to mitigate SEEs are presented. The layout technique minimizes the distance between the drains of sister devices in the differential signal path

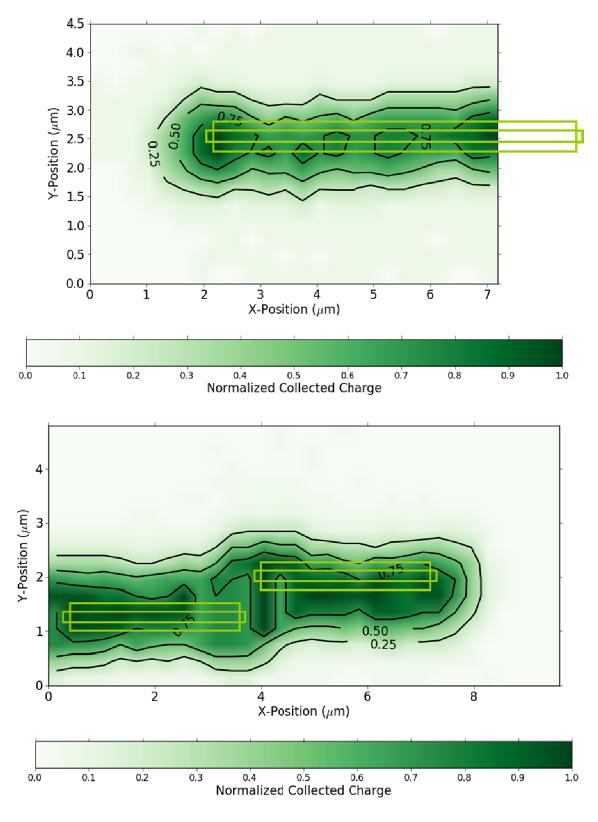


Fig. 70. Baseline case of charge collection on a single transistor without the effects of charge sharing for M1 and M2.

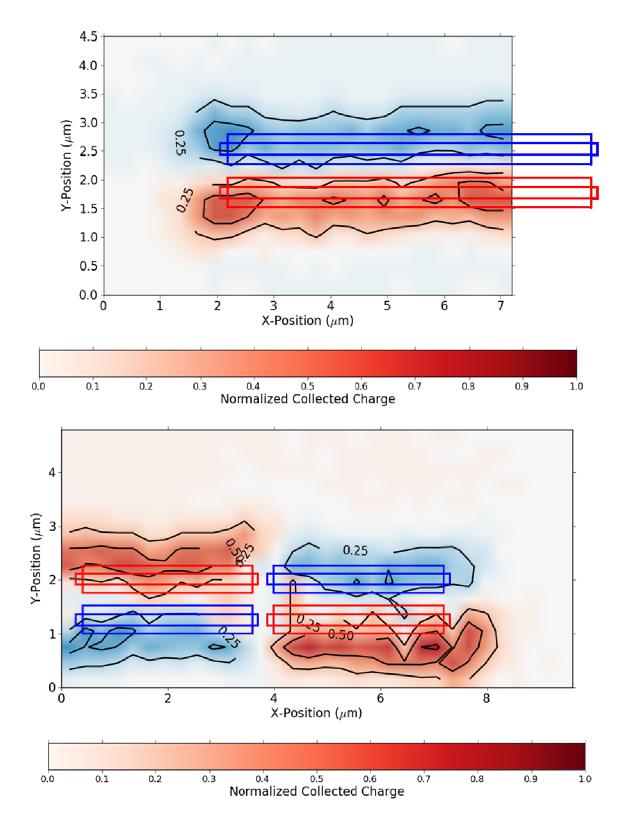


Fig. 71. The magnitude of the difference of charge collected between transistors A and B for M1 (top) and M2 (bottom).

TABLE II

SENSITIVE AREAS COLLECTING UNIQUE CHARGE GREATER THAN HALF OF THE MAXIMUM DEPOSITED CHARGE FOR BASELINE AND RHBL M1 AND M2.

	M1 (μm <sup>2</sup> )	M2 (μm²)
Baseline	6.39	12.24
RHBL	0.94	1.85

through matched and common-centroid techniques to maximize the likelihood of an ion strike affecting both sides of the differential pair, therefore cancelling some, or all, of the resulting transient. The sensitive area for both layout techniques is reduced by a factor of at least 6.5 over the baseline case of no charge sharing. There is neither penalty nor benefit for using a common-centroid layout in the case where the transistors need to be separated into unit cells as long as the drains of the devices are placed as close together as design rules allow. These tests were conducted with only n-channel devices. It is expected that p-channel devices will only enhance the charge sharing phenomena [116]. Analysis of the symmetry of the devices using a quadrant of the experimental data mirrored upon itself to reduce experimental variation will be fully described in the final paper. The results from this study indicate that a practice of layout with close drain proximity for sister transistors along the fully-differential signal path will greatly reduce the sensitive area of the circuit. The penalty is additional wiring overhead and additional capacitance in the cases where common-centroid layout would not normally be employed, but the overall charge sharing, and therefore single-event mitigation, is dramatically enhanced.

#### **CHAPTER VIII**

#### **CONCLUSIONS**

### Conclusion

This research uses circuit simulations, behavioral modeling, and experimental testing to characterize the effects of SEEs and provide novel RHBD techniques for generalized pipelined ADC circuits. First, a metric for comparing SE-vulnerability between multiple designs was developed. Signal-to-noise ratio provides an excellent metric when comparing different single-event mitigation design choices in an ADC. The most significant advantage of using SNR is not to evaluate the performance of one particular circuit, but to compare the performance of two or more different RHBD techniques on the same circuit or system, or to compare the relative hardn.ess of two or more different circuit topologies. In such situations, the simulated error rate can be set sufficiently high enough to allow the designer to make a valid comparison between designs. Because signal-to-noise ratio is so commonly used to characterize analog and mixed-signal systems, the SNR metric should prove equally useful in quantifying the benefit of future RHBD techniques applied to a very broad range of designs such as analog-to-digital converters, digital-to-analog converters, RF circuits, and analog signal processing circuits.

The single-event sensitivity of pipelined ADCs with multi-bit stages has been analyzed and compared to 1.5-bit stage alternatives. Multi-bit stages are commonly used in high-resolution pipelined ADC designs to provide reduced thermal noise, area, and

power. Multi-bit stages can also provide advantages with respect to single-event vulnerability when compared to 1.5-bit stages. By utilizing a more robust encoding scheme with little area penalty, errors resulting from comparator upsets in a multi-bit stage can be limited to one LSB with a topology nearly as effective as 1.5-bit stages using comparator TMR in the first pipeline stage. Pipelined ADCs with multi-bit stages will also have fewer MDACs, leading to less sensitive area, although it may be necessary to increase capacitor values in order to decrease SE errors resulting from strikes in the MDACs. These results indicate that with proper design, pipelined ADCs using multi-bit stages can be as effective as, and much more robust than, their 1.5-bit stage counterparts when mitigating single-event errors in radiation environments.

Previous SE-hardening recommendations have been limited to hardening the digital circuits or increasing the sizes of sampling capacitors in the analog circuits. This work has expanded and provides much more thorough designs for hardening pipelined ADCs. 1.5-bit stages can benefit by applying TMR to the comparators. SE-sensitivity to comparator upset in multi-bit stages can been masked and/or corrected by using better robust encoding logic schemes. Also, the analog circuitry has less sensitive area in pipelined ADC designs using multi-bit stages than 1.5-bit stages.

The comparators, sample-and-hold amplifier, and multiplying digital-to-analog converter sub-circuits are likely to be fully-differential and use switched-capacitor circuits in advanced high-performance designs. Until recently switched-capacitor circuits were highly vulnerable to SE because of floating nodes. Hardening options were limited to resizing the sampling capacitors. A novel RHBD technique, dual path hardening, has been developed that significantly decreases the SE-vulnerability of

switched-capacitor circuits and is applicable in both closed-loop and open-loop designs.

Results from simulations and laser testing have validated dual-path hardening.

Signal information in fully-differential analog circuits is stored as the difference of two data paths. This significantly improves the noise margins since noise shared across both data paths does not affect the signal information. While charge sharing is a major issue in highly-scaled digital circuits, it can be advantageous in analog circuits. Results from recent laser testing have validated layout techniques that share charge more efficiently thus providing improved SE-hardening in fully-differential analog circuits.

## Design Techniques for SE-Hardened Pipelined ADCs

Unless SE radiation-hardened-by-design (RHBD) techniques are used, pipelined ADCs will be sensitive to single-events. The majority of previous work has focused on hardening the digital circuitry through various techniques: temporal-hardening, resistive feedback, and TMR [61]-[66], [69]. However, the analog sub-circuits are vulnerable to single-events as well and prior to this work hardening options were limited to increasing the size of the sampling capacitors, increasing nodal capacitance, and using auto-zeroing switched-capacitor architectures to restrain the duration or error [63], [64], [68].

This work has led to many additional recommendations for hardening pipelined ADCs. Since each pipeline stage quantizes the signal with decreasing significance; the effort of SE hardening should focus with the beginning stages. Simple architecture changes can limit output errors produced by comparator upsets. Comparator TMR is very effective in 1.5-bit stages, but, in multi-bit stages can have a high cost in terms of area and power. While traditional encoder logic schemes in multi-bit stages are effective

for protecting against metastability issues, they are still vulnerable to SEs. Instead, robust logic schemes can be implemented, such as equation (19), that will either correct or mask many errors. In advanced designs the analog/mixed-signal sub-circuits (comparator, sample-and-hold amplifier, and multiplying digital-to-analog converter) are likely to use switched-capacitor topologies. Unfortunately switched-capacitor circuits contain floating nodes which produce larger errors from charge collection. Dual-path hardening has been developed and experimentally verified for hardening the vulnerable floating nodes in switched-capacitor designs with minimal tradeoffs. Advanced analog/mixed-signal designs are also fully-differential, therefore sensitive area can be significantly decreased through layout considerations. "Sister" devices across the differential data paths should be placed as close as possible in layout and even use common-centroid or interleaved geometries. This will promote common-mode charge, which is easily distinguishable from the data signal and is rejected by amplifiers.

The pipelined ADC signal path can be hardened by combining the analog/mixed-signal RHBD techniques developed in this work with the previous recommendations for digital logic and latches. The reference voltage and clock circuits are also vulnerable to single-events, but were not covered in this work. Steps must be taken to harden these control circuits as well.

#### REFERENCES

- [1] T. C. May and M. H. Woods, "Alpha Particle-Induced Soft Errors in Dynamic Memories," *IEEE Trans. Elec. Dev.*, vol. 26, no. 1, pp. 2-9, Jan. 1979.
- [2] E. Normand, "Single Event Effects in Avionics," *IEEE Trans. Nucl. Sci.*, vol. 43, no. 2, pp. 461-474, April 1996.
- [3] H. C. Koons, J. E. Mazur, R. S. Selesnick, J. B. Blake, J. F. Fennell, J. L. Roeder, and P. C. Anderson, "The impact of the space environment on space systems," *Aerospace Technical Report*, no. TR-99(1670)-1, July, 1999.
- [4] P. D. Bradley and E. Normand, "Single Event Upsets in Implantable Cardioverter Defibrillators," *IEEE Trans. Nucl. Sci.*, vol. 45, no. 6, pp. 2929-2939, Dec. 1998.
- [5] J. Wilkinson and S. Hareland, "A Cautionary Tale of Soft Errors Induced by SRAM Packaging Materials," *IEEE Trans. Dev. And Mat. Reliab.*, vol. 5, no. 3, pp. 428-433, Sept. 2005.
- [6] T. L. Turflinger, M. V. Davey, "Transient radiation test techniques for high-speed analog-to-digital converters," *IEEE Trans. Nuc. Sci.*, vol. 36, no. 6, pp. 2356-2361, Dec. 1989.
- [7] T. L. Turflinger and M. V. Davey, "Understanding Single Event Phenomena in Complex Analog and Digital Integrated Circuits," *IEEE Trans. Nucl. Sci.*, vol. 37, no. 6, pp. 1832-1838, Dec. 1990.
- [8] D. J. Wilson and D. A. Dorn, "Characterization of single event effects for the AD677, 16 bit A/D converter," *Proc. IEEE Radiation Effects Data Workshop*, pp. 113-117, 2007.
- [9] R. A. Reed, P. W. Marshall, M. A. Carts, G. L. Henegar, and R. B. Katz, "Proton-induced single event upset characterization of a 1 giga-sample per second analog-to-digital convert," *Radiation and Its Effects on Components and Systems*, 1999 Fifth European Conference on, pp. 188-192, 1999.
- [10] S. P. Buchner, T. J. Meehan, A. B. Campbell, K. A. Clark, D. McMorrow, "Characterization of single-event upsets in a flash analog-to-digital converter (AD9058)," *IEEE Trans. Nucl. Sci.*, vol. 47, no. 6, pp. 2358-2364, 2000.
- [11] S. Buchner, A. B. Campbell, A. Sternberg, L. W. Massengill, D. McMorrow, C. Dyer, "Validity of using a fixed analog input for evaluating the SEU sensitivity of a flash analog-to-digital converter," *IEEE Trans. Nucl. Sci.*, vol. 52, no. 1, pp. 462-467, Feb. 2005.

- [12] W. F. Heidergott, R. Ladbury, P. W. Marshall, S. Buchner, A. B. Campbell, R. A. Reed, J. Hockmuth, N. Kha, C. Sieleck, A. Assad, "Complex SEU signatures in high-speed analog-to-digital conversion," *IEEE Trans. Nucl. Sci.*, vol. 48, no. 6, pp. 1828-1832, Dec. 2001.
- [13] K. Kruckmeyer, R. L. Rennie, and V. Ramachandran, "Use of Code Error and Beat Frequency Test Method to Identify Single Event Upset Sensitive Circuits in a 1 GHz Analog to Digital Converter," *IEEE Trans. Nucl. Sci.*, vol. 55, no. 4, pp. 2013-2018, Aug. 2008.
- [14] K. G. Merkel and A. L. Wilson, "A survey of high performance analog-to-digital converters for defense space applications," *Aerospace Conference, Proceedings*, 2003 IEEE, vol. 5, pp. 2415-2427, Mar. 2003.
- Y. Boulghassoul, S. Buchner, D. Morrow, V. Pouget, L. W. Massengill, P. Fouillat, W. T. Holman, C. Poivey, J. W. Howard, M. Savage, M. C. Maher, "Investigation of millisecond-long analog single-event transisents in the LM6144 op amp," *IEEE Trans. Nucl. Sci.*, vol. 51, no. 6, pp. 3529, 3536, Dec. 2004.
- [16] Y. Boulghassoul, L. W. Massengill, A. L. Sternberg, B. L. Bhuva, "Effects of technology scaling on the SET sensitivity of RF CMOS Voltage-controlled oscillators," *IEEE Trans. Nucl. Sci.*, vol. 52, no. 6, pp. 2426-2432, Dec. 2005.
- T. D. Loveless, L. W. Massengill, B. L. Bhuva, W. T. Holman, A. F. Witulski, and Y. Boulghassoul, "A hardened-by-design technique for RF digital phase-locked-loops," *IEEE Trans. Nucl. Sci.*, vol. 53, no. 6, pp. 3432–3438, Dec. 2006.
- [18] J. T. Wallmark and S. M. Marcus, "Minimum size and maximum packing density of nonredundant semiconductor devices," Proc. IRE, vol. 50, pp. 286–298, 1962.
- [19] C. W. Gwyn, D. L. Scharfetter, J. L. Wirth, "The Analysis of Radiation Effects in Semiconductor Devices," *IEEE Trans. Nucl. Sci.*, vol. 14, no. 6, pp. 153-169, Dec. 1967.
- [20] V. A. J. van Lint, J. H. Alexander, D. K. Nichols, P. R. Ward, "Computerized Model for Response of Transistors to a Pulse of Ionizing Radiation," *IEEE Trans. Nucl. Sci.*, vol. 14, no. 6, pp. 170-178, Dec. 1967.
- [21] D. Binder, E. C. Smith, A. B. Holman, "Satellite Anomalies from Galactic Cosmic Rays," *IEEE Trans. Nucl. Sci.*, vol. 22, no. 6, pp. 2675-2680, Dec. 1975.

- [22] G. E. Moore, "Progress in Digital Integrated Electronics," *IEDM Tech. Dig.*, vol. 21, pp. 11-13, 1975.
- [23] T. R. Oldham, "How Device Scaling Affects Single Event Sensitivity," in *IEEE NSREC Short Course*, 2003, pp. IV-1–IV-66.
- [24] J. Mazur, "The Radiation Environment Outside and Inside a Spacecraft," in *IEEE NSREC Short Course*, 2002, pp. II-1–II-69.
- [25] Nikkei Science, Inc. of Japan, image by K. Endo.
- [26] J. A. Van Allen, C. E. McIlwain, and G. H. Ludwig, "Radiation observations with satellite 1958 EX," *J. Geophys. Res.*, vol. 64, no. 3, pp. 271–286, 1959.
- [27] W. J. Stapor, P. T. McDonald, A. R, Knudson, A. B. Campbell, and B. G. Glagola, "Charge Collection in Silicon for Ions of Different Energy but Same Linear Energy Transfer (LET)," *IEEE Trans. on Nucl. Sci.*, vol. 35, no. 6, pp. 1585–1590, Dec. 1988.
- [28] M. Xapsos, "Modeling the Space Radiation Environment," in *IEEE NSREC Short Course*, 2006, pp. II-1–II-62.
- [29] E. G. Stassinopoulos, J. P. Raymond, "The Space Radiation Environment for Electronics," *IEEE Proceedings*, vol. 76, no. 11, pp. 1423-1442, Nov. 1988.
- [30] J. Barth, "Modeling Space Radiation Environments," in *IEEE NSREC Short Course*, 1997, pp. I-1-I-83.
- [31] National Aeronautics and Space Administration's Goddard Space Flight Center, Solar & Heliospheric Observatory (SOHO) Project. [Online]. Available: <a href="http://sohowww.nascom.nasa.gov/gallery/images/cycle001.html">http://sohowww.nascom.nasa.gov/gallery/images/cycle001.html</a>
- [32] R. A. Mewaldt, M. D. Looper, C. M. S. Cohen, G. M. Mason, D. K. Haggerty, M. I. Desai, A. W. Labrador, R. A. Leske, J. E. Mazur, "Solar-Particle Energy Spectra during the Large Events of October-November 2003 and January 2005," 29<sup>th</sup> International Cosmic Ray Conference, June 2005.
- [33] R. A. Medwadlt, "Elemental Composition and Energy Spectra of Galactic Cosmic Rays," *Proc. from Conference on Interplanetary Particle Environment*, JPL Publication 88-28, pp. 121-132, JPL, Pasadena, CA, April 1988.
- [34] T. C. May and M. H. Woods, "A New Physical Mechanism for Soft Error in Dynamic Memories," *Proc.* 16<sup>th</sup> Int'l Reliability Physics Symp. (IRPS), IEEE EDS, pp. 33-40, 1978.

- [35] A. Maheshwari and A. Lesea, "Flip-Chip Package Substrate Solder Issue," Xilinx White Paper: Virtex-II and Virtex-II Pro Families, WP208(v1.1), pp. 1-4, Jan. 2004.
- [36] R. L. Fleischer, "Cosmic Ray Interaction with Boron: A Possible Source of Soft Errors," *IEEE Trans. Nucl. Sci.*, vol. 30, no. 5, pp. 4013-4015, Oct. 1983.
- [37] T. R. Oldham, S. Murril, and C. T. Self, "Single Event Upset of VLSI Memory Circuits Induced by Thermal Neutrons," *Hardened Electronics and Radiation Technology Conference*, 1986.
- [38] S. M. Sze, *Physics of Semiconductor Devices*, Wiley, New York, 1981.
- [39] L. W. Massengill, "SEU modeling and prediction techniques," in *IEEE NSREC Short Course*, 1993, pp. III-1–III-93.
- [40] S. Buchner, "Single-Event Transients in Linear Integrated Circuits," in *IEEE NSREC Short Course*, 2005, pp. IV-1-IV-77.
- [41] R. D. Evans, *The Atomic Nucleus*, McGraw-Hill Book Company, Inc, New York, 1955.
- [42] C. M. Hsieh, P. C. Murley, and R. R. O'Brien, "A field-funneling effect on the collection of alpha-particle-generated carriers in silicon devices," *IEEE Electron Device Lett.*, vol. 2, pp. 103-105, Dec. 1981.
- [43] R. Baumann, "Single-event effects in advanced CMOS," in *IEEE NSREC Short Course*, 2005, pp. II-1–II-59.
- [44] A. K. Sutton, J. D. Cressler, M. A. Carts, P. W. Marshall, J. A. Pellish, R. A. Reed, M. L. Alles, N. Guogu, "Proton-induced SEU in SiGe digital logic at cryogenic temperatures," *Int'l Semiconductor Device Research Symp.*, pp. 1-2, Dec. 2007.
- [45] K. M. Warren, R. A. Weller, M. H. Mendenhall, R. A. Reed, D. R. Ball, C. L. Howe, B. D. Olson, M. L. Alles, L. W. Massengill, R. D. Schrimpf, N. F. Haddad, S. E. Doyle, D. McMorrow, J. S. Melinger, W. T. Lotshaw, "The Contributions of Nuclear Reactions to Single Event Upset Cross-Section Measurements in a High-Density SEU Hardened SRAM Topology," *IEEE Trans. Nucl. Sci.*, vol. 52, no. 6, pp. 2125-2136, Dec. 2005.
- [46] B. D. Olson, D. R. Ball, K. M. Warren, L. W. Massengill, N. F. Haddad, S. E. Doyle, D. McMorrow, "Simultaneous Single Event Charge Sharing and Parasitic Bipolar Conduction in Highly-Scaled SRAM Design," *IEEE Trans. Nucl. Sci...*, vol. 52, no. 6, pp. 2132-2136, Dec. 2005.

- [47] T. Weatherford, "From carriers to contacts, a review of SEE charge collection processes in devices," in *IEEE NSREC Short Course*, 2002, pp. IV-1–IV-53.
- [48] G. C. Messenger, "Collection of Charge on Junction Nodes from Ion Tracks," *IEEE Trans. Nucl. Sci.*, vol. 29, no. 6, pp. 2024-2031, Dec. 1982.
- [49] R. S. Wagner, N. Bordes, J. M. Bradley, C. J. Maggiore, A. R. Knudson, A. B. Campbell, "Alpha-, boron-, silicon-, and iron-ion induced current transients in low-capacitance silicon and GaAs diodes," *IEEE Trans. Nucl. Sci.*, vol. 35, no. 6, pp. 1578-1584, Dec. 1988.
- [50] S. DasGupta, "Trends in single event pulse widths and pulse shapes in deep submicron CMOS," *M.S. thesis*, Vanderbilt Univ., Nashville, TN, 2007.
- [51] P. E. Allen and D. R. Holberg, *CMOS Analog Circuit Design*, 2<sup>nd</sup> Edition, Oxford University Press, New York, 2004.
- [52] B. Baker, "What does the ADC SNR mean?," *Electronics Design, Strategy, News*, May 27, 2004. [Online]. Available: <a href="http://www.edn.com/article/475552-What does the ADC SNR mean .php">http://www.edn.com/article/475552-What does the ADC SNR mean .php</a>
- [53] S. H. Lewis, "Video-Rate Analog-to-Digital Conversion Using Pipelined Architectures," *Ph.D. Dissertation*, Univ. of Cal. Berkeley, Berkeley, CA, 1987.
- [54] D. W. Cline, "Noise, Speed, and Power Trade-offs in Pipelined Analog to Digital Converters," *Ph.D. Dissertation*, Univ. of Cal. Berkeley, Berkeley, CA, 1995.
- [55] T. L. Turflinger, M. V. Davey, B. M. Mappes, "Single event effects in analog-to-digital converters: Device performance and system impact," *IEEE Trans. Nuc. Sci.*, vol. 41, no. 6, pp. 2187-2194, Dec. 1994.
- [56] M. V. O'Bryan, K. A. LaBel, R. A. Reed, J. W. Howard, J. L. Barth, C. M. Seidleck, P. W. Marshall, C. J. Marshall, H. S. Kim, D. K. Hawkins, M. A. Carts, K. E. Forslund, "Recent Radiation Damage and Single Event Effect Results for Microelectronics," *Radiation Effects Data Workshop*, 1999.
- [57] C. Poivey, J. Forney, C. Palor, "Heavy ion single event effects test of 8 bits ADC AD7821 from Analog Devices 12 bits ADC AD9223 from Analog Devices 12 bits ADC LTC1272 from Linear Technology," http://radhome.gsfc.nasa.gov/radhome/papers/T080101\_ADC.pdf, August 2001.

- [58] M. V. O'Bryan, K. A. LaBel, R. L. Ladbury, C. Poivey, J. W. Howard Jr., R. A. Reed, S. D. Kniffin, S. P. Buchner, J. P. Bings, J. L. Titus, S. D. Clark, T. L. Turflinger, C. M. Seidleck, C. J. Marshall, P. W. Marshall, H. S. Kim, D. K. Hawkins, M. A. Carts, J. D. Forney, M. R. Jones, A. B. Sanders, T. L. Irwin, S. R. Cox, Z. A. Kahric, C. D. Palor, J. A. Sciarini, "Current Single Event Effects and Radiation Damage Results for Candidate Spacecraft Electronics," *Radiation Effects Data Workshop*, 2002.
- [59] M. D. Berg, H. Kim, A. Phan, "SEE Tests for Texas Instruments ADS5424 ADC," http://radhome.gsfc.nasa.gov/radhome/papers/T111207\_ADS5424.pdf, Nov. 2007.
- [60] M. V. O'Bryan, K. A. LaBel, S. P. Buchner, R. L. Ladbury, C. F. Poivey, T. R. Oldham, M. J. Campola, M. A. Carts, M. D. Berg, A. B. Sanders, S. R. Mackey, "Compendium of Recent Single Event Effects Results for Candidate Spacecraft Electronics for NASA," *Radiation Effects Data Workshop*, 2008.
- [61] J. S. Kauppila, "The design of a custom single-event hardened analog-to-digital converter," *M.S. thesis*, Vanderbilt Univ., Nashville, TN, 2003.
- [62] J. S. Kauppila, L. W. Massengill, W. T. Holman, A. V. Kauppila, S. Sanathanamurthy, "Single even simulation methodology for analog/mixed signal design hardening," *IEEE Trans. Nucl. Sci.*, vol. 51, no. 6, pp. 3603-3608, Dec. 2004.
- [63] A. L. Sternberg, L. W. Massengill, M. Hale, B. Blalock, "Single-Event Sensitivity and Hardening of a Pipelined Analog-to-Digital Converter," *IEEE Trans. Nucl. Sci.*, vol. 53, no. 6, pp. 3532-3538, 2006.
- [64] A. L. Sternberg, "Single-event response and hardening techniques for high-performance pipelined analog-to-digital converters," *Ph.D. Dissertation*, Vanderbilt Univ., Nashville, TN, 2006.
- [65] M. Singh and I. Koren, "Reliability enhancement of analog-to-digital-converters," *Proc. of IEEE Symp. on Defect and Fault Tolerance in VLSI*, pp. 347-353, 2001.
- [66] M. Singh and I. Koren, "Fault-sensitivity analysis and reliability enhancement of analog-to-digital converters," *IEEE Trans. on VLSI*, vol. 11, no. 5, pp. 839-852, 2003.
- [67] V. Pouget, D. Lewis, and P. Fouillat, "Time-resolved scanning of integrated circuits with a pulsed laser; application to transient fault injection in an adc," *Proc. of Instrumentation and Measurement Conference*, 2003.

- [68] E. Mikkola, B. Vermeire, H. J. Barnaby, H. G. Parks, and K. Borhani, "SET tolerant CMOS comparator," *IEEE Trans. Nucl. Sci.*, vol. 51, no. 6, pp. 3609–3614, Dec. 2004.
- [69] P. Bellandi, F. Brandani, A. S. Brogna, S. Chicca, L. Colombini, C. Garbossa, S. Puccini, R. Saletti, M. Stagi, "A 12-bit pipelined self-calibrated radiation hardened adc for aerospace applications," *IEEE Workshop on Radiation Effects on Components and Systems*, vol. 1, pp. 141-144, 2002.
- [70] B. D. Olson, W. T. Holman, L. W. Massengill, and B. L. Bhuva, "Evaluation of Radiation-Hardened Design Techniques Using Frequency Domain Analysis," *IEEE Trans. Nucl. Sci.*, vol. 55, pp. 2957-2961, 2008.
- [71] T. L. Turflinger, "Single-Event Effects in Analog and Mixed-Signal Integrated Circuits," *IEEE Trans. Nucl. Sci.*, vol. 43, no. 2, pp. 594-602, 1996.
- [72] Y. Boulghassoul, L. W. Massengill, T. L. Turflinger, and W. T. Holman, "Frequency Domain Analysis of Analog Single-Event Transients in Linear Circuits," *IEEE Trans. Nucl. Sci.*, vol. 49, no. 6, pp. 3142-3147, Dec. 2002.
- [73] A. V. Kauppila, L. W. Massengill, W. T. Holman, G. L. Vaughn, and J. S. Kauppila, "Frequency-Domain Analysis of Analog Single-Event Transients (ASETs) Based on Energy Spectral Density," *IEEE Trans. Nucl. Sci.*, vol. 51, no. 6, pp. 3537-3545, Dec. 2004.
- [74] W. Peterson, *Error-Correcting Codes*, 2nd ed. Cambridge, MA: MIT Press, 1980, p. 560.
- [75] S. H. Lewis, "Optimizing the Stage Resolution in Pipelined, Multistage, Analog-to-Digital Converters for Video-Rate Applications," *IEEE Trans. Circuits Syst. II*, vol. 39, pp. 516-523, Aug. 1992.
- [76] J. Goes, J. C. Vital, J. E. Franca, "Systematic Design for Optimization of High-Speed Self-Calibrated Pipelined A/D Converters," *IEEE Trans. Circuits Syst. II*, vol. 45, pp. 1513-1526, Dec. 1998.
- [77] P. T. F. Kwok, H. C. Luong, "Power Optimization for Pipeline Analog-to-Digital Converters," *IEEE Trans. Circuits Syst. II*, vol. 46, pp. 549-553, May 1999.
- [78] R. Lotfi, M. Taherzadeh-Sani, M. Y. Azizi, O. Shoaei, "A Low-Power Design Methodology for High-Resolution Pipelined Analog-to-Digtial Converters," *IEEE Intl. Symp. Low Power Elect. Design*, pp. 334- 339, Aug. 2003.

- [79] P. J. Quinn, A. H. M. van Roermund, "Design and Optimization of Multi-bit Front-end Stage and Scaled Back-end Stages of Pipelined ADCs," *IEEE Intl. Symp. Circuits Syst.*, vol. 3, pp. 1964-1967, May 2005.
- [80] B. D. Olson, W. T. Holman, L. W. Massengill, B. L. Bhuva, P. R. Fleming, "Single-Event Effect Mitigation in Switched-Capacitor Comparator Designs," *IEEE Trans. Nucl. Sci.*, vol. 55, no. 6, pp. 3440-3446, Dec. 2008.
- [81] P. R. Fleming, B. D. Olson, W. T. Holman, B. L. Bhuva, and L. W. Massengill, "Design Technique for Mitigation of Soft Errors in Differential Switched-Capacitor Circuits," *IEEE Trans. Cir. and Sys. II: Express Briefs*, vol. 55, pp. 838-842, 2008.
- [82] J. Peterson, "A monolithic video AD converter," *IEEE J. Solid-State Circuits*, vol. SC-14, no. 6, pp. 932-937, Dec. 1979.
- [83] C. W. Mangelsdorf, "A 400-MHz Input Flash Converter with Error Correction," *IEEE J. Solid-Stage Circuits*, vol. 25, no. 1, pp. 184-191, Feb. 1990.
- [84] T. Monnier, F. M. Roche, F. Corbiere, "Restructuring of the flash A/D converter to improve SEU rad tolerance," *Radiation and Its Effects on Components and Systems*, 1999 Fifth European Conference on, pp. 353-357, 1999.
- [85] R. Koga, S. D. Pinkerton, S. C. Moss, D. C. Mayer, S. LaLumondiere, S. J. Hansel, K. B. Crawford, and W. R. Crain, "Observation of single event upsets in analog microcircuits," *IEEE Trans. Nucl. Sci.*, vol. 40, no. 6, pp. 1838–1844, Dec. 1993.
- [86] D. K. Nichols, J. R. Coss, T. F. Miyahira, and H. R. Schwartz, "Heavy ion and proton induced single event transients in comparators," *IEEE Trans. Nucl. Sci.*, vol. 42, no. 6, pp. 2960–2967, Dec. 1996.
- [87] R. Koga, S. H. Crain, K. B. Crawford, S. C. Moss, S. D. LaLumondiere, and J. W. Howard, Jr., "Single event transient (SET) sensitivity of radiation hardened and COTS voltage comparators," in *Proc. IEEE Radiation Effects Data Workshop*, 2000, pp. 53–60.
- [88] A. H. Johnston, G. M. Swift, T. F. Miyahira, and L. D. Edmonds, "A model for single-event transients in comparators," *IEEE Trans. Nucl. Sci.*, vol. 47, no. 6, pp. 2624–2633, Dec. 2000.

- [89] C. Poivey, J. W. Howard, Jr., S. Buchner, K. A. LaBel, J. D. Forney, H. S. Kim, and A. Assad, "Development of a test methodology for single-event transients (SETs) in linear devices," *IEEE Trans. Nucl. Sci.*, vol. 48, no. 6, pp. 2180–2186, Dec. 2001.
- [90] A. L. Sternberg, L. W. Massengill, R. D. Schrimpf, and P. Calvel, "Application determinance of single-event transient characteristics in the LM111 comparator," *IEEE Trans. Nucl. Sci.*, vol. 48, no. 6, pp. 1855–1858, Dec. 2001.
- [91] S. Buchner, D. McMorrow, A. L. Sternberg, L. W. Massengill, R. L. Pease, and M. C. Maher, "Single-event transient (SET) characterization of an LM119 voltage comparator: An approach to SET model validation using a pulsed laser," *IEEE Trans. Nucl. Sci.*, vol. 49, no. 3, pp. 1502–1508, April 2002.
- [92] M. W. Savage, T. Turflinger, J. L. Titus, H. F. Barsun, A. L. Sternberg, Y. Boulghassoul, and L. W. Massengill, "Variations in SET pulse shapes in the LM124A and LM111," in *Proc. IEEE Radiation Effects Data Workshop*, 2002, pp. 75–81.
- [93] A. H. Johnston, T. F. Miyahira, L. D. Edmonds, and F. Irom, "Single-Event transients in high-speed comparators," *IEEE Trans. Nucl. Sci.*, vol. 49, no. 6, pp. 3082–3089, Dec. 2002.
- [94] S. D. LaLumondiere, R. Koga, P. Yu, M. C. Maher, and S. C. Moss, "Laser-induced and heavy ion-induced single-event transient (SET) sensitivity measurements on 139-type comparators," *IEEE Trans. Nucl. Sci.*, vol. 49, no. 6, pp. 3121–3128, Dec. 2002.
- [95] R. L. Pease, A. L. Sternberg, Y. Boulghassoul, L. W. Massengill, S. Buchner, D. McMorrow, D. S.Walsh, G. L. Hash, S. D. LaLumondiere, and S. C. Moss, "Comparison of SETs in bipolar linear circuits generated with an ion microbeam, laser light, and circuit simulation," *IEEE Trans. Nucl. Sci.*, vol. 49, no. 6, pp. 3163–3170, Dec. 2002.
- [96] S. Buchner, J. W. Howard, Jr., C. Poivey, D. McMorrow, and R. L. Pease, "Pulsed-laser testing methodology for single event transients in linear devices," *IEEE Trans. Nucl. Sci.*, vol. 51, no. 6, pp. 3716–3722, Dec. 2004.
- [97] M. F. Bernard, L. Dusseau, S. Buchner, D. McMorrow, R. Ecoffet, J. Boch, J.-R. Vaille, R. D. Schrimpf, and K. A. LaBel, "Impact of total ionizing dose on the analog single event transient sensitivity of a linear bipolar integrated circuit," *IEEE Trans. Nucl. Sci.*, vol. 54, no. 6, pp. 2534–2540, Dec. 2007.

- [98] N. W. van Vonno and B. R. Doyle, "Design considerations and verification testing of an SEE-hardened quad comparator," *IEEE Trans. Nucl. Sci.*, no. 6, vol. 48, pp. 1859–1864, Dec. 2001.
- [99] P. E. Allen and E. Sanchez-Sinencio, *Switched-Capacitor Circuits*, Van Nostrand Reinhold, New York, 1984.
- [100] B. Zhao and A. Leuciuc, "Single event transients characterization in SOI CMOS comparators," *IEEE Trans. Nucl. Sci.*, vol. 51, no. 6, pp. 3360–3364, Dec. 2004.
- [101] P. R. Fleming, "An RHBD technique to improve the single-event vulnerability of switched-capacitor differential circuits," M.S. thesis, Vanderbilt Univ., Nashville, TN, 2007.
- [102] S. DasGupta, A. F. Witulski, B. L. Bhuva, M. L. Alles, R. A. Reed, O. A. Amusan, J. R. Ahlbin, R. D. Schrimpf, and L. W. Massengill, "Effect of well and substrate potential modulation on single event pulse shape in deep submicron CMOS," *IEEE Trans. Nucl. Sci.*, vol. 54, no. 6, pp. 2407–2412, Dec. 2007.
- [103] Y.-M. Lin, B. Kim, and P. R. Gray, "A 13-b 2.5-MHz self-calibrated pipelined A/D converter in 3-μm CMOS," *IEEE J. Solid-State Circuits*, vol. 26, no. 4, pp. 628–636, April 1991.
- [104] U.-K. Moon and B.-S. Song, "Background digital calibration techniques for pipelined ADCs," *IEEE Trans. Circuits Syst. II, Analog. Digit. Signal Process.*, vol. 44, no. 2, pp. 102–109, Feb. 1997.
- [105] S.-U. Kwak, B.-S. Song, and K. Bacrania, "A 15-b, 5-Msample/s low-spurious CMOS ADC," *IEEE J. Solid-State Circuits*, vol. 32, no. 12, pp. 1866–1875, Dec. 1997.
- [106] T. F. Boggess, K. M. Bohnert, K. Mansour, S. C. Moss, I. W. Boyd, and A. L. Smirl, "Simultaneous measurement of the two-photon coefficient and free-carrier cross section above the bandgap of crystalline silicon," *IEEE J. Quantum Electron.*, vol. 22, no. 2, pp. 360–368, Feb. 1986.
- [107] D. McMorrow, W. T. Lotshaw, J. S. Melinger, S. Buchner and R. L. Pease "Subbandgap laser-induced single event effects: Carrier generation via two-photon absorption," *IEEE Trans. Nucl. Sci.*, vol. 49, pp. 3002, Dec. 2002.
- [108] D. McMorrow , W. T. Lotshaw , J. S. Melinger , S. Buchner , Y. Boulghassoul , L. W. Massengill and R. Pease "Three-dimensional mapping of single-event effects using two photon absorption," *IEEE Trans. Nucl. Sci.*, vol. 50, pp. 2199, Dec. 2003.

- [109] D. McMorrow, S. Buchner, W.T. Lotshaw, J.S. Melinger, M. Maher, M.W. Savage, "Demonstration of single-event effects induced by through-wafer two-photon absorption," *IEEE Trans. Nucl. Sci.*, vol. 51, pp. 3553, Dec. 2004.
- [110] D. McMorrow, W.T. Lotshaw, J.S. Melinger, S. Buchner, M. Maher, M. Savage, J.D. Davis, R.K. Lawrence, J.H. Bowman, R.D. Brown, D. Carlton, J. Pena and J. Vasquez, N.F. Haddad, K.M. Warren, and L.M. Massengill, "Single-Event Upset in Flip-Chip SRAM Induced by Through-Wafer Two-Photon-Absorption," *IEEE Trans. Nucl. Sci.*, vol. 52, pp. 2421, Dec. 2005.
- [111] T.D. Loveless, L.W. Massengill, B.L. Bhuva, W.T. Holman, R.A. Reed, D. McMorrow, J.S. Melinger, P. Jenkins, "A Single-Event-Hardened Phase-Locked Loop Fabricated in 130 nm CMOS," *IEEE Trans. Nucl. Sci.*, vol. 54, pp.2012, Dec. 2007.
- [112] J. D. Black, A. L. Sternberg, M. L. Alles, A. F. Witulski, B. L. Bhuva, L. W. Massengill, J. M. Benedetto, M. P. Baze, J. L. Wert, and M. G. Hubert, "Multiple-bit upset in 130 nm CMOS technology," *IEEE Trans. Nucl. Sci.*, vol. 52, no. 6, pp. 2536–2541, Dec. 2005.
- [113] O. A. Amusan, A. F. Witulski, L. W. Massengill, B. L. Bhuva, P. R. Fleming, M. L. Alles, A. L. Sternberg, J. D. Black, and R. D. Schrimpf, "Charge collection and charge sharing in a 130 nm CMOS technology," *IEEE Trans. Nucl. Sci.*, vol. 53, no. 6, pp. 3253–3258, Dec. 2006.
- [114] A. T. Kelly, P. R. Felming, W. T. Holman, A. F. Witulski, B. L. Bhuva, and L. W. Massengill, "Differential Analog Layout for Improved ASET Tolerance," *IEEE Trans. Nucl. Sci.*, vol. 54, pp. 2053-2059, Dec. 2007.
- [115] A. Hastings. *The Art of Analog Layout*, Upper Saddle River, NJ: Pearson Prentice Hall, 2006, pp. 277-281.
- [116] O. A. Amusan, P. R. Fleming, B. L. Bhuva, L. W. Massengill, A. F. Witulski, M. C. Casey, D. McMorrow, S. A. Nation, F. Barsun, J. S. Melinger, M. J. Gadlage, and T. D. Loveless, "Laser verification of on-chip charge collection measurement circuit," *IEEE Trans. Nucl. Sci.*, vol. 55, pp. 3309–3313, Dec. 2008.